PREV CLASS NEXT CLASS FRAMES NO FRAMES ALL CLASSES

SUMMARY: NESTED | FIELD | CONSTR | METHOD DETAIL: FIELD | CONSTR | METHOD

compact1, compact2, compact3 java.lang

Class Math

java.lang.Object java.lang.Math

public final class Math
extends Object

The class Math contains methods for performing basic numeric operations such as the elementary exponential, logarithm, square root, and trigonometric functions.

Unlike some of the numeric methods of class StrictMath, all implementations of the equivalent functions of class Math are not defined to return the bit-for-bit same results. This relaxation permits better-performing implementations where strict reproducibility is not required.

By default many of the Math methods simply call the equivalent method in StrictMath for their implementation. Code generators are encouraged to use platform-specific native libraries or microprocessor instructions, where available, to provide higher-performance implementations of Math methods. Such higher-performance implementations still must conform to the specification for Math.

The quality of implementation specifications concern two properties, accuracy of the returned result and monotonicity of the method. Accuracy of the floating-point Math methods is measured in terms of ulps, units in the last place. For a given floating-point format, an ulp of a specific real number value is the distance between the two floating-point values bracketing that numerical value. When discussing the accuracy of a method as a whole rather than at a specific argument, the number of ulps cited is for the worst-case error at any argument. If a method always has an error less than 0.5 ulps, the method always returns the floating-point number nearest the exact result; such a method is correctly rounded. A correctly rounded method is generally the best a floating-point approximation can be; however, it is impractical for many floating-point methods to be correctly rounded. Instead, for the Math class, a larger error bound of 1 or 2 ulps is allowed for certain methods. Informally, with a 1 ulp error bound, when the exact result is a representable number, the exact result should be returned as the computed result; otherwise, either of the two floating-point values which bracket the exact result may be returned. For exact results large in magnitude, one of the endpoints of the bracket may be infinite. Besides accuracy at individual arguments, maintaining proper relations between the method at different arguments is also important. Therefore, most methods with more than 0.5 ulp errors are required to be semi-monotonic: whenever the mathematical function is non-decreasing, so is the floating-point approximation, likewise, whenever the mathematical function is non-increasing, so is the floating-point approximation. Not all approximations that have 1 ulp accuracy will automatically meet the monotonicity requirements.

The platform uses signed two's complement integer arithmetic with int and long primitive types. The developer should choose the primitive type to ensure that arithmetic operations consistently produce correct results, which in some cases means the operations will not overflow the range of values of the computation. The best practice is to choose the primitive type and algorithm to avoid overflow. In cases where the size is int or long and overflow errors need to be detected, the methods addExact, subtractExact, multiplyExact, and toIntExact throw an ArithmeticException when the results overflow. For other arithmetic operations such as divide, absolute value, increment, decrement, and negation overflow occurs only with a specific minimum or maximum value and should be checked against the minimum or maximum as appropriate.

Since:

JDK1.0

Field Summary

Fields

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Modifier and Type	Field and Description	
static double	E The double value that is closer than any other to e , the base of the natural logarithms.	
static double	PI The double value that is closer than any other to <i>pi</i> , the ratio of the circumference of a circle to its diameter.	

Concrete Methods

Method Summary

Static Methods

All Mathods

All Methods Stati	ic Methods Concrete Methods
Modifier and Type	Method and Description
static double	<pre>abs(double a) Returns the absolute value of a double value.</pre>
static float	<pre>abs(float a) Returns the absolute value of a float value.</pre>
static int	<pre>abs(int a) Returns the absolute value of an int value.</pre>
static long	<pre>abs(long a) Returns the absolute value of a long value.</pre>
static double	acos (double a) Returns the arc cosine of a value; the returned angle is in the range 0.0 through pi .

static int addExact(int x, int y)

Returns the sum of its arguments, throwing an exception if the

result overflows an int.

static long addExact(long x, long y)

Returns the sum of its arguments, throwing an exception if the

result overflows a long.

static double asin(double a)

Returns the arc sine of a value; the returned angle is in the range -

pi/2 through pi/2.

static double atan(double a)

Returns the arc tangent of a value; the returned angle is in the

range -pi/2 through pi/2.

static double atan2(double y, double x)

Returns the angle *theta* from the conversion of rectangular

coordinates (x, y) to polar coordinates (r, theta).

static double cbrt(double a)

Returns the cube root of a double value.

static double ceil(double a)

Returns the smallest (closest to negative infinity) double value that

is greater than or equal to the argument and is equal to a

mathematical integer.

static double copySign(double magnitude, double sign)

Returns the first floating-point argument with the sign of the

second floating-point argument.

static float copySign(float magnitude, float sign)

Returns the first floating-point argument with the sign of the

second floating-point argument.

static double cos(double a)

Returns the trigonometric cosine of an angle.

static double cosh(double x)

Returns the hyperbolic cosine of a double value.

static int decrementExact(int a)

Returns the argument decremented by one, throwing an exception

if the result overflows an int.

static long decrementExact(long a)

Returns the argument decremented by one, throwing an exception

if the result overflows a long.

static double exp(double a)

Returns Euler's number *e* raised to the power of a double value. static double expm1(double x) Returns e^{x} -1. static double floor(double a) Returns the largest (closest to positive infinity) double value that is less than or equal to the argument and is equal to a mathematical integer. static int floorDiv(int x, int y) Returns the largest (closest to positive infinity) int value that is less than or equal to the algebraic quotient. floorDiv(long x, long y) static long Returns the largest (closest to positive infinity) long value that is less than or equal to the algebraic quotient. floorMod(int x, int y) static int Returns the floor modulus of the int arguments. static long floorMod(long x, long y) Returns the floor modulus of the long arguments. static int getExponent(double d) Returns the unbiased exponent used in the representation of a double. static int getExponent(float f) Returns the unbiased exponent used in the representation of a float. static double hypot(double x, double y) Returns $\operatorname{sgrt}(x^2 + y^2)$ without intermediate overflow or underflow. static double IEEEremainder(double f1, double f2) Computes the remainder operation on two arguments as prescribed by the IEEE 754 standard. static int incrementExact(int a) Returns the argument incremented by one, throwing an exception if the result overflows an int. static long incrementExact(long a) Returns the argument incremented by one, throwing an exception if the result overflows a long. static double log(double a) Returns the natural logarithm (base e) of a double value. static double

log10(double a)

Returns the base 10 logarithm of a double value.

static double log1p(double x) Returns the natural logarithm of the sum of the argument and 1. max(double a, double b) static double Returns the greater of two double values. static float max(float a, float b) Returns the greater of two float values. static int max(int a, int b) Returns the greater of two int values. max(long a, long b) static long Returns the greater of two long values. static double min(double a, double b) Returns the smaller of two double values. static float min(float a, float b) Returns the smaller of two float values. static int min(int a, int b) Returns the smaller of two int values. static long min(long a, long b) Returns the smaller of two long values. static int multiplyExact(int x, int y) Returns the product of the arguments, throwing an exception if the result overflows an int. multiplyExact(long x, long y) static long Returns the product of the arguments, throwing an exception if the result overflows a long. static int negateExact(int a) Returns the negation of the argument, throwing an exception if the result overflows an int. static long negateExact(long a) Returns the negation of the argument, throwing an exception if the result overflows a long. static double nextAfter(double start, double direction) Returns the floating-point number adjacent to the first argument in the direction of the second argument. static float nextAfter(float start, double direction) Returns the floating-point number adjacent to the first argument in the direction of the second argument. static double nextDown(double d)

Returns the floating-point value adjacent to d in the direction of negative infinity.

Returns the floating-point value adjacent to f in the direction of negative infinity.

static double nextUp(double d)

Returns the floating-point value adjacent to d in the direction of positive infinity.

Returns the floating-point value adjacent to f in the direction of positive infinity.

Returns the value of the first argument raised to the power of the second argument.

static double random()

Returns a double value with a positive sign, greater than or equal to 0.0 and less than 1.0.

static double rint(double a)

Returns the double value that is closest in value to the argument and is equal to a mathematical integer.

static long round(double a)

Returns the closest long to the argument, with ties rounding to positive infinity.

static int round(float a)

Returns the closest int to the argument, with ties rounding to positive infinity.

static double scalb(double d, int scaleFactor)

Returns $d \times 2^{\text{scaleFactor}}$ rounded as if performed by a single correctly rounded floating-point multiply to a member of the double value set.

Returns $f \times 2^{\text{scaleFactor}}$ rounded as if performed by a single correctly rounded floating-point multiply to a member of the float value set.

static double signum(double d)

Returns the signum function of the argument; zero if the argument is zero, 1.0 if the argument is greater than zero, -1.0 if the argument is less than zero.

static float signum(float f)

Returns the signum function of the argument; zero if the argument

is zero, 1.0f if the argument is greater than zero, -1.0f if the

argument is less than zero.

static double sin(double a)

Returns the trigonometric sine of an angle.

static double sinh(double x)

Returns the hyperbolic sine of a double value.

static double sqrt(double a)

Returns the correctly rounded positive square root of a double

value.

static int subtractExact(int x, int y)

Returns the difference of the arguments, throwing an exception if

the result overflows an int.

Returns the difference of the arguments, throwing an exception if

the result overflows a long.

static double tan(double a)

Returns the trigonometric tangent of an angle.

static double tanh(double x)

Returns the hyperbolic tangent of a double value.

static double toDegrees(double angrad)

Converts an angle measured in radians to an approximately

equivalent angle measured in degrees.

static int toIntExact(long value)

Returns the value of the long argument; throwing an exception if

the value overflows an int.

static double toRadians(double angdeg)

Converts an angle measured in degrees to an approximately

equivalent angle measured in radians.

static double **ulp**(double d)

Returns the size of an ulp of the argument.

static float ulp(float f)

Returns the size of an ulp of the argument.

Methods inherited from class java.lang.Object

clone, equals, finalize, getClass, hashCode, notify, notifyAll, toString,
wait, wait

Field Detail

E

public static final double E

The double value that is closer than any other to *e*, the base of the natural logarithms.

See Also:

Constant Field Values

PΙ

public static final double PI

The double value that is closer than any other to *pi*, the ratio of the circumference of a circle to its diameter.

See Also:

Constant Field Values

Method Detail

sin

public static double sin(double a)

Returns the trigonometric sine of an angle. Special cases:

- If the argument is NaN or an infinity, then the result is NaN.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result. Results must be semimonotonic.

Parameters:

a - an angle, in radians.

Returns:

the sine of the argument.

cos

public static double cos(double a)

Returns the trigonometric cosine of an angle. Special cases:

• If the argument is NaN or an infinity, then the result is NaN.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - an angle, in radians.

Returns:

the cosine of the argument.

tan

public static double tan(double a)

Returns the trigonometric tangent of an angle. Special cases:

- If the argument is NaN or an infinity, then the result is NaN.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - an angle, in radians.

Returns:

the tangent of the argument.

asin

public static double asin(double a)

Returns the arc sine of a value; the returned angle is in the range -pi/2 through pi/2. Special cases:

- If the argument is NaN or its absolute value is greater than 1, then the result is NaN.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - the value whose arc sine is to be returned.

Returns:

the arc sine of the argument.

acos

public static double acos(double a)

Returns the arc cosine of a value; the returned angle is in the range 0.0 through pi. Special case:

• If the argument is NaN or its absolute value is greater than 1, then the result is NaN.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - the value whose arc cosine is to be returned.

Returns:

the arc cosine of the argument.

atan

public static double atan(double a)

Returns the arc tangent of a value; the returned angle is in the range -pi/2 through pi/2. Special cases:

- If the argument is NaN, then the result is NaN.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - the value whose arc tangent is to be returned.

Returns:

the arc tangent of the argument.

toRadians

public static double toRadians(double angdeg)

Converts an angle measured in degrees to an approximately equivalent angle measured in radians. The conversion from degrees to radians is generally inexact.

Parameters:

angdeg - an angle, in degrees

Returns:

the measurement of the angle angdeg in radians.

Since:

1.2

toDegrees

public static double toDegrees(double angrad)

Converts an angle measured in radians to an approximately equivalent angle measured in degrees. The conversion from radians to degrees is generally inexact; users should *not* expect cos(toRadians(90.0)) to exactly equal 0.0.

Parameters:

angrad - an angle, in radians

Returns:

the measurement of the angle angrad in degrees.

Since:

1.2

exp

public static double exp(double a)

Returns Euler's number *e* raised to the power of a double value. Special cases:

- If the argument is NaN, the result is NaN.
- If the argument is positive infinity, then the result is positive infinity.
- If the argument is negative infinity, then the result is positive zero.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - the exponent to raise e to.

Returns:

the value e^a , where e is the base of the natural logarithms.

log

public static double log(double a)

Returns the natural logarithm (base e) of a double value. Special cases:

- If the argument is NaN or less than zero, then the result is NaN.
- If the argument is positive infinity, then the result is positive infinity.
- If the argument is positive zero or negative zero, then the result is negative infinity.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - a value

Returns:

the value ln a, the natural logarithm of a.

log10

public static double log10(double a)

Returns the base 10 logarithm of a double value. Special cases:

- If the argument is NaN or less than zero, then the result is NaN.
- If the argument is positive infinity, then the result is positive infinity.
- If the argument is positive zero or negative zero, then the result is negative infinity.
- If the argument is equal to 10^n for integer n, then the result is n.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

a - a value

Returns:

the base 10 logarithm of a.

Since:

1.5

sart

public static double sqrt(double a)

Returns the correctly rounded positive square root of a double value. Special cases:

- If the argument is NaN or less than zero, then the result is NaN.
- If the argument is positive infinity, then the result is positive infinity.
- If the argument is positive zero or negative zero, then the result is the same as the argument.

Otherwise, the result is the double value closest to the true mathematical square root of the argument value.

Parameters:

a - a value.

Returns:

the positive square root of a. If the argument is NaN or less than zero, the result is NaN.

cbrt

public static double cbrt(double a)

Returns the cube root of a double value. For positive finite x, cbrt(-x) == -cbrt(x); that is, the cube root of a negative value is the negative of the cube root of that value's magnitude. Special cases:

If the argument is NaN, then the result is NaN.

- If the argument is infinite, then the result is an infinity with the same sign as the argument.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result.

Parameters:

a - a value.

Returns:

the cube root of a.

Since:

1.5

IEEEremainder

Computes the remainder operation on two arguments as prescribed by the IEEE 754 standard. The remainder value is mathematically equal to $f1 - f2 \times n$, where n is the mathematical integer closest to the exact mathematical value of the quotient f1/f2, and if two mathematical integers are equally close to f1/f2, then n is the integer that is even. If the remainder is zero, its sign is the same as the sign of the first argument. Special cases:

- If either argument is NaN, or the first argument is infinite, or the second argument is positive zero or negative zero, then the result is NaN.
- If the first argument is finite and the second argument is infinite, then the result is the same as the first argument.

Parameters:

fl - the dividend.

f2 - the divisor.

Returns:

the remainder when f1 is divided by f2.

ceil

```
public static double ceil(double a)
```

Returns the smallest (closest to negative infinity) double value that is greater than or equal to the argument and is equal to a mathematical integer. Special cases:

- If the argument value is already equal to a mathematical integer, then the result is the same as the argument.
- If the argument is NaN or an infinity or positive zero or negative zero, then the result is the same as the argument.
- If the argument value is less than zero but greater than -1.0, then the result is negative zero.

Note that the value of Math.ceil(x) is exactly the value of -Math.floor(-x).

Parameters:

a - a value.

Returns:

the smallest (closest to negative infinity) floating-point value that is greater than or equal to the argument and is equal to a mathematical integer.

floor

public static double floor(double a)

Returns the largest (closest to positive infinity) double value that is less than or equal to the argument and is equal to a mathematical integer. Special cases:

- If the argument value is already equal to a mathematical integer, then the result is the same as the argument.
- If the argument is NaN or an infinity or positive zero or negative zero, then the result is the same as the argument.

Parameters:

a - a value.

Returns:

the largest (closest to positive infinity) floating-point value that less than or equal to the argument and is equal to a mathematical integer.

rint

public static double rint(double a)

Returns the double value that is closest in value to the argument and is equal to a mathematical integer. If two double values that are mathematical integers are equally close, the result is the integer value that is even. Special cases:

- If the argument value is already equal to a mathematical integer, then the result is the same as the argument.
- If the argument is NaN or an infinity or positive zero or negative zero, then the result is the same as the argument.

Parameters:

a - a double value.

Returns:

the closest floating-point value to a that is equal to a mathematical integer.

atan2

Returns the angle *theta* from the conversion of rectangular coordinates (x, y) to polar coordinates (r, theta). This method computes the phase *theta* by computing an arc tangent of y/x in the range of -pi to pi. Special cases:

- If either argument is NaN, then the result is NaN.
- If the first argument is positive zero and the second argument is positive, or the first argument is positive and finite and the second argument is positive infinity, then the result is positive zero.
- If the first argument is negative zero and the second argument is positive, or the first argument is negative and finite and the second argument is positive infinity, then the result is negative zero.
- If the first argument is positive zero and the second argument is negative, or the first argument is positive and finite and the second argument is negative infinity, then the result is the double value closest to *pi*.
- If the first argument is negative zero and the second argument is negative, or the first argument is negative and finite and the second argument is negative infinity, then the result is the double value closest to -pi.
- If the first argument is positive and the second argument is positive zero or negative zero, or the first argument is positive infinity and the second argument is finite, then the result is the double value closest to pi/2.
- If the first argument is negative and the second argument is positive zero or negative zero, or the first argument is negative infinity and the second argument is finite, then the result is the double value closest to -pi/2.
- If both arguments are positive infinity, then the result is the double value closest to pi/4.
- If the first argument is positive infinity and the second argument is negative infinity, then the result is the double value closest to 3*pi/4.
- If the first argument is negative infinity and the second argument is positive infinity, then the result is the double value closest to -pi/4.
- If both arguments are negative infinity, then the result is the double value closest to -3*pi/4.

The computed result must be within 2 ulps of the exact result. Results must be semi-monotonic.

Parameters:

- y the ordinate coordinate
- x the abscissa coordinate

Returns:

the *theta* component of the point (r, theta) in polar coordinates that corresponds to the point (x, y) in Cartesian coordinates.

pow

Returns the value of the first argument raised to the power of the second argument. Special cases:

- If the second argument is positive or negative zero, then the result is 1.0.
- If the second argument is 1.0, then the result is the same as the first argument.
- If the second argument is NaN, then the result is NaN.
- If the first argument is NaN and the second argument is nonzero, then the result is NaN.
- If
- the absolute value of the first argument is greater than 1 and the second argument is positive infinity, or
- the absolute value of the first argument is less than 1 and the second argument is negative infinity,

then the result is positive infinity.

- If
- the absolute value of the first argument is greater than 1 and the second argument is negative infinity, or
- the absolute value of the first argument is less than 1 and the second argument is positive infinity,

then the result is positive zero.

- If the absolute value of the first argument equals 1 and the second argument is infinite, then the result is NaN.
- If
- the first argument is positive zero and the second argument is greater than zero, or
- ullet the first argument is positive infinity and the second argument is less than zero, then the result is positive zero.
- If
- $\bullet\,$ the first argument is positive zero and the second argument is less than zero, or
- the first argument is positive infinity and the second argument is greater than zero,

then the result is positive infinity.

- If
- the first argument is negative zero and the second argument is greater than zero but not a finite odd integer, or
- the first argument is negative infinity and the second argument is less than zero but not a finite odd integer,

then the result is positive zero.

- If
- the first argument is negative zero and the second argument is a positive finite odd integer, or
- the first argument is negative infinity and the second argument is a negative finite odd integer,

then the result is negative zero.

- If
- the first argument is negative zero and the second argument is less than zero but not a finite odd integer, or
- the first argument is negative infinity and the second argument is greater than zero but not a finite odd integer,

then the result is positive infinity.

If

- the first argument is negative zero and the second argument is a negative finite odd integer, or
- the first argument is negative infinity and the second argument is a positive finite odd integer,

then the result is negative infinity.

- · If the first argument is finite and less than zero
 - if the second argument is a finite even integer, the result is equal to the result of raising the absolute value of the first argument to the power of the second argument
 - if the second argument is a finite odd integer, the result is equal to the negative
 of the result of raising the absolute value of the first argument to the power of
 the second argument
 - if the second argument is finite and not an integer, then the result is NaN.
- If both arguments are integers, then the result is exactly equal to the mathematical result of raising the first argument to the power of the second argument if that result can in fact be represented exactly as a double value.

(In the foregoing descriptions, a floating-point value is considered to be an integer if and only if it is finite and a fixed point of the method ceil or, equivalently, a fixed point of the method floor. A value is a fixed point of a one-argument method if and only if the result of applying the method to the value is equal to the value.)

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

- a the base.
- b the exponent.

Returns:

the value a^b.

round

public static int round(float a)

Returns the closest int to the argument, with ties rounding to positive infinity.

Special cases:

- If the argument is NaN, the result is 0.
- If the argument is negative infinity or any value less than or equal to the value of Integer.MIN VALUE, the result is equal to the value of Integer.MIN VALUE.
- If the argument is positive infinity or any value greater than or equal to the value of Integer.MAX_VALUE, the result is equal to the value of Integer.MAX_VALUE.

Parameters:

a - a floating-point value to be rounded to an integer.

Returns:

the value of the argument rounded to the nearest int value.

See Also:

Integer.MAX VALUE, Integer.MIN VALUE

round

public static long round(double a)

Returns the closest long to the argument, with ties rounding to positive infinity.

Special cases:

- If the argument is NaN, the result is 0.
- If the argument is negative infinity or any value less than or equal to the value of Long.MIN_VALUE, the result is equal to the value of Long.MIN_VALUE.
- If the argument is positive infinity or any value greater than or equal to the value of Long.MAX_VALUE, the result is equal to the value of Long.MAX_VALUE.

Parameters:

a - a floating-point value to be rounded to a long.

Returns:

the value of the argument rounded to the nearest long value.

See Also:

Long.MAX VALUE, Long.MIN VALUE

random

public static double random()

Returns a double value with a positive sign, greater than or equal to 0.0 and less than 1.0. Returned values are chosen pseudorandomly with (approximately) uniform distribution from that range.

When this method is first called, it creates a single new pseudorandom-number generator, exactly as if by the expression

```
new java.util.Random()
```

This new pseudorandom-number generator is used thereafter for all calls to this method and is used nowhere else.

This method is properly synchronized to allow correct use by more than one thread. However, if many threads need to generate pseudorandom numbers at a great rate, it may reduce contention for each thread to have its own pseudorandom-number generator.

Returns:

a pseudorandom double greater than or equal to 0.0 and less than 1.0.

See Also:

```
Random.nextDouble()
```

addExact

Returns the sum of its arguments, throwing an exception if the result overflows an int.

Parameters:

```
x - the first value
```

y - the second value

Returns:

the result

Throws:

ArithmeticException - if the result overflows an int

Since:

1.8

addExact

Returns the sum of its arguments, throwing an exception if the result overflows a long.

Parameters:

```
x - the first value
```

y - the second value

Returns:

the result

Throws:

ArithmeticException - if the result overflows a long

Since:

1.8

subtractExact

Returns the difference of the arguments, throwing an exception if the result overflows an int.

```
Parameters:
x - the first value
y - the second value to subtract from the first

Returns:
the result
Throws:
ArithmeticException - if the result overflows an int
Since:
```

subtractExact

1.8

Returns the difference of the arguments, throwing an exception if the result overflows a long.

Parameters:

x - the first value

y - the second value to subtract from the first

Returns:

the result

Throws:

ArithmeticException - if the result overflows a long

Since

1.8

multiplyExact

Returns the product of the arguments, throwing an exception if the result overflows an int.

Parameters:

x - the first value

y - the second value

Returns:

the result

Throws:

ArithmeticException - if the result overflows an int Since:
1.8

multiplyExact

Returns the product of the arguments, throwing an exception if the result overflows a long.

Parameters:

x - the first value

y - the second value

Returns:

the result

Throws:

ArithmeticException - if the result overflows a long

Since:

1.8

incrementExact

```
public static int incrementExact(int a)
```

Returns the argument incremented by one, throwing an exception if the result overflows an int.

Parameters:

a - the value to increment

Returns:

the result

Throws:

ArithmeticException - if the result overflows an int

Since:

1.8

incrementExact

public static long incrementExact(long a)

Returns the argument incremented by one, throwing an exception if the result overflows a long.

Parameters:

a - the value to increment

Returns:

the result

Throws:

ArithmeticException - if the result overflows a long

Since:

1.8

decrementExact

public static int decrementExact(int a)

Returns the argument decremented by one, throwing an exception if the result overflows an int.

Parameters:

a - the value to decrement

Returns:

the result

Throws:

ArithmeticException - if the result overflows an int

Since:

1.8

decrementExact

public static long decrementExact(long a)

Returns the argument decremented by one, throwing an exception if the result overflows a long.

Parameters:

a - the value to decrement

Returns:

the result

Throws:

ArithmeticException - if the result overflows a long

Since:

negateExact

public static int negateExact(int a)

Returns the negation of the argument, throwing an exception if the result overflows an int.

Parameters:

a - the value to negate

Returns:

the result

Throws:

ArithmeticException - if the result overflows an int

Since:

1.8

negateExact

public static long negateExact(long a)

Returns the negation of the argument, throwing an exception if the result overflows a long.

Parameters:

a - the value to negate

Returns:

the result

Throws:

ArithmeticException - if the result overflows a long

Since:

1.8

toIntExact

public static int toIntExact(long value)

Returns the value of the long argument; throwing an exception if the value overflows an int.

Parameters:

value - the long value

Returns:

the argument as an int

Throws:

ArithmeticException - if the argument overflows an int

Since:

1.8

floorDiv

Returns the largest (closest to positive infinity) int value that is less than or equal to the algebraic quotient. There is one special case, if the dividend is the Integer.MIN_VALUE and the divisor is -1, then integer overflow occurs and the result is equal to the Integer.MIN_VALUE.

Normal integer division operates under the round to zero rounding mode (truncation). This operation instead acts under the round toward negative infinity (floor) rounding mode. The floor rounding mode gives different results than truncation when the exact result is negative.

- If the signs of the arguments are the same, the results of floorDiv and the / operator are the same.
 - For example, floorDiv(4, 3) == 1 and (4 / 3) == 1.
- If the signs of the arguments are different, the quotient is negative and floorDiv returns the integer less than or equal to the quotient and the / operator returns the integer closest to zero.

For example, floorDiv(-4, 3) == -2, whereas (-4 / 3) == -1.

Parameters:

```
x - the dividend
```

y - the divisor

Returns:

the largest (closest to positive infinity) int value that is less than or equal to the algebraic quotient.

Throws:

ArithmeticException - if the divisor y is zero

Since:

1.8

See Also:

floorMod(int, int), floor(double)

floorDiv

Returns the largest (closest to positive infinity) long value that is less than or equal to the algebraic quotient. There is one special case, if the dividend is the Long.MIN_VALUE and the divisor is -1, then integer overflow occurs and the result is equal to the Long.MIN_VALUE.

Normal integer division operates under the round to zero rounding mode (truncation). This operation instead acts under the round toward negative infinity (floor) rounding mode. The floor rounding mode gives different results than truncation when the exact result is negative.

For examples, see floorDiv(int, int).

Parameters:

x - the dividend

y - the divisor

Returns:

the largest (closest to positive infinity) long value that is less than or equal to the algebraic quotient.

Throws:

ArithmeticException - if the divisor y is zero

Since:

1.8

See Also:

floorMod(long, long), floor(double)

floorMod

Returns the floor modulus of the int arguments.

The floor modulus is x - (floorDiv(x, y) * y), has the same sign as the divisor y, and is in the range of -abs(y) < r < +abs(y).

The relationship between floorDiv and floorMod is such that:

```
• floorDiv(x, y) * y + floorMod(x, y) == x
```

The difference in values between floorMod and the % operator is due to the difference between floorDiv that returns the integer less than or equal to the quotient and the / operator that returns the integer closest to zero.

Examples:

- If the signs of the arguments are the same, the results of floorMod and the % operator are the same.
 - floorMod(4, 3) == 1; and (4 % 3) == 1
- If the signs of the arguments are different, the results differ from the % operator.
 - floorMod(+4, -3) == -2; and (+4 % -3) == +1
 - floorMod(-4, +3) == +2; and (-4 % +3) == -1
 - floorMod(-4, -3) == -1; and (-4 % -3) == -1

If the signs of arguments are unknown and a positive modulus is needed it can be computed as (floorMod(x, y) + abs(y)) % abs(y).

Parameters:

```
x - the dividend
```

y - the divisor

Returns:

```
the floor modulus x - (floorDiv(x, y) * y)
```

Throws:

ArithmeticException - if the divisor y is zero

Since:

1.8

See Also:

floorDiv(int, int)

floorMod

Returns the floor modulus of the long arguments.

The floor modulus is x - (floorDiv(x, y) * y), has the same sign as the divisor y, and is in the range of -abs(y) < r < +abs(y).

The relationship between floorDiv and floorMod is such that:

• floorDiv(x, y) * y + floorMod(x, y) == x

For examples, see floorMod(int, int).

Parameters:

```
x - the dividend
```

v - the divisor

Returns:

the floor modulus x - (floorDiv(x, y) * y)

Throws:

ArithmeticException - if the divisor y is zero

Since:

1.8

See Also:

floorDiv(long, long)

abs

```
public static int abs(int a)
```

Returns the absolute value of an int value. If the argument is not negative, the argument is returned. If the argument is negative, the negation of the argument is returned.

Note that if the argument is equal to the value of Integer.MIN_VALUE, the most negative representable int value, the result is that same value, which is negative.

Parameters:

a - the argument whose absolute value is to be determined

Returns:

the absolute value of the argument.

abs

public static long abs(long a)

Returns the absolute value of a long value. If the argument is not negative, the argument is returned. If the argument is negative, the negation of the argument is returned.

Note that if the argument is equal to the value of Long.MIN_VALUE, the most negative representable long value, the result is that same value, which is negative.

Parameters:

a - the argument whose absolute value is to be determined

Returns:

the absolute value of the argument.

abs

```
public static float abs(float a)
```

Returns the absolute value of a float value. If the argument is not negative, the argument is returned. If the argument is negative, the negation of the argument is returned. Special cases:

- If the argument is positive zero or negative zero, the result is positive zero.
- If the argument is infinite, the result is positive infinity.
- If the argument is NaN, the result is NaN.

In other words, the result is the same as the value of the expression:

Float.intBitsToFloat(0x7fffffff & Float.floatToIntBits(a))

Parameters:

a - the argument whose absolute value is to be determined

Returns:

the absolute value of the argument.

abs

public static double abs(double a)

Returns the absolute value of a double value. If the argument is not negative, the argument is returned. If the argument is negative, the negation of the argument is returned. Special cases:

- If the argument is positive zero or negative zero, the result is positive zero.
- If the argument is infinite, the result is positive infinity.
- If the argument is NaN, the result is NaN.

In other words, the result is the same as the value of the expression:

Double.longBitsToDouble((Double.doubleToLongBits(a)<<1)>>>1)

Parameters:

a - the argument whose absolute value is to be determined

Returns:

the absolute value of the argument.

max

Returns the greater of two int values. That is, the result is the argument closer to the value of Integer.MAX_VALUE. If the arguments have the same value, the result is that same value.

Parameters:

- a an argument.
- b another argument.

Returns:

the larger of a and b.

max

Returns the greater of two long values. That is, the result is the argument closer to the value of Long.MAX_VALUE. If the arguments have the same value, the result is that same value.

Parameters:

```
a - an argument.
```

b - another argument.

Returns:

the larger of a and b.

max

Returns the greater of two float values. That is, the result is the argument closer to positive infinity. If the arguments have the same value, the result is that same value. If either value is NaN, then the result is NaN. Unlike the numerical comparison operators, this method considers negative zero to be strictly smaller than positive zero. If one argument is positive zero and the other negative zero, the result is positive zero.

Parameters:

a - an argument.

b - another argument.

Returns:

the larger of a and b.

max

Returns the greater of two double values. That is, the result is the argument closer to positive infinity. If the arguments have the same value, the result is that same value. If either value is NaN, then the result is NaN. Unlike the numerical comparison operators, this method considers negative zero to be strictly smaller than positive zero. If one argument is positive zero and the other negative zero, the result is positive zero.

Parameters:

a - an argument.

b - another argument.

Returns:

the larger of a and b.

min

Returns the smaller of two int values. That is, the result the argument closer to the value of Integer.MIN_VALUE. If the arguments have the same value, the result is that same value.

Parameters:

```
a - an argument.
```

b - another argument.

Returns:

the smaller of a and b.

min

Returns the smaller of two long values. That is, the result is the argument closer to the value of Long.MIN_VALUE. If the arguments have the same value, the result is that same value.

Parameters:

```
a - an argument.
```

b - another argument.

Returns:

the smaller of a and b.

min

Returns the smaller of two float values. That is, the result is the value closer to negative infinity. If the arguments have the same value, the result is that same value. If either value is NaN, then the result is NaN. Unlike the numerical comparison operators, this method considers negative zero to be strictly smaller than positive zero. If one argument is positive zero and the other is negative zero, the result is negative zero.

Parameters:

```
a - an argument.
```

b - another argument.

Returns:

the smaller of a and b.

min

Returns the smaller of two double values. That is, the result is the value closer to negative infinity. If the arguments have the same value, the result is that same value. If either value is NaN, then the result is NaN. Unlike the numerical comparison operators, this method considers negative zero to be strictly smaller than positive zero. If one argument is positive zero and the other is negative zero, the result is negative zero.

Parameters:

a - an argument.

b - another argument.

Returns:

the smaller of a and b.

ulp

```
public static double ulp(double d)
```

Returns the size of an ulp of the argument. An ulp, unit in the last place, of a double value is the positive distance between this floating-point value and the double value next larger in magnitude. Note that for non-NaN x, ulp(-x) == ulp(x).

Special Cases:

- If the argument is NaN, then the result is NaN.
- If the argument is positive or negative infinity, then the result is positive infinity.
- If the argument is positive or negative zero, then the result is Double.MIN VALUE.
- If the argument is $\pm Double.MAX$ VALUE, then the result is equal to 2^{971} .

Parameters:

d - the floating-point value whose ulp is to be returned

Returns:

the size of an ulp of the argument

Since:

1.5

ulp

```
public static float ulp(float f)
```

Returns the size of an ulp of the argument. An ulp, unit in the last place, of a float value is the positive distance between this floating-point value and the float value next larger in magnitude. Note that for non-NaN x, ulp(-x) == ulp(x).

Special Cases:

- If the argument is NaN, then the result is NaN.
- If the argument is positive or negative infinity, then the result is positive infinity.
- If the argument is positive or negative zero, then the result is Float.MIN VALUE.
- If the argument is \pm Float.MAX_VALUE, then the result is equal to 2^{104} .

Parameters:

f - the floating-point value whose ulp is to be returned

Returns:

the size of an ulp of the argument

Since:

1.5

signum

```
public static double signum(double d)
```

Returns the signum function of the argument; zero if the argument is zero, 1.0 if the argument is greater than zero, -1.0 if the argument is less than zero.

Special Cases:

- If the argument is NaN, then the result is NaN.
- If the argument is positive zero or negative zero, then the result is the same as the argument.

Parameters:

d - the floating-point value whose signum is to be returned

Returns:

the signum function of the argument

Since:

1.5

signum

```
public static float signum(float f)
```

Returns the signum function of the argument; zero if the argument is zero, 1.0f if the argument is greater than zero, -1.0f if the argument is less than zero.

Special Cases:

• If the argument is NaN, then the result is NaN.

• If the argument is positive zero or negative zero, then the result is the same as the argument.

Parameters:

f - the floating-point value whose signum is to be returned

Returns:

the signum function of the argument

Since:

1.5

sinh

public static double sinh(double x)

Returns the hyperbolic sine of a double value. The hyperbolic sine of x is defined to be $(e^x - e^{-x})/2$ where e is Euler's number.

Special cases:

- If the argument is NaN, then the result is NaN.
- If the argument is infinite, then the result is an infinity with the same sign as the argument.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 2.5 ulps of the exact result.

Parameters:

x - The number whose hyperbolic sine is to be returned.

Returns:

The hyperbolic sine of x.

Since:

1.5

cosh

public static double cosh(double x)

Returns the hyperbolic cosine of a double value. The hyperbolic cosine of x is defined to be $(e^x + e^{-x})/2$ where e is Euler's number.

Special cases:

- If the argument is NaN, then the result is NaN.
- If the argument is infinite, then the result is positive infinity.
- If the argument is zero, then the result is 1.0.

The computed result must be within 2.5 ulps of the exact result.

Parameters:

x - The number whose hyperbolic cosine is to be returned.

Returns:

The hyperbolic cosine of x.

Since:

1.5

tanh

```
public static double tanh(double x)
```

Returns the hyperbolic tangent of a double value. The hyperbolic tangent of x is defined to be $(e^x - e^{-x})/(e^x + e^{-x})$, in other words, $\sinh(x)/\cosh(x)$. Note that the absolute value of the exact tanh is always less than 1.

Special cases:

- If the argument is NaN, then the result is NaN.
- If the argument is zero, then the result is a zero with the same sign as the argument.
- If the argument is positive infinity, then the result is +1.0.
- If the argument is negative infinity, then the result is -1.0.

The computed result must be within 2.5 ulps of the exact result. The result of tanh for any finite input must have an absolute value less than or equal to 1. Note that once the exact result of tanh is within 1/2 of an ulp of the limit value of ± 1 , correctly signed ± 1.0 should be returned.

Parameters:

x - The number whose hyperbolic tangent is to be returned.

Returns:

The hyperbolic tangent of x.

Since:

1.5

hypot

Returns $\operatorname{sqrt}(x^2 + y^2)$ without intermediate overflow or underflow.

Special cases:

- If either argument is infinite, then the result is positive infinity.
- If either argument is NaN and neither argument is infinite, then the result is NaN.

The computed result must be within 1 ulp of the exact result. If one parameter is held constant, the results must be semi-monotonic in the other parameter.

Parameters:

x - a value

y - a value

Returns:

 $sgrt(x^2 + y^2)$ without intermediate overflow or underflow

Since:

1.5

expm1

public static double expm1(double x)

Returns e^x -1. Note that for values of x near 0, the exact sum of expm1(x) + 1 is much closer to the true result of e^x than exp(x).

Special cases:

- If the argument is NaN, the result is NaN.
- If the argument is positive infinity, then the result is positive infinity.
- If the argument is negative infinity, then the result is -1.0.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic. The result of expm1 for any finite input must be greater than or equal to -1.0.

Note that once the exact result of e^{X} - 1 is within 1/2 ulp of the limit value -1, -1.0 should be returned.

Parameters:

x - the exponent to raise e to in the computation of e^{X} -1.

Returns:

the value e^{X} - 1.

Since:

1.5

log1p

public static double log1p(double x)

Returns the natural logarithm of the sum of the argument and 1. Note that for small values x, the result of log1p(x) is much closer to the true result of ln(1 + x) than the floating-point evaluation of log(1.0+x).

Special cases:

- If the argument is NaN or less than -1, then the result is NaN.
- If the argument is positive infinity, then the result is positive infinity.
- If the argument is negative one, then the result is negative infinity.
- If the argument is zero, then the result is a zero with the same sign as the argument.

The computed result must be within 1 ulp of the exact result. Results must be semi-monotonic.

Parameters:

x - a value

Returns:

the value ln(x + 1), the natural log of x + 1

Since:

1.5

copySign

Returns the first floating-point argument with the sign of the second floating-point argument. Note that unlike the StrictMath.copySign method, this method does not require NaN sign arguments to be treated as positive values; implementations are permitted to treat some NaN arguments as positive and other NaN arguments as negative to allow greater performance.

Parameters:

magnitude - the parameter providing the magnitude of the result sign - the parameter providing the sign of the result

Returns:

a value with the magnitude of magnitude and the sign of sign.

Since:

1.6

copySign

Returns the first floating-point argument with the sign of the second floating-point argument. Note that unlike the StrictMath.copySign method, this method does not require NaN sign arguments to be treated as positive values; implementations are permitted to treat some NaN arguments as positive and other NaN arguments as negative to allow greater performance.

Parameters:

magnitude - the parameter providing the magnitude of the result
sign - the parameter providing the sign of the result
Returns:
a value with the magnitude of magnitude and the sign of sign.
Since:
1.6

getExponent

public static int getExponent(float f)

Returns the unbiased exponent used in the representation of a float. Special cases:

- If the argument is NaN or infinite, then the result is Float.MAX_EXPONENT + 1.
- If the argument is zero or subnormal, then the result is Float.MIN_EXPONENT -1.

Parameters:

f - a float value

Returns:

the unbiased exponent of the argument

Since:

1.6

getExponent

public static int getExponent(double d)

Returns the unbiased exponent used in the representation of a double. Special cases:

- If the argument is NaN or infinite, then the result is Double.MAX_EXPONENT + 1.
- If the argument is zero or subnormal, then the result is Double.MIN EXPONENT -1.

Parameters:

d - a double value

Returns:

the unbiased exponent of the argument

Since:

1.6

nextAfter

 Returns the floating-point number adjacent to the first argument in the direction of the second argument. If both arguments compare as equal the second argument is returned.

Special cases:

- If either argument is a NaN, then NaN is returned.
- If both arguments are signed zeros, direction is returned unchanged (as implied by the requirement of returning the second argument if the arguments compare as equal).
- If start is ±Double.MIN_VALUE and direction has a value such that the result should have a smaller magnitude, then a zero with the same sign as start is returned.
- If start is infinite and direction has a value such that the result should have a smaller magnitude, Double.MAX_VALUE with the same sign as start is returned.
- If start is equal to ± Double.MAX_VALUE and direction has a value such that the result should have a larger magnitude, an infinity with same sign as start is returned.

Parameters:

start - starting floating-point value

direction - value indicating which of start's neighbors or start should be returned

Returns:

The floating-point number adjacent to start in the direction of direction.

Since:

1.6

nextAfter

Returns the floating-point number adjacent to the first argument in the direction of the second argument. If both arguments compare as equal a value equivalent to the second argument is returned.

Special cases:

- If either argument is a NaN, then NaN is returned.
- If both arguments are signed zeros, a value equivalent to direction is returned.
- If start is ±Float.MIN_VALUE and direction has a value such that the result should have a smaller magnitude, then a zero with the same sign as start is returned.
- If start is infinite and direction has a value such that the result should have a smaller magnitude, Float.MAX_VALUE with the same sign as start is returned.
- If start is equal to ± Float.MAX_VALUE and direction has a value such that the result should have a larger magnitude, an infinity with same sign as start is returned.

Parameters:

start - starting floating-point value

direction - value indicating which of start's neighbors or start should be returned

Returns:

The floating-point number adjacent to start in the direction of direction.

Since:

1.6

nextUp

public static double nextUp(double d)

Returns the floating-point value adjacent to d in the direction of positive infinity. This method is semantically equivalent to nextAfter(d, Double.POSITIVE_INFINITY); however, a nextUp implementation may run faster than its equivalent nextAfter call.

Special Cases:

- If the argument is NaN, the result is NaN.
- If the argument is positive infinity, the result is positive infinity.
- If the argument is zero, the result is Double.MIN_VALUE

Parameters:

d - starting floating-point value

Returns:

The adjacent floating-point value closer to positive infinity.

Since:

1.6

nextUp

public static float nextUp(float f)

Returns the floating-point value adjacent to f in the direction of positive infinity. This method is semantically equivalent to nextAfter(f, Float.POSITIVE_INFINITY); however, a nextUp implementation may run faster than its equivalent nextAfter call.

Special Cases:

- If the argument is NaN, the result is NaN.
- If the argument is positive infinity, the result is positive infinity.
- If the argument is zero, the result is Float.MIN VALUE

Parameters:

f - starting floating-point value

Returns:

The adjacent floating-point value closer to positive infinity.

Since:

1.6

nextDown

public static double nextDown(double d)

Returns the floating-point value adjacent to d in the direction of negative infinity. This method is semantically equivalent to nextAfter(d, Double.NEGATIVE_INFINITY); however, a nextDown implementation may run faster than its equivalent nextAfter call.

Special Cases:

- If the argument is NaN, the result is NaN.
- If the argument is negative infinity, the result is negative infinity.
- If the argument is zero, the result is -Double.MIN_VALUE

Parameters:

d - starting floating-point value

Returns:

The adjacent floating-point value closer to negative infinity.

Since:

1.8

nextDown

public static float nextDown(float f)

Returns the floating-point value adjacent to f in the direction of negative infinity. This method is semantically equivalent to nextAfter(f, Float.NEGATIVE_INFINITY); however, a nextDown implementation may run faster than its equivalent nextAfter call.

Special Cases:

- If the argument is NaN, the result is NaN.
- If the argument is negative infinity, the result is negative infinity.
- If the argument is zero, the result is -Float.MIN VALUE

Parameters:

f - starting floating-point value

Returns:

The adjacent floating-point value closer to negative infinity.

Since:

1.8

scalb

Returns d \times 2 scaleFactor rounded as if performed by a single correctly rounded floating-point multiply to a member of the double value set. See the Java Language Specification for a discussion of floating-point value sets. If the exponent of the result is between Double.MIN_EXPONENT and Double.MAX_EXPONENT, the answer is calculated exactly. If the exponent of the result would be larger than Double.MAX_EXPONENT, an infinity is returned. Note that if the result is subnormal, precision may be lost; that is, when scalb(x, n) is subnormal, scalb(scalb(x, n), -n) may not equal x. When the result is non-NaN, the result has the same sign as d.

Special cases:

- If the first argument is NaN, NaN is returned.
- If the first argument is infinite, then an infinity of the same sign is returned.
- If the first argument is zero, then a zero of the same sign is returned.

Parameters:

```
d - number to be scaled by a power of two.
scaleFactor - power of 2 used to scale d
Returns:
```

d × 2scaleFactor

Since:

1.6

scalb

Returns f \times 2 scaleFactor rounded as if performed by a single correctly rounded floating-point multiply to a member of the float value set. See the Java Language Specification for a discussion of floating-point value sets. If the exponent of the result is between Float.MIN_EXPONENT and Float.MAX_EXPONENT, the answer is calculated exactly. If the exponent of the result would be larger than Float.MAX_EXPONENT, an infinity is returned. Note that if the result is subnormal, precision may be lost; that is, when scalb(x, n) is subnormal, scalb(scalb(x, n), -n) may not equal x. When the result is non-NaN, the result has the same sign as f.

Special cases:

- If the first argument is NaN, NaN is returned.
- If the first argument is infinite, then an infinity of the same sign is returned.
- If the first argument is zero, then a zero of the same sign is returned.

Parameters:

f - number to be scaled by a power of two.

scaleFactor - power of 2 used to scale f

Returns:

f × 2 scaleFactor

Since:

1.6

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Submit a bug or feature

For further API reference and developer documentation, see Java SE Documentation. That documentation contains more detailed, developer-targeted descriptions, with conceptual overviews, definitions of terms, workarounds, and working code examples.

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