Homework: Context-Free Grammar

Learning Objectives:

In this homework, we are going to exercise the following key knowledge points on the topic of context-free grammar (CFG)

- 1. understanding the relations of strings and grammars
- 2. performing derivations and constructing parse trees
- 3. determining and resolving ambiguity
- 4. designing a grammar to describe given string patterns

Instructions:

- 1. Total points: 40 pt
- 2. Early deadline: Sept 11 (Wed) 11:59 pm, Regular deadline Sept 13 (Fri) 11:59 pm (you can continue working on the homework till TA starts to grade the homework)
- 3. How to submit:
 - Submit your document to Canvas under Assignments, Homework 1
 - Please provide the complete solutions in one pdf file
 - You can write your solutions in latex or word and then convert it to pdf; or you can submit a scanned document with legible handwritten solutions

Questions:

- 1. (10 pt) Given a string a0b10c and the context free grammar G:
 - $S \to SA|A|SD$
 - $A \to a|b|c$
 - $D \to 0|1$
 - (a) (2 pt) What are the terminals and non-terminals of the grammar?
 - (b) (2 pt) Give a leftmost derivation for the string
 - (c) (2 pt) Give a rightmost derivation for the string
 - (d) (2 pt) Give a parse tree for the string
 - (e) (2 pt) Write 3 strings using the terminals that do not belong to the language of the grammar L(G)
- 2. (10 pt) Consider the following grammar:
 - terminals: x, y, z, >, <, 0, 1, (,), if, then, else

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- non-terminals: S, F, B, T, E, N
- \bullet start symbol: S
- production rules:

$$S \to F|T N T$$

$$F \rightarrow \text{if } B \text{ then } S | \text{if } B \text{ then } S \text{ else } S$$

$$B \to (T E T)$$

$$T \rightarrow x|y|z|1|0$$

$$E \rightarrow > | <$$

$$N \rightarrow + |-| =$$

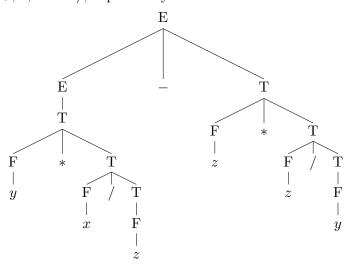
- (a) (4 pt) Draw two different parse trees for the string if (x > y) then if (x < z) then x = 1 else x = 0
- (b) (2 pt) Modify the grammar to remove ambiguity.
- (c) (2 pt) Draw the parse tree for the string using new grammar
- (d) (2 pt) Explain how your new grammar modifies the parse trees you drew in the first step to remove ambiguity
- 3. (10 pt) Consider the following grammar:
 - terminals: x, y, z, +, -, *, /
 - ullet non-terminals: E, T, F, V
 - \bullet start symbol: E
 - production rules:

$$E \rightarrow E + T|E - T|T$$

$$T \to F * T|F/T|F$$

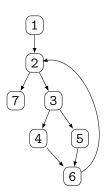
$$F \to x|y|z$$

- (a) (4 pt) What is the associativity of the operators +, -, * and /; explain why.
- (b) (3 pt) What is the precedence of +,-,* and /; explain why.
- (c) (3 pt) Given a parse tree



Explain how the value of the string is generated.

- 4. (10 pt) Design CFGs for the given languages:
 - (a) (2 pt) Write a grammar that describes the strings $0^*1^+2^*$.
 - (b) (3 pt) Write a grammar that describes the strings $0^n 1^m$, where n > m.
 - (c) (5 pt) Given a graph below, where 1 is an entry and 7 is an exit, we can generate paths like 127, 1234627, 1235627, 12356234627 ... Write a grammar that describes these paths.



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