Package 'clusterSim'

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Title Searching for Optimal Clustering Procedure for a Data Set

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2 cluster.Description

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Description

Descriptive statistics calculated separately for each cluster and variable: arithmetic mean and standard deviation, median and median absolute deviation, mode

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Usage

```
cluster.Description(x, cl, sdType="sample")
```

Arguments

x matrix or dataset

cl a vector of integers indicating the cluster to which each object is allocated sdType type of standard deviation: for "sample" (n-1) or for "population" (n)

Value

Three-dimensional array:

First dimension contains cluster number

Second dimension contains original coordinate (variable) number from matrix or data set

Third dimension contains number from 1 to 5:

- 1 arithmetic mean
- 2 standard deviation
- 3 median
- 4 median absolute deviation (mad)
- 5 mode (value of the variable which has the largest observed frequency. This formula is applicable for nominal and ordinal data only).

For example:

desc<-cluster.Description(x,cl)

desc[2,4,2] - standard deviation of fourth coordinate of second cluster

desc[3,1,5] - mode of first coordinate (variable) of third cluster

desc[1,,] - all statistics for all dimensions (variables) of first cluster

desc[,,3] - medians of all dimensions (variables) for each cluster

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See Also

```
cluster. Sim, mean, sd, median, mad
```

```
library(clusterSim)
data(data_ratio)
cl <- pam(data_ratio,5)
desc <- cluster.Description(data_ratio,cl$cluster)
print(desc)</pre>
```

4 cluster.Gen

cluster.Gen	Random cluster generation with known structure of clusters

Description

Random cluster generation with known structure of clusters (optionally with noisy variables and outliers)

Usage

Arguments

١	•	
	numObjects	number of objects in each cluster - positive integer value or vector with the same size as <i>nrow(means)</i> , e.g. numObjects=c(50,20)
	means	matrix of cluster means (e.g. means=matrix($c(0,8,0,8),2,2$)). If means = NULL matrix should be read from <i>means</i> _< <i>modelNumber>.csv file</i>
	cov	covariance matrix (the same for each cluster, e.g. cov=matrix($c(1, 0, 0, 1), 2, 2)$). If cov=NULL matrix should be read from
		cov_ <modelnumber>.csv file. Note: you cannot use this argument for generation of clusters with different covariance matrices. Those kind of generation should be done by setting fixedCov to FALSE and using appropriate model</modelnumber>
	model	model number, model=1 - no cluster structure. Observations are simulated from uniform distribution over the unit hypercube in number of dimensions (variables) given in numNoisyVar argument;
		model=2 - means and covariances are taken from arguments means and cov (see Example 1);
		model=3,4,,20 - see file
		\\$R_HOME\library\clusterSim\pdf\clusterGen_details.pdf;
		model=21,22,if fixedCov=TRUE means should be read from means_ <modelnumber>.csv and covariance matrix for all clusters should be read from cov_<modelnumber>.csv and if fixedCov=FALSE means should be read from means_<modelnumber>.csv and covariance matrices should be read separately for each cluster from</modelnumber></modelnumber></modelnumber>
		cov_ <modelnumber>_<clusternumber>.csv</clusternumber></modelnumber>
	fixedCov	if fixedCov=TRUE covariance matrix for all clusters is the same and if
		fixedCov=FALSE each cluster is generated from different covariance matrix - see model
	dataType	"m" - metric (ratio, interval), "o" - ordinal, "s" - symbolic interval

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numCategories number of categories (for ordinal data only). Positive integer value or vector with the same size as *ncol(means)* plus number of noisy variables. number of noisy variables. For model=1 it means number of variables numNoisyVar numOutliers number of outliers (for metric and symbolic interval data only). If a positive integer - number of outliers, if value from <0,1> - percentage of outliers in whole data set rangeOutliers range for outliers (for metric and symbolic interval data only). The default range is [1, 10]. The outliers are generated independently for each variable for the whole data set from uniform distribution. The generated values are randomly added to maximum of j-th variable or subtracted from minimum of j-th variable "csv" - a dot as decimal point or "csv2" - a comma as decimal point in inputType *means*_<*modelNumber*>.*csv* and *cov*_<*modelNumber*>.*csv* files inputHeader inputHeader=TRUE indicates that input files (means_<modelNumber>..csv; cov_<modelNumber...>.csv contain header row inputRowNames inputRowNames=TRUE indicates that input files (*means*_<*modelNumber*>.*csv*; cov\ <modelNumber...>.csv) contain first column with row names or with number of objects (positive integer values) outputCsv optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data) outputCsv2 optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data) outputColNames outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names outputRowNames outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Details

See file \\$R_HOME\library\clusterSim\pdf\clusterGen_details.pdf for further details

Value

clusters cluster number for each object, for model=1 each object belongs to its own clus-

ter thus this variable contains objects numbers

data generated data: for metric and ordinal data - matrix with objects in rows and

variables in columns; for symbolic interval data three-dimensional structure: first dimension represents object number, second - variable number and third

dimension contains lower- and upper-bounds of intervals

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Steinley, D., Henson, R. (2005), *OCLUS: an analytic method for generating clusters with known overlap*, "Journal of Classification", vol. 22, 221-250.

Walesiak, M., Dudek, A. (2008), *Identification of noisy variables for nonmetric and symbolic data in cluster analysis*, In: C. Preisach, H. Burkhardt, L. Schmidt-Thieme, R. Decker (Eds.), Data analysis, machine learning and applications, Springer-Verlag, Berlin, Heidelberg, 85-92.

```
# Example 1
library(clusterSim)
means <- matrix(c(0,7,0,7),2,2)
cov \leftarrow matrix(c(1,0,0,1),2,2)
grnd <- cluster.Gen(numObjects=60, means=means, cov=cov, model=2,</pre>
numOutliers=8)
colornames <- c("red","blue","green")</pre>
grnd$clusters[grnd$clusters==0]<-length(colornames)</pre>
plot(grnd$data,col=colornames[grnd$clusters],ask=TRUE)
# Example 2
library(clusterSim)
grnd <- cluster.Gen(50,model=4,dataType="m",numNoisyVar=2)</pre>
data <- as.matrix(grnd$data)</pre>
colornames <- c("red","blue","green")</pre>
plot(grnd$data,col=colornames[grnd$clusters],ask=TRUE)
# Example 3
library(clusterSim)
grnd<-cluster.Gen(50,model=4,dataType="o",numCategories=7, numNoisyVar=2)</pre>
plotCategorial(grnd$data,,grnd$clusters,ask=TRUE)
# Example 4 (1 nonnoisy variable and 2 noisy variables, 3 clusters)
library(clusterSim)
grnd <- cluster.Gen(c(40,60,20), model=2, means=c(2,14,25),
cov=c(1.5,1.5,1.5),numNoisyVar=2)
colornames <- c("red","blue","green")</pre>
plot(grnd$data,col=colornames[grnd$clusters],ask=TRUE)
# Example 5
library(clusterSim)
grnd <- cluster.Gen(c(20,35,20,25),model=14,dataType="m",numNoisyVar=1,</pre>
fixedCov=FALSE, numOutliers=0.1, outputCsv2="data14.csv")
data <- as.matrix(grnd$data)</pre>
colornames <- c("red","blue","green","brown","black")</pre>
```

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```
grnd$clusters[grnd$clusters==0]<-length(colornames)</pre>
plot(grnd$data,col=colornames[grnd$clusters],ask=TRUE)
# Example 6 (this example needs files means_24.csv)
# and cov_24.csv to be placed in working directory
# library(clusterSim)
# grnd<-cluster.Gen(c(50,80,20),model=24,dataType="m",numNoisyVar=1,</pre>
# numOutliers=10, rangeOutliers=c(1,5))
# print(grnd)
# data <- as.data.frame(grnd$data)</pre>
# colornames<-c("red","blue","green","brown")</pre>
# grnd$clusters[grnd$clusters==0]<-length(colornames)</pre>
# plot(data,col=colornames[grnd$clusters],ask=TRUE)
# Example 7 (this example needs files means_25.csv and cov_25_1.csv)
# cov_25_2.csv, cov_25_3.csv, cov_25_4.csv, cov_25_5.csv
# to be placed in working directory
# library(clusterSim)
\# grnd<-cluster.Gen(c(40,30,20,35,45),model=25,numNoisyVar=3,fixedCov=F)
# data <- as.data.frame(grnd$data)</pre>
# colornames<-c("red","blue","green","magenta","brown")</pre>
# plot(data,col=colornames[grnd$clusters],ask=TRUE)
```

cluster.Sim

Determination of optimal clustering procedure for a data set

Description

Determination of optimal clustering procedure for a data set by varying all combinations of normalization formulas, distance measures, and clustering methods

Usage

```
\label{local-cluster} cluster. Sim (x,p,minClusterNo,maxClusterNo,icq="S",outputHtml="",outputCsv="",outputCsv2="",normalizations=NULL,distances=NULL,methods=NULL)
```

Arguments

x	matrix or dataset
p	path of simulation: 1 - ratio data, 2 - interval or mixed (ratio & interval) data, 3 - ordinal data, 4 - nominal data, 5 - binary data, 6 - ratio data without normalization, 7 - interval or mixed (ratio & interval) data without normalization, 8 - ratio data with k-means, 9 - interval or mixed (ratio & interval) data with k-means
minClusterNo	minimal number of clusters, between 2 and no. of objects - 1 (for G3: no. of objects - 2)
maxClusterNo	maximal number of clusters, between 2 and no. of objects - 1 (for G3: no. of objects - 2; for KL: no. of objects - 3), greater or equal minClusterNo

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icq	Internal cluster quality index, "S" - Silhouette, "G1" - Calinski & Harabasz index, "G2" - Baker & Hubert index , "G3" - Hubert & Levine index, "KL" - Krzanowski & Lai index
outputHtml	optional, name of html file with results
outputCsv	optional, name of csv file with results
outputCsv2	optional, name of csv (comma as decimal point sign) file with results
normalizations	optional, vector of normalization formulas that should be used in procedure
distances	optional, vector of distance measures that should be used in procedure
methods	optional, vector of classification methods that should be used in procedure

Details

Parameter normalizations for each path may be the subset of the following values

path 1: "n6" to "n11" (if measurement scale of variables is ratio and transformed measurement scale of variables is ratio) or "n1" to "n5" (if measurement scale of variables is ratio and transformed measurement scale of variables is interval)

```
path 2: "n1" to "n5"
path 3 to 7: "n0"
path 8: "n1" to "n11"
path 9: "n1" to "n5"
```

Parameter distances for each path may be the subset of the following values

path 1: "d1" to "d7" (if measurement scale of variables is ratio and transformed measurement scale of variables is ratio) or "d1" to "d5" (if measurement scale of variables is ratio and transformed measurement scale of variables is interval)

```
path 2: "d1" to "d5"
path 3: "d8"
path 4: "d9"
path 5: "b1" to "b10"
path 6: "d1" to "d7"
path 7: "d1" to "d5"
path 8 and 9: N.A.
Parameter methods for each path may be the subset of the following values path 1 to 7: "m1" to "m8"
path 8: "m9"
path 9: "m9"
See file ../doc/clusterSim_details.pdf for further details
```

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Value

result optimal value of icq for all classifications
normalization normalization used to obtain optimal value of icq
distance distance measure used to obtain optimal value of icq

method clustering method used to obtain optimal value of icq

classes number of clusters for optimal value of icq

time time of all calculations for path

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References

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Walesiak, M., Dudek, A. (2007), Symulacyjna optymalizacja wyboru procedury klasyfikacyjnej dla danego typu danych - charakterystyka problemu, Zeszyty Naukowe Uniwersytetu Szczecinskiego nr 450, 635-646.

See Also

```
data.Normalization, dist.GDM, dist.BC, dist.SM, index.G1, index.G2, index.G3, index.S, index.KL, hclust, dist,
```

```
library(clusterSim)
# Commented due to long execution time
#data(data_ratio)
#cluster.Sim(data_ratio, 1, 2, 3, "G1", outputCsv="results1")
#data(data_interval)
#cluster.Sim(data_interval, 2, 2, 4, "G1", outputHtml="results2")
```

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```
#data(data_ordinal)
#cluster.Sim(data_ordinal, 3, 2, 4,"G2", outputCsv2="results3")
#data(data_nominal)
#cluster.Sim(data_nominal, p=4, 2, 4, icq="G3", outputHtml="results4", methods=c("m2","m3","m5"))
#data(data_binary)
#cluster.Sim(data_binary, p=5, 2, 4, icq="S", outputHtml="results5", distances=c("b1","b3","b6"))
data(data_ratio)
cluster.Sim(data_ratio, 1, 2, 4,"G1", outputCsv="results6",normalizations=c("n1","n3"),
distances=c("d2","d5"),methods=c("m5","m3","m1"))
```

comparing. Partitions Calculate agreement indices between two partitions

Description

Calculate agreement indices between two partitions

Usage

```
comparing.Partitions(cl1,cl2,type="nowak")
```

Arguments

cl1	A vector of integers (or letters) indicating the cluster to which each object is allocated for first clustering
c12	A vector of integers (or letters) indicating the cluster to which each object is allocated for second clustering
type	"rand" - for Rand index, "crand" - for adjusted Rand index or "nowak" for Nowak index

Details

See file \\$R_HOME\library\clusterSim\pdf\comparingPartitions_details.pdf for further details. Rand and adjusted Rand indices uses classAgreement function from e1071 library.

Value

Returns value of index.

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References

Hubert, L., Arabie, P. (1985), *Comparing partitions*, "Journal of Classification", no. 1, 193-218.

Nowak, E. (1985), *Wskaznik podobienstwa wynikow podzialow*, "Przeglad Statystyczny" ["Statistical Review"], no. 1, 41-48.

Rand, W.M. (1971), *Objective criteria for the evaluation of clustering methods*, "Journal of the American Statistical Association", no. 336, 846-850.

See Also

```
replication.Mod
```

Examples

```
# Example 1
library(clusterSim)
dataSet<-cluster.Gen(model=5)</pre>
cl1<-dataSet$clusters
cl2<-kmeans(dataSet$data,2)$cluster</pre>
print(comparing.Partitions(cl1,cl2,type="rand"))
# Example 2
library(clusterSim)
data(data_patternGDM1)
z<-data.Normalization(data_patternGDM1,type="n1")
d<-dist.GDM(z,method="GDM1")</pre>
cl1<-pam(d,3,diss=TRUE)$clustering</pre>
cl2<-pam(d,4,diss=TRUE)$clustering
print(comparing.Partitions(cl1,cl2,type="crand"))
# Example 3
library(clusterSim)
data(data_patternGDM1)
z<-data.Normalization(data_patternGDM1,type="n9")</pre>
d<-dist.GDM(z,method="GDM1")</pre>
cl1<-pam(d,3,diss=TRUE)$clustering</pre>
hc<-hclust(d, method="complete")</pre>
cl2<-cutree(hc,k=3)
print(comparing.Partitions(cl1,cl2,type="nowak"))
```

data.Normalization

Types of variable (column) and object (row) normalization formulas

Description

Types of variable (column) and object (row) normalization formulas

Usage

```
data.Normalization (x,type="n0",normalization="column")
```

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Arguments

vector, matrix or dataset Χ type of normalization: n0 - without normalization type n1 - standardization ((x-mean)/sd) n2 - positional standardization ((x-median)/mad) n3 - unitization ((x-mean)/range) n3a - positional unitization ((x-median)/range) n4 - unitization with zero minimum ((x-min)/range) n5 - normalization in range <-1,1> ((x-mean)/max(abs(x-mean))) n5a - positional normalization in range <-1,1> ((x-median)/max(abs(x-median))) n6 - quotient transformation (x/sd) n6a - positional quotient transformation (x/mad) n7 - quotient transformation (x/range) n8 - quotient transformation (x/max) n9 - quotient transformation (x/mean) n9a - positional quotient transformation (x/median)

n10 - quotient transformation (x/sum)

n11 - quotient transformation (x/sqrt(SSQ))

n12 - normalization ((x-mean)/sqrt(sum((x-mean)^2)))

n12a - positional normalization ((x-median)/sqrt(sum((x-median)^2)))

n13 - normalization with zero being the central point ((x-midrange)/(range/2))

normalization "column" - normalization by variable, "row" - normalization by object

Details

See file .../doc/dataNormalization_details.pdf for further details

Value

Normalized data

Author(s)

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See Also

```
cluster.Sim
```

Examples

```
library(clusterSim)
data(data_ratio)
z1 <- data.Normalization(data_ratio,type="n1",normalization="column")
z2 <- data.Normalization(data_ratio,type="n10",normalization="row")</pre>
```

data_binary

Binary data

Description

Binary variables for eight people

Format

data.frame: 8 objects, 10 variables

Source

Kaufman, L., Rousseeuw, P.J. (1990), Finding groups in data: an introduction to cluster analysis, Wiley, New York, p. 24.

```
library(clusterSim)
data(data_binary)
cluster.Sim(data_binary, p=5, 2, 6, icq="S",
outputHtml="results5", distances=c("b1","b3","b6"))
```

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data_interval

Interval data

Description

Artificially generated interval data

Format

```
data.frame: 75 objects, 5 variables, 5-class structure
```

Source

Artificially generated data

Examples

```
library(clusterSim)
data(data_interval)
cluster.Sim(data_interval, 2, 2, 3, "G1", outputHtml="results2")
```

data_mixed

Mixed data

Description

Artificial mixed data

Format

data.frame: 25 objects, 4 variables (1, 3 - interval variables, 2 - ordinal variable, 4, nominal variable

Source

Artificial data

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 $data_nominal$

Nominal data

Description

Artificial nominal data

Format

data.frame: 26 objects, 12 variables

Source

Artificial data

Examples

```
library(clusterSim)
data(data_nominal)
cluster.Sim(data_nominal, p=4, 2, 5, icq="G3",
outputHtml="results4", methods=c("m2","m3","m5"))
```

 $data_ordinal$

Ordinal data

Description

Artificial ordinal data

Format

data.frame: 26 objects, 12 variables

Source

Artificial data

```
library(clusterSim)
data(data_ordinal)
cluster.Sim(data_ordinal, 3, 3, 12,"S",
outputCsv2="results3")
```

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data_patternGDM1	Metric data with 17 objects and 10 variables (8 stimulant variables, 2
	destimulant variables)

Description

Metric data with 17 objects and 10 variables (8 stimulant variables, 2 destimulant variables)

Data on the Polish voivodships, owing to the conditions of the population living in cities in 2007. The analysis includes the following variables:

- x1 dwellings in per cent fitted with water-line system,
- x2 dwellings in per cent fitted with lavatory,
- x3 dwellings in per cent fitted with bathroom,
- x4 dwellings in per cent fitted with gas-line system,
- x5 dwellings in per cent fitted with central heating,
- x6 average number of rooms per dwelling,
- x7 average number of persons per dwelling,
- x8 average number of persons per room,
- x9 usable floor space in square meter per dwelling,
- x10 usable floor space in square meter per person.

Types of performance variables:

x1 - x6, x9, x10 - stimulants,

x7, x8 - destimulants.

Format

```
data.frame: 17 objects, 10 variables
```

Source

Voivodships Statistical Yearbook, Poland 2008.

```
# Example 1
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n4",patternType<-"lower",patternCoordinates<-"manual",
patternManual<-c(0,0,0,0,0,"min","max","max","min","min"),
nominalTransfMethod <-NULL)
print(res)</pre>
```

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```
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p), max(gdm_p)), xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object",lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
# Example 2
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n2",patternType<-"upper",</pre>
patternCoordinates<-"dataBounds",patternManual<-NULL,
nominalTransfMethod <-NULL)</pre>
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p),xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p), max(gdm_p)), xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
```

data_patternGDM2

Ordinal data with 27 objects and 6 variables (3 stimulant variables, 2 destimulant variables and 1 nominant variable)

Description

Ordinal data with 27 objects and 6 variables (3 stimulant variables, 2 destimulant variables and 1 nominant variable)

Residential housing properties were described by the following variables:

- x1 Location of environmental land, which is linked to a dwelling (1 poor, 2 inadequate, 3 satisfactory, 4 good, 5 very good),
- x2 Standard utility of a dwelling (1 bad, 2 low, 3 average, 4 high),
- x3 Living conditions occurring on the land, which is linked to a dwelling (1 bad, 2 average, 3 good),
- x4 Location of land, which is related to dwelling in the area of the city (1 central, 2 downtown, 3 intermediate, 4 peripheral),
- x5 Type of condominium (1 low, 2 large),
- x6 Area of land, which is related to dwelling (1 below the contour of the building, 2 outline of the building, 3 the outline of the building with the environment acceptable, such as parking, playground, 4 the outline of the building with the environment too much).

Types of performance variables:

```
x1, x2, x3 - stimulants,
```

18 data_patternGDM2

```
x4, x5 - destimulants,x6 - nominant (the nominal category: 3).
```

Format

data.frame: 27 objects, 6 variables

Source

data from real estate market

```
# Example 1
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="lower", patternCoordinates="manual",
patternManual=c("min","min",0,5,"max","max"),
nominalTransfMethod="symmetrical")
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object",lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
# Example 2
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,</pre>
patternType="upper", patternCoordinates="dataBounds",
patternManual=NULL, nominalTransfMethod="database")
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p), xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
```

data_ratio 19

data_ratio

Ratio data

Description

Artificially generated ratio data

Format

```
data.frame: 75 objects, 5 variables, 5-class structure
```

Source

Artificially generated data

Examples

```
library(clusterSim)
data(data_ratio)
c <- pam(data_ratio,10)
index.G1(data_ratio, c$clustering)</pre>
```

data_symbolic

Symbolic interval data

Description

Artificially generated symbolic interval data

Format

3-dimensional array: 125 objects, 6 variables, third dimension represents begining and end of interval, 5-class structure

Source

Artificially generated data

```
library(clusterSim)
data(data_symbolic)
r<- HINoV.Symbolic(data_symbolic, u=5)
print(r$stopri)
plot(r$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r$stopri[,1])),labels=r$stopri[,1])</pre>
```

20 dist.BC

dist.BC

Calculates Bray-Curtis distance measure for ratio data

Description

Calculates Bray-Curtis distance measure for ratio data

Usage

```
dist.BC (x)
```

Arguments

Х

matrix or dataset

Details

See file \\$R_HOME\library\clusterSim\pdf\distBC_details.pdf for further details

Value

object with calculated distance

Author(s)

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References

Cormack, R.M. (1971), *A review of classification (with discussion)*, "Journal of the Royal Statistical Society", ser. A, part 3, 321-367.

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wroclaw, p. 41.

See Also

```
dist.GDM, dist.SM, dist
```

```
library(clusterSim)
sampleData <- cbind(c(2,3,5),c(4,5,6),c(5,3,4))
d <- dist.BC(sampleData)</pre>
```

dist.GDM 21

re
r

Description

Calculates Generalized Distance Measure for variables measured on metric scale (ratio & interval) or ordinal scale

Usage

```
dist.GDM(x, method="GDM1", weightsType="equal", weights=NULL)
GDM(x, method="GDM1", weightsType="equal", weights=NULL)
GDM1(x, weightsType="equal", weights=NULL)
GDM2(x, weightsType="equal", weights=NULL)
```

Arguments

x matrix or data setmethod GDM1 or GDM2

"GDM1" - metric scale (ratio & interval)

"GDM2" - ordinal scale

weightsType equal or different1 or different2

"equal" - equal weights

"different1" - vector of different weights should satisfy conditions: each weight

takes value from interval [0; 1] and sum of weights equals one

"different2" - vector of different weights should satisfy conditions: each weight takes value from interval [0; m] and sum of weights equals m (m - the number

of variables)

weights vector of weights

Details

See file \\$R_HOME\library\clusterSim\pdf\distGDM_details.pdf for further details

Value

object with calculated distance

Author(s)

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22 dist.SM

References

Walesiak, M. (1999), *Distance Measure for Ordinal Data*, "Argumenta Oeconomica", No. 2 (8), 167-173.

Jajuga, K., Walesiak, M., Bak, A. (2003), *On the general distance measure*, In: M. Schwaiger, O. Opitz (Eds.), Exploratory data analysis in empirical research, Springer-Verlag, Berlin, Heidelberg, 104-109.

Walesiak, M. (2006), *Uogolniona miara odleglosci w statystycznej analizie wielowymiarowej [The Generalized Distance Measure in multivariate statistical analysis]*, Wydawnictwo AE, Wroclaw.

See Also

```
dist.BC, dist.SM, dist
```

Examples

```
#Example 1
library(clusterSim)
data(data_ratio)
d1 <- GDM(data_ratio, method="GDM1")</pre>
data(data_ordinal)
d2 <- GDM(data_ordinal, method="GDM2")</pre>
d3 <- GDM1(data_ratio)</pre>
d4 <- GDM2(data_ordinal)
#Example 2
library(clusterSim)
data(data_ratio)
d1w <- GDM(data_ratio, method="GDM1", weightsType="different1",</pre>
weights=c(0.4,0.1,0.3,0.15,0.05))
data(data_ordinal)
d2w <- GDM(data_ordinal, method="GDM2", weightsType="different2",</pre>
weights=c(1,3,0.5,1.5,1.8,0.2,0.4,0.6,0.2,0.4,0.9,1.5))
```

dist.SM

Calculates Sokal-Michener distance measure for nominal variables

Description

Calculates Sokal-Michener distance measure for nominal variables

Usage

```
dist.SM(x)
```

Arguments

Χ

matrix or data set

dist.Symbolic 23

Details

See file \\$R_HOME\library\clusterSim\pdf\distSM_details.pdf for further details

Value

object with calculated distance

Author(s)

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References

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wroclaw, p. 43.

Kaufman, L., Rousseeuw, P.J. (1990), Finding groups in data: an introduction to cluster analysis, Wiley, New York, p. 28.

See Also

```
dist.GDM, dist.BC, dist
```

Examples

```
library(clusterSim)
data(data_nominal)
d <- dist.SM(data_nominal)</pre>
```

dist.Symbolic

Calculates distance between symbolic interval-valued data

Description

Calculates distance between symbolic interval-valued data for four distance types

Usage

```
dist.Symbolic(data,type="U_2",gamma=0.5,power=2)
```

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Arguments

data symbolic data

type type of distance used for symbolic interval-valued data

U_2 - Ichino and Yaguchi distance

M - distance between points given by means of intervals (for interval-values

variables),

H - Hausdorff distance,

S - sum of distances between all corresponding vertices of hyperrectangles given

by symbolic objects with interval-valued variables)

gamma parameter for calculating Ichino and Yaguchi distance

power parameter (q) for calculating Ichino and Yaguchi distance

Details

See file \\$R_HOME\library\clusterSim\pdf\distSymbolic_details.pdf for further details

Author(s)

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References

Billard, L., Diday, E. (2006), Symbolic data analysis. Conceptual statistics and data mining, Wiley, Chichester.

See Also

dist.SM

Examples

```
library(clusterSim)
dataSymbolic<-cluster.Gen(numObjects=10,model=5,dataType="s")$data
print(dist.Symbolic(dataSymbolic))</pre>
```

HINOV. Mod Modification of Carmone

Modification of Carmone, Kara\& Maxwell Heuristic Identification of Noisy Variables (HINoV) method

Description

Modification of Heuristic Identification of Noisy Variables (HINoV) method

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Usage

```
HINoV.Mod (x, type="metric", s = 2, u, distance=NULL, method = "kmeans", Index ="cRAND")
```

Arguments

X	data matrix
type	"metric" (default) - all variables are metric (ratio, interval), "nonmetric" - all variables are nonmetric (ordinal, nominal) or vector containing for each variable value "m"(metric) or "n"(nonmetric) for mixed variables (metric and nonmetric), e.g. type=c("m", "n", "n", "m")
S	for metric data only: 1 - ratio data, 2 - interval or mixed (ratio & interval) data
u	number of clusters (for metric data only)
distance	NULL for kmeans method (based on data matrix) and nonmetric data for ratio data: "d1" - Manhattan, "d2" - Euclidean, "d3" - Chebychev (max), "d4" - squared Euclidean, "d5" - GDM1, "d6" - Canberra, "d7" - Bray-Curtis
	for interval or mixed (ratio & interval) data: "d1", "d2", "d3", "d4", "d5"
method	NULL for nonmetric data
	clustering method: "kmeans" (default) , "single", "ward.D", "ward.D2", "complete", "average", "mcquitty", "median", "centroid", "pam"
Index	"cRAND" - corrected Rand index (default); "RAND" - Rand index

Details

See file ../doc/HINoVMod_details.pdf for further details

Value

parim $m \times m$ symmetric matrix (m - number of variables). Matrix contains pairwise

corrected Rand (Rand) indices for partitions formed by the j-th variable with

partitions formed by the l-th variable

topri sum of rows of parim

stopri ranked values of topri in decreasing order

Author(s)

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References

Carmone, F.J., Kara, A., Maxwell, S. (1999), *HINoV: a new method to improve market segment definition by identifying noisy variables*, "Journal of Marketing Research", November, vol. 36, 501-509.

Hubert, L.J., Arabie, P. (1985), Comparing partitions, "Journal of Classification", no. 1, 193-218.

26 HINoV.Symbolic

Rand, W.M. (1971), Objective criteria for the evaluation of clustering methods, "Journal of the American Statistical Association", no. 336, 846-850.

Walesiak, M. (2005), *Variable selection for cluster analysis - approaches, problems, methods*, Plenary Session of the Committee on Statistics and Econometrics of the Polish Academy of Sciences, 15 March, Wroclaw.

Walesiak, M., Dudek, A. (2008), *Identification of noisy variables for nonmetric and symbolic data in cluster analysis*, In: C. Preisach, H. Burkhardt, L. Schmidt-Thieme, R. Decker (Eds.), Data analysis, machine learning and applications, Springer-Verlag, Berlin, Heidelberg, 85-92.

See Also

```
hclust, kmeans, dist, dist.GDM, dist.BC, dist.SM, cluster.Sim
```

Examples

```
# for metric data
library(clusterSim)
data(data_ratio)
r1<- HINoV.Mod(data_ratio, type="metric", s=1, 4, method="kmeans",
     Index="cRAND")
print(r1$stopri)
plot(r1$stopri[,2],xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r1$stopri[,1])),labels=r1$stopri[,1])
# for nonmetric data
library(clusterSim)
data(data_nominal)
r2<- HINoV.Mod (data_nominal, type="nonmetric", Index = "cRAND")</pre>
print(r2$stopri)
plot(r2$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r2$stopri[,1])),labels=r2$stopri[,1])
# for mixed data
library(clusterSim)
data(data_mixed)
r3<- HINoV.Mod(data_mixed, type=c("m","n","m","n"), s=2, 3, distance="d1",
     method="complete", Index="cRAND")
print(r3$stopri)
plot(r3$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r3$stopri[,1])),labels=r3$stopri[,1])
```

HINoV.Symbolic

Modification of Carmone, Kara\& Maxwell Heuristic Identification of Noisy Variables (HINoV) method for symbolic interval data

HINoV.Symbolic 27

Description

Modification of Heuristic Identification of Noisy Variables (HINoV) method for symbolic interval data

Usage

```
HINoV.Symbolic(x, u=NULL, distance="H", method = "pam",
Index = "cRAND")
```

Arguments

x symbolic interval data: a 3-dimensional table, first dimension represents ob-

ject number, second dimension - variable number, and third dimension contains

lower- and upper-bounds of intervals

u number of clusters

distance "M" - minimal distance between all vertices of hyper-cubes defined by symbolic

interval variables; "H" - Hausdorff distance; "S" - sum of squares of distance between all vertices of hyper-cubes defined by symbolic interval variables

method clustering method: "single", "ward.D", "ward.D2", "complete", "average", "mc-

quitty", "median", "centroid", "pam" (default)

Index "cRAND" - corrected Rand index (default); "RAND" - Rand index

Details

See file ../doc/HINoVSymbolic_details.pdf for further details

Value

parim $m \times m$ symmetric matrix (m - number of variables). Matrix contains pairwise

corrected Rand (Rand) indices for partitions formed by the j-th variable with

partitions formed by the l-th variable

topri sum of rows of parim

stopri ranked values of topri in decreasing order

Author(s)

Marek Walesiak <marek.walesiak@ue.wroc.pl>, Andrzej Dudek <andrzej.dudek@ue.wroc.pl> Department of Econometrics and Computer Science, University of Economics, Wroclaw, Poland http://keii.ue.wroc.pl/clusterSim

References

Carmone, F.J., Kara, A., Maxwell, S. (1999), *HINoV: a new method to improve market segment definition by identifying noisy variables*, "Journal of Marketing Research", November, vol. 36, 501-509.

Hubert, L.J., Arabie, P. (1985), Comparing partitions, "Journal of Classification", no. 1, 193-218.

28 index.DB

Rand, W.M. (1971), *Objective criteria for the evaluation of clustering methods*, "Journal of the American Statistical Association", no. 336, 846-850.

Walesiak, M., Dudek, A. (2008), *Identification of noisy variables for nonmetric and symbolic data in cluster analysis*, In: C. Preisach, H. Burkhardt, L. Schmidt-Thieme, R. Decker (Eds.), Data analysis, machine learning and applications, Springer-Verlag, Berlin, Heidelberg, 85-92.

See Also

```
hclust, kmeans, cluster.Sim
```

Examples

```
library(clusterSim)
data(data_symbolic)
r<- HINoV.Symbolic(data_symbolic, u=5)
print(r$stopri)
plot(r$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r$stopri[,1])),labels=r$stopri[,1])
#symbolic data from .csv file
#library(clusterSim)
#dsym<-as.matrix(read.csv2(file="csv/symbolic.csv"))</pre>
#dim(dsym)<-c(dim(dsym)[1],dim(dsym)[2]%/%2,2)
#r<- HINoV.Symbolic(dsym, u=5)</pre>
#print(r$stopri)
#plot(r$stopri[,2], xlab="Variable number", ylab="topri",
#xaxt="n", type="b")
#axis(1,at=c(1:max(r$stopri[,1])),labels=r$stopri[,1])
```

index.DB

Calculates Davies-Bouldin's index

Description

Calculates Davies-Bouldin's cluster separation measure

Usage

```
index.DB(x, c1, d=NULL, centrotypes="centroids", p=2, q=2)
```

Arguments

X	data
cl	vector of integers indicating the cluster to which each object is allocated
d	optional distance matrix, used for calculations if centrotypes="medoids"
centrotypes	"centroids" or "medoids"

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p	the power of the Minkowski distance between centroids or medoids of clusters: p=1 - Manhattan distance; p=2 - Euclidean distance
q	the power of dispersion measure of a cluster: q=1 - the average distance of objects in the r-th cluster to the centroid or medoid of the r-th cluster; q=2 - the standard deviation of the distance of objects in the r-th cluster to the centroid or medoid of the r-th cluster

Details

```
See file ../doc/indexDB_details.pdf for further details
```

Thanks to prof. Christian Hennig c.hennig@ucl.ac.uk for finding and fixing the "immutable p" error

Value

DB	Davies-Bouldin's index
r	vector of maximal R values for each cluster
R	R matrix \$(S_r+S_s)/d_rs\$
d	matrix of distances between centroids or medoids of clusters
S	vector of dispersion measures for each cluster
centers	coordinates of centroids or medoids for all clusters

Author(s)

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References

Davies, D.L., Bouldin, D.W. (1979), *A cluster separation measure*, IEEE Transactions on Pattern Analysis and Machine Intelligence, vol. 1, no. 2, 224-227.

See Also

```
index.G1, index.G2, index.G3, index.S, index.H, index.Gap, index.KL
```

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1 <- pam(data_ratio, 4)
d<-dist(data_ratio)
print(index.DB(data_ratio, cl1$clustering,d, centrotypes="medoids"))
# Example 2
library(clusterSim)</pre>
```

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```
data(data_ratio)
cl2 <- pam(data_ratio, 5)</pre>
print(index.DB(data_ratio, cl2$clustering, centrotypes="centroids"))
# Example 3
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="euclidean")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=8
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
hc <- hclust(md, method="complete")</pre>
cl2 <- cutree(hc, k=nc)</pre>
res[nc-min_nc+1, 2] <- DB <- index.DB(data_ratio, cl2, centrotypes="centroids")$DB</pre>
clusters <- rbind(clusters, cl2)</pre>
print(paste("min DB for",(min_nc:max_nc)[which.min(res[,2])],"clusters=",min(res[,2])))
print("clustering for min DB")
print(clusters[which.min(res[,2]),])
write.table(res,file="DB_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="DB", xaxt="n")
axis(1, c(min_nc:max_nc))
# Example 4
library(clusterSim)
data(data_ordinal)
md <- dist.GDM(data_ordinal, method="GDM2")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=6
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc</pre>
clusters <- NULL
for (nc in min_nc:max_nc)
hc <- hclust(md, method="complete")</pre>
cl2 <- cutree(hc, k=nc)</pre>
res[nc-min_nc+1,2] <- DB <- index.DB(data_ordinal,cl2,d=md,centrotypes="medoids")$DB</pre>
clusters <- rbind(clusters, cl2)</pre>
print(paste("min DB for",(min_nc:max_nc)[which.min(res[,2])],"clusters=",min(res[,2])))
print("clustering for min DB")
print(clusters[which.min(res[,2]),])
write.table(res,file="DB_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="DB", xaxt="n")
axis(1, c(min_nc:max_nc))
```

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Calculates Calinski-Harabasz pseudo F-statistic

Description

Calculates Calinski-Harabasz pseudo F-statistic

Usage

```
index.G1 (x,cl,d=NULL,centrotypes="centroids")
```

Arguments

^	uata
cl	A vector of integers indicating the cluster to which each object is allocated
d	optional distance matrix, used for calculations if centrotypes="medoids"

centrotypes "centroids" or "medoids"

data

Details

See file .../doc/indexG1_details.pdf for further details.

thank to Nejc Ilc from University of Ljubljana for fixing error for one-element clusters.

Value

Calinski-Harabasz pseudo F-statistic

Author(s)

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References

Calinski, T., Harabasz, J. (1974), A dendrite method for cluster analysis, "Communications in Statistics", vol. 3, 1-27.

Everitt, B.S., Landau, E., Leese, M. (2001), Cluster analysis, Arnold, London, p. 103.

Gatnar, E., Walesiak, M. (Eds.) (2004), Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research], Wydawnictwo AE, Wroclaw, p. 338.

Gordon, A.D. (1999), Classification, Chapman & Hall/CRC, London, p. 62.

Milligan, G.W., Cooper, M.C. (1985), An examination of procedures of determining the number of cluster in a data set, "Psychometrika", vol. 50, no. 2, 159-179.

See Also

```
index.G2,index.G3,index.S, index.H,index.KL,index.Gap, index.DB
```

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
c<- pam(data_ratio,10)</pre>
index.G1(data_ratio,c$clustering)
# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="euclidean")</pre>
# nc - number_of_clusters
min nc=2
max_nc=20
res <- array(0,c(max_nc-min_nc+1,2))</pre>
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
cl2 <- pam(md, nc, diss=TRUE)</pre>
res[nc-min_nc+1,2] <- G1 <- index.G1(data_ratio,cl2$cluster,centrotypes="centroids")</pre>
clusters <- rbind(clusters, cl2$cluster)</pre>
print(paste("max G1 for",(min_nc:max_nc)[which.max(res[,2])],"clusters=",max(res[,2])))
print("clustering for max G1")
print(clusters[which.max(res[,2]),])
write.table(res,file="G1_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="G1", xaxt="n")
axis(1, c(min_nc:max_nc))
```

index.G2

Calculates G2 internal cluster quality index

Description

Calculates G2 internal cluster quality index - Baker & Hubert adaptation of Goodman & Kruskal's Gamma statistic

Usage

```
index.G2(d,c1)
```

Arguments

d 'dist' object

cl A vector of integers indicating the cluster to which each object is allocated

Details

See file \\$R_HOME\library\clusterSim\pdf\indexG2_details.pdf for further details

Value

calculated G2 index

Author(s)

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References

Everitt, B.S., Landau, E., Leese, M. (2001), Cluster analysis, Arnold, London, p. 104.

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wroclaw, p. 339.

Gordon, A.D. (1999), Classification, Chapman & Hall/CRC, London, p. 62.

Hubert, L. (1974), Approximate evaluation technique for the single-link and complete-link hierarchical clustering procedures, "Journal of the American Statistical Association", vol. 69, no. 347, 698-704.

Milligan, G.W., Cooper, M.C. (1985), An examination of procedures of determining the number of cluster in a data set, "Psychometrika", vol. 50, no. 2, 159-179.

See Also

```
index.G1, index.G3, index.S, index.H, index.KL, index.Gap, index.DB
```

```
# Example 1
library(clusterSim)
data(data_ratio)
d <- dist.GDM(data_ratio)</pre>
c \leftarrow pam(d, 5, diss = TRUE)
icq <- index.G2(d,c$clustering)</pre>
print(icq)
# Example 2
library(clusterSim)
data(data_ordinal)
d <- dist.GDM(data_ordinal, method="GDM2")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=6
res <- array(0,c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
```

```
clusters <- NULL
for (nc in min_nc:max_nc)
{
    cl2 <- pam(d, nc, diss=TRUE)
    res[nc-min_nc+1,2] <- G2 <- index.G2(d,cl2$cluster)
    clusters <- rbind(clusters,cl2$cluster)
}
print(paste("max G2 for",(min_nc:max_nc)[which.max(res[,2])],"clusters=",max(res[,2])))
print("clustering for max G2")
print(clusters[which.max(res[,2]),])
write.table(res,file="G2_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="G2", xaxt="n")
axis(1, c(min_nc:max_nc))</pre>
```

index.G3

Calculates G3 internal cluster quality index

Description

Calculates G3 Hubert & Levine internal cluster quality index

Usage

```
index.G3(d,cl)
```

Arguments

d 'dist' object

cl A vector of integers indicating the cluster to which each object is allocated

Details

See file \\$R_HOME\library\clusterSim\pdf\indexG3_details.pdf for further details

Value

calculated G3 index

Author(s)

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References

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wroclaw, p. 339.

Gordon, A.D. (1999), Classification, Chapman & Hall/CRC, London, p. 62.

Milligan, G.W., Cooper, M.C. (1985), An examination of procedures of determining the number of cluster in a data set, "Psychometrika", vol. 50, no. 2, 159-179.

See Also

```
index.G1, index.G2, index.S, index.H, index.KL, index.Gap, index.DB
```

```
# Example 1
library(clusterSim)
data(data_ratio)
d <- dist.GDM(data_ratio)</pre>
c \leftarrow pam(d, 5, diss = TRUE)
icq <- index.G3(d,c$clustering)</pre>
print(icq)
# Example 2
library(clusterSim)
data(data_ordinal)
d <- dist.GDM(data_ordinal, method="GDM2")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=6
res <- array(0,c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc</pre>
clusters <- NULL
for (nc in min_nc:max_nc)
hc <- hclust(d, method="complete")</pre>
cl2 <- cutree(hc, k=nc)</pre>
res[nc-min_nc+1,2] \leftarrow G3 \leftarrow index.G3(d,cl2)
clusters <- rbind(clusters,cl2)</pre>
}
print(paste("min G3 for",(min_nc:max_nc)[which.min(res[,2])],"clusters=",min(res[,2])))
print("clustering for min G3")
print(clusters[which.min(res[,2]),])
write.table(res,file="G3_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="G3", xaxt="n")
axis(1, c(min_nc:max_nc))
```

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index.Gap

Calculates Tibshirani, Walther and Hastie gap index

Description

Calculates Tibshirani, Walther and Hastie gap index

Usage

```
index.Gap (x, clall, reference.distribution="unif", B=10,
method="pam",d=NULL,centrotypes="centroids")
```

Arguments

Χ data

clall Two vectors of integers indicating the cluster to which each object is allocated

in partition of n objects into u, and u+1 clusters

reference.distribution

"unif" - generate each reference variable uniformly over the range of the observed values for that variable or "pc" - generate the reference variables from a uniform distribution over a box aligned with the principal components of the data. In detail, if $X=\{x_i\}$ is our n x m data matrix, assume that the columns have mean 0 and compute the singular value decomposition \$X=UDV^T\$. We transform via \$X'=XV\$ and then draw uniform features Z' over the ranges of the columns of X', as in method a) above. Finally we back-transform via

\$Z=Z'V^T\$ to give reference data Z

the number of simulations used to compute the gap statistic the cluster analysis method to be used. This should be one of: "ward.D", method

"ward.D2", "single", "complete", "average", "mcquitty", "median", "centroid",

"pam", "k-means", "diana"

d optional distance matrix, used for calculations if centrotypes="medoids"

"centroids" or "medoids" centrotypes

Details

В

See file .../doc/indexGap_details.pdf for further details

Thanks to dr Michael P. Fay from National Institute of Allergy and Infectious Diseases for finding "one column error".

Value

Gap Tibshirani, Walther and Hastie gap index for u clusters

diffu necessary value for choosing correct number of clusters via gap statistic Gap(u)-

[Gap(u+1)-s(u+1)]

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Author(s)

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References

Tibshirani, R., Walther, G., Hastie, T. (2001), *Estimating the number of clusters in a data set via the gap statistic*, "Journal of the Royal Statistical Society", ser. B, vol. 63, part 2, 411-423.

See Also

```
index.G1, index.G2, index.G3, index.S, index.H, index.KL, index.DB
```

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1<-pam(data_ratio,4)</pre>
cl2<-pam(data_ratio,5)</pre>
clall<-cbind(cl1$clustering,cl2$clustering)</pre>
g<-index.Gap(data_ratio, clall, reference.distribution="unif", B=10,</pre>
   method="pam")
print(g)
# Example 2
library(clusterSim)
means <- matrix(c(0,2,4,0,3,6), 3, 2)
cov \leftarrow matrix(c(1,-0.9,-0.9,1), 2, 2)
x <- cluster.Gen(numObjects=40, means=means, cov=cov, model=2)</pre>
x <- x$data
md <- dist(x, method="euclidean")^2</pre>
# nc - number_of_clusters
min_nc=1
max_nc=5
min <- 0
clopt <- NULL</pre>
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc</pre>
found <- FALSE
for (nc in min_nc:max_nc){
  cl1 <- pam(md, nc, diss=TRUE)</pre>
  cl2 <- pam(md, nc+1, diss=TRUE)</pre>
  clall <- cbind(cl1$clustering, cl2$clustering)</pre>
  gap <- index.Gap(x,clall,B=20,method="pam",centrotypes="centroids")</pre>
  res[nc-min_nc+1, 2] <- diffu <- gap$diffu
  if ((res[nc-min_nc+1, 2] >=0) && (!found)){
    nc1 <- nc
    min <- diffu
    clopt <- cl1$cluster</pre>
```

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```
found <- TRUE
  }
}
if (found){
print(paste("Minimal nc where diffu>=0 is",nc1,"for diffu=",round(min,4)),quote=FALSE)
print("I have not found clustering with diffu>=0", quote=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="diffu",xaxt="n")
abline(h=0, untf=FALSE)
axis(1, c(min_nc:max_nc))
# Example 3
library(clusterSim)
means <- matrix(c(0,2,4,0,3,6), 3, 2)
cov \leftarrow matrix(c(1,-0.9,-0.9,1), 2, 2)
x <- cluster.Gen(numObjects=40, means=means, cov=cov, model=2)</pre>
x <- x$data
md <- dist(x, method="euclidean")^2</pre>
# nc - number_of_clusters
min_nc=1
max_nc=5
min <- 0
clopt <- NULL</pre>
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc</pre>
found <- FALSE
for (nc in min_nc:max_nc){
  cl1 <- pam(md, nc, diss=TRUE)</pre>
  cl2 <- pam(md, nc+1, diss=TRUE)</pre>
  clall <- cbind(cl1$clustering, cl2$clustering)</pre>
  gap <- index.Gap(x,clall,B=20,method="pam",d=md,centrotypes="medoids")</pre>
  res[nc-min_nc+1, 2] <- diffu <- gap$diffu</pre>
  if ((res[nc-min_nc+1, 2] >=0) && (!found)){
    nc1 <- nc
    min <- diffu
    clopt <- cl1$cluster</pre>
    found <- TRUE
}
if (found){
print(paste("Minimal nc where diffu>=0 is",nc1,"for diffu=",round(min,4)),quote=FALSE)
print("I have not found clustering with diffu>=0",quote=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="diffu", xaxt="n")
abline(h=0, untf=FALSE)
axis(1, c(min_nc:max_nc))
```

index.H

Description

Calculates Hartigan index

Usage

```
index.H (x,clall,d=NULL,centrotypes="centroids")
```

Arguments

x data

clall Two vectors of integers indicating the cluster to which each object is allocated

in partition of n objects into u and u+1 clusters

d optional distance matrix, used for calculations if centrotypes="medoids"

centrotypes "centroids" or "medoids"

Details

See file \\$R_HOME\library\clusterSim\pdf\indexH_details.pdf for further details

Value

Hartigan index

Author(s)

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References

Hartigan, J. (1975), Clustering algorithms, Wiley, New York.

Milligan, G.W., Cooper, M.C. (1985), An examination of procedures of determining the number of cluster in a data set, "Psychometrika", vol. 50, no. 2, 159-179.

Tibshirani, R., Walther, G., Hastie, T. (2001), *Estimating the number of clusters in a data set via the gap statistic*, "Journal of the Royal Statistical Society", ser. B, vol. 63, part 2, 411-423.

See Also

```
index.G1, index.G2, index.G3, index.S, index.KL, index.Gap, index.DB
```

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```
# Example 1
library(clusterSim)
data(data_ratio)
cl1<-pam(data_ratio,4)</pre>
cl2<-pam(data_ratio,5)</pre>
clall<-cbind(cl1$clustering,cl2$clustering)</pre>
index.H(data_ratio,clall)
# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="euclidean")</pre>
# nc - number_of_clusters
min_nc=1
max_nc=20
min <- 0
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc
found <- FALSE
clusters <- NULL
for (nc in min_nc:max_nc)
print(nc)
hc <- hclust(md, method="complete")</pre>
cl1 <- cutree(hc, k=nc)</pre>
cl2 <- cutree(hc, k=nc+1)</pre>
clall <- cbind(cl1,cl2)</pre>
res[nc-min_nc+1,2] <- H <- index.H(data_ratio,clall,centrotypes="centroids")</pre>
if ((res[nc-min_nc+1, 2]<10) && (!found)){
       nc1 <- nc
       min <- H
       clopt <- cl1</pre>
   found <- TRUE
}
if (found)
print(paste("minimal nc for H<=10 equals",nc1,"for H=",min))</pre>
print("clustering for minimal nc where H<=10")</pre>
print(clopt)
}else
print("Clustering not found with H<=10")</pre>
write.table(res,file="H_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="H",xaxt="n")
abline(h=10, untf=FALSE)
axis(1, c(min_nc:max_nc))
# Example 3
library(clusterSim)
```

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```
data(data_ratio)
md <- dist(data_ratio, method="manhattan")</pre>
# nc - number_of_clusters
min_nc=1
max_nc=20
min <- 0
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc</pre>
found <- FALSE
clusters <- NULL
for (nc in min_nc:max_nc)
print(nc)
hc <- hclust(md, method="complete")</pre>
cl1 <- cutree(hc, k=nc)</pre>
cl2 <- cutree(hc, k=nc+1)</pre>
clall <- cbind(cl1,cl2)</pre>
res[nc-min_nc+1,2] <- H <- index.H(data_ratio,clall,d=md,centrotypes="medoids")</pre>
if ((res[nc-min_nc+1, 2]<10) && (!found)){
       nc1 <- nc
       min <- H
       clopt <- cl1</pre>
   found <- TRUE
}
}
if (found)
print(paste("minimal nc for H<=10 equals",nc1,"for H=",min))</pre>
print("clustering for minimal nc where H<=10")</pre>
print(clopt)
}else
print("Clustering not found with H<=10")</pre>
write.table(res,file="H_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="H",xaxt="n")
abline(h=10, untf=FALSE)
axis(1, c(min_nc:max_nc))
```

index.KL

Calculates Krzanowski-Lai index

Description

Calculates Krzanowski-Lai index

Usage

```
index.KL (x,clall,d=NULL,centrotypes="centroids")
```

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Arguments

x data

clall Three vectors of integers indicating the cluster to which each object is allocated

in partition of n objects into u-1, u, and u+1 clusters

d optional distance matrix, used for calculations if centrotypes="medoids"

centrotypes "centroids" or "medoids"

Details

See file ../doc/indexKL_details.pdf for further details

Value

Krzanowski-Lai index

Author(s)

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References

Krzanowski, W.J., Lai, Y.T. (1988), A criterion for determining the number of groups in a data set using sum of squares clustering, "Biometrics", 44, 23-34.

Milligan, G.W., Cooper, M.C. (1985), An examination of procedures of determining the number of cluster in a data set, "Psychometrika", vol. 50, no. 2, 159-179.

Tibshirani, R., Walther, G., Hastie, T. (2001), *Estimating the number of clusters in a data set via the gap statistic*, "Journal of the Royal Statistical Society", ser. B, vol. 63, part 2, 411-423.

See Also

```
index.G1, index.G2, index.G3, index.S, index.H, index.Gap, index.DB
```

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1<-pam(data_ratio,4)
cl2<-pam(data_ratio,5)
cl3<-pam(data_ratio,6)
clall<-cbind(cl1$clustering,cl2$clustering,cl3$clustering)
index.KL(data_ratio,clall)
# Example 2
library(clusterSim)
data(data_ratio)</pre>
```

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```
md <- dist(data_ratio, method="manhattan")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=15
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc</pre>
clusters <- NULL
for (nc in min_nc:max_nc)
  if(nc-1==1){
    clustering1<-rep(1,nrow(data_ratio))</pre>
  else{
    clustering1 <- pam(md, nc-1, diss=TRUE)$clustering</pre>
  clustering2 <- pam(md, nc, diss=TRUE)$clustering</pre>
  clustering3 <- pam(md, nc+1, diss=TRUE)$clustering</pre>
  clall<- cbind(clustering1, clustering2, clustering3)</pre>
  res[nc-min_nc+1,2] <- KL <- index.KL(data_ratio,clall,centrotypes="centroids")</pre>
  clusters <- rbind(clusters, clustering2)</pre>
}
print(paste("max KL for",(min_nc:max_nc)[which.max(res[,2])],"clusters=",max(res[,2])))
print("clustering for max KL")
print(clusters[which.max(res[,2]),])
write.table(res,file="KL_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="KL",xaxt="n")
axis(1, c(min_nc:max_nc))
# Example 3
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="manhattan")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=15
res <- array(0, c(max_nc-min_nc+1, 2))</pre>
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  if(nc-1==1){
    clustering1<-rep(1,nrow(data_ratio))</pre>
  else{
    clustering1 <- pam(md, nc-1, diss=TRUE)$clustering</pre>
  clustering2 <- pam(md, nc, diss=TRUE)$clustering</pre>
  clustering3 <- pam(md, nc+1, diss=TRUE)$clustering</pre>
  clall<- cbind(clustering1, clustering2, clustering3)</pre>
  res[nc-min_nc+1,2] <- KL <- index.KL(data_ratio,clall,d=md,centrotypes="medoids")</pre>
  clusters <- rbind(clusters, clustering2)</pre>
print(paste("max KL for",(min_nc:max_nc)[which.max(res[,2])],"clusters=",max(res[,2])))
```

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```
print("clustering for max KL")
print(clusters[which.max(res[,2]),])
write.table(res,file="KL_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="KL",xaxt="n")
axis(1, c(min_nc:max_nc))
```

index.S

Calculates Rousseeuw's Silhouette internal cluster quality index

Description

Calculates Rousseeuw's Silhouette internal cluster quality index

Usage

```
index.S(d,cl,singleObject=0)
```

Arguments

d 'dist' object

cl A vector of integers indicating the cluster to which each object is allocated

singleObject 0 - s(i)=0 or 1 - s(i)=1. When cluster contains a single object, it is unclear how

a(i) of Silhouette index should be defined (see Kaufman & Rousseeuw (1990),

p. 85).

Details

See file \\$R_HOME\library\clusterSim\pdf\indexS_details.pdf for further details

Value

calculated Silhouette index

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References

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wroclaw, 342-343, erratum.

Kaufman, L., Rousseeuw, P.J. (1990), Finding groups in data: an introduction to cluster analysis, Wiley, New York, 83-88.

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See Also

```
index.G1, index.G2, index.G3, index.KL, index.H, index.Gap, index.DB
```

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
d <- dist.GDM(data_ratio)</pre>
c \leftarrow pam(d, 5, diss = TRUE)
icq <- index.S(d,c$clustering)</pre>
print(icq)
# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="manhattan")</pre>
# nc - number_of_clusters
min_nc=2
max_nc=20
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
cl2 <- pam(md, nc, diss=TRUE)</pre>
res[nc-min_nc+1, 2] <- S <- index.S(md,cl2$cluster)</pre>
clusters <- rbind(clusters, cl2$cluster)</pre>
print(paste("max S for",(min_nc:max_nc)[which.max(res[,2])],"clusters=",max(res[,2])))
print("clustering for max S")
print(clusters[which.max(res[,2]),])
write.table(res,file="S_res.csv",sep=";",dec=",",row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="S",xaxt="n")
axis(1, c(min_nc:max_nc))
```

initial.Centers

Calculation of initial clusters centers for k-means like alghoritms

Description

Function calculates initial clusters centers for k-means like alghoritms with the following alghoritm (similar to SPSS QuickCluster function)

- (a) if the distance between x_k and its closest cluster center is greater than the distance between the two closest centers $(M_m \text{ and } M_n)$, then x_k replaces either M_m or M_n , whichever is closer to x_k .
- (b) If x_k does not replace a cluster initial center in (a), a second test is made: If that distance d_q greater than the distance between M_q and its closest M_i , then x_k replaces M_q .

where:

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```
M_i - initial center of i-th cluster x_k - vector of k-th observation d(...,...) - Euclidean distance d_{mn} = min_{ij}d(M_i,M_j) d_q = min_id(x_k,M_i)
```

Usage

```
initial.Centers(x, k)
```

Arguments

x matrix or dataset

k number of initial cluster centers

Value

Numbers of objects choosen as initial cluster centers

Author(s)

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References

Hartigan, J. (1975), Clustering algorithms, Wiley, New York.

See Also

```
cluster.Sim
```

```
#Example 1 (numbers of objects choosen as initial cluster centers)
library(clusterSim)
data(data_ratio)
ic <- initial.Centers(data_ratio, 10)
print(ic)

#Example 2 (application with kmeans algorithm)
library(clusterSim)
data(data_ratio)
kmeans(data_ratio,data_ratio[initial.Centers(data_ratio, 10),])</pre>
```

ordinalToMetric 47

ordinalToMetric	Reinforcing measurement scale for ordinal data	

Description

Reinforcing measurement scale for ordinal data (ordinal to metric scale)

Usage

```
ordinalToMetric(data, scaleType="o", patternCoordinates)
```

Arguments

data matrix or dataset

scaleType "o" - variables measured on ordinal scale, "m" - variables measured on metric

scale, "o/m" - vector with mixed variables - e.g. c("o","m","m","o","o","m")

patternCoordinates

vector containing pattern coordinates c(...) given by the reaseracher for data (for metric variables - NA, for ordinal variables - one of the categories for each

ordinal variable (e.g. maximum category))

Details

```
See file ../doc/ordinalToMetric_details.pdf for further details
```

Value

pdata raw (primary) data matrix

tdata data matrix after transformation of ordinal variables into metric variables

cpattern vector containing pattern coordinates

Author(s)

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Walesiak, M. (1993), Statystyczna analiza wielowymiarowa w badaniach marketingowych [Multivariate statistical analysis in marketing research]. Wroclaw University of Economics, Research Papers no. 654.

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Walesiak, M. (1999), *Distance Measure for Ordinal Data*, "Argumenta Oeconomica", No. 2 (8), 167-173.

Walesiak, M. (2011), *Uogólniona miara odległości GDM w statystycznej analizie wielowymiarowej z wykorzystaniem programu R [The Generalized Distance Measure GDM in multivariate statistical analysis with R]*, Wydawnictwo Uniwersytetu Ekonomicznego, Wroclaw.

Walesiak, M. (2014), Wzmacnianie skali pomiaru dla danych porządkowych w statystycznej analizie wielowymiarowej [Reinforcing measurement scale for ordinal data in multivariate statistical analysis], Taksonomia 22, Prace Naukowe Uniwersytetu Ekonomicznego we Wrocławiu no. 327, 60-68.

See Also

dist.GDM

Examples

```
# Example 1
library(clusterSim)
data(data_patternGDM2)
res1<-ordinalToMetric(data_patternGDM2,scaleType="o",patternCoordinates=c(5,4,3,1,1,3))
print(res1)

# Example 2
library(clusterSim)
data(data_patternGDM2)
res2<-ordinalToMetric(data_patternGDM2,scaleType="o",patternCoordinates=c(5,4,3,4,2,4))
print(res2)</pre>
```

pattern.GDM1

An application of GDM1 distance for metric data to compute the distances of objects from the pattern object (upper or lower)

Description

An application of GDM1 distance for metric data to compute the distances of objects from the upper (ideal point co-ordinates) or lower (anti-ideal point co-ordinates) pattern object

Usage

```
pattern.GDM1(data, performanceVariable, scaleType="i",
nomOptValues=NULL, weightsType="equal", weights=NULL,
normalization="n0", patternType="upper",
patternCoordinates="dataBounds", patternManual=NULL,
nominalTransfMethod=NULL)
```

pattern.GDM1 49

Arguments

scaleType

data matrix or dataset

performanceVariable

vector containing three types of performance variables:

s for stimulants where higher value means better performance d for destimulants where low values indicate better performance

n for nominants where the best value is implied. Object performance is posi-

tively assessed if the measure has implied value

"i" - variables measured on interval scale, "r" - variables measured on ratio scale,

"r/i" - vector with mixed variables

nomOptValues vector containing optimal values for nominant variables and NA values for stim-

ulants and destimulants. If performanceVariable do not contain nominant

variables this nomOptValues may be set to NULL

weightsType equal or different1 or different2

"equal" - equal weights

"different1" - vector of different weights should satisfy conditions: each weight takes value from interval [0; 1] and sum of weights equals one

"different2" - vector of different weights should satisfy conditions: each weight takes value from interval [0; m] and sum of weights equals m (m - the number

of variables)

normalization normalization formulas as in data. Normalization function

weights vector of weights

patternType "upper" - ideal point co-ordinates consists of the best variables' values

"lower" - anti-ideal point co-ordinates consists of the worst variables' values

patternCoordinates

"dataBounds" - pattern should be calculated as following: "upper" pattern (maximum for stimulants, minimum for destimulants), "lower" pattern (minimum for stimulants, maximum for destimulants)

"manual" - pattern should be given in patternManual variable

patternManual Pattern co-ordinates contain:

real numbers

"min" - for minimal value of variable

"max" - for maximal value of variable

nominalTransfMethod

method of transformation of nominant to stimulant variable:

"q" - quotient transformation

"d" - difference transformation

Details

See file .../doc/patternGDM1_details.pdf for further details

50 pattern.GDM1

Value

pdata raw (primary) data matrix

tdata data matrix after transformation of nominant variables (with pattern in last row)

data matrix after normalization (with pattern in last row)

distances GDM1 distances from pattern object

sortedDistances

sorted GDM1 distances from pattern object

Author(s)

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References

Jajuga, K., Walesiak, M., Bak, A. (2003), *On the general distance measure*, In: M. Schwaiger, O. Opitz (Eds.), Exploratory data analysis in empirical research, Springer-Verlag, Berlin, Heidelberg, 104-109.

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Walesiak, M. (2006), *Uogólniona miara odleglosci w statystycznej analizie wielowymiarowej [The Generalized Distance Measure in multivariate statistical analysis]*, Wydawnictwo AE, Wroclaw.

Walesiak, M. (2011), Uogólniona miara odległości GDM w statystycznej analizie wielowymiarowej z wykorzystaniem programu R [The Generalized Distance Measure GDM in multivariate statistical analysis with R], Wydawnictwo UE, Wroclaw.

See Also

dist.GDM,data.Normalization

```
# Example 1
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n4",patternType<-"lower",patternCoordinates<-"manual",
patternManual<-c("min","min","min","min","min","min","max","max","max","min"),
nominalTransfMethod <-NULL)
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),xaxt="n",</pre>
```

pattern.GDM2 51

```
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
# Example 2
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n2",patternType<-"upper",</pre>
patternCoordinates<-"dataBounds",patternManual<-NULL,
nominalTransfMethod<-NULL)
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p),xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
# Example 3
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
scaleType="r",nomOptValues=NULL,weightsType<-"different2",
weights=c(1.1,1.15,1.15,1.1,1.1,0.7,0.7,1.2,0.8,1.0),
normalization<-"n6",patternType<-"upper",patternCoordinates<-"manual",</pre>
patternManual<-c(100,100,100,100,100,"max","min","min","max","max"),</pre>
nominalTransfMethod <-NULL)</pre>
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p),xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p), max(gdm_p)), xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
```

pattern.GDM2

An application of GDM2 distance for ordinal data to compute the distances of objects from the pattern object (upper or lower)

Description

An application of GDM2 distance for ordinal data to compute the distances of objects from the upper (ideal point co-ordinates) or lower (anti-ideal point co-ordinates) pattern object

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Usage

```
pattern.GDM2(data, performanceVariable, nomOptValues=NULL,
weightsType="equal", weights=NULL, patternType="upper",
patternCoordinates="dataBounds", patternManual=NULL,
nominalTransfMethod=NULL)
```

Arguments

data matrix or dataset

performanceVariable

vector containing three types of performance variables:

s for stimulants where higher value means better performance d for destimulants where low values indicate better performance

n for nominants where the best value is implied. Object performance is posi-

tively assessed if the measure has implied value

nomOptValues vector containing optimal values for nominant variables and NA values for stim-

ulants and destimulants. If performanceVariable do not contain nominant

variables this nomOptValues may be set to NULL

weightsType equal or different1 or different2

"equal" - equal weights

"different1" - vector of different weights should satisfy conditions: each weight

takes value from interval [0; 1] and sum of weights equals one

"different2" - vector of different weights should satisfy conditions: each weight takes value from interval [0; m] and sum of weights equals m (m - the number

of variables)

weights vector of weights

patternType "upper" - ideal point co-ordinates consists of the best variables' values

"lower" - anti-ideal point co-ordinates consists of the worst variables' values

patternCoordinates

"dataBounds" - pattern should be calculated as following: "upper" pattern (maximum for stimulants, minimum for destimulants, nominal value for nominants),

"lower" pattern (minimum for stimulants, maximum for destimulants)

"manual" - pattern should be given in patternManual variable

patternManual Pattern co-ordinates contain:

real numbers

"min" - for minimal value of variable

"max" - for maximal value of variable

"nom" - for nominal value of variable (for upper pattern only - given in nomOptValues

nominalTransfMethod

method of transformation of nominant to destimulant variable for patternType="lower":

"database" - for each nominant separately GDM2 distance is calculated between each nominant observation (with repetitions - all variable values are used in calculation) and nominal value. Next the variable observations are replaced by those distances

pattern.GDM2 53

"symmetrical" - for each nominant separately GDM2 distance is calculated between each nominant observation (without repetition - each observation is used once) and nominal value. Next the variable observations are replaced by those distances

Details

See file ../doc/patternGDM2_details.pdf for further details

Value

pdata raw (primary) data matrix

data matrix after transformation of nominant variables (with pattern in last row)

distances GDM2 distances from pattern object

sortedDistances

sorted GDM2 distances from pattern object

Author(s)

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References

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Walesiak, M. (2006), *Uogolniona miara odleglosci w statystycznej analizie wielowymiarowej [The Generalized Distance Measure in multivariate statistical analysis]*, Wydawnictwo AE, Wroclaw.

Walesiak, M. (2011), *Uogólniona miara odległości GDM w statystycznej analizie wielowymiarowej z wykorzystaniem programu R [The Generalized Distance Measure GDM in multivariate statistical analysis with R]*, Wydawnictwo UE, Wroclaw.

See Also

dist.GDM

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Examples

```
# Example 1
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="lower", patternCoordinates="manual",
patternManual=c("min", "min", 0, 5, "max", "max"),
nominalTransfMethod="symmetrical")
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
# Example 2
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="upper", patternCoordinates="dataBounds",
patternManual=NULL, nominalTransfMethod="database")
print(res)
gdm_p<-res$distances</pre>
plot(cbind(gdm_p,gdm_p), xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
```

plotCategorial

Plot categorial data on a scatterplot matrix

Description

Plot categorial data on a scatterplot matrix (optionally with clusters)

Usage

```
plotCategorial(x, pairsofVar=NULL, cl=NULL, clColors=NULL,...)
```

Arguments

x data matrix (rows correspond to observations and columns correspond to variables)

plotCategorial3d 55

pairsofVar	pairs of variables - all variables (pairsofVar=NULL) or selected variables, e.g. pairsofVar=c(1,3,4)
cl	cluster membership vector
clColors	The colors of clusters. The colors are given arbitrary (clColors=TRUE) or by hand, e.g. clColors=c("red","blue","green"). The number of colors equals the number of clusters
	Arguments to be passed to methods, such as graphical parameters (see par).

Author(s)

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See Also

```
plotCategorial3d, colors, pairs
```

Examples

```
# Example 1
library(clusterSim)
data(data_ordinal)
plotCategorial(data_ordinal, pairsofVar=c(1,3,4,9), cl=NULL,
clColors = NULL)

# Example 2
library(clusterSim)
grnd <- cluster.Gen(50,model=5,dataType="o",numCategories=5)
plotCategorial(grnd$data, pairsofVar=NULL, cl=grnd$clusters,
clColors=TRUE)

# Example 3
library(clusterSim)
grnd<-cluster.Gen(50,model=4,dataType="o",numCategories=7, numNoisyVar=2)
plotCategorial(grnd$data, pairsofVar=NULL, cl=grnd$clusters,
clColors = c("red", "blue", "green"))</pre>
```

plotCategorial3d

Plot categorial data with three-dimensional plots

Description

Plot categorial data with three-dimensional plots (optionally with clusters)

Usage

```
plotCategorial3d(x, tripleofVar=c(1,2,3), cl=NULL, clColors=NULL,...)
```

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Arguments

X	data matrix (rows correspond to observations and columns correspond to variables)
tripleofVar	triple of variables - vector of the number of variables, e.g. tripleofVar = c(1, 3, 4)
cl	cluster membership vector
clColors	The colors of clusters. The colors are given arbitrary (clColors=TRUE) or by hand, e.g. clColors=c("red","blue","green"). The number of colors equals the number of clusters
	Arguments to be passed to methods, such as graphical parameters (see par).

Author(s)

Marek Walesiak <marek.walesiak@ue.wroc.pl>, Andrzej Dudek <andrzej.dudek@ue.wroc.pl> Department of Econometrics and Computer Science, University of Economics, Wroclaw, Poland http://keii.ue.wroc.pl/clusterSim

See Also

```
plotCategorial,colors
```

```
# These examples do not run on Mac_OS-X. We're working to fix them
# They run quite well on Windows and Linux in meantime
# Example 1
#library(clusterSim)
#data(data_ordinal)
#plotCategorial3d(data_ordinal, tripleofVar=c(1,3,9), cl=NULL,
#clColors=NULL)
# Example 2
#library(clusterSim)
#grnd <- cluster.Gen(50,model=5,dataType="o",numCategories=5)</pre>
#plotCategorial3d(grnd$data, tripleofVar=c(1,2,3), cl=grnd$clusters,
#clColors=TRUE)
# Example 3
#library(clusterSim)
#grnd <- cluster.Gen(50, model=4, dataType="o", numCategories=7, numNoisyVar=2)</pre>
#plotCategorial3d(grnd$data, tripleofVar=c(1,2,4), cl=grnd$clusters,
#clColors=c("red","blue","green"))
```

plotInterval 57

plotInterval	Plot symbolic interval-valued data on a scatterplot matrix	

Description

Plot symbolic interval-valued data on a scatterplot matrix (optionally with clusters)

Usage

```
plotInterval(x, pairsofsVar=NULL, cl=NULL, clColors=NULL,...)
```

Arguments

X	symbolic interval-valued data
pairsofsVar	pairs of symbolic interval variables - all variables (pairsofsVar=NULL) or selected variables, e.g. pairsofsVar=c(1,3,4)
cl	cluster membership vector
clColors	The colors of clusters. The colors are given arbitrary (clColors=TRUE) or by hand, e.g. clColors=c("red","blue","green"). The number of colors equals the number of clusters
	Arguments to be passed to methods, such as graphical parameters (see par).

Author(s)

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See Also

```
plotCategorial,plotCategorial3d, colors, pairs
```

```
# Example 1
library(clusterSim)
data(data_symbolic)
plotInterval(data_symbolic, pairsofsVar=c(1,3,4,6), cl=NULL,
clColors=NULL)

# Example 2
library(clusterSim)
grnd <- cluster.Gen(60, model=5, dataType="s", numNoisyVar=1,
numOutliers=10, rangeOutliers=c(1,5))
grnd$clusters[grnd$clusters==0] <- max(grnd$clusters)+1
# To colour outliers
plotInterval(grnd$data, pairsofsVar=NULL, cl=grnd$clusters,</pre>
```

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```
clColors=TRUE)

# Example 3
library(clusterSim)
grnd <- cluster.Gen(50, model=4, dataType="s", numNoisyVar=2,
numOutliers=10, rangeOutliers=c(1,4))
grnd$clusters[grnd$clusters==0] <- max(grnd$clusters)+1
# To colour outliers
plotInterval(grnd$data, pairsofsVar=NULL, cl=grnd$clusters,
clColors=c("red","blue","green","yellow"))</pre>
```

replication.Mod

Modification of replication analysis for cluster validation

Description

Modification of replication analysis for cluster validation

Usage

```
replication.Mod(x, v="m", u=2, centrotypes="centroids", normalization=NULL, distance=NULL, method="kmeans", S=10, fixedAsample=NULL)
```

Arguments

X	data matrix
V	type of data: metric ("r" - ratio, "i" - interval, "m" - mixed), nonmetric ("o" - ordinal, "n" - multi-state nominal, "b" - binary)
u	number of clusters given arbitrary
centrotypes	"centroids" or "medoids"
normalization	optional, normalization formulas for metric data (normalization by variable):
	for ratio data: "n0" - without normalization, "n6" - (x/sd), "n6a" - (x/mad), "n7" - (x/range), "n8" - (x/max), "n9" - (x/mean), "n9a" - (x/median), "n10" - (x/sum), "n11" - x/sqrt(SSQ)
	for interval or mixed data: "n0" - without normalization, "n1" - (x-mean)/sd, "n2" - (x-median)/mad, "n3" - (x-mean)/range, "n3a" - positional unitization (x-median)/range, "n4" - (x-min)/range, "n5" - (x-mean)/max[abs(x-mean)], "n5a" - (x-median)/max[abs(x-median)], "n12" - normalization (x - mean)/(sum(x - mean)^2)^0.5, "n12a" - positional normalization (x - median)/(sum(x - median)^2)^0.5, "n13" - normalization with zero being the central point ((x-midrange)/(range/2))
distance	distance measures NULL for "kmeans" method (based on data matrix), for ratio data: "d1" - Manhattan, "d2" - Euclidean, "d3" - Chebychev (max), "d4" - squared Euclidean, "d5" - GDM1, "d6" - Canberra, "d7" - Bray-Curtis

for interval or mixed (ratio & interval) data: "d1", "d2", "d3", "d4", "d5"

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for ordinal data: "d8" - GDM2

for multi-state nominal: "d9" - Sokal & Michener

for binary data: "b1" = Jaccard; "b2" = Sokal & Michener; "b3" = Sokal & Sneath (1); "b4" = Rogers & Tanimoto; "b5" = Czekanowski; "b6" = Gower & Legendre (1); "b7" = Ochiai; "b8" = Sokal & Sneath (2); "b9" = Phi of Pearson;

"b10" = Gower & Legendre (2)

method clustering method: "kmeans" (default), "single", "complete", "average", "mc-

quitty", "median", "centroid", "ward.D", "ward.D2", "pam", "diana"

S the number of simulations used to compute mean corrected Rand index

fixedAsample if NULL A sample is generated randomly, otherwise this parameter contains

object numbers arbitrarily assigned to A sample

Details

See file ../doc/replication.Mod_details.pdf for further details

Value

Α	3-dimensional array containing data matrices for A sample of objects in each
	simulation (first dimension represents simulation number, second - object num-
	ber, third - variable number)
В	3-dimensional array containing data matrices for B sample of objects in each

simulation (first dimension represents simulation number, second - object number, third - variable number)

centroid 3-dimensional array containing centroids of u clusters for A sample of objects in

each simulation (first dimension represents simulation number, second - cluster

number, third - variable number)

medoid 3-dimensional array containing matrices of observations on u representative ob-

> jects (medoids) for A sample of objects in each simulation (first dimension represents simulation number, second - cluster number, third - variable number)

2-dimensional array containing cluster numbers for A sample of objects in each clusteringA

simulation (first dimension represents simulation number, second - object num-

ber)

clusteringB 2-dimensional array containing cluster numbers for B sample of objects in each

simulation (first dimension represents simulation number, second - object num-

clusteringBB 2-dimensional array containing cluster numbers for B sample of objects in each

simulation according to 4 step of replication analysis procedure (first dimension

represents simulation number, second - object number)

cRand value of mean corrected Rand index for S simulations

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See Also

```
cluster.Sim, hclust, kmeans, dist, dist.BC, dist.SM, dist.GDM,
data.Normalization
```

Examples

```
library(clusterSim)
data(data_ratio)
w <- replication.Mod(data_ratio, u=5, S=10)
print(w)

library(clusterSim)
data(data_binary)
replication.Mod(data_binary,"b", u=2, "medoids", NULL,"b1", "pam", fixedAsample=c(1,3,6,7))</pre>
```

shapes.blocks3d

Generation of data set containing two clusters with untypical shapes (cube divided into two parts by main diagonal plane)

Description

Generation of data set containing two clusters with untypical shapes (cube starting at point (0,0,0) divided into two parts by main diagonal plane)

Usage

```
shapes.blocks3d(numObjects=180,shapesUnitSize=0.5, shape2coordinateX=1.2,
shape2coordinateY=1.2,shape2coordinateZ=1.2, outputCsv="", outputCsv2="",
outputColNames=TRUE, outputRowNames=TRUE)
```

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Arguments

numObjects number of objects in each cluster - positive integer value or vector with length=2

shapesUnitSize length of one unit for shape (maximal heigth, width and depth of shape is

2*shapesUnitSize)

shape2coordinateX

maximal value for second shape in first (X) dimension

shape2coordinateY

maximal value for second shape in second (Y) dimension

shape2coordinateZ

maximal value for second shape in third (Z) dimension

outputCsv optional, name of csv file with generated data (first column contains id, second

- number of cluster and others - data)

outputCsv2 optional, name of csv (a comma as decimal point and a semicolon as field sep-

arator) file with generated data (first column contains id, second - number of

cluster and others - data)

outputColNames outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2

parameters) contains first row with column names

outputRowNames outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2

parameters) contains a vector of row names

Value

clusters cluster number for each object

data generated data - matrix with objects in rows and variables in columns

Author(s)

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See Also

shapes.worms,shapes.circles2,shapes.circles3,shapes.bulls.eye,shapes.two.moon

```
library(clusterSim)
library(rgl)
sb3d<-shapes.blocks3d(300,1,3,3,3)
plot3d(sb3d$data,col=rainbow(2)[sb3d$clusters])</pre>
```

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	shapes.circles2	Generation of data set containing two clusters with untypical ring shapes (circles)
--	-----------------	---

Description

Generation of data set containing two clusters with untypical ring shapes. For each point first random radius r from given interval is generated then random angle alpha and finally the coordinates of point are calculated as (r*cos(alpha),r*sin(alpha)). For bull's eye data set second shape is filled circle (r starts from 0)

Usage

shapes.circles2(numObjects=180, shape1rFrom=0.75, shape1rTo=0.9, shape2rFrom=0.35, shape2rTo=0.5, outputCsv="", outputCsv2="", outputColNames=TRUE, outputRowNames=TRUE) shapes.bulls.eye(numObjects=180, shape1rFrom=0.75, shape1rTo=0.95, shape2rTo=0.45, outputCsv="", outputCsv2="", outputColNames=TRUE, outputRowNames=TRUE)

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2,
shape1rFrom	minimal value of radius for first ring
shape1rTo	maximal value of radius for first ring
shape2rFrom	minimal value of radius for second ring
shape2rTo	maximal value of radius for second ring
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputCo1Names=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	$output RowNames = TRUE\ indicates\ that\ output\ file\ (given\ by\ outputCsv\ and\ outputCsv2\ parameters)\ contains\ a\ vector\ of\ row\ names$

Value

clusters cluster number for each object

data generated data - matrix with objects in rows and variables in columns

Author(s)

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See Also

shapes.worms,shapes.circles3,shapes.bulls.eye,shapes.two.moon,shapes.blocks3d

Examples

```
#Example1
library(clusterSim)
sc2<-shapes.circles2(180)
plot(sc2$data,col=rainbow(2)[sc2$clusters])
#Example2
library(clusterSim)
sbe<-shapes.bulls.eye(numObjects=c(120,60))
plot(sbe$data,col=rainbow(2)[sbe$clusters])</pre>
```

shapes.circles3

Generation of data set containing three clusters with untypical ring shapes (circles)

Description

Generation of data set containing three clusters with untypical ring shapes. For each point first random radius r from given interval is generated then random angle alpha and finally the coordinates of point are calculated as (r*cos(alpha),r*sin(alpha))

Usage

```
shapes.circles3(numObjects=180,shape1rFrom=0.15,shape1rTo=0.3,
shape2rFrom=0.55,shape2rTo=0.7,shape3rFrom=1.15,shape3rTo=1.3,
outputCsv="", outputCsv2="", outputColNames=TRUE, outputRowNames=TRUE)
```

Arguments

number of objects in each cluster - positive integer value or vector with length=3,
minimal value of radius for first ring
maximal value of radius for first ring
minimal value of radius for second ring
maximal value of radius for second ring
minimal value of radius for third ring
maximal value of radius for third ring
optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)

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outputColNames outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2

parameters) contains first row with column names

outputRowNames outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2

parameters) contains a vector of row names

Value

clusters cluster number for each object

data generated data - matrix with objects in rows and variables in columns

Author(s)

Marek Walesiak <marek.walesiak@ue.wroc.pl>, Andrzej Dudek <andrzej.dudek@ue.wroc.pl> Department of Econometrics and Computer Science, University of Economics, Wroclaw, Poland http://keii.ue.wroc.pl/clusterSim

See Also

shapes.worms,shapes.circles2,shapes.bulls.eye,shapes.two.moon,shapes.blocks3d

Examples

```
#Example1
library(clusterSim)
sc3a<-shapes.circles3(180)
plot(sc3a$data,col=rainbow(3)[sc3a$clusters])

#Example2
library(clusterSim)
sc3b<-shapes.circles3(numObjects=c(120,180,240))
plot(sc3b$data,col=rainbow(3)[sc3b$clusters])</pre>
```

shapes.two.moon

Generation of data set containing two clusters with untypical shapes (similar to waxing and waning crescent moon)

Description

Generation of data set containing two clusters with untypical shapes (similar to waxing and waning crescent moon). For each point first random radius r from given interval is generated then random angle alpha and finally the coordinates of point are calculated as (a+abs(r*cos(alpha)),r*sin(alpha) for first shape and (-abs(r*cos(alpha)),r*sin(alpha)-b for second shape

Usage

```
shapes.two.moon(numObjects=180,shape1a=-0.4,shape2b=1,shape1rFrom=0.8,
shape1rTo=1.2,shape2rFrom=0.8, shape2rTo=1.2, outputCsv="", outputCsv2="",
outputColNames=TRUE, outputRowNames=TRUE)
```

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Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2,
shape1a	parameter a for first shape
shape2b	parameter b for first shape
shape1rFrom	minimal value of radius for first shape
shape1rTo	maximal value of radius for first shape
shape2rFrom	minimal value of radius for second shape
shape2rTo	maximal value of radius for second shape
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters cluster number for each object

data generated data - matrix with objects in rows and variables in columns

Author(s)

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See Also

shapes.worms, shapes.circles 2, shapes.circles 3, shapes.bulls.eye, shapes.blocks 3d

```
library(clusterSim)
stm<-shapes.two.moon(180)
plot(stm$data,col=rainbow(2)[stm$clusters])</pre>
```

shapes.worms

shapes.worms	Generation of data set containing two clusters with untypical parabolic shapes (worms)

Description

Generation of data set containing two clusters with untypical parabolic shapes (first is given by $y=x^2$, second by $y=-(x-a)^2+b$ with distortion from <-tol,+tol>)

Usage

```
shapes.worms (numObjects=180, shape1x1=-2, shape1x2=2, shape2x1=-0.5, shape2x2=2.5, shape2a=1.5, shape2b=5.5, tol=0.1, outputCsv="", outputCsv2="", outputColNames=TRUE, outputRowNames=TRUE)
```

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2
shape1x1	starting value on abscissa axis for shape 1
shape1x2	end value on abscissa axis for shape 1
shape2x1	starting value on abscissa axis for shape 2
shape2x2	end value on abscissa axis for shape 2
shape2a	parameter a of shape 2
shape2b	parameter b of shape 2
tol	tolerance - each generated point is randomized by adding runif(1,0,tol)
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputCo1Names=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters cluster number for each object

data generated data - matrix with objects in rows and variables in columns

Author(s)

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See Also

shapes.worms,shapes.circles2,shapes.circles3,shapes.bulls.eye,shapes.two.moon,shapes.blocks3d

Examples

```
library(clusterSim)
sw<-shapes.worms(180)
plot(sw$data,col=rainbow(2)[sw$clusters])</pre>
```

speccl

A spectral clustering algorithm

Description

A spectral clustering algorithm. Cluster analysis is performed by embedding the data into the subspace of the eigenvectors of an affinity matrix

Usage

```
speccl(data,nc,distance="GDM1",sigma="automatic",sigma.interval="default",
mod.sample=0.75,R=10,iterations=3,na.action=na.omit,...)
```

Arguments

data	matrix or dataset
nc	the number of clusters
distance	distance function used to calculate affinity matrix: "sEuclidean" - squared Euclidean distance, "euclidean" - Euclidean distance, "manhattan" - city block distance, "maximum" - Chebyshev distance, "canberra" - Lance and Williams Canberra distance, "BC" - Bray-Curtis distance measure for ratio data, "GDM1" - GDM distance for metric data, "GDM2" - GDM distance for ordinal data, "SM" - Sokal-Michener distance measure for nominal variables
sigma	scale parameter used to calculate affinity matrix: sigma="automatic" - an algorithm for searching optimal value of sigma parameter; sigma=200 - value of sigma parameter given by researcher, e.g. 200
sigma.interval	sigma.interval="default" - from zero to square root of sum of all distances in lower triangle of distance matrix for "sEuclidean" and from zero to sum of all distances in lower triangle of distance matrix for other distances; sigma.interval=1000 - from zero to value given by researcher, e.g. 1000
mod.sample	proportion of data to use when estimating sigma (default: 0.75)
R	the number of intervals examined in each step of searching optimal value of sigma parameter algorithm (See/doc/speccl_details.pdf)
iterations	the maximum number of iterations (rounds) allowed in algorithm of searching optimal value of sigma parameter
na.action	the action to perform on NA
• • •	arguments passed to kmeans procedure

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Details

See file .../doc/speccl_details.pdf for further details

Value

returns the lower triangle of the distance matrix

a vector of integers indicating the cluster to which each object is allocated

the number of objects in each cluster

withinss the within-cluster sum of squared distances for each cluster

Ematrix data matrix n x u (n - the number of objects, u - the number of eigenvectors)

Ymatrix normalized data matrix n x u (n - the number of objects, u - the number of eigenvectors)

sigma the value of scale parameter given by searching algorithm

Author(s)

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See Also

```
dist.GDM,kmeans,dist,dist.binary,dist.SM,dist.BC
```

```
# Commented due to long execution time
# Example 1
#library(clusterSim)
#library(mlbench)
#data<-mlbench.spirals(100,1,0.03)
#plot(data)
#x<-data$x
#res1<-speccl(x,nc=2,distance="GDM1",sigma="automatic",</pre>
```

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```
#sigma.interval="default",mod.sample=0.75,R=10,iterations=3)
#clas1<-res1$cluster
#print(data$classes)
#print(clas1)
#cRand<-classAgreement(table(as.numeric(as.vector(data$classes)),</pre>
#res1$clusters))$crand
#print(res1$sigma)
#print(cRand)
# Example 2
#library(clusterSim)
#grnd2<-cluster.Gen(50,model=4,dataType="m",numNoisyVar=1)</pre>
#data<-as.matrix(grnd2$data)</pre>
#colornames<-c("red","blue","green")</pre>
#grnd2$clusters[grnd2$clusters==0]<-length(colornames)</pre>
#plot(grnd2$data,col=colornames[grnd2$clusters])
#us<-nrow(data)*nrow(data)/2
#res2<-speccl(data,nc=3,distance="sEuclidean",sigma="automatic",</pre>
#sigma.interval=us,mod.sample=0.75,R=10,iterations=3)
#cRand<-comparing.Partitions(grnd2$clusters,res2$clusters,type="crand")</pre>
#print(res2$sigma)
#print(cRand)
# Example 3
#library(clusterSim)
#grnd3<-cluster.Gen(40,model=4,dataType="o",numCategories=7)</pre>
#data<-as.matrix(grnd3$data)</pre>
#plotCategorial(grnd3$data,pairsofVar=NULL,cl=grnd3$clusters,
#clColors=c("red","blue","green"))
#res3<-speccl(data,nc=3,distance="GDM2",sigma="automatic",</pre>
#sigma.interval="default",mod.sample=0.75,R=10,iterations=3)
#cRand<-comparing.Partitions(grnd3$clusters,res3$clusters,type="crand")</pre>
#print(res3$sigma)
#print(cRand)
# Example 4
library(clusterSim)
data(data_nominal)
res4<-speccl(data_nominal,nc=4,distance="SM",sigma="automatic",
sigma.interval="default",mod.sample=0.75,R=10,iterations=3)
print(res4)
```

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