

Identifying Textual Clusters with Non-negative Matrix Factorization

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How Do We Compare Manuscripts?

- Start with collation—aligning texts at *variation units*

ΚΑΤΑ ΛΟΥΚΑΝ		10:1-4
οὐ ἤμελλεν αὐτὸς ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерισμὸς	B K C 1071 uw
οὐ ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	φ ⁷⁵
οὐ ἤμελλεν αὐτὸς <u>εἰσεργεσθαι</u> .	2 ἔλεγεν οὖν πρὸς αὐτούς, Ὁ μὲν θерисμὸς	A
οὐ ἔμελλεν ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ θерисμὸς	D
οὐ ἔμελλεν αὐτὸς ἔρχεσθαι.	2 ἔλεγεν οὖν πρὸς αὐτούς, Ὁ μὲν θерисμὸς	Y K S IT 28 565 τ
οὐ ἔμελλεν αὐτὸς ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	L 124 579
οὐ ἤμελλεν αὐτὸς <u>εἰσεργεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	Θ
οὐ ἔμελλεν αὐτὸς <u>ἀπεργεσθαι</u> .	2 ἔλεγεν οὖν πρὸς αὐτούς, Ὁ μὲν θерисμὸς	Ω
οὐ ἔμελλεν αὐτὸς <u>εἰσεργεσθαι</u> .	2 εἶπεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	f ¹
οὐ ἤμελλεν αὐτὸς <u>διεργεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	f ¹³
οὐ ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	33
οὐ ἤμελλεν αὐτὸς <u>εἰσπορεύεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	157
οὐ ἔμελλεν αὐτὸς <u>πορεύεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θерисμὸς	700 [↓1424
οὐ ἤμελλεν αὐτὸς ἔρχεσθαι.	2 ἔλεγεν οὖν πρὸς αὐτούς, Ὁ μὲν θерисμὸς	Ⲑ M N U W Γ Δ Α Ψ 2
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου τοῦ θерισμοῦ ὅπως		B φ ⁷⁵ uwτ tell
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου τοῦ θерισμοῦ ὅπως <u>ἀν</u>		Y K M Π
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε τοῦ <u>θεοῦ</u> τοῦ θерισμοῦ ὅπως		D*
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε τοῦ κυρίου τοῦ θерισμοῦ ὅπως		D ^c
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου		H
πολύς, οἱ δὲ ητε οὖν τοῦ κυρίου τοῦ θерισμοῦ ὅπως		33
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου τοῦ θерισμοῦ <u>ἵνα</u>		579

(Source: Swanson, *New Testament Greek Manuscripts*, Luke, 183)

How Do We Compare Manuscripts?

- Start with collation—aligning texts at *variation units*

ΚΑΤΑ ΛΟΥΚΑΝ						10:1-4	
		1	2	3			
οὐ ἤμελλεν αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	δὲ πρὸς αὐτούς,	Ὁ μὲν	θερισμός	B & C 1071	uw
οὐ αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	δὲ πρὸς αὐτούς,	Ὁ μὲν	θερισμός	75	
οὐ ἤμελλεν αὐτὸς <u>εἰσερῆσθαι</u> .	2	ἔλεγεν	οὖν πρὸς αὐτούς,	Ὁ μὲν	θερισμός	A	
οὐ ἔμελλεν ἔρχεσθαι.	2	ἔλεγεν	δὲ πρὸς αὐτούς,	Ὁ μὲν	θερισμός	D	
οὐ ἔμελλεν αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	οὖν πρὸς αὐτούς,	Ὁ μὲν	θερισμός	Y K S II 28 565	τ
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οὐ ἤμελλεν αὐτὸς <u>εἰσερῆσθαι</u> .	2	ἔλεγεν	δὲ πρὸς αὐτούς,	Ὁ μὲν	θερισμός	Θ	
οὐ ἔμελλεν αὐτὸς <u>ἀπέρῆσθαι</u> .	2	ἔλεγεν	οὖν πρὸς αὐτούς,	Ὁ μὲν	θερισμός	Ω	
οὐ ἔμελλεν αὐτὸς <u>εἰσερῆσθαι</u> .	2	εἶπεν	δὲ πρὸς αὐτούς,	Ὁ μὲν	θερισμός	f ¹	
οὐ ἤμελλεν αὐτὸς <u>διέρῆσθαι</u> .	2	ἔλεγεν	δὲ πρὸς αὐτούς,	Ὁ μὲν	θερισμός	f ¹³	
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οὐ ἤμελλεν αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	οὖν πρὸς αὐτούς,	Ὁ μὲν	θερισμός	78	M N U W Γ Δ Α Ψ 2
		4	5	6	7		
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	οὖν	τοῦ	κυρίου	τοῦ	θερισμοῦ	ὅπως	B 75 uw t rel
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	οὖν	τοῦ	κυρίου	τοῦ	θερισμοῦ	ὅπως	αν Y K M Π
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	τοῦ	θεοῦ	τοῦ	θερισμοῦ	ὅπως		D*
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	τοῦ	κυρίου	τοῦ	θερισμοῦ	ὅπως		D ^c
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	οὖν	τοῦ	κυρίου		H
πολύς, οἱ δὲ ητε	οὖν	τοῦ	κυρίου	τοῦ	θερισμοῦ	ὅπως	33
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	οὖν	τοῦ	κυρίου	τοῦ	θερισμοῦ	ἵνα	579

How Do We Compare Manuscripts?

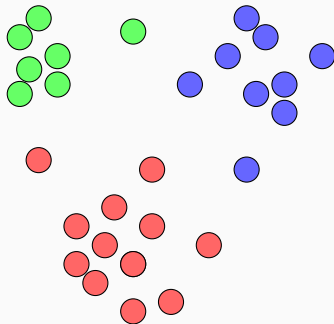
- This provides a simple basis of comparison between pairs of manuscripts
 - Number of units where both agree
 - For a proportion, divide by number of units where the readings of both are known
- “Pre-genealogical coherence” in the Coherence-Based Genealogical Method (CBGM)

Genealogical comparisons for W1 = 5:					
W2	DIR	NR	PASS	EQ	
35	>	4	115	101	(87.826%)
453	>	4	116	101	(87.069%)
03	>	7	116	98	(84.483%)
1611	<		116	98	(84.483%)
88	<		116	97	(83.621%)
1739	>	8	115	97	(84.348%)

- Can we use mutual agreement to classify manuscripts into groups?

The Quantitative Method

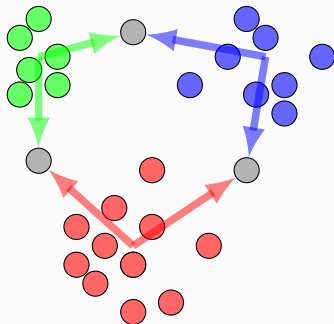
- Colwell and Tune: if manuscripts agree significantly more with one another than they do with other manuscripts, then they form a family, or *text-type*¹
 - $\geq 70\%$ with one another, and $\geq 10\%$ more than with others



1. Colwell and Tune, "Quantitative Relationships."

The Quantitative Method

- Problems:
 - All units (including those involving singular readings and common scribal errors) have equal weight
 - Mixture in the transmission process is a problem²



The Quantitative Method

- For efficiency and accuracy, comparisons should be done on the basis of *informative* points of variation³
- Specific readings, not the variation units containing them
- But how do we know which ones are the most informative?

KATA ΛΟΥΚΑΝ

10.1-4

ΚΑΤΑ ΛΟΥΚΑΝ		1	2	3		10.1
οὐ ἤμελλεν αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	δὲ	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	B K C 1071 uw
οὐ αὐτὸς ἔρχεσθ...	2	ἔλεγεν	δ...	πρὸς αὐ.....	θερ.....	ϕ ⁷⁵
οὐ ἤμελλεν αὐτὸς <u>εἰσεργεσθαι</u> .	2	ἔλεγεν	οὖν	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	A
οὐ <u>ἔμελλεν</u> ἔρχεσθαι.	2	ἔλεγεν	δὲ	πρὸς αὐτούς, 'Ο	θερισμὸς	D
οὐ <u>ἔμελλεν</u> αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	οὖν	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	Y K S Π 28 565 τ
οὐ <u>ἔμελλεν</u> αὐτὸς ἔρχεσθαι.	2	ἔλεγεν	δὲ	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	L 124 579
οὐ ἤμελλεν αὐτὸς <u>εἰσεργεσθαι</u> .	2	ἔλεγεν	δὲ	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	Θ
οὐ <u>ἔμελλεν</u> αὐτὸς <u>ἀπεργεσθαι</u> .	2	ἔλεγεν	οὖν	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	Ω
οὐ <u>ἔμελλεν</u> αὐτὸς <u>εἰσεργεσθαι</u> .	2	εἶπεν	δὲ	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	ϕ ¹
οὐ ἤμελλεν αὐτὸς <u>διεργεσθαι</u> .	2	ἔλεγεν	δὲ	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	ϕ ¹³
οὐ ὅς ἔρχεσθαι.	2	ἔλεγεν	δὲ	πρὸς αὐτούς, 'Ο μὲν	θερισμὸς	33
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πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	4	οὖν	τοῦ	κυρίου	τοῦ θερισμοῦ ὅπως	B ϕ ⁷⁵ uw τ ell
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	5	οὖν	τοῦ	κυρίου	τοῦ θερισμοῦ ὅπως ἂν	Y K M Π
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	6	τοῦ	θεοῦ	τοῦ θερισμοῦ ὅπως	D*	
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	7	τοῦ	κυρίου	τοῦ θερισμοῦ ὅπως	D ^c	
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	8	οὖν	τοῦ	κυρίου ὅπως	H
πολύς, οἱ δὲ ἤτε	9	οὖν	τοῦ	κυρίου	τοῦ θερισμοῦ ὅπως	33
πολύς, οἱ δὲ ἔργαται ὀλίγοι· δεήθητε	10	οὖν	τοῦ	κυρίου	τοῦ θερισμοῦ ἵνα	579

3. Colwell, "Method in Locating."

The Claremont Profile Method

- Start with an established set of manuscript groups⁴
- Filter out variation units involving common types of variation and singular / subsingular readings to get a set of *test passages*
- Readings supported by group manuscripts = the group's *profile*

KATA ΛΟΥΚΑΝ

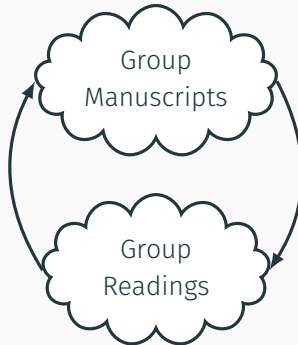
10.1-4

οὐ ἤμελλον αὐτὸς ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θερισιμός	B x C 1071 uw
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οὐ ἤμελλον αὐτὸς <u>εἰσεργεσθαι</u> .	2 ἔλεγεν <u>οὖν</u> πρὸς αὐτούς, Ὁ μὲν θερισιμός	A
οὐ ἔμελλον ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ θερισιμός	D
οὐ ἔμελλον αὐτὸς ἔρχεσθαι.	2 ἔλεγεν <u>οὖν</u> πρὸς αὐτούς, Ὁ μὲν θερισιμός	Y K S IT 28 565 τ
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οὐ ἔμελλον αὐτὸς <u>ἀπεργεσθαι</u> .	2 ἔλεγεν <u>οὖν</u> πρὸς αὐτούς, Ὁ μὲν θερισιμός	Ω
οὐ ἔμελλον αὐτὸς <u>εἰσεργεσθαι</u> .	2 <u>εἶπεν</u> δὲ πρὸς αὐτούς, Ὁ μὲν θερισιμός	f ¹
οὐ ἤμελλον αὐτὸς <u>διεργεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θερισιμός	f ¹³
οὐ ἡμελλεν αὐτὸς ἔρχεσθαι.	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θερισιμός	33
οὐ ἤμελλον αὐτὸς <u>εἰσπορεύεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θερισιμός	157
οὐ ἔμελλον αὐτὸς <u>πορεύεσθαι</u> .	2 ἔλεγεν δὲ πρὸς αὐτούς, Ὁ μὲν θερισιμός	700
οὐ ἤμελλον αὐτὸς ἔρχεσθαι.	2 ἔλεγεν <u>οὖν</u> πρὸς αὐτούς, Ὁ μὲν θερισιμός	[↓1424 M N U W Γ Δ Α Ψ 2
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου τοῦ θερισιμοῦ ὅπως		B 75 uwτ tell
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου τοῦ θερισιμοῦ ὅπως <u>ἂν</u>		Y K M Π
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε τοῦ θεοῦ τοῦ θερισιμοῦ ὅπως		D*
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε τοῦ κυρίου τοῦ θερισιμοῦ ὅπως		H
πολύς, οἱ δὲ ἡμελλεν αὐτὸς ἔρχεσθαι.		33
πολύς, οἱ δὲ ἐργάται ὀλίγοι· δεήθητε οὖν τοῦ κυρίου τοῦ θερισιμοῦ ὅπως		579

4. Wisse, Profile Method.

The Claremont Profile Method

- This allows us to isolate informative readings for group classification
- Also robust to mixture
- But it needs manuscript groups to be established first!
- “Good manuscripts have good readings, and good readings are found in good manuscripts”



Non-negative Matrix Factorization

- *Non-negative matrix factorization* (NMF), a machine learning technique, uses this circular relationship to solve both problems
- Represent our collation as a matrix **A** with a row for each variant reading and a column for each manuscript
- m rows by n columns

		ⲡ ⁷⁵	A	B	D	K	f ¹	579
Unit 1	ἔλεγεν	1	1	1	1	1	0	1
	εἶπεν	0	0	0	0	0	1	0
Unit 2	δὲ	1	0	1	1	0	1	1
	οὐν	0	1	0	0	1	0	0
Unit 3	μὲν	0	1	1	0	1	1	1
	omit	0	0	0	1	0	0	0
Unit 4	οὐν	1	1	1	0	1	1	1
	omit	0	0	0	1	0	0	0
Unit 5	κυρίου	1	1	1	0	1	1	1
	θεοῦ	0	0	0	1	0	0	0
Unit 6	ὅπως	1	1	1	1	1	1	0
	ἵνα	0	0	0	0	0	0	1
Unit 7	omit	1	1	1	1	0	1	1
	ἄν	0	0	0	0	1	0	0

Non-negative Matrix Factorization

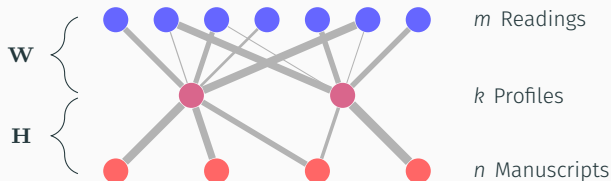
- The goal is to approximate this original matrix as the product of two smaller matrices with non-negative entries:

$$\mathbf{A} \approx \mathbf{WH}$$

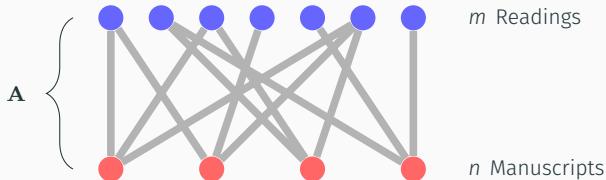
- Specify a number k of underlying textual profiles (there are metrics for finding good choices)
- \mathbf{W} : m rows and k columns; defines group readings
- \mathbf{H} : k rows and n columns; defines makeup of manuscripts in terms of profiles

Non-negative Matrix Factorization

- Use two sets of relationships with a few components...



...to reconstruct the large set of original relationships



Non-negative Matrix Factorization

- The process:
 1. Start with guesses for \mathbf{W} and \mathbf{H}
 2. Fix \mathbf{W} , optimize the weights in \mathbf{H} (Quantitative Method)
 3. Fix \mathbf{H} , optimize the weights in \mathbf{W} (Claremont Profile Method)
 4. Repeat steps 2 and 3 until the difference between \mathbf{A} and \mathbf{WH} no longer decreases



- Guaranteed to terminate with *locally optimal* groupings in \mathbf{W} and \mathbf{H}^5

5. Grippo and Sciandrone, "On the Convergence."

Results: Jude

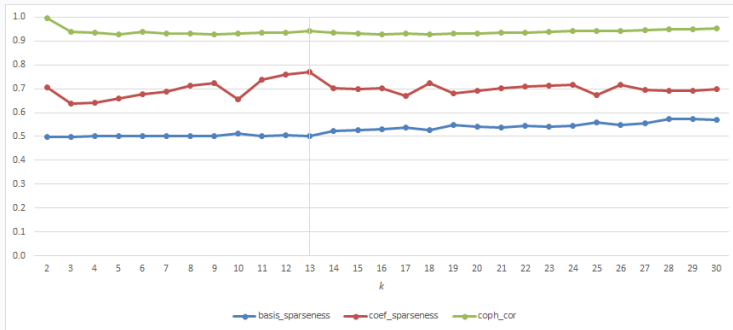
- Tommy Wasserman's collation of Jude contains 1346 variant readings and 560 manuscripts (including lectionaries)⁶
- Filtering out 42 fragmentary manuscripts (< 300 known readings) yields a matrix **A** with $m = 1346$ rows and $n = 518$ columns
- The fragmentary manuscripts can be classified after groups are established⁷

6. Wasserman, *The Epistle of Jude*.

7. For details, see the appendix of McCollum, "Biclustering Readings and Manuscripts."

Results: Jude

- We select the number of profiles k based on several factors:
 - Overlap of readings in profiles
 - Mixture of profiles in manuscripts
 - Consistency of manuscript groupings when random starting points are used (the *cophenetic correlation coefficient*)⁸



8. Brunet et al., “Metagenes and Molecular Pattern Discovery.”

Results: Jude

- The $k = 13$ groups identified by NMF correspond to groups in the Catholic Epistles identified in the literature

Members (by Gregory-Aland number)	Group
920, 1277, 1859, 1719, 452, 1857, 1871, 941, 1103, 1352, etc.	K (von Soden)
141, 204, 394, 444, 1101, 1723, 1737, 1752, 1865, 2221, etc.	K ^r (von Soden)
390, 1863, 912, 234, 1861, 2085, 1753, 2279, 42, 996, etc.	K ^c (von Soden)
L606, L938, L145, L840, L740, L2106, L2394, L809, L1279, L62, etc.	Lectionary (Colwell)
606, 454, 641, 103, 221, 2125, 314, 250, 1888, 393, etc.	O, Θδ Commentaries (von Soden)
619, 1780, 1175, 330, 1769, 2516, 917, 451, 1162, 601, etc.	f ¹⁷⁸⁰ (unidentified)
1563, 1718, 1425, 1359, 1066, 0142, 056	f ⁰¹⁴² (unidentified)

Results: Jude

- The $k = 13$ groups identified by NMF correspond to groups in the Catholic Epistles identified in the literature

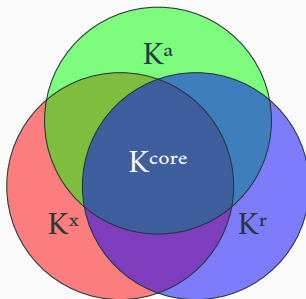
Members (by Gregory-Aland number)	Group
03, 623, \mathfrak{P}^{72} , 81, 5, 326, 33, 1837, 93, 665, etc.	H (von Soden)
321, 918, 307, 453, 2197, 2818, 1678, 94, 2186, 1840, etc.	f^{453} (Spencer, Wachtel, Howe)
323, 1241, 322, 1739, 1881, 2298, 6	f^{1739} (Zuntz, Geer)
1505, 2495, 1611, 1292, 630, 2200, 1765, 1832, 2494, 876, etc.	f^{2138} /Harklean (Amphoux)
1843, 1869, 506, 1903, 489, 927, 203, 1868, 1729, 1873, etc.	I (von Soden)
915, 88, 459, 104, 1846, 1838, 1842, 1845	f^{915} (unidentified)

- Applying NMF to Morrill's collation of all continuous-text manuscripts of John 18 illustrates some of the idiosyncrasies of the method and how to deal with them⁹
- Significantly larger and more “square” collation: $m = 1545$ variant readings and $n = 1610$ manuscripts after filtering out fragmentary manuscripts (< 350 known readings)
- (Recall that the collation matrix for Jude was 1346×518)

9. Morrill, “Complete Collation and Analysis.”

Results: John 18

- Applying NMF to the matrix as-is separates readings common to multiple groups into their own “core” profiles
- No manuscripts belong to these profiles, but many appear “mixed” with it
- Symptom of volume and similarity of manuscripts, especially Byzantine ones

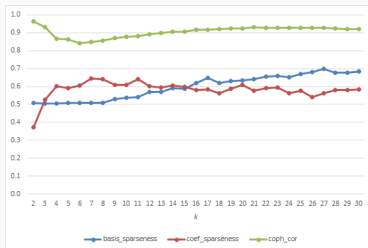


Results: John 18

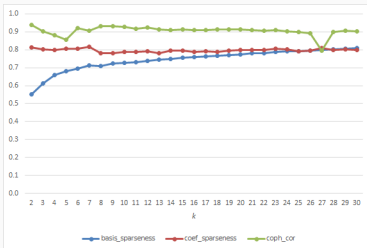
- To remedy this, weigh readings in the original matrix by their *inverse document frequency* (IDF)¹⁰

$$\log \frac{n}{\#\{\text{MSS with reading}\}}$$

- Removing singular readings is helpful in this setting
- Encourages NMF to isolate unique group readings in profiles



No weighting



IDF weighting

10. Jones, "Statistical Interpretation."

- With $k = 12$, NMF identifies known groups from the literature

Members (by Gregory-Aland number)	Group
2605, 492, 1215, 2897, 1090, 1567, 1210, 851, 494, 2406, etc.	K^x (von Soden)
47, 1126, 61, 1138, 58, 56, 189, 1236, 825, 1614, etc.	K^r (von Soden)
2902, 1219, 1079, 489, 114, 2404, 389, 2193, 699, 1627, etc.	K^a (von Soden)
1534, 741, 857, 744, 2735, 1160, 817, 1261, 2470, 833, etc.	Θ_ε Commentaries (von Soden)
892, 977, 555, 16, 152, 513, 1243, 829, 348, 1579, etc.	$f^{16} + f^{1216}$ (Wisse)
1663, 1413, 2291, 86, 569, 71, 1170, 1014, 1531, 2705, etc.	M27+Cl1531 (Wisse)

Results: John 18

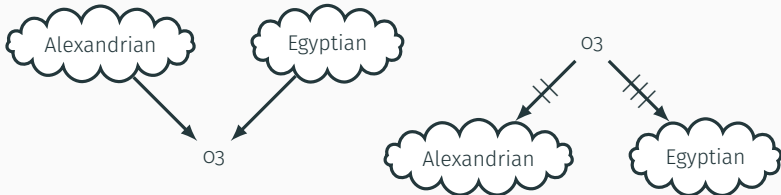
- With $k = 12$, NMF identifies known groups from the literature

Members (by Gregory-Aland number)	Group
01, 032, 05, 579, 1654, 2561, 1242	Egyptian
1820, 2129, 865, 033, 019, 1819, 213, 03, 33, 1321, etc.	Alexandrian
1, 1582, 357, 138, 565, 209, 994, 2713, 2575, 1784, etc.	f^1 (Lake)
13, 788, 826, 828, 543, 69, 346, 1689, 124, 2786, etc.	f^{13} (Lake and Lake, Geerlings)
2524, 1001, 1268, 2397, 352, 2728, 132, 175, 1701, 2252, etc.	Cl1001+Cl352 (Wisse)
1446, 1050, 706, 1457, 827, 2620, 1128, 0211, 2707, 1402, etc.	Cl827 (Wisse)

Concluding Observations

- In John 18, Gregory-Aland 03 (Codex Vaticanus, B) stands out as an instructive example
- Appears to be mixed between the “Egyptian” and “Alexandrian” profiles, but could preserve a text earlier than both
- NMF identifies relationships, but not their directions
- Pre-genealogical, but not genealogical

	"03"
Kx	0.0290
Cl1001+Cl352	0.0000
Theophylact	0.0000
f13	0.0000
f1	0.0000
Alexandrian	1.1248
Egyptian	1.0556
Kr	0.0000
Ka	0.0000
M27+Cl1531	0.0000
f16+f1216	0.0000
Cl827	0.0000



Concluding Observations

- The advantage: few assumptions and editorial decisions are required
- Intended for use in “pre-processing” (manuscript and test reading selection)
- Useful for other applications (new manuscript classification)
- Work in progress: applying NMF to ~2000 manuscripts in the *pericope adulterae* (with Maurice A. Robinson)

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