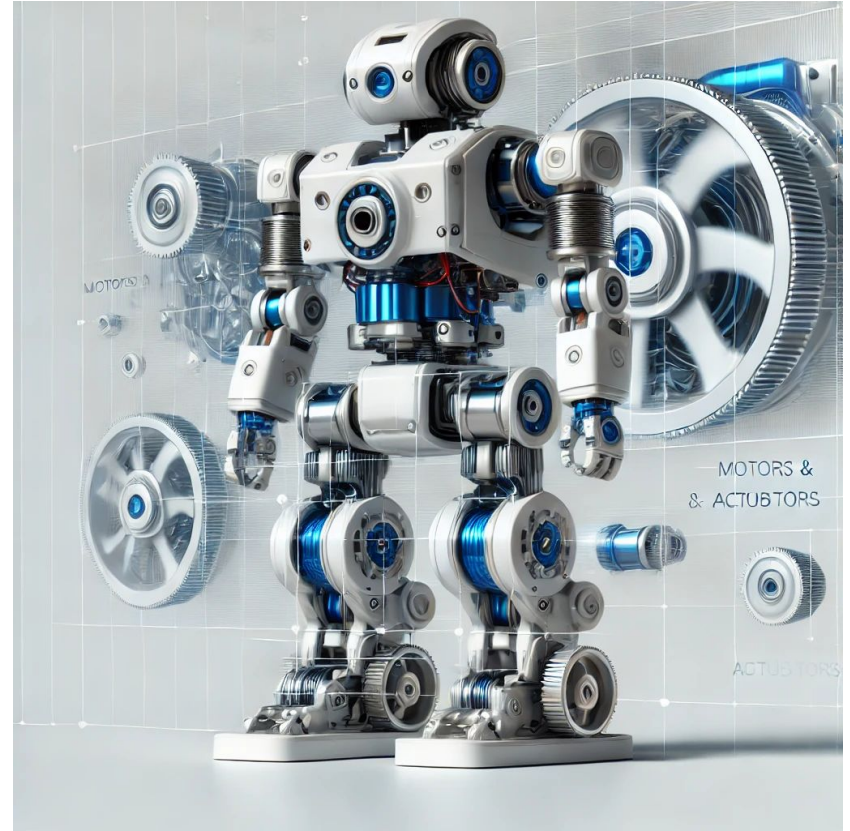


# Motors and Motion Sensors

07/10/2025

Dr. Jizhong Xiao



# Outline

## 1. Robot Actuators

- Stepper Motor
- DC Motor
- Servo Motor

## 2. Motor Feedback Sensors

- Rotary Encoder
- Hall Effect Sensor

## 3. Motor Speed Control



1

# **Robot Actuators**

# Robot Actuators

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Stepper motors

DC motors

Servo motors

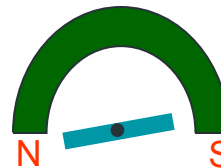
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Physics review:

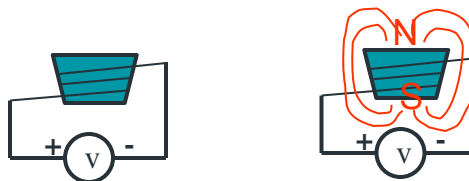
Nature is lazy.

Things seek lowest energy states.

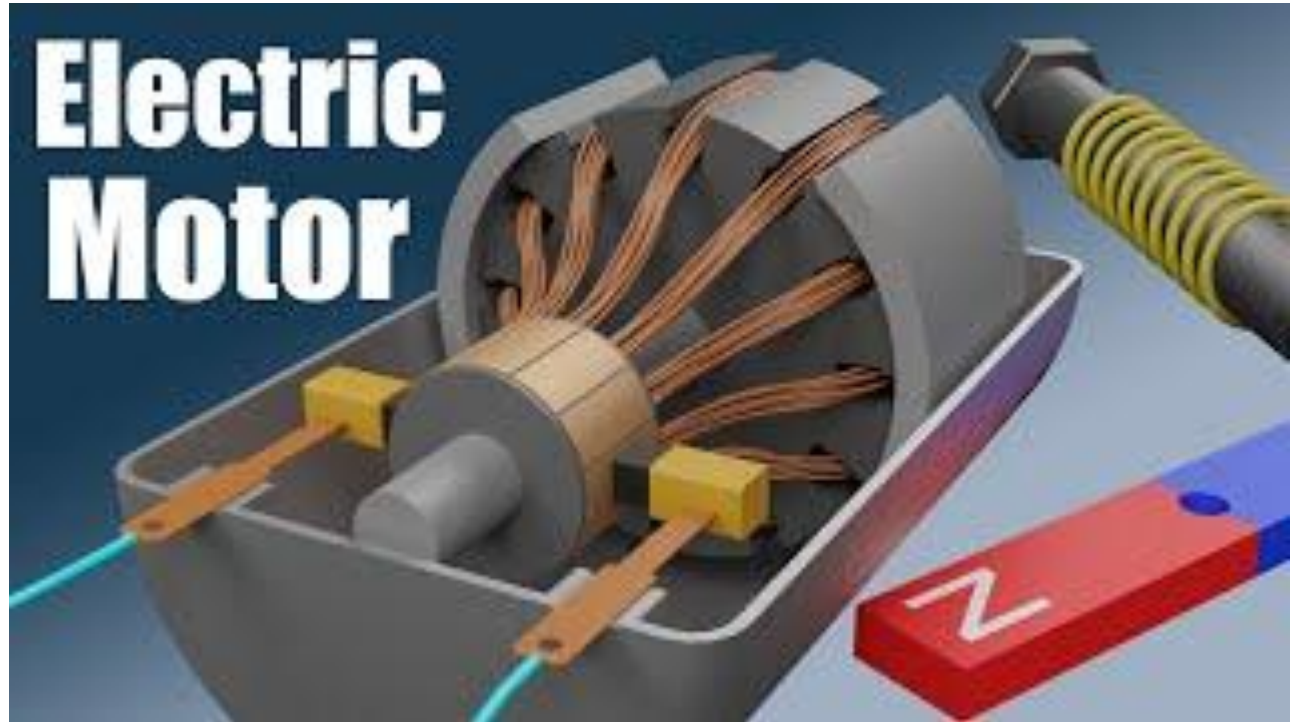
- iron core vs. magnet
- magnetic fields tend to line up



Electromagnetic fields and magnetic fields are the same thing.



## How Electric Motors Work?

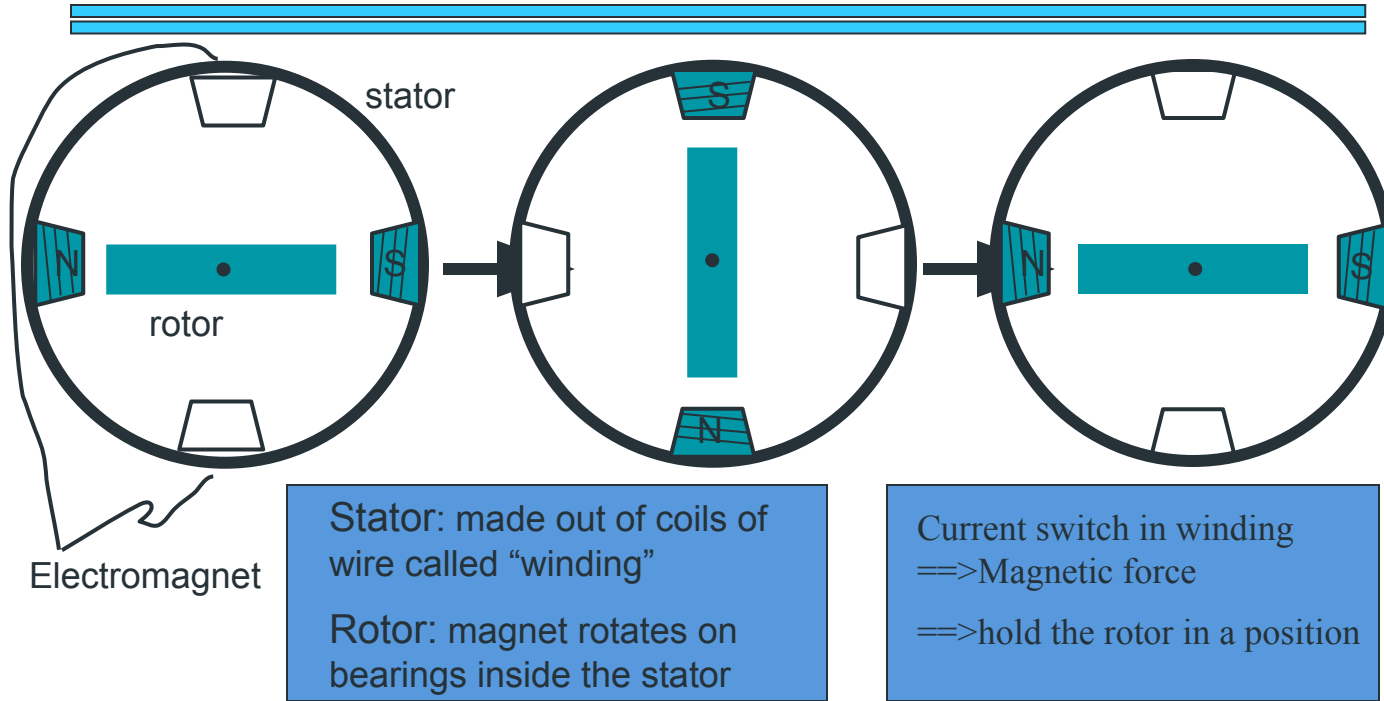




1.1

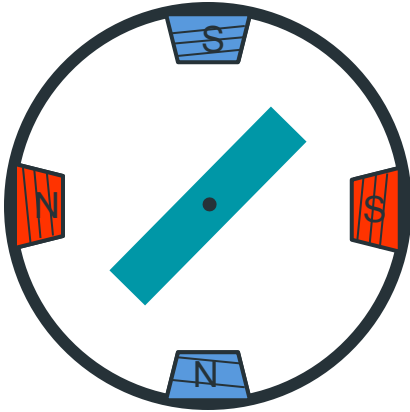
# Stepper Motors

# Stepper Motor Basics

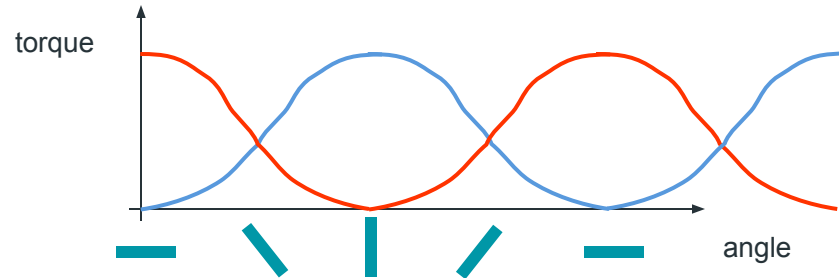


- Direct control of rotor position (no sensing needed) → printers  
computer disk drives
- Low resolution

# Increased Resolution



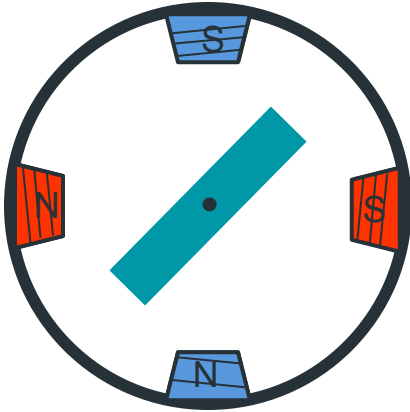
Half stepping





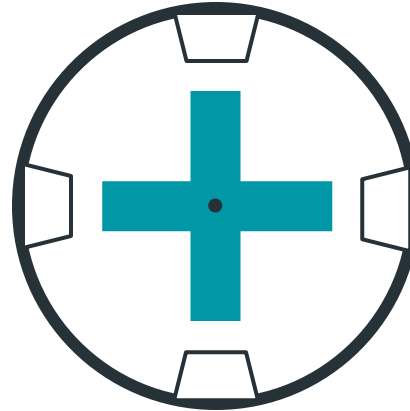
# Increased Resolution

---



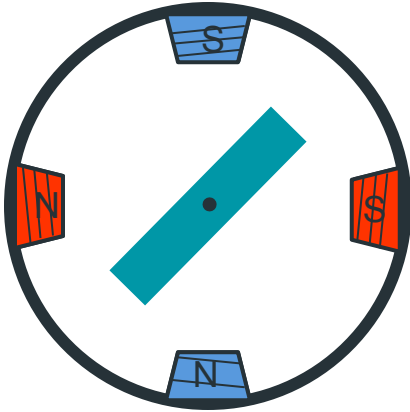
Half stepping

More teeth on rotor or stator



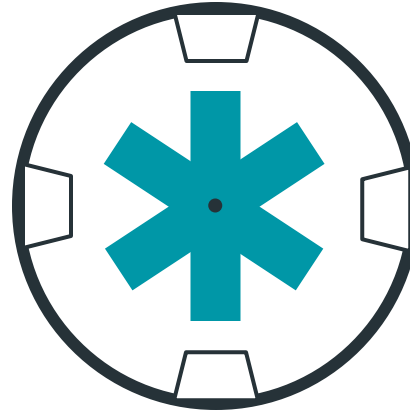
# Increased Resolution

---

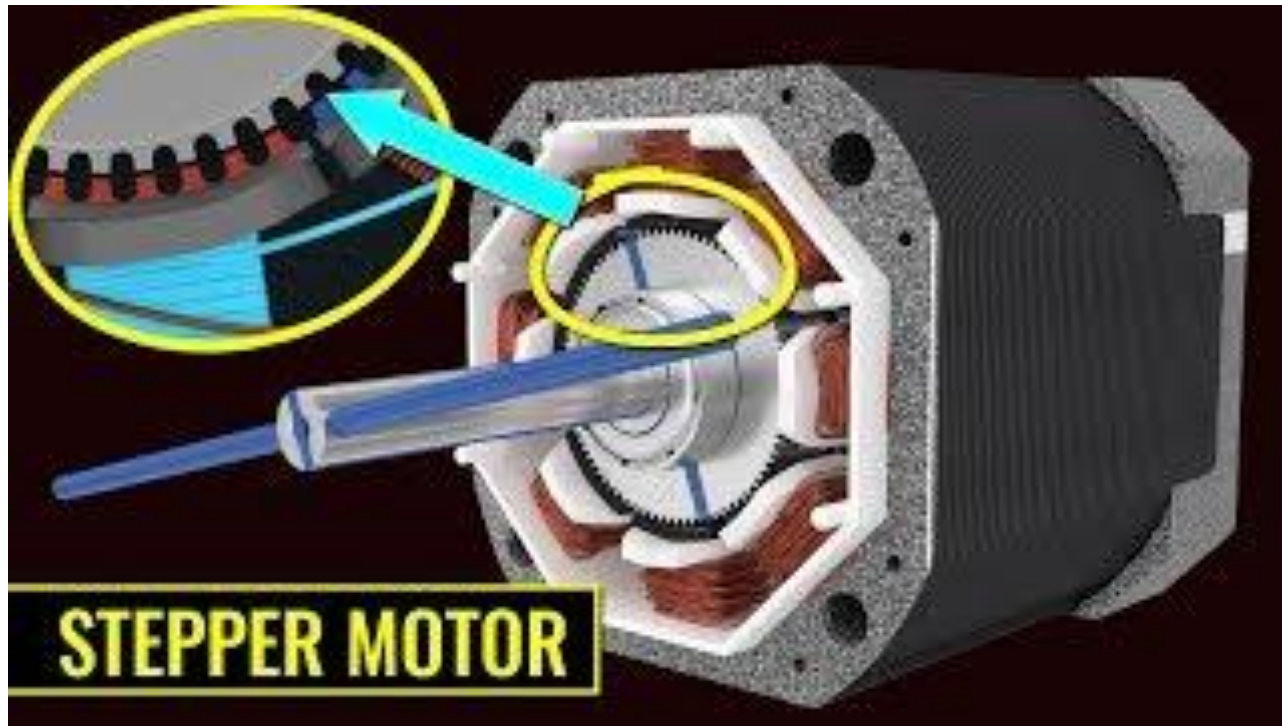


Half stepping

More teeth on rotor or stator



## How Does a Stepper Motor Works?

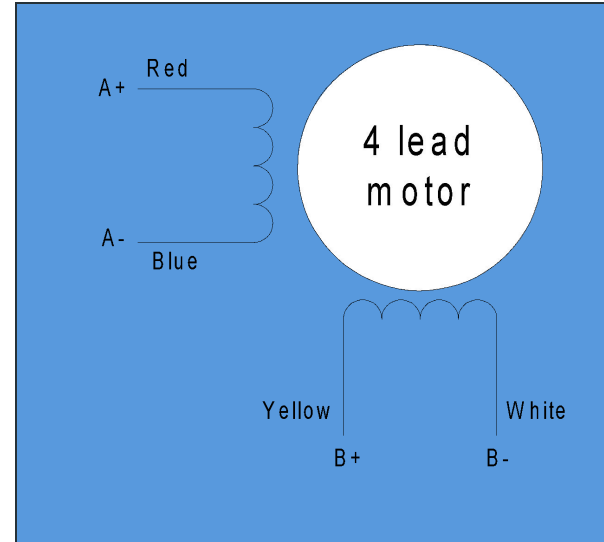


# How to Control?

## 4 Lead Wire Configuration

Step Table				
Step	Red	Blue	Yellow	White
0	+	-	+	-
1	-	+	+	-
2	-	+	-	+
3	+	-	-	+
4	+	-	+	-

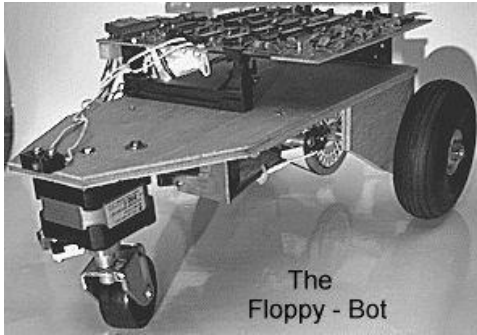
Clockwise Facing Mounting End



Each step, like the second hand of a clock => tick, tick  
Increase the frequency of the steps => continuous motion

# Motoring along...

---



- direct control of position
- precise positioning (The amount of rotational movement per step depends on the construction of the motor)

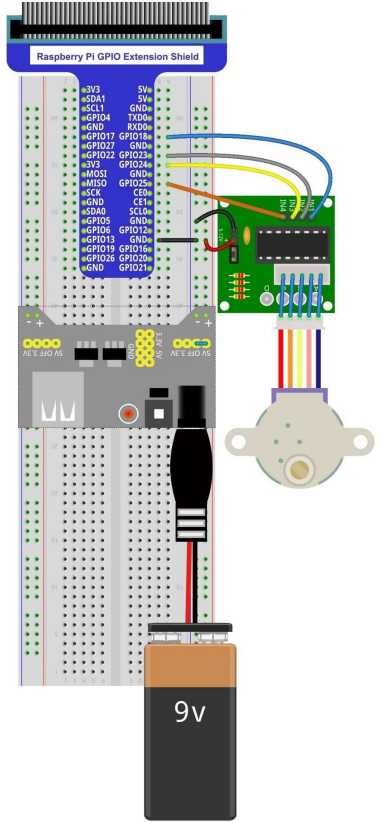
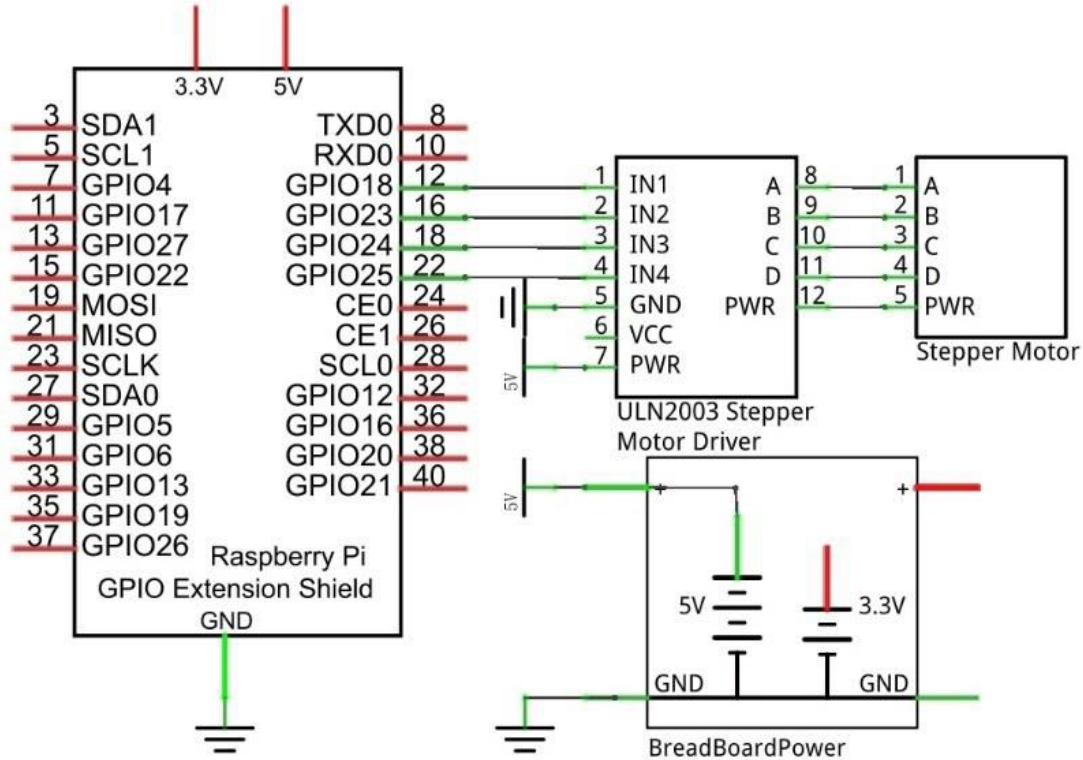


- Easy to Control
- under-damping leads to oscillation at low speeds
- torque is lower at high speeds than the primary alternative...

## Stepper Motors Explained



## Project 16: Stepper Motor Experiment





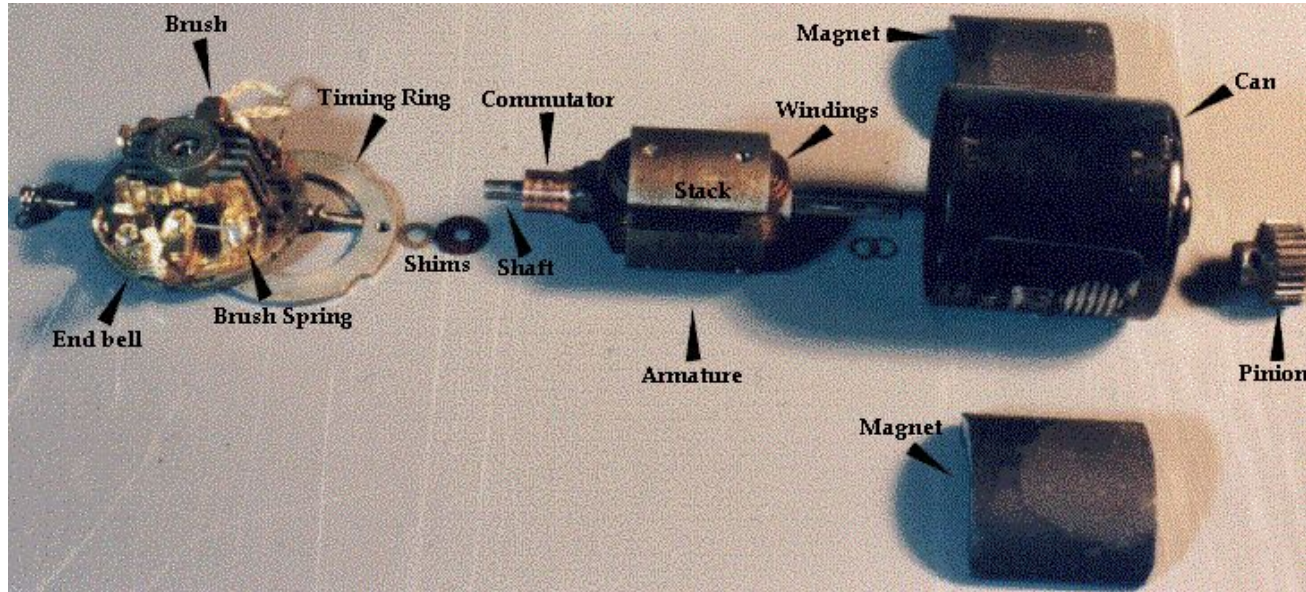
**1.2**

**DC Motors**



# DC motors -- exposed !

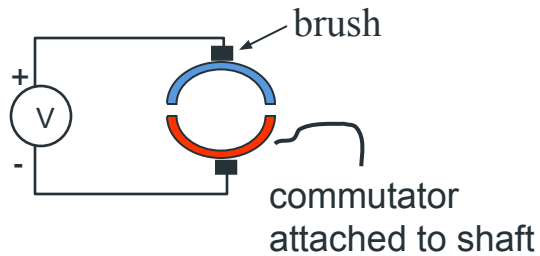
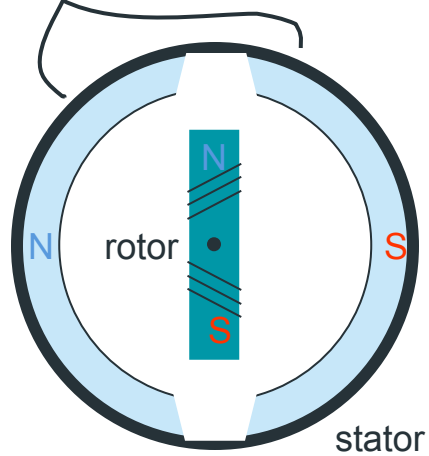
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# DC motor basics

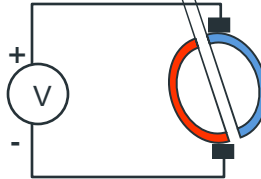
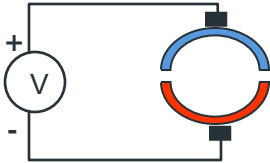
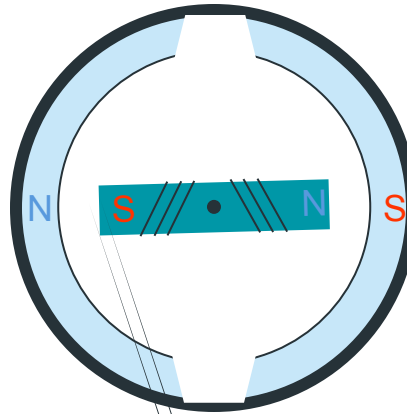
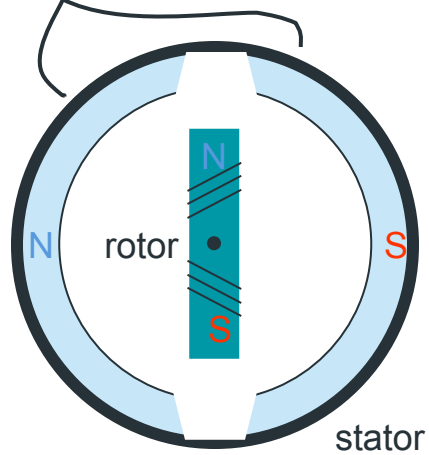
---

permanent  
magnets



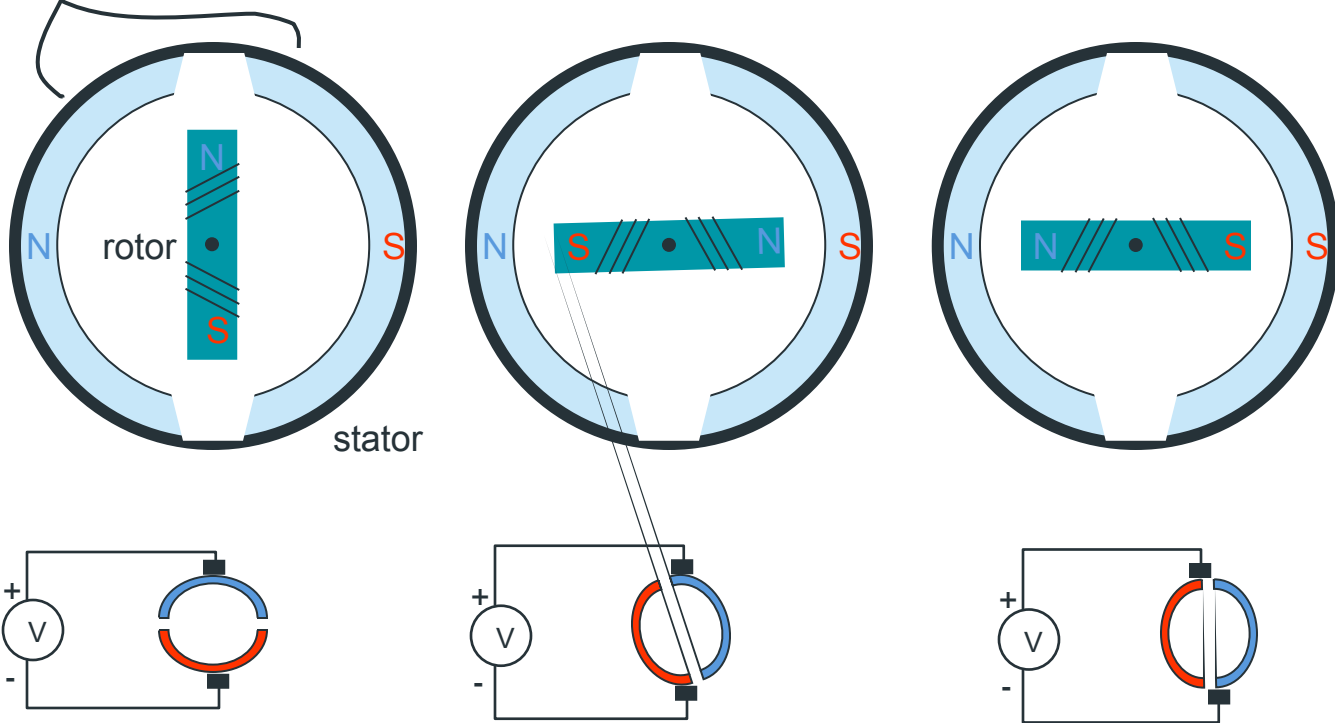
# DC motor basics

permanent  
magnets



# DC motor basics

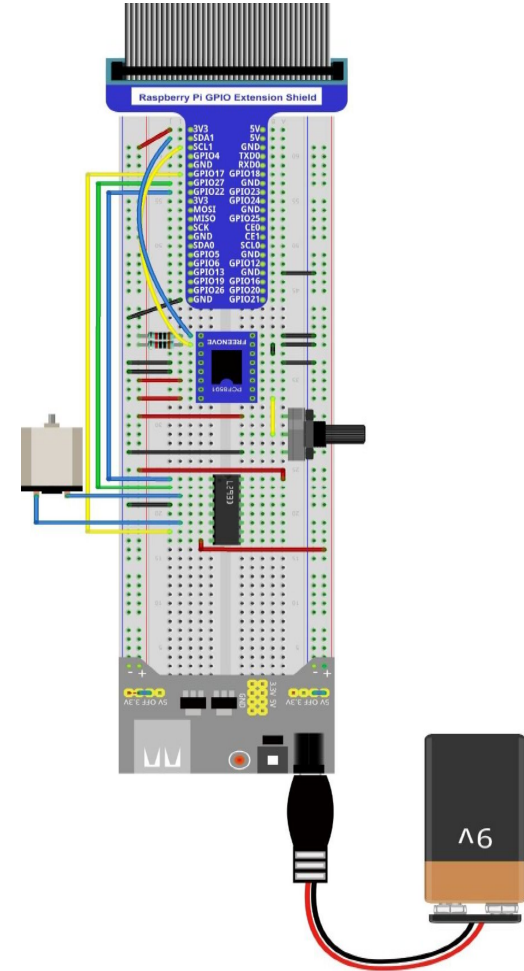
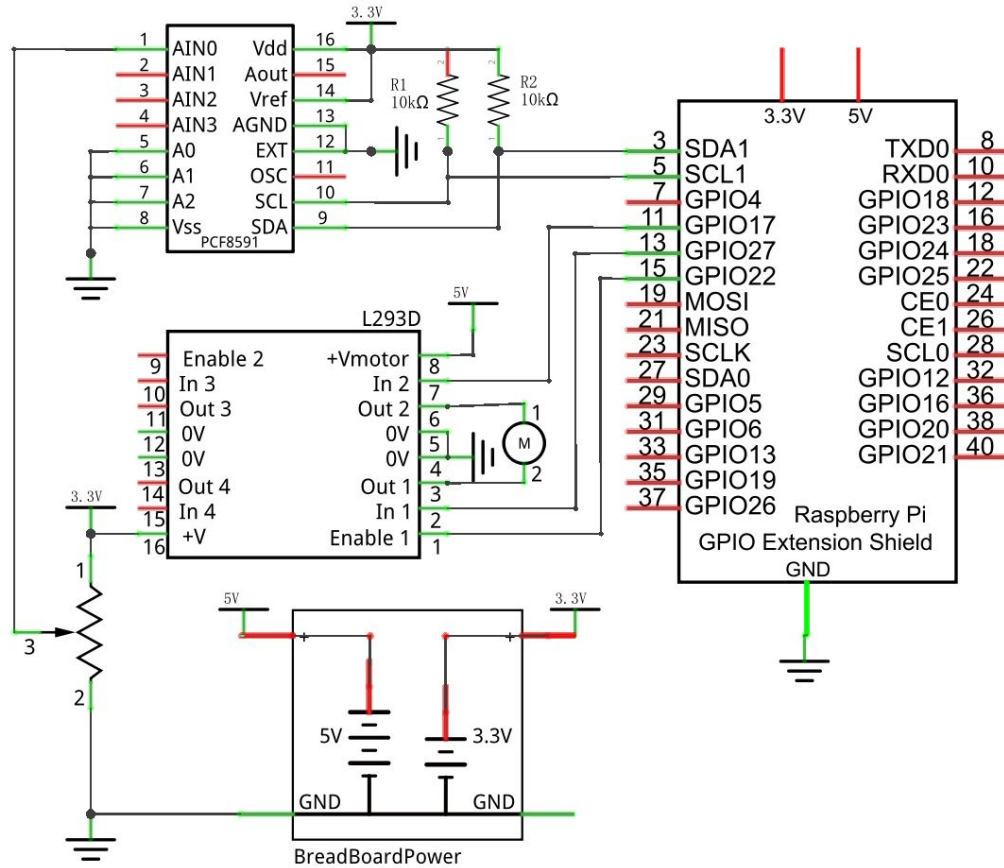
permanent  
magnets



## DC Motors Explained



## Project 13: DC Motor and Driver



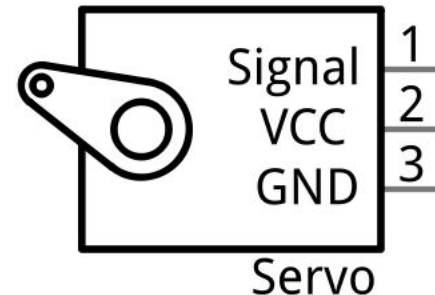
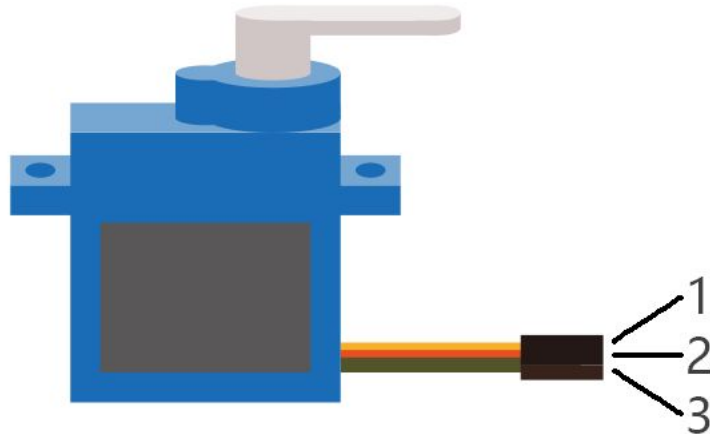


1.3

## **Servo Motors**

# Servo motor

- ❖ Compact package which consists of a DC Motor, a set of reduction gears to provide torque, a sensor for position feedback (potentiometer or encoder), and a closed-loop controller that uses position feedback to control its motion and final position.
- ❖ Servos can output higher torque than a simple DC Motor alone and they are widely used to control motion in toys, robots, etc.
- ❖ Servos have three wire leads, VCC, GND and servomotor signal
- ❖ Use a PWM signal with a duty cycle in a certain range to drive the Servo to the designated angle

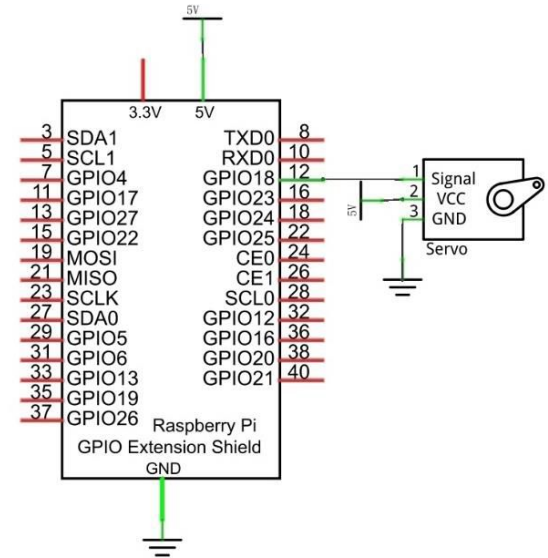
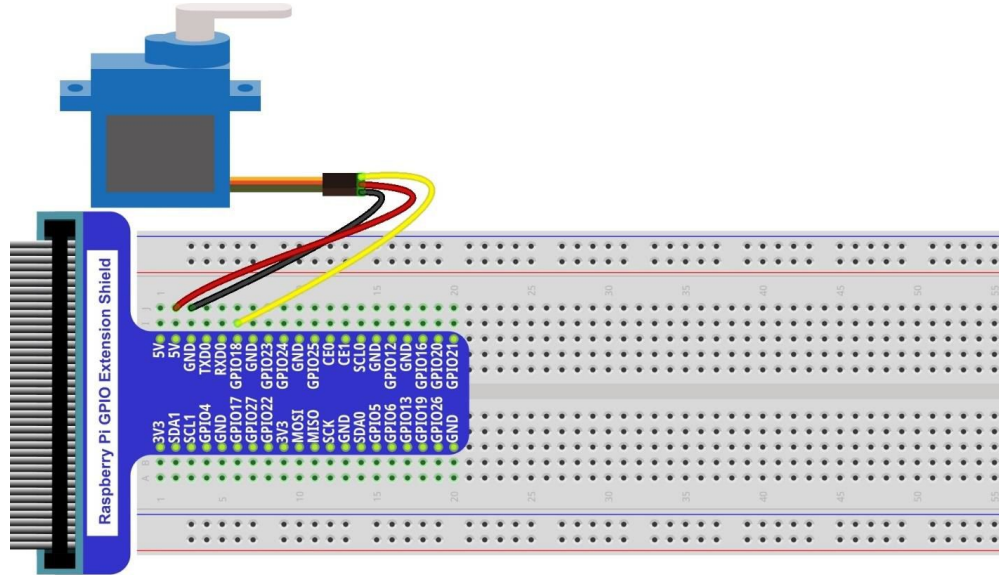




## Servo Motors Explained



## Project 15: Servo Motor Experiment





2

# **Motor Feedback Sensors**

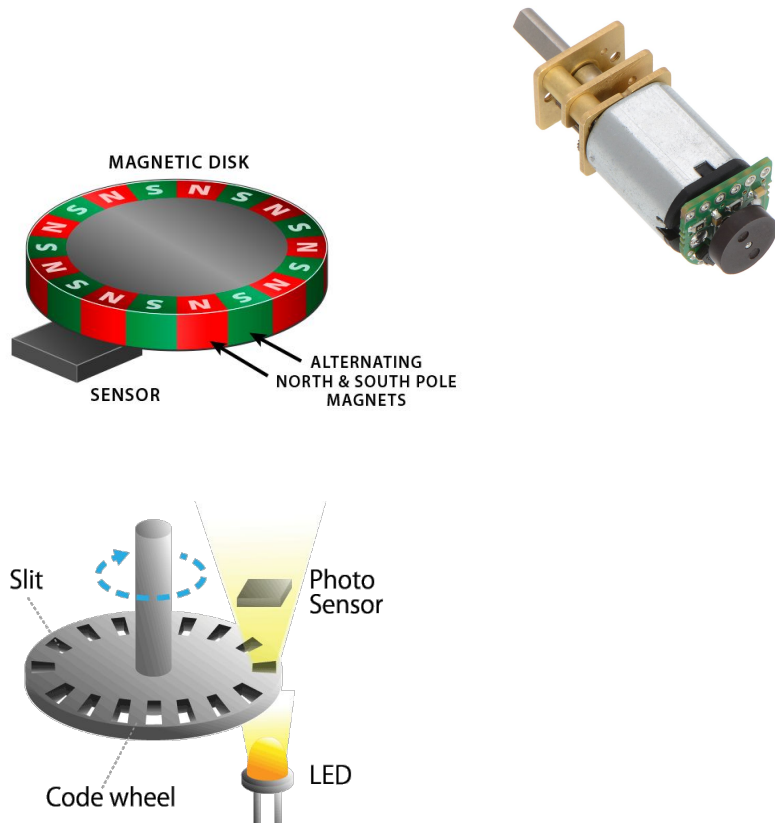
# ● Encoders

Encoders continually measure the rotation of the motor

Gives us a way to tell how **far** and **fast** we are traveling!

## Magnetic vs Optical Encoders

- Hall Effect Sensors



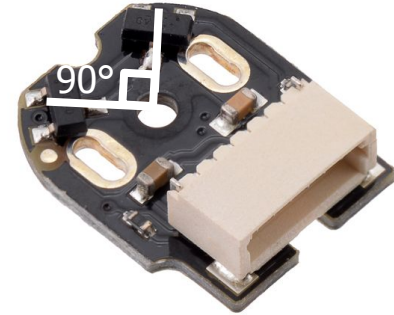
# Magnetic Encoders

Senses change in rotational position as  
motor spins  
6 pole magnetic disk (60° between each pole)

2 Hall Effect Sensors (90° between each sensor)

- Detects the presence of a magnetic field

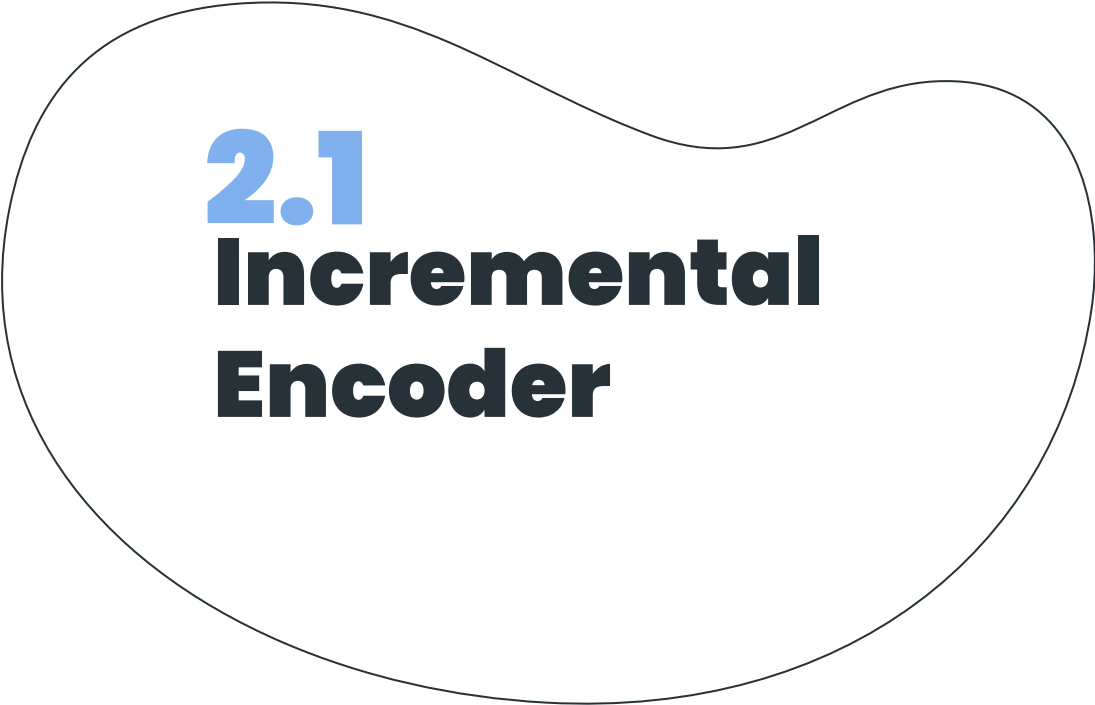
**Hall Effect:** Production of a voltage difference from a current and a magnetic field



# Motor Position Sensors

---

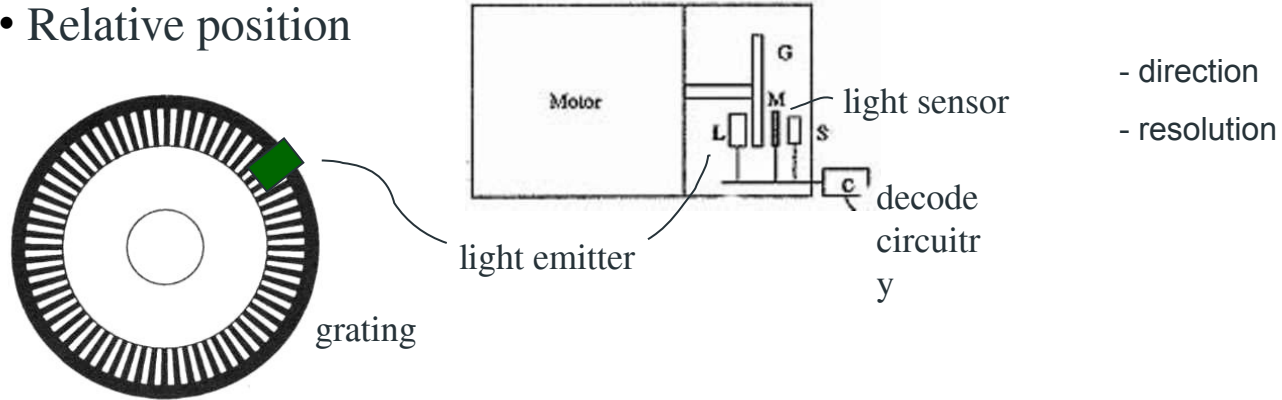
- Optical Encoders
  - Relative position
  - Absolute position
- Hall Effect Sensors



## 2.1 **Incremental Encoder**

# Optical Encoders

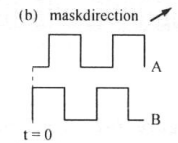
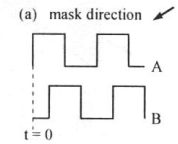
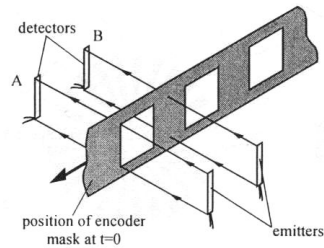
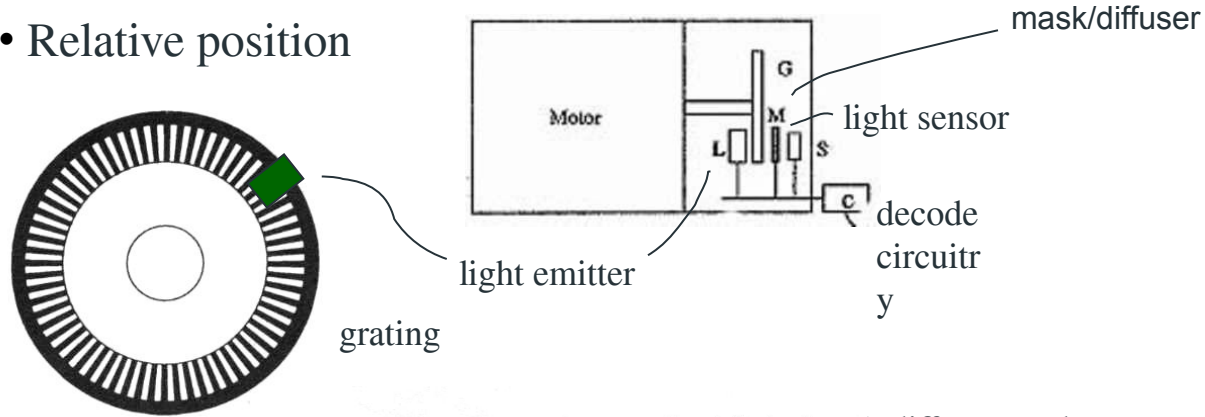
- Relative position





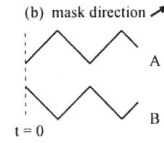
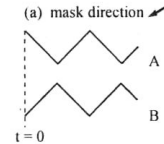
# Optical Encoders

- Relative position



saturated quadrature signals

Ideal



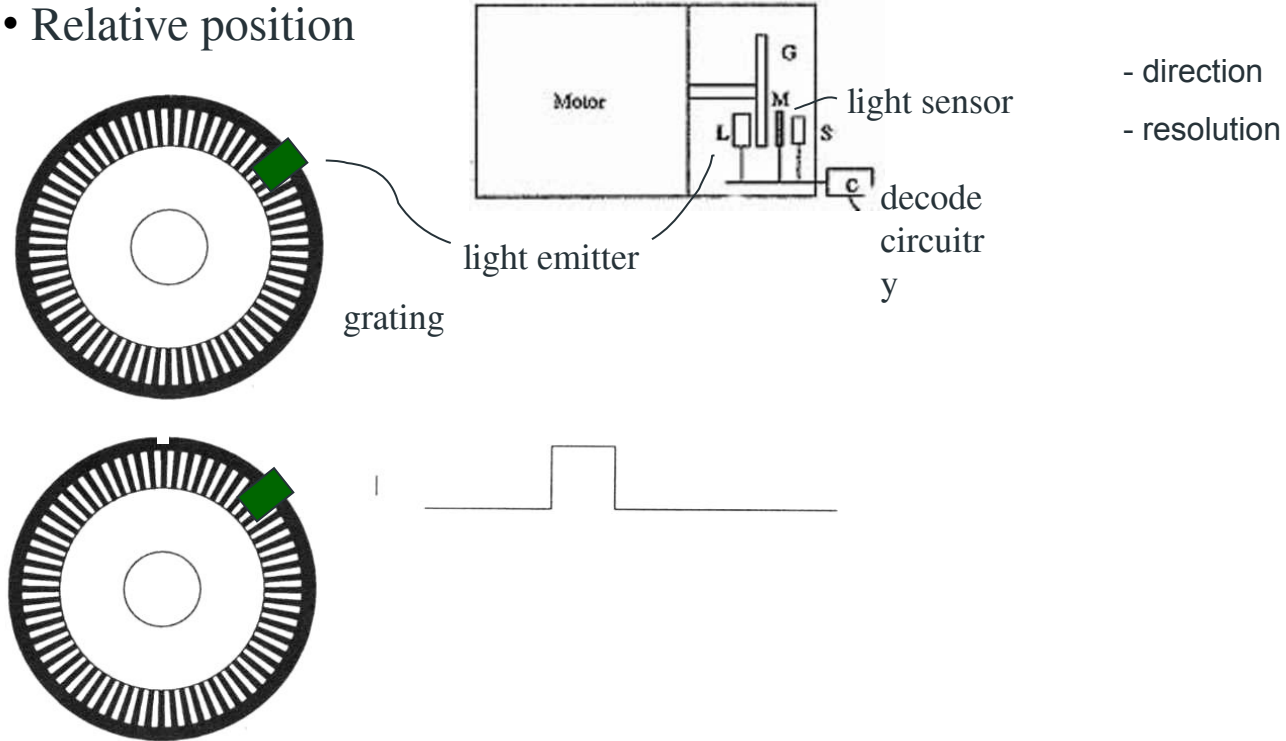
linear quadrature signals

Real

A diffuser tends to smooth these signals

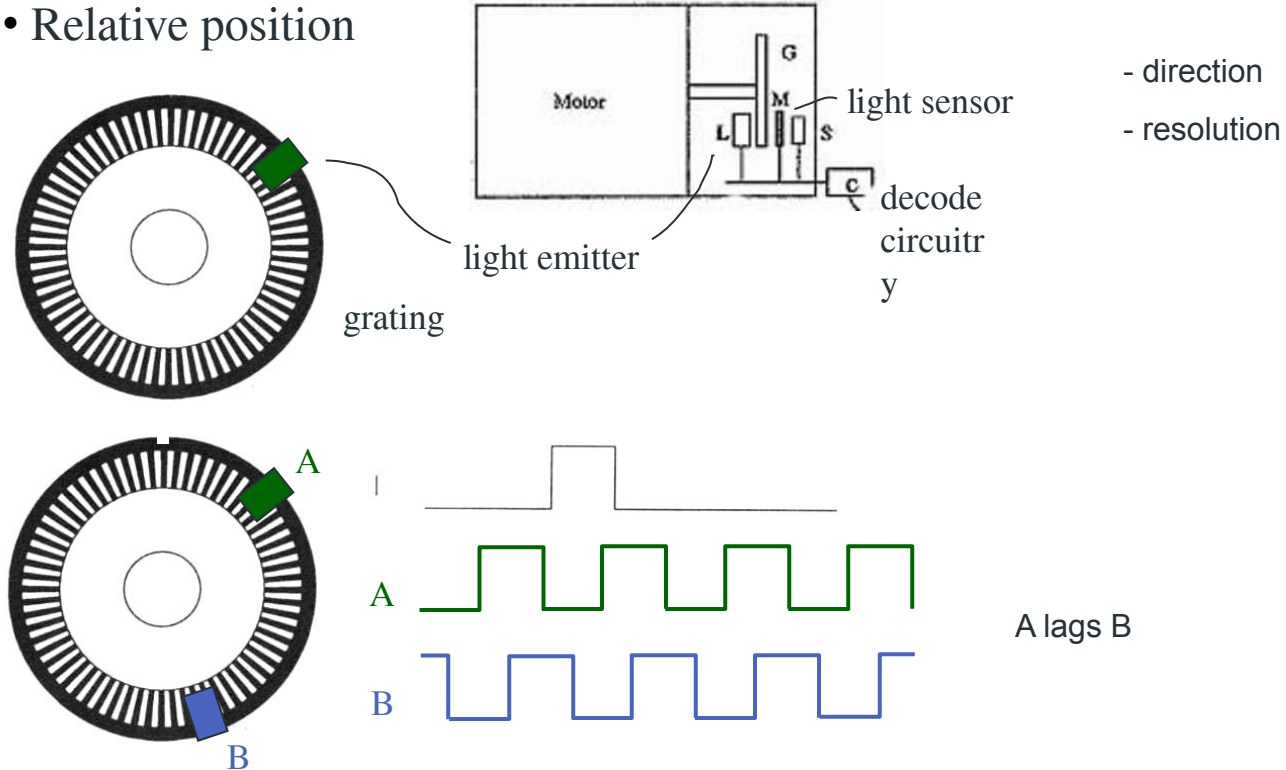
# Optical Encoders

- Relative position



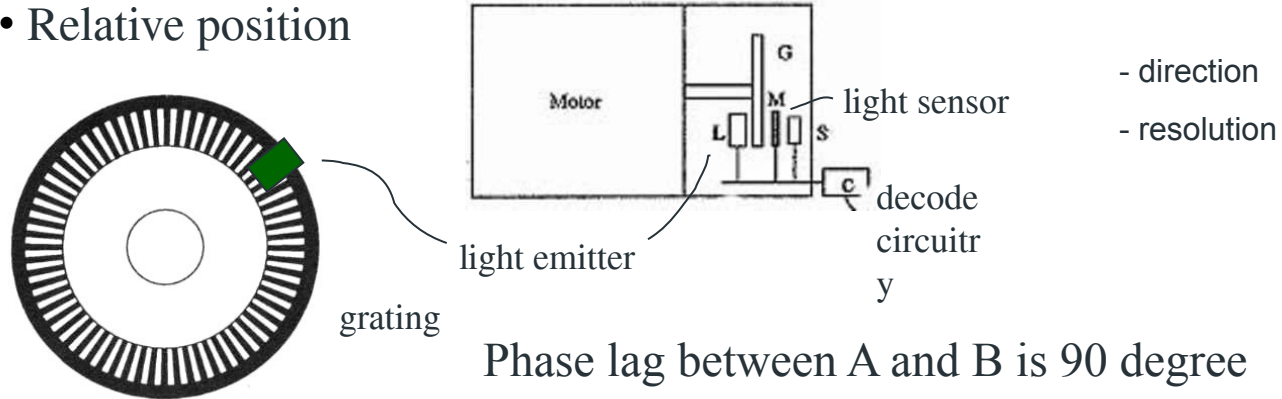
# Optical Encoders

- Relative position

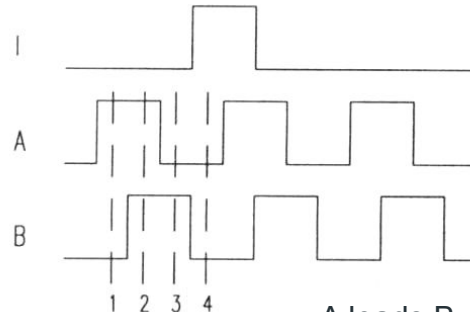
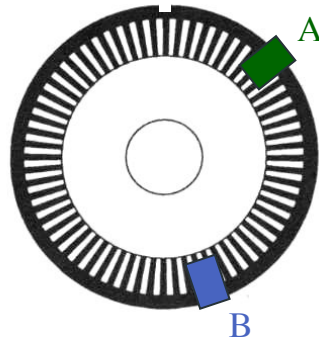


# Optical Encoders

- Relative position



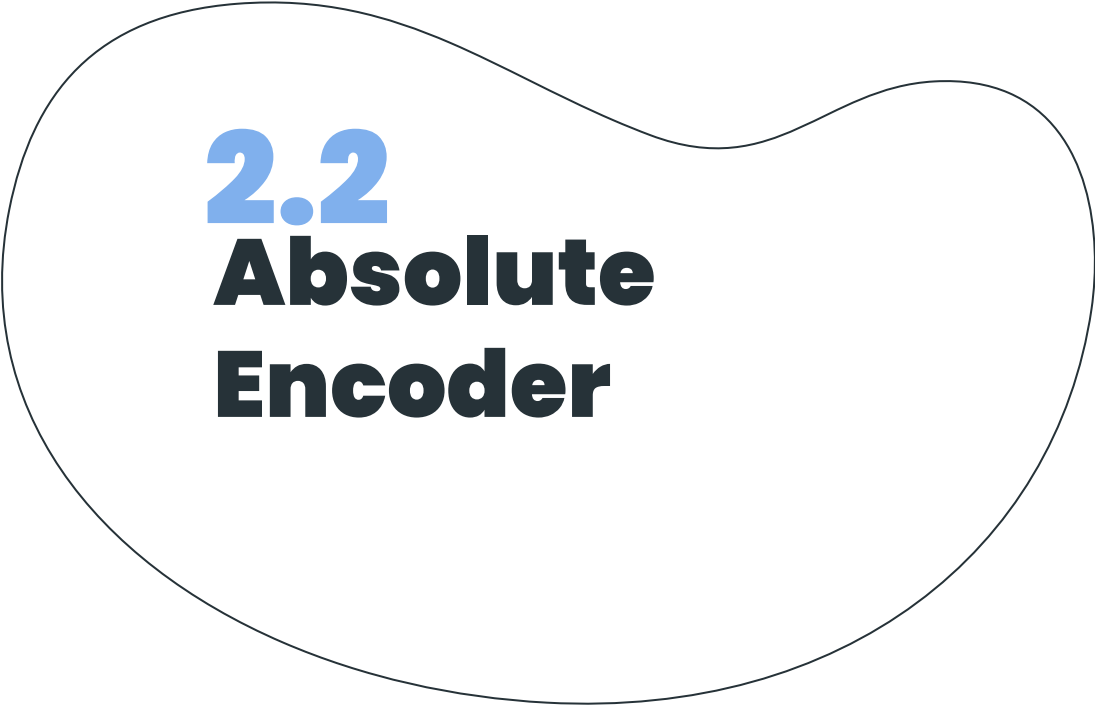
Phase lag between A and B is 90 degree



State	Ch A	Ch B
S <sub>1</sub>	High	Low
S <sub>2</sub>	High	High
S <sub>3</sub>	Low	High
S <sub>4</sub>	Low	Low

## Incremental Encoder

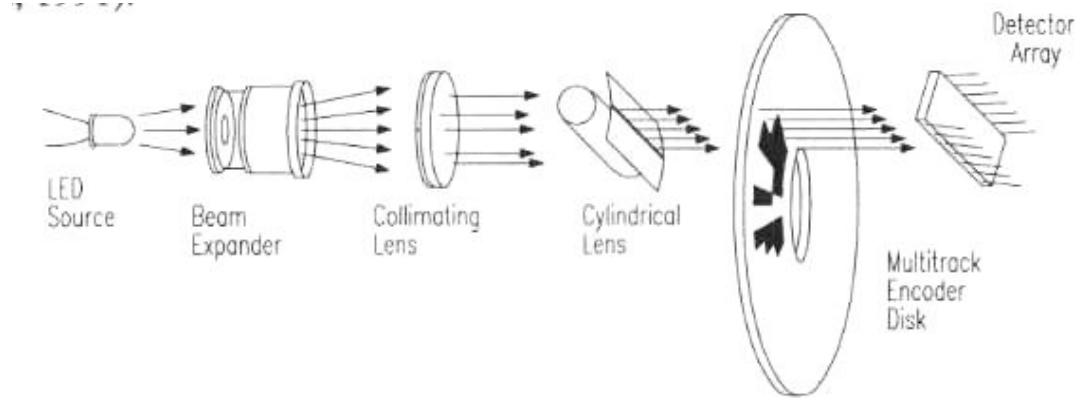




## 2.2 **Absolute Encoder**

# Optical Encoders

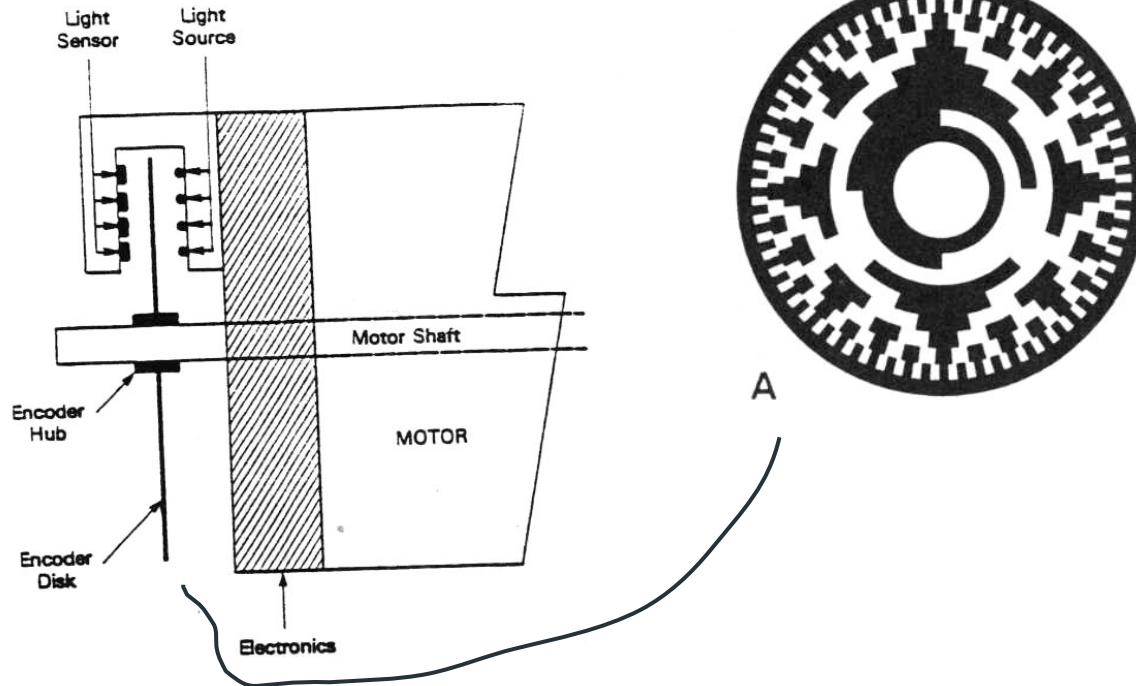
- Detecting absolute position



something simpler ?

# Absolute Encoders

- Detecting absolute position



wires ?



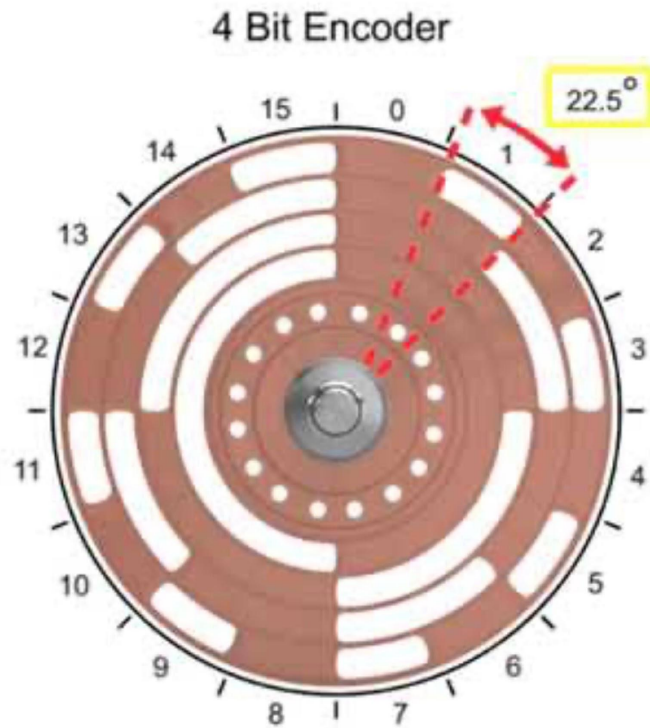
# Gray Code

#	Binary	
0	0	000
1	1	001
2	10	011
3	11	010
4	100	110
5	101	111
6	110	101
7	111	100
8	1000	
9	1001	



among others...

## Absolute Encoder



## Incremental v.s. Absolute Encoder

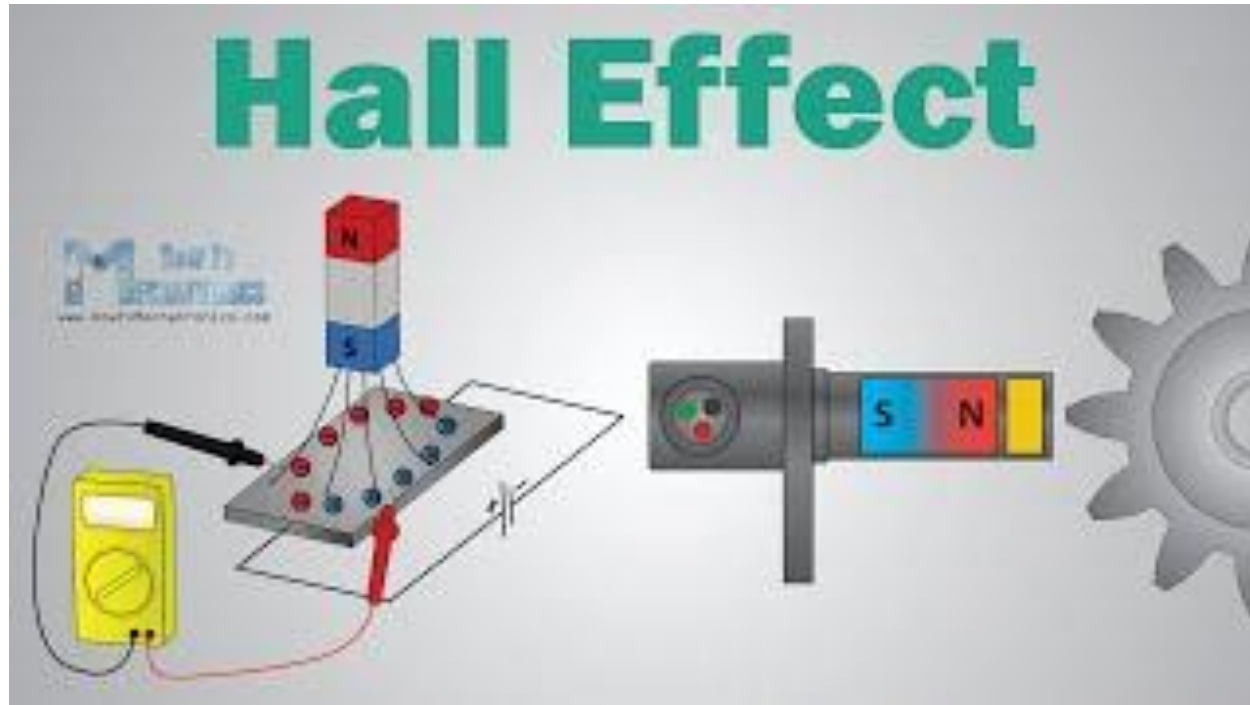
# ABSOLUTE VS. INCREMENTAL ENCODERS





## **2.3** **Hall Effect Sensors**

## Hall Effect and Hall Effect Sensors





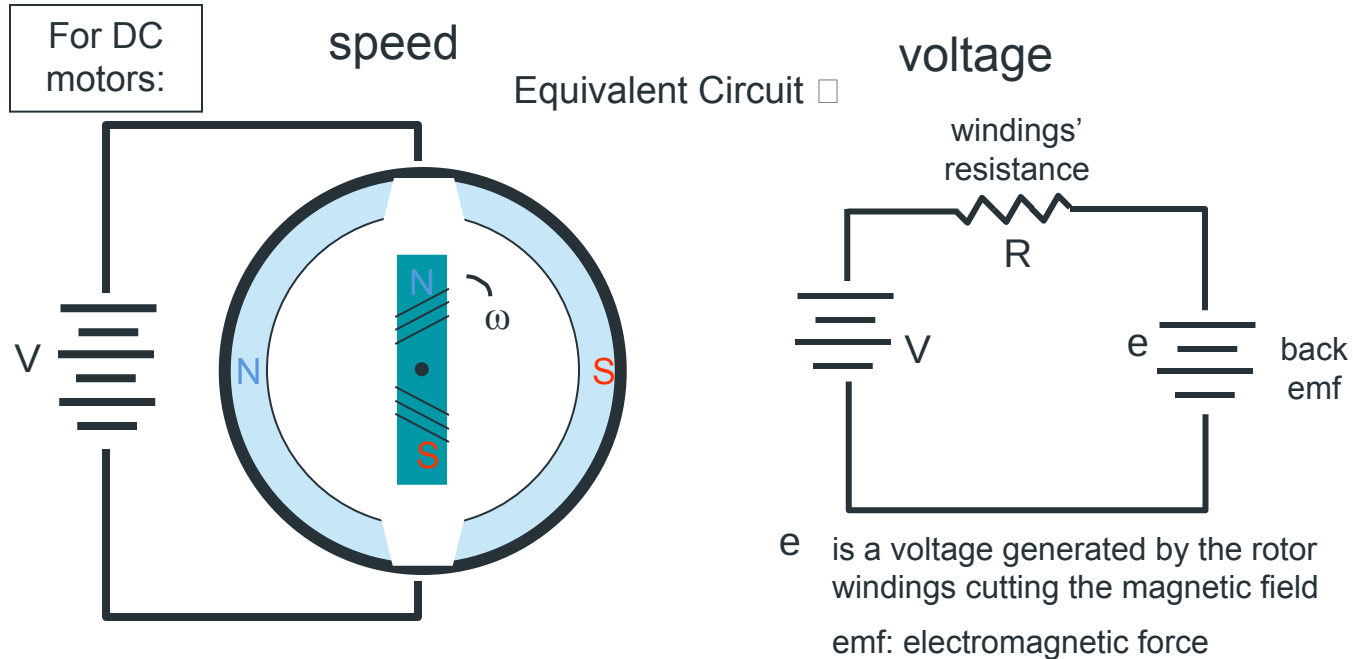
3

# Motor Control

# Motor Control

Control: getting motors to do what you want them to

What you want to control  $\neq$  what you can control

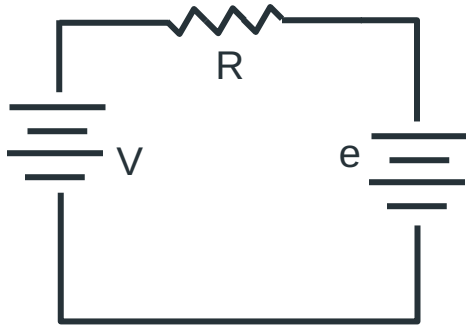


# Controlling speed with voltage

- The back emf depends only on the motor speed.
- The motor's torque depends only on the current,  $I$ .

$$e = k_e \omega$$

$$\tau = k_\tau I$$



DC motor model

Equivalent Circuit



# Controlling speed with voltage

- The back emf depends only on the motor speed.
- The motor's torque depends only on the current,  $I$ .

$$e = k_e \omega$$

$$\tau = k_\tau I$$

---

$$V = IR + e$$

How is  $V$  related to  $\omega$  ?

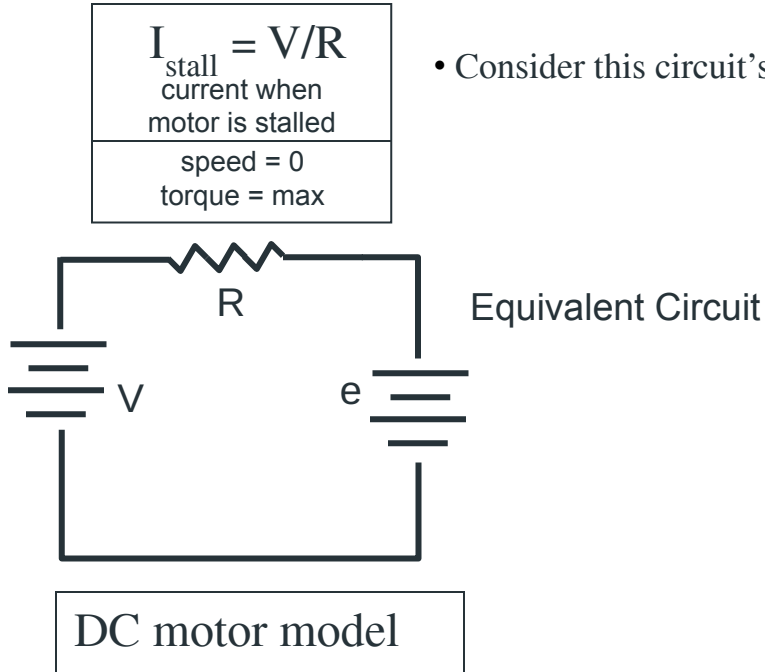
$$V = \frac{\tau R}{k_\tau} + k_e \omega$$

- or -

$$\omega = -\frac{R}{k_\tau k_e} \tau + \frac{V}{k_e}$$

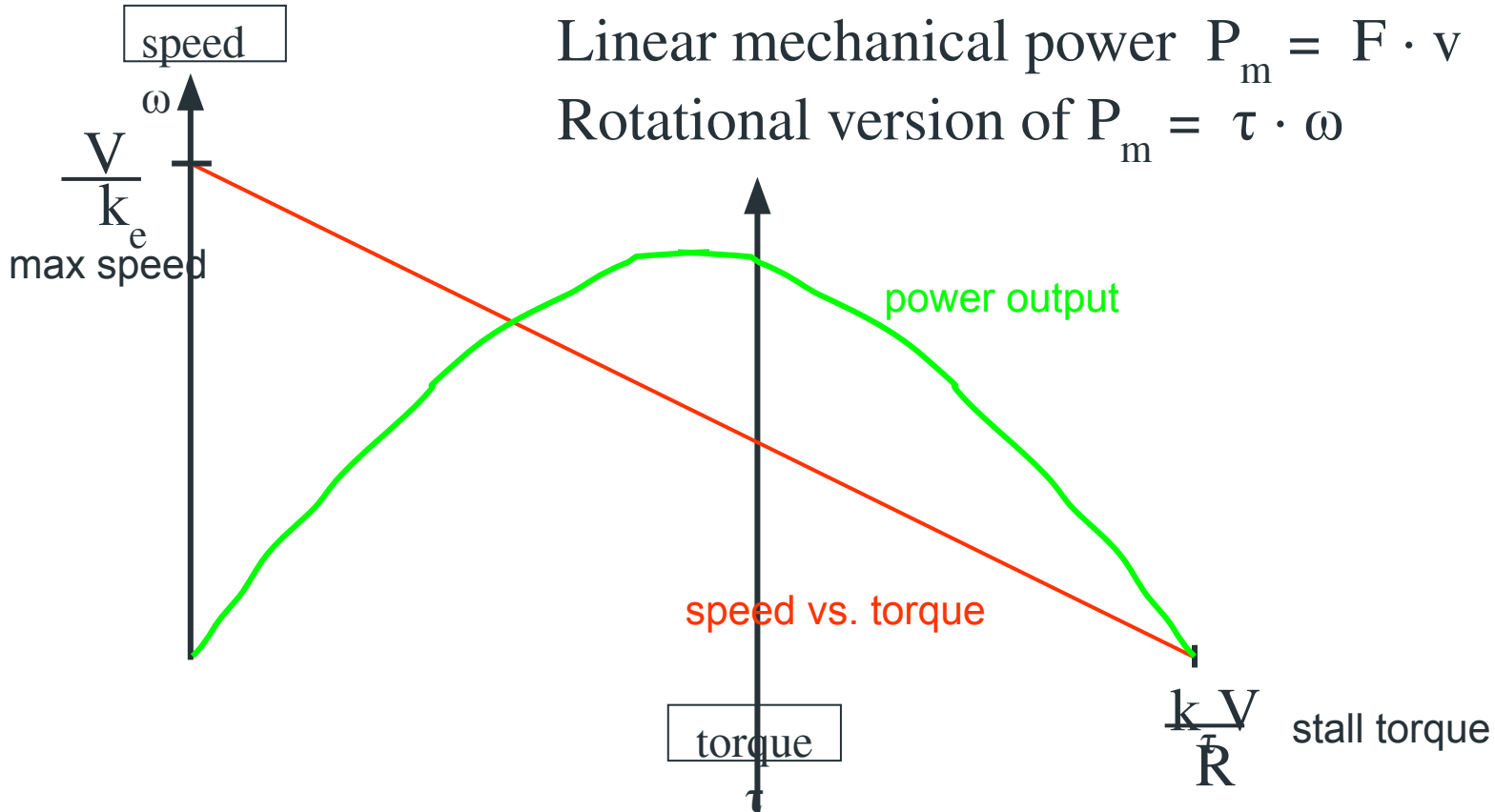
Speed is proportional to voltage.

- Consider this circuit's  $V$ :

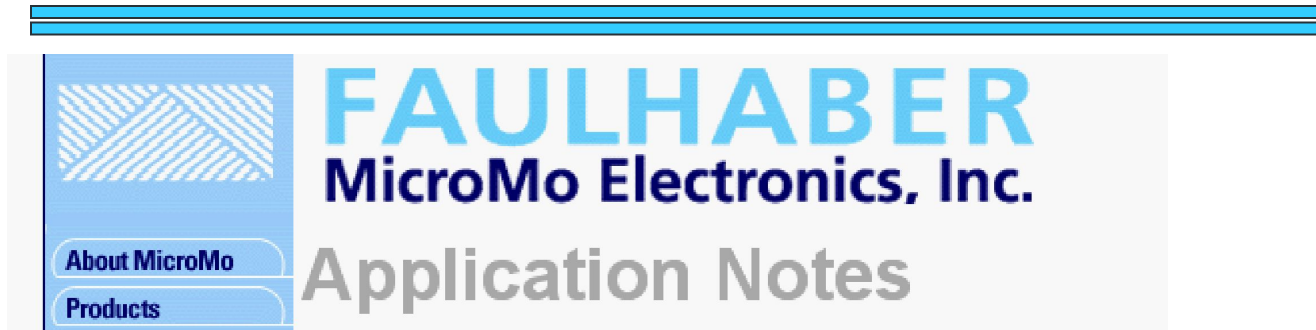


# speed vs. torque

at a fixed voltage



# Motor specs



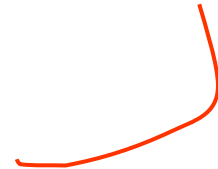
## Electrical Specifications (@22°C)

For motor type 1624		003S	006S	012S	024
nominal supply voltage	(Volts)	3	6	12	24
armature resistance	(Ohms)	1.6	8.6	24	75
maximum power output	(Watts)	1.41	1.05	1.50	1.92
maximum efficiency	(%)	76	72	74	74
no-load speed	(rpm)	12,000	10,600	13,000	14,400
no-load current	(mA)	30	16	10	6
friction torque	(oz-in)	.010	.011	.013	.013
stall torque	(oz-in)	.613	.510	.600	.694
velocity constant	(rpm/v)	4065	1808	1105	611
back EMF constant	(mV/rpm)		.246	.553	.905
torque constant	(oz-in/A)	.333	.748	1.223	2.212
armature inductance	(mH)	.085	.200	.750	3.00

$k_e$



$k_\tau$



# Back to control

---

Basic input / output relationship:

$$V = \frac{\tau R}{k_\tau} + k_e \omega$$

We can control the  
voltage applied  $V$ .

---

We want a particular  
motor speed  $\omega$ .

How to change the voltage?

$V$  is usually controlled via PWM -- “pulse width modulation”

3

## DC Motor Control

Turning the motors on and off,  
controlling  
the motor's direction and speed



## Checklist for Motor Control

---



Motor On/Off State



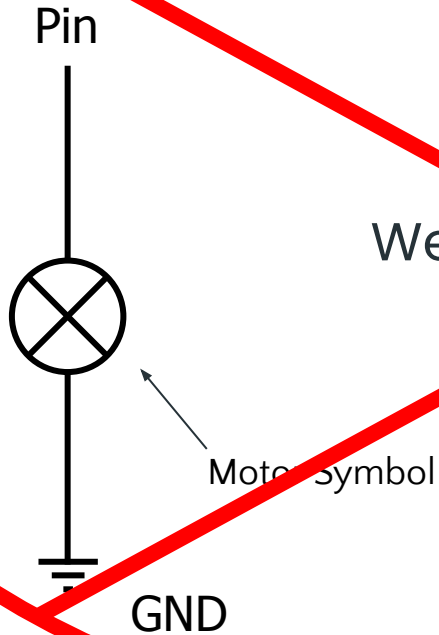
Motor Direction



Motor Speed



# Motor On/Off State



We can connect the motors directly to the output pins on the microcontroller

# ● Motor On/Off State

We can't power the motor directly from the MCU!!

Why? Not enough voltage or current from the MCU

Motors require at least 6V and can draw up to 0.67A

MCU can only supply 3.3V and relatively little current



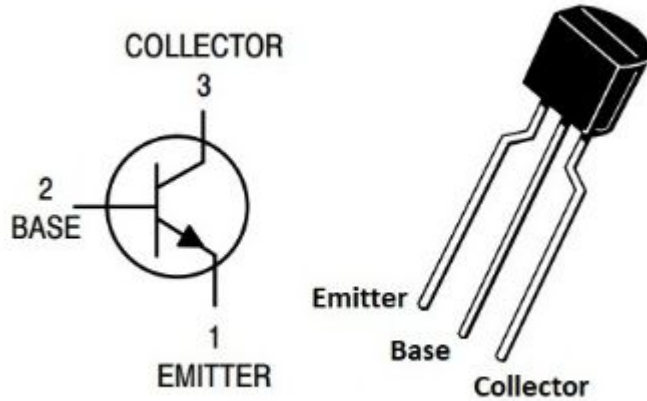
Big boi battery power



MCU power



# (Part of) The Solution: Transistors



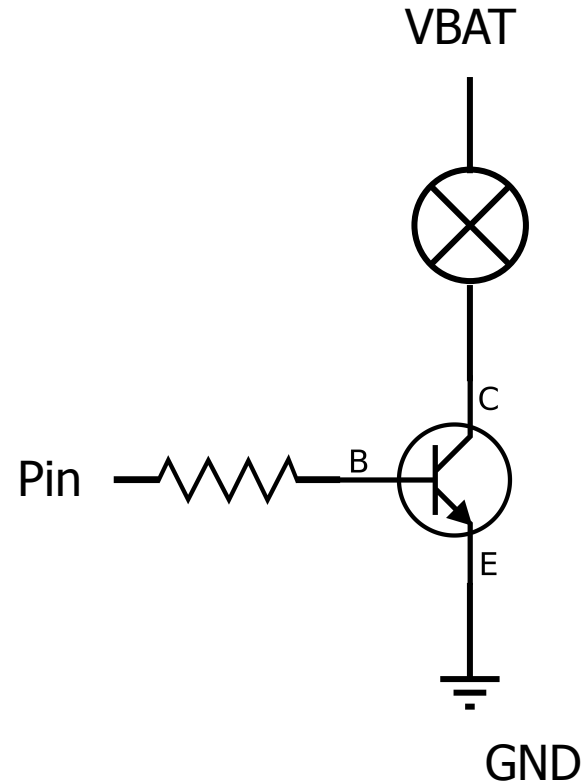
The NPN transistor acts as a normally open switch

When voltage is applied to the base, current is allowed to flow between the collector and the emitter.

Similar to relays, except faster and better suited for smaller applications

# ● (Part of) The Solution: Transistors

We can control the on and off state of the motor from the MCU using an NPN transistor!



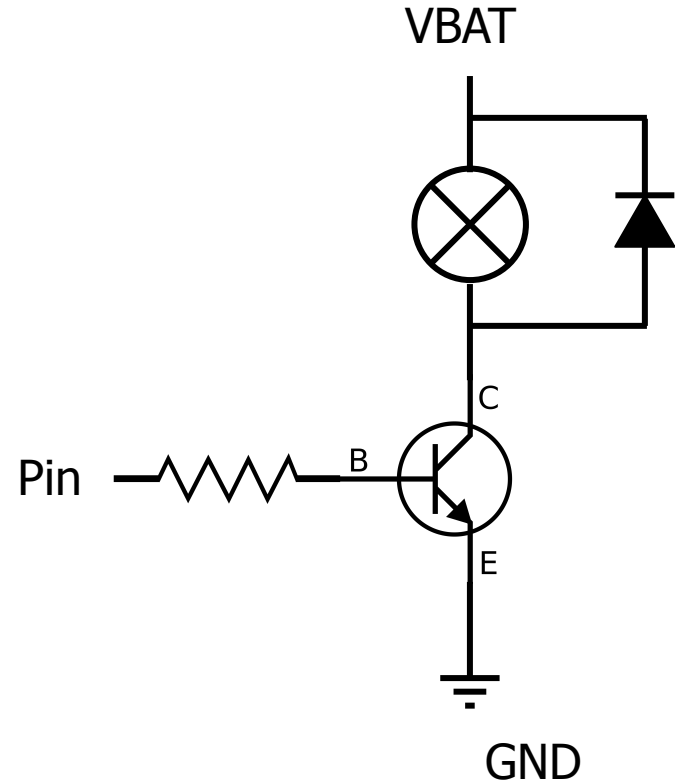
# Flyback Diode

Recall that motors involve creating magnetic fields...

Inductance!

Turning motors off results in a temporary voltage spike to maintain current (back emf)

Diode: allows current to flow in ONE direction





## Checklist for Motor Control

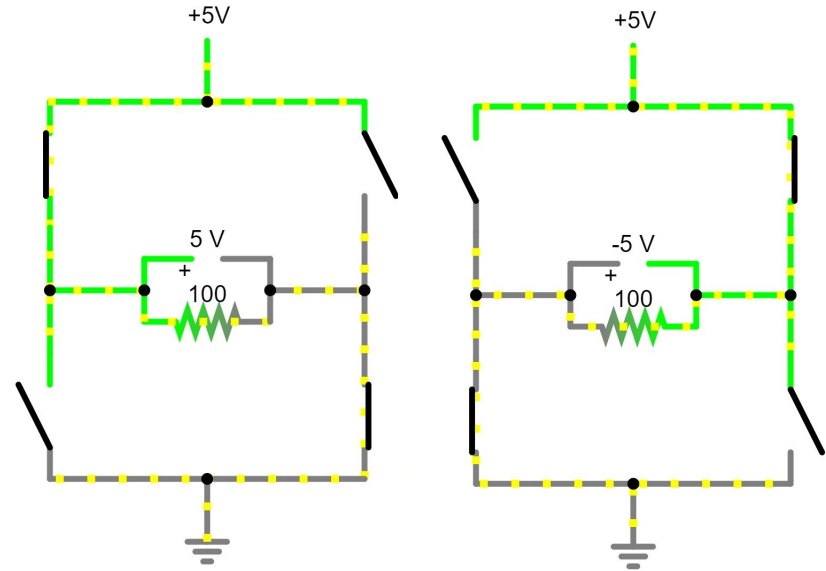
---

- ☒ Motor On/Off State
- ☐ Motor Direction
- ☐ Motor Speed



We can take advantage  
of this fact to create a  
circuit called an H-Bridge

<https://tinyurl.com/yxn4yk4>



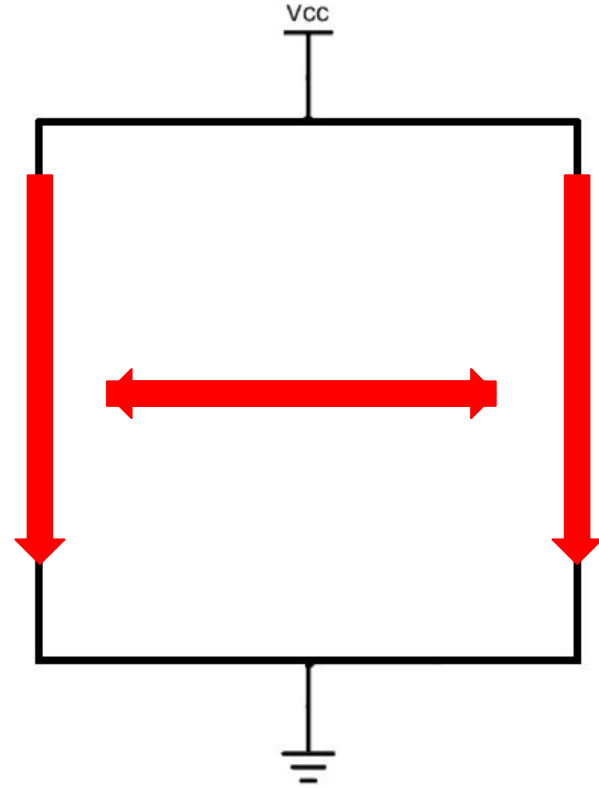
# H-Bridge

## Four Transistors, Four Flyback Diodes

Turning on Q1 and Q4  $\Rightarrow$  current flows through the motor to the **right**.

Turning on Q2 and Q3  $\Rightarrow$  current flows through the motor to the **left**.

Turning on all four transistors results in a short circuit – **Don't do it!**



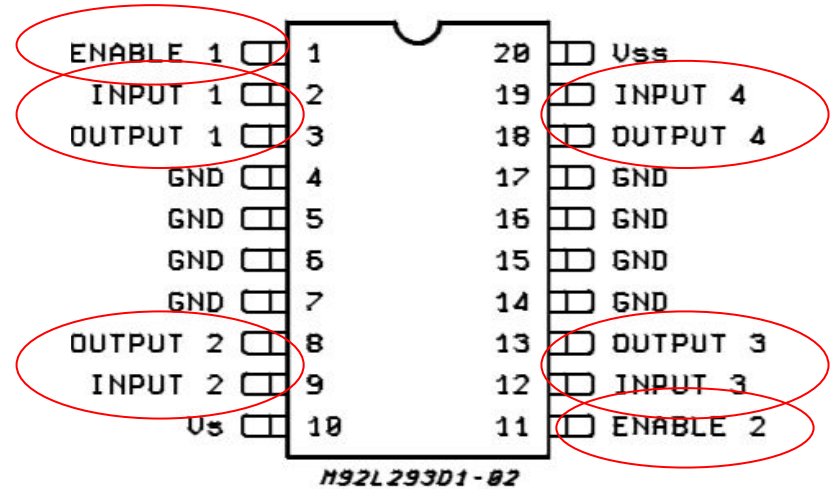
# Dual ● H-Bridge S

One IC to control two motors!

Four **Inputs**: each input is connected to two transistors (i.e input 1 turns on Q1 and Q4)

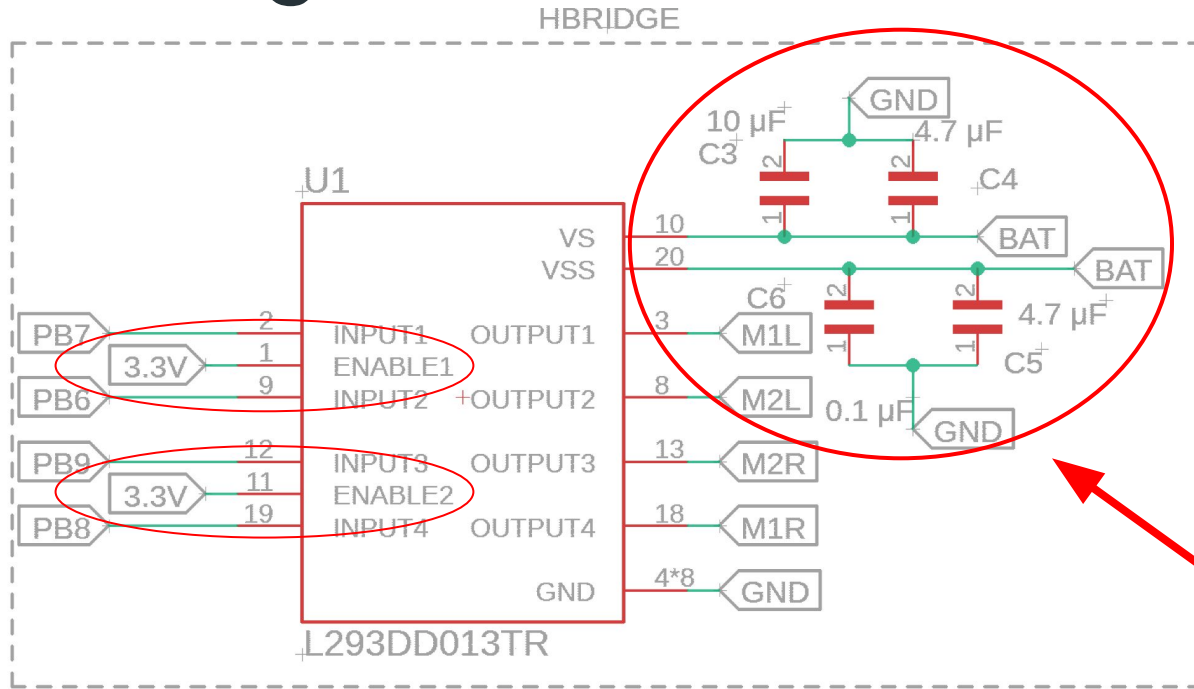
Four **Outputs**: two outputs to connect to each motor

**Enable Pins**: activate the H-Bridge and allow us to turn on the transistors



L293DD H-Bridge

# Dual ● H-Bridge S

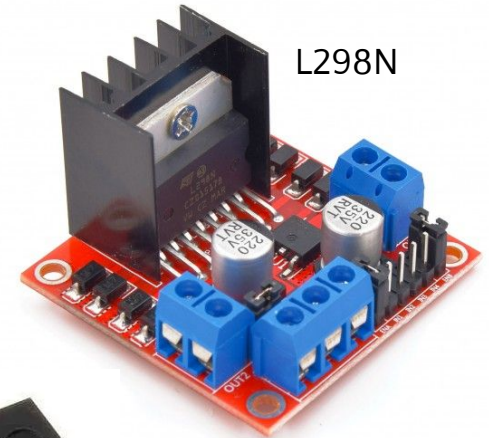
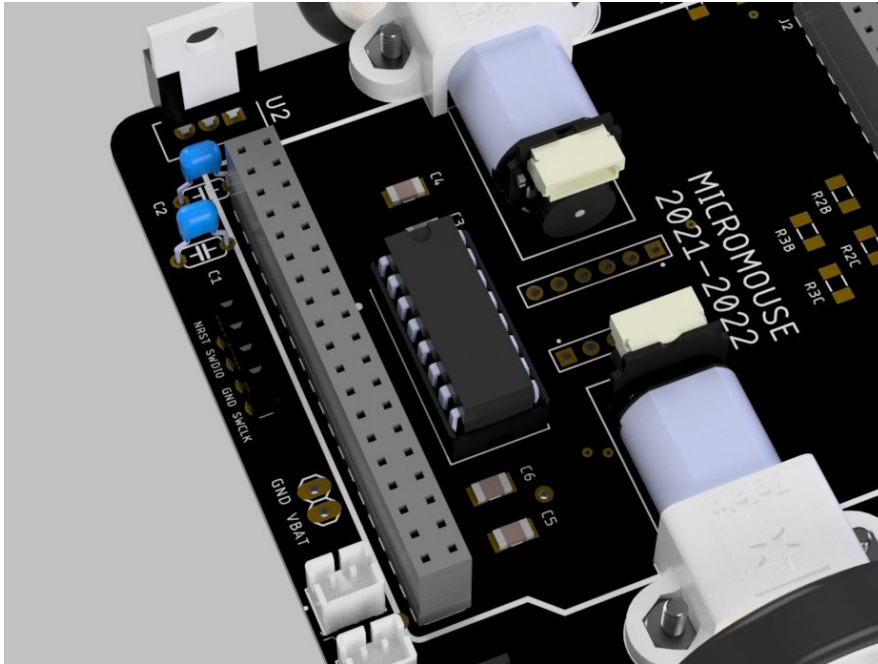


**Decoupling Capacitors:**

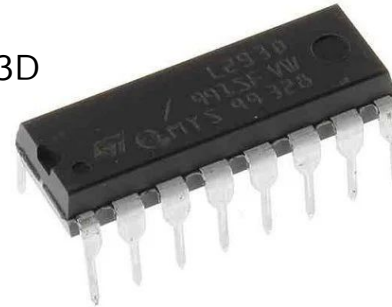
Low pass filter to remove noise



## The Physical H-Bridge ICs



L293D





## Checklist for Motor Control

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Motor On/Off State



Motor Direction



Motor Speed



## The Problem: Motor Speed



Since we are directly connecting the motors to the battery voltage, we only have two speeds -> 0% and 100%

How do we tell the motors to go 50% speed? 75%?

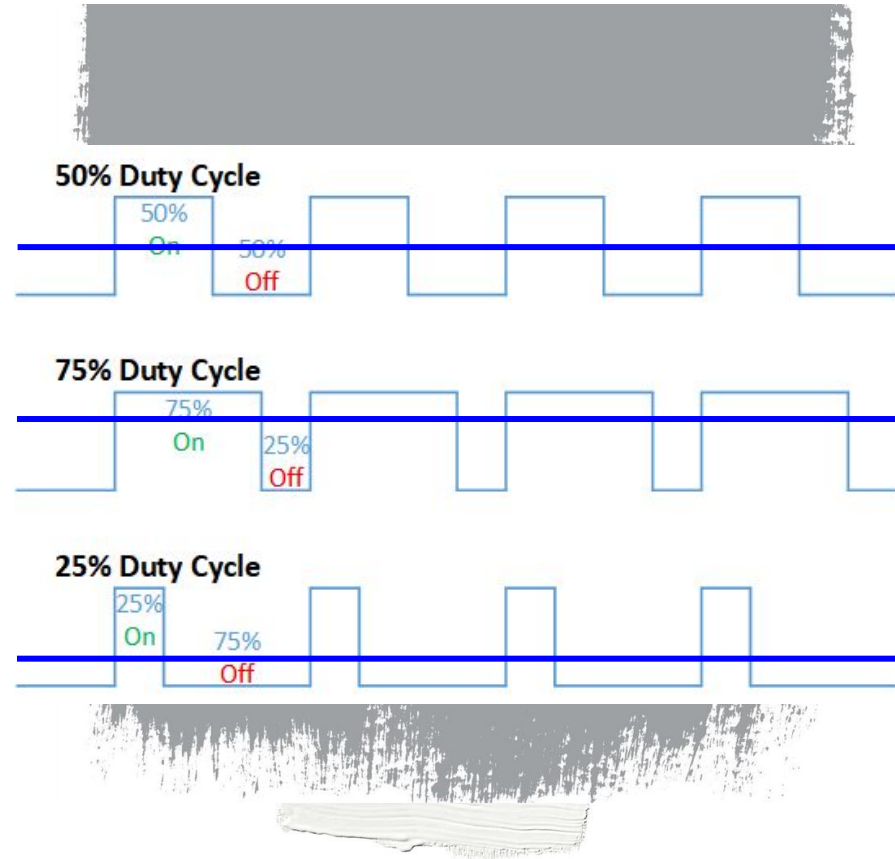
# PWM

We can rapidly mix on and off inputs to create a range of voltages

Motors have inertia, so they respond slowly to rapid voltage changes

Quick Vocab Terms:

- PWM: Pulse-Width Modulation
- Duty Cycle: % of time in the ON state
- Frequency: # of cycles per second





# PWM on our MCU

Implemented using Timers!

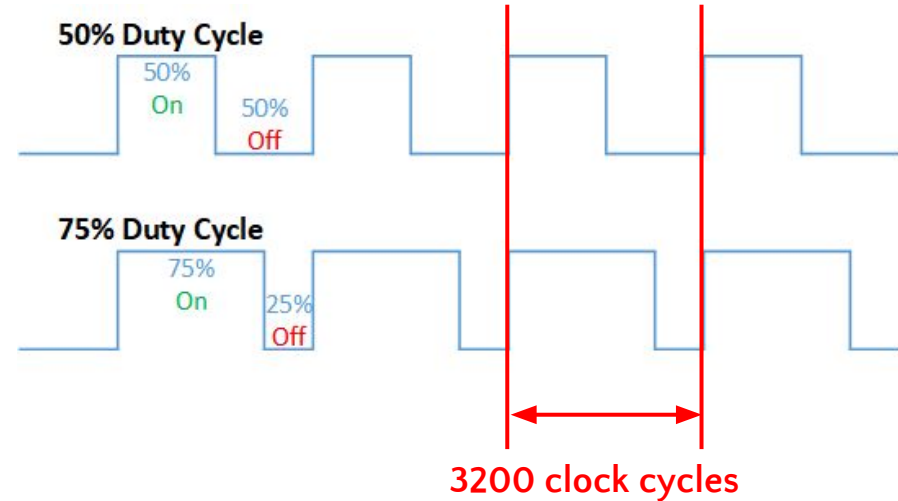
MCU Clock Speed 16 MHz

H-Bridge Max Frequency 5 kHz

Counter Period:  $16 \text{ MHz} / 5 \text{ kHz} = \mathbf{3200 \text{ clock cycles}}$

Pulse Value: Clock cycles to stay on per period

Ex. 75% duty cycle  $\Rightarrow$  2400 clock cycles on, 800 off





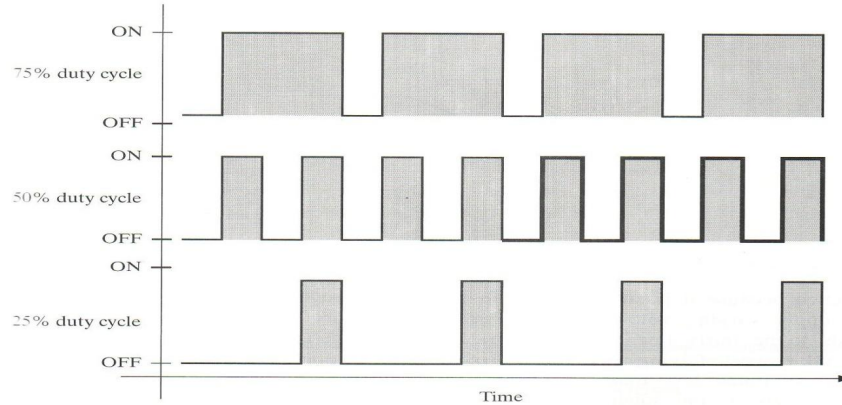
## Checklist for Motor Control

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- ☒ Motor On/Off State
- ☒ Motor Direction
- ☒ Motor Speed

# PWM

- PWM -- “pulse width modulation



- Duty cycle:
  - The ratio of the “On time” and the “Off time” in one cycle
  - Determines the fractional amount of full power delivered to the motor