

## Module 2 Assignment

### Linear Programming Formulations

#### Problem 1: Back Savers Backpacks

##### Decision Variables

$x_C$  = number of Collegiate backpacks produced per week  
 $x_M$  = number of Mini backpacks produced per week

##### Objective Function

Maximize weekly profit:

$$Z = 32x_C + 24x_M$$

##### Constraints

Fabric:

$$3x_C + 2x_M \leq 5000$$

Labor:

$$45x_C + 40x_M \leq 84,000$$

Sales limits:

$$x_C \leq 1000$$

$$x_M \leq 1200$$

Nonnegativity:

$$x_C \geq 0, \quad x_M \geq 0$$

#### Problem 2: Weigelt Corporation (Three Plants, Three Sizes)

##### Decision Variables

$x_{iL}$  = units of Large produced per day at plant  $i$  ( $i = 1,2,3$ )

$x_{iM}$  = units of Medium produced per day at plant  $i$  ( $i = 1,2,3$ )

$x_{iS}$  = units of Small produced per day at plant  $i$  ( $i = 1,2,3$ )

$u$  = common utilization fraction of each plant's capacity ( $0 \leq u \leq 1$ )

##### Objective Function

Maximize daily profit:

$$Z = 420 \sum x_{iL} + 360 \sum x_{iM} + 300 \sum x_{iS}, \text{ for } i = 1..3$$

## Constraints

Capacity with equal utilization:

$$x_{1L} + x_{1M} + x_{1S} \leq 750u$$

$$x_{2L} + x_{2M} + x_{2S} \leq 900u$$

$$x_{3L} + x_{3M} + x_{3S} \leq 450u$$

Storage:

$$20x_{1L} + 15x_{1M} + 12x_{1S} \leq 13,000$$

$$20x_{2L} + 15x_{2M} + 12x_{2S} \leq 12,000$$

$$20x_{3L} + 15x_{3M} + 12x_{3S} \leq 5,000$$

Market demand:

$$\sum x_{iL} \leq 900$$

$$\sum x_{iM} \leq 1200$$

$$\sum x_{iS} \leq 750$$

Nonnegativity:

$$x_{iL}, x_{iM}, x_{iS} \geq 0 \text{ for } i=1,2,3$$

$$0 \leq u \leq 1$$