Parallel Orthogonal Recursive Bisection

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Introduction

Introduction

Expansion upon previous parallel sorting project

Objectives:

- Given set of data
- Develop parallel orthogonal recursive bisection (ORB) algorithm
- Utilize a k-d tree to organize data
- Maximize use of MPI using multiple nodes
- Require both serial/parallel build/search operations
- Search the k-d data with a list of points and 3 radii

Introduction

SUBLISTSSSSS

Workflow:

- Using Git effectively (multiple branches, few merge conflicts)
- Extreme coding if FUN...and powerful
- Prototyping: we each wrote our own, implementation based on Graham's MATLAB code

Implementation

Our main was quite simple due to our organization of the project into many levels of functions

We also were able to use much of the basic initialization and data importing functions from the previous project

Algorithm 1: main(···)

- 1: Initialize MPI
- 2: Set number of files, lines per file to read
- 3: import the data
- 4: Initialize tree
- 5: buildTree($data, tree, comm, \cdots$)
- 6: Search the tree with search501(tree, \cdots)
- 7: Finalize MPI

To build the tree, we use several functions which perform different aspects/sections of the task

Functions:

- buildTree
- buildTree_serial
- buildTree_parallel
- getSortDim

buildTree checks the number of compute nodes in the current communicator and determines whether to call the parallel or serial versions of the code

Algorithm 2: buildTree (\cdots)

```
1: q = \mathsf{Size} of current communicator
```

- 2: if q > 1 then
- 3: $buildTree_parallel(\cdots)$
- 4: **else**
- 5: buildTree_serial (\cdots)
- 6: end if

buildTree_serial performs ORB using a single compute node

Algorithm 3: buildTree_serial($data, tree, \cdots$)

```
1: if tree.n > 1 then
 2:
       Calculate x, y, z mins, maxs, ranges, and partition center
 3:
       Sort data over sortDim = \operatorname{argmax}(x, y, z \text{ ranges})
      Split data: dataL, dataR
 4:
 5:
       if |dataL| > 0 then
 6:
          Create tree L
7:
          buildTree_serial( dataL, tree.L, \cdots )
 8:
      end if
 9.
       if |dataR| > 0 then
10:
          Create tree. R.
11:
          buildTree_serial( dataR, tree.R, \cdots )
12:
       end if
13: else
14:
       Store data (a single point)
15: end if
```

buildTree_parallel performs ORB using a multiple compute nodes

Algorithm 4: buildTree_parallel($data, tree, comm, \cdots$)

- 1: Call getSortDim(\cdots): calculates x,y,z mins, maxs, ranges, partition center, and returns sortDim
- 2: Sort data over sortDim using parallelSort $(data, sortDim, comm, \cdots)$
- 3: if myRank < numNodes/2 then
- 4: Create tree.L. commL
- 5: buildTree_parallel($data, tree.L, comm, \cdots$)
- 6: else
- 7: Create tree.R, commR
- 8: buildTree_parallel($data, tree.R, comm, \cdots$)
- 9: end if

It is assumed that tree.n>1 will never occur in build/tree_parallel since we usually deal with large amounts of data

getSortDim finds the longest axis and stores several key tree fields

Algorithm 5: getSortDim($data, tree, comm, \cdots$)

- 1: Each process gets it local x,y,z min and \max
- 2: Rank 0 receives these, determines the global x,y,z min and max, determines the sortDim, and Bcast's all of these values back to the other nodes
- 3: The global mins/maxs, partition center, and partition radius are stored in tree
- 4: return sortDim

Searching the tree

searchTree_serial returns the number of points within a given radius
about a given point

Algorithm 6: searchTree_serial(tree, rad, point)

```
1: found = 0
2: d = \sqrt{\sum_{i=1}^{3} (point[i] - tree.c[i])^2}
3: if d < rad + tree.rad then
      if tree.L = NULL \&\& tree.R = NULL then
4:
5:
         return 1
6:
     else
7:
         if tree.L != NULL then
8:
            found += searchTree\_serial(tree.L, rad, point)
9:
         end if
10:
         if tree.R = NULL then
11:
            found += searchTree\_serial(tree.R, rad, point)
12:
         end if
13:
      end if
14: end if
```

Searching the tree

search501 reads the 501-st data file and loops through the points
contained within (as well as the three given radii), calling
searchTree_serial for each

Algorithm 7: search501(tree, path, \cdots)

1:

We had to make several significant alterations to our parallelSort program in order to integrate it into our KD tree project

Changes:

- Make rank 0 do work
- Use specified communicator
- Conversion to function
- better adaptBins

Making rank 0 do work:

- Initially, rank 0 was just a master node which coordinated the other worker nodes
- This technique is very inefficient for parallel ORB since it requires us to switch to serial mode sooner
- The solution involved 1) cleverly altering a large number of if statements in the code and 2) changing how certain types of sends/recvs were handled

Using a specified communicator:

- Initially, parallelSort and all of its associated functions used MPI_COMM_WORLD (hard-coded)
- ullet To use a specified communicator comm, it must be passed as an argument into any function that uses it
- This required a simple but tedious process of editing

Here is how parallelSort is structured now that it is a function

Algorithm 8: parallelSort(data, rows, myRank, sortDim, comm, \cdots)

- 1: Locally sort data on each compute node using a qsort
- 2: Determine the global min/max of the sortDim
- 3: Create linearly spaced bin edges over range on rank 0 and Bcast
- 4: Bin the data on each compute node and accumulate on rank 0
- 5: Calculate *uniformity*
- 6: while uniformity < threshold && iterations < M do
- 7: Adapt the bin edges on rank 0 and Bcast
- 8: Bin the data on each compute node and accumulate on rank 0
- 9: Calculate *uniformity*
- 10: end while
- 11: Swap data between compute nodes and do data cleanup

We also wished to modify our original adaptBins function

Old adaptBins:

- Local method
- Based on the normalized gradient of the bin counts
- Scaled so that bin edges remain properly ordered
- New: Scaled to decrease of time to avoid oscillations
- Pros: able to handle nonlinearities in distribution, good at fine-tuning
- **Cons:** edges from from dense regions are slow to converge, slower with more nodes

$$\Delta C = 2.0(C_{i+1}^m - C_i^m)/(C_{i+1}^m + C_i^m)$$

$$\Delta E = E_{i+1}^m - E_i^m$$

$$S(m) = 1 - (1 - 0.1)(1 - \exp(-0.03m)$$

$$E_i^{m+1} = E_i^m + 0.475(S(m)\Delta C\Delta E)$$
(1)

We also wished to modify our original adaptBins function

New adaptBins:

- Global method
- Based on the integrated, linearly interpolated, cumulative distribution
- Bin edges placed where linear interpolation would assume uniformity
- Pros: fast initial convergence in approximately linear regions, same speed with more nodes
- Cons: can oscillate near dense regions

$$\hat{C}(x) = \hat{C}(E_{i'}^m) + C_{i'}^m \frac{x - E_{i'}^m}{E_{i'+1}^m - E_{i'}^m} = (i+1)\frac{D}{N}$$
 (2)

$$E_i^{m+1} = E_{i'}^m + \left((i+1)\frac{D}{N} - C(E_{i'}^m) \right) (E_{i'+1}^m - E_{i'}^m) / C_{i'}^m \tag{3}$$

Since both methods' pros and cons are disjoint, alternating between them gives a method which can outperform either individually

Demos:

- thin dense distribution at boundary, nBins = 2, 3, 10
- wide distribution in center, nBins = 2, 3, 10
- 0

Validation

Validation

MATLAB Demos:

- 2D animation of MATLAB prototype
- 3D visualization at the end of the parallel phase of teh C++ implementation

Validation

Other validation methods:

- Set search sphere center on a data point, use tiny radius, find 1 point
- Set an arbitrary search sphere point, increase radius, points found increases monotonically
- dumpTree writes each compute node's tree to a file for analysis

Results

Conclusions

Challenges

Challenges:

- parallelSort conversions
- memory leaks
- malloc when you should realloc
- multiple communicators (comm)
- adaptBins convergence problems
- debug print statement clutter
- array out of bounds issues
- inconsistent usage pointer-to-pointer calls for *data[] and *rows (due to swapArrayParts)
- no planning for function arguments and return values (constant editing of h-files)
- testing was difficult due to cluster overloading and hardware errors

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Successes

Successes:

- few merge conflicts and fast debugging through extreme coding and Git branches
- visualizing output through MATLAB
- efficient delegation of tasks

Future Work

Future work:

- cloud computing
- use of coding techniques for personal research