

神秘模板库

Toy ASM Truck

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一切的开始

宏定义

数据结构

ST 表

- 二维

```
1 int f[maxn][maxn][10][10];
2 inline int highbit(int x) { return 31 - __builtin_clz(x); }
3 inline int calc(int x, int y, int xx, int yy, int p, int q) {
4     return max(
5         max(f[x][y][p][q], f[xx - (1 << p) + 1][yy - (1 << q) + 1][p][q]),
6         max(f[xx - (1 << p) + 1][y][p][q], f[x][yy - (1 << q) + 1][p][q])
7     );
8 }
9 void init() {
10     FOR (x, 0, highbit(n) + 1)
11     FOR (y, 0, highbit(m) + 1)
12         FOR (i, 0, n - (1 << x) + 1)
13             FOR (j, 0, m - (1 << y) + 1) {
14                 if (!x && !y) { f[i][j][x][y] = a[i][j]; continue; }
15                 f[i][j][x][y] = calc(
16                     i, j,
17                     i + (1 << x) - 1, j + (1 << y) - 1,
18                     max(x - 1, 0), max(y - 1, 0)
19                 );
20             }
21 }
22 inline int get_max(int x, int y, int xx, int yy) {
23     return calc(x, y, xx, yy, highbit(xx - x + 1), highbit(yy - y + 1));
24 }
```

数学

类欧几里得

- $m = \lfloor \frac{an+b}{c} \rfloor$.
- $f(a, b, c, n) = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor$: 当 $a \geq c$ or $b \geq c$ 时, $f(a, b, c, n) = (\frac{a}{c})n(n+1)/2 + (\frac{b}{c})(n+1) + f(a \bmod c, b \bmod c, c, n)$; 否则 $f(a, b, c, n) = nm - f(c, c-b-1, a, m-1)$ 。
- $g(a, b, c, n) = \sum_{i=0}^n i \lfloor \frac{ai+b}{c} \rfloor$: 当 $a \geq c$ or $b \geq c$ 时, $g(a, b, c, n) = (\frac{a}{c})n(n+1)(2n+1)/6 + (\frac{b}{c})n(n+1)/2 + g(a \bmod c, b \bmod c, c, n)$; 否则 $g(a, b, c, n) = \frac{1}{2}(n(n+1)m - f(c, c-b-1, a, m-1) - h(c, c-b-1, a, m-1))$ 。
- $h(a, b, c, n) = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor^2$: 当 $a \geq c$ or $b \geq c$ 时, $h(a, b, c, n) = (\frac{a}{c})^2 n(n+1)(2n+1)/6 + (\frac{b}{c})^2 (n+1) + (\frac{a}{c})(\frac{b}{c})n(n+1) + h(a \bmod c, b \bmod c, c, n) + 2(\frac{a}{c})g(a \bmod c, b \bmod c, c, n) + 2(\frac{b}{c})f(a \bmod c, b \bmod c, c, n)$; 否则 $h(a, b, c, n) = nm(m+1) - 2g(c, c-b-1, a, m-1) - 2f(c, c-b-1, a, m-1) - f(a, b, c, n)$ 。

Pollard-Rho

```
1 template<const int test_case> // set 8 usually
2 struct Pollard_Rho {
3     vector<long long> fac;
4     long long quick_pow(long long a, long long b, long long mod) {
5         long long ans = 1;
6         while (b) {
7             if (b&1) ans = (__int128)ans*(__int128)a%mod;
8             b >>= 1, a = (__int128)a*(__int128)a%mod;
9         }
10        return ans;
11    }
12    bool Miller_Rabin(long long n) { // return if n is a prime
13        if (n < 3) return n == 2;
14        long long a = n-1, b = 0;
15        while (a%2 == 0) a /= 2, ++b;
```

```

16     for (int i = 0, j; i < test_case; i++) {
17         long long x = rand()%(n-2)+2, v = quick_pow(x, a, n);
18         if (v == 1 || v == n-1) continue;
19         for (j = 0; j < b; j++) {
20             v = (__int128)v*(__int128)v%n;
21             if (v == n-1) break;
22         }
23         if (j >= b) return false;
24     }
25     return true;
26 }
27 long long f(long long x, long long c, long long n) { return ((__int128)x * x + c) % n; }
28 long long rho(long long x) {
29     long long s = 0, t = 0;
30     long long c = (__int128)rand() % (x - 1) + 1;
31     int step = 0, goal = 1;
32     long long val = 1;
33     for (goal = 1; goal <= 1, s = t, val = 1) {
34         for (step = 1; step <= goal; ++step) {
35             t = f(t, c, x);
36             val = (__int128)val * abs(t - s) % x;
37             if ((step % 127) == 0) {
38                 long long d = __gcd(val, x);
39                 if (d > 1) return d;
40             }
41         }
42         long long d = __gcd(val, x);
43         if (d > 1) return d;
44     }
45 }
46 void find(long long x) {
47     if (x == 1) return;
48     if (Miller_Rabin(x)) {
49         fac.push_back(x);
50         return;
51     }
52     long long p = x;
53     while (p >= x) p = rho(x);
54     //while ((x % p) == 0) x /= p;
55     find(x/p), find(p);
56 }
57 vector<long long> factor(long long n) { // return the factors of n
58     srand((unsigned)time(NULL));
59     fac.clear();
60     find(n);
61     sort(fac.begin(), fac.end());
62     return fac;
63 }
64 };

```

ex-gcd

```

1  template<typename T>
2  struct ex_gcd {
3      T gcd(const T a, const T b, T &x, T &y) { // x'=x_0+b/gcd, y'=y_0-a/gcd
4          if (b == 0) {x = 1, y = 0; return a; }
5          T d = gcd(b, a%b, x, y);
6          T t = x;
7          x = y;
8          y = t - a/b*y;
9          return d;
10     }
11     T inv(const T a, const T m) { // return -1 if inv is not exist
12         if (a == 0 || m <= 1) return -1;
13         T x, y, d = gcd(a, m, x, y);
14         if (d != 1) return -1;
15         return (x%m+m)%m;
16     }
17 };

```

crt

```
1 template<typename T>
2 struct crt {
3     ex_gcd<T> *exgcd = new ex_gcd<T>();
4     T cal(const T *a, const T *m, const int n) { // a[1..n], m[1..n], gcd(m_i) = 1
5         T M = 1, ans = 0;
6         for (int i = 1; i <= n; i++) M *= m[i];
7         for (int i = 1; i <= n; i++)
8             (ans += (__int128)a[i]*(M/m[i])%M*exgcd->inv(M/m[i], m[i])%M) %= M;
9         return ans;
10    }
11 } ;
```

ex-crt

```
1 template<typename T>
2 struct ex_crt {
3     ex_gcd<T> *exgcd = new ex_gcd<T>();
4     T cal(T *a, T *m, const int n) { // a[1..n], m[1..n], return -1 if no ans
5         T x, y, gcd, lcm;
6         for (int i = 2; i <= n; i++) {
7             gcd = exgcd->gcd(m[1], m[i], x, y);
8             if ((a[i]-a[1])%gcd) return -1;
9             lcm = (__int128)m[1]*m[i]/gcd;
10            x = (__int128)x*(a[i]-a[1])/gcd%lcm;
11            gcd = m[i]/gcd;
12            x = (x%gcd+gcd)%gcd;
13            a[1] = ((__int128)m[1]*x%lcm+a[1])%lcm, m[1] = lcm;
14        }
15        return a[1];
16    }
17 } ;
```

图论

LCA

- 倍增

```
1 void dfs(int u, int fa) {
2     pa[u][0] = fa; dep[u] = dep[fa] + 1;
3     FOR (i, 1, SP) pa[u][i] = pa[pa[u][i-1]][i-1];
4     for (int& v: G[u]) {
5         if (v == fa) continue;
6         dfs(v, u);
7     }
8 }
9
10
11 int lca(int u, int v) {
12     if (dep[u] < dep[v]) swap(u, v);
13     int t = dep[u] - dep[v];
14     FOR (i, 0, SP) if (t & (1 << i)) u = pa[u][i];
15     FORD (i, SP-1, -1) {
16         int uu = pa[u][i], vv = pa[v][i];
17         if (uu != vv) { u = uu; v = vv; }
18     }
19     return u == v ? u : pa[u][0];
20 }
```

计算几何

二维几何：点与向量

```
1 #define y1 yy1
2 #define nxt(i) ((i + 1) % s.size())
3 typedef double LD;
```

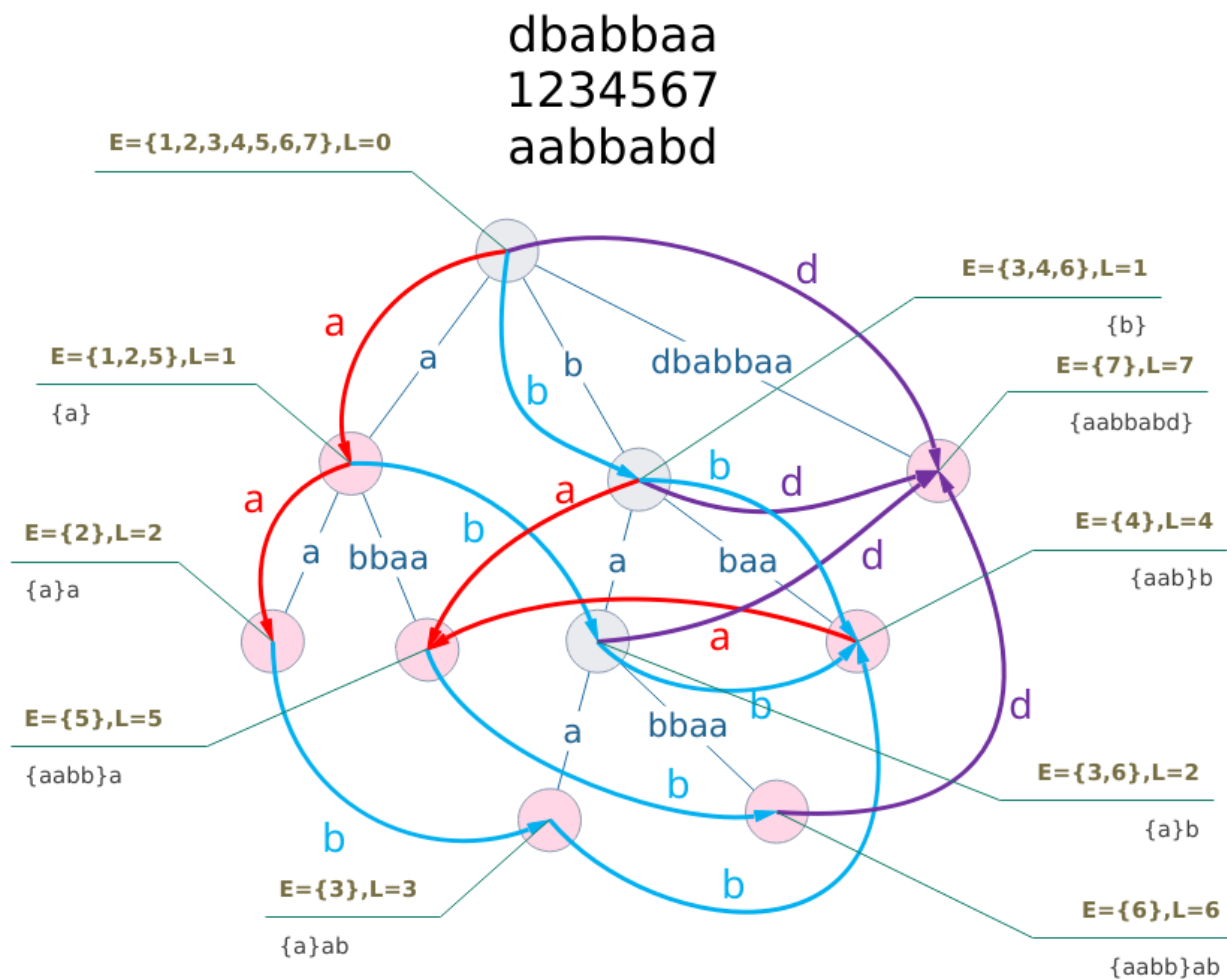
```

4  const LD PI = 3.14159265358979323846;
5  const LD eps = 1E-10;
6  int sgn(LD x) { return fabs(x) < eps ? 0 : (x > 0 ? 1 : -1); }
7  struct L;
8  struct P;
9  typedef P V;
10 struct P {
11     LD x, y;
12     explicit P(LD x = 0, LD y = 0): x(x), y(y) {}
13     explicit P(const L& l);
14 };
15 struct L {
16     P s, t;
17     L() {}
18     L(P s, P t): s(s), t(t) {}
19 };
20
21 P operator + (const P& a, const P& b) { return P(a.x + b.x, a.y + b.y); }
22 P operator - (const P& a, const P& b) { return P(a.x - b.x, a.y - b.y); }
23 P operator * (const P& a, LD k) { return P(a.x * k, a.y * k); }
24 P operator / (const P& a, LD k) { return P(a.x / k, a.y / k); }
25 inline bool operator < (const P& a, const P& b) {
26     return sgn(a.x - b.x) < 0 || (sgn(a.x - b.x) == 0 && sgn(a.y - b.y) < 0);
27 }
28 bool operator == (const P& a, const P& b) { return !sgn(a.x - b.x) && !sgn(a.y - b.y); }
29 P::P(const L& l) { *this = l.t - l.s; }
30 ostream &operator << (ostream &os, const P &p) {
31     return (os << "(" << p.x << "," << p.y << ")");
32 }
33 istream &operator >> (istream &is, P &p) {
34     return (is >> p.x >> p.y);
35 }
36
37 LD dist(const P& p) { return sqrt(p.x * p.x + p.y * p.y); }
38 LD dot(const V& a, const V& b) { return a.x * b.x + a.y * b.y; }
39 LD det(const V& a, const V& b) { return a.x * b.y - a.y * b.x; }
40 LD cross(const P& s, const P& t, const P& o = P()) { return det(s - o, t - o); }
41 // -----

```

字符串

后缀自动机



多项式

NTT 模数

```
1 NTTPrimes = {1053818881, 1051721729, 1045430273, 1012924417, 1007681537, 1004535809, 998244353, 985661441,  
  ↪ 976224257, 975175681};  
2 NTTPrimitiveRoots = {7, 6, 3, 5, 3, 3, 3, 3, 3, 17};
```

FFT

```
1 namespace FFT{  
2     const db pi=acos(-1);  
3     struct cp{  
4         db re,im;  
5         cp(db _re=0,db _im=0){re=_re;im=_im;}  
6         cp operator +(cp b){return cp(re+b.re,im+b.im);}  
7         cp operator -(cp b){return cp(re-b.re,im-b.im);}  
8         cp operator *(cp b){return cp(re*b.re-im*b.im,re*b.im+im*b.re);}  
9     };  
10    int r[N];cp c[N<<1];  
11    inline void fft(cp *a,int f,int n){  
12        rep(i,0,n-1) if(r[i]>i) swap(a[r[i]],a[i]);  
13        for(int i=1;i<n;i<=<1){
```

```

14         cp wn(cos(pi/i),f*sin(pi/i));
15         for(int j=0,p=(i<<1);j<n;j+=p){
16             cp w(1,0);
17             for(int k=0;k<i;++k,w=w*wn){
18                 cp x=a[j+k],y=w*a[j+k+i];
19                 a[j+k]=x+y;a[j+k+i]=x-y;
20             }
21         }
22     }
23     if(f==-1){rep(i,0,n-1) a[i].re/=n,a[i].im/=n;}
24 }
25 inline int mul(db *a,db *b,int n,int m){
26     n+=m;rep(i,0,n) c[i]=cp(a[i],b[i]);
27     int l=0;m=n;for(n=1;n<=m;n<=1) ++l;
28     rep(i,0,n-1) r[i]=(r[i>>1]>>1)|((i&1)<<(l-1));
29     rep(i,m+1,n) c[i]=cp(0,0);
30     fft(c,1,n);rep(i,0,n-1) c[i]=c[i]*c[i];
31     fft(c,-1,n);
32     rep(i,0,m) a[i]=c[i].im/2;
33     return n;
34 }
35 }

```

NTT

```

1 namespace NTT{
2     const int P=998244353,g=3,ig=332748118;
3     inline int qpow(int a,int b){int q=1;while(b){if(b&1)q=1LL*q*a%P;a=1LL*a*a%P;b>>=1;}return q;}
4     int r[N],ow[N],inv[N];
5     inline void ntt(int *a,int f,int n){
6         rep(i,0,n-1) if(r[i]>i) swap(a[i],a[r[i]]);
7         for(int i=1;i<n;i<=1){
8             int wn=qpow(f,(P-1)/(i<<1));
9             ow[0]=1;rep(k,1,i-1) ow[k]=1LL*ow[k-1]*wn%P;
10            for(int j=0,p=(i<<1);j<n;j+=p){
11                for(int k=0;k<i;++k){
12                    int x=a[j+k],y=1LL*ow[k]*a[j+k+i]%P;
13                    a[j+k]=(x+y)%P;a[j+k+i]=(x-P-y)%P;
14                }
15            }
16        }
17        if(f==ig){
18            int iv=qpow(n,P-2);
19            rep(i,0,n-1) a[i]=1LL*a[i]*iv%P;
20        }
21    }
22    int tma[N],tmb[N];
23    inline int mul(int *a,int *b,int n,int m,int ci){
24        int _n=n,_m=m,l=0;m+=n;for(n=1;n<=m;n<=1) ++l;
25        rep(i,0,n-1) r[i]=(r[i>>1]>>1)|((i&1)<<(l-1));
26        rep(i,0,n-1) tma[i]=a[i];rep(i,0,n-1) tmb[i]=b[i];
27        rep(i,_n+1,n) tma[i]=0;rep(i,_m+1,n) tmb[i]=0;
28        ntt(tma,g,n);ntt(tmb,g,n);
29        while(ci){
30            if(ci&1) rep(i,0,n-1) tma[i]=1LL*tma[i]*tmb[i]%P;
31            rep(i,0,n-1) tmb[i]=1LL*tmb[i]*tmb[i]%P;
32            ci>>=1;
33        }
34        ntt(tma,ig,n);
35        rep(i,0,n-1) a[i]=tma[i];
36        return n;
37    }
38 }
39 inline void prepare(){
40     //NTT inv
41     using NTT::inv;using NTT::P;
42     inv[1]=1;rep(i,2,N-1) inv[i]=1LL*(P-P/i)*inv[P%i]%P;
43 }

```