

# **MAS1802: Computing Project**

Due on Tuesday 14th May at 4:00pm

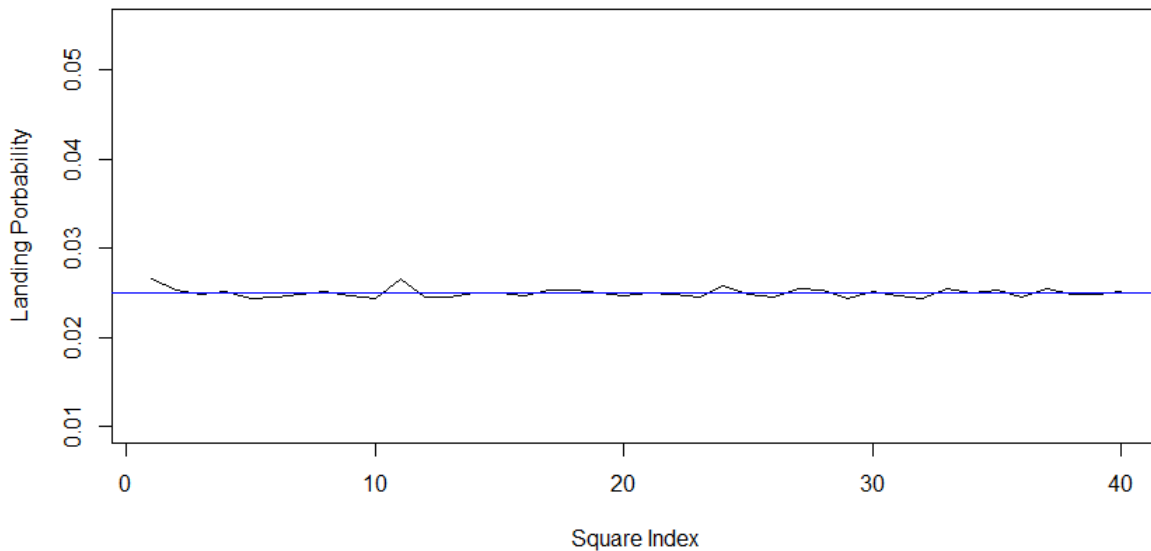
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## Section 1: Monopoly

### Initial Simulation

Below is a plot of `SimulateMonopoly1`, showing a baseline probability of 2.5% to land on any given square.



### Adding further complexity

#### Main Function: `SimulateMonopoly`

The `while` loop on line 6 freezes the roll counter if the player rolls a double as to simulate ‘free rolls’, and to prevent the case of the simulation ending on a double where it is possible two further doubles could result in being sent to jail.

```
1 SimulateMonopoly = function(no_of_rolls) {
2   landings = numeric(40)
3   current = 1
4   doubles = 0
5   for (i in 1:no_of_rolls) {
6     while (TRUE) { # Stops ‘i’ from incrementing on doubles
7       roll = RollTwoDice()
8       if (doubles == 3) {
9         current = 11 # Send to jail on rolling three doubles
10        doubles = 0 # Reset doubles counter
11      } else {
12        current = current + sum(roll)
13        if (roll[1] == roll[2]) {
14          doubles = doubles + 1 # Increment doubles counter on rolling a
15                                double
16        }
17        if (current > 40) {
18          current = current - 40
19        }
20        landings[current] = landings[current] + 1
21        # Community Chests Squares
22        if (current == 3 || current == 18 || current == 34) {
```

```
22         cc_move = CommunityChest(current)
23         if (cc_move != current) {
24             current = cc_move
25             landings[current] = landings[current] + 1
26         }
27     }
28     # Go to Jail
29     if (current == 31) {
30         jail = 11
31         current = jail
32         landings[current] = landings[current] + 1
33     }
34     # Chance Squares
35     if (current == 8 || current == 23 || current == 37) {
36         chance_move = Chance(current)
37         if (chance_move != current) {
38             current = chance_move
39             landings[current] = landings[current] + 1
40         }
41     }
42 }
43 if (roll[1] != roll[2]) {
44     break # Increment 'i' if a non-double is rolled
45 }
46 }
47 }
48 return(landings)
49 }
```

#### Helper Function: Community Chest

```
1 CommunityChest = function(current) {
2     goto = current
3     u = runif(1) # Create random number between 0 and 1
4     if (u < 1 / 16) {
5         goto = 1 # Advance to Go
6     } else if (u < 2 / 16) {
7         goto = 11 # Go to Jail
8     } else if (u < 3 / 16) {
9         goto = 2 # Go to Old Kent Road
10    } else if (u < 4 / 16) {
11        goto = Chance(current) # Take a chance card
12    }
13    return(goto)
14 }
```

**Helper Function: Chance Cards**

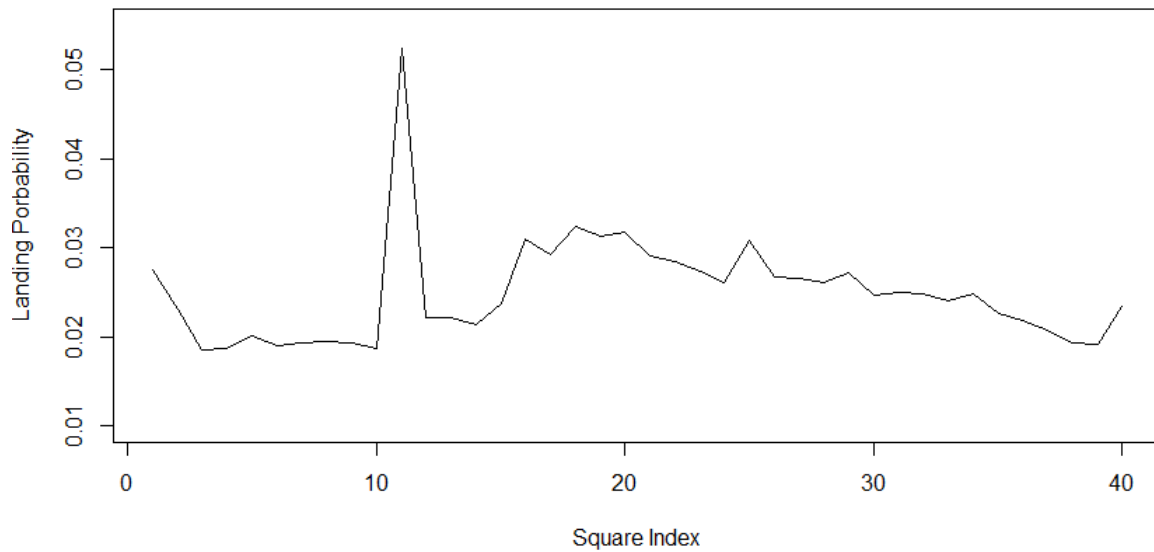
```
1 Chance = function(current) {
2   goto = current
3   u = runif(1) # Create random number between 0 and 1
4   if (u < 1 / 16) {
5     goto = 1 # Advance to Go
6   } else if (u < 2 / 16) {
7     goto = 25 # Advance to Trafalgar Square
8   } else if (u < 3 / 16) {
9     goto = 12 # Advance to Pall Mall
10  } else if (u < 4 / 16) {
11    goto = 11 # Go to Jail
12  } else if (u < 5 / 16) {
13    goto = 16 # Take a trip to Marylebone Station
14  } else if (u < 6 / 16) {
15    goto = 40 # Advance to Mayfair
16  } else if (u < 7 / 16) {
17    if (current >= 1 & current <= 13) {
18      goto = 13 # Advance to nearest utility
19    }
20    if (current >= 14 & current <= 29) {
21      goto = 29 # Advance to nearest utility
22    }
23    if (current >= 30 & current <= 40) {
24      goto = 13 # Advance to nearest utility
25    }
26  } else if (u < 8 / 16) {
27    goto = current - 3 # Go back three spaces
28  }
29  return(goto)
30 }
```

**Helper Function: Rolling Dice**

```
1 RollTwoDice = function() {
2   d1 = sample(1:6, 1)
3   d2 = sample(1:6, 1)
4   roll = c(d1, d2)
5   return(roll)
6 }
```

## Final plot

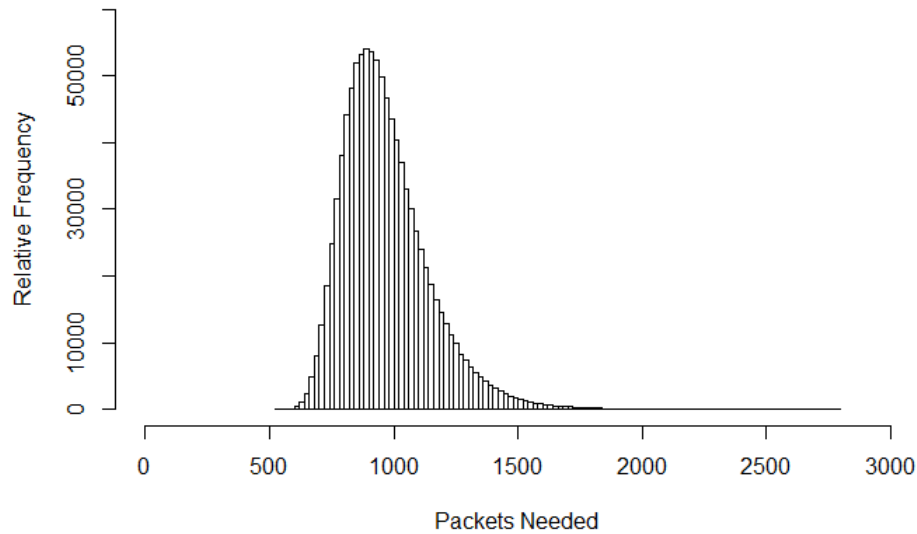
The final plot was carried out with `number_of_rolls=100,000,000`. The final results suggest landing on the Jail square had the highest likelihood, of 6.42%, whereas the lowest likelihood was to land on the Community Chest at square 3, with a probability of 2.27%. The average probability of landing on any given square was still 2.5%, meaning on average it is over twice as likely to land on jail than any other given square.



## Section 2: Sticker Album

### Main Function

Across 1,000,000 simulations, the average amount of packets needed for a full set was 969.417. This would suggest an average cost of £775.53. In these simulations, in the most unlucky case it took 2789 packets to complete a set, totalling £2231.20, and in the luckiest case it took only 538 packets, costing £430.40. The standard deviation for packets needed was 174.15, implying a £139.32 standard deviation for cost.



```

1  sim_number = 1000000
2  packets_bought = vector(length = sim_number)
3
4  sticker_sim = function(sim_number) {
5    for (i in 1:sim_number) {
6      stickers = 1:682 # Sticker sequence, a vector containing an entry for each
7                       # sticker.
8      for (j in 1:10000) { # Open up to 10,000 packs of stickers (arbitrary
9                           # upper limit).
10         packet = sample(1:682, 5, replace = TRUE) # Create a packet from a
11              # random pool 682 of stickers, with replacement.
12
13         for (k in 1:5) { # Pick 5 stickers from the random pool, find the picked
14             # stickers' entry in 'stickers' vector and set to zero.
15             stickers[packet[k]] = 0
16         }
17
18         # If all entries in 'stickers' vector are zero then all stickers have
19         # been collected, stop looping.
20         if (sum(stickers) == 0) {
21             packets_bought[i] = j
22             break
23         }
24     }
25 }

```

```
21     }
22     return(packets_bought)
23 }
24
25 output_vector = sticker_sim(sim_number)
26 sum(output_vector) / sim_number # Outputs average number of packets needed for
    a full set
```