

# Neural Networks For People Who Get Confused Easily

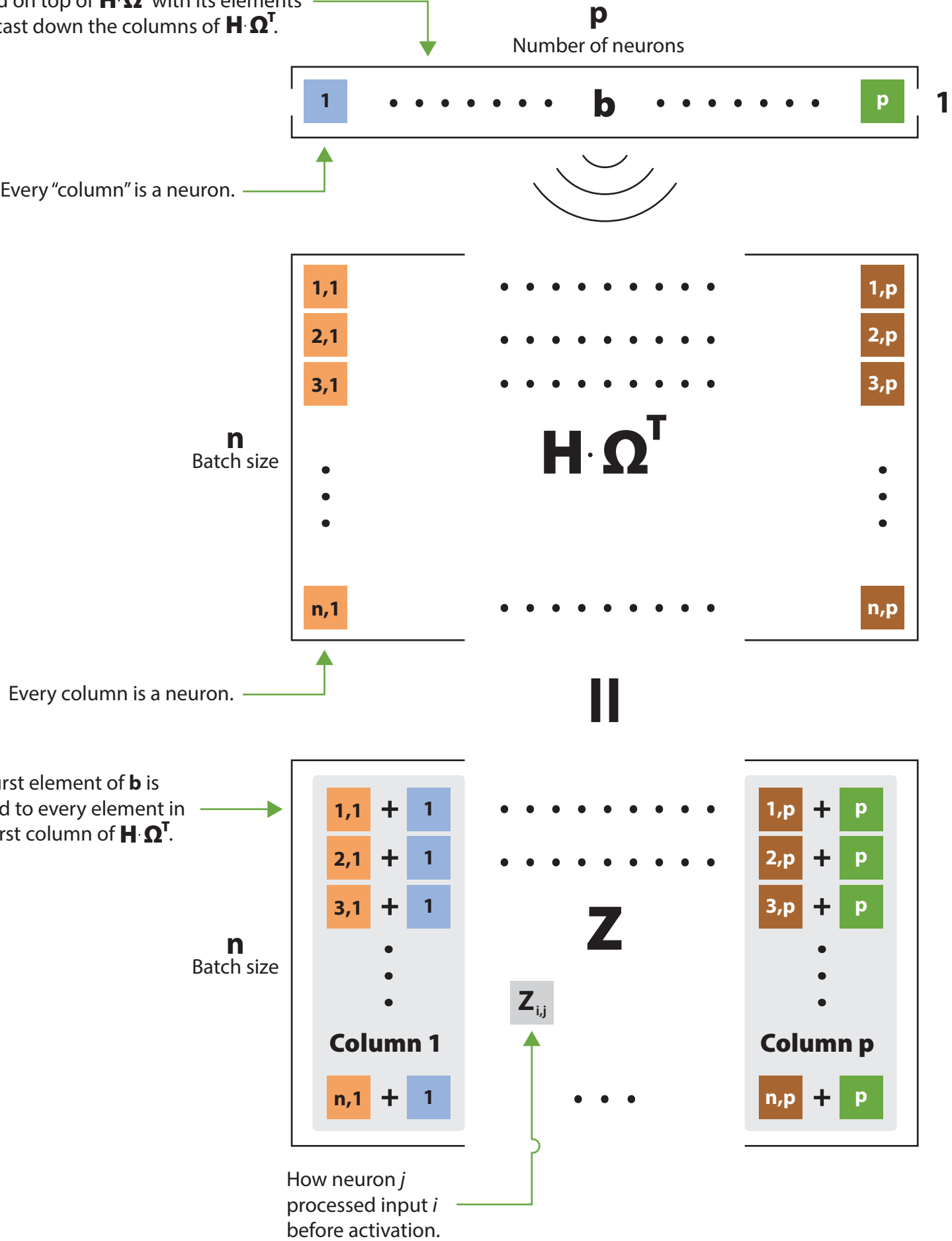


by James McCammon (A fellow who gets confused easily)

## Broadcasting

### How “broadcasting” $\mathbf{b}$ works

It’s useful to think of  $\mathbf{b}$  as a row vector stacked on top of  $\mathbf{H} \cdot \mathbf{\Omega}^T$  with its elements broadcast down the columns of  $\mathbf{H} \cdot \mathbf{\Omega}^T$ .



#### Notes

1. What broadcasting is doing from a mathematical perspective is taking the outer product of  $\mathbf{b}$  and an implicitly defined, usually unshown vector of 1s, denoted as  $\mathbf{1}_n$ , where  $n$  is the same as our batch size. This outer product has the effect of creating a new matrix of the same size as  $\mathbf{H} \cdot \mathbf{\Omega}^T$ . We can then add the terms element wise.

The vector of 1s is constructed to be a column vector. We then transpose  $\mathbf{b}$ . This gives us an  $(n \times 1)$  vector of 1s times  $\mathbf{b}$ , which is  $(1 \times p)$ . The result is a matrix that is  $(n \times p)$ , the same size as  $\mathbf{H} \cdot \mathbf{\Omega}^T$ . The outer product can be thought of using standard matrix multiplication, taking the vectors of 1s as an  $(n \times 1)$  matrix and  $\mathbf{b}$  as an  $(1 \times p)$  matrix. Standard matrix multiplication rules then apply. This new matrix contains the elements of  $\mathbf{b}$  in each row, copied  $n$  times. See the example below for an example.

$$\begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} \otimes \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \end{bmatrix} = \begin{bmatrix} 1 \times 1 & 1 \times 2 & 1 \times 3 & 1 \times 4 & 1 \times 5 \\ 1 \times 1 & 1 \times 2 & 1 \times 3 & 1 \times 4 & 1 \times 5 \\ 1 \times 1 & 1 \times 2 & 1 \times 3 & 1 \times 4 & 1 \times 5 \\ 1 \times 1 & 1 \times 2 & 1 \times 3 & 1 \times 4 & 1 \times 5 \\ 1 \times 1 & 1 \times 2 & 1 \times 3 & 1 \times 4 & 1 \times 5 \end{bmatrix}$$