



# Chapter 3

### Classical Encryption Techniques

### Definitions

#### **Plaintext**

An original message

#### Ciphertext

The coded message

### Enciphering/encrypt ion

 The process of converting from plaintext to ciphertext

### Deciphering/decrypt ion

 Restoring the plaintext from the ciphertext

#### Cryptography

 The area of study of the many schemes used for encryption

### Cryptographic system/cipher

A scheme

#### Cryptanalysis

 Techniques used for deciphering a message without any knowledge of the enciphering details

#### Cryptology

 The areas of cryptography and cryptanalysis

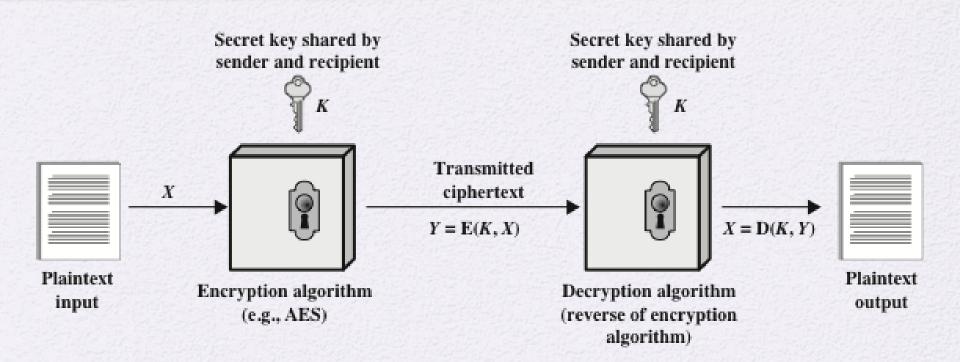
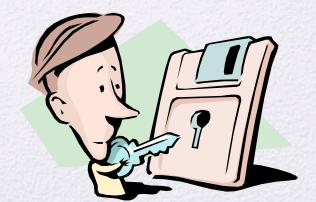


Figure 3.1 Simplified Model of Symmetric Encryption

### Symmetric Cipher Model

- There are two requirements for secure use of conventional encryption:
  - A strong encryption algorithm
  - Sender and receiver must have obtained copies of the secret key in a secure fashion and must keep the key secure



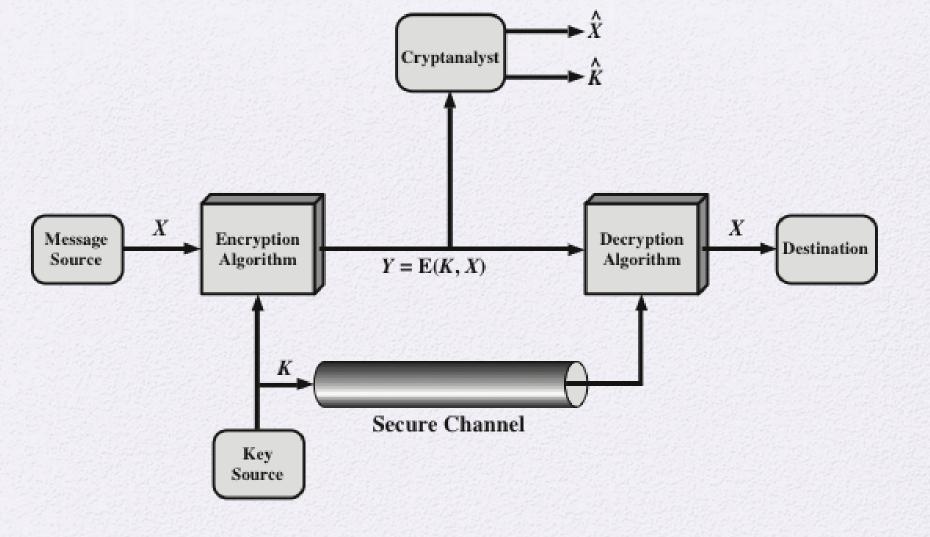


Figure 3.2 Model of Symmetric Cryptosystem

# Cryptographic Systems

Characterized along three independent dimensions:

The type of operations used for transforming plaintext to ciphertext

Substitution

Transposition

The number of keys used

Symmetric, single-key, secret-key, conventional encryption

Asymmetric, twokey, or public-key encryption The way in which the plaintext is processed

Block cipher

Stream cipher

# Cryptanalysis and Brute-Force Attack

#### Cryptanalysis

- Attack relies on the nature of the algorithm plus some knowledge of the general characteristics of the plaintext
- Attack exploits the characteristics of the algorithm to attempt to deduce a specific plaintext or to deduce the key being used

#### **Brute-force attack**

- Attacker tries every possible key on a piece of ciphertext until an intelligible translation into plaintext is obtained
- On average, half of all possible keys must be tried to achieve success

Type of Attack	Known to Cryptanalyst
Ciphertext Only	Encryption algorithm
	• Ciphertext
Known Plaintext	Encryption algorithm
	Ciphertext
	• One or more plaintext-ciphertext pairs formed with the secret key
Chosen Plaintext	• Encryption algorithm
	Ciphertext
	Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key
Chosen Ciphertext	Encryption algorithm
	Ciphertext
	• Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key
Chosen Text	• Encryption algorithm
	• Ciphertext
	Plaintext message chosen by cryptanalyst, together with its corresponding ciphertext generated with the secret key
	Ciphertext chosen by cryptanalyst, together with its corresponding decrypted plaintext generated with the secret key

Table 3.1
Types of
Attacks
on
Encrypted
Messages

## **Encryption Scheme Security**

- Unconditionally secure
  - No matter how much time an opponent has, it is impossible for him or her to decrypt the ciphertext simply because the required information is not there
- Computationally secure
  - The cost of breaking the cipher exceeds the value of the encrypted information
  - The time required to break the cipher exceeds the useful lifetime of the information

### Brute-Force Attack

Involves trying every possible key until an intelligible translation of the ciphertext into plaintext is obtained

On average, half of all possible keys must be tried to achieve success

To supplement the brute-force approach, some degree of knowledge about the expected plaintext is needed, and some means of automatically distinguishing plaintext from garble is also needed

### Substitution Technique

- Is one in which the letters of plaintext are replaced by other letters or by numbers or symbols
- If the plaintext is viewed as a sequence of bits, then substitution involves replacing plaintext bit patterns with ciphertext bit patterns





### Caesar Cipher



- Simplest and earliest known use of a substitution cipher
- Used by Julius Caesar
- Involves replacing each letter of the alphabet with the letter standing three places further down the alphabet
- Alphabet is wrapped around so that the letter following Z is A

plain: meet me after the toga party

cipher: PHHW PH DIWHU WKH WRJD SDUWB

# Caesar Cipher Algorithm

Can define transformation as:

Mathematically give each letter a number

Algorithm can be expressed as:

$$c = E(3, p) = (p + 3) \mod (26)$$

A shift may be of any amount, so that the general Caesar algorithm is:

$$C = E(k, p) = (p + k) \mod 26$$

 Where k takes on a value in the range 1 to 25; the decryption algorithm is simply:

$$p = D(k, C) = (C - k) \mod 26$$

### Figure 3.3

### Brute-Force Cryptanalysis of Caesar Cipher

(This chart can be found on page 75 in the textbook)

	PHHW	РП	DIMIO	MIXII	MKOD	SDOMP
KEY						
1	oggv	og	chvgt	vjg	vqic	rctva
2	nffu	nf	bgufs	uif	uphb	qbsuz
3	meet	me	after	the	toga	party
4	ldds	ld	zesdq	sgd	snfz	ozqsx
5	kccr	kc	ydrcp	rfc	rmey	nyprw
6	jbbq	jb	xcqbo	qeb	qldx	mxoqv
7	iaap	ia	wbpan	pda	pkcw	lwnpu
8	hzzo	hz	vaozm	ocz	ojbv	kvmot
9	gyyn	дy	uznyl	nby	niau	julns
10	fxxm	fx	tymxk	max	mhzt	itkmr
11	ewwl	ew	sxlwj	lzw	lgys	hsjlq
12	dvvk	dv	rwkvi	kyv	kfxr	grikp
13	cuuj	cu	qvjuh	jxu	jewq	fqhjo
14	btti	bt	puitg	iwt	idvp	epgin
15	assh	as	othsf	hvs	hcuo	dofhm
16	zrrg	zr	nsgre	gur	gbtn	cnegl
17	yqqf	уq	mrfqd	ftq	fasm	bmdfk
18	хрре	хр	lqepc	esp	ezrl	alcej
19	wood	wo	kpdob	dro	dyqk	zkbdi
20	vnnc	vn	jocna	cqn	схрј	yjach
21	ummb	um	inbmz	bpm	bwoi	xizbg
22	tlla	tl	hmaly	aol	avnh	whyaf
23	skkz	sk	glzkx	znk	zumg	vgxze
24	rjjy	rj	fkyjw	ymj	ytlf	ufwyd
25	qiix	qi	ejxiv	xli	xske	tevxc

סשוותם חד סע שעש וועשדת עם שטעם

### Monoalphabetic Cipher

#### Permutation

- Of a finite set of elements S is an ordered sequence of all the elements of S, with each element appearing exactly once
- If the "cipher" line can be any permutation of the 26 alphabetic characters, then there are 26! or greater than 4 x 10<sup>26</sup> possible keys
  - This is 10 orders of magnitude greater than the key space for DES
  - Approach is referred to as a monoalphabetic substitution cipher because a single cipher alphabet is used per message

## Monoalphabetic Cipher

Plain Text	а	b	c	d	e	f	g	h	i	j	k	1	m	n	O	р	q	r	s	t	u	v	w	X	у	Z
Key	X	D	G	S	Z	Α	Ν	Υ	O	В	Т	M	J	C	Ε	V	F	Н	K	W	Р	L	Q	U	R	1

Plain Text
Cipher Text

S	е	c	r	е	t	w	r	i	t	i	n	g	S
K	Z	G	Н	Z	W	Q	Н	0	W	0	C	N	K

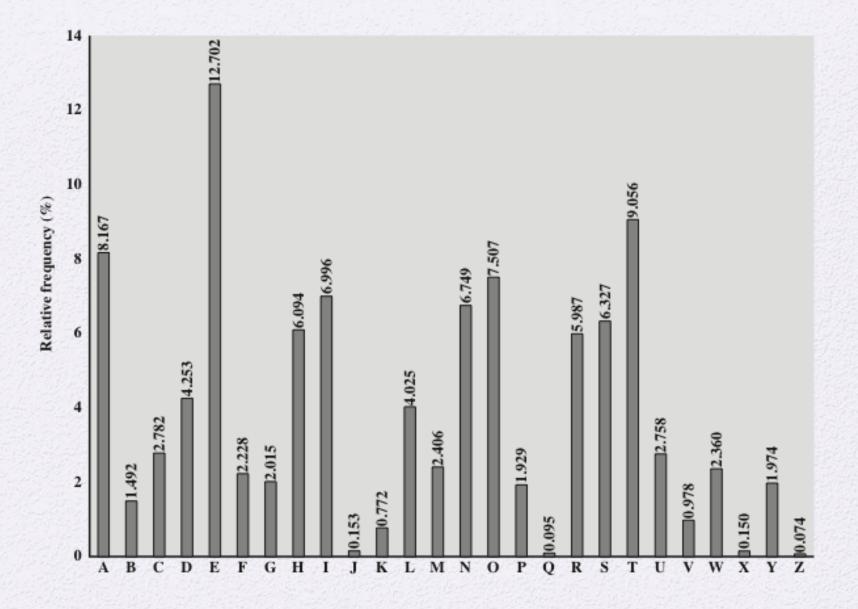


Figure 3.5 Relative Frequency of Letters in English Text

#### Cipher text

UZQSOVUOHXMOPVGPOZPEVSGZWSZOPFPESXUDBMETSXAIZ VUEPHZHMDZSHZOWSFPAPPDTSVPQUZWYMXUZUHSX EPYEPOPDZSZUFPOMBZWPFUPZHMDJUDTMOHMO

#### Frequency of Alphabets

P 13.33	H 5.83	F 3.33	B 1.67	C 0.00
Z 11.67	D 5.00	W 3.33	G 1.67	K 0.00
S 8.33	E 5.00	Q 2.50	Y 1.67	L 0.00
U 8.33	V 4.17	T 2.50	I 0.83	N 0.00
O 7.50	X 4.17	A 1.67	J 0.83	R 0.00
M 6.67				

#### **Cryptanalysis**

- It seems likely that cipher letters P and Z are the equivalents of plain letters e and t, but it is not certain which is which.
- The letters S, U, O, M, and H probably correspond to plain letters from the set {a, h, i, n, o, r, s}.
- Letters A, B, G, Y, I, J are likely included in the set {b, j, k, q, v, x, z}.
- After this make some tentative assignments to fill in the plain text to see if it looks like a reasonable message.
- Or certain words may be known in text or we could look for repeating sequences of cipher letters and try to deduce their plain text equivalents

UZQSOVUOHXMOPVGPOZPEVSGZWSZOPFPESXUDBMETSXAIZ

ta e e te a that e e a

VUEPHZHMDZSHZOWSFPAPPDTSVPQUZWYMXUZUHSX

e t ta t ha e ee a e th t a

EPYEPOPDZSZUFPOMBZWPFUPZHMDJUDTMOHMQ

e e e tat e the t

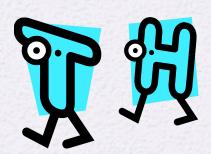
Partial representation of the cipher text

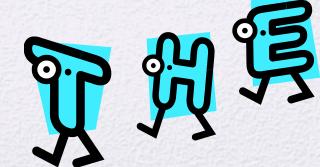
it was disclosed yesterday that several informal but direct contacts have been made with political representatives of the viet cong in moscow

Plain text

# Monoalphabetic Ciphers

- Easy to break because they reflect the frequency data of the original alphabet
- Countermeasure is to provide multiple substitutes (homophones) for a single letter
- Digram
  - Two-letter combination
  - Most common is th
- Trigram
  - Three-letter combination
  - Most frequent is the





# Playfair Cipher

- Best-known multiple-letter encryption cipher
- Treats digrams in the plaintext as single units and translates these units into ciphertext digrams
- Based on the use of a 5 x 5 matrix of letters constructed using a keyword
- Invented by British scientist Sir Charles Wheatstone in 1854
- Used as the standard field system by the British Army in World War I and the U.S. Army and other Allied forces during World War II

# Playfair Key Matrix

- Fill in letters of keyword (minus duplicates) from left to right and from top to bottom, then fill in the remainder of the matrix with the remaining letters in alphabetic order
- Using the keyword MONARCHY:

M	0	N	A	R
C	Н	Y	В	D
E	F	G	I/J	K
L	Р	Q	S	Т
U	٧	W	X	Z

# Rules for Playfair Substitution

- Repeating plaintext letters that are in the same pair are separated with a filler letter, such as x, so that balloon would be treated as ballx lo on.
- Two plaintext letters that fall in the same row of the matrix are each replaced by the letter to the right, with the first element of the row circularly following the last. For example, ar is encrypted as RM.
- Two plaintext letters that fall in the same column are each replaced by the letter beneath, with the top element of the column circularly following the last. For example, mu is encrypted as CM.
- Otherwise, each plaintext letter in a pair is replaced by the letter that lies in its own row and the column occupied by the other plaintext letter. Thus, hs becomes BP and ea becomes IM (or JM, as the encipherer wishes).

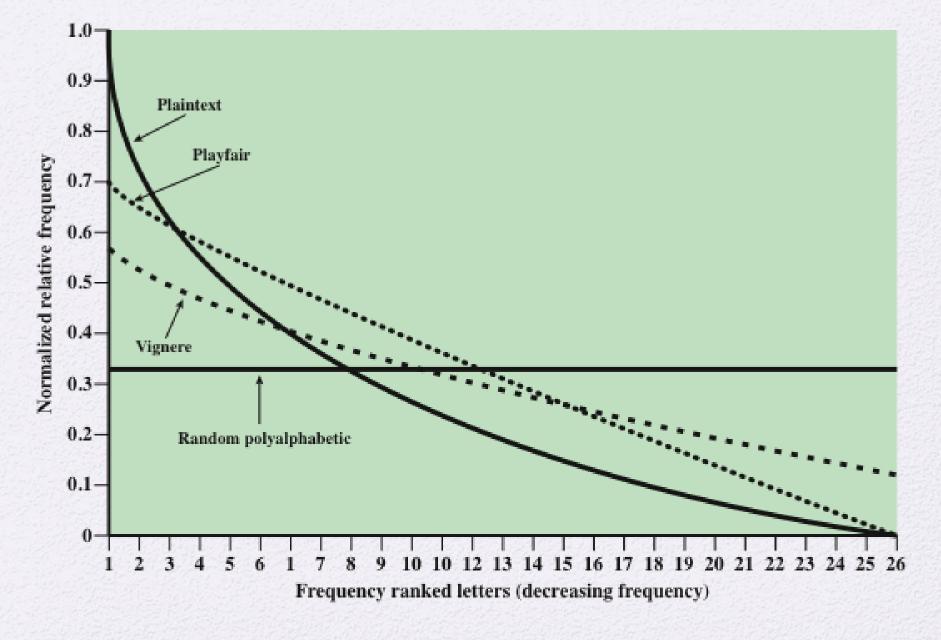


Figure 3.6 Relative Frequency of Occurrence of Letters

## Polyalphabetic Ciphers

- Polyalphabetic substitution cipher
  - Improves on the simple monoalphabetic technique by using different monoalphabetic substitutions as one proceeds through the plaintext message

### All these techniques have the following features in common:

- A set of related monoalphabetic substitution rules is used
- A key determines which particular rule is chosen for a given transformation

# Vigenère Cipher

- Best known and one of the simplest polyalphabetic substitution ciphers
- In this scheme the set of related monoalphabetic substitution rules consists of the 26 Caesar ciphers with shifts of 0 through
   25
- Each cipher is denoted by a key letter which is the ciphertext letter that substitutes for the plaintext letter a

# Example of Vigenère Cipher

- To encrypt a message, a key is needed that is as long as the message
- Usually, the key is a repeating keyword
- For example, if the keyword is deceptive, the message "we are discovered save yourself" is encrypted as:

key: deceptivedeceptive

plaintext: wearediscoveredsaveyourself

ciphertext: ZICVTWQNGRZGVTWAVZHCQYGLMGJ

# Vigenère Autokey System

 A keyword is concatenated with the plaintext itself to provide a running key

• Example:

key: deceptivewearediscoveredsav

plaintext: wearediscoveredsaveyourself

ciphertext: ZICVTWQNGKZEIIGASXSTSLVVWLA

- Even this scheme is vulnerable to cryptanalysis
  - Because the key and the plaintext share the same frequency distribution of letters, a statistical technique can be applied

## Vernam Cipher

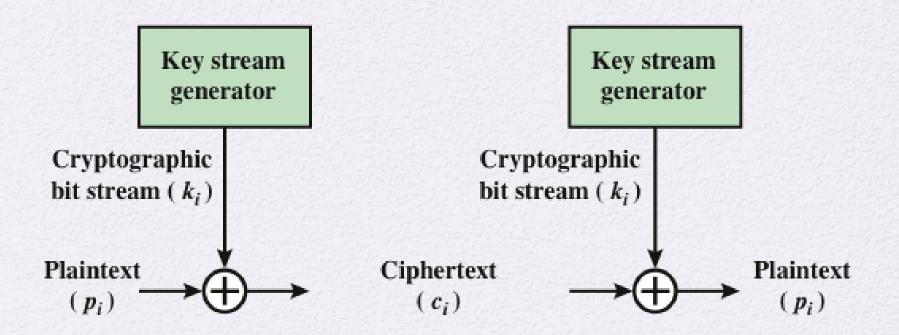


Figure 3.7 Vernam Cipher

### One-Time Pad

- Improvement to Vernam cipher proposed by an Army Signal Corp officer, Joseph Mauborgne
- Use a random key that is as long as the message so that the key need not be repeated
- Key is used to encrypt and decrypt a single message and then is discarded
- Each new message requires a new key of the same length as the new message
- Scheme is unbreakable
  - Produces random output that bears no statistical relationship to the plaintext
  - Because the ciphertext contains no information whatsoever about the plaintext, there is simply no way to break the code



### Difficulties

- The one-time pad offers complete security but, in practice, has two fundamental difficulties:
  - There is the practical problem of making large quantities of random keys
    - Any heavily used system might require millions of random characters on a regular basis
  - Mammoth key distribution problem
    - For every message to be sent, a key of equal length is needed by both sender and receiver
- Because of these difficulties, the one-time pad is of limited utility
  - Useful primarily for low-bandwidth channels requiring very high security
- The one-time pad is the only cryptosystem that exhibits perfect secrecy (see Appendix F)

## Rail Fence Cipher

- Simplest transposition cipher
- Plaintext is written down as a sequence of diagonals and then read off as a sequence of rows
- To encipher the message "meet me after the toga party" with a rail fence of depth 2, we would write:

m e m a t r h t g p r y
e t e f e t e o a a t
Encrypted message is:
MEMATRHTGPRYETEFETEOAAT

### Row Transposition Cipher

- Is a more complex transposition
- Write the message in a rectangle, row by row, and read the message off, column by column, but permute the order of the columns
  - The order of the columns then becomes the key to the algorithm

Key: 4312567

Plaintext: attackp

ostpone

duntilt

woamxyz

Ciphertext: TTNAAPTMTSUOAODWCOIXKNLYPETZ

# Steganography

3rd March

Dear George,

Greetings to all at Oxford. Many thanks for your letter and for the Summer examination package. All Entry Forms and Fees Forms should be ready for final despatch to the Syndicate by Friday 20th or at the very latest, I'm told, by the 21st. Admin has improved here, though there's room for improvement still; just give us all two or three more years and we'll really show you! Please don't let these wretched 16+ proposals destroy your basic O and A pattern. Certainly this sort of change, if implemented immediately, would bring chaos.

Sincerely yours,

A Puzzle for Inspector Morse (from *The Silent World of Nicholas Quinn*, by Colin Dexter)

### Other Steganography Techniques



#### Character marking

- Selected letters of printed or typewritten text are over-written in pencil
- The marks are ordinarily not visible unless the paper is held at an angle to bright light

#### Invisible ink

 A number of substances can be used for writing but leave no visible trace until heat or some chemical is applied to the paper

#### Pin punctures

 Small pin punctures on selected letters are ordinarily not visible unless the paper is held up in front of a light

#### Typewriter correction ribbon

 Used between lines typed with a black ribbon, the results of typing with the correction tape are visible only under a strong light

### Steganography vs. Encryption

- Steganography
   has a number of
   drawbacks when
   compared to encryption
  - It requires a lot of overhead to hide a relatively few bits of information
  - Once the system is discovered, it becomes virtually worthless

- The advantage of steganography
  - It can be employed by parties who have something to lose should the fact of their secret communication (not necessarily the content) be discovered
- Encryption flags traffic as important or secret or may identify the sender or receiver as someone with something to hide

### Summary

- Symmetric Cipher Model
  - Cryptography
  - Cryptanalysis and Brute-Force Attack
- Transposition techniques



- Substitution techniques
  - Caesar cipher
  - Monoalphabetic ciphers
  - Playfair cipher
  - Polyalphabetic ciphers
  - One-time pad
- Steganography