Hello World

#### 1 Delimiters

See how the delimiters are of reasonable size in these examples

$$(a+b)\left[1 - \frac{b}{a+b}\right] = a,$$

$$\sqrt{|xy|} \le \left|\frac{x+y}{2}\right|,$$

even when there is no matching delimiter

$$\int_a^b u \frac{d^2 v}{dx^2} dx = u \frac{dv}{dx} \bigg|_a^b - \int_a^b \frac{du}{dx} \frac{dv}{dx} dx.$$

## 2 Spacing

Differentials often need a bit of help with their spacing as in

$$\iint xy^2 \, dx \, dy = \frac{1}{6}x^2y^3,$$

whereas vector problems often lead to statements such as

$$u = \frac{-y}{x^2 + y^2}$$
,  $v = \frac{x}{x^2 + y^2}$ , and  $w = 0$ .

Occasionally one gets horrible line breaks when using a list in mathematics such as listing the first twelve primes 2, 3, 5, 7, 11, 13, 17, 19, 23. In such cases, perhaps include \mathcode'\,="213B inside the inline maths environment so that the list breaks: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37. Be discerning about when to do this as the spacing is different.

## 3 Arrays

Arrays of mathematics are typeset using one of the matrix environments as in

$$\begin{bmatrix} 1 & x & 0 \\ 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} 1 + xy \\ y - 1 \end{bmatrix}.$$

Case statements use cases:

$$|x| = \begin{cases} x, & \text{if } x \ge 0, \\ -x, & \text{if } x < 0. \end{cases}$$

Many arrays have lots of dots all over the place as in

# 4 Equation arrays

In the flow of a fluid film we may report

$$u_{\alpha} = \epsilon^2 \kappa_{xxx} \left( y - \frac{1}{2} y^2 \right), \tag{1}$$

$$v = \epsilon^3 \kappa_{xxx} y \,, \tag{2}$$

$$p = \epsilon \kappa_{xx} \,. \tag{3}$$

Alternatively, the curl of a vector field (u, v, w) may be written with only one equation number:

$$\omega_{1} = \frac{\partial w}{\partial y} - \frac{\partial v}{\partial z}, 
\omega_{2} = \frac{\partial u}{\partial z} - \frac{\partial w}{\partial x}, 
\omega_{3} = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}.$$
(4)

Whereas a derivation may look like

$$(p \wedge q) \vee (p \wedge \neg q) = p \wedge (q \vee \neg q)$$
 by distributive law  $= p \wedge T$  by excluded middle  $= p$  by identity

## 5 Functions

Observe that trigonometric and other elementary functions are typeset properly, even to the extent of providing a thin space if followed by a single letter argument:

$$\exp(i\theta) = \cos\theta + i\sin\theta$$
,  $\sinh(\log x) = \frac{1}{2}\left(x - \frac{1}{x}\right)$ .

With sub- and super-scripts placed properly on more complicated functions,

$$\lim_{q \to \infty} ||f(x)||_q = \max_x |f(x)|,$$

and large operators, such as integrals and

$$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}$$
 where  $n! = \prod_{i=1}^n i$ ,  
 $\overline{U_{\alpha}} = \bigcap_{\alpha} U_{\alpha}$ .

In inline mathematics the scripts are correctly placed to the side in order to conserve vertical space, as in  $1/(1-x) = \sum_{n=0}^{\infty} x^n$ .

#### 6 Accents

Mathematical accents are performed by a short command with one argument, such as

$$\tilde{f}(\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(x)e^{-i\omega x} dx$$

or

$$\dot{\vec{\omega}} = \vec{r} \times \vec{I} \, .$$

#### 7 Command definition

The Airy function, Ai(x), may be incorrectly defined as this integral

$$Ai(x) = \int \exp(s^3 + isx) ds.$$

This vector identity serves nicely to illustrate two of the new commands:

$$\boldsymbol{\nabla}\times\boldsymbol{q}=\boldsymbol{i}\left(\frac{\partial w}{\partial y}-\frac{\partial v}{\partial z}\right)+\boldsymbol{j}\left(\frac{\partial u}{\partial z}-\frac{\partial w}{\partial x}\right)+\boldsymbol{k}\left(\frac{\partial v}{\partial x}-\frac{\partial u}{\partial y}\right).$$

Recall that typesetting multi-line mathematics is an art normally too hard for computer recipes. Nonetheless, if you need to be automatically flexible about multi-line mathematics, and you do not mind some rough typesetting, then perhaps invoke \parbox to help as follows:

$$u_1 = -2\gamma\epsilon^2 s_2 + \mu\epsilon^3 \left(\frac{3}{8}s_2 + \frac{1}{8}s_1i\right) + \epsilon^3 \left(-\frac{81}{32}s_4s_2^2 - \frac{27}{16}s_4s_2s_1i + \frac{9}{32}s_4s_1^2 + \frac{27}{32}s_3s_2^2i - \frac{9}{16}s_3s_2s_1 - \frac{3}{32}s_3s_1^2i\right) + \int_a^b 1 - 2x + 3x^2 - 4x^3 dx$$

Also, sometimes use \parbox to typeset multiline entries in tables.

### 8 Theorems et al.

**Definition 1 (right-angled triangles)** A right-angled triangle is a triangle whose sides of length a, b and c, in some permutation of order, satisfies  $a^2 + b^2 = c^2$ .

Lemma 2 The triangle with sides of length 3, 4 and 5 is right-angled.

This lemma follows from the Definition 1 as  $3^2 + 4^2 = 9 + 16 = 25 = 5^2$ .

**Theorem 3 (Pythagorean triplets)** Triangles with sides of length  $a = p^2 - q^2$ , b = 2pq and  $c = p^2 + q^2$  are right-angled triangles.

Prove this Theorem 3 by the algebra  $a^2 + b^2 = (p^2 - q^2)^2 + (2pq)^2 = p^4 - 2p^2q^2 + q^4 + 4p^2q^2 = p^4 + 2p^2q^2 + q^4 = (p^2 + q^2)^2 = c^2$ .