

# The Study of Time Constant Analysis in Random Telegraph Noise at the Subthreshold Voltage Region

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**Abstract**—We extracted time constants capture and emission of Random Telegraph Noise (RTN), and their dependencies of the gate-source voltage from numerous MOSFETs and discuss the trapping and detrapping processes of carriers at the subthreshold voltage region. The dependence of time to capture on gate-source voltage cannot be determined by the trap depth from the interface and but by the distance between the trap and the carrier to be captured and the trap energy level. On the other hand, it is considered that the dependence of time to emission is determined by the distance between the trap and the Si/SiO<sub>2</sub> interface and the trap energy level. It is easy to understand emission processes compared to capture processes. We observed various emission processes caused by tunneling to Si substrate side, tunneling to gate electrode side and tunneling to either Si substrate side or gate electrode side depending on gate-source voltage.

Evaluating the time constants individually is indispensable to characterize the trap which causes RTN in subthreshold voltage region.

**Keywords**—component; MOSFET, Random Telegraph Noise (RTN), Subthreshold Voltage, Time Constant

## I. INTRODUCTION

Random Telegraph Noise (RTN) has been believed as one of the physical origins of low frequency noise. The phenomenon is characterized by a discrete and random fluctuation of conductance in carrier transport and the number of conduction carriers, which is caused by the capture/emission of the conduction carrier by/from individual traps in an insulator film or bulk material [1].

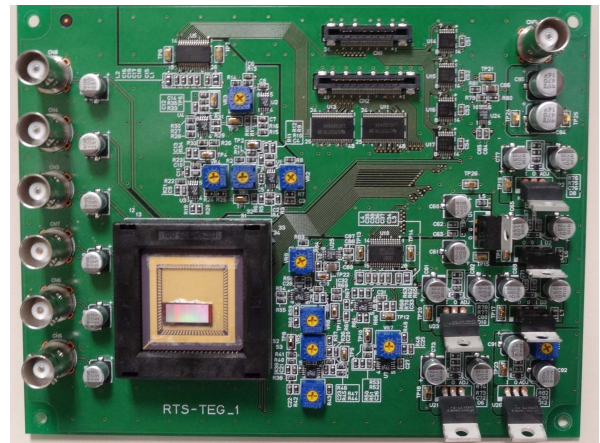
Recently, the impacts of RTN on the MOSFETs have become larger as the progression of CMOS circuit scaling down continues. It is known that RTN amplitude is greater as the number of channel carriers decreases. The channel carrier density ( $Q_{ch}$ ) is very small in the subthreshold region, and then RTN becomes very large even in the relatively large MOSFETs. Especially, the in-pixel source-follower transistors in CMOS image sensors are operated in near the subthreshold voltage region. RTN causes image quality degradation of CMOS image sensors [2, 3]. Consequently, a reduction of RTN is strongly required.

The amplitude and the time constants including the time to capture and the time to emission ( $\tau_c$  and  $\tau_e$ ) are important parameters of RTN characteristics. An accurate evaluation at these parameters is indispensable for an understanding of the mechanism of RTN. In this paper, we extracted  $\tau_c$  and  $\tau_e$  accurately in the subthreshold region and based on the experimental data of fabricated MOSFETs, we discuss about models of capture and emission processes with the traps which

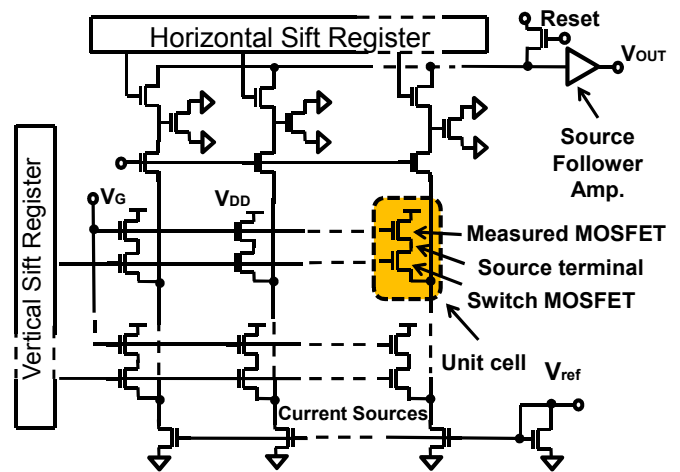
cause RTN.

## II. EXPERIMENTAL

The analysis of RTN requires a measuring numerous MOSFETs because the RTN characteristics:  $\tau_c$ ,  $\tau_e$  and amplitude, have large variation by the variation of the trap properties: energy level and special location and the variation of channel caused by the non-uniformity effect [4]. We employed the arrayed test circuit to detect and analyze RTN statistically from numerous MOSFETs in a short time [5, 6]. Fig.1 shows (a) Measurement system (b) the arrayed test circuit diagram. Measured MOSFETs are placed in an array, and a short time measurement is carried out by reading the output



(a) Measurement system



(b) Arrayed test circuit diagram.  
Figure 1. Measurement system

voltage ( $V_{out}$ ), while a constant drain current is applied. RTN appears as the voltage fluctuation of the output voltage which is the source terminal voltage of the measured MOSFET. The test circuit was fabricated by the standard 0.22  $\mu\text{m}$  CMOS technology. The gate oxide thickness ( $T_{ox}$ ), the gate length and the gate width of MOSFETs were 5.7 nm, 0.22  $\mu\text{m}$  and 0.28  $\mu\text{m}$ , respectively. 131072-MOSFETs were arrayed in the test pattern. Fig.2 shows the measurement sequence. To detect MOSFETs with RTN, a root mean square of  $V_{out}$  in time domain ( $V_{rms}$ ) were extracted with the sampling period of 0.7 s and record time of 600 s [5, 6].

We extracted MOSFETs of which  $V_{rms}$  were greater than 680  $\mu\text{V}$ . 8215-MOSFETs were extracted. Then, 137-MOSFETs were selected randomly for analyzing RTN characteristics by the high frequency sampling measurements. The RTN parameters of  $\tau_c$ ,  $\tau_e$  and the amplitude were extracted accurately with sampling period of 1  $\mu\text{s}$  and record time of 600 s ( $6 \times 10^8$  points) and set the same back bias ( $V_{bs}$ ) of -1.2 V was applied for every MOSFET. The back bias difference caused by threshold voltage ( $V_{th}$ ) variation was eliminated. For the simplicity of analysis, we removed RTN with more than two states after high frequency sampling (109 / 137 MOSFET). In this experiment we discuss the RTN time constants of twenty-eight MOSFETs with two states RTN.

Fig. 3 shows the method of RTN parameter extraction from the  $V_{gs}$ -time data [7]. Average values of  $\tau_c$  and  $\tau_e$  ( $\langle\tau_c\rangle$  and  $\langle\tau_e\rangle$ ) were extracted by fitting the distribution of extracted  $\tau_c$  and  $\tau_e$  using (1), assuming these phenomena follow the Poisson process [1].

$$\text{Counts}(\tau_{c,e}) = A \exp\left(-\frac{\tau_{c,e}}{\langle\tau_{c,e}\rangle}\right) \quad (1)$$

where A is a constant.

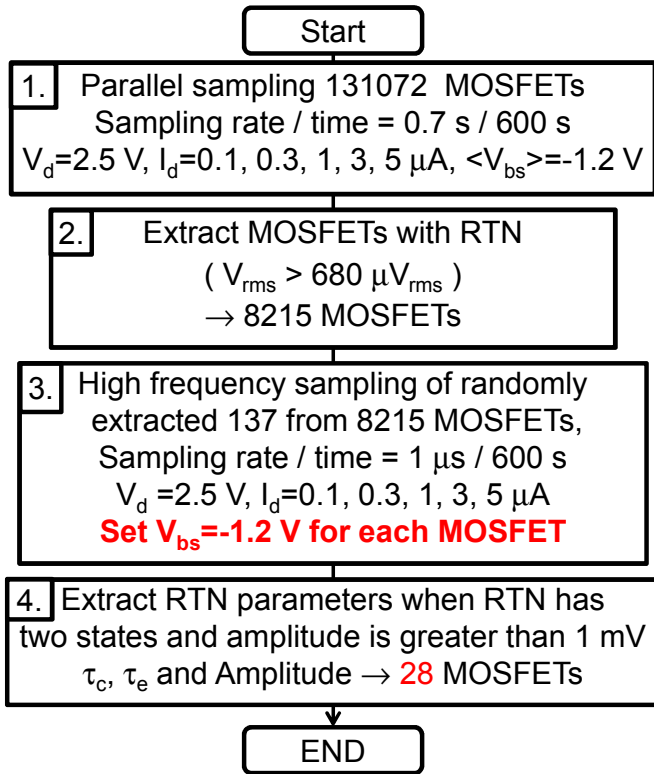


Figure 2. Measurement sequence

### III. RESULTS AND DISCUSSIONS

Fig.4 shows the cumulative probability of  $V_{rms}$  in Gumbel plot for five drain currents ( $I_d$ ).  $V_{rms}$  value increase as the decrease of  $I_d$ . It is because the screening effect of the potential barrier of the trapped charge becomes greater as the decrease of the number of the channel carriers [8].

Fig.5 shows the band diagram for the energy changing of trap in the oxide when  $V_{gs}$  changes. Assuming the trap energy level does not change as  $V_{gs}$  changes,  $E_t$  follows (2).

$$\Delta(E_t - E_c) = \frac{X \cdot \Delta V_{ox}}{T_{ox}} \quad (2)$$

The  $E_c$  and  $V_{ox}$  are the lowest energy of conduction band and applied oxide voltage. Assuming the distance between the trap and the electron to be captured is the same as X, and electrons are captured/emission of the conduction carrier by/from the inversion layer. The tunneling probability of the electron in channel to the trap and that of from the trap to the conduction band decreases and increases with  $V_{ox}$  increasing respectively. As a result, it is considered that  $\tau_c$  decreases and  $\tau_e$  increases with the increase of  $V_{gs}$ .

Fig.6 show the time constants as a function of  $V_{gs}$  for (a)  $\tau_e$  and (b)  $\tau_c$ . In Fig.6 (a), almost all  $\tau_e$  increase as the increase of  $V_{gs}$ . On the contrary,  $\tau_c$  decrease with  $V_{gs}$  increase for all samples. The slopes of  $\tau_c$  are much larger than those of  $\tau_e$ . When carrier is captured by the tunnel effect, the  $\tau_c$  follows (3).

$$\tau_c = \frac{1}{v_n \sigma_n Q_{ch}} \exp\left(\frac{E_t - E_c}{kT}\right) \quad (3)$$

Where  $v_n$ ,  $\sigma_n$ , k and T are thermal velocity, capture cross-section, Boltzmann constant and temperature, respectively. And then,  $\tau_c$  depends on the potential barrier from the channel to the trap and the number of channel carriers. Fig.7 shows the  $(\tau_c \times I_d)$  as a function of  $V_{gs}$ .  $\tau_c$  are normalized by  $Q_{ch}$ , assuming  $I_d$  is proportional to  $Q_{ch}$ . By normalizing by  $Q_{ch}$ ,  $(\tau_c \times I_d)$  is related the tunneling probability for one electron. For example (A) and (B),  $(\tau_c \times I_d)$  of the some samples decrease in the increase of  $V_{gs}$ .

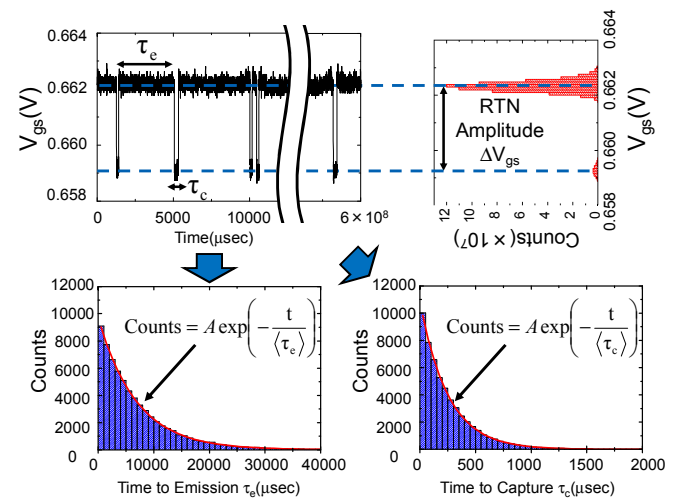


Figure 3. Definitions and extraction methods of  $\langle\tau_c\rangle$ ,  $\langle\tau_e\rangle$  and amplitude from RTN waveform data [7].

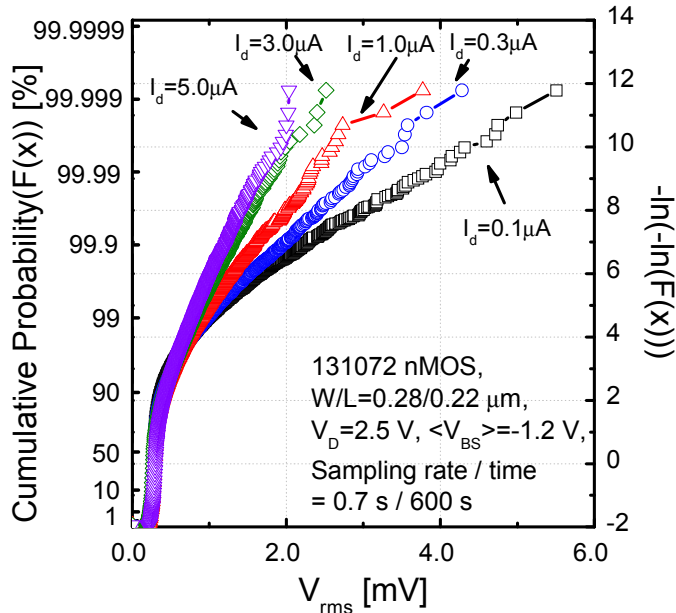


Figure 4. Cumulative probability of  $V_{rms}$  for five drain currents.

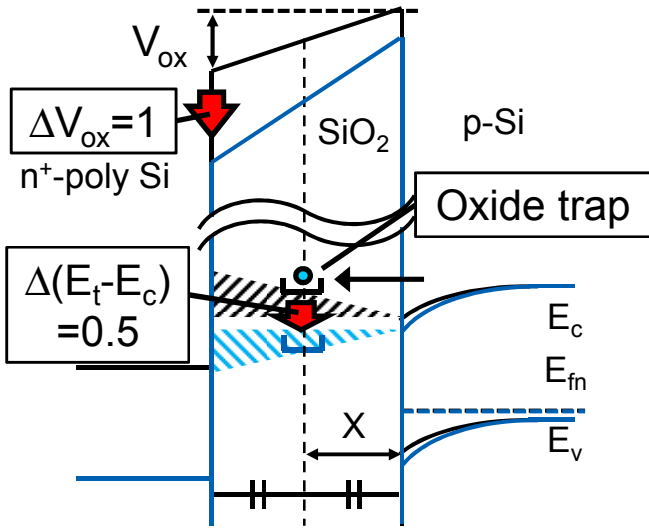
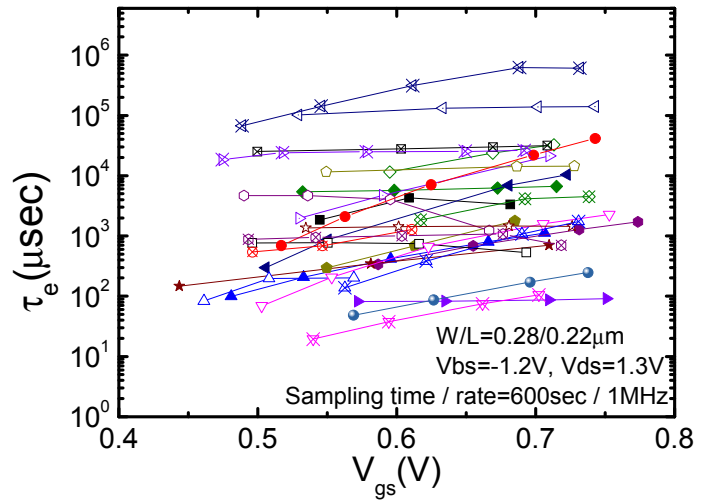


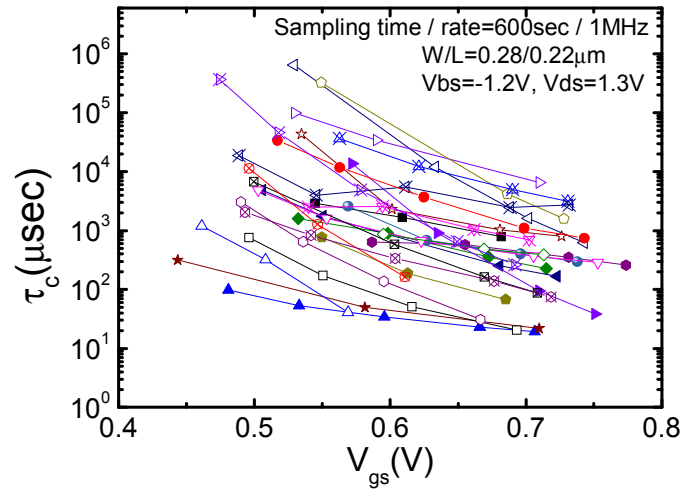
Figure 5. Band diagram of the trap energy changing as  $V_{gs}$  increasing.

and there is great variation among the slope of  $(\tau_c \times I_d)$ . On the contrary, for example (C),  $(\tau_c \times I_d)$  of the 10 samples increase with an increase of  $V_{gs}$ . These characteristics of (C) are very complicated and cannot be explained if the distance of trap and a carrier to be captured is the same as the trap depth. Fig.8 shows (a) 3D and (b) cross-sectional schematic views of locations of the trap and the channel of the type same as (C) in Fig.7. The carrier is captured from percolation path [4]. The percolation path is formed at the Si interface from the source to the drain locally, and then the distance between the trap and the electron to be captured is not the depth of trap ( $X$ ), and the carrier number in the percolation path is not defined as  $Q_{ch}$ . It is considered that the distance between the percolation path and the trap become longer as the increase of  $V_{gs}$ .

On the other hand, the emission is considered to be determined from the trap to the nearest state of either the Si substrate conduction band of Si substrate or the gate electrode regardless of the percolation path in Si substrate because there are the empty states in the conduction band exist in the silicon



(a) Slopes of  $\tau_e$  vs.  $V_{gs}$



(b) Slopes of  $\tau_c$  vs.  $V_{gs}$

Figure 6. Time constants as a function of  $V_{gs}$  for (a)  $\tau_e$  and (b)  $\tau_c$ .

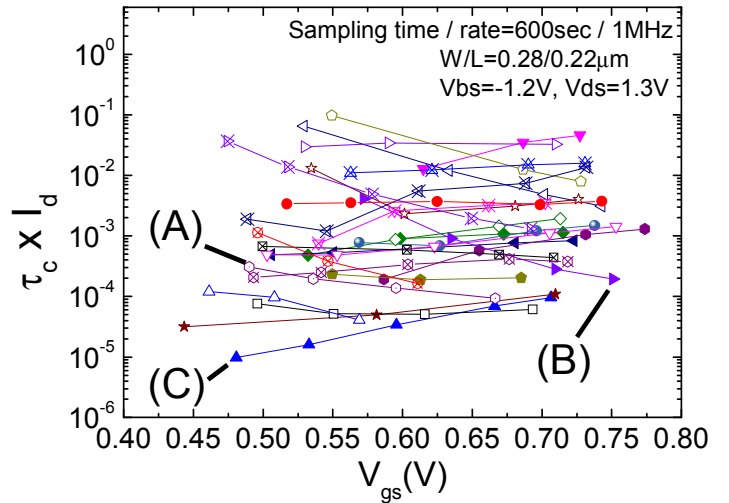


Figure 7. Normalized  $\tau_c$  ( $I_d \times \tau_c$ ) as a function of  $V_{gs}$   
By normalizing by  $Q_{ch}$ ,  $(\tau_c \times I_d)$  is related the tunneling probability for one electron.

surface. As mentioned above, the dependence of  $V_{gs}$  on  $\tau_c$  becomes complicated. When percolation paths are formed, and the number of trapped electron is one, it is considered that tunneling probability depends on only  $E_t$ ,  $X$ , and  $V_{gs}$ .

We classified the obtained dependencies of  $\tau_e$  on  $V_{gs}$  into three



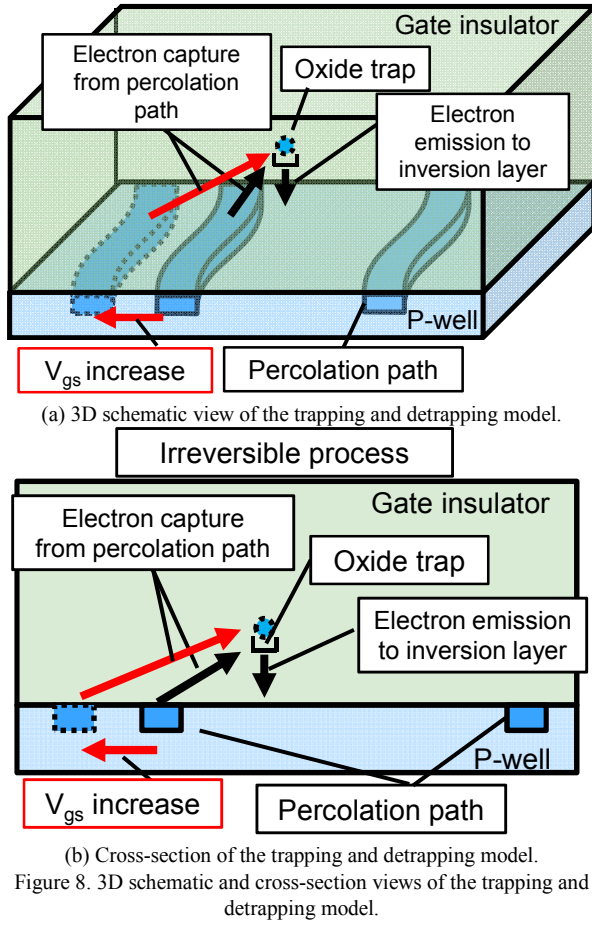


Figure 8. 3D schematic and cross-section views of the trapping and detrapping model.

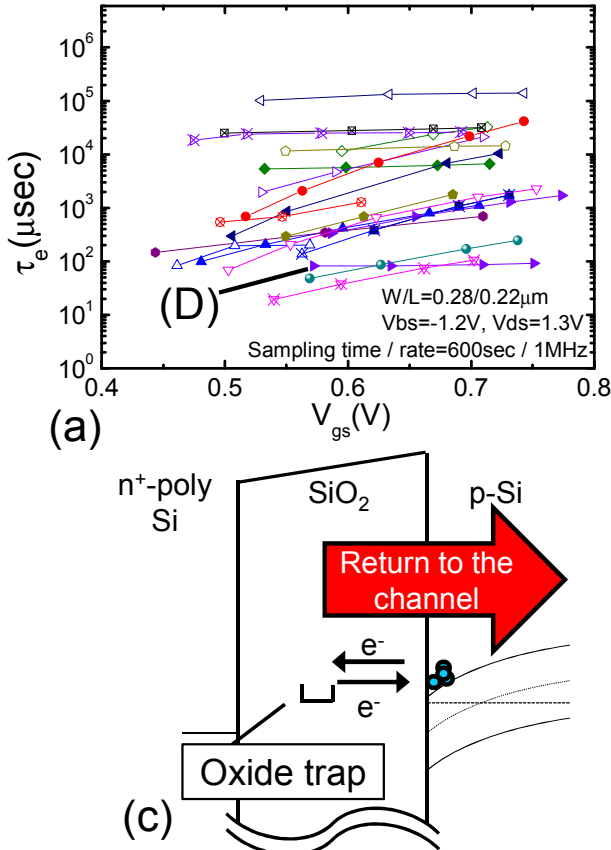


Figure 9. The measurement data and trap-detrapping model of category 1 ( $\tau_e$  monotone increasing).

(a)  $\tau_e$  as the function of  $V_{gs}$ , (b) RTN waveform  $I_d = 0.3 \sim 5\mu\text{A}$ , (c) Trap-detrapping model

categories as explained below. In Fig 9-11, (a)  $\tau_e$  as the function of  $V_{gs}$ , (b) RTN wave forms of typical (c) band diagram with trapping and detrapping process respectively for each category.

In category 1,  $\tau_e$  monotonically increases as the increase of  $V_{gs}$  as shown in Fig.9 (a). In Fig.9 (b), the amplitude becomes smaller and  $\tau_e$  becomes shorter with the increase of  $V_{gs}$  ( $I_d$ ). As shown in Fig.9 (b), (D) has two states RTN; these indicate that RTN of sample (D) is confirmed to be caused by one trap. It is considered that the tunneling probability decrease with an increase of  $V_{gs}$  and this indicates that the direction of emission is from the trap to the Si substrate side as shown in Fig.9(c).

In category 2,  $\tau_e$  monotonically decreases as the increase of  $V_{gs}$  as shown in Fig.10 (a). In Fig.10 (b), the amplitude becomes smaller,  $\tau_e$  becomes shorter with the increase of  $V_{gs}$  ( $I_d$ ) respectively. Then, these indicate that the RTN of sample (E) is defined to be caused by one trap. It is considered that tunneling probability increases with an increase of  $V_{gs}$  and the direction of emission is from the trap to the gate electrode side. In this case, the trapped carrier is emitted to the gate electrode side though the electron is captured from the Si substrate side to the trap, then the processes in category 2 are irreversible process as shown in Fig 10 (c).

In category 3,  $\tau_e$  increases with the increase of  $V_{gs}$  at small  $V_{gs}$  region, however  $\tau_e$  decreases with the increase of  $V_{gs}$  at a large  $V_{gs}$  region as shown in Fig.11 (a). In Fig.11 (b), RTN amplitude monotonically decreases with the increase of  $V_{gs}$  and  $\tau_e$  decreases with the increase of  $V_{gs}$  ( $I_d$ ), monotonically. It is

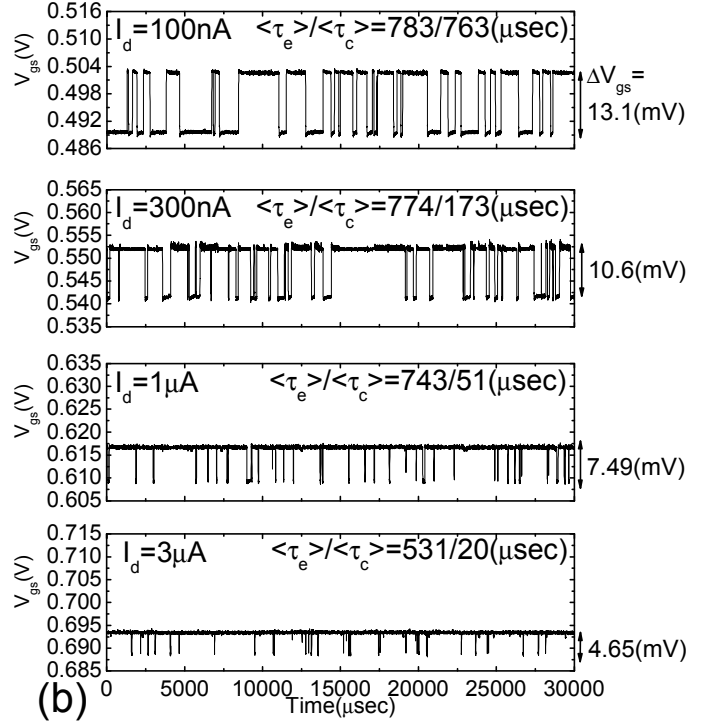
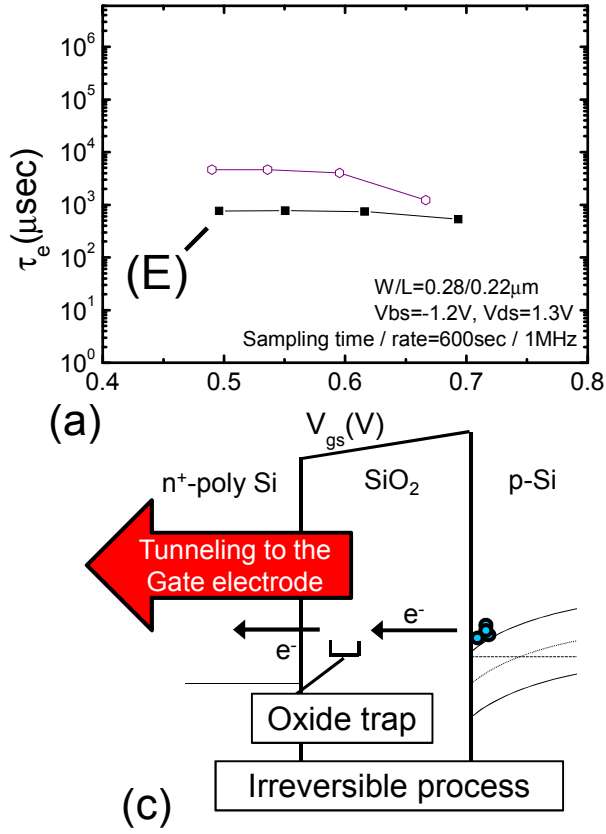


Figure 10. The measurement data and trap-detrap model of category 2 ( $\tau_e$  monotone decreasing).

(a)  $\tau_e$  as a function of  $V_{gs}$ , (b) RTN waveform  $I_d = 0.1 \sim 3 \mu A$ , (c) Trap-detrap model

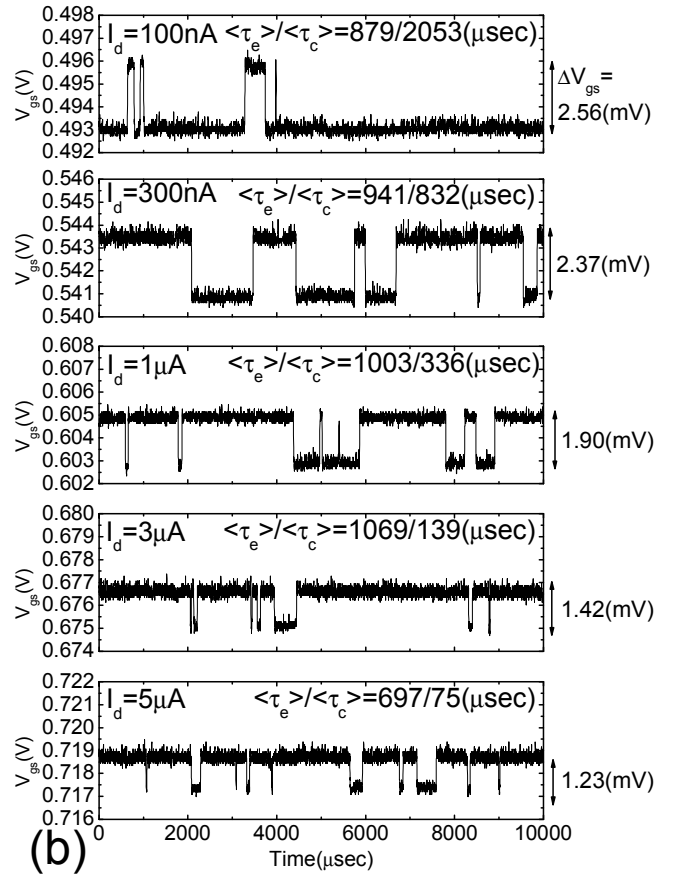
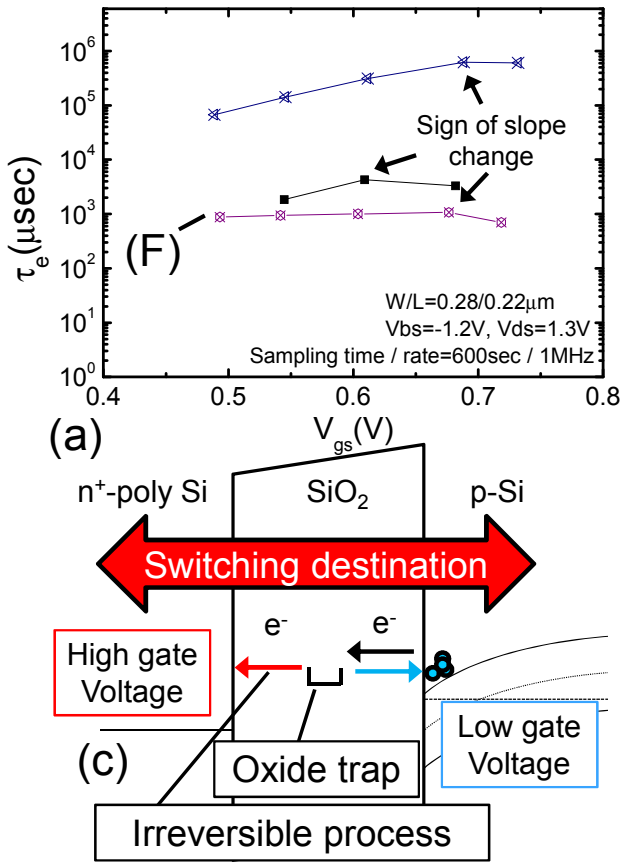


Figure 11. The measurement data and trap-detrap model of category 3 (the slope of  $\tau_e$  with regards to  $V_{gs}$  changes).

(a)  $\tau_e$  as a function of  $V_{gs}$ , (b) RTN waveform  $I_d = 0.1 \sim 5 \mu A$ , (c) Trap-detrap model

considered that the RTN of the sample (F) is caused by one trap. The tunneling probability dependence on  $V_{gs}$  changes at  $V_{gs}$  of 0.68 V. When small  $V_{gs}$  is applied, the trapped carrier is emitted to the Si substrate side, on the contrary when large  $V_{gs}$  is applied, the tunneling probability to the gate electrode side becomes larger than that to the Si substrate side. In this case as shown in Fig.11 (c), the trapped carrier is emitted to Si substrate side at the small  $V_{gs}$  region and to gate electrode side at the large  $V_{gs}$  region. When the trapped carrier is emitted to the gate electrode side, the process in category 3 is irreversible process.

#### IV. CONCLUSION

We extracted the various time constants of RTN and their dependence on  $V_{gs}$  and then proposed some trapping and detrapping to explain the experimental data of fabricated MOSFET. In our measurement the dependence of  $\tau_c$  on  $V_{gs}$  cannot be determined by the trap depth from the interface but by the distance between the trap and the carrier to be captured and the trap energy level. On the contrary, since time to emission is mainly determined by the  $V_{gs}$ . It is easy to understand emission processes compared to capture processes. We observed various emission processes caused by tunneling to Si substrate side, tunneling to gate electrode side and tunneling to either Si substrate side or gate electrode side depending on  $V_{gs}$ . Some of these categories are irreversible process and it is considered that these phenomena hardly follow Shockley-Read-Hall statistics [1, 9].

Evaluating the  $\tau_c$  and  $\tau_e$  individually is indispensable to characterize the RTN trap in subthreshold region of MOSFET operation.

#### ACKNOWLEDGMENT

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