

Understanding Asymmetric Encryption Algorithms

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Abstract—This paper contains information on how various cryptology algorithms work including RSA public key encryption, ElGamal asymmetric cryptology and Elliptic Curve public key encryption.

I. INTRODUCTION

Writing an introduction sentence is hard.

A. Types of Encryption

1) *Asymmetric Encryption*: Asymmetric encryption is also known as public key cryptography. These public key systems work by having a public key and a private key. The duty of the public key is to encrypt a message. The encrypted message is only able to be decrypted by an appropriate private key. One major down side of public key systems is that creating the key tends to be computationally expensive.

2) *Symmetric Encryption*: Symmetric encryption uses a single key for encryption and decryption. The keys on both sides are not always identical but both can encrypt and decrypt a message. Typically a symmetric encryption uses one of two methods stream ciphers or block ciphers. Stream ciphers encrypt data as it comes typically a few bytes at a time. For block ciphers a number of bits is taken at a time and is encrypted. If the data is too small to fit into a block it is padded so that it can fit into a block. Some common algorithms that use symmetric encryption are AES and blowfish.

3) *Hashing*: Do we want to talk about hashing? Hashing isn't exactly a method of encryption but uses encryption ideas to create secure fields. could be used for more filler maybe?

4) *Hybrid Cryptosystems*: These kinds of cryptosystems give us the best of both asymmetric and symmetric encryption methods. TODO talk about hybrid systems

B. Dependant Algorithms

There are many algorithms that different forms of cryptography rely on. This could be like an appendix type area maybe? I want to try and keep the algorithm talk less cluttered by talking about the parts they depend on first. then in the algorithm section we can focus on that we already explained what the underlying parts are here is the algorithm.

1) *AKS Primality Test*: Do we need to go into detail of algorithms that our algorithm is Dependant on? Maybe we make this section to help fill space up and make us look smart?

2) *Cyclic Groups*: integer and modular addition $-_i$ related to eulers totient function what all of rsa is based on more or less define gcd and modular exponentiation cyclic groups are also used by elgamal i have discovered

3) *Euler's Totient Function*: used in the rsa algorithm for something

4) *Padding Schemes*: I bet a lot of these will need padding schemes and we should probably have a talk about this

5) *Extended Euclidean Algorithm*: This is used in rsa for creating a decryption key

II. RSA ASYMMETRIC CRYPTOGRAPHY

The RSA asymmetric cryptography algorithm is named after its creators Ron Rivest, Adi Shamir and Leonard Adleman and was first thought of in 1973. At the time it was highly classified and wasn't declassified until 1997. The idea behind this algorithm is to use large prime numbers to create a public key and a private key.

A. Private and Public Key Generation

The key generation process is a five step process.

1) *Creating Large Prime Numbers*: First we calculate two large prime numbers using the AKS Test. These will be denoted p and q . We want both of these values to be relatively the same length digit wise but it can differ a bit.

2) *Compute n* : Computing n is just the product of p and q . The value of n will be used as the modulus for our keys and it's length is known as the key length.

$$n = p * q$$

3) *Compute Euler's Totient Function*: Now we must use Euler's totient function to give us a max value for our public key e . Luckily we are able to use algebra to make computing this value much easier.

$$\phi(n) = \phi(p) \phi(q) = (p-1)(q-1) = n - (p+q-1)$$

4) *Create Public Key*: Now we need to create a value for e which will be our public key exponent for encrypting a message. For this value we want to use a reasonably small value without it being too small.

$$1 < e < \phi(n)$$

5) *Create Private Key*: Lastly since we have generated a value for e we will create d which will be used for decryption. To generate d we compute the modular multiplicative inverse of e (modulo $\phi(n)$). This value is commonly computed using the Extended Euclidean Algorithm. This is represented by the equation below.

$$d \equiv e^{-1} \pmod{\phi(n)}$$

B. *Encrypting and Decrypting a Message*

With the values of e and d determined the next step is to use this key pair to encrypt and decrypt a cipher text. To start a message we need to convert it's text into a number. This is done by the use of ASCII values and by using an agreed upon padding scheme. To compute a ciphertext c we use the following equation.

$$c \equiv m^e \pmod{n}$$

TODO finish writing how to decrypt a message for RSA

C. *Example of Usage*

To start with an example we will need to prime numbers to act as our p and q . Let $p = 31583$ and $q = 33857$. This makes the value of $n = 1069305631$ which we can use to compute our Euler's totient so $\phi(n) = 1069240192$. With these values created a public and private key can be created. Let $e = 69240875$ which was arbitrarily chosen and now d is computed. Using the extended Euclidean algorithm to compute the modular multiplicative inverse we get $d = 359143683$. The values of d and e are our private and public keys respectively and can now be used for message encryption/decryption. Let our plain text message $m = \text{"Hello"}$. First we use an ASCII table to determine the value of m as a large integer. A simple way to do this is to concatenate each ASCII value together to form the integer. So let $m = 72101108108111$

D. *Security Concerns*

III. ELGAMAL ASYMMETRIC CRYPTOGRAPHY

A. *Private and Public Key Generation*

B. *Example of Usage*

C. *Security Concerns*

IV. ELLIPTIC CURVE ASYMMETRIC CRYPTOGRAPHY

A. *Private and Public Key Generation*

B. *Example of Usage*

C. *Security Concerns*

V. COMPARISON

Here would be a good spot to compare and contrast all of them. this is the area that i think he wants us to focus on but I don't know

VI. CONCLUSION

The conclusion goes here.

ACKNOWLEDGMENT

I don't plan on having acknowledgments but since it is in the template i will leave it here for now

VII. REFERENCES

<http://mathworld.wolfram.com/CyclicGroup.html>
<http://www.cs.princeton.edu/dsri/modular-inversion-answer.php>