

For a semisimple linear algebraic group  $G \leq \mathrm{GL}(m, \mathbb{C})$  defined over  $\mathbb{Q}$ , and for a subring  $R$  of  $\mathbb{C}$ , write  $G_R = G \cap \mathrm{GL}(m, R)$ . A subgroup  $\Gamma \leq G_{\mathbb{Q}}$  is **arithmetic** if it is commensurable to  $G_{\mathbb{Z}}$ .