



Chapter 4

Block Ciphers and the Data Encryption Standard

Stream Cipher

Encrypts a digital data stream one bit or one byte at a time

Examples:

- Autokeyed Vigenère cipher
- Vernam cipher

In the ideal case, a one-time pad version of the Vernam cipher would be used, in which the keystream is as long as the plaintext bit stream

If the cryptographic keystream is random, then this cipher is unbreakable by any means other than acquiring the keystream

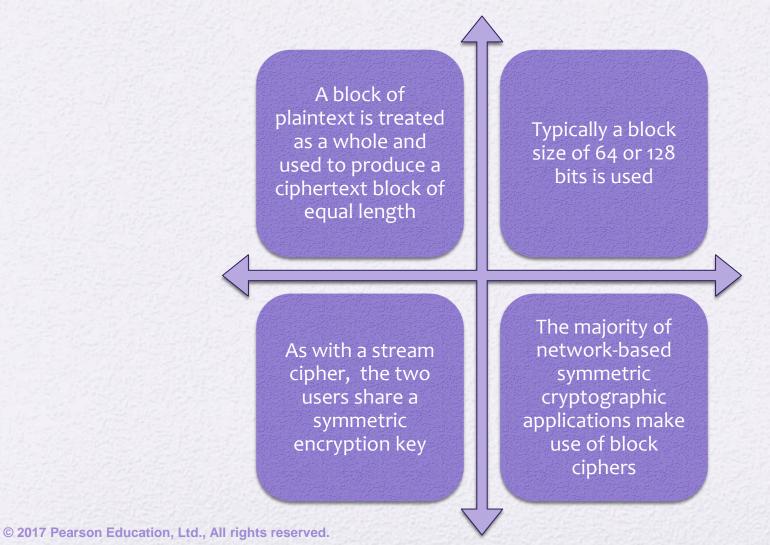
- Keystream must be provided to both users in advance via some independent and secure channel
- This introduces insurmountable logistical problems if the intended data traffic is very large

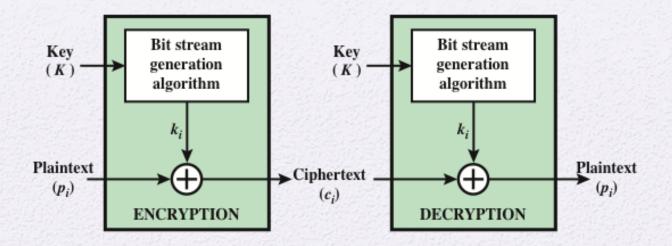
For practical reasons the bitstream generator must be implemented as an algorithmic procedure so that the cryptographic bit stream can be produced by both users

> It must be computationally impractical to predict future portions of the bit stream based on previous portions of the bit stream

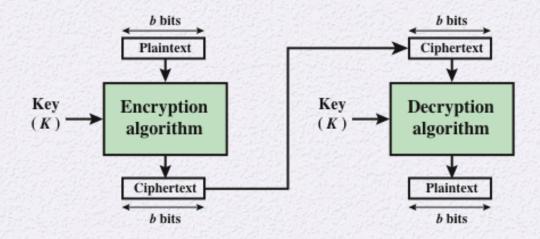
The two users need only share the generating key and each can produce the keystream

Block Cipher





(a) Stream Cipher Using Algorithmic Bit Stream Generator



(b) Block Cipher

Figure 4.1 Stream Cipher and Block Cipher

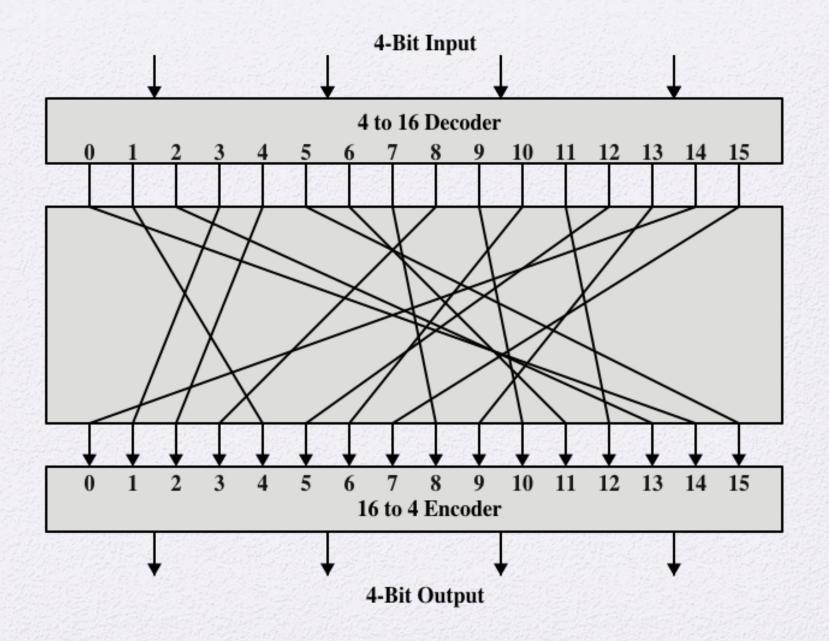


Figure 4.2 General *n*-bit-*n*-bit Block Substitution (shown with n = 4)

Table 4.1

Encryption and Decryption Tables for Substitution Cipher of Figure

4.2

Plaintext	Ciphertext	
0000	1110	
0001	0100	
0010	1101	
0011	0001	
0100	0010	
0101	1111	
0110	1011	
0111	1000	
1000	0011	
1001	1010	l
1010	0110	
1011	1100	
1100	0101	
1101	1001	
1110	0000	
1111	0111	

Ciphertext	Plaintext
0000	1110
0001	0011
0010	0100
0011	1000
0100	0001
0101	1100
0110	1010
0111	1111
1000	0111
1001	1101
1010	1001
1011	0110
1100	1011
1101	0010
1110	0000
1111	0101

Difficulties: Ideal Block Cipher

- Smaller block sizes makes it vulnerable to statistical analysis
 - Solution: Larger block sizes
- Larger block sizes not feasible from an implementation and performance point of view.
- Key length an important aspect
 - 64-bit block to thwart statistical attacks
 - Key length for 64-bit blocks?

Feistel Cipher

 Feistel proposed the use of a cipher that alternates substitutions and permutations

Substitutions

 Each plaintext element or group of elements is uniquely replaced by a corresponding ciphertext element or group of elements

Permutation

- No elements are added or deleted or replaced in the sequence, rather the order in which the elements appear in the sequence is changed
- Is a practical application of a proposal by Claude Shannon to develop a product cipher that alternates confusion and diffusion functions
- Is the structure used by many significant symmetric block ciphers currently in use

Diffusion and Confusion

- Terms introduced by Claude Shannon to capture the two basic building blocks for any cryptographic system
 - Shannon's concern was to thwart cryptanalysis based on statistical analysis

Diffusion

- The statistical structure of the plaintext is dissipated into long-range statistics of the ciphertext
- This is achieved by having each plaintext digit affect the value of many ciphertext digits

Confusion

- Seeks to make the relationship between the statistics of the ciphertext and the value of the encryption key as complex as possible
- Even if the attacker can get some handle on the statistics of the ciphertext, the way in which the key was used to produce that ciphertext is so complex as to make it difficult to deduce the key

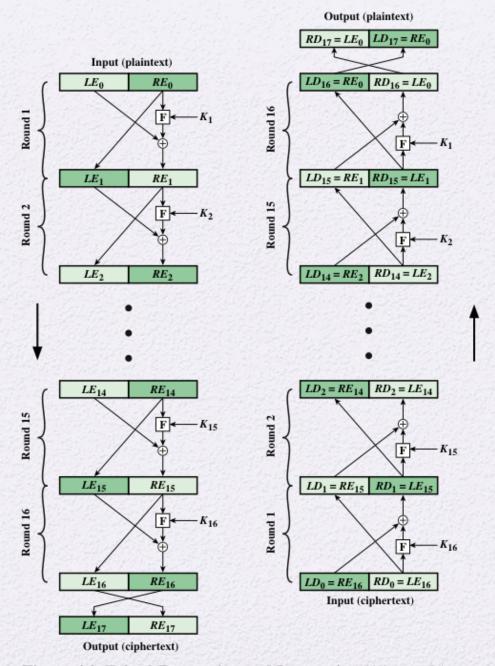


Figure 4.3 Feistel Encryption and Decryption (16 rounds)

Feistel Cipher Design Features

Block size

 Larger block sizes mean greater security but reduced encryption/decryption speed for a given algorithm

Key size

 Larger key size means greater security but may decrease encryption/decryption speeds

Number of rounds

 The essence of the Feistel cipher is that a single round offers inadequate security but that multiple rounds offer increasing security

Subkey generation algorithm

 Greater complexity in this algorithm should lead to greater difficulty of cryptanalysis

Round function F

 Greater complexity generally means greater resistance to cryptanalysis

Fast software encryption/decryption

 In many cases, encrypting is embedded in applications or utility functions in such a way as to preclude a hardware implementation; accordingly, the speed of execution of the algorithm becomes a concern

Ease of analysis

 If the algorithm can be concisely and clearly explained, it is easier to analyze that algorithm for cryptanalytic vulnerabilities and therefore develop a higher level of assurance as to its strength

Feistel Example

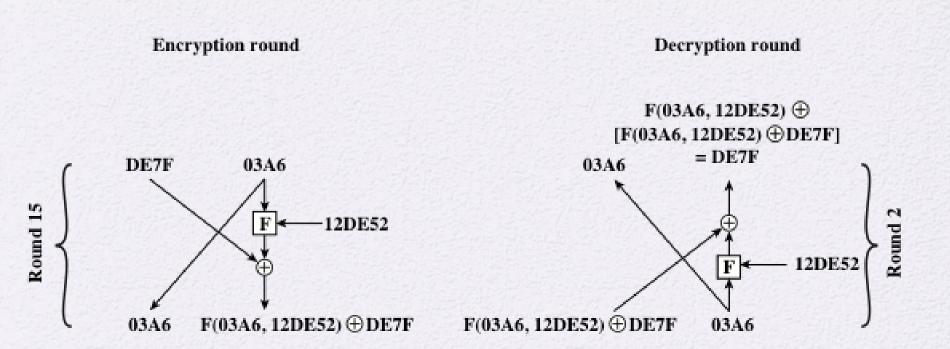


Figure 4.4 Feistel Example

Data Encryption Standard (DES)

- Issued in 1977 by the National Bureau of Standards (now NIST) as Federal Information Processing Standard 46
- Was the most widely used encryption scheme until the introduction of the Advanced Encryption Standard (AES) in 2001
- Algorithm itself is referred to as the Data Encryption Algorithm (DEA)
 - Data are encrypted in 64-bit blocks using a 56-bit key
 - The algorithm transforms 64-bit input in a series of steps into a 64-bit output
 - The same steps, with the same key, are used to reverse the encryption

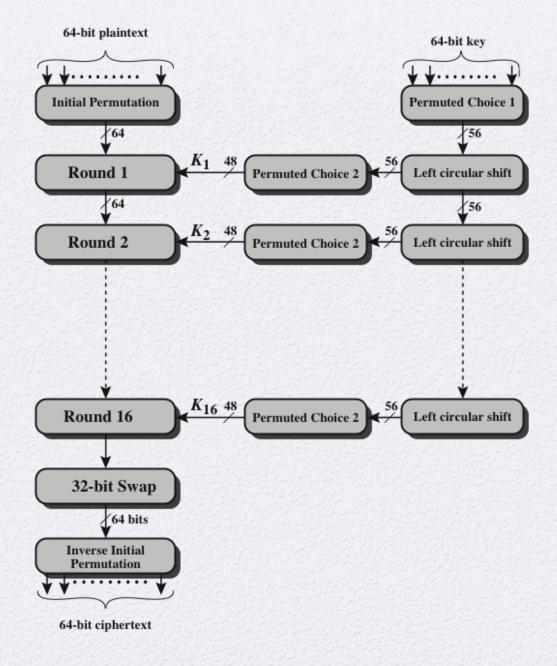
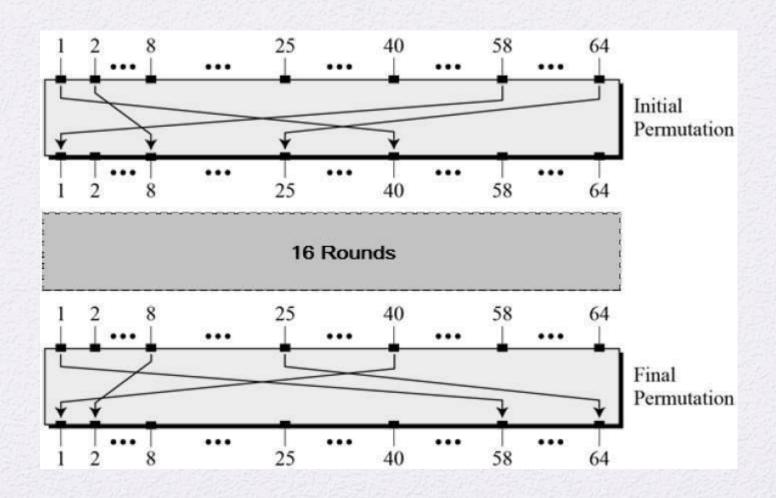


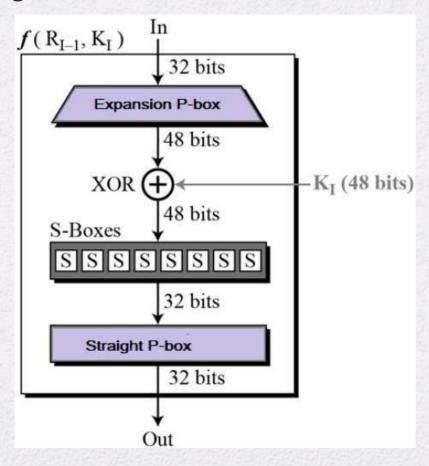
Figure 4.5 General Depiction of DES Encryption Algorithm

Initial and final permutation

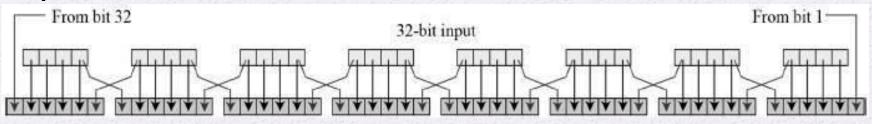


Round Function

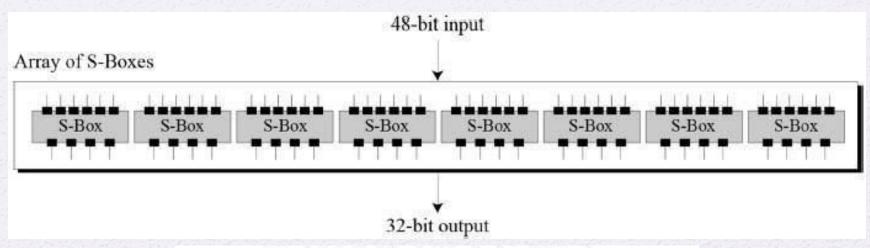
Applied to the right most 32-bits.

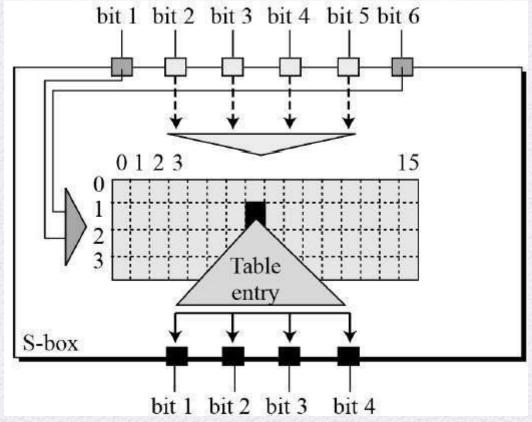


Expansion Permutation Box



32	01	02	03	04	05
04	05	06	07	08	09
08	09	10	11	12	13
12	13	14	15	16	17
16	17	18	19	20	21
20	21	22	23	24	25
24	25	26	27	28	29
28	29	31	31	32	01





Example (Sbox)

Row #	\mathbf{S}_1	1	2	3				7								15	Column #
0	14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7	
1	0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8	
2	4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0	
3	15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13	
	S(i, j) < 16, can be represented with 4 bits																

Example: B = 101111

$$b_1b_6 = 11 = 3 \text{ (row)}$$

 $b_2b_3b_4b_5 = 0111 = 7 \text{ (column)}$

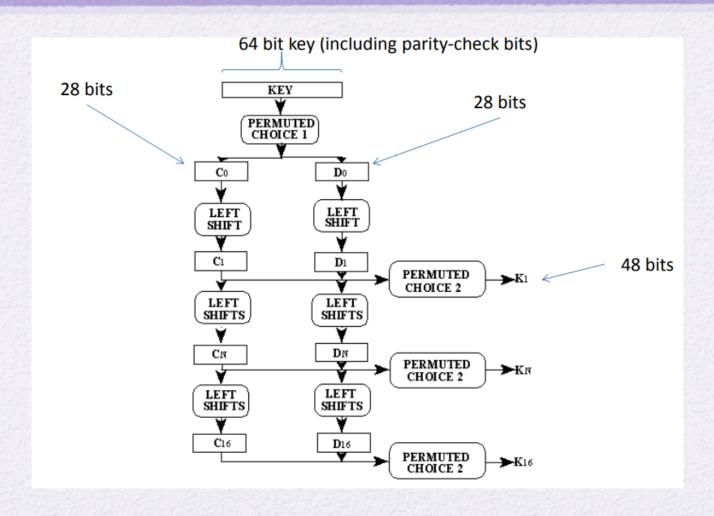
Let output the of sbox be C

$$C = 7 = 0111$$

Straight Permutation

16	07	20	21	29	12	28	17
01	15	23	26	05	18	31	10
02	08	24	14	32	27	03	09
19	13	30	06	22	11	04	25

Key Generation



DES Permuted Choice 1 and 2 (PC-1, PC-2)

Parity-check bits (namely, bits 8,16, 4,32,40,48,56,64) are not chosen, they do not appear in **PC-1**



				Left			
	57	49	41	33	25	17	9
	1	58	50	42	34	26	18
	10	2	59	51	43	35	27
	19	11	3	60	52	44	36
				Right	•		
	63	55	47	39	31	23	15
	7	62	54	46	38	30	22
	14	6	61	53	45	37	29
	21	13	5	28	20	12	4
•							

14	17	11	24	1	5	3	28
15	6	21	10	23	19	12	4
26	8	16	7	27	20	13	2
41	52	31	37	47	55	30	40
51	45	33	48	44	49	39	56
34	53	46	42	50	36	29	32



PC-2 selects the 48-bit subkey for each round from the 56-bit key-schedule state

Rotation

Example: From the original 64-bit key

 $\mathbf{K} = 00010011\ 00110100\ 01010111\ 011111001\ 10011011\ 10111100\ 11011111\ 111110001$

we get the 56-bit permutation

 $\mathbf{K}^+ = 1111000\ 0110011\ 0010101\ 0101111\ 0101010\ 1011001\ 1001111\ 0001111$

Next, split this key into left and right halves, C_0 and D_0 , where each half has 28 bits.

Example: From the permuted key K+, we get

 $C_{\theta} = 1111000 \ 0110011 \ 0010101 \ 0101111$ $D_{\theta} = 0101010 \ 1011001 \ 1001111 \ 0001111$

Example: From original pair C_0 and D_0 we obtain:

 $C_I = 1110000110011001010101011111$ $D_I = 1010101011001100111100011110$

 $C_2 = 11000011001100101010101111111$ $D_2 = 0101010110011001111000111101$

 $C_3 = 00001100110010101010111111111$

 $D_3 = 0101011001100111100011110101$

 $\pmb{C_4} = 00110011001010101011111111100$

 $\boldsymbol{D_4} = 0101100110011110001111010101$

Iteration	Number of
Number	Left Shifts
1	1
2	1
3	2
4	2
5	2
6	2
7	2
8	2 2
9	1
10	2
11	2
12	2
13	2
14	2 2
15	2
16	1
	-

DES Weak Keys

- Weak keys: keys make the same sub-key to be generated in more than one round.
- Result: reduce cipher complexity
- Weak keys can be avoided at key generation.
- DES has 4 weak keys
 - 01010101 01010101
 - FEFEFEFE FEFEFEFE
 - E0E0E0E0 F1F1F1F1
 - 1F1F1F1F 0E0E0E0E

DES Decryption

• Decryption uses the same algorithm as encryption, except that the subkeys K_1 , K_2 ,... K_{16} are applied in reversed order

Table 4.2

DES Example

(Table can be found on page 132 in textbook)

Round	Ki	Li	Ri
IP		5a005a00	3cf03c0f
1	1e030f03080d2930	3cf03c0f	bad22845
2	0a31293432242318	bad22845	99e9b723
3	23072318201d0c1d	99e9b723	0bae3b9e
4	05261d3824311a20	0bae3b9e	42415649
5	3325340136002c25	42415649	18b3fa41
6	123a2d0d04262a1c	18b3fa41	9616fe23
7	021f120b1c130611	9616fe23	67117cf2
8	1c10372a2832002b	67117cf2	c11bfc09
9	04292a380c341f03	c11bfc09	887fbc6c
10	2703212607280403	887fbc6c	600f7e8b
11	2826390c31261504	600f7e8b	f596506e
12	12071c241a0a0f08	f596506e	738538b8
13	300935393c0d100b	738538b8	c6a62c4e
14	311e09231321182a	c6a62c4e	56b0bd75
15	283d3e0227072528	56b0bd75	75e8fd8f
16	2921080b13143025	75e8fd8f	25896490
IP-1		da02ce3a	89ecac3b

Note: DES subkeys are shown as eight 6-bit values in hex format

Round		δ	Round		δ
	02468aceeca86420	1	9	c11bfc09887fbc6c	32
	12468aceeca86420			99f911532eed7d94	
1	3cf03c0fbad22845	1	10	887fbc6c600f7e8b	34
	3cf03c0fbad32845			2eed7d94d0f23094	
2	bad2284599e9b723	5	11	600f7e8bf596506e	37
	bad3284539a9b7a3			d0f23094455da9c4	
3	99e9b7230bae3b9e	18	12	f596506e738538b8	31
	39a9b7a3171cb8b3			455da9c47f6e3cf3	
4	0bae3b9e42415649	34	13	738538b8c6a62c4e	29
	171cb8b3ccaca55e			7f6e3cf34bc1a8d9	
5	4241564918b3fa41	37	14	c6a62c4e56b0bd75	33
	ccaca55ed16c3653			4bc1a8d91e07d409	
6	18b3fa419616fe23	33	15	56b0bd7575e8fd8f	31
	d16c3653cf402c68			1e07d4091ce2e6dc	
7	9616fe2367117cf2	32	16	75e8fd8f25896490	32
	cf402c682b2cefbc			1ce2e6dc365e5f59	
8	67117cf2c11bfc09	33	IP-1	da02ce3a89ecac3b	32
	2b2cefbc99f91153		***************************************	057cde97d7683f2a	

Table 4.3 Avalanche Effect in DES: Change in Plaintext

Round		δ
	02468aceeca86420	0
	02468aceeca86420	
1	3cf03c0fbad22845	3
	3cf03c0f9ad628c5	
2	bad2284599e9b723	11
	9ad628c59939136b	
3	99e9b7230bae3b9e	2.5
	9939136b768067b7	
4	0bae3b9e42415649	29
	768067b75a8807c5	
5	4241564918b3fa41	26
	5a8807c5488dbe94	
6	18b3fa419616fe23	26
	488dbe94aba7fe53	
7	9616fe2367117cf2	27
	aba7fe53177d21e4	
8	67117cf2c11bfc09	32
	177d21e4548f1de4	

Round		δ
9	c11bfc09887fbc6c	34
	548f1de471f64dfd	
10	887fbc6c600f7e8b	36
	71f64dfd4279876c	
11	600f7e8bf596506e	32
	4279876c399fdc0d	
12	f596506e738538b8	28
	399fdc0d6d208dbb	
13	738538b8c6a62c4e	33
	6d208dbbb9bdeeaa	
14	c6a62c4e56b0bd75	30
	b9bdeeaad2c3a56f	
15	56b0bd7575e8fd8f	33
	d2c3a56f2765c1fb	
16	75e8fd8f25896490	30
	2765c1fb01263dc4	
IP-1	da02ce3a89ecac3b	30
	ee92b50606b62b0b	

Table 4.4 Avalanche Effect in DES: Change in Key

Table 4.5 Average Time Required for Exhaustive Key Search

Key Size (bits)	Cipher	Number of Alternative Keys	Time Required at 10 ⁹ Decryptions/s	Time Required at 10 ¹³ Decryptions/s
56	DES	$2^{56} \approx 7.2 \times 10^{16}$	2^{55} ns = 1.125 years	1 hour
128	AES	$2^{128} \approx 3.4 \times 10^{38}$	$2^{127} \text{ns} = 5.3 \times 10^{21} \text{years}$	$5.3 \times 10^{17} \text{years}$
168	Triple DES	$2^{168} \approx 3.7 \times 10^{50}$	$2^{167} \text{ns} = 5.8 \times 10^{33} \text{years}$	5.8×10^{29} years
192	AES	$2^{192} \approx 6.3 \times 10^{57}$	$2^{191} \text{ns} = 9.8 \times 10^{40} \text{years}$	9.8×10^{36} years
256	AES	$2^{256} \approx 1.2 \times 10^{77}$	$2^{255} \text{ns} = 1.8 \times 10^{60} \text{years}$	1.8×10^{56} years
26 characters (permutation)	Monoalphabetic	$2! = 4 \times 10^{26}$	$2 \times 10^{26} \text{ns} = 6.3 \times 10^9 \text{years}$	$6.3 \times 10^6 \mathrm{years}$

Strength of DES

Timing attacks

- One in which information about the key or the plaintext is obtained by observing how long it takes a given implementation to perform decryptions on various ciphertexts
- Exploits the fact that an encryption or decryption algorithm often takes slightly different amounts of time on different inputs
- So far it appears unlikely that this technique will ever be successful against DES or more powerful symmetric ciphers such as triple DES and AES

Block Cipher Design Principles: Number of Rounds

The greater the number of rounds, the more difficult it is to perform cryptanalysis

In general, the criterion should be that the number of rounds is chosen so that known cryptanalytic efforts require greater effort than a simple brute-force key search attack

If DES had 15 or fewer rounds, differential cryptanalysis would require less effort than a brute-force key search

Block Cipher Design Principles: Design of Function F

- The heart of a Feistel block cipher is the function F
- The more nonlinear F, the more difficult any type of cryptanalysis will be
- The SAC and BIC criteria appear to strengthen the effectiveness of the confusion function

The algorithm should have good avalanche properties

Strict avalanche criterion (SAC)

States that any output bit j of an S-box should change with probability 1/2 when any single input bit i is inverted for all i, j Bit independence criterion (BIC)

States that output bits j and k should change independently when any single input bit i is inverted for all i, j, and k

Block Cipher Design Principles: Key Schedule Algorithm

- With any Feistel block cipher, the key is used to generate one subkey for each round
- In general, we would like to select subkeys to maximize the difficulty of deducing individual subkeys and the difficulty of working back to the main key
- It is suggested that, at a minimum, the key schedule should guarantee key/ciphertext Strict Avalanche Criterion and Bit Independence Criterion

Summary

- Traditional Block Cipher
 Structure
 - Stream ciphers
 - Block ciphers
 - Motivation for the Feistel cipher structure
 - Feistel cipher
- The Data Encryption Standard (DES)
 - Encryption
 - Decryption
 - Avalanche effect



- The strength of DES
 - Use of 56-bit keys
 - Nature of the DES algorithm
 - Timing attacks
- Block cipher design principles
 - Number of rounds
 - Design of function F
 - Key schedule algorithm