

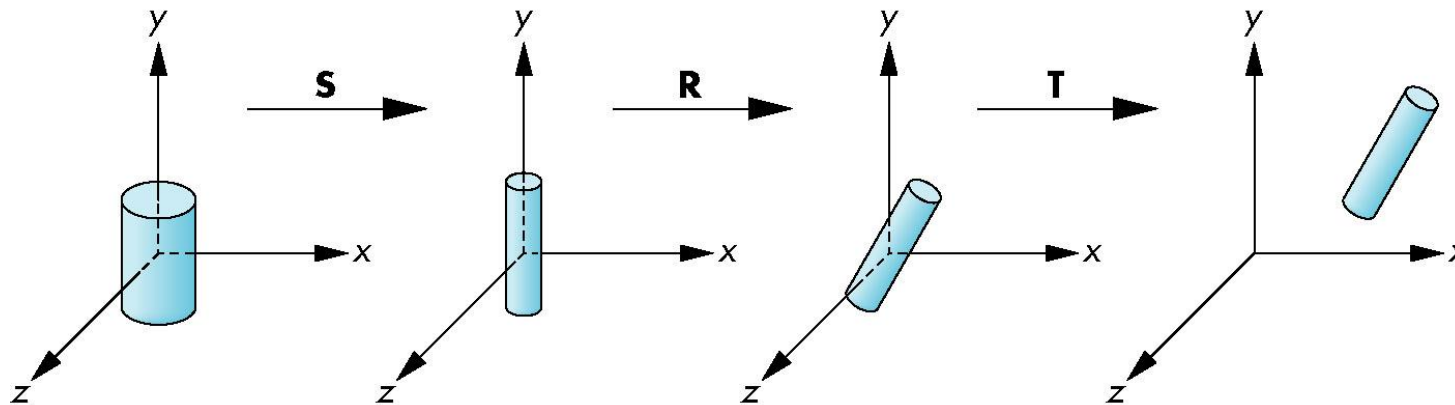
Hierarchical Modeling

14TH WEEK, 2022



Instance Transformation

- Start with a prototype object (a symbol)
- Each appearance of the object in the model is an instance
 - Must scale, orient, position
 - Defines instance transformation



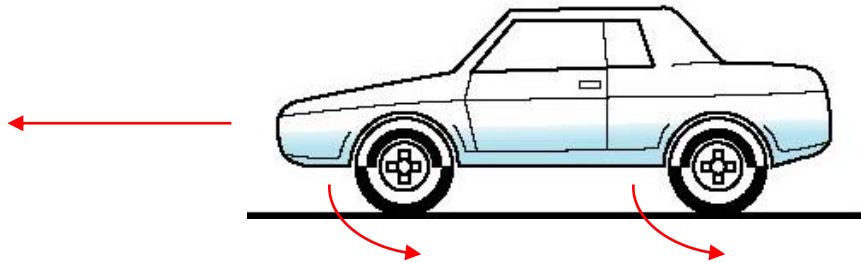
Symbol-Instance Table

- Can store a model by assigning a number to each symbol and storing the parameters for the instance transformation

Symbol	Scale	Rotate	Translate
1	s_x, s_y, s_z	$\theta_x, \theta_y, \theta_z$	d_x, d_y, d_z
2			
3			
1			
1			
.			
.			

Relationships in Car Model

- Symbol-instance table does not show relationships between parts of model
- Consider model of car
 - Chassis + 4 identical wheels
 - Two symbols
- Rate of forward motion determined by rotational speed of wheels



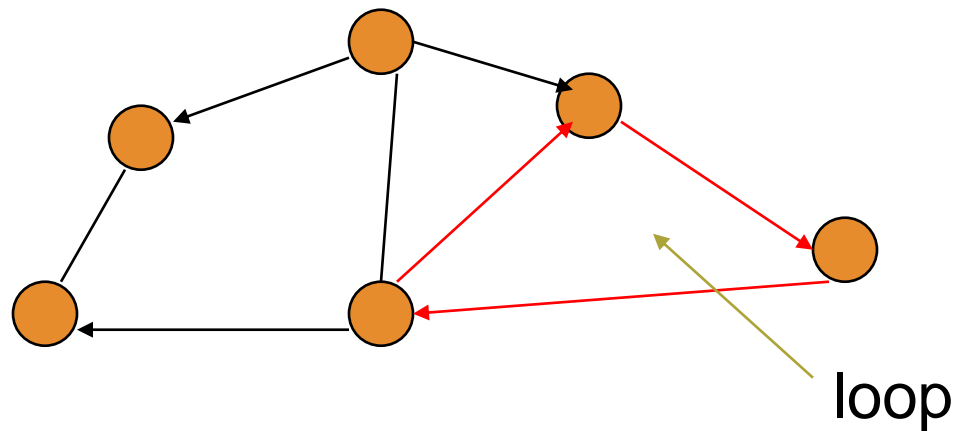
Structure Through Function Calls

```
car(speed)
{
    chassis()
    wheel(right_front);
    wheel(left_front);
    wheel(right_rear);
    wheel(left_rear);
}
```

- Fails to show relationships well
- Look at problem using a graph

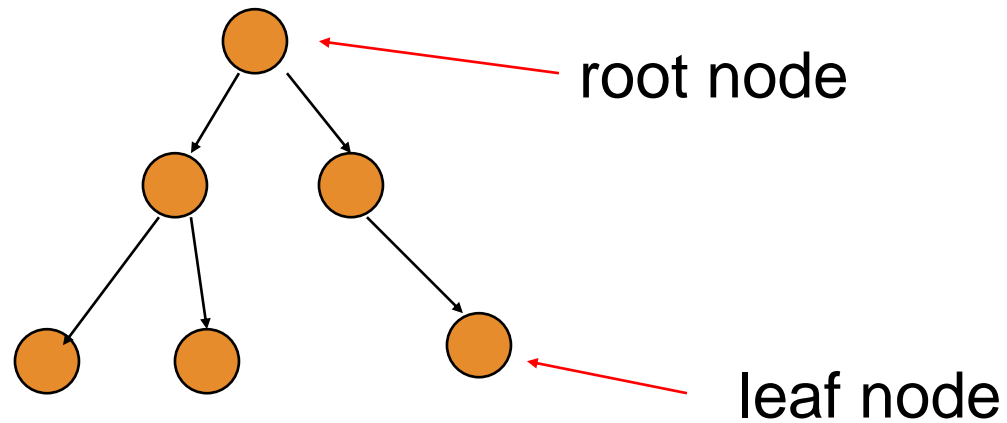
Graphs

- Set of nodes and edges (*links*)
- Each connects a pair of nodes
 - Directed or undirected
- Cycle: directed path that is a loop

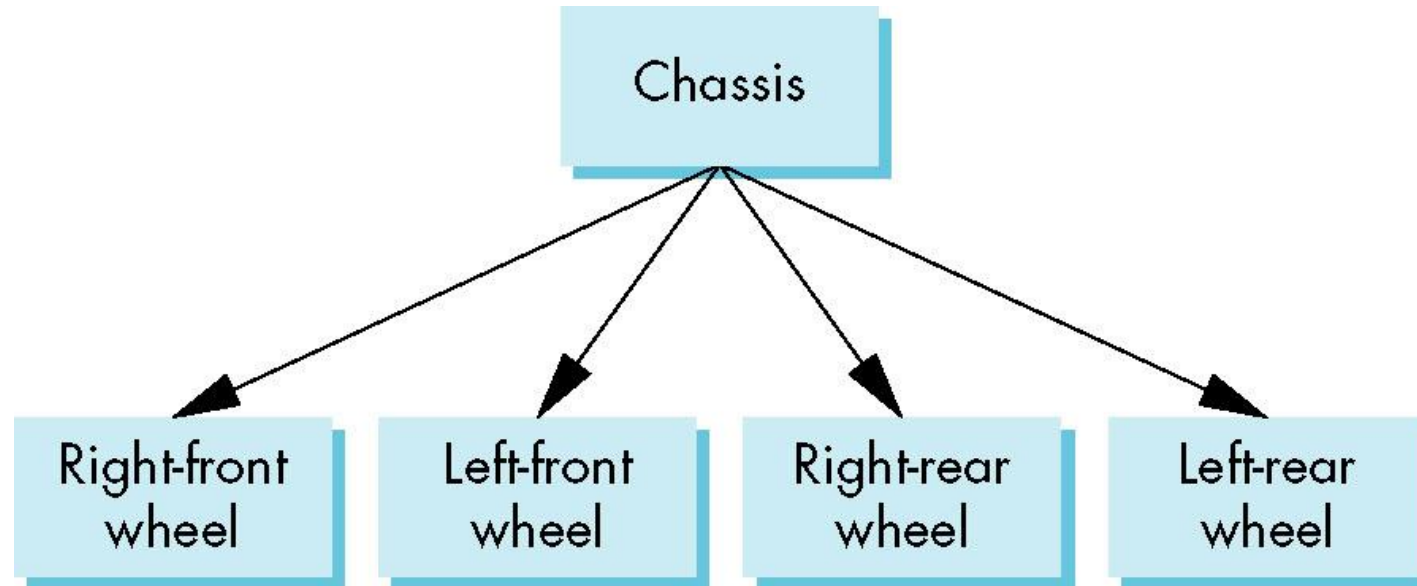


Trees

- Graph in which each node (except the root) has exactly one parent node
 - May have multiple children
 - Leaf or terminal node: no children

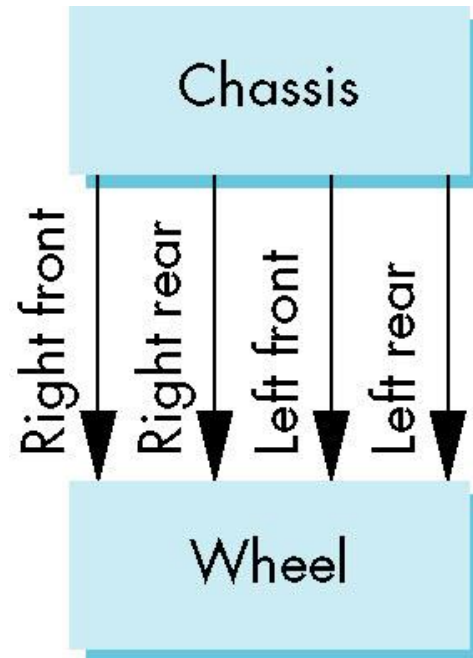


Tree Model of Car



DAG Model

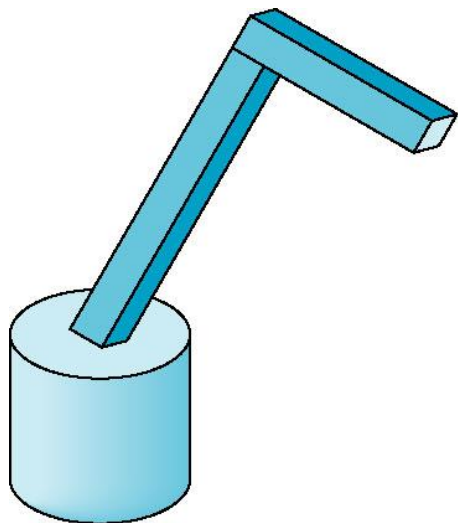
- If we use the fact that all wheels are identical, we get a directed acyclic graph
 - Not much different than dealing with a tree



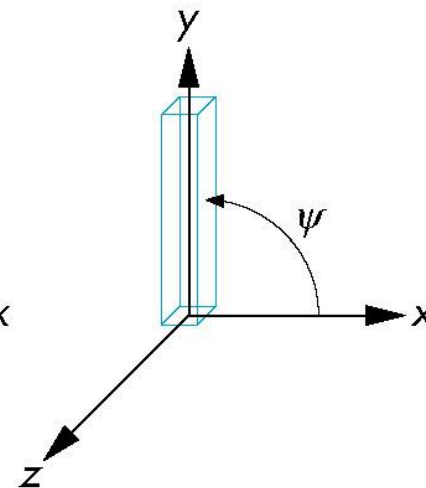
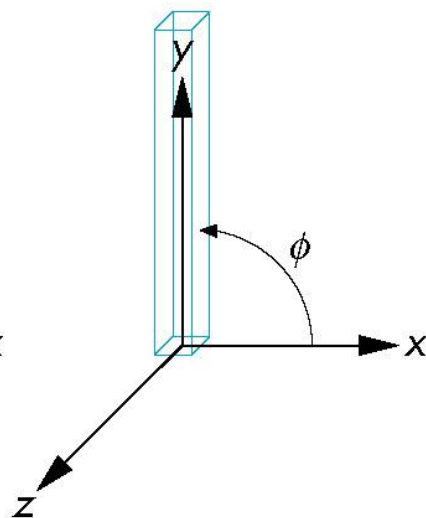
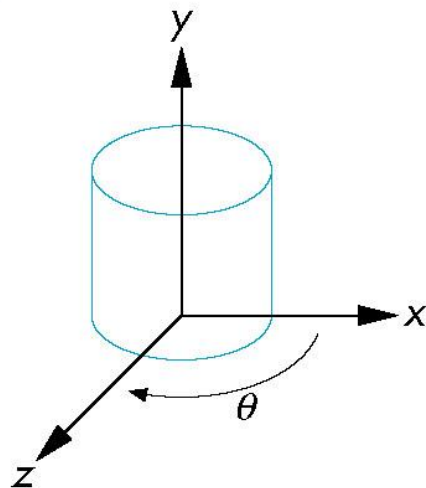
Modeling with Trees

- Must decide what information to place in nodes and what to put in edges
- Nodes
 - What to draw
 - Pointers to children
- Edges
 - May have information on incremental changes to transformation matrices (can also store in nodes)

Robot Arm



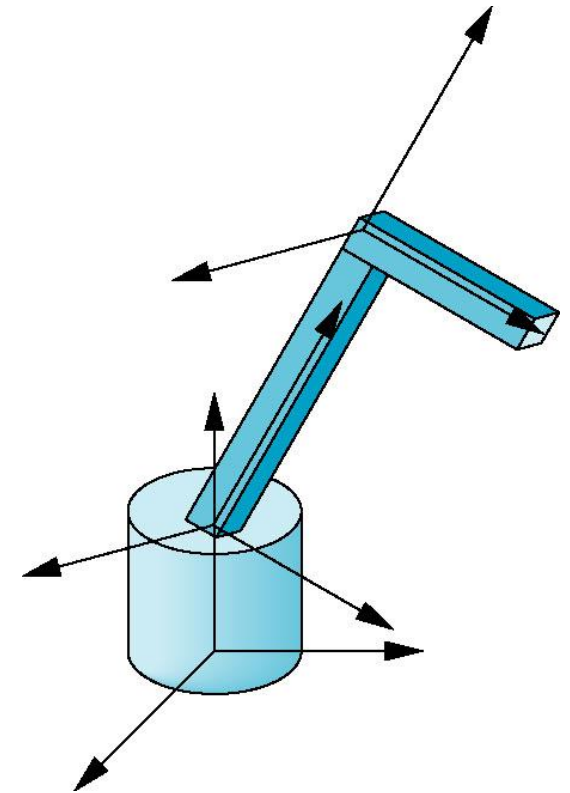
robot arm



parts in their own
coordinate systems

Articulated Models

- Robot arm is an example of an articulated model
 - Parts connected at joints
 - Can specify state of model by giving all joint angles



Relationships in Robot Arm

- Base rotate independently
 - Single angle determines position
- Lower arm attached to base
 - Its position depends on rotation of base
 - Must also translate relative to base and rotate about connecting joint
- Upper arm attached to lower arm
 - Its position depends on both base and lower arm
 - Must translate relative to lower arm and rotate about joint connecting to lower arm

Required Matrices

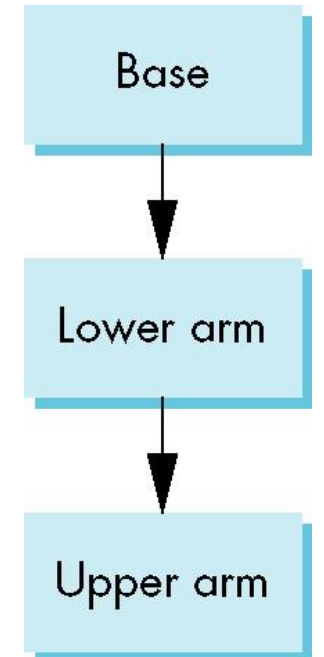
- Rotation of base: \mathbf{R}_b
 - Apply $\mathbf{M} = \mathbf{R}_b$ to base
- Translate lower arm relative to base: \mathbf{T}_{lu}
- Rotate lower arm around joint: \mathbf{R}_{lu}
 - Apply $\mathbf{M} = \mathbf{R}_b \mathbf{T}_{lu} \mathbf{R}_{lu}$ to lower arm
- Translate upper arm relative to lower arm: \mathbf{T}_{uu}
- Rotate upper arm around joint: \mathbf{R}_{uu}
 - Apply $\mathbf{M} = \mathbf{R}_b \mathbf{T}_{lu} \mathbf{R}_{lu} \mathbf{T}_{uu} \mathbf{R}_{uu}$ to upper arm

WebGL Code for Robot

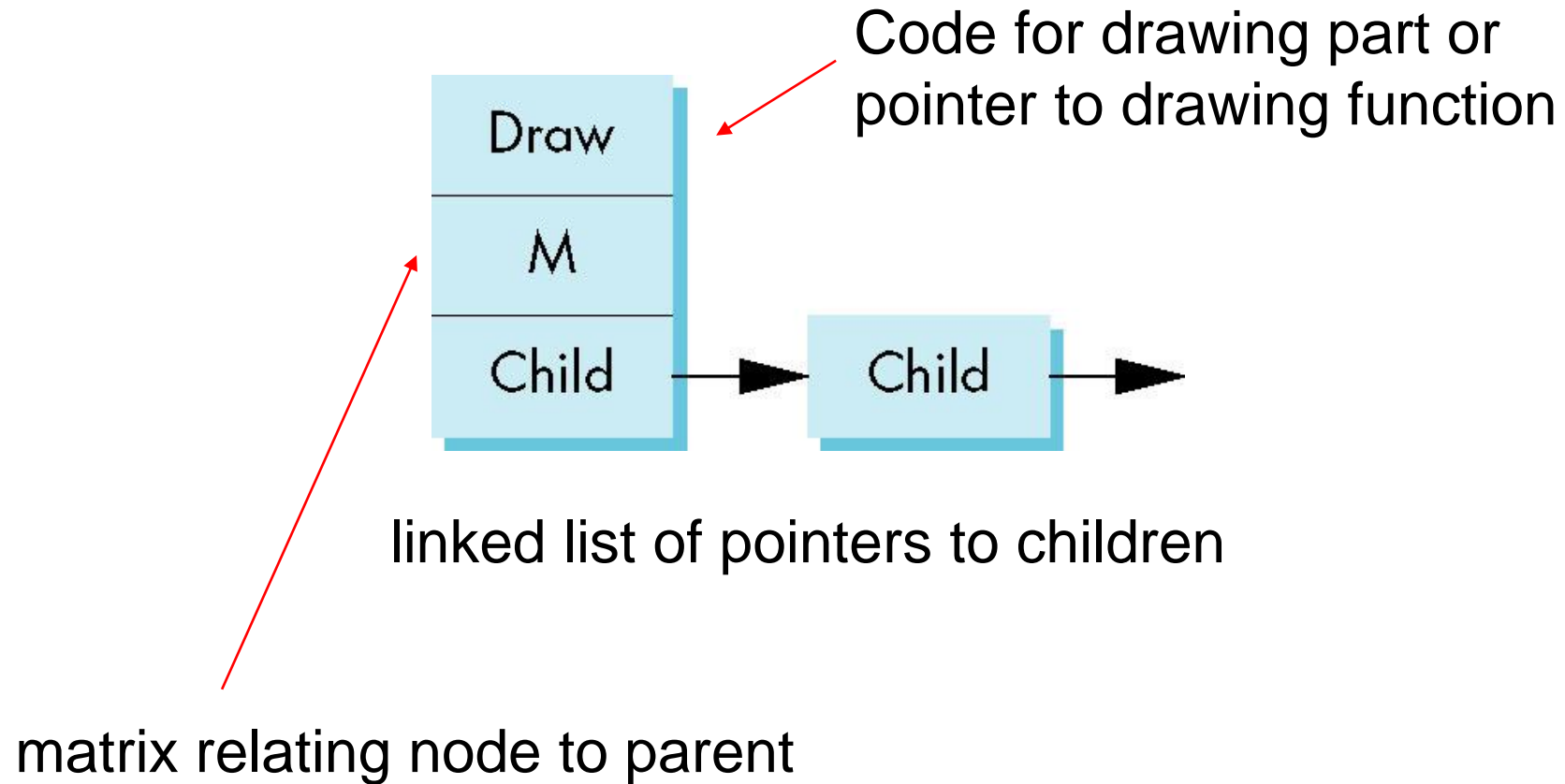
```
var render = function() {  
    gl.clear( gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT );  
  
    modelViewMatrix = rotate(theta[Base], 0, 1, 0 );  
    base();  
  
    modelViewMatrix = mult(modelViewMatrix, translate(0.0, BASE_HEIGHT, 0.0));  
    modelViewMatrix = mult(modelViewMatrix, rotate(theta[LowerArm], 0, 0, 1 ));  
    lowerArm();  
  
    modelViewMatrix = mult(modelViewMatrix, translate(0.0, LOWER_ARM_HEIGHT, 0.0));  
    modelViewMatrix = mult(modelViewMatrix, rotate(theta[UpperArm], 0, 0, 1 ));  
    upperArm();  
  
    requestAnimationFrame(render);  
}
```

Tree Model of Robot

- Note code shows relationships between parts of model
 - Can change “look” of parts easily without altering relationships
- Simple example of tree model
- Want a general node structure for nodes



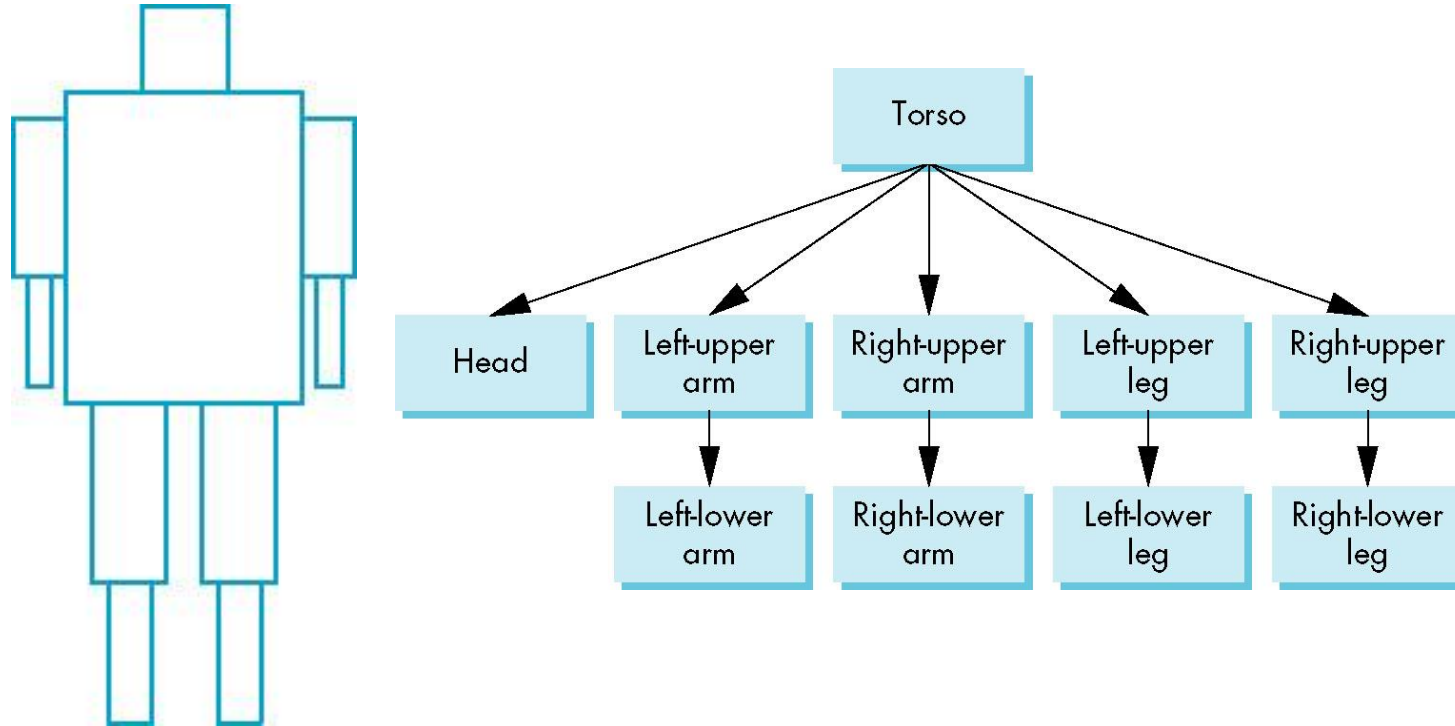
Possible Node Structure



Generalizations

- Need to deal with multiple children
 - How do we represent a more general tree?
 - How do we traverse such a data structure?
- Animation
 - How to use dynamically?
 - Can we create and delete nodes during execution?

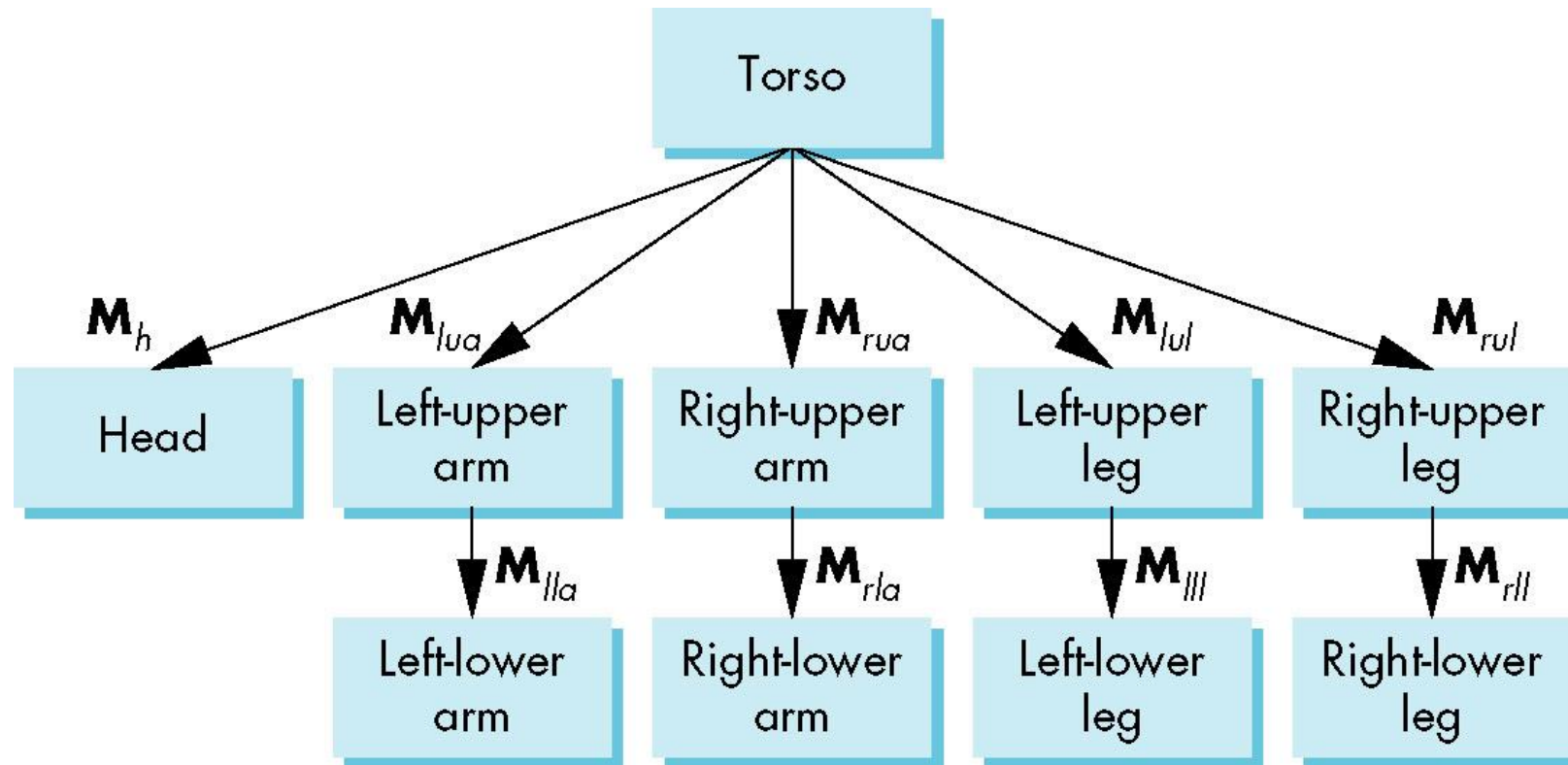
Humanoid Figure



Building the Model

- Can build a simple implementation using quadrics: ellipsoids and cylinders
- Access parts through functions
 - `torso()`
 - `leftUpperArm()`
- Matrices describe position of node with respect to its parent
 - \mathbf{M}_{lla} positions left lower leg with respect to left upper arm

Tree with Matrices



Display and Traversal

- The position of the figure is determined by 11 joint angles (two for the head and one for each other part)
- Display of the tree requires a graph traversal
 - Visit each node once
 - Display function at each node that describes the part associated with the node, applying the correct transformation matrix for position and orientation

Transformation Matrices

- There are 10 relevant matrices
 - \mathbf{M} positions and orients entire figure through the torso which is the root node
 - \mathbf{M}_h positions head with respect to torso
 - \mathbf{M}_{lua} , \mathbf{M}_{rua} , \mathbf{M}_{lul} , \mathbf{M}_{rul} position arms and legs with respect to torso
 - \mathbf{M}_{lla} , \mathbf{M}_{rla} , \mathbf{M}_{lll} , \mathbf{M}_{rll} position lower parts of limbs with respect to corresponding upper limbs

Stack-based Traversal

- Set model-view matrix to \mathbf{M} and draw torso
- Set model-view matrix to \mathbf{MM}_h and draw head
- For left-upper arm need \mathbf{MM}_{lua} and so on
- Rather than recomputing \mathbf{MM}_{lua} from scratch or using an inverse matrix, we can use the matrix stack to store \mathbf{M} and other matrices as we traverse the tree

Traversal Code

```
figure() {  
    PushMatrix() ← save present model-view matrix  
    torso();  
    Rotate (...) ← update model-view matrix for head  
    head();  
    PopMatrix() ← recover original model-view matrix  
    PushMatrix(); ← save it again  
    Translate(...);  
    Rotate (...) ← update model-view matrix  
                    for left upper arm  
    left_upper_arm();  
    PopMatrix(); ← recover and save original  
                  model-view matrix again  
    PushMatrix();  
                    ← rest of code  
}
```

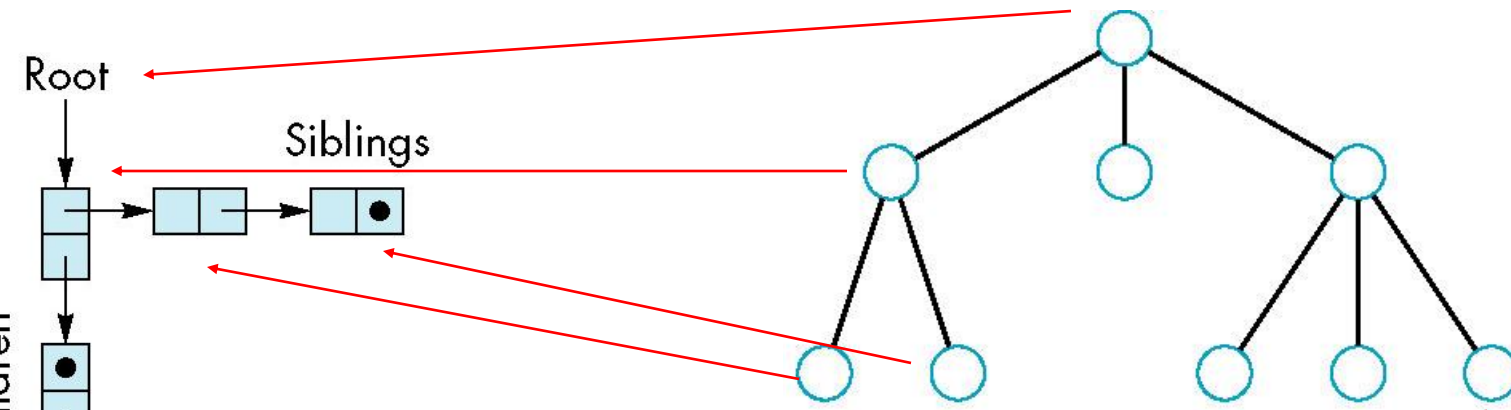
Analysis

- The code describes a particular tree and a particular traversal strategy
 - Can we develop a more general approach?
- Note that the sample code does not include state changes, such as changes to colors
 - May also want to push and pop other attributes to protect against unexpected state changes affecting later parts of the code

General Tree Data Structure

- Need a data structure to represent tree and an algorithm to traverse the tree
- We will use a left-child right-sibling structure
 - Uses linked lists
 - Each node in data structure is two pointers
 - Left: next node
 - Right: linked list of children

Left-Cl



Tree Node Structure

- At each node we need to store
 - Pointer to sibling
 - Pointer to child
 - Pointer to a function that draws the object represented by the node
 - Homogeneous coordinate matrix to multiply on the right of the current model-view matrix
 - Represents changes going from parent to node
 - In WebGL this matrix is a 1D array storing matrix by columns

Creating a Tree Node

```
function createNode(transform, render, sibling, child)
{
    var node = {
        transform: transform,
        render: render,
        sibling: sibling,
        child: child,
    }
    return node;
};
```

Initializing Nodes

```
function initNodes(Id) {  
    var m = mat4();  
    switch(Id) {  
        case torsoId:  
            m = rotate(theta[torsoId], 0, 1, 0);  
            figure[torsoId] = createNode(m, torso, null, headId);  
            break;  
        case head1Id:  
        case head2Id:  
            m = translate(0.0, torsoHeight+0.5*headHeight, 0.0);  
            m = mult(m, rotate(theta[head1Id], 1, 0, 0));  
            m = mult(m, rotate(theta[head2Id], 0, 1, 0));  
            m = mult(m, translate(0.0, -0.5*headHeight, 0.0));  
            figure[headId] = createNode(m, head, leftUpperArmId, null);  
            break;  
    }  
}
```

Notes

- The position of figure is determined by 11 joint angles stored in **theta[11]**
- Animate by changing the angles and redisplaying
- We form the required matrices using rotate and translate
- Because the matrix is formed using the model-view matrix, we may want to first push original model-view matrix on matrix stack

Preorder Traversal

```
function traverse(Id) {
    if(Id == null) return;
    stack.push(modelViewMatrix);
    modelViewMatrix = mult(modelViewMatrix, figure[Id].transform);
    figure[Id].render();
    if(figure[Id].child != null) traverse(figure[Id].child);
    modelViewMatrix = stack.pop();
    if(figure[Id].sibling != null) traverse(figure[Id].sibling);
}

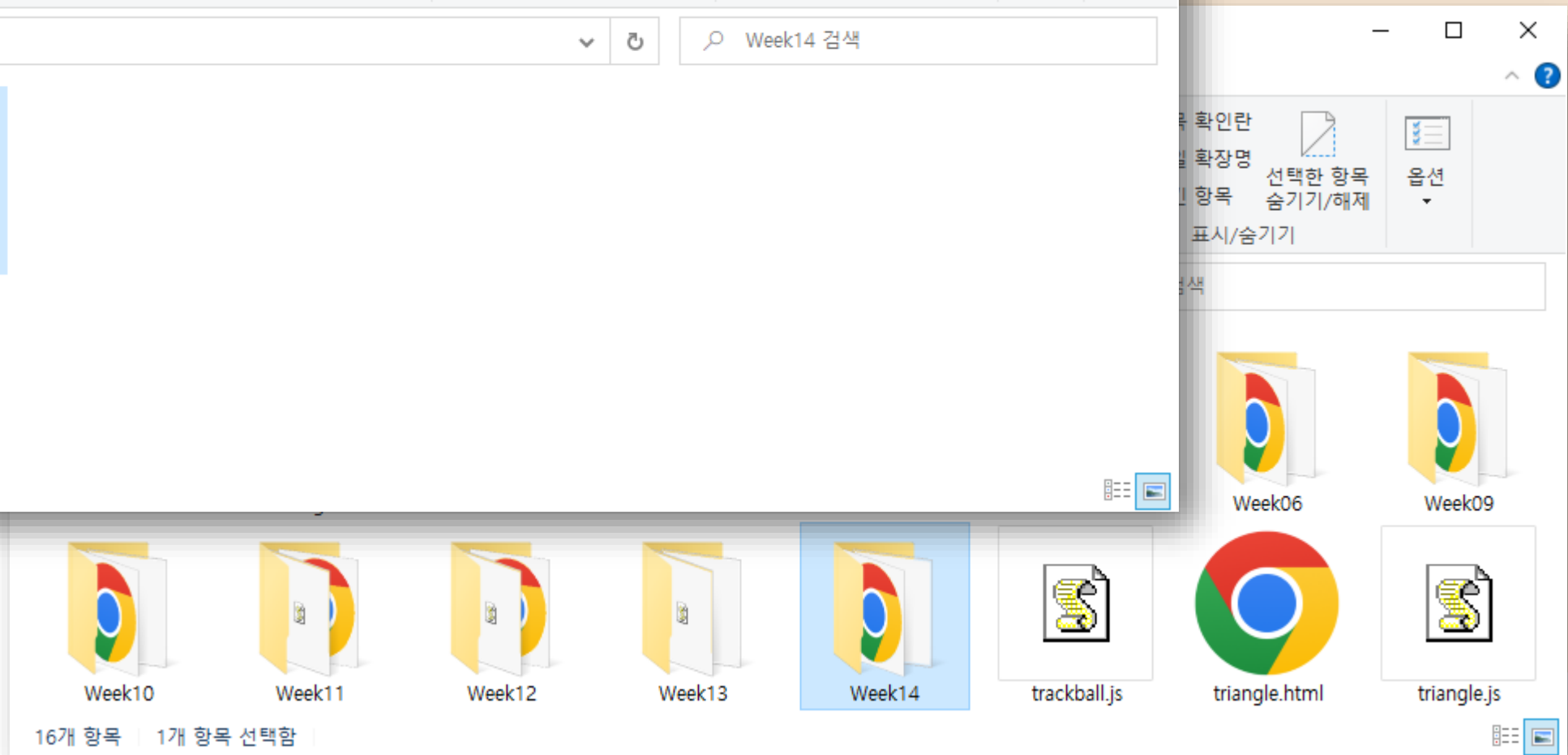
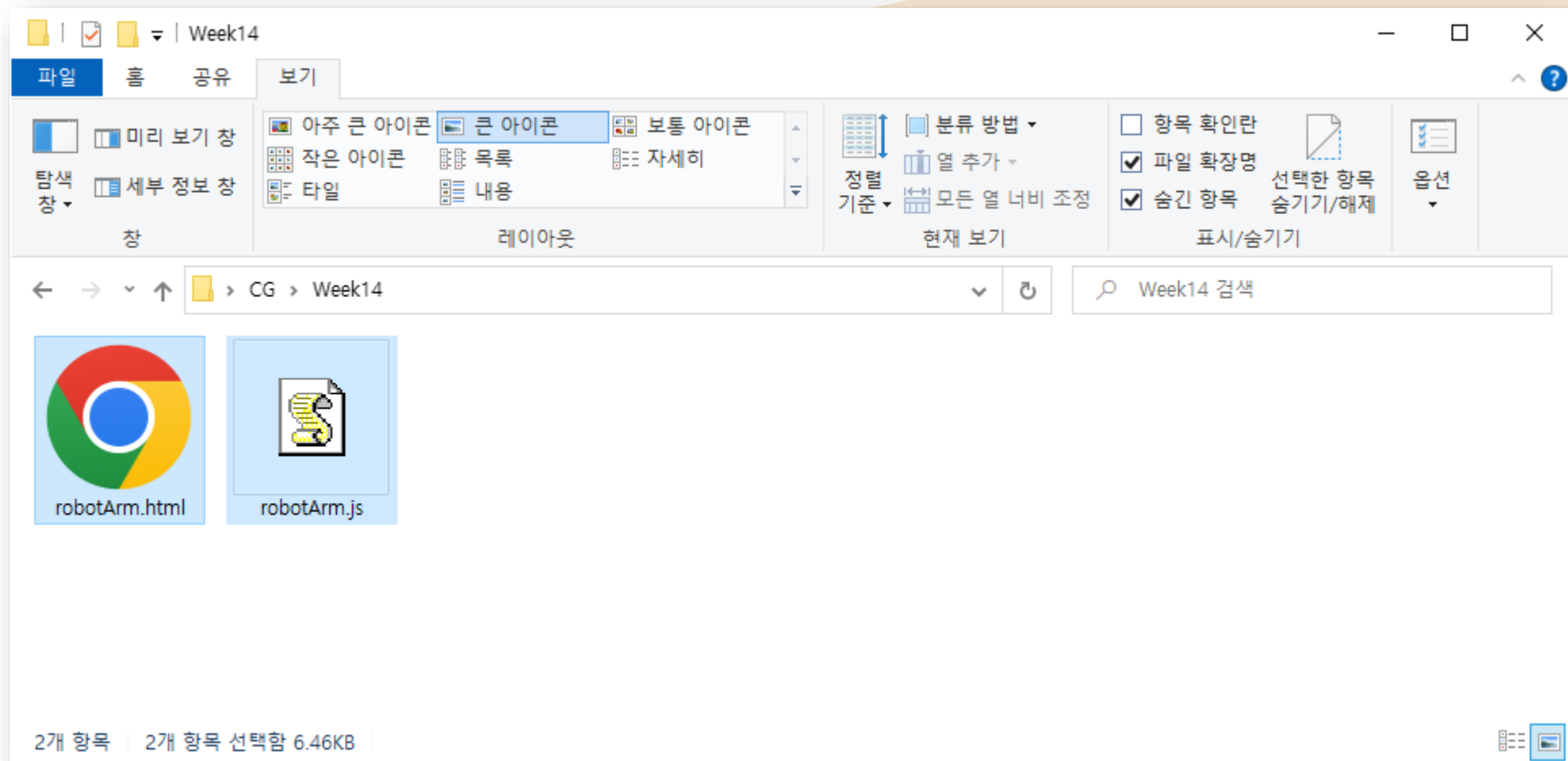
var render = function() {
    gl.clear( gl.COLOR_BUFFER_BIT );
    traverse(torsoId);
    requestAnimationFrame(render);
}
```

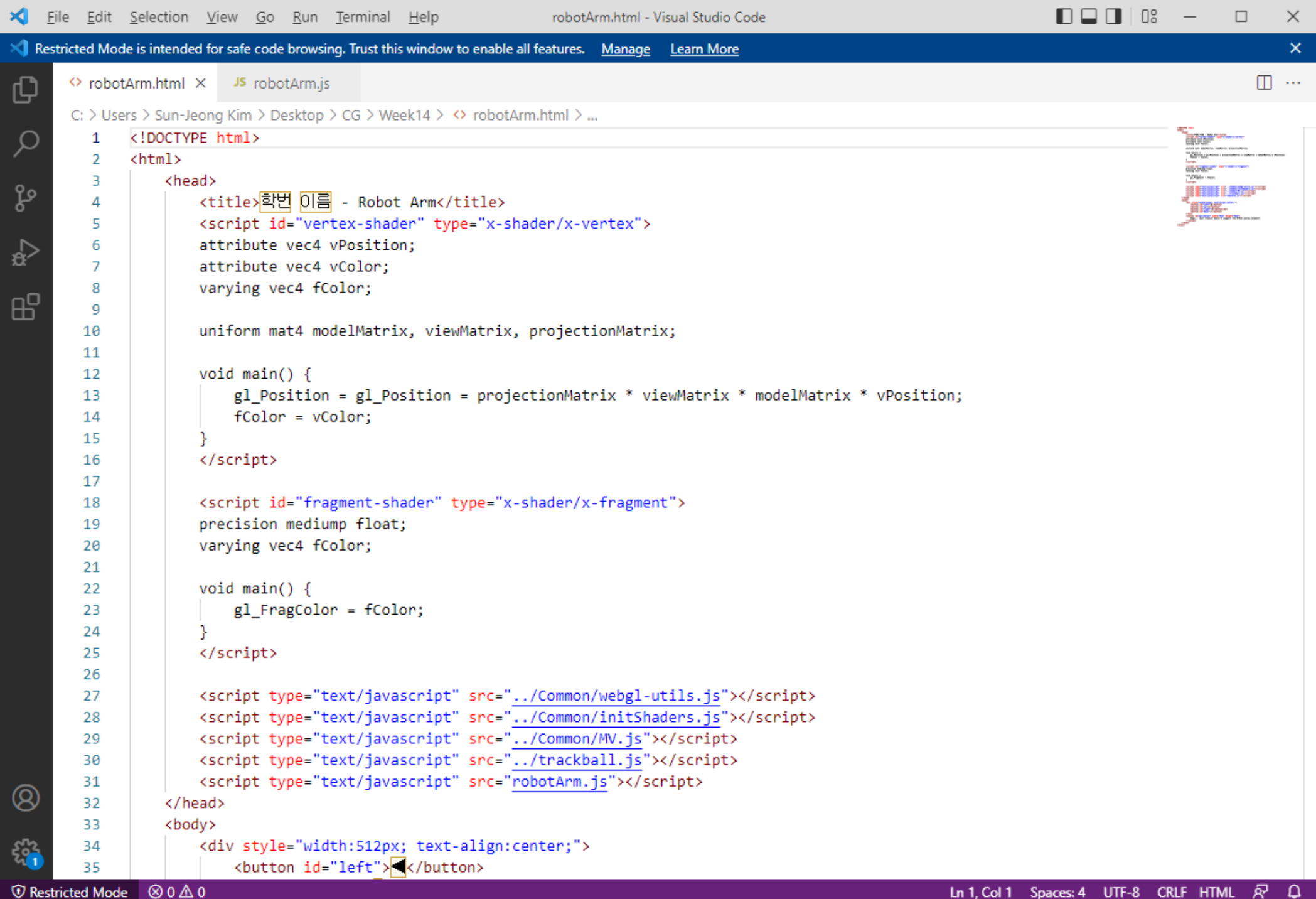
Notes

- We must save model-view matrix before multiplying it by node matrix
 - Updated matrix applies to children of node but not to siblings which contain their own matrices
- The traversal program applies to any left-child right-sibling tree
 - The particular tree is encoded in the definition of the individual nodes
- The order of traversal matters because of possible state changes in the functions

Dynamic Trees

- Because we are using JS, the nodes and the node structure can be changed during execution
- Definition of nodes and traversal are essentially the same as before but we can add and delete nodes during execution
- In desktop OpenGL, if we use pointers, the structure can be dynamic





FileEditSelectionViewGoRunTerminalHelp

robotArm.html - Visual Studio Code

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robotArm.html x JS robotArm.js

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```
<script type="text/javascript" src="../../Common/webgl-utils.js"></script>
<script type="text/javascript" src="../../Common/initShaders.js"></script>
<script type="text/javascript" src="../../Common/MV.js"></script>
<script type="text/javascript" src="../../trackball.js"></script>
<script type="text/javascript" src="robotArm.js"></script>
</head>
<body>
  <div style="width:512px; text-align:center;">
    <button id="left">◀</button>
    <button id="up">▲</button>
    <button id="right">▶</button><br>
    <button id="down">▼</button>
  </div>
  <canvas id="gl-canvas" width="512" height="512">
    Oops... your browser doesn't support the HTML5 canvas element!
  </canvas>
</body>
</html>
```

Ln 1, Col 1

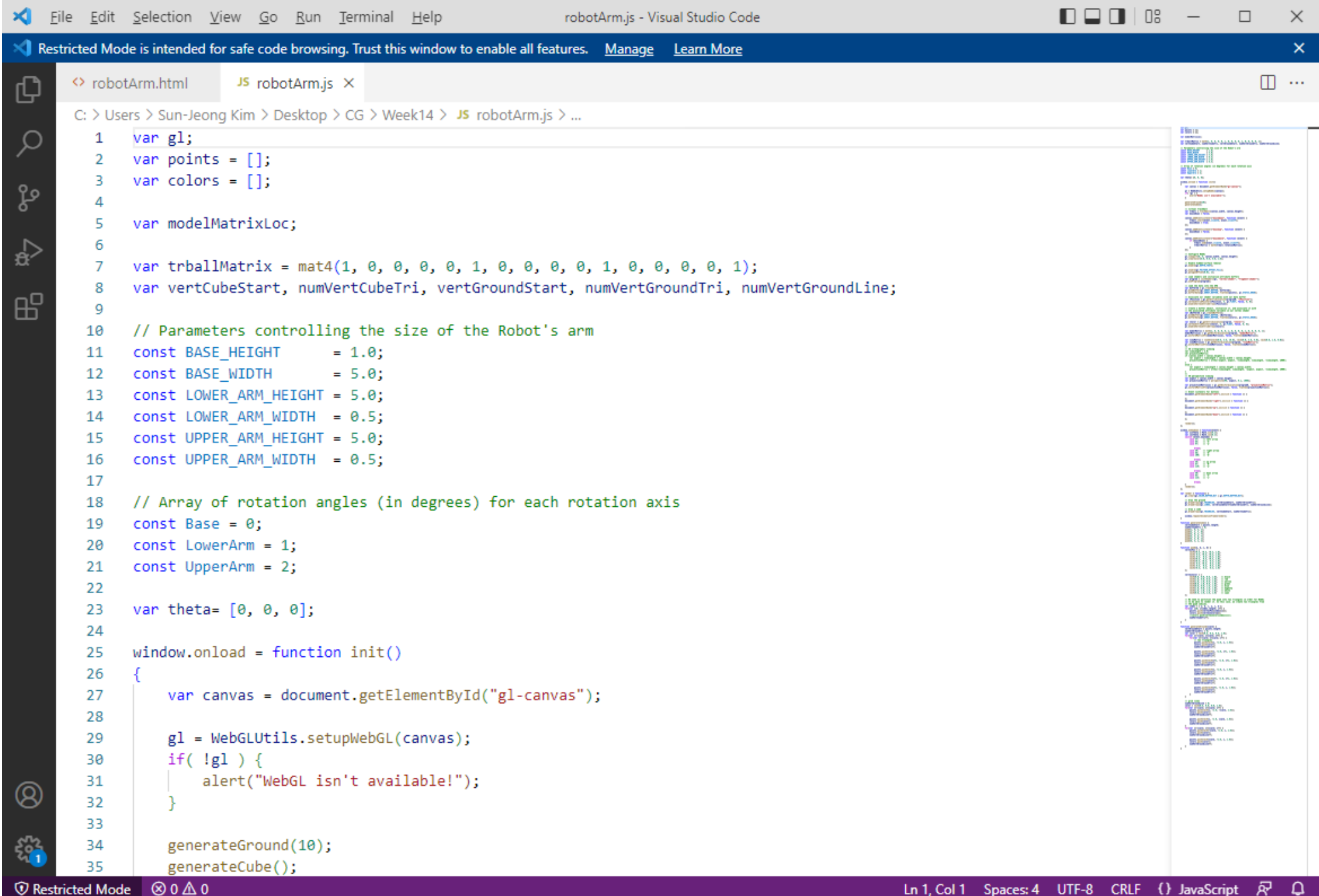
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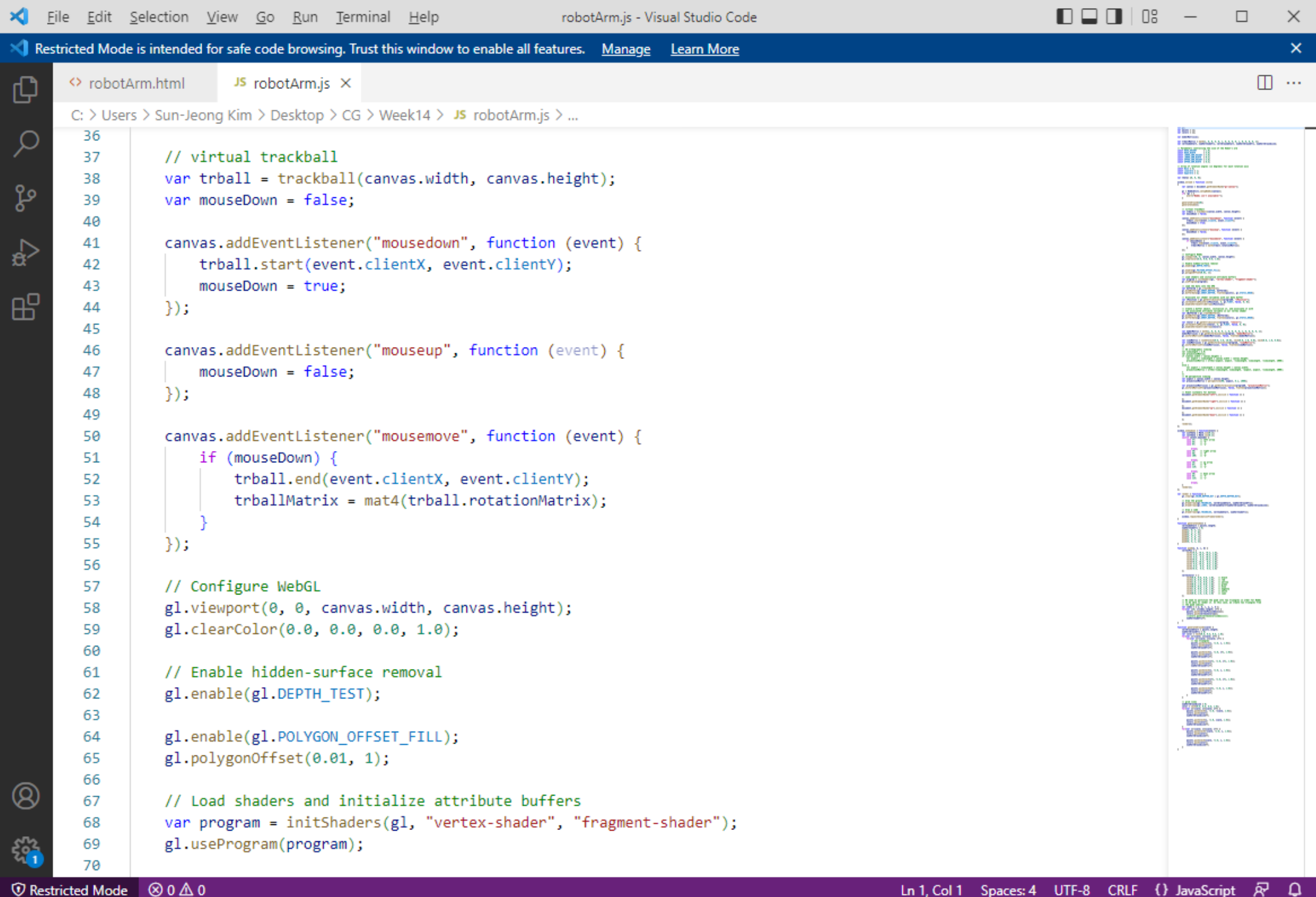
UTF-8

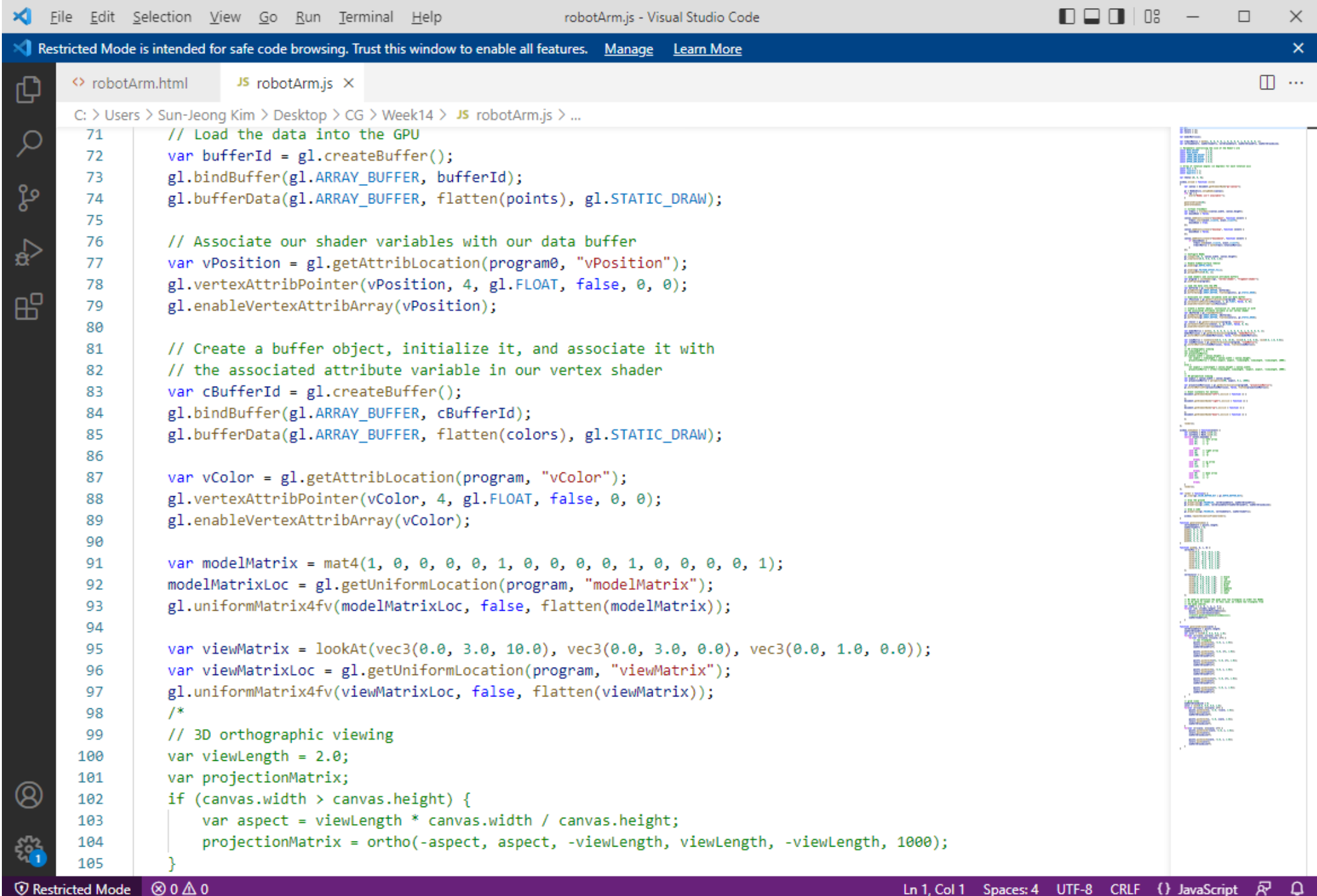
CRLF

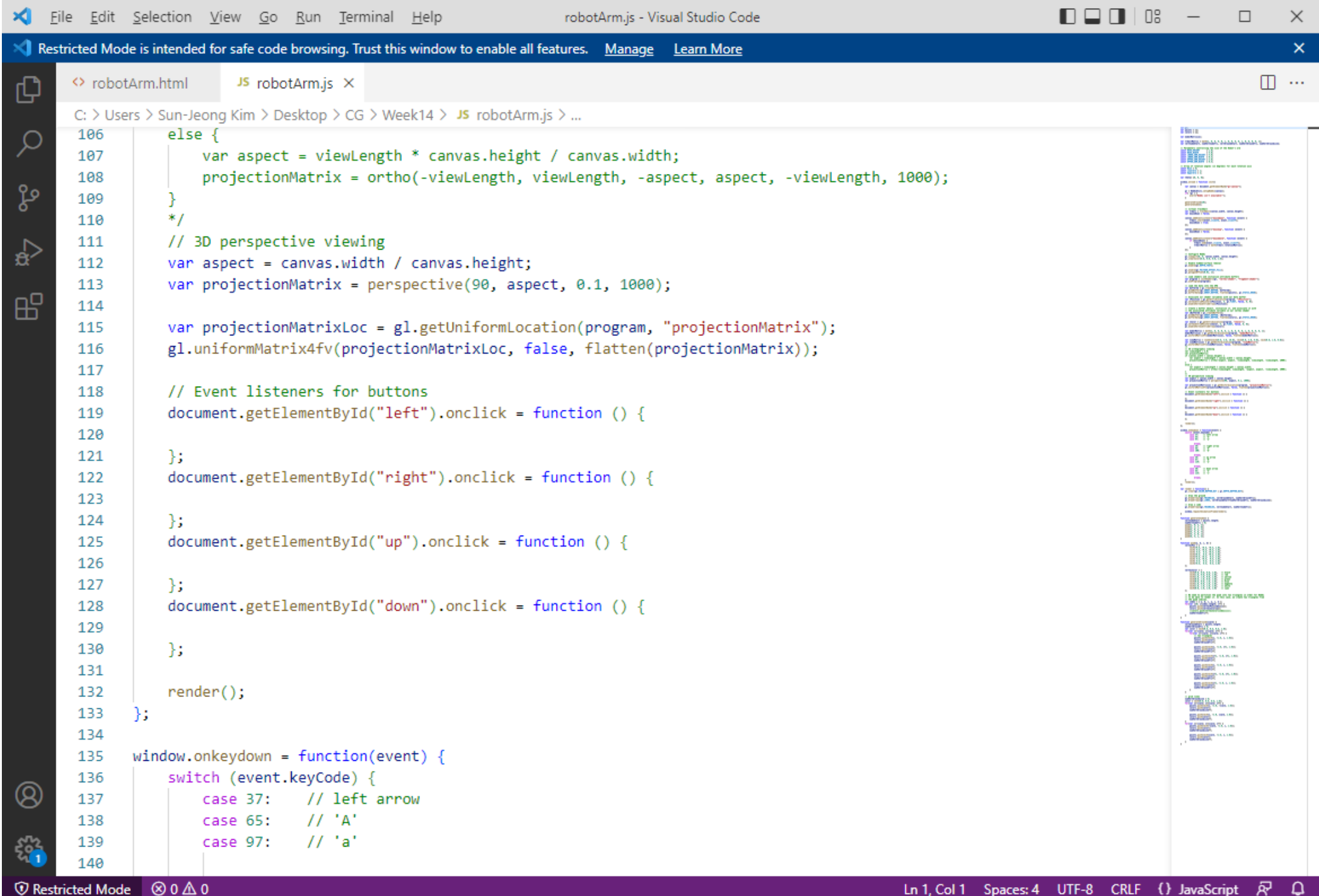
HTML

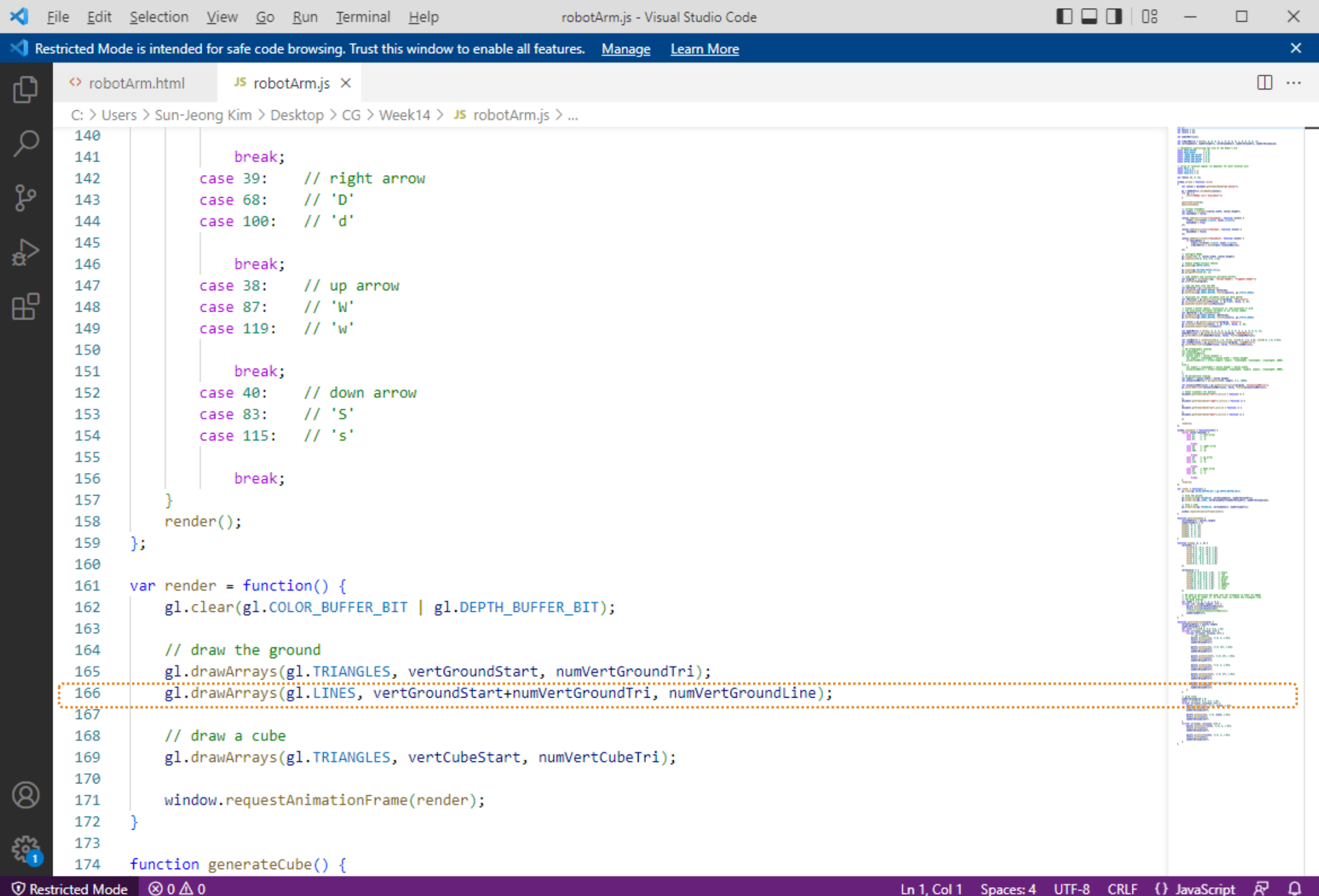
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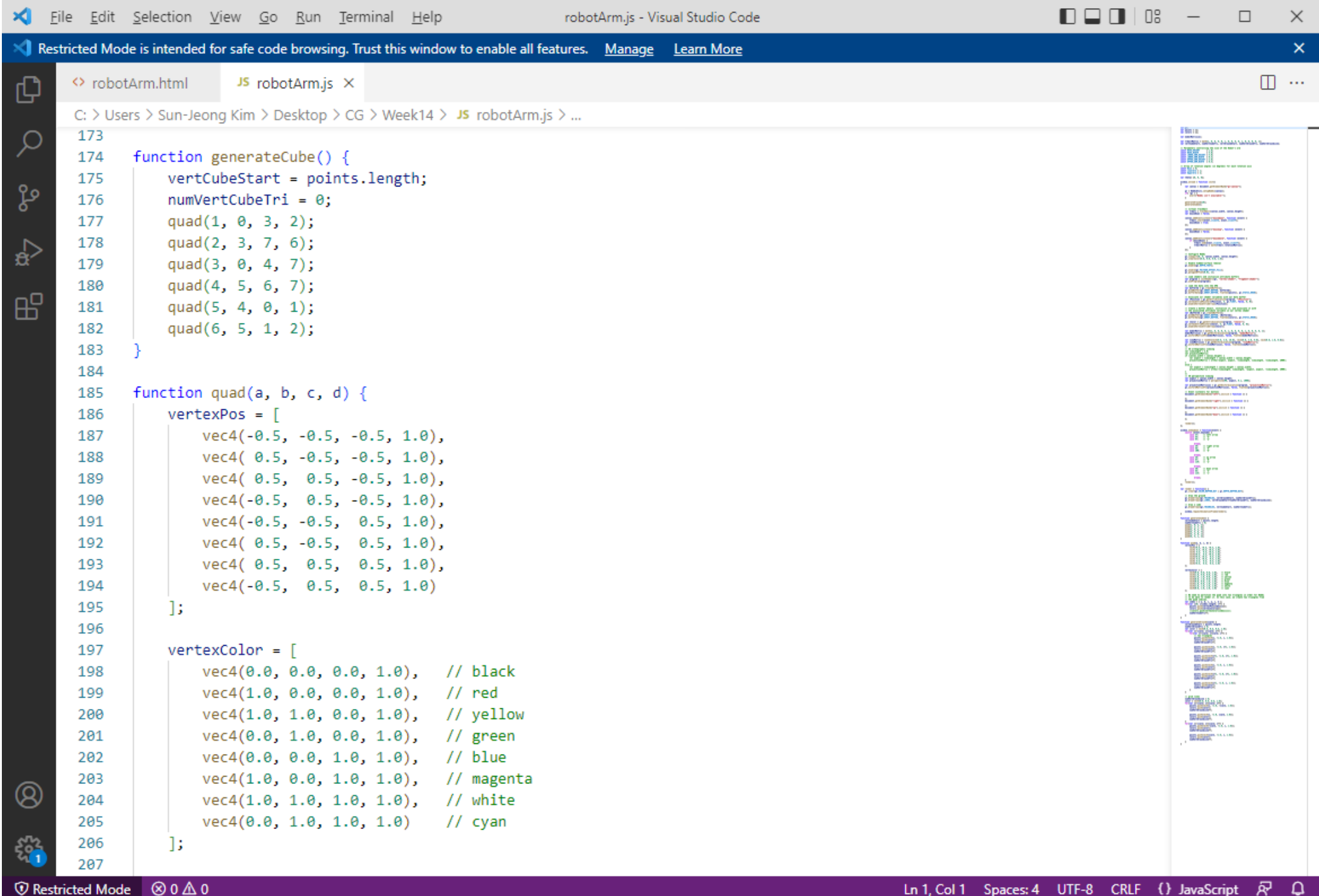


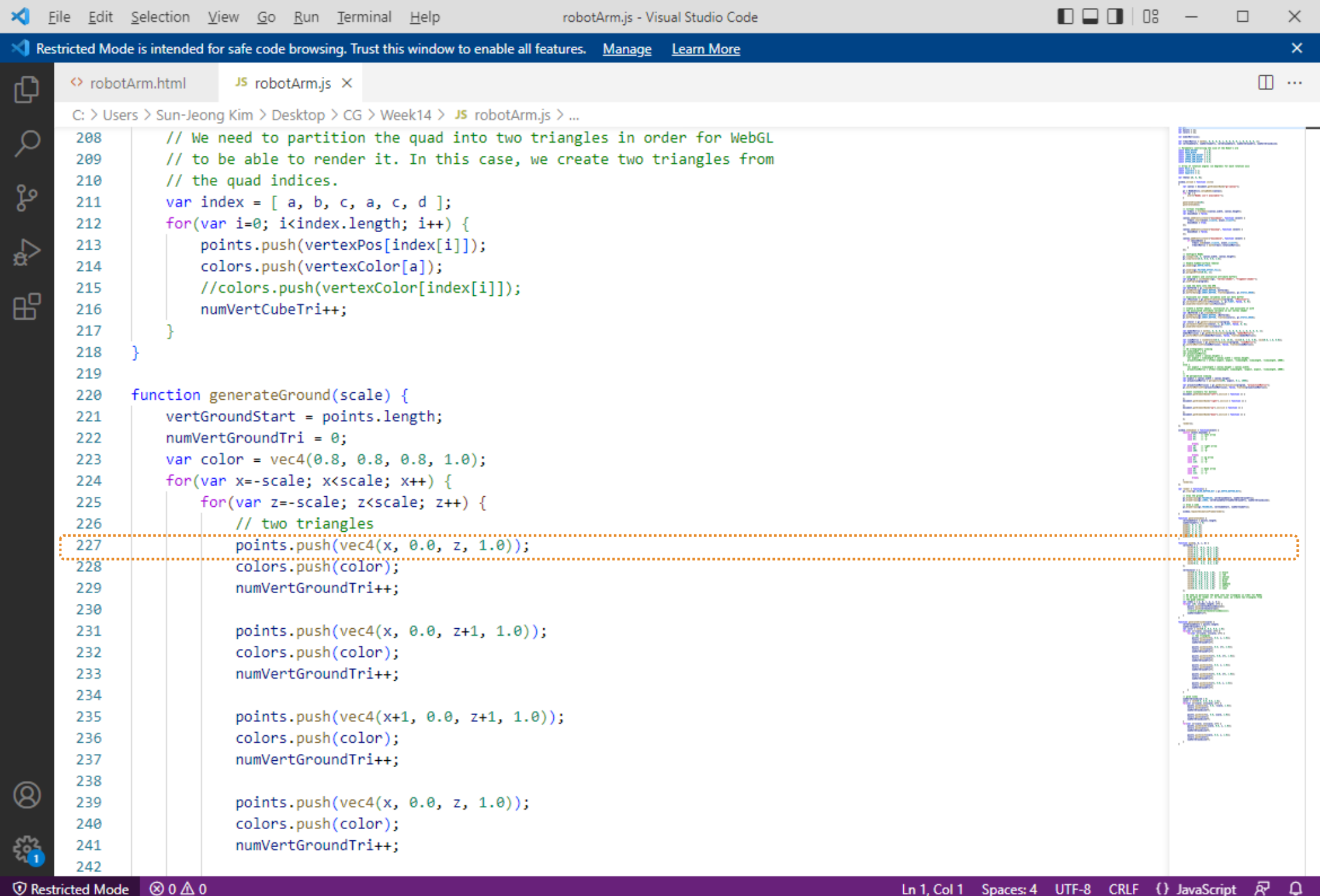


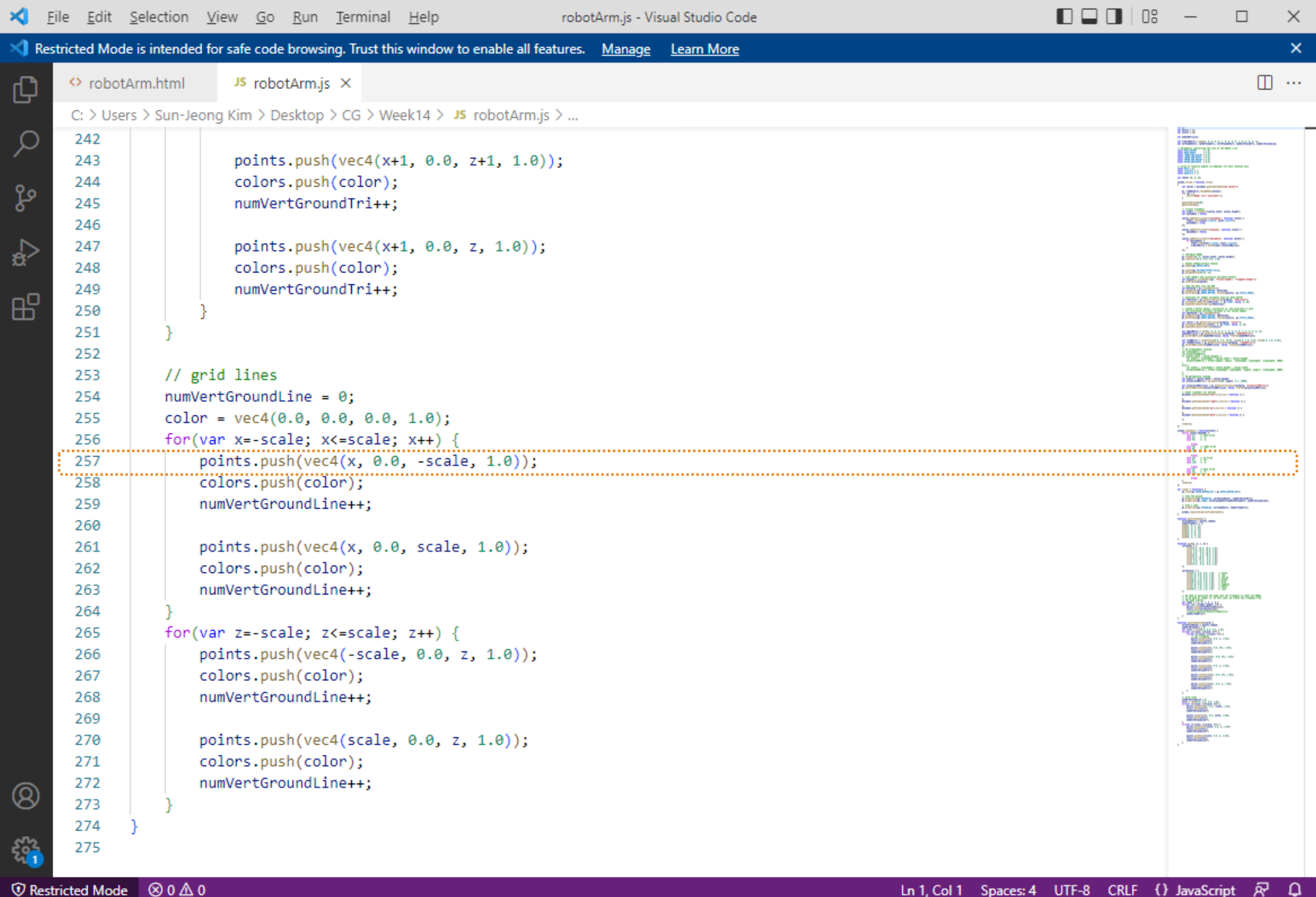


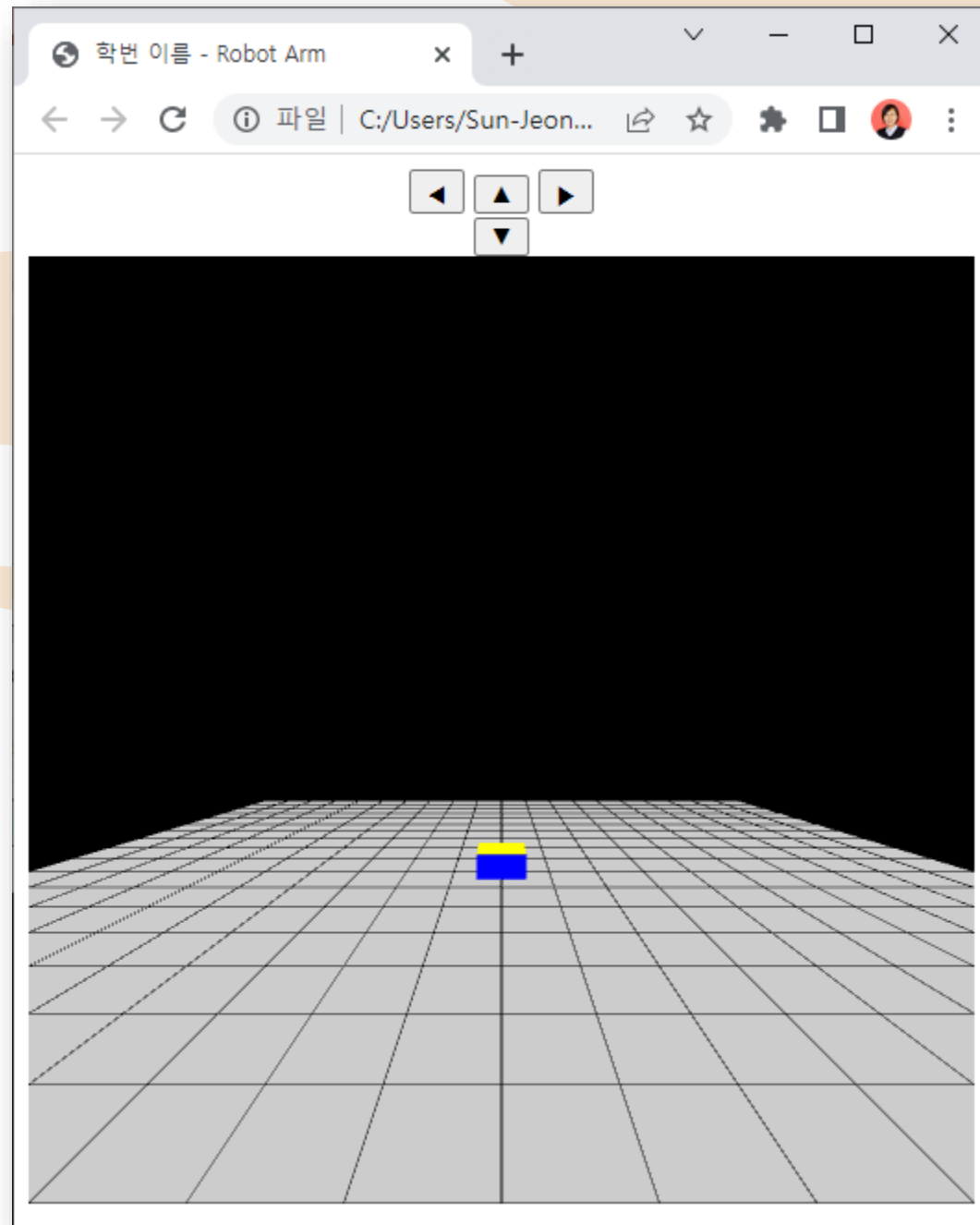












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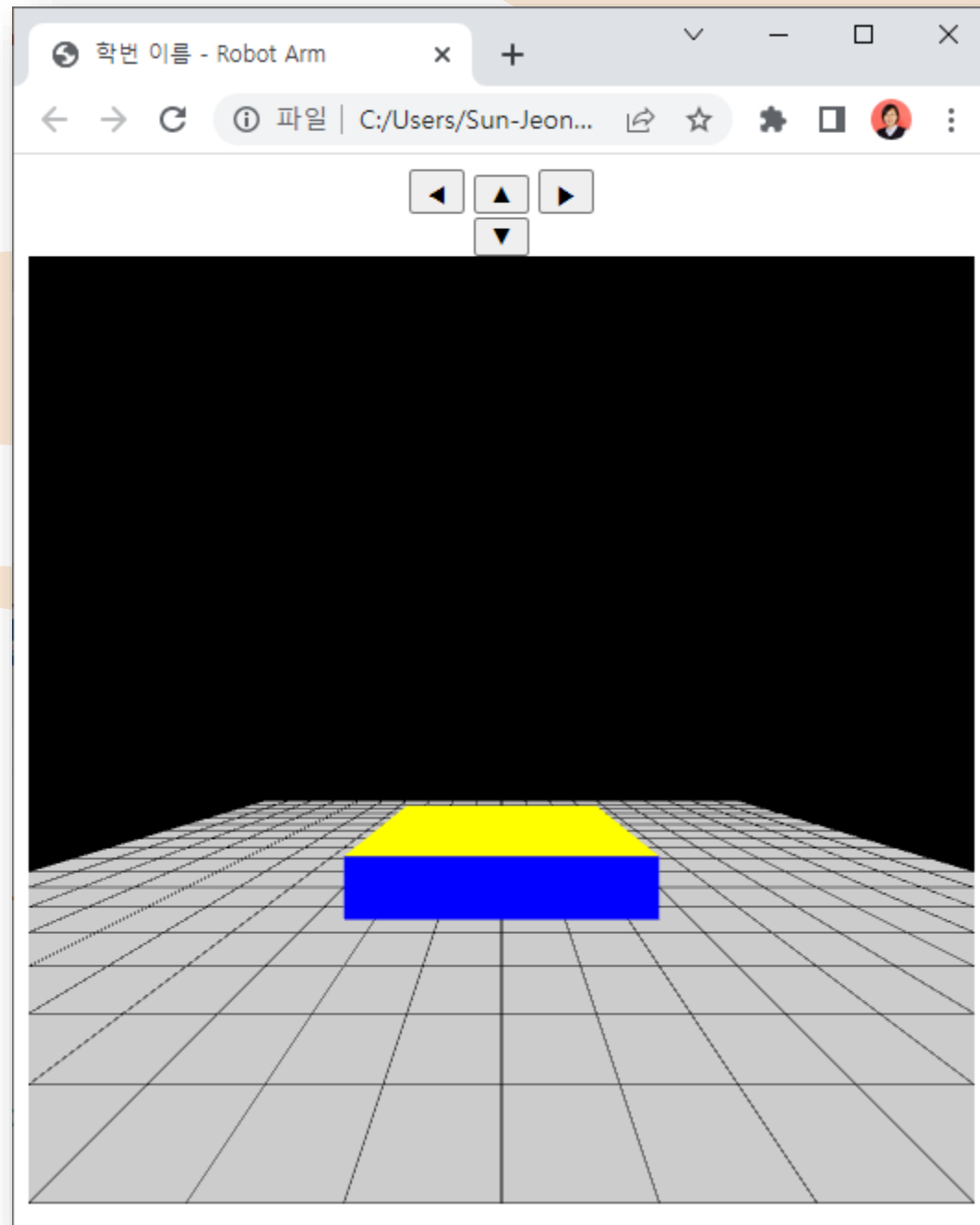
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robotArm.html JS robotArm.js X

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```
160
161 var render = function() {
162     gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
163
164     var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
165
166     // draw the ground
167     ground(modelMatrix);
168
169     // draw a cube
170     //gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
171
172     // draw the robot arm
173     base(modelMatrix);
174
175     window.requestAnimationFrame(render);
176 }
177
178 function ground(modelMatrix) {
179     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
180     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
181     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
182 }
183
184 function base(modelMatrix) {
185     var sMatrix = scale(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
186     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
187     var instanceMatrix = mult(modelMatrix, tMatrix);
188     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));
189     gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
190 }
191
192 function generateCube() {
193     vertCubeStart = points.length;
194     numVertCubeTri = 0;
```

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- lowerArm

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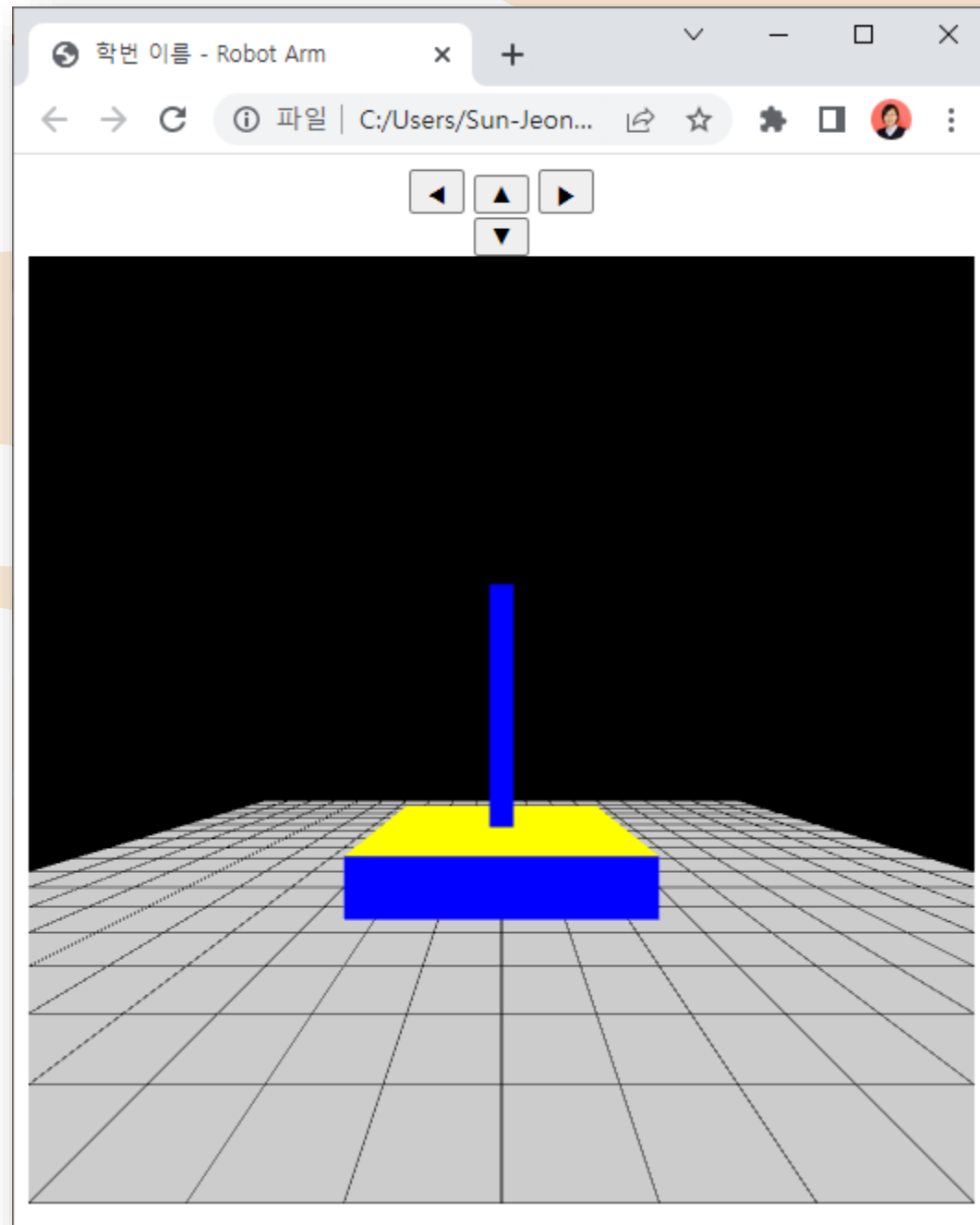
lowerArm

```

180
181 function ground(modelMatrix) {
182     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
183     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
184     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
185 }
186
187 function base(modelMatrix) {
188     var sMatrix = scalem(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
189     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
190     var instanceMatrix = mult(modelMatrix, tMatrix);
191     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));
192     gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
193 }
194
195 function lowerArm(modelMatrix) {
196     var sMatrix = scalem(LOWER_ARM_WIDTH, LOWER_ARM_HEIGHT, LOWER_ARM_WIDTH);
197     var tMatrix = mult(translate(0.0, 0.5*LOWER_ARM_HEIGHT, 0.0), sMatrix);
198     var instanceMatrix = mult(modelMatrix, tMatrix);
199     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));
200     gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
201 }
202
203 function generateCube() {
204     vertCubeStart = points.length;
205     numVertCubeTri = 0;
206     quad(1, 0, 3, 2);
207     quad(2, 3, 7, 6);
208     quad(3, 0, 4, 7);
209     quad(4, 5, 6, 7);
210     quad(5, 4, 0, 1);
211     quad(6, 5, 1, 2);
212 }
213
214 function quad(a, b, c, d) {

```

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```

160
161 var render = function() {
162     gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
163
164     var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
165
166     // draw the ground
167     ground(modelMatrix);
168
169     // draw a cube
170     //gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
171
172     // draw the robot arm
173     base(modelMatrix);
174
175     modelMatrix = mult(modelMatrix, translate(0.0, BASE_HEIGHT, 0.0));
176     lowerArm(modelMatrix);
177
178     modelMatrix = mult(modelMatrix, translate(0.0, LOWER_ARM_HEIGHT, 0.0));
179     upperArm(modelMatrix);
180
181     window.requestAnimationFrame(render);
182 }
183
184 function ground(modelMatrix) {
185     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
186     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
187     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
188 }
189
190 function base(modelMatrix) {
191     var sMatrix = scale(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
192     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
193     var instanceMatrix = mult(modelMatrix, tMatrix);
194     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));

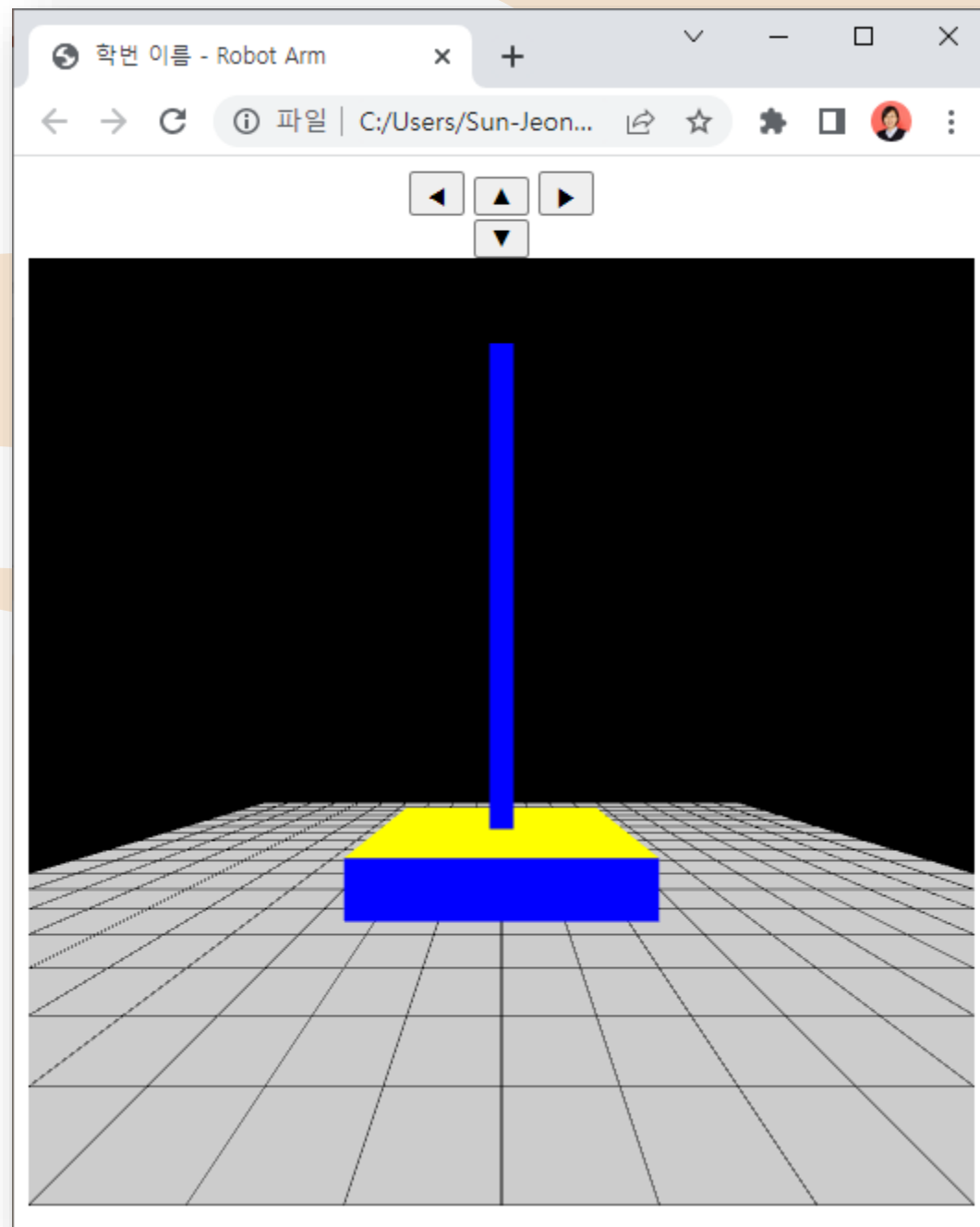
```

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```
183
184 function ground(modelMatrix) {
185     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
186     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
187     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
188 }
189
190 function base(modelMatrix) {
191     var sMatrix = scale(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
192     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
193     var instanceMatrix = mult(modelMatrix, tMatrix);
194     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));
195     gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
196 }
197
198 function lowerArm(modelMatrix) {
199     var sMatrix = scale(LOWER_ARM_WIDTH, LOWER_ARM_HEIGHT, LOWER_ARM_WIDTH);
200     var tMatrix = mult(translate(0.0, 0.5*LOWER_ARM_HEIGHT, 0.0), sMatrix);
201     var instanceMatrix = mult(modelMatrix, tMatrix);
202     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));
203     gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
204 }
205
206 function upperArm(modelMatrix) {
207     var sMatrix = scale(UPPER_ARM_WIDTH, UPPER_ARM_HEIGHT, UPPER_ARM_WIDTH);
208     var tMatrix = mult(translate(0.0, 0.5*UPPER_ARM_HEIGHT, 0.0), sMatrix);
209     var instanceMatrix = mult(modelMatrix, tMatrix);
210     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(instanceMatrix));
211     gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
212 }
213
214 function generateCube() {
215     vertCubeStart = points.length;
216     numVertCubeTri = 0;
217     quad(1, 0, 3, 2);
```

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robotArm.js - Visual Studio Code

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robotArm.html JS robotArm.js


C: > Users > Sun-Jeong Kim > Desktop > CG > Week14 > JS robotArm.js > render

135 window.onkeydown = function(event) {
136 switch (event.keyCode) {
137 case 65: // 'A'
138 case 97: // 'a'
139 theta[Base] -= 2.0;
140 break;
141 case 68: // 'D'
142 case 100: // 'd'
143 theta[Base] += 2.0;
144 break;
145 case 37: // left arrow
146 break;
147 case 39: // right arrow
148 break;
149 case 38: // up arrow
150 case 87: // 'W'
151 case 119: // 'w'
152 break;
153 case 40: // down arrow
154 case 83: // 'S'
155 case 115: // 's'
156 break;
157 break;
158 }
159 render();
160 };
161 };
162 };
163 var render = function() {
164 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
165 var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
166 // draw the ground
167 ground(modelMatrix);
168 };
169 };

135 window.onkeydown = function(event) {
136 switch (event.keyCode) {
137 case 65: // 'A'
138 case 97: // 'a'
139 theta[Base] -= 2.0;
140 break;
141 case 68: // 'D'
142 case 100: // 'd'
143 theta[Base] += 2.0;
144 break;
145 case 37: // left arrow
146 break;
147 case 39: // right arrow
148 break;
149 case 38: // up arrow
150 case 87: // 'W'
151 case 119: // 'w'
152 break;
153 case 40: // down arrow
154 case 83: // 'S'
155 case 115: // 's'
156 break;
157 break;
158 }
159 render();
160 };
161 };
162 };
163 var render = function() {
164 gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
165 var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
166 // draw the ground
167 ground(modelMatrix);
168 };
169 };

Ln 175, Col 68 Spaces: 4 UTF-8 CRLF JavaScript

6



```

162
163 var render = function() {
164     gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
165
166     var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
167
168     // draw the ground
169     ground(modelMatrix);
170
171     // draw a cube
172     //gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
173
174     // draw the robot arm
175     modelMatrix = mult(modelMatrix, rotate(theta[Base], 0, 1, 0));
176     base(modelMatrix);
177
178     modelMatrix = mult(modelMatrix, translate(0.0, BASE_HEIGHT, 0.0));
179     lowerArm(modelMatrix);
180
181     modelMatrix = mult(modelMatrix, translate(0.0, LOWER_ARM_HEIGHT, 0.0));
182     upperArm(modelMatrix);
183
184     window.requestAnimationFrame(render);
185 }
186
187 function ground(modelMatrix) {
188     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
189     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
190     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
191 }
192
193 function base(modelMatrix) {
194     var sMatrix = scalem(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
195     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
196     var instanceMatrix = mult(modelMatrix, tMatrix);

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1. $\frac{1}{x^2} = x^{-2}$
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27. $\frac{1}{x^{28}} = x^{-28}$
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31. $\frac{1}{x^{32}} = x^{-32}$
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32. $\frac{1}{x^{33}} = x^{-33}$
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 $\frac{d}{dx} x^{-49} = -49x^{-50} = -\frac{49}{x^{50}}$

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51. $\frac{1}{x^{52}} = x^{-52}$
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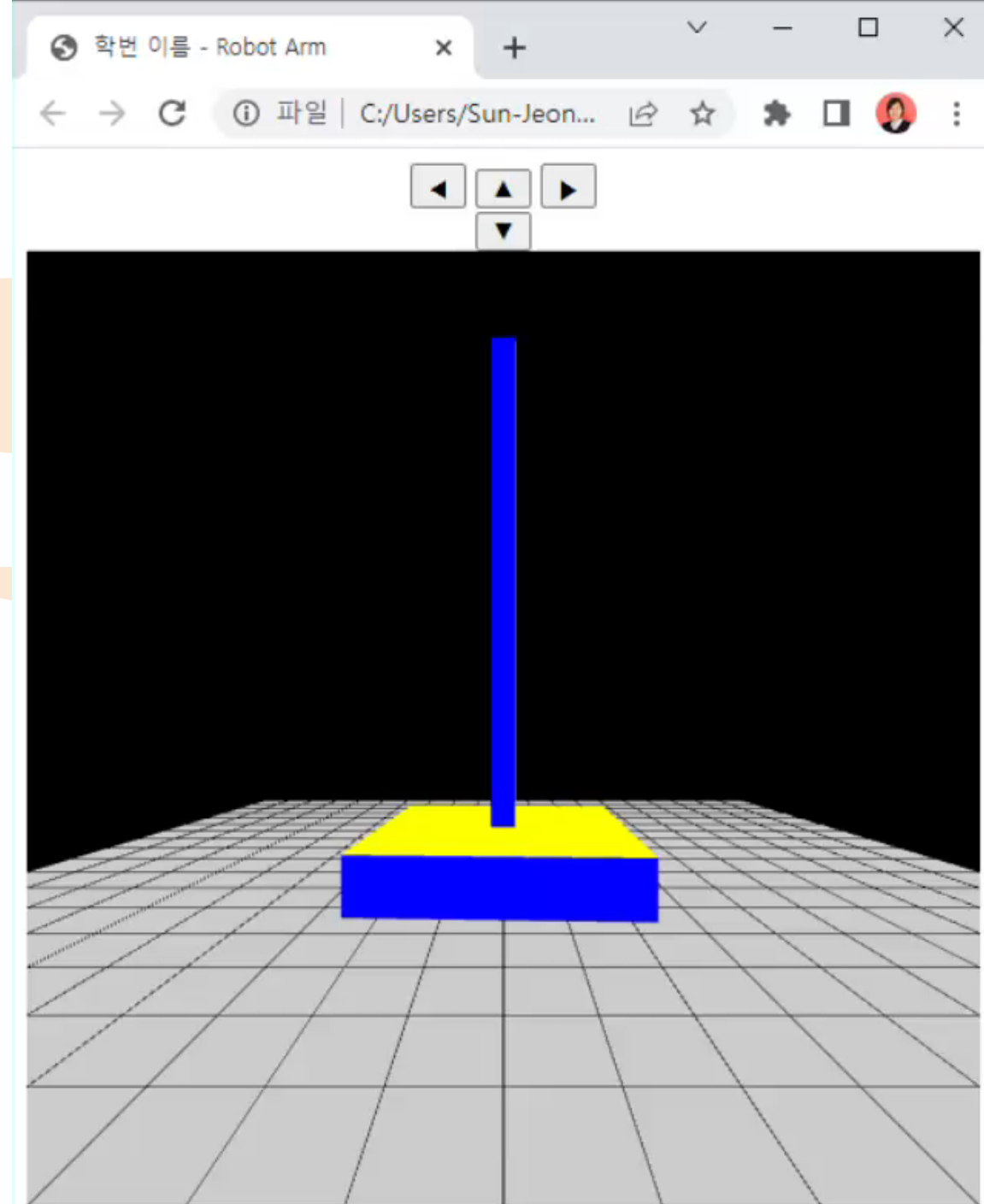
52. $\frac{1}{x^{53}} = x^{-53}$
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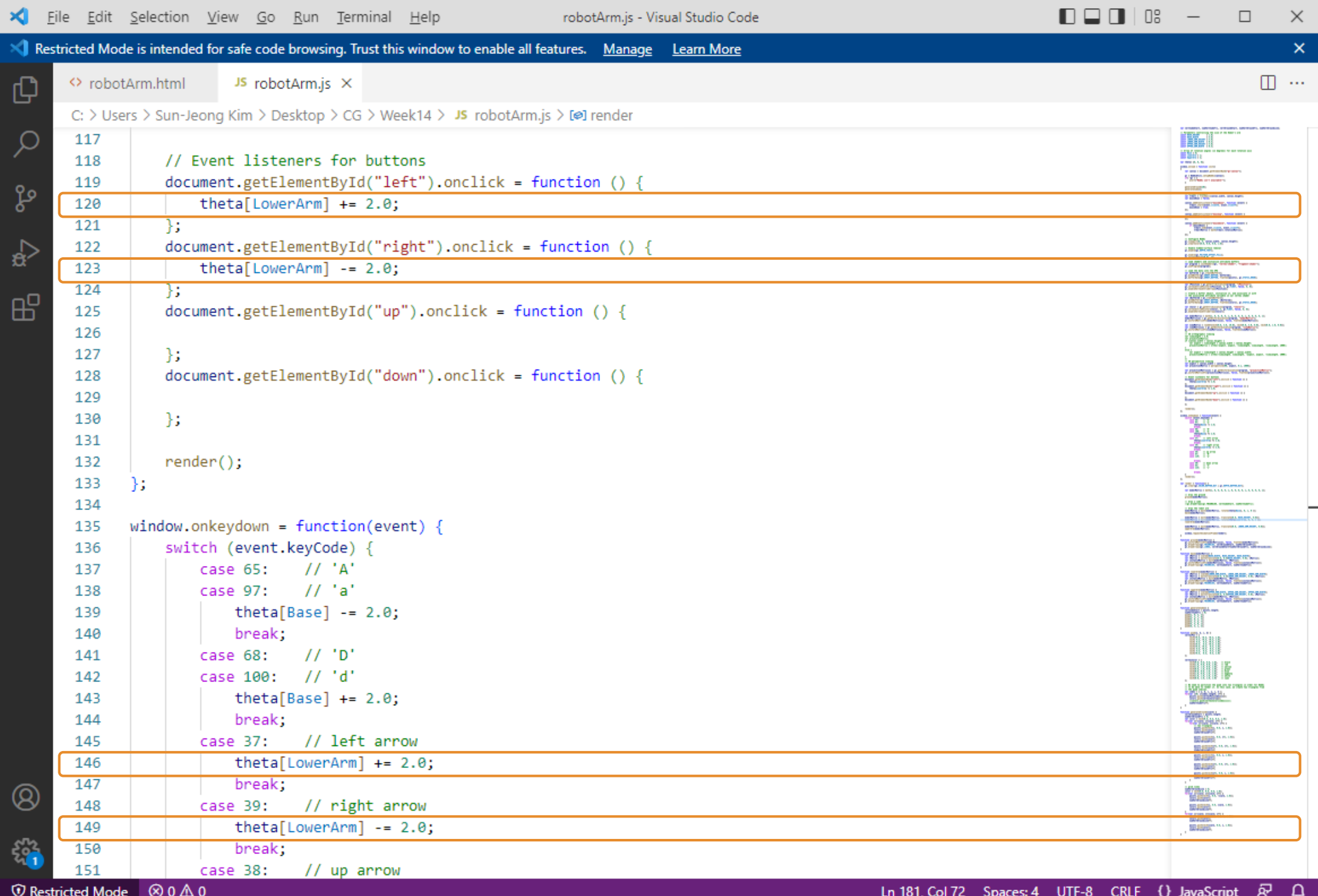
53. $\frac{1}{x^{54}} = x^{-54}$
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54. $\frac{1}{x^{55}} = x^{-55}$
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56. $\frac{1}{x^{57}} = x^{-57}$
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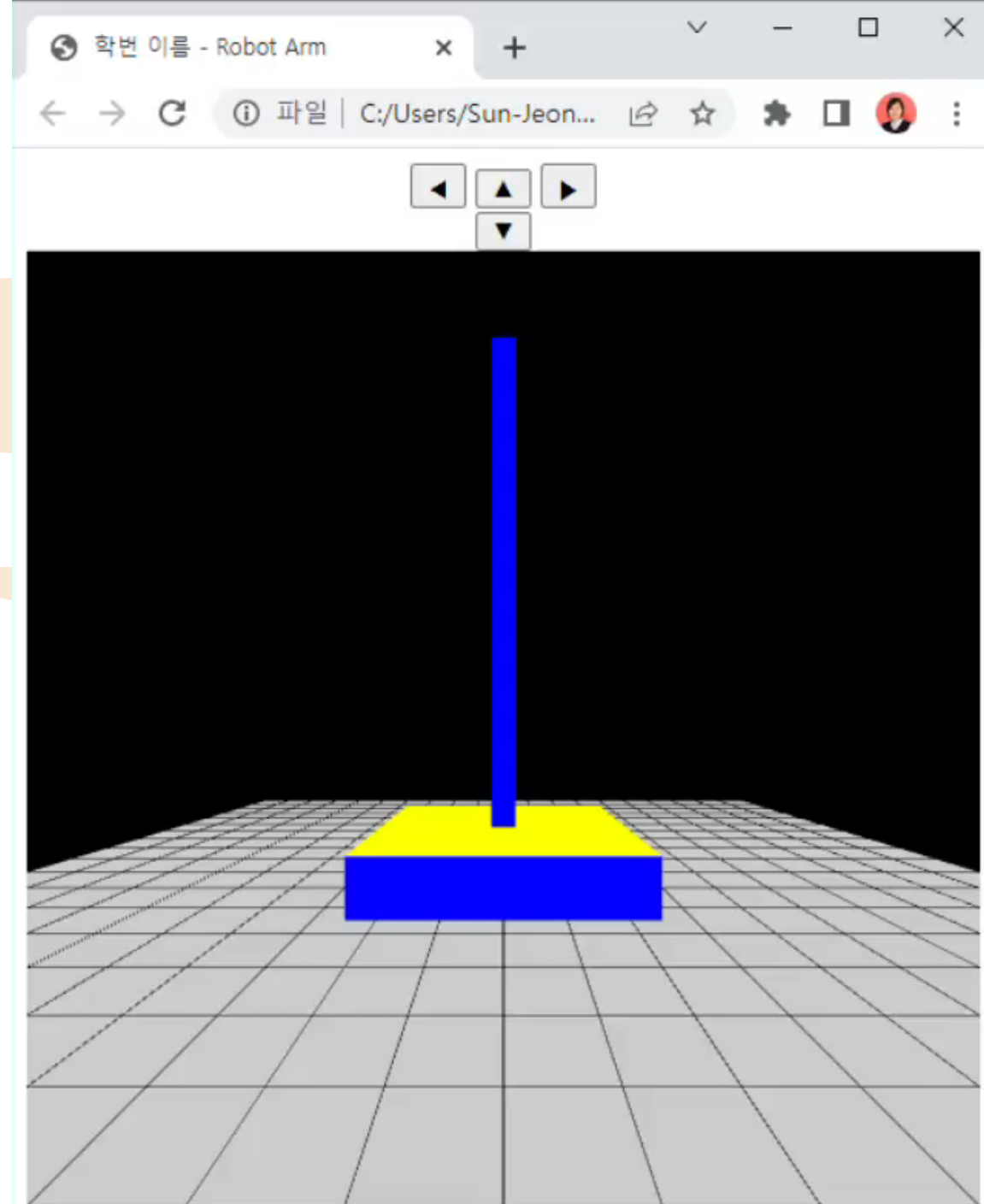


robotArm.html JS robotArm.js

C: > Users > Sun-Jeong Kim > Desktop > CG > Week14 > JS robotArm.js > render

```
164
165 var render = function() {
166     gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
167
168     var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
169
170     // draw the ground
171     ground(modelMatrix);
172
173     // draw a cube
174     //gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
175
176     // draw the robot arm
177     modelMatrix = mult(modelMatrix, rotate(theta[Base], 0, 1, 0));
178     base(modelMatrix);
179
180     modelMatrix = mult(modelMatrix, translate(0.0, BASE_HEIGHT, 0.0));
181     modelMatrix = mult(modelMatrix, rotate(theta[LowerArm], 0, 0, 1));
182     lowerArm(modelMatrix);
183
184     modelMatrix = mult(modelMatrix, translate(0.0, LOWER_ARM_HEIGHT, 0.0));
185     upperArm(modelMatrix);
186
187     window.requestAnimationFrame(render);
188 }
189
190 function ground(modelMatrix) {
191     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
192     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
193     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
194 }
195
196 function base(modelMatrix) {
197     var sMatrix = scale(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
198     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
```

```
164
165 var render = function() {
166     gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
167
168     var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
169
170     // draw the ground
171     ground(modelMatrix);
172
173     // draw a cube
174     //gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
175
176     // draw the robot arm
177     modelMatrix = mult(modelMatrix, rotate(theta[Base], 0, 1, 0));
178     base(modelMatrix);
179
180     modelMatrix = mult(modelMatrix, translate(0.0, BASE_HEIGHT, 0.0));
181     modelMatrix = mult(modelMatrix, rotate(theta[LowerArm], 0, 0, 1));
182     lowerArm(modelMatrix);
183
184     modelMatrix = mult(modelMatrix, translate(0.0, LOWER_ARM_HEIGHT, 0.0));
185     upperArm(modelMatrix);
186
187     window.requestAnimationFrame(render);
188 }
189
190 function ground(modelMatrix) {
191     gl.uniformMatrix4fv(modelMatrixLoc, false, flatten(modelMatrix));
192     gl.drawArrays(gl.TRIANGLES, vertGroundStart, numVertGroundTri);
193     gl.drawArrays(gl.LINES, vertGroundStart+numVertGroundTri, numVertGroundLine);
194 }
195
196 function base(modelMatrix) {
197     var sMatrix = scale(BASE_WIDTH, BASE_HEIGHT, BASE_WIDTH);
198     var tMatrix = mult(translate(0.0, 0.5*BASE_HEIGHT, 0.0), sMatrix);
```



robotArm.js - Visual Studio Code

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robotArm.html JS robotArm.js

C: > Users > Sun-Jeong Kim > Desktop > CG > Week14 > JS robotArm.js > render

```
125     document.getElementById("up").onclick = function () {
126         theta[UpperArm] += 2.0;
127     };
128     document.getElementById("down").onclick = function () {
129         theta[UpperArm] -= 2.0;
130     };
131
132     render();
133 };
134
135 window.onkeydown = function(event) {
136     switch (event.keyCode) {
137         case 65: // 'A'
138         case 97: // 'a'
139             theta[Base] -= 2.0;
140             break;
141         case 68: // 'D'
142         case 100: // 'd'
143             theta[Base] += 2.0;
144             break;
145         case 37: // left arrow
146             theta[LowerArm] += 2.0;
147             break;
148         case 39: // right arrow
149             theta[LowerArm] -= 2.0;
150             break;
151         case 38: // up arrow
152             theta[UpperArm] += 2.0;
153             break;
154         case 40: // down arrow
155             theta[UpperArm] -= 2.0;
156             break;
157         case 87: // 'W'
158         case 119: // 'w'
159             break;
```

Ln 187, Col 68 Spaces: 4 UTF-8 CRLF JavaScript

robotArm.js - Visual Studio Code

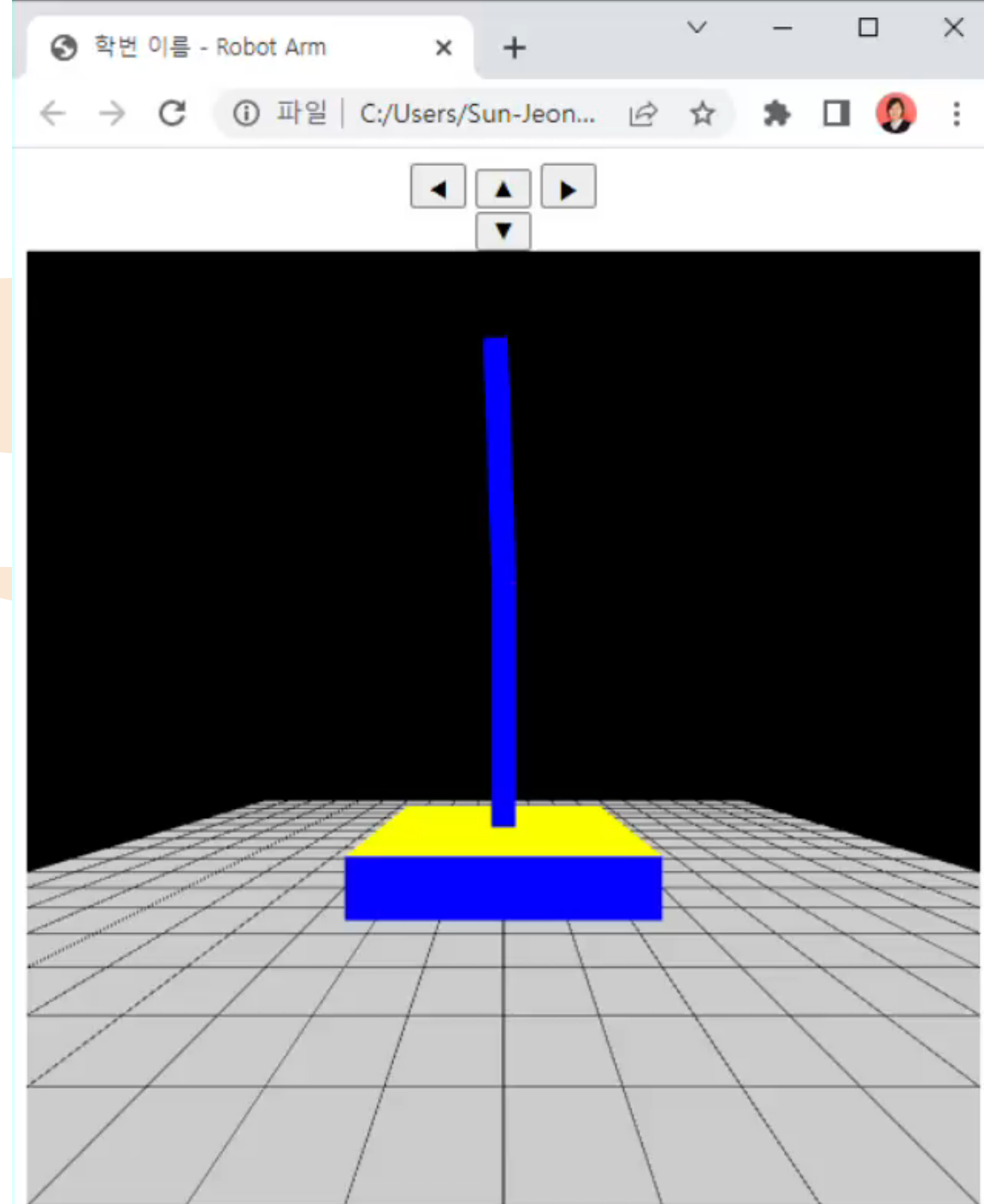
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robotArm.html JS robotArm.js

C: > Users > Sun-Jeong Kim > Desktop > CG > Week14 > JS robotArm.js > render

```
159         break;
160     case 83:    // 'S'
161     case 115:   // 's'
162         break;
163     }
164     render();
165 };
166
167 var render = function() {
168     gl.clear(gl.COLOR_BUFFER_BIT | gl.DEPTH_BUFFER_BIT);
169
170     var modelMatrix = mat4(1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 1);
171
172     // draw the ground
173     ground(modelMatrix);
174
175     // draw a cube
176     //gl.drawArrays(gl.TRIANGLES, vertCubeStart, numVertCubeTri);
177
178     // draw the robot arm
179     modelMatrix = mult(modelMatrix, rotate(theta[Base], 0, 1, 0 ));
180     base(modelMatrix);
181
182     modelMatrix = mult(modelMatrix, translate(0.0, BASE_HEIGHT, 0.0));
183     modelMatrix = mult(modelMatrix, rotate(theta[LowerArm], 0, 0, 1 ));
184     lowerArm(modelMatrix);
185
186     modelMatrix = mult(modelMatrix, translate(0.0, LOWER_ARM_HEIGHT, 0.0));
187     modelMatrix = mult(modelMatrix, rotate(theta[UpperArm], 0, 0, 1 ));
188     upperArm(modelMatrix);
189
190     window.requestAnimationFrame(render);
191 }
192
193 function ground(modelMatrix) {
```

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연습 문제

- ADSW 키를 이용하여 Base를 전후좌우로 이동(translation) 시키시오.
- Base의 회전은 PageUp(33), PageDown(34)키를 이용하시오.