

The correct model specification is

$$\begin{aligned}m_0(U, V_0) &= \beta_{01}U + V_0 \\m_1(U, V_1) &= \beta_{11} + \beta_{12}U + V_1,\end{aligned}$$

where  $U \sim \text{Unif}[0, 1]$ ,  $V_0 \sim N(U, 1.5)$ , and  $V_1 \sim N(-U, 1.5)$ . The true values of the MTR coefficients are  $\beta_{01} = 6$ ,  $\beta_{11} = 7$ , and  $\beta_{12} = 8$ . However, the specifications of  $V_0$  and  $V_1$  will make it impossible for the estimator to consistently estimate  $\beta_{01}$  and  $\beta_{12}$  (both estimates will converge towards a value of 7).

The instrument  $Z$  is equal to either 1 or 2, and the true propensity scores are

$$\begin{aligned}\mathbb{P}[D = 1 | Z = 1] &= \phi_1 = 0.4 \\\mathbb{P}[D = 1 | Z = 2] &= \phi_2 = 0.6.\end{aligned}$$

The true ATU is 7.

The model is specified correctly for the estimator. A nonparametric probability model is estimated.

To estimate the coverage probabilities for the confidence intervals constructed in each simulation, I count the number of Monte Carlo simulations for which the coefficient of interest falls within the confidence interval, and then divide by the total number of Monte Carlo simulations (1000 for each sample size).

	N = 100	N = 1000	N = 2000
ATU: avg. estimate	9.036	7.272	7.108
ATU: avg. bootstrap s.e. estimate	104.935	2.568	1.156
ATU: population s.d.	70.172	1.670	1.148
Propensity: avg. coef. estimate, $\phi_1$	0.401	0.401	0.400
Propensity: avg. coef. estimate, $\phi_2$	0.600	0.600	0.599
Propensity: avg. bootstrap s.e., $\phi_1$	0.069	0.022	0.016
Propensity: avg. bootstrap s.e., $\phi_2$	0.069	0.022	0.015
Propensity: population s.d., $\phi_1$	0.069	0.022	0.016
Propensity: population s.d., $\phi_2$	0.071	0.022	0.016
MTR: avg. coef. estimate, $\beta_{01}$	7.047	6.998	7.006
MTR: avg. coef. estimate, $\beta_{11}$	6.091	6.864	6.949
MTR: avg. coef. estimate, $\beta_{12}$	11.041	7.537	7.216
MTR: avg. bootstrap s.e., $\beta_{01}$	0.365	0.112	0.079
MTR: avg. bootstrap s.e., $\beta_{11}$	51.537	1.271	0.574
MTR: avg. bootstrap s.e., $\beta_{12}$	209.883	5.121	2.301
MTR: population s.d., $\beta_{01}$	0.360	0.112	0.081

MTR: population s.d., $\beta_{11}$	34.832	0.828	0.567
MTR: population s.d., $\beta_{12}$	140.327	3.321	2.282
ATU: 90% CI1 (quantile method) coverage prob.	0.923	0.899	0.889
ATU: 95% CI1 (quantile method) coverage prob.	0.951	0.951	0.941
ATU: 90% CI2 (percentile method) coverage prob.	0.939	0.930	0.920
ATU: 95% CI2 (percentile method) coverage prob.	0.950	0.958	0.959
Propensity: 90% CI1 coverage prob., $\phi_1$	0.893	0.902	0.887
Propensity: 90% CI1 coverage prob., $\phi_2$	0.894	0.884	0.882
Propensity: 95% CI1 coverage prob., $\phi_1$	0.941	0.951	0.940
Propensity: 95% CI1 coverage prob., $\phi_2$	0.929	0.944	0.940
Propensity: 90% CI2 coverage prob., $\phi_1$	0.893	0.904	0.888
Propensity: 90% CI2 coverage prob., $\phi_2$	0.896	0.883	0.884
Propensity: 95% CI2 coverage prob., $\phi_1$	0.940	0.951	0.941
Propensity: 95% CI2 coverage prob., $\phi_2$	0.930	0.944	0.942
MTR: 90% CI1 coverage prob., $\beta_{01}$	0.073	0.000	0.000
MTR: 90% CI1 coverage prob., $\beta_{11}$	0.933	0.905	0.896
MTR: 90% CI1 coverage prob., $\beta_{12}$	0.914	0.879	0.855
MTR: 95% CI1 coverage prob., $\beta_{01}$	0.126	0.000	0.000
MTR: 95% CI1 coverage prob., $\beta_{11}$	0.957	0.956	0.946
MTR: 95% CI1 coverage prob., $\beta_{12}$	0.941	0.940	0.921
MTR: 90% CI2 coverage prob., $\beta_{01}$	0.126	0.080	0.066
MTR: 90% CI2 coverage prob., $\beta_{11}$	0.888	0.670	0.598
MTR: 90% CI2 coverage prob., $\beta_{12}$	0.982	0.974	0.964
MTR: 95% CI2 coverage prob., $\beta_{01}$	0.147	0.098	0.080
MTR: 95% CI2 coverage prob., $\beta_{11}$	0.900	0.767	0.684
MTR: 95% CI2 coverage prob., $\beta_{12}$	0.995	0.995	0.988
Bootstraps per simulation	1000.000	1000.000	1000.000
Avg. # bootstraps with collinearities	2.639	0.000	0.000