Team Control Number

For	office use only
T1	
T2	
T3	
T4	

68	94	10
----	----	----

For	office use only	N
F1		<u>ii</u>
F2		▣
F3		_
F4		

Problem Chosen

2017 MCM/ICM Summary Sheet

(Your team's summary should be included as the first page of your electronic submission.)

Type a summary of your results on this page. Do not include the name of your school, advisor, or team members on this page.

Understanding the socioeconomic processes and tensions underlying population stability is imperative for establishing a population of humans on Mars. The objective of our team was to develop governmental and welfare policies that would allow for a population of 10,000 new residents on Mars to develop an egalitarian civilization that surpasses similar civilizations on Earth. To accomplish this goal, our team was tasked with building a model that evaluates the parameters related to income, education, and equality for the new population.

We developed an agent-based model that simulates a population of 10,000 agents on Mars using real world data given by the US Census' data on occupational income. In our model, each agent, or Martian citizen, progresses through their lifecycle by attending college, searching for jobs, and earning income. The government then protects these individual agents from economic harm using programs such as welfare and minimum wage. To maximize both social welfare and productivity, we chose to monitor the state of the economy and create metrics that would measure the effect of agent-based factors on the community's well-being. We measured multiple parameters of the community generated by these agents, which allowed us to evaluate the condition of the economy. From these parameters, we generated three metrics: the Income Metric I, the Education Metric E, and the Equality Metric Q. The income metric favors higher per capita income values on Mars and punishes a wage gap between the rich and the poor that is either too large or too small. The education metric measures the amount of unemployment as an economical factor and the student-to-faculty ratio as a social welfare factor so as to evaluate education through both the lens of productivity and well-being. Finally, the Equality Metric compares the proportion of women in occupations on Mars to their proportion in jobs on Earth to illustrate the dynamic social equality present in Population Zero. Additionally, our model includes several economic indicators and properties like the inflation rate, a progressive tax system, total investment, and government debt to add further to the dynamic equilibrium of the economy.

Using our model, we found that the best initial population had a mean age of 37 and a ratio of 1:10 of innovators to producers. Analysis of our metrics suggests that the Martian society can support more than 10,000 people in case of an emergency migration from Earth, assuming that infrastructure is present. We found that a minimum wage of \$70,000 provided the greatest benefit to society. As maternity and paternity leave lengths did not have a great impact on GDP, we determined that a maternity leave length of 10 months and a paternity leave length of 3 months. Government control of inflation proved to be critical to maintaining the purchasing power of the people. A progressive tax system served to increase income inequality while keeping investment high and government debt low, allowing the government to provide for increased education and infrastructure needs in the future. Most importantly, a happiness survey can be utilized to create a a strong, collaborative society working to reach common goals.

POLICY ADVISOR

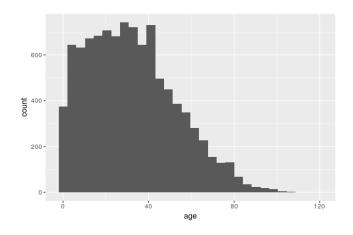
January 24, 2017

Dr. Isabelle C. Moss Director of LIFE Quai Gustave-Ador 1207 GenÃÍve, Switzerland

Dear Dr. Moss:

Thank you for working with us to design a plan to colonize Mars! We are excited to be a part of humanity's greatest advancement since the Moon Landing – UTOPIA: 2100. We have developed a model to address your concerns about the social and economic equality in UTOPIA: 2100. We aimed to produce policy measures that would maximize income equality, gender equality, and educational advancement in the society.

Considering the complexity of describing governmental policy for a society on an entirely new planet, we developed an intricate, agent-based model that suggested that the initial population should be composed of a 50:50 ratio of males: females to optimize the equality metric. We also determined that the occupations of each person should be chosen so that the proportion of people in each job (as defined by the Bureau of Labor Statistics) is conserved. We found that choosing a population with a mean age of 37, and which consisted of more teenagers and children than older people, resulted in high GDP values and optimized the education and income metrics (see image below). Selecting a population with a 10%proportion of innovators (those individuals with jobs in management and science who are more likely to invest in technological advancement) produced optimal unemployment rates. Other factors such as marital status and ethnicity are less influential on the overall development of the colony, so ensuring that these demographics are equally represented is adequate. The use of unskilled labor has become substantially lower when compared to the 21st century due to the rise of automation and innovations in the robotics industry. Therefore, we suggest that the government require and fund the two-year college education of all people, eliminating "unskilled labor" from UTOPIA: 2100. When we tested various population distributions, we noticed some oscillations in education demand. In particular, after a few years into the model, the demand for education slowly fell over time. However, as the new generation came into the college education system, a huge spike in the education demand occurred. To mitigate the effects of this influx, the Martian government should be prepared to provide funds during the sudden influx of students.



The first thing to be done in the new Martian civilization is social welfare. In order to correctly in ment this, the civilization's government must be able to provide universal healthcare, college tuition, social security, and welfare. We also tested various social benefits like minimum wage. According to our income metrics, a minimum wage value of \$70000 (adjusted for projected inflation in 2100) will provide the optimal benefit to society. On the other hand, maternity and paternity leave appear to have an insignificant economic effect. Setting these two lengths to 10 months and 3 months respectively may help increase the happiness and well-being of our population.

The government is also responsible for the social and economic well-being of all citizens of UTOPIA: 2100. As a result, the central banking institution must ensure that inflation rates stay below income growth rates to prevent loss of purchasing power and keep investment levels high. We propose a progressive tax system to help fund government spending while reducing income inequalities. The tax rate should be maintained so that the government is not earning large sums of money and so that the people are not losing much of their hard-earned income due to the government. Strict non-discriminatory policies should be implemented in the job sector to increase gender equality; people should not be denied jobs due to their gender, race, and other characteristics.

An extremely efficient and reliable method to measure the progress of UTOPIA: 2100 is the happiness index, which can be measured by implementing a survey in which citizens report their satisfaction about governmental policies (such as maternity/paternity leave length, unemployment, and inflation). By increasing the overall happiness of the people through this survey, the government can gain the people's trust, and form a strong, collaborative society working to reach common goals.

By following these policies, we hope to achieve the following:

- The development of a large middle class that composes the vast majority of the population. We also hope to minimize the number of minimum wage workers and have only a small number of extremely wealthy people.
- The unemployment rate is stable and low, and our education systems can adequately accommodate and teach the population. We hope to eventually have government subsidisation of 4-year college educations for all students.
- There is an equal proportion of women to men in each job field.

With these policies in place, the government need only develop physical infrastructure (living quarters, food production facilities, etc.) as population size grows. Given the initial population size and characteristics, keeping up with the population growth should not be difficult.

In the event of a disaster on Earth resulting in a need for large scale migrations, the government on Mars needs to improve its physical infrastructure to accommodate the large influx of immigrants. However, none of the policies need to be altered substantially.

We thank you for your cooperation in this grand endeavor and we wish the best for UTOPIA: 2100.

Sincerely,

Mathher

Matthew C. McConaughey

Senior Policy Advisor Mathematical Analyst

LABORATORY OF INTERSTELLAR, FINANCIAL, AND EXPLORATION POLICY

E: mcconaughey@icm.gov

M: (555)555-5555



Introduction

Houston, we have a problem! The Laboratory of Interstellar, Financial, and Exploration Policy (LIFE) has conducted multiple studies, designed the infrastructure, and conducted scientific experiments to allow for the first human population to live on Mars. This first population, called Population Zero, will include 10,000 people. The mission of Population Zero is to create a sustainable society by maximizing both economic output and happiness in the workplace for its citizens.

This project, termed UTOPIA: 2100, outlines the goal of creating an optimal workforce for the 22nd century to give all people the greatest quality of life with a vision of sustainability for the next 100 years on Mars. This martian community will be driven by egalitarian principles in economics, government, workforce, and justice systems.

In the process of developing an economic-workforce-education system for Population Zero, LIFE has tasked our group of mathematical modelers and policy advisors to develop a set of policies to facilitate the migration to Mars. The goal of our team is to consider income, education, and equality as they relate to the goals of Population Zero and provide policy recommendations that will accommodate such interplanetary community projects.

Restatement of Problem

Our group is tasked with developing policy recommendations that will allow Population Zero to maximize both economic output and happiness in the workplace for their citizens. The vision of the UTOPIA: 2100 project is to produce a sustainable population on Mars. The International Coalition on Mars (ICM) has provided directives for our group to develop these recommendations.

Parametrization of Factors

We are tasked with defining parameters related to income, education, and social equality for Population Zero. This involves the consideration of workforce demographics, educational demographics, governmental infrastructure that facilitates these parameters, and policies that will ensure that such parameters are maximized.

In completing this directive, we are asked to identify specific outcomes that would indicate positive outcomes for these three factors for the next decade. We are also asked to suggest possible demographics of Population Zero that would lead to positive results. Furthermore, metrics are to be created that can measure these parameters.

Sample Population

We are tasked with synthesizing a sample population of 10,000 that would ensure the goals of UTOPIA: 2100. In doing so, we must consider the demographics of age, sex, and education. Furthermore, this population must be capable of facilitating the goals of UTOPIA: 2100.

Model

Finally, we are tasked with building a model that can describe the population dynamics for the next ten years. In doing so, we must determine the salary distribution that will balance productivity and

well being. We are also asked to characterize innovations that could improve our model. In add we conduct sensitivity analysis for a 100-year plan and consider emergency evacuation migrapatterns from Earth to Mars.

Definitions and Assumptions

Since it is challenging to predict all variables and factors that may affect our model, we made certain assumptions to produce a working model.

- Every Martian goes to college to obtain at least an Associate's Degree.
 - Due to the high level of technical skills required to survive the new life on Mars as well as the predicted high demand for education in the 22nd century[1], we mandate that all citizens become well-educated.
- Education Diplomas are issued at 2-, 4-, 6-, and 8-year intervals.
 - We assume every college student follows the traditional pattern of Associate's in 2 years, Bachelor's in 4 years, Master's in 6 years, and Ph. D in 8 years. Other degree options that require more than 8 years are not covered in our model.
- Every individual is actively pursuing a job given that they are of working age and are not a permanent stay-at-home mom or dad.
 - In our model, pursuing a job and becoming a productive citizen is more important than holding degrees that require higher levels of education. In an egalitarian society, the social welfare of the Martian citizens should not depend on the education to which they are privy.
- Members of the population on Mars will retire at the age of 70, and their life expectancy will be 100 years.
 - According to the UN Population Bureau, the life expectancy in the 22nd century will be 100[2]. In addition, from historical charts [3], it can be seen that average retirement age has increased from 57 in 1991 to 60 in 2012. This is roughly an increase of 1 year in retirement per 7 years passed. Extrapolated to the year 2100, a retirement age of 70 is a reasonable estimate.
- Race, ethnicity, or religion have no impact on a population's ability to progress on Mars.
 - The cultural values borne from race, ethnicity, and religion are difficult to quantify or express in a model.
- Incomes, the number of workers in each occupation, and general prices will increase at the same annual rate as they currently do.
 - Using the same annual rate of increase is a reasonable way to extrapolate $22^{\rm nd}$ century incomes, prices, and job occupations from current ones.
- The necessary infrastructure (ex. homes and other essentials) is already present on Mars before Population Zero.
 - It is reasonable to assume that LIFE has already built infrastructure to support Population Zero.
- The familial relationships between individuals agents are not considered
 - Representing familial units in an agent-based model requires an underlying network. Such a network is computationally intensive and difficult to evaluate over 10,000 nodes.
- The time of death is not contingent upon the events that take place in your life.
 - Our model does not take into account the hard-to-quantify relationships between income and occupation on health.

本资料由迈思数模整理www.maisums.com



- Other than maternity and paternity leave, our model does not consider any other forms of
 - It is challenging to quantify events in the life of an agent in our model that would result
 in unpaid leave.

Analysis of Problem

The two important themes in this problem are the maximization of social welfare and productivity. The new society in Mars is based upon egalitarian principles and must be able to provide for the well being of its citizens whilst producing an unparalleled economy.

Since we are creating an entirely independent and self-sustaining civilization, we can incorporate several desirable characteristics that may or may not be present on Earth. The first such characteristic for our Martian civilization is personal initiative: every individual should be motivated to increase the well-being of his or her self. This motivation usually comes in the form of higher wages for the individual. Although a simple concept, the lack of personal initiative was a main contributor to the downfall of Communism [4]. Rather than reducing the behavior of members of the population to a set of variables, it is important to maintain the characteristics of each individual agent so as to account for this personal initiative in our model.

The second essential characteristic of our advanced civilization is social welfare. In particular, the Martian government should be able to provide funds to accommodate health care, college education, maternity/paternity leave, and other socially useful public goods. Having this would allow our Martian civilization to potentially surpass the United States in social welfare programs.

Our plan to approach this problem is to develop an agent-based model, where agents represent Population Zero on Mars. Although we considered models based on differential mathematics, traditional differential equation models do not account for personal initiative. Furthermore, such systems often overlook complex interactions that occur due to the behavior of discreet agents rather than continuous variables. Therefore, we chose to use an agent-based model, as it accurately represents a person's impact on society as well as the interactions between and within citizens. To characterize our civilization, we created the model in NetLogo.

Model Design and Justification

To better understand the mechanics and interactions in the system, we will describe our model by analyzing the life of Bob, a person born on Mars.

Our model categorizes people into 4 lifestages (0, 1, 2, 3, and 4) based on their age and occupation. When Bob is born, his lifestage is 0. Once Bob becomes 5 years old, he starts attending primary school, and his lifestage is set to 1. Bob continues through his education until he graduates high school. Bob receives an Associate's degree because college education is paid for and required by the government.

After getting his Associate's degree, Bob looks for a job. However, he can only search for jobs which have an education requirement of 2 years or less. If Bob finds such a job on his first try, he takes it; otherwise, he can either continue to search for a job (and is classified as unemployed) with a

probability p_2 or go back to school with a probability $(1-p_2)$. If he goes back to school, he conthis education and obtains a Bachelor's degree. Once again, he searches for a job, but this time, and search for jobs which have an education requirement of 4 years or less. If Bob does not get a job and goes back to school (now with a probability $(1-p_4)$), he gets his Master's degree and searches for a job again (this time searching through jobs with an education requirement of 6 years or less). If he still does not get a job and goes back to school once more (with probability $(1-p_6)$), he obtains a Ph.D. Then, he leaves college with probability $p_8 = 1$ and continues to search for a job (with any education requirement) until he finds one.

If Bob has a Bachelor's, Master's, or a Doctorate, there is a chance that he will get a job with a lower education requirement than his educational attainment. For example, let us assume that Bob has a Master's degree and is searching for a job. Although there are no available positions for jobs with an educational requirement of 6 or 4 years, there is an availability for a job with an educational requirement of 2 years. Bob then takes this job, and is classified as underemployed since he is "overqualified" for his job.

People who are underemployed continue to search for jobs while they work. In this case, Bob will see if there are any job availabilities with education requirements of 4 or 6 years. If he finds one, he will quit his current job and take the new job. If he finds more than one job with different educational requirements (both higher than that of his current job), he will take the job with the highest educational requirement that he satisfies. Once Bob has a job whose educational requirement matches his level of education, he is no longer classified as underemployed.

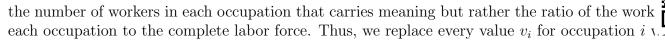
The Census Data

To determine the set of available jobs at every step in our model, we need data that indicates the likely distribution of jobs that will be available on Mars. To do this, we use the United States Bureau of Labor Statistics' (BLS) data from 2011 to 2015. The BLS categorizes the set of all occupations in the US into 22 primary categories. Each category contains the number of people in that category, mean income, median income, percentile 10 income, percentile 25 income, percentile 75 income, and percentile 90 income¹. To extrapolate the data for the year 2100 for each individual occupation, we perform an exponential fit with the 5 years of available data to determine the annual growth rate of both income and number of workers. Given these growth rates, we scale current US employment and income values to that of 2100 US.

The last thing we need for each occupation type is the minimum education necessary for that occupation. The BLS does not provide each of the 22 occupations with a minimum education level. Instead, we referenced independent sources to determine these values. Our calculations can be are summarized in Table 1 and Table 2 in the Appendix.

At every tick in the model, an "Income File" and "Job Distribution" are evaluated. The "Income File" contains data about the mean income and percentile incomes for agents in the model, whilst the "Job Distribution" contains the distributions of jobs in the model. Both variables initially start at the extrapolated values for 2100 but grow dynamically with time (using the same annual growth rates). However, since the population of Mars is not the same as the population of the US, it is not

 $^{^{1}}$ Two data points were given a value of # on the data-set since they were over 187200. We replaced them with 187200.



$$\frac{v_i}{\sum_i v_i}$$

to obtain the fraction of total jobs that are of occupation i. To calculate the number of actual jobs on Mars, we need to multiply by the size of the job market (i.e. the number of people demanding jobs). This is equal to the number of people working, the number of unemployed individuals, and the subset of students in college that are actively requesting jobs at the time. However, in the real world, job creation and job elimination are not instantaneous: there is some inflexibility in changing the number of jobs. To account for this, the set of available jobs is reset according to the size of the job market once a year instead of once a tick. Note that in our model, ticks are evaluated 6 times per year.

To determine the income for each person who is hired, each worker is given a "percentile." If this percentile is 10, then that worker receives the percentile 10 income from our job ratios. If the percentile is 25, then that worker receives the percentile 25 income. If a worker is given a percentile between 10 and 25, then that worker receives a weighted average of the known values of the percentile 10 and percentile 25 incomes. In other words, if the worker is given a percentile of x, then his or her income is

$$(25-x) \times (\text{percentile } 10) + (x-10) \times (\text{percentile } 25)$$

If a worker's percentile is below 10, he or she receives minimum-wage (which will be described in detail later). If a worker's percentile is above 90, we cannot interpolate due to a lack of data, and therefore set it to be the percentile 90 income. Of course, there must also be room for growth for the worker's income. To account for this growth, the worker's income increases by some fixed amount given by his or her job's growth rate every year.

When a worker receives a job, he or she is randomly assigned a percentile from 10 to 50 as a starting salary. When Population Zero arrives on Mars, their salary begins at the percentile appropriate for their age and education, given that they started fresh out of college. When calculating the percentile growth rate, we wanted employees to grow by at least 20 percentiles in their tenure. We found the median tenure to be 4.3 years[42], so we set the percentile growth rate to $\frac{20}{4.3} = 4.65$.

There is a 2% chance that a given worker will lose his job every year [43]. If a worker loses his job, he will look for a new one in the job market and will remain unemployed until he finds one.

There is also a probability that a worker will quit his/her job and become a stay-at-home parent. In this case, the worker is removed from the labor force and his/her lifestage is set to 4, though they do not receive social security until they reach 70 years of age. The probability that a worker becomes a stay-at-home parent depends upon his/her gender and is inversely proportional to his/her level of education [50, 51, 52].

Level of Education	Male	Female
Associate	0.07	0.25
Bachelor	0.03	0.19
Master	0.02	0.09
Ph. D	0.01	0.06



The probabilities p_2 , p_4 , p_6 , and p_8 are set using the 2015 US Census Bureau data on Educat Attainment: [28]:

Associate	Bachelor	Master	Ph. D
22537	46515	18683	6987

To illustrate this, consider p_4 . It is defined to be the number of people who leave college with a Bachelor's degree over the number people who leave college with a Bachelor's degree or higher. Thus

$$p_4 = \frac{46515}{46515 + 18683 + 6987} = 0.49$$

Birth and Death

Now, let us consider another agent in our model, Alice. Alice is approximately 26 years old, has a job, and is married to Bob². As Alice is a female between the ages of 18 and 50, there is a chance that she will have a child. This probability p_{baby} is given as a function of age (a) and the number of babies previously conceived (b). The probability is inversely proportional to the number of babies previously conceived since one is less likely to give birth if one already has a lot of children. The probability peaks at 26 years of age (as shown by [38]) and is lower at the boundaries of 18 and 50 years of age. Thus:

$$p_{\text{baby}} = k \times \frac{\left(\frac{\frac{1}{6}a - 3}{(\frac{1}{6}a - 4)^2 + 1}\right)}{b + 1}$$

Notice that this metric is proportional to a constant k. To simulate the world birth rate of 2.4 [39], we use the constant $k = 0.265^3$ (as determined by trial-and-error). If Alice is going to have a child, a timer starts for her. Once that timer reaches 9 months, the baby is born. After the baby is born, Alice cannot have a child for at least another 15 months.

When Alice's baby timer reaches 7 months, she goes on maternity leave (if she has a job). The maternity leave's length is varied during model testing to determine its effect on different metrics discussed later. Wages that Alice receives during her maternity leave are not counted in any of the income metrics as these are transfer payments subsidized by the government. When Alice's maternity leave ends, Bob's paternity leave begins. The paternity leave length is also varied.⁴

Let us once again consider Bob, who is now 70 years old. Bob now retires and begins receiving Social Security from the government. Bob's lifestage is set to 4, and he continues to live in this manner for some time. When people are born, their lifespan is predetermined using a gamma distribution. The mean lifespan is 100 years, with a variation of 10 years. Once Bob's age equals his lifespan, he

²Note that there are no family structures built into the model; we are assuming one here for the sake of explanation ³When Population Zero is initialized on the model, this constant is incremented to its final value over 20 years to prevent large baby booms - this also simulates the fact that people would not immediately reproduce at high rates once on Mars.

⁴In the actual model, when Alice's maternity leave ends, the paternity leave of a random, working male who is not already on leave will begin.



dies. This is the life cycle of a person living in our model of UTOPIA: 2100.

To illustrate the life cycle, we provide the following flowchart.

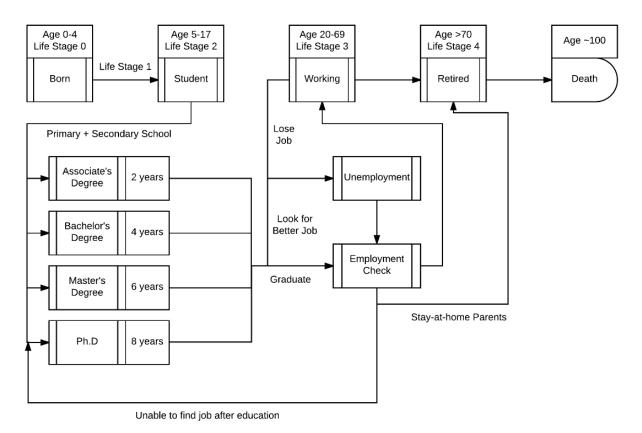
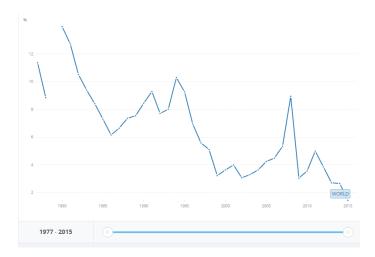


Figure 1: A Flowchart illustrating the life of individual agents in the model.

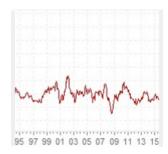
Global Inflation

As we begin to consider monetary costs and the bureaucracy, it is important to consider the global inflation that occurs between today and the 22^{nd} century. US inflation from 1923 to 2012 is illustrated below [37]:





tion for the remainder of the 21st century. To avoid this pitfall, we consider Canada's inflation From the following figure, we see that Canada has a very stable inflation rate [40]:



As Canada tends to favor economic stability over rapid economic growth, we will model our economy after Canada's economy, since our goal is to maximize both productivity and social welfare. Current Canadian inflation is around 1.3% [41], so this will be the world inflation rate used to convert from the $21^{\rm st}$ century to $22^{\rm nd}$ century monetary values.

Economic Indicators & Essentials

The goal of Population Zero is to create a society that far exceeds the economic strength of similar societies on Earth, yet achieves a societal equilibrium across income, equality in workspace, and education. As such, it is important to monitor the condition of the economy induced by our agent-based model. We calculate various economic indicators that allow us to track the development and progress of UTOPIA: 2100.

Taxes

To preserve income equality, we have implemented a progressive tax system with 5 tax brackets. All taxes are deducted from each consumer's income. These taxes primarily represent income tax rates, but can be adjusted to include sales tax, property tax, etc. The tax rate for each bracket is a fraction of the "overall tax rate" (OTR), which is varied during model testing. We can vary the tax rate to determine the effect on GDP, government debt, and our income metric. The following are the tax brackets and their corresponding rates:

Tax Bracket	Tax Rate
≤ Minimum Wage	0%
$Minimum Wage - \left(\frac{Minimum Wage + Income Mean}{2}\right)$	OTR 6
$(\frac{\text{Minimum Wage} + \text{Income Mean}}{2})$ – Income Mean	OTR 5
Income Mean – 75 th Income Percentile	$\frac{\text{OTR}}{4}$
75 th Income Percentile – 90 th Income Percentile	$\frac{\text{OTR}}{3}$
$\geq 90^{\rm th}$ Income Percentile	$\frac{\text{OTR}}{2}$

Government Spending and Debt

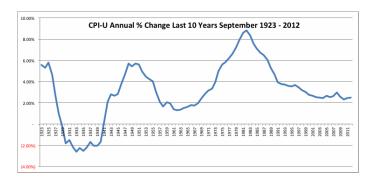
In order to be an idyllic civilization, the government must pay for public goods that benefit society. As stated earlier, the government must pay for the college education of all students, social security, welfare, infrastructure, and health care. The amount of funds spent on each of these was calculated using ratios from the U.S. government with the exception of health care, which was calculated from

Canada. The values are \$42,155 per student per year (education) [31], \$168,281,905 per 10,000 p per year (health care) [32], \$158,625,722 per 10,000 people per year (infrastructure) [30], \$59,00 per year (welfare) [34], and \$45,000 per person over 70 per year (social security) [33].

Government debt is the accumulated value of the budget deficit over time. The deficit is calculated by the total money collected through annual taxes minus the total annual government spending.

Inflation

To model inflation rates in our society, we consider the following graph [53]:



This graph is approximately sinusoidal. Though there are deviations, we can reasonably assume that inflation tends to follow a sinusoidal pattern.

The inflation over time (in our model) is given as a function of two sinusoids. This function models the cyclic nature of inflation while also accounting for yearly fluctuations. The fluctuations in inflation that occur over long periods of time tend to coincide with the business cycle, and are represented with a larger change in amplitude. Consequently, brief variation in inflation, represented by the amplitude of the sinusoid with an annual period, is relatively small.

Inflation(t) =
$$0.0025 \sin\left(\frac{2\pi t}{20}\right) + 0.008 - 0.0005 \cos(2\pi t)$$

Inflation directly affects our model by reigning back income growth. In particular, our model divides every person's salary by the combined effect of inflation to obtain its "real value". Minimum-wage, welfare, and social security are unaffected by this since the government is presumed to update these values to keep up with inflation.

Unemployment

The unemployment rate is given by the following function:

$$Unemployment = \frac{Number of Workers}{Labor Force}$$

We can think of unemployment as a metric of how poorly the current education levels in the population match the actual set of available jobs. Therefore a high unemployment implies that the current education system is not working properly and requires intervention.

Marginal Propensity to Consume (MPC)

The MPC is a variable quantity in our model. It is set to 0.9 to mimic the MPC of the United Similar 2016 [29]. MPC controls the amount of consumer expenditures and the investment schedule as detailed later.

Consumer Expenditures

All consumers (people) spend an amount of money equal to welfare (as it is the bare minimum wage necessary to survive). In other words, if a consumer had 0 income, he or she will still spend the amount of dollars equal to welfare. For every dollar of income thereafter, a consumer spends MPC of that. Therefore in total, a consumer spends

Income
$$\times MPC$$
 + Welfare

Interest Rate

The interest rate is a value varied for testing purposes that determines the effectiveness of investment spending. The rate is constant since reserve banks do not generally change the rate. It is currently set to 0.75% [35].

Investment Spending

People invest money proportionally to the amount they save from their income (retired and college students do not invest). Investment spending is inversely proportional to inflation, as people would be less likely to invest in weaker money. Since a consumer saves (1 - MPC) for every dollar amount gained in income, and consumers are welfare in debt with 0 income, the total amount of savings is $(1 - \text{MPC})(\text{income} - \frac{\text{welfare}}{1 - \text{MPC}})$.

Investment =
$$\frac{(Income - \frac{Welfare}{1-MPC})(1 - MPC)}{1 + Inflation}$$

Investment spending leads to returns on investment for consumers.

Gross Domestic Product (GDP)

GDP is calculated as a sum of Consumer Expenditures, Government Spending, Investment Spending, and Net Exports. However, because we are aiming to create a self-sustaining society, we assume that there are no Net Exports. A steadily rising GDP indicates a growing yet stable economy.

Parametrization of Social Welfare and Productivity

Income Metric

We design three metrics to measure the success of Population Zero in maximizing productivity and well being. The values of these three metrics are used to determine the success of Population Zero over a ten-year period. The income metric measures the population's propensity to facilitate a productive economy whilst punishing a wage gap that may be detrimental to the happiness and social welfare of the population. In general, the mean income of Population Zero should rise faster than inflation so as to maintain a stable economy. Furthermore, an increasing mean income also facilitates a wealthier economy, and therefore a productive society. However, it is often the case that only a certain section of the population is capable of increasing their income, whilst others are constrained by societal factors. To punish such a gap between the rich and the poor, our income metric I is the multiplicative combination of a component μ_I that accounts for increase in mean income and a component σ_I that



accounts for wage gap.

$$I = \mu_I \cdot \sigma_I$$

The mean μ_I is simply the ratio of the total income and the working population⁵. In our model, the working population is assigned a lifestage of 3.

$$\mu_I = \frac{\text{Total income of workers not on leave}}{\text{Number of people at lifestage 3}}$$

The component σ_I is designed to punish a wage gap that is either too small or too large. A small wage gap would necessitate the redistribution of wealth by the government and would slow down the productivity of the economy due to a lack of capital and incentive to innovate. However, a large wage gap is likely to be detrimental to the social welfare and result in an ever-decreasing middle class. Thus, the following function was devised to punish both large and small wage gaps. A larger value of I suggests a stronger income distribution in Population Zero.

$$\sigma_I = \frac{\sigma}{(\sigma)^2 + 0.55}$$

where $\sigma = \text{Standard Deviation}$ (Total income of workers not on leave)/Income Mean

This graph quickly rises from (0,0) to form a peak then slowly converges to zero. To determine the value of the constant (0.55), we found that the Gini Coefficient of a well developed country was approximately 0.4 [55]. Using the fact that incomes tend to form a log-normal distribution, we were able to use the conversion $G = \text{erf}\left(\frac{\sigma}{2}\right)$ [56], which implies that $\sigma = 0.74$. We then solved for the constant that would make the variance function peak at $\sigma = 0.74$, which evaluated to be 0.55.

As was mentioned previously, the standard metric for evaluating income inequality is the Gini Coefficient, which is defined as [54].

$$G = \frac{\sum_{i=1}^{n} \sum_{j=1}^{n} |x_i - x_j|}{2n \sum_{i=1}^{n} x_i}$$

The Gini Coefficient essentially calculates the difference in income between every pair of people, and normalizes it by the number of people, which is the most comprehensive method of analyzing income inequality. However, calculating the Gini Coefficient at every step of our model would be extremely computationally intensive $(O(n^2)$, since n^2 pairs exist). We therefore developed the Income Metric I as a computational alternative.

The per capita income of the United States was reported to be \$36,257 [45] in the year 2015. Adjusting for inflation, this per capita income is around \$176,769. The estimated value of the sigma component σ_I is less than 0.5 [44]. Thus, the income metric for the United States in the year 2095 is I = 88384. Comparatively, the goal for Population Zero is to achieve an income metric of at least I > 150000.

Education Metric

The education metric E measures the quality of education provided on Mars for Population Zero. goal of the university system is two-fold: to increase the productivity of the community by educating the public and to provide the social benefit of a proper, well-proportioned, and involved education. To measure the effect of education on the economy directly, we consider the unemployment rate as an indicator of education/job mismatch, as this relates directly to the number of students that graduate and are able to find jobs. To account for the quality of education provided to students, we multiply the unemployment rate with the student-to-faculty ratio across our university system to include a measure of education quality in the classroom. However in this student-to-faculty ratio, we consider the total number of years of education of all faculty members instead of strictly the number of faculty. Note that a smaller value of E indicates a better education system.

$$E = \text{Unemployment} \times \frac{\text{Number of Students}}{\sum_{\text{faculty}} \text{Years of Education}}$$

The number of students paid for by the government in the United States in 2010 was estimated to be 47,929,619 [46]. The total number of high school teachers has been estimated to be 3,385,000 [47] with every teacher having on average 4.58 years of education[48]. The unemployment rate in 2010 was 9.6% [49]. Thus, the value of the unemployment metric in 2010 was E = 0.0297. Comparatively, the goal for Population Zero is to achieve an education metric of at most E < 0.03.

Equality Metric

The equality metric Q measures the difference between the proportion of women in each job on Mars and Earth. One of the goals of UTOPIA: 2100 is to ensure that women are accurately represented in each job sector. Equality paves a path for productivity and social welfare. It stabilizes the playing field for both sexes and normalizes the experience in the workforce, resulting in a higher productivity. Furthermore, equality in the workplace is important for the social well-being of men and women alike, since diversity breeds open mindedness, acceptance, and empathy. To measure equality, we use the following formula:

$$Q = \frac{1}{\text{Labor Force}} \sum_{j \in \text{jobs}} c_j \cdot W_j$$

 c_i = Weight representing underrepresentation of women in that job type.

$$= \left(\frac{\text{\# of women in job type on Earth}}{\text{total \# of people in job type on Earth}} - \frac{\text{\# of women in job type on Mars}}{\text{total \# of people in job type on Mars}}\right)^2$$

 W_i = Number of women in job type, including those on maternity or paternity leave

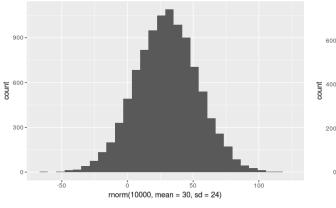
Due to the construction of this metric, Mars will always be compared to the ratios that are present on Earth. Therefore, the value of Q on Earth is always equal to 0. The goal of Population Zero is to achieve an equality metric Q > 3.5.

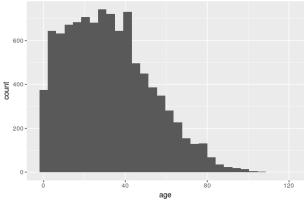
All three of our metrics are interconnected through the economic indicators. Unemployment is the key factor that impacts all three metrics. As unemployment rises, more people are living on welfare,

and our income metric decreases. Similarly, our education metric increases (which is a negindicator) as it is proportional to unemployment. Our equality metric is imbalanced by a run unemployment as firing more workers could result in an imbalance in the male-female worker ratio of a women-heavy occupation. Note that all metrics are evaluated every two months in our model.

Characteristics of Population Zero

We synthesized a sample population of 10,000 people for this model. We consider only the sex, age, and occupation of each agent. In our model, the education level associated with each occupation is pre-determined. Therefore, the occupation assigned to each person speaks to the level of education that each agent possesses. A random sampling of sex with equal probability resulted in 4954 females and 5046 males. The age of all people was determined from a normal distribution centered at $\mu = 30$ years of age and a standard deviation of $\sigma = 24$, as seen in Figure 2a. The absolute value of this distribution was taken so as to remove any negative values of age and to increase the number of teenagers and children sent to Mars. This age distribution is illustrated in Figure 2b and is designed in such a manner so as to closely resemble the age distribution of developed countries [5]. This synthesized age distribution has a mean of $\mu = 36.7$ years of age. The occupations of the people were determined by a weighted sampling, using proportions that were extrapolated from the Bureau of Labor Statistics.





(a) The initial age distribution

(b) The age distribution of Population Zero

Of the 22 major occupations, we characterized three as occupations involving innovators and the rest as occupations involving producers. These innovative occupations were (1) Management Occupations, (2) Computer and Mathematical Occupations, and (3) Life, Physical, and Social Science Occupations. A total of 1421 innovators are thus present in Population Zero. On a societal level, the function of innovators is to generate capital by investing money and creating jobs for other members of society⁶. Thus, innovators are important for maintaining the welfare of an egalitarian society. However, innovators can also increase the disparity between the rich and the poor. Our initial data set for Population Zero maintained a 1:10 ratio of innovators to producers to maximize both welfare and income equality. However, sensitivity analysis with multiple types of occupation distributions was conducted to understand the impact of innovators and producers on the Martian society.

The use of unskilled labor is hypothesized to become substantially lower when compared to the 20th century due to the rise of automation and innovations in the robotics industry. In fact, we ran

⁶Innovators invest 50% more than the typical citizen; See Appendix for further details

our model with a government that pays for and supports the education of all members up to years of college, thus producing a highly educated set of skilled citizens that can work alongside automation to become more productive rather than compete with the automation and hinder the already challenging task of living on Mars.

In Population Zero, it becomes unnecessary to consider the distribution of families vs. single people, as the likelihood of people reproducing right after they land on Mars is relatively low.

Results

Optimal Salary and Minimum Wage Distribution

In our model, the amount of welfare that was provided to unemployed peoples was calculated using the minimum amount of money required to live in an average city in the United States and adjusting for inflation in 2095 [34]. Minimum-wage, on the other hand, is a value set by the Martian government. If minimum wage is too low, the GDP significantly decreased, along with consumer expenditures. Furthermore the mean income will likely decrease, causing the income-metric to decrease. Also if the minimum wage is too close in amount to welfare, the members of the population would not have any incentive to work. On the other hand, when minimum wage is too high, they may be too little variation among the population, decreasing the potential of "personal initiative" and decreasing the income-metric.

Minimum Wage	Income Metric	GDP
65000	181056	2431800000
70000	183379	2443000000
75000	182186	2445000000
80000	182909	2448000000

In the table above, we see a definite positive correlation between minimum wage and GDP (as expected). An increase of roughly 5000 in minimum wage leads to an increase of about 11 million initially from 65000 to 70000, followed by increases of 2 million for the rest. On the other hand, the income wage can be seen to hit a peak at a minimum wage amount of 70000 dollars. Given the high income metric and the large increase in GDP, a minimum wage of \$70,000 is logically the best value to consider.

Contribution of New Ideas

As our technology advances, more "unskilled" jobs can be given to robots or other forms of automated devices. As the government requires and funds the 2-year college education of all people, workers would be unlikely to be without a job due to machines replacing them. As technology advances even more and we are able to increase our GDP, the government can begin to fund the 4-year college education of all people, leading to a more skilled and efficient workforce. The increase in GDP and productivity due to the higher skill level of the workers would also serve as an incentive for government to subsidize college education.

A key measure of the success of UTOPIA: 2100 is the happiness index. While it is largely subjective (and thus cannot be accurately measured in the quantitative model), implementing such a measure

would allow the government to increase the overall happiness of the society. The government calculate the happiness index through a survey, consisting of questions similar to those found http://www.grossnationalhappiness.com/Questionnaire/Questionnaire2014.pdf. Questions would include satisfaction about maternity/paternity leave, educational opportunities, and general stress levels. By increasing the overall happiness of the people, the government can gain the people's trust, and form a strong, collaborative society working to reach common goals.

Maternity and Paternity Leave

Maternity and Paternity leave lengths present a curious set of pros and cons to the economy. While the people on maternity and paternity leave do receive income, they are much less active in the economy, and therefore contribute less to the overall GDP as their incomes are essentially considered transfer payments. Furthermore, the incomes of the people on leave are not counted in the overall income metric, as doing so would represent an inaccurate productivity of the population. By implementing the happiness index survey, the government can easily calculate a leave length that maximizes the income metric while keeping happiness high.

By changing the maternity/paternity leave lengths on the model, we found that⁷

Maternity Leave - 10 Months		Paternity Leave - 3 Months	
Paternity Leave	Income Metric	Maternity Leave	Income Metric
1 Month	181415.918	2 Months	184061.442
2 Months	182953.169	4 Months	182521.232
3 Months	182705.453	6 Months	182033.492
4 Months	181697.193	8 Months	182696.682
5 Months	182111.493	10 Months	182705.453
6 Months	182256.076	12 Months	184019.439
7 Months	183022.395	14 Months	182867.229
8 Months	181720.176	16 Months	183826.363
9 Months	182812.225	18 Months	183220.033
10 Months	182756.155	20 Months	182181.098

In the table above, we see that the relationship between maternity/paternity leave and the incomemetric is heavily arbitrary: a maternity leave of 2 and 12 months return almost the same incomemetric. Therefore we can conclude that the cost associated with increasing maternity and paternity leave is insignificant compared to the value gained by increases in the happiness index.

The Subgroups of the Workforce

We have implemented a progressive taxation system in which the workforce is divided into several tax-brackets as defined in our model design. The people in the higher tax-brackets more strongly prefer lower tax rates. This is reflected by the income metric, which increases as tax rate is decreased.

 $^{^{7}}$ Paternity Leave was set relative to a Maternity Leave of 10 months, Maternity Leave was set relative to a Paternity Leave of 3 months



However, lower tax rates also create an immense increase in government debt. This relations described as follows:

Tax Rate	Income Metric	Government Debt
30	202442	2435615966
35	200593	2203859518
40	198452	1991658290
45	193952	1772320817
50	192268	1575884465
55	189427	1389024511
60	186683	1186607709
65	184507	1016978870
70	180049	871943235
75	177063	711551404
80	174896	538459074
85	171446	401100465
90	168890	282366320

We also subdivided our workforce into innovators and non-innovators, with innovators investing approximately 1.5 times as much as non-innovators. As the tax-rate increases, the investment of these innovators decreases significantly. However, this investment is essential if our civilization is to grow and develop in the long-term. The relationship between tax-rate and investment is as follows:

Tax Rate	Investment By Innovators
35	15275282
40	12381247
45	10046593
50	7301852
55	6418527
60	3215712

Note that investment is heavily elastic with tax-rate. Therefore we should strive to reduce the tax-rate whenever possible to ensure a high level of investment.

100-year

When we progress from a 10-year model to a 100 year model, it becomes necessary to consider other parameters. For example, inflation begins to play a crucial role in economic growth over 100 years. If inflation becomes higher than the growth rate of a given job's income, workers with that job will start to lose purchasing power. This results in much greater income disparity, evidenced by lower income metric values.

To counter the adverse effects of inflation on income growth, we implement a governmenta icy that keeps inflation at bay. Through the central banking institution (by buying securities), government can regulate inflation to ensure that most workers are not losing purchasing power. We implemented this in our model by setting the inflation rate to oscillate about a value that would not harm the vast majority of workers.

The other parameter that played an important role in the long-term model was the "baby-constant", a factor that helps determine the rate of population growth. If the baby-constant was set to be static over 100 years, there was a massive baby boom at the beginning. This wave of new babies then flooded the job market in another 20 years, causing unemployment to skyrocket. To prevent this calamity from occurring, we allowed the baby-constant to gradually increase to its final value over 20 years. This resulted in a much smaller wave of new babies and allowed the population to stabilize much more quickly while not raising unemployment by a large amount. Gradually increasing the baby-constant also accounts for the fact that people will be less likely to reproduce immediately after they have arrived on a new planet, but they will tend to settle down gradually.

Behavior of Age Dynamics over Time

When the model is run initially, a distinct set of generation waves is visible in the age distribution, as seen in Figure 3a. The wave on the right inside Figure 3a is Population Zero, whilst all other waves are new populations born on Mars. Over time, the original population phases out and the wave of new generations completely take over, as seen in Figure 3b. Interestingly, all populations tested eventually reach the steady state that is visible in Figure 3c, wherein the birth rate and death rate are roughly equal and population growth is steady. The waves of generations become indiscernible. This is the form of age distribution described by the United Nations for developed countries [5].

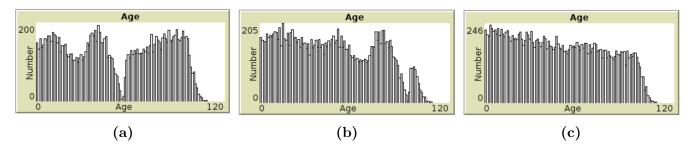


Figure 3: Age distributions across a 100-year model

The short-term instability that occurs before birth and death rates are equal is not without its disadvantages. When Population Zero is first initialized, there are naturally very few babies being born. Thus, after a few years, there are very few individuals who are currently inside the college education system. As the model progresses, more babies are born, leading to a sudden spike in the number of children being born. When these children progress to college, there is a sudden spike in the demand for education:



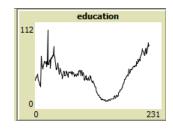


Figure 4: Notice the sudden drop then spike in the education metric

Since the education metric is subject to natural market forces, the government must intervene to provide additional funds and employment during this time of high educational demand.

Sensitivity Analysis

We conducted different initial population selections and compared the effects on the metrics and economic indicators. Since we are only selecting based on age, sex, and occupation, all of the following selection processes are highly sustainable.

Size	Population Characteristics	Notes
10000	Population Zero	See Characteristics of Population Zero
10000	25% female, 75% male	male/female ratio stabilizes at 1 after 100 years; population increases for 30 years and decreases later, ends at 9000; equality still rises but equality is lower; relatively low GDP
10000	75% female, 25% male	population increases steadily to 28000; male/female ratio stabilizes at 1 after 100 years; equality rises but higher than usual; GDP rises for 20 years, falls for 20 years, then rises from then on out; GDP is higher than usual
10000	age, occupation, and sex have an equal chance of being selected	third lowest GDP before Population 2; Equality is approximately same; population slightly increases to 11000
10000	older people (mean of 60)	lowest GDP; population falls continuous until 80 years in where it stabilizes to 4000; equality peaks at its highest at 50 years but decreases normally to an average equality
10000	50% innovators and 50% producers with occupation ratios conserved	GDP and equality are steady increase; unemployment peaks at 11% in 15 years which is much worse than the other populations; education metric is very high; income metric is the lowest out of all the populations

All populations eventually demonstrated a stable unemployment rate of around 3-4%. The equality metric for all populations is around 10. The income metric is generally above 400,000, and rises

steadily over time. The income distribution is skewed to the left, but maintains a middle class primary difference between the population groups is how the population grows relative to the isselection of 10000 people. For more unrestrained growth, a 75% female and 25% male population is optimal. For a more conservative growth, a population in which age, sex, and occupation are independent is more optimal. It is important to note that simply stuffing "innovators" into the population will lead a very high unemployment and other problems.

To test the effects of increased population size in migration phases due to disasters that may occur on Earth, such as "planet-sized comet strike," we tested our model on various populations sizes with random distributions of personal characteristics to simulate the fact that there is no chance to pick and choose the population that migrates during an emergency. We sampled sizes of 10,000, 20,000, 40,000, 80,000, and 100,000. Each agent in these samples had an equal chance to be male or female. Furthermore, the age was equally distributed between 1 and 100 years of age. Finally, occupations were distributed without priority for any one vocation.

The normal migratory population displayed a higher GDP and a much higher income metric (almost 1.5 times as high). The population always grew in every simulation, albeit slowly. The equality metric was generally higher than Population Zero. Unemployment was essentially the same across all populations, but the education metric was significantly higher in migratory populations when compared to Population Zero. GDP increases linearly with population in migration patterns. All other characteristics are comparable across the different populations tested for migration emergencies.

Our model suggests that with these policies, our economy can handle mass migrations of peoples with random attributes. However, infrastructure is not considered in our agent-based model and must be reevaluated in the case that such a migration does occur.

Strengths and Weaknesses

Strengths

- Our model incorporates many of the socioeconomic aspects of a civilization such as the job market, taxation, population growth, and education system. This allows us to make informed predictions about UTOPIA: 2100's development and will enable us to prepare for the challenges that we predict from the model.
- Our agent-based model allows for different combinations to occur in every agent, such as age, sex, education, and income. Unlike a continuous model, where we are forced to generalize such combinations and quantify the interactions between different variables in a broad scope, an agent-based approach allows our model to better characterize the interactions that may occur and reveal outcomes that are often not quantifiable with pure mathematics.
- Our model is robust as it allows for economic considerations of large scale migrations over arbitrarily large time scales. Though we only rigorously tested our model's efficacy for 100 years, we know that the model will continue to make predictions given that the patterns of inflation, interest rate, and other economic indicators holds and the age distribution achieves an equilibrium.
- Our model utilizes metrics that are evaluated continuously, thus allowing us to observe the state of the economy and social welfare at different points of population stress. For instance, between two generations, there is often a lack of teachers and a surplus of students, which is exemplified



by the rise in the education metric. Thus, policy can be designed to not only address the i population on Mars, but also analyze policy options for certain intervals in the model.

• Our model includes a large amount of dynamic elements over time. For example, every citizen is given a dynamic income, which is dynamically affected by sinusoidal inflation and taxation. By allowing characteristics to vary, we reduce the number of assumptions, and therefore reduce the number of possible invariant critical points that may break when the model is put under stress by varying population characteristics.

Weaknesses

- Our model is heavily dependent on current census data of employment, inflation, income growth, percentage of bachelor degrees, and other Census data. Therefore, relatively small changes in this data can compound into large amounts of variation over 80 years.
- Our model is strictly economic in nature. Therefore our model does not take into account the physical infrastructure needed to facilitate a civilization on a large scale. In particular, our model may imply that a large initial population is more digestible than it may be in actuality.
- Our model is probabilistic in nature, meaning that it will return slightly different values when run under the same initial settings. Therefore, multiple trials of our model must be run to determine a value.
- Our model does not consider family structure. In actuality, there may be transfers of income and other interactions within a family that may not be accounted for in this model.

Conclusion and Future Work

We were tasked with the job of modeling and characterizing the income, education, and equality of the Martian population over the course of 10 and 100 years in an effort to maximize the social welfare and productivity of the new civilization. We began by creating an agent-based model that characterized the combined effect of the personal initiative of every Martian citizen and the social welfare provided by the government. By defining the income, education, and equality metrics, we were are able to identify positive and negative characteristics of the Martian economy.

We found that the best initial population had a mean age of 37 and a ratio of 1:10 of innovators to producers. The Martian society can also support more than 10,000 people in emergency situations, assuming that there is adequate infrastructure. We also determined that a maternity leave length of 10 months and a paternity leave length of 3 months would be optimal. Furthermore, the minimum wage was determined to be optimal at around \$70,000. Government control of inflation and a progressive tax system served to increase income inequality while keeping investment high and government debt low, allowing the government to provide for increased education and infrastructure needs. A happiness survey can be utilized to create a strong, collaborative society working to reach common goals.

Given enough time, our group can extend the model to include family structures by implementing an underlying network to simulate inheritance. We can also consider infrastructure as a potential parameter when considering mass migration from the Earth to Mars. To infinity and beyond!



Appendix

Table 1

Name	Education	Workers in 2015
Management Occupations	6 [6]	1.0174
Business and Financial Operations Occupations	4 [7]	1.0184
Computer and Mathematical Occupations	6 [8]	1.0229
Architecture and Engineering Occupations	4 [9]	1.0179
Life, Physical, and Social Science Occupations	8 [10]	1.0134
Community and Social Service Occupations	2 [11]	1.0128
Legal Occupations	8 [12]	1.0127
Education, Training, and Library Occupations	4 [13]	1.0102
Arts, Design, Entertainment, Sports, and Media Occupations	4 [14]	1.0138
Healthcare Practitioners and Technical Occupations	8 [15]	1.0169
Healthcare Support Occupations	8 [16]	1.0190
Protective Service Occupations	4 [17]	1.0108
Food Preparation and Serving Related Occupations	2 [18]	1.0157
Building and Grounds Cleaning and Maintenance Occupations	2 [19]	1.0143
Personal Care and Service Occupations	2 [20]	1.0100
Sales and Related Occupations	4 [21]	1.0112
Office and Administrative Support Occupations	4 [22]	1.0159
Farming, Fishing, and Forestry Occupations	2 [23]	1.0202
Construction and Extraction Occupations	2 [24]	1.0165
Installation, Maintenance, and Repair Occupations	2 [25]	1.0148
Production Occupations	4 [26]	1.0143
Transportation and Material Moving Occupations	2 [27]	1.0141



Table 2

Name	Income ⁸	Income Growth Rate
Management Occupations	115020	6936990
Business and Financial Operations Occupations	73800	7032560
Computer and Mathematical Occupations	86170	4005250
Architecture and Engineering Occupations	82980	2475390
Life, Physical, and Social Science Occupations	71220	1146110
Community and Social Service Occupations	46160	1972140
Legal Occupations	103460	1062370
Education, Training, and Library Occupations	53000	8542670
Arts, Design, Entertainment, Sports, and Media Occupations	56980	1843600
Healthcare Practitioners and Technical Occupations	77800	8021800
Healthcare Support Occupations	29520	3989910
Protective Service Occupations	44610	3351620
Food Preparation and Serving Related Occupations	22850	12577080
Building and Grounds Cleaning and Maintenance Occupations	27080	4407050
Personal Care and Service Occupations	25650	4307500
Sales and Related Occupations	39320	14462120
Office and Administrative Support Occupations	36330	21846420
Farming, Fishing, and Forestry Occupations	26360	454230
Construction and Extraction Occupations	47580	5477820
Installation, Maintenance, and Repair Occupations	45990	5374150
Production Occupations	36220	9073290
Transportation and Material Moving Occupations	35160	9536610



NetLogo Model Code

```
1 extensions[csv]
2 globals
3 [
    data
    file
    prev-income-mean
6
    income-mean
    depreciation
8
    mu-constant
9
    income-d
10
    income-var
    earth
13
    mars
    inflation-amp
14
    inflation-period
15
    inflation-amp-2
16
    inflation-period-2
17
    inflation-constant
18
19
    prob-4-job
    prob-6-job
20
    prob-8-job
21
    available-jobs
22
    labor-force
23
24
    census
    income-file
25
    population
26
    total-inflation
27
    government-debt
    bracket-1
29
    bracket-2
    bracket-3
31
    bracket-4
32
    bracket-5
33
34
    tax-rate-1
    tax-rate-2
35
36
    tax-rate-3
    tax-rate-4
37
    tax-rate-5
38
39
40 turtles-own
41
    age
42
    job
43
    working?
44
    education
45
    student?
46
47
    sex
    on-leave
48
    income
    lifestage; 0 if infant, 1 if student, 2 if college, 3 if adult, 4 if retired, sendng primarly 3'
50
        s, age limit for initial populations
    time-in-job
52
    growth-rate
    percentile
    underemployed?
54
    baby-cooldown
```



```
num-babies
56
     innovator
58
     experience
     death
59
     gross-income
60
61
62 patches-own[; TO DO Set num-babies per women to 2.4
              ; TO DO Set taxes and taxation to nice values
63
              ; TO DO SET minimum wage, welfare, social security
64
65
66
67
   ;breed[mouse mice]
  to toggle
     if (mouse-down?)[
    ]
73 end
74
75 to read
     file-close-all
     file-open "datas.csv"
     set data []
    let data-row []
     while [not file-at-end?] [
80
      set data-row csv:from-row file-read-line
81
      set data lput data-row data
82
    ٦
    file-close-all
84
     file-open readfile
85
     set population []
86
     set data-row []
     while [not file-at-end?] [
88
      set data-row csv:from-row file-read-line
      set population lput data-row population
90
    ]
91
    file-close-all
92
    file-open "earth.csv"
    set earth []
94
     set data-row []
     while [not file-at-end?][
96
      set data-row csv:from-row file-read-line
97
      set earth lput data-row earth
98
99
100
    process
101 end
102 to process
     set file
    n-values 22 [
104
       [arg] ->
       (list (item 0 (item arg data)) (item 1 (item arg data)) (item 2 (item arg data)) (item 3 (item
           arg data)) (item 4 (item arg data)) (item 5 (item arg data)) (item 6 (item arg data)) (
          item 8 (item arg data)) (item 7 (item arg data)) (item 10 (item arg data)) (item 12 (item
          arg data)) 0 arg (item 13 item arg data))
    ]; NAME A_MEAN A_10 A_25 A_50 A_75 A_90 A_rate 8 work force 9 work force rate 10 education
        laborers id INNOVATOR V. PRODUCER
     set population bf population
```



```
set population map [[pop] ->(list read-sex item 1 pop ((item 2 pop) + random-float 1) item 3
         ] population
     ; M/F AGE JOB
    set earth map [[a]->(list round (item 0 a * item 1 a) item 1 a)] earth
112 end
113 to setup
    clear-all
114
    reset-ticks
115
     ;;import-drawing "mars.png"
    read
117
    set bracket-1 minimum-wage
118
    set bracket-2 round ((minimum-wage + income-mean) / 2)
119
    set bracket-3 income-mean
120
    set bracket-4 555000
121
    set bracket-5 775000
    set tax-rate-1 tax-rate / 6
    set tax-rate-2 tax-rate / 5
    set tax-rate-3 tax-rate / 4
    set tax-rate-4 tax-rate / 3
126
    set tax-rate-5 tax-rate / 2
    set total-inflation 1
    set mu-constant 1
129
    set income-d 0.55
130
    set inflation-period 20
131
    set inflation-constant 0.008
132
    set inflation-amp 0.0025
133
    set inflation-amp-2 0.0005
134
    set inflation-period-2 1
135
    set-default-shape turtles "person"
136
    set mars n-values 22 [
138
      [arg]->
139
      [0 \ 0]
140
141
    ]
    set prob-4-job 0.49106860 + 0.197240345 + 0.03564114 + 0.038122
142
    set prob-6-job 0.197240345 + 0.03564114 + 0.038122
143
    set prob-8-job 0.03564114 + 0.038122
144
    set-census
    let rr length filter [[arg]->(not (item 2 arg = -1)) and item 1 arg < 70 and item 1 arg >= 18]
146
        population
    set available-jobs map [[arg]-> arg * rr] census
147
    foreach population [
148
      [arg]->
149
      crt 1 [
        setxy random-xcor random-ycor
        set size 0.35
        set color green + 1
153
        set age item 1 arg
        set sex item 0 arg
        set student? false
156
        set underemployed? false
157
        set death abs (200 - random-gamma 1000 10)
158
        set on-leave 0
159
        set baby-cooldown 0
        set num-babies 0
        ifelse((not (item 2 arg = -1)) and item 1 arg < 70 and item 1 arg >= 18)[
162
          set lifestage 3
```



```
set education item 10 item item 2 arg file
164
          ifelse(item item 2 arg available-jobs > 0)[
            set available-jobs replace-item item 2 arg available-jobs ((item item 2 arg
166
                 available-jobs) - 1)
            set job item 2 arg
167
            set working? true
            set innovator item 13 item job file; TODO give innovator when jobs are assigned, check for
169
                  other 63's
            set time-in-job 0
            set percentile 10
            set growth-rate random-normal (4.65) .4
172
            let ar item job file
173
            set file replace-item item 12 ar file replace-item 11 ar ((item 11 ar) + 1)
            set labor-force labor-force + 1
            ifelse(sex = "female")[
176
              set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
                  mars) + 1))
            ][
178
              set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) + 1
179
            ]
          ٦
181
           182
            set working? false
183
          ]
184
         ][
185
          set working? false
186
          if(item 1 arg >= 70)[
            set lifestage 4
189
          if(item 1 arg < 5)[
190
            set lifestage 0
193
          if(item 1 arg < 18 and item 1 arg >= 5)[
            set lifestage 1
194
          if(item 1 arg \geq 18 and item 1 arg < 70)[
196
197
            set lifestage 2
            set student? true
198
          ٦
199
         ]
200
       ]
201
202
     set labor-force count turtles with [working?]
203
     set-census
204
     set-available-jobs
205
     set-income-file
     ask turtles[
207
       set percentile (min (list 90 (5 + random 11 + (max (list 0 (age - 20))) * growth-rate))) -
208
           growth-rate / ticks-per-year
       grow-income
209
     set income-mean (sum [income] of (turtles with [working? and on-leave <= 0])) / (count turtles
211
         with [lifestage = 3])
     set prev-income-mean 1
     set income-var (standard-deviation [income] of turtles) / income-mean
213
214 end
```

```
215 to set-census
     let s sum map [[arg] -> item 8 arg * (item 9 arg) ^ (80 + ticks / ticks-per-year)] file
     set census map [[arg] -> item 8 arg * (item 9 arg) ^ (80 + ticks / ticks-per-year) / s] file
217
219 to set-available-jobs
     set available-jobs map [[arg]-> round ((count turtles with [lifestage = 3] + (count turtles with
          [student?] / 2 / ticks-per-year)) * item (item 12 arg) census - item 11 arg)] file
221 end
222 to go
     if(ticks >= stop-time)[
223
       stop
224
     ]
225
     set-census
226
     if(abs (ticks / ticks-per-year - round ticks / ticks-per-year) < 0.0001)[</pre>
227
       set-income-file
228
     ;if(abs ( 4 * ticks / ticks-per-year - round 4 * ticks / ticks-per-year) < 0.0001)[
230
       set-available-jobs
231
     ;]
232
     set-inflation
233
     ask turtles[
       if(working?)[;10 @ 25, 25 @ 35, 50 @ 45, 75 @ 55, 90 @ 65
235
         set time-in-job time-in-job + 1 / ticks-per-year
236
         set experience experience + 1 / ticks-per-year
237
         lose-job
238
239
         ;Add welfare + minimum-wagw
       1
240
241
       set-education
       set-age
242
       grow-income
243
       adjust-income
244
       create-babies
       if (age >= death)[
246
        if(working?)[
          retire
         ]
249
         die
250
251
       1
     1
252
253
     set prev-income-mean income-mean
     set income-mean (sum [income] of (turtles with [working? and on-leave <= 0])) / (count turtles</pre>
254
         with [lifestage = 3])
     set income-var (standard-deviation [income] of turtles with [working?]) / income-mean
255
     set-government-debt
256
     tick
257
258 end
   to lose-job
259
     if(random-float 1 < 1 - (1 - 0.02) ^ (1 / ticks-per-year))[
260
261
       set working? false
       set underemployed? false
262
       set income 0
       set file replace-item job file replace-item 11 item job file ((item 11 item job file) - 1)
264
       set labor-force labor-force - 1
265
       set available-jobs replace-item job available-jobs ((item job available-jobs) + 1)
266
       ifelse(sex = "female")[
         set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job mars) -
268
             1))
```



```
][
269
         set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
       ]
271
       set job 0
     ٦
273
275 to-report baby-constant
     report baby-constant-final * min (list 20 ((ticks) / ticks-per-year)) / 20
277 end
278 to-report baby-prob [b n]
     let a floor b
     report baby-constant * (a / 6 - 3) / ((a / 6 - 4) ^ 2 + 1) / (n + 1)
280
   end; TODO
282 to-report read-sex [hi]
     if(hi = 1)[
       report "male"
284
     ]
     report "female"
286
287 end
288 to create-babies
     ifelse(sex = "male" and on-leave > 0)[
       set on-leave on-leave - 12
290
     ][
291
       set on-leave 0
292
     ]
293
     if (sex = "female" and age >= 18 and age < 50)[
294
       ifelse(baby-cooldown > 0)[
295
         set baby-cooldown baby-cooldown - 1
         if((baby-cooldown + 1) * 4 > 5 * ticks-per-year and baby-cooldown * 4 <= 5 * ticks-per-year)
297
          hatch 1 [
298
             set student? false
             set age random-float (1 / ticks-per-year)
300
301
             set baby-cooldown 0
             set working? false
302
             set sex read-sex random 2
303
304
             set lifestage 0
             set underemployed? false
             set num-babies 0
306
             setxy random-xcor random-ycor
307
             set death abs (200 - random-gamma 1000 10)
308
             set income 0
309
             set baby-cooldown 0
310
             set experience 0
311
             set on-leave 0
312
             set job 0
313
             set education 0
             set time-in-job 0
315
316
             set growth-rate 0
             set percentile 10
317
             set innovator ifelse-value (random-float 1 < 0.1)</pre>
             [1] [0]
319
           ]
320
           set num-babies num-babies + 1
321
         ifelse(on-leave > 0)[
323
           set on-leave on-leave - 12
324
```



```
][
325
           set on-leave 0
326
327
         if((baby-cooldown + 1) * 12 > ticks-per-year * 17 and baby-cooldown * 12 <= ticks-per-year *
           set on-leave ((maternity-leave) * ticks-per-year) - 1
329
330
         if(on-leave < 0 and sex = "female")[</pre>
331
           set on-leave 0
           ask one-of turtles with [sex = "male" and abs (age - [age] of myself) <= 5 and on-leave <=
333
             set on-leave (ticks-per-year * paternity-leave) - 1
334
           ]
336
       ][
337
         if(random-float 1 < 1 - (1 - (baby-prob age num-babies))^(1 / ticks-per-year))[</pre>
338
           set baby-cooldown 2 * ticks-per-year
         ]
340
       ]
341
     ٦
342
343 end
344 to set-income-file
     set income-file n-values 22 [
       [arg] ->
346
       (list (item 0 (item arg file)) ((item 1 (item arg file))* (item 7 item arg file) ^ (85 + ticks
347
            / ticks-per-year)) ((item 2 item arg file) * (item 7 item arg file) ^ (85 + ticks /
           ticks-per-year)) ((item 3 item arg file) * (item 7 item arg file) ^ (80 + ticks /
           ticks-per-year)) ((item 4 item arg file) * (item 7 item arg file) ^ (85 + ticks /
           ticks-per-year)) ((item \frac{5}{1} item arg file) * (item \frac{7}{1} item arg file) \frac{60}{1} + ticks /
           ticks-per-year)) ((item 6 item arg file) * (item 7 item arg file) ^ (85 + ticks /
           ticks-per-year)))
     ]
348
349 end
350 to set-education
     if (age < 18 - 0.0001 and age + 1 / ticks-per-year >= 18 - 0.0001 and not student?)[
351
       set student? true
       set education 0
353
354
     7
     if(student?)[
355
       if(education < 2 - 0.0001 and education + 1 / \text{ticks-per-year} >= 2 - 0.0001)[
356
         set education education + 1 / ticks-per-year
357
         check-job
358
359
         stop
360
       if(education < 4 - 0.0001 and education + 1 / ticks-per-year >= 4 - 0.0001)[
361
         set education education + 1 / ticks-per-year
362
         check-job
         stop
364
365
       1
       if (education < 6 - 0.0001 and education + 1 / \text{ticks-per-year} >= 6 - 0.0001)[
366
         set education education + 1 / ticks-per-year
         check-job
368
369
         stop
370
       if(education < 8 - 0.0001 and education + 1 / \text{ticks-per-year} >= 8 - 0.0001)[
         set education education + 1 / ticks-per-year
372
         check-job
373
```



```
374
         stop
       ]
375
       set education education + 1 / ticks-per-year
376
377
     if(((not working?) or underemployed?) and lifestage = 3 and age + 1 / ticks-per-year < 70; and
378
         abs (2 * ticks / ticks-per-year - round 2 * ticks / ticks-per-year) < 0.0001
       )[
379
       check-job
380
     ٦
381
382 end
383 to check-job
     let grow random-normal (4.65) .4
384
     if(round education = 2)[
       foreach file [
386
         [arg]->
387
         if( item 10 arg = 2 and item item 12 arg available-jobs > 0 and ((not underemployed?) or
388
             item 10 item job file < 2))[</pre>
          ifelse(sex = "female" and random-float 1 < 0.25) or (sex = "male" and random-float 1 < 0.0
389
              7)[
            if(working?)[
390
              set labor-force labor-force - 1
              set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
392
                   1)
              set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
393
              ifelse(sex = "female")[
394
                set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
395
                    mars) - 1))
              ][
396
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
397
                     1))
              ]
398
            ]
            set working? false
400
401
            set student? false
            set underemployed? false
402
            set lifestage 4
403
            stop
404
405
          ][
            if(working?)[
406
              set labor-force labor-force - 1
407
              set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
408
              set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
409
              ifelse(sex = "female")[
410
                set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
411
                    mars) - 1))
              ][
412
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
413
                     1))
              ]
414
            set job item 12 arg
416
            set working? true
417
            set student? false
418
            set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
            set labor-force labor-force + 1
420
            set available-jobs replace-item (item 12 arg) available-jobs ((item (item 12 arg)
421
```



```
available-jobs) - 1)
422
             set time-in-job (
             set underemployed? false
423
             set growth-rate grow
             set percentile 10 + random (skew * 2 - 20)
425
             set innovator item 13 item job file
426
             ifelse(sex = "female")[
427
               set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
428
                   mars) + 1))
            ][
429
               set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) + 1
430
             ]
             stop
432
           ]
433
         ]
434
       if(random-float 1 > prob-4-job and not underemployed?)[
436
         if(working?)[
437
           set labor-force labor-force - 1
438
           set file replace-item job file replace-item 11 item job file ((item 11 item job file) - 1)
           set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
440
           ifelse(sex = "female")[
441
             set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job mars)
442
          ][
443
             set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) - 1))
444
           ٦
         set working? false
447
         set student? false
448
         set underemployed? false
       ]
450
451
       ; TO DO: FAMILIES
     ]
452
     if(round education = 4)[
453
       foreach file [
454
         [arg]->
         if (item \frac{10}{10} arg = \frac{4}{10} and item item \frac{12}{10} arg available-jobs > \frac{0}{10} and ((not underemployed?) or
456
             item 10 item job file < 4))[</pre>
           ifelse(sex = "female" and random-float 1 < 0.19) or (sex = "male" and random-float 1 < 0.0
457
               3)[
             if (working?) [
               set labor-force labor-force - 1
459
               set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
460
               set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
               ifelse(sex = "female")[
462
                 set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
                     mars) - 1))
              ][
                 set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
465
               ]
466
             ]
             set working? false
468
             set student? false
469
```



```
set underemployed? false
470
            set lifestage 4
472
            stop
          ][
473
            if(working?)[
              set labor-force labor-force - 1
              set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
476
              set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
              ifelse(sex = "female")[
478
                set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
                    mars) - 1))
              ][
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
481
                     1))
              ]
482
            ]
            set job item 12 arg
484
            set working? true
485
            set student? false
486
            set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
            set labor-force labor-force + 1
488
            set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
489
                available-jobs - 1)
            set time-in-job 0
490
            set underemployed? false
491
            set growth-rate grow
492
            set percentile 10 + random (skew * 2 - 20)
            set innovator item 13 item job file
494
            ifelse(sex = "female")[
495
              set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
496
                  mars) + 1))
            ][
497
498
              set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) + 1
500
            stop
          ]
501
         ]
502
503
       if(not working?)[
504
         foreach file [
505
           [arg]->
          if (item 10 arg = 2 and item item 12 arg available-jobs > 0 and ((not underemployed?) or
507
               item 10 item job file < 2))[
            ifelse(sex = "female" and random-float 1 < 0.19) or (sex = "male" and random-float 1 < 0.
508
                03)[
              if(working?)[
509
                set labor-force labor-force - 1
                set file replace-item job file replace-item 11 item job file ((item 11 item job file)
                     - 1)
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
                ifelse(sex = "female")[
513
                  set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
514
                       mars) - 1)
                ][
515
                  set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
516
```



```
- 1))
                ]
              ]
518
              set working? false
519
              set student? false
520
              set underemployed? false
              set lifestage 4
              stop
            ][
              if(working?)[
                set labor-force labor-force - 1
526
                set file replace-item job file replace-item 11 item job file ((item 11 item job file)
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
528
                ifelse(sex = "female")[
                  set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
530
                       mars) - 1))
                ][
                  set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
                       - 1))
534
535
              set job item 12 arg
              set working? true
              set student? false
              set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
538
              set labor-force labor-force + 1
              set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
                  available-jobs - 1)
              set time-in-job 0
541
              set underemployed? true
              set growth-rate grow + 0.1
              set percentile 10 + random (skew * 2 - 20)
544
545
              set innovator item 13 item job file
              ifelse(sex = "female")[
546
                set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
                    mars) + 1))
              ][
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) +
549
                     1))
              ]
550
              stop
551
554
       if(random-float prob-4-job > prob-6-job and not underemployed?)[
        if(working?)[
          set labor-force labor-force - 1
          set file replace-item job file replace-item 11 item job file ((item 11 item job file) - 1)
          set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
          ifelse(sex = "female")[
561
            set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job mars)
562
                 - 1))
          ][
            set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) - 1))
564
          ]
565
```



```
]
566
         set working? false
567
         set student? false
568
         set underemployed? false
569
       ٦
570
     ]
     if(round education = 6)[
572
       foreach file [
573
         [arg]->
         if (item 10 arg = 6 and item item 12 arg available-jobs > 0 and ((not underemployed?) or
             item 10 item job file < 6))[</pre>
          ifelse(sex = "female" and random-float 1 < .09) or (sex = "male" and random-float 1 < 0.02
              ٦ (
            if(working?)[
              set labor-force labor-force - 1
578
              set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
579
              set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
580
              ifelse(sex = "female")[
581
                set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
                    mars) - 1)
              ][
583
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
584
                     1))
              ]
585
586
            ]
            set working? false
587
            set student? false
            set underemployed? false
            set lifestage 4
590
            stop
          ][
            if(working?)[
594
              set labor-force labor-force - 1
              set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
595
              set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
596
597
              ifelse(sex = "female")[
                set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
598
                    mars) - 1))
              ][
599
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
600
                     1))
              ]
601
602
            set job item 12 arg
603
            set working? true
            set student? false
605
            set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
606
            set labor-force labor-force + 1
607
            set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
608
                available-jobs - 1)
            set time-in-job 0
609
            set underemployed? false
610
            set growth-rate grow
            set percentile 10 + random (skew * 2 - 20)
612
            set innovator item 13 item job file
613
```

```
ifelse(sex = "female")[
614
               set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
615
                   mars) + 1))
             ][
616
               set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) + 1
617
             ]
618
             stop
619
           ٦
620
         ]
621
       ]
622
       if(not working?)[
623
         foreach file [
           [arg]->
625
           if (item \frac{10}{10} arg = \frac{4}{10} and item item \frac{12}{10} arg available-jobs > \frac{10}{10} and ((not underemployed?) or
               item 10 item job file < 4))[</pre>
             ifelse(sex = "female" and random-float 1 < .09) or (sex = "male" and random-float 1 < 0.09)
                 2)[
               if(working?)[
628
                 set labor-force labor-force - 1
                 set file replace-item job file replace-item 11 item job file ((item 11 item job file)
                 set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
631
                 ifelse(sex = "female")[
                   set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
633
                        mars) - 1))
                ][
634
                   set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
                        - 1))
                ٦
636
               ]
637
               set working? false
               set student? false
639
640
               set underemployed? false
               set lifestage 4
641
               stop
             ][
643
               if(working?)[
                 set labor-force labor-force - 1
645
                 set file replace-item job file replace-item 11 item job file ((item 11 item job file)
646
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
647
                 ifelse(sex = "female")[
                   set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
649
                        mars) - 1))
                ][
650
                   set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
                        - 1))
                ]
652
               ]
653
               set job item 12 arg
               set working? true
655
               set student? false
656
               set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
657
               set labor-force labor-force + 1
               set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
659
```



```
set time-in-job 0
660
               set underemployed? true
661
662
               set growth-rate grow + 0.1
               set percentile 10 + random (skew * 2 - 20)
663
               set innovator item 13 item job file
664
               ifelse(sex = "female")[
665
                 set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
666
                     mars) + 1)
              ][
667
                 set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) +
668
               ]
669
               stop
671
           ]
         ]
673
       ]
       if(not working?)[
675
         foreach file [
676
           [arg]->
           if (item 10 arg = \frac{2}{2} and item item \frac{12}{2} arg available-jobs > \frac{0}{2} and ((not underemployed?) or
               item 10 item job file < 2))[</pre>
             ifelse(sex = "female" and random-float 1 < .09) or (sex = "male" and random-float 1 < 0.09
679
                 2)[
               if(working?)[
680
                 set labor-force labor-force - 1
681
                 set file replace-item job file replace-item 11 item job file ((item 11 item job file)
682
                      -1
                 set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
683
                ifelse(sex = "female")[
684
                   set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
685
                        mars) - 1)
                ][
686
                   set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
687
                        - 1))
               ]
689
690
               set working? false
               set student? false
691
               set underemployed? false
692
               set lifestage 4
693
               stop
694
             ][
               if(working?)[
696
                 set labor-force labor-force - 1
697
                 set file replace-item job file replace-item 11 item job file ((item 11 item job file)
698
                      - 1)
                 set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
699
                 ifelse(sex = "female")[
                   set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
701
                        mars) - 1))
                ][
702
                   set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
703
                        - 1))
                ]
               ]
705
               set job item 12 arg
706
```



```
set working? true
707
              set student? false
708
              set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
709
              set labor-force labor-force + 1
              set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
                  available-jobs - 1)
              set time-in-job 0
712
              set underemployed? true
713
              set growth-rate grow + 0.2
              set percentile 10 + random (skew * 2 - 20)
715
              set innovator item 13 item job file
716
              ifelse(sex = "female")[
717
                set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
                    mars) + 1)
              ][
719
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) +
                     1))
              ]
721
722
              stop
            ٦
723
          1
725
726
       if(random-float prob-6-job > prob-8-job and not underemployed?)[
         if(working?)[
          set labor-force labor-force - 1
729
          set file replace-item job file replace-item 11 item job file ((item 11 item job file) - 1)
730
          set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
          ifelse(sex = "female")[
732
            set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job mars)
733
                 - 1))
          ][
            set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) - 1))
736
          ]
737
         set working? false
         set student? false
739
         set underemployed? false
       ٦
741
     ]
742
     if(round education = 8)[
743
       foreach file [
744
         [arg]->
745
         if( item 10 arg = 8 and item item 12 arg available-jobs > 0 and ((not underemployed?) or
746
             item 10 item job file < 8))[
          ifelse(sex = "female" and random-float 1 < .06) or (sex = "male" and random-float 1 < 0.01
747
              )[
            if (working?) [
748
              set labor-force labor-force - 1
749
              set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
              set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
751
              ifelse(sex = "female")[
752
                set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
                    mars) - 1)
              ][
754
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
755
```



```
1))
              ]
             ]
757
             set working? false
758
             set student? false
             set underemployed? false
             set lifestage 4
761
             stop
762
          ][
             if(working?)[
764
               set labor-force labor-force - 1
               set file replace-item job file replace-item 11 item job file ((item 11 item job file) -
766
               set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
767
               ifelse(sex = "female")[
                 set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
                    mars) - 1)
              ][
770
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) -
771
               ]
             set job item 12 arg
             set working? true
             set student? false
             set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
             set labor-force labor-force + 1
778
             set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
                 available-jobs - 1)
             set time-in-job 0
780
             set underemployed? false
781
             set growth-rate grow
             set percentile 10 + random (skew * 2 - 20)
783
784
             set innovator item 13 item job file
             ifelse(sex = "female")[
785
               set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
                  mars) + 1))
               set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) + 1
             ]
789
             stop
790
           ٦
793
       if(not working?)[
794
         foreach file [
           [arg]->
796
           if (item \frac{10}{10} arg = \frac{6}{10} and item item \frac{12}{10} arg available-jobs > \frac{0}{10} and ((not underemployed?) or
               item 10 item job file < 6))[
             ifelse(sex = "female" and random-float 1 < .06) or (sex = "male" and random-float 1 < 0.0
                 1)[
               if(working?)[
799
                set labor-force labor-force - 1
800
                 set file replace-item job file replace-item 11 item job file ((item 11 item job file)
                      - 1)
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
802
```

```
ifelse(sex = "female")[
803
                   set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item
804
                        mars) - 1)
                ][
805
                   set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
806
                ]
807
               ]
808
               set working? false
               set student? false
810
               set underemployed? false
811
               set lifestage 4
812
               stop
             ][
814
               if(working?)[
                 set labor-force labor-force - 1
816
                 set file replace-item job file replace-item 11 item job file ((item 11 item job file)
817
                 set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
818
                 ifelse(sex = "female")[
819
                   set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
820
                        mars) - 1)
                ][
821
                   set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
822
                ]
823
               ٦
824
               set job item 12 arg
               set working? true
826
               set student? false
827
               set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
828
               set labor-force labor-force + 1
               set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
830
                   available-jobs - 1)
               set time-in-job 0
831
               set underemployed? true
832
833
               set growth-rate grow + 0.1
834
               set percentile 10 + random (skew * 2 - 20)
               set innovator item 13 item job file
               ifelse(sex = "female")[
836
                 set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
837
                     mars) + 1))
              ][
838
                 set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) +
839
                      1))
               ]
840
               stop
             ]
842
           ]
843
         ]
844
       if(not working?)[
846
         foreach file [
847
           [arg]->
848
           if (item 10 arg = \frac{4}{10} and item item \frac{12}{10} arg available-jobs > \frac{1}{10} and ((not underemployed?) or
               item 10 item job file < 4))[</pre>
             ifelse(sex = "female" and random-float 1 < .06) or (sex = "male" and random-float 1 < 0.0
850
```



```
1)[
              if(working?)[
851
                set labor-force labor-force - 1
852
                set file replace-item job file replace-item 11 item job file ((item 11 item job file)
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
                ifelse(sex = "female")[
855
                  set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
856
                       mars) - 1)
                ][
857
                  set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
                       - 1))
                ]
860
              set working? false
              set student? false
862
              set underemployed? false
              set lifestage 4
864
              stop
865
            ][
866
              if(working?)[
                set labor-force labor-force - 1
868
                set file replace-item job file replace-item 11 item job file ((item 11 item job file)
869
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
870
                ifelse(sex = "female")[
871
                  set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
                       mars) - 1))
873
                  set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
                       - 1))
                ]
              ]
876
              set job item 12 arg
              set working? true
              set student? false
              set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
880
              set labor-force labor-force + 1
              set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
882
                  available-jobs - 1)
              set time-in-job 0
883
              set underemployed? true
884
              set growth-rate grow + 0.2
              set percentile 10 + random (skew * 2 - 20)
886
              set innovator item 13 item job file
              ifelse(sex = "female")[
888
                set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
                    mars) + 1))
890
              ][
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) +
891
                     1))
892
893
              stop
            ]
894
          ]
         ]
896
       ]
897
```



```
if(not working?)[
898
         foreach file [
899
           [arg]->
900
           if (item 10 arg = 2 and item item 12 arg available-jobs > 0 and ((not underemployed?) or
901
               item 10 item job file < 2))[</pre>
            ifelse(sex = "female" and random-float 1 < .06) or (sex = "male" and random-float 1 < 0.0
902
                1)[
              if(working?)[
903
                set labor-force labor-force - 1
                set file replace-item job file replace-item 11 item job file ((item 11 item job file)
905
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
906
                ifelse(sex = "female")[
                  set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
908
                       mars) - 1)
                ][
909
                  set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
910
                ]
911
              ٦
912
              set working? false
              set student? false
914
              set underemployed? false
915
              set lifestage 4
916
              stop
917
            ][
918
              if(working?)[
919
                set labor-force labor-force - 1
                set file replace-item job file replace-item 11 item job file ((item 11 item job file)
921
                     - 1)
                set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
922
                ifelse(sex = "female")[
                  set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job
924
                       mars) - 1))
                ][
925
                  set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars)
                       - 1))
              ]
928
              set job item 12 arg
930
              set working? true
              set student? false
931
              set file replace-item item 12 arg file replace-item 11 arg (item 11 arg + 1)
              set labor-force labor-force + 1
933
              set available-jobs replace-item item 12 arg available-jobs (item item 12 arg
934
                  available-jobs - 1)
              set time-in-job 0
              set underemployed? true
936
937
              set growth-rate grow + 0.3
              set percentile 10 + random (skew * 2 - 20)
938
              set innovator item 13 item job file
              ifelse(sex = "female")[
940
                set mars replace-item job mars (list ((item 0 item job mars) + 1) ((item 1 item job
941
                    mars) + 1)
              ][
                set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) +
943
```



```
]
944
               stop
945
             ]
946
          ]
         ٦
948
949
       if(not underemployed?)[
950
         if(working?)[
951
           set labor-force labor-force - 1
           set file replace-item job file replace-item 11 item job file ((item 11 item job file) - 1)
953
           set available-jobs replace-item job available-jobs ((item job available-jobs) - 1)
954
           ifelse(sex = "female")[
955
             set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job mars)
                  - 1))
          ][
957
             set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) - 1))
958
           ]
960
         set student? false
961
         set working? false
962
         set underemployed? false
964
     ]
965
     set education round education
966
967 end
968 to retire
     if(working?)[
969
       set available-jobs replace-item job available-jobs (item job available-jobs + 1)
       set labor-force labor-force - 1
971
       set underemployed? false
972
       set file replace-item job file replace-item 11 item job file ((item 11 item job file) - 1)
973
       ifelse(sex = "female")[
         set mars replace-item job mars (list ((item 0 item job mars) - 1) ((item 1 item job mars) -
975
             1))
       ][
976
         set mars replace-item job mars (list (item 0 item job mars) ((item 1 item job mars) - 1))
978
     set working? false
980
981
982 to-report unemployment-rate
     if(count turtles with [lifestage = 3] = 0)[
983
       report 0
985
     report 1 - ((labor-force) / (count turtles with [lifestage = 3]))
986
987 end
   to grow-income
     if(working?)[
989
       set percentile percentile + growth-rate / ticks-per-year
990
       if(percentile < 10)[</pre>
991
         set income minimum-wage
         stop
993
994
       if(percentile < 25)[</pre>
995
         set income ((item 2 (item job income-file)) * (25 - percentile) + (item 3 (item job
             income-file)) * (percentile - 10)) / 15 / total-inflation
997
         stop
```



```
998
       if(percentile < 50)[</pre>
999
          set income ((item 3 (item job income-file)) * (50 - percentile) + (item 4 (item job
1000
              income-file)) * (percentile - 25)) / 25 / total-inflation
          stop
1001
       ]
1002
       if(percentile < 75)[</pre>
1003
          set income ((item 4 (item job income-file)) * (75 - percentile) + (item 5 (item job
1004
              income-file)) * (percentile - 50)) / 25 / total-inflation
          stop
1005
       ]
1006
       if(percentile < 90)[</pre>
1007
          set income ((item 5 (item job income-file)) * (90 - percentile) + (item 6 (item job
1008
              income-file)) * (percentile - 75)) / 15 / total-inflation
1009
       ]
        set income item 6 (item job income-file) / total-inflation
1011
      if(lifestage = 3 and (not working?))[
1013
        set income welfare
1014
      ٦
1015
1016 end
1017 to adjust-income
      set gross-income income
1018
      set income income - taxation income
1019
      if(income < minimum-wage and working?)[</pre>
1020
          set income minimum-wage
1021
     1
1022
      if(not working?)[
       set income 0
1024
      if(investment > 0 and working?)[
1026
       set income income + interest-rate * investment
1027
1029 end
1030 to set-age
      set age age + 1 / ticks-per-year
      if(age < 5)[
       set lifestage 0
1034
        stop
1035
      if(age < 18)[
1036
       set lifestage 1
       stop
1038
1039
      if(age >= 70 or lifestage = 4)[
1040
       if(not (lifestage = 4))[
1041
         retire
1043
       ]
       set lifestage 4
        stop
      if(student?)[
1047
       set lifestage 2
1048
1049
       stop
     1
      set lifestage 3
```



```
1052 end
1053 to-report investment
     report (1 / (1 + inflation)) * (income - welfare / (1 - MPC)) * (1 - MPC) * ifelse-value (
         innovator = 1) [1.5][1]
1055 end
1056 to-report gdp
     report (sum [income] of turtles with [working?]) * MPC + welfare * count turtles with [lifestage
          >= 3] + government-spending + sum [investment] of turtles with [working?]
1058 end
1059 ;to-report mean-metric
1060 ; let dmu (abs (income-mean - prev-income-mean)) / (income-mean + prev-income-mean) * 2 *
       ticks-per-year
1061 ; report dmu / (dmu + mu-constant * income-mean); TO DO set mu-constant
1062 ;end
1063 to-report variance-metric
     report (income-var) / ((income-var) ^ 2 + income-d)
1066 to-report income-metric
     report income-mean * variance-metric
1067
1068 end
1069 to-report equal [a b]
     if(item 1 b = 0)[
       report 0
1071
     1
     report ((item 0 a ) / (item 1 a) - (item 0 b) / (item 1 b)) ^ 2
1073
1074 end
1075 to-report equality-c
     let x (map equal earth mars)
     report map [[arg]-> arg / sum x ] x
1078 end
1079 to-report equality
     let women n-values 22 [
       [arg]->
1081
       count turtles with [sex = "female" and job = arg]
1082
     ]
1083
     report sum (map [[a b] -> a * b] equality-c women) / labor-force
1084
1085 end
1086 to-report inflation
     report sinoid (ticks / ticks-per-year)
1087
1088 end
1089 to-report sinoid [hi]
     report inflation-amp * sin (hi * 360 / inflation-period) + inflation-constant - inflation-amp-2
         * cos (hi * 360 / inflation-period-2)
1091 end
1092 to set-inflation
     set total-inflation total-inflation * (1 + inflation) ^ (1 / ticks-per-year)
1094 end
1095 to-report education-metric
     let t sum ([education] of turtles with [job = 7]) + sum ([experience] of turtles with [job = 7])
     if(t = 0)[
       set t (1 / 2)
     report 100 * unemployment-rate * count turtles with [student?] / t
1100
1101 end
1102 to-report government-spending
     report count turtles with [student?] * 42155 + ((168281905 + 158625722 ) * count turtles / 10000
         ) + count turtles with [lifestage = 3 and (not working?)] * welfare + count turtles with [
```



```
age >= 70] * social-security
1104; insurance everything else defense + 79312861
1105 end
1106 to set-government-debt
     set government-debt government-debt + (government-spending - sum [taxation income] of turtles
         with [lifestage = 3]) / ticks-per-year
1108 end
1109 to-report taxation [n]
     let tax 0
1111
     if (n > bracket-5) [
       set tax (tax + (tax-rate-5 * (n - bracket-5)))
       set n (bracket-5)
1113
     ]
1114
     if (n > bracket-4) [
       set tax (tax + (tax-rate-4 * (n - bracket-4)))
1116
       set n (bracket-4)
1117
1118
     if (n > bracket-3) [
1119
       set tax (tax + (tax-rate-3 * (n - bracket-3)))
1120
       set n (bracket-3)
1121
1122
     if (n > bracket-2) [
1123
       set tax (tax + (tax-rate-2 * (n - bracket-2)))
       set n (bracket-2)
1125
1126
     if (n > bracket-1) [
1127
       set tax (tax + (tax-rate-1 * (n - bracket-1)))
1128
       set n (bracket-1)
1129
1130
     report tax
1131
1132 end
```



Population Characteristics

Every person in the population has certain characteristics associated with them that helps determine their interactions in the society and economy. We now provide a brief description of these characteristics.

- Age This value reports the age of the person and is set to zero when the person is born.
- Job This value represents the person's job field (0 22). If the person does not have a job, this value is set to -1.
- Working? This value reports true if the person has a job and false if they do not have a job.
- Education This value represents the number of years of education of the person (0 Not yet in college, 2 Associate, 4 Bachelor, 6 Master, 8 Ph. D).
- Student? This value reports true if the person is in school/college and false if they are not.
- Sex This value reports the sex of the person (male or female)
- On-leave This value represents the number of months of maternity/paternity leave that a person has. If on-leave = 0, the person is not on leave.
- Income This value represents the net-income of the person.
- Gross-Income This value represents the gross-income of the person.
- Lifestage This value represents the lifestage of the person: 0 if infant, 1 if student, 2 if college, 3 if adult, and 4 if retired/stay-at-home-parent.
- Time-In-Job This value represents the amount of time that a person has been in his/her latest job.
- Experience This value represents the total amount of time that a person has worked in all of their jobs (their total work experience).
- Growth Rate This value represents the percentile growth rate of a person. It is a randomly selected value normally distributed about a mean of 4.6 and a standard deviation of .4
- Percentile This value represents the income percentile of the person.
- Underemployed? This value reports true if the person is overqualified for their job (i.e. their level of education is greater than the education requirement of their job) and false if they are not.
- Baby-Cooldown This value represents the time that a person cannot have another baby. If this value is 0, the person can have another baby (given that they are of the appropriate age).
- Num-Babies This value represents the number of children that a baby has. It is inversely proportional to the probability that a person will have another baby.
- Innovator This value represents whether or not a person will be an innovator (0 Non-Innovator, 1 Innovator). Approximately 10% of the population is composed of innovators, and innovators tend to invest 50% more than non-innovators (this amount is set by the user).
- Death This value represents the lifespan of a person. If a person's age equals his lifespan, he will die.

References



- [1] "A Skills Model for 22nd Century Higher Education." The Blue Review. 19 June 2013. Web. 23 Jan. 2017.
- [2] "World Population to 2300." UN Journal (n.d.): n. pag. Web. 22 Jan. 2017.
- [3] Gallup, Inc. "In U.S., Average Retirement Age Up to 61." Gallup.com. 15 May 2013. Web. 22 Jan. 2017.
- [4] "Communism and Computer Ethics." Communism: Work Ethic and Motivation. Stanford University, n.d. Web. 22 Jan. 2017.
- [5] "World Population Ageing." Department of Economic and Social Affairs. United Nations. 2013. Web. Jan. 22. 2017.
- [6] "What are the Requirements Needed to Obtain a Business Management Degree?" BusinessManagementDegree.net. 2017. Web. 22. Jan. 2017.
- [7] "What are the Educational Requirements for a Financial Advisor Career?" Learn.org. 2017. Web. 22. Jan. 2017.
- [8] "Computer Programmer Education Requirements and Career Information." Study.com. 2017. Web. 22. Jan. 2017.
- [9] "Architect Educational Requirements." Study.com. 2017. Web. Jan. 22. 2017.
- [10] "Cancer Researcher: Job Description and Education Requirements." Study.com. 2017. Web. Jan. 22. 2017.
- [11] "Becoming a Social Worker: Starting Out." SocialWorkLicensure.org. 2017. Web. 22. Jan. 2017.
- [12] "Business Law Career Options and Education Requirements." Study.com. 2017. Web. Jan. 22. 2017.
- [13] "What do you have to major in to become a Teacher?" Study.com. 2017. Web. Jan. 22. 2017.
- [14] "Fashion Designer: Education Requirements and Career Info" Study.com. 2017. Web. Jan. 22. 2017.
- [15] "Requirements to Become a Doctor in the U.S." Study.com. 2017. Web. Jan. 22. 2017.
- [16] American Scoeity of Anesthesiologists. "How to Prepare for a Career in Anesthesiology." ASAHQ.org. 2017. Web. 22. Jan. 2017.
- [17] "Joining the Central Intelligence Agency." CIAAgentEdu.org. 2017. Web. Jan. 22. 2017.
- [18] Eisele, Greg. "How Long is Culinary School?" The University of Tennessee. Jan. 19. 2016. Web. Jan. 22. 2017.
- [19] "Building Maintenance Education Requirements and Degree Program Info." Study.com. 2017. Web. Jan. 22. 2017.
- [20] "Personal Care Worker: Job Description, Salary Info and Requirements." Study.com. 2017. Web. Jan. 22. 2017.

本资料由迈思数模整理www.maisums.com



- [21] "Sales Associate: Job Description, Requirements and Career Information." Study.com. Web. Jan. 22, 2017.
- [22] "Office Manager: Job Profile and Education Requirements." Study.com. 2017. Web. Jan. 22. 2017.
- [23] "Forestry Training Programs and Requirements." Study.com. 2017. Web. Jan. 22. 2017.
- [24] "Constrution Degree Programs and College Majors." Study.com. 2017. Web. Jan. 22. 2017.
- [25] "Cable Technician: Job Duties and Requirements." Study.com. 2017. Web. Jan. 22. 2017.
- [26] "Career Information for a Degree in Industrial Engineering." Study.com. Web. Jan. 22. 2017.
- [27] "Transportation Degree Programs with Course Descriptions." Study.com. 2017. Web. Jan. 22. 2017.
- [28] "Educational Attainment in the United States: 2013 Detailed Tables." U.S. Census Bureau, Demographic Internet Staff. Web. 22 Jan. 2017.
- [29] Ross, Sean. "How Does the Marginal Propensity to Consume in the United States Compare to Other Countries?" Investopedia. 04 June 2015. Web. 22 Jan. 2017.
- [30] "What Is the Total Government Spending?" US Total Government Spending in dollar Trillion, Breakdown for 2017 Charts. Web. 22 Jan. 2017.
- [31] "Cost and Length of Associates Degree Programs." Associates Degree. Associates Degree.com. 2017. Web. 22. Jan. 2017.
- [32] "Spending." Canadian Institute for Health Information. 2017. Web. Jan. 22. 2017.
- [33] "Fact Sheet Social Security." Social Security. Social Security Administration. 2016. Web. Jan. 22. 2017.
- [34] Glasmeier, Amy K. "Living Wage Calculation for North Carolina." Living Wage Calculator. Massachusetts Institute of Technology. 2017. Web. Jan. 22. 2017.
- [35] Tankersley, Jim. "Federal Reserve raises interest rates for second time in a decade." The Washington Post. 14 Dec. 2016. Web. Jan. 22. 2017.
- [36] The Space Report. Rep. Colarado Springs: Space Foundation, 2016. Print.
- [37] "Inflation, Consumer Prices (annual %)." Inflation, Consumer Prices (annual %) Data. Web. 22 Jan. 2017.
- [38] "Delayed Childbearing: More Women Are Having Their First Child Later in Life." Centers for Disease Control and Prevention. Centers for Disease Control and Prevention, 12 Aug. 2009. Web. 22 Jan. 2017.
- [39] "Fertility Rate, Total (births per Woman)." Fertility Rate, Total (births per Woman) Data. Web. 22 Jan. 2017.
- [40] Media, Triami. "Historic Inflation Canada CPI Inflation." Historic Inflation Canada Historic CPI Inflation Canada. Web. 22 Jan. 2017.

n Canada. Web. 22 Jan. 2017. 本资料由迈思数模整理www.maisums.com



- [41] Staff. "Canada's Inflation Rate Ticks up to 1.3% in September." Global News. 21 Oct. Web. 22 Jan. 2017.
- [42] "Employee Tenure Summary." U.S. Bureau of Labor Statistics. United States Department of Labor. 22. Sep. 2016. Web. Jan. 22. 2017.
- [43] Blastland, Michael. "Go Figure: How Likely Are You to Lose Your Job?" BBC News. BBC, 08 Dec. 2011. Web. 22 Jan. 2017.
- [44] Dagum, Camilo. "Income Inequality Measures." Encyclopedia of Statistical Sciences (2004): n. pag. Web.
- [45] Proctor, Bernadette D. et al. "Income and Poverty in the United States." U.S. Department of Commerce. Sep. 2016. Web. Jan. 22. 2017.
- [46] Bauman, Kurt and Davis, Jessica. "Estimates of School Enrollment by Grade in the American Community Survey, the Current Population Survey, and the Common Core of Data." Economic and Housing Statistics Division. U.S. Census Bureau. Dec. 31. 2013. Web. Jan. 22. 2017.
- [47] "Number and Percentage Distribution of Teachers in Public and Private Elementary and Secondary Schools, by Selected Teacher Characteristics: Selected Years, 1987-88 through 2011-12." National Center for Education Statistics. U.S. Department of Education. July 2013. Web. Jan. 22. 2017.
- [48] "Highest Degree Earned, Years of Full-time Teaching Experience, and Average Class Size for Teachers in Public Elementary and Secondary Schools, by State: 2011-12." National Center for Education Statistics. IES, n.d. Web. 23 Jan. 2017.
- [49] "State Unemployment Rates in 2010." TED: The Economics Daily. Bureau of Labor Statistics, United States Department of Labor. March 01. 2011. Web. Jan. 22. 2017.
- [50] Cohn, D'Vera, Gretchen Livingston, and Wendy Wang. "Chapter 2: Stay-at-Home Mothers by Demographic Group." Pew Research Center's Social & Demographic Trends Project. 08 Apr. 2014. Web. 22 Jan. 2017.
- [51] Livingston, Gretchen. "Chapter 1: The Likelihood of Being a Stay-at-Home Father." Pew Research Center's Social & Demographic Trends Project. 05 June 2014. Web. 22 Jan. 2017.
- [52] Livingston, Gretchen. "Opting Out? About 10% of Highly Educated Moms Are Staying at Home." Pew Research Center. 07 May 2014. Web. 22 Jan. 2017.
- [53] "Bogleheads.org." CPI Max and Min Changes since 1913 Bogleheads.org. Web. 23 Jan. 2017.
- [54] Payne, Stephen. "The Info List Gini Index." The Info List.com. 2015. Web. Jan. 22. 2017.
- [55] Bourne, Murray. "The Gini Coefficient of Wealth Distribution." The InMath Blog. SquareCirclez. Feb. 24. 2010. Web. Jan. 22. 2017.
- [56] Crow, E. L., & Shimizu, K. (Eds.). (1988). Lognormal distributions: Theory and applications (Vol. 88). New York: M. Dekker, page 11.