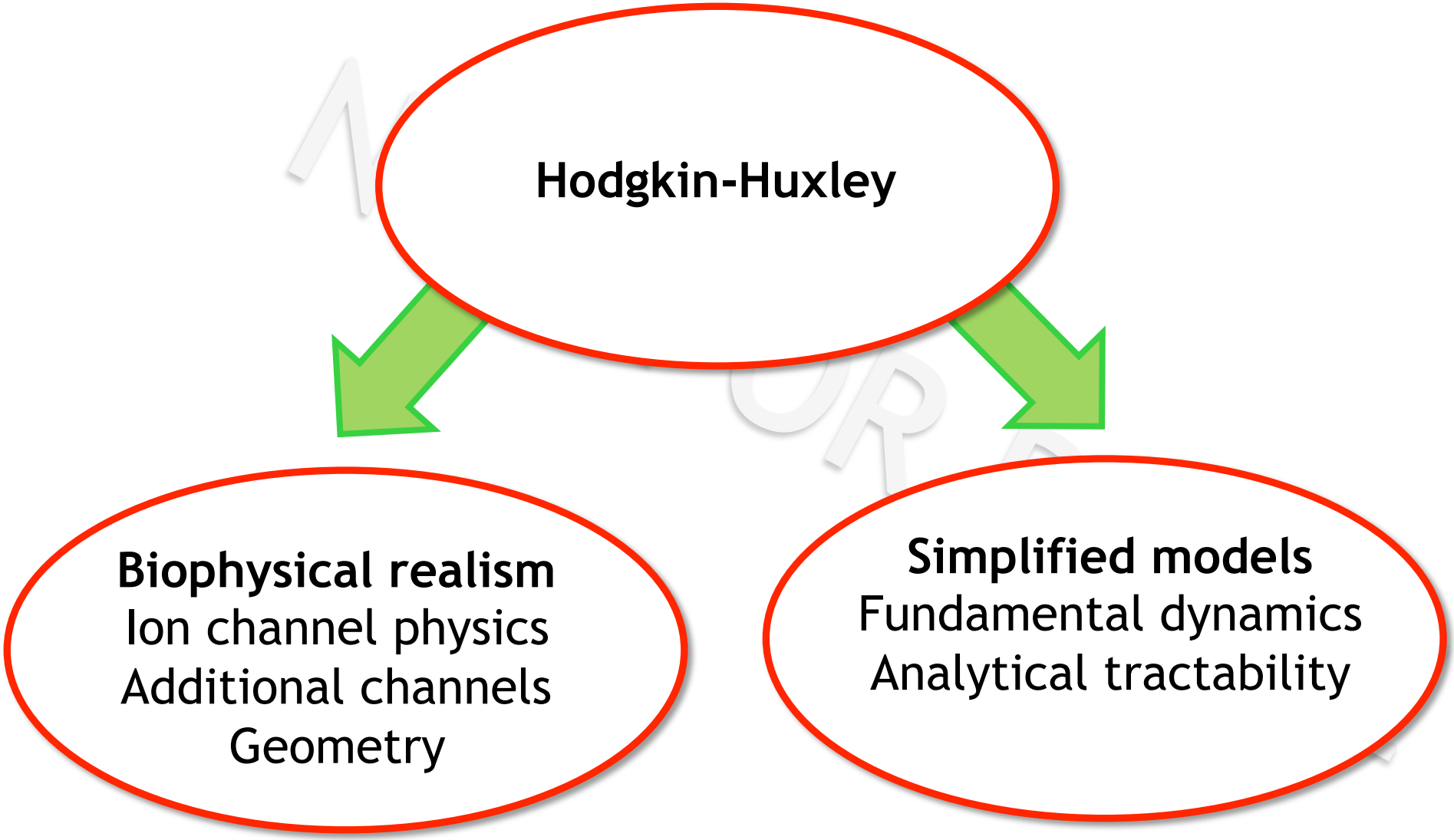
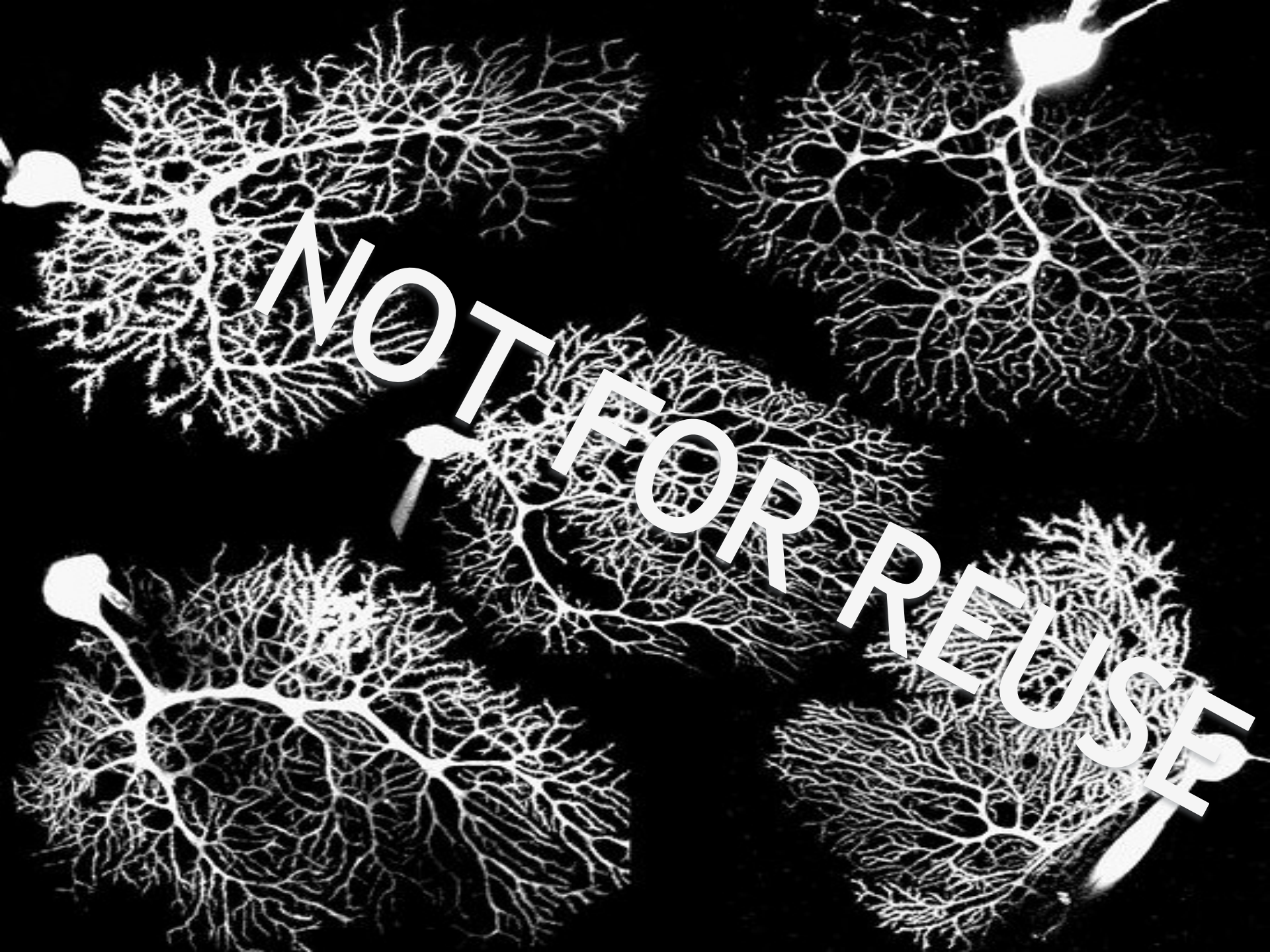
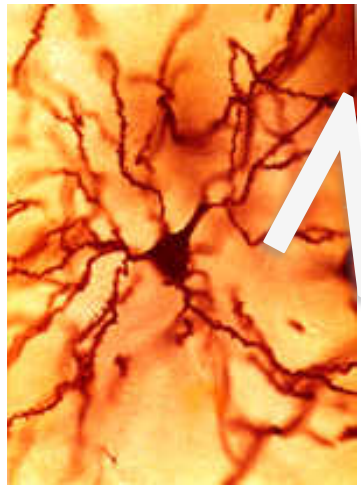
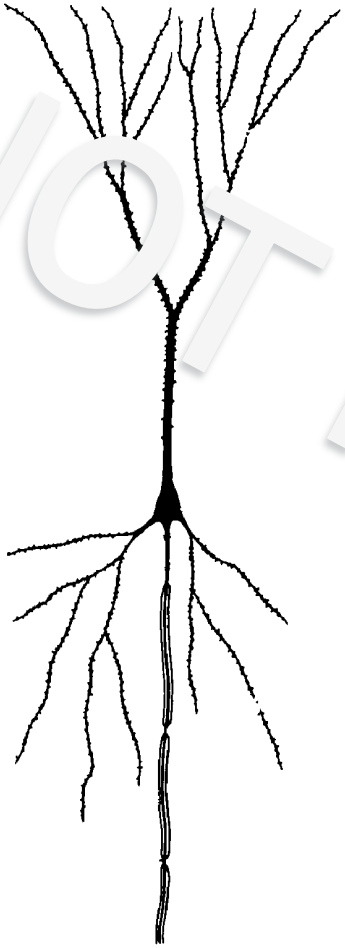
Where to from here?



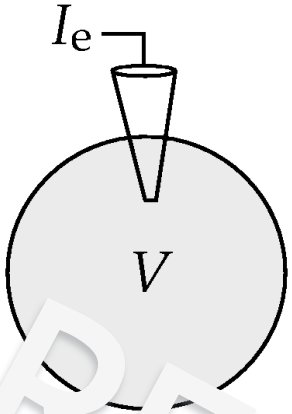

NOT FOR REUSE

Neurons have complicated spatial structures





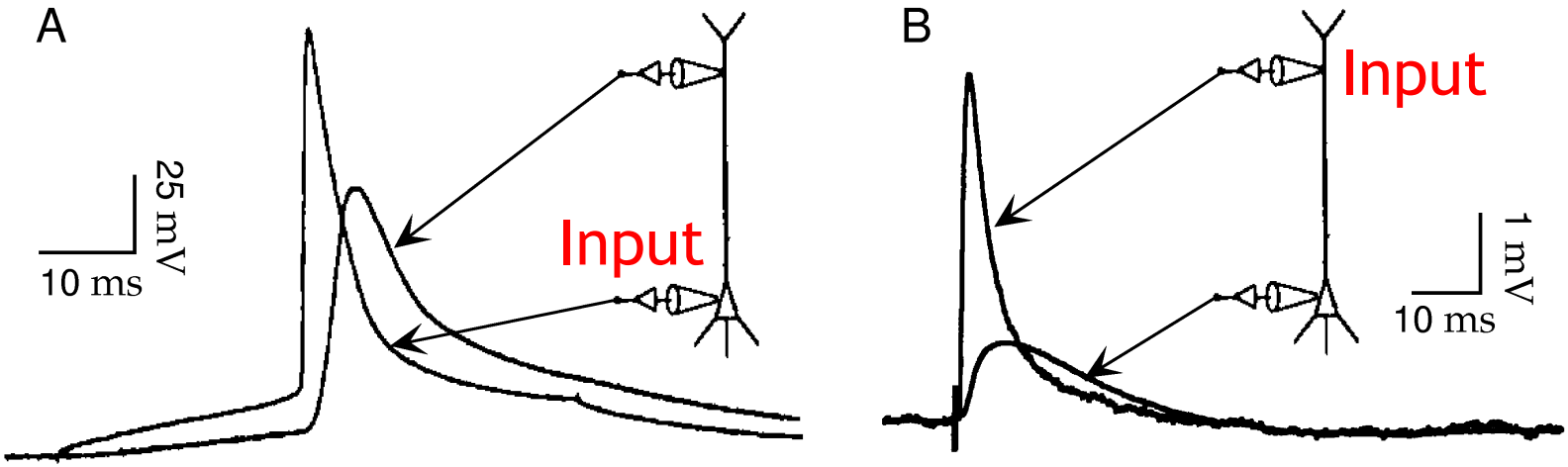
?



Real Neurons

Our Model

Geometry matters!



Inject current at the cell body and record effect in a dendrite

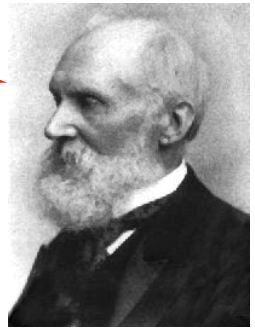
Inject current in a dendrite and record effect at the cell body

Voltage decays with distance in passive membranes (How?)

Dayan and Abbott

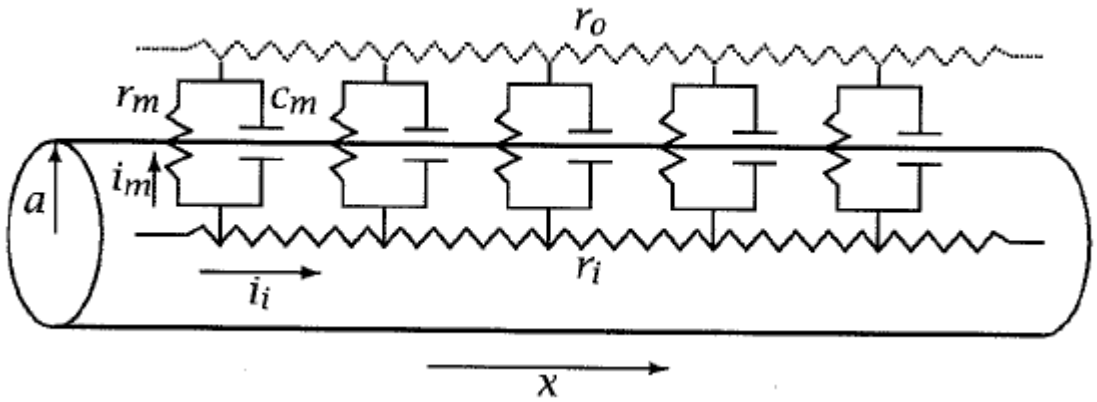
Linear cables

This problem sounds familiar!



Lord Kelvin
(1824-1907)
Developed cable theory for undersea cables

Voltage *V* is a function of *both x and t*



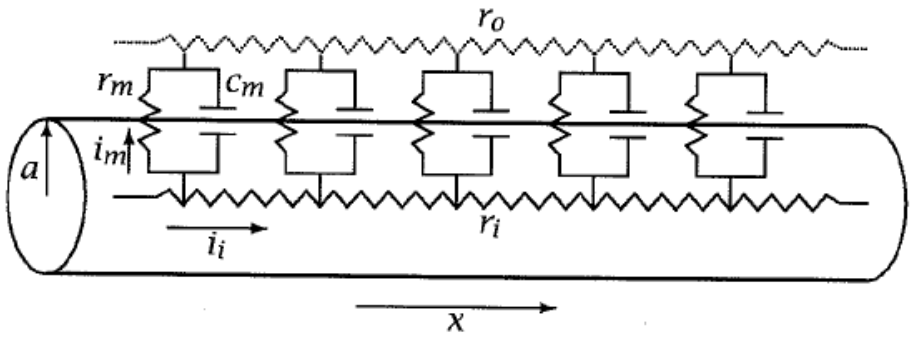
r_m and r_i are the membrane and axial resistances, i.e. the resistances of a thin slice of the cylinder

Johnston and Wu

The cable equation

Before we had:

$$i_m = i_C + i_{\text{ionic}} = c_m \frac{\partial V_m}{\partial t} + \frac{V_m}{r_m}$$



Now we also have to consider i_i, the current down the cable, due to voltage changes in *x*.
That current works against internal resistance, r_i

$$\frac{1}{r_i}\frac{\partial^2 V_m(x,t)}{\partial x^2} = c_m \frac{\partial V}{\partial t} + \frac{V_m}{r_m}.$$

or

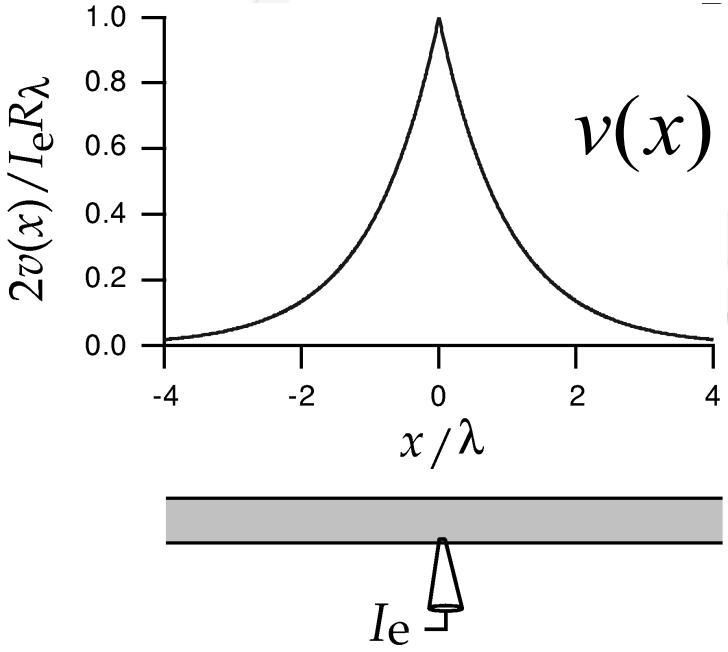
$$\lambda^2 \frac{\partial^2 V_m}{\partial x^2} = \tau_m \frac{\partial V_m}{\partial t} + V_m$$

where

$\tau_m = r_m c_m$ Time constant

$\lambda = \sqrt{\frac{r_m}{r_i}}$ Space constant

How does voltage decay in space?



$$v(x) \propto e^{\left(-\frac{|x|}{\lambda}\right)}$$

Potential decays exponentially from x = 0

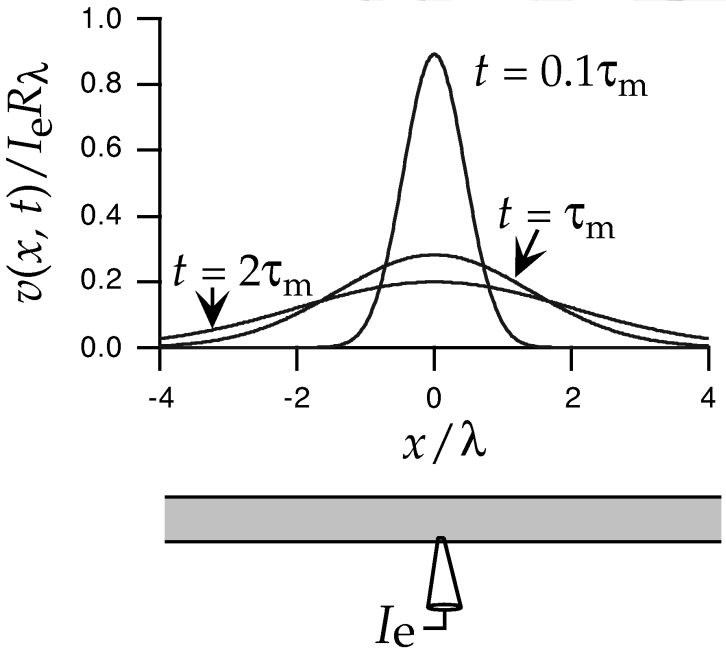
Infinite Cable,
Constant current at x = 0

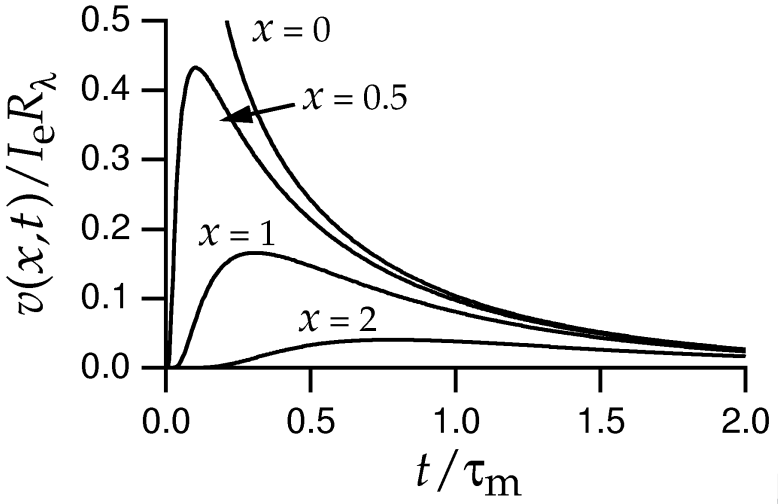
Dayan and Abbott

How does voltage decay over space and time?

Infinite Cable,

Current pulse at t = 0, x = 0





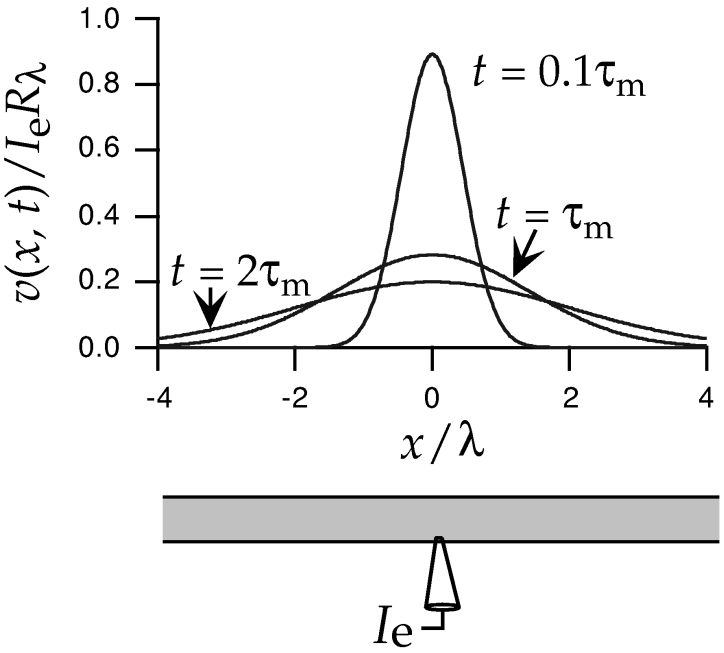
Potential peaks later (and at lower values) for points further away from input

General solution: filter and impulse response

$$V(x,t) \propto \sqrt{\frac{\tau}{4\pi\lambda^2 t}} e^{-\frac{t}{\tau} - \frac{\tau x^2}{4\lambda^2 t}}$$

Diffusive spread

Exponential decay



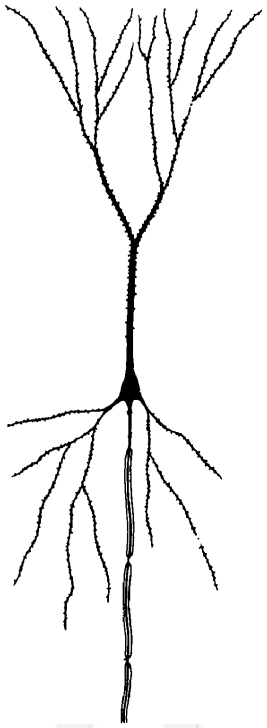
OK: now what?

1. The geometry can be extremely complicated

Cable Equation

$$\frac{1}{r_i}\frac{\partial^2 V_m(x,t)}{\partial x^2} = c_m\frac{\partial V}{\partial t} + \frac{V_m}{r_m} \cdot \; + i_e$$

?

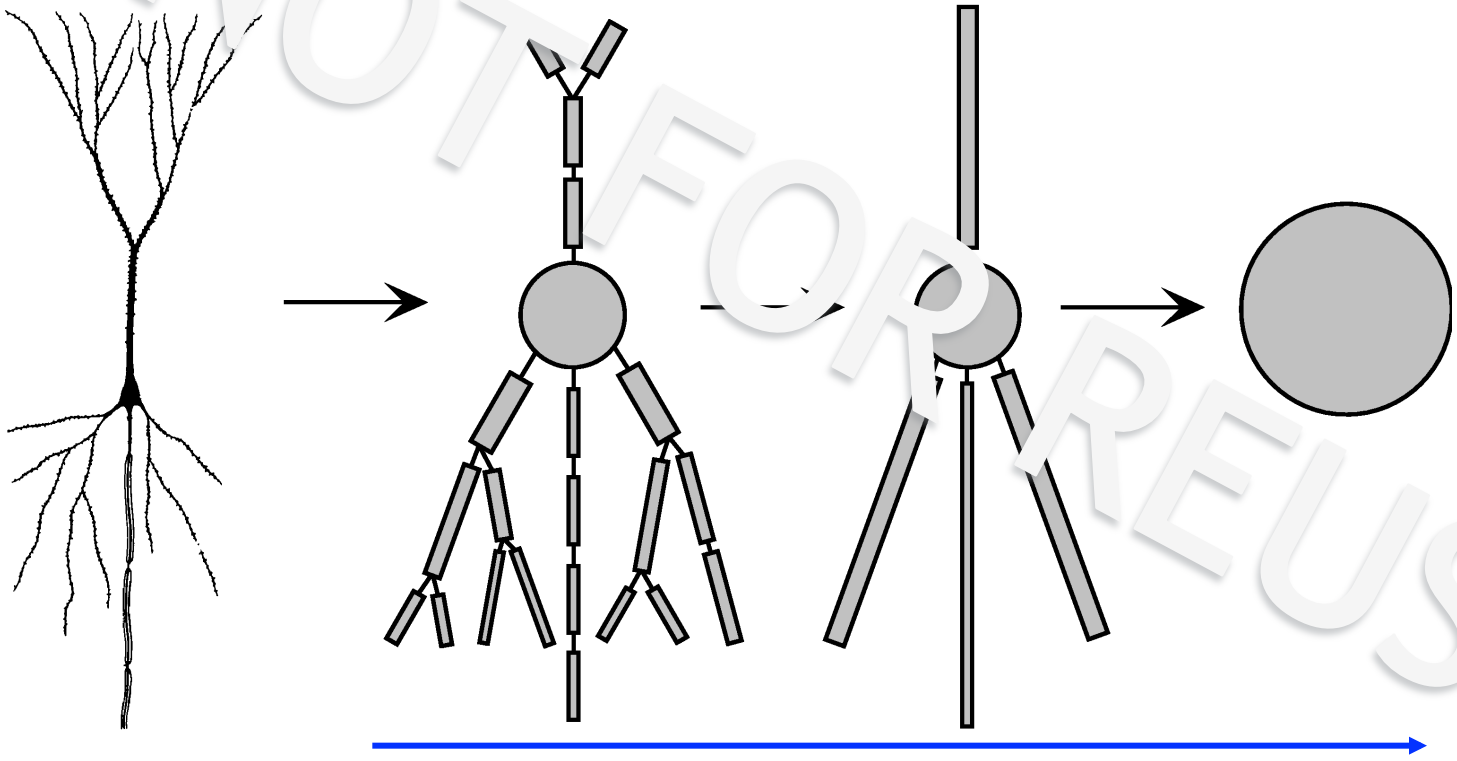


2. And, um, ion channels?

➔ Quickly becomes intractable to solve analytically for realistic neurons

Solution: Divide and Conquer

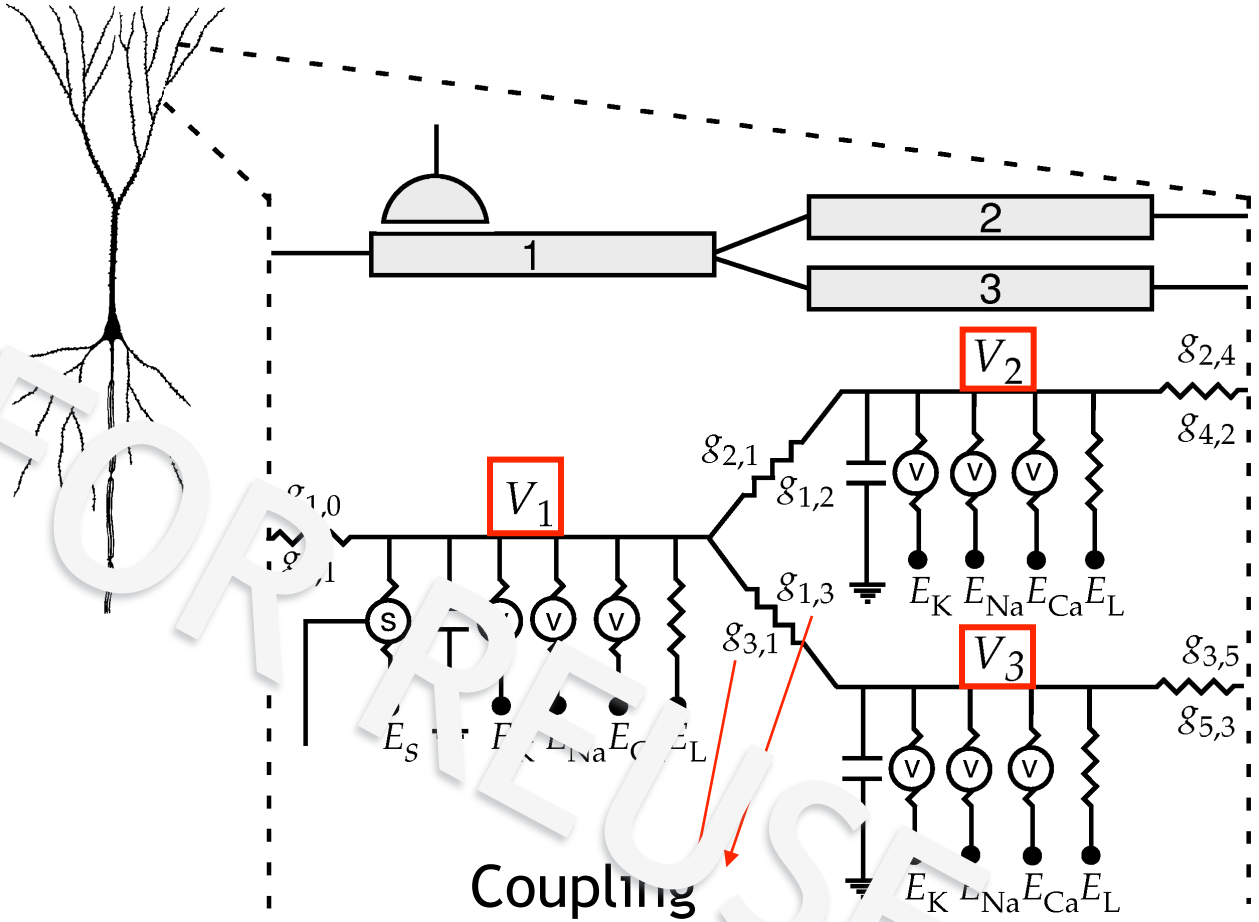
Compartmental models



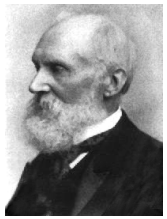
Decreasing number of “compartments”

Each compartment = one dV/dt equation (usually no dependence on x)

The gory details

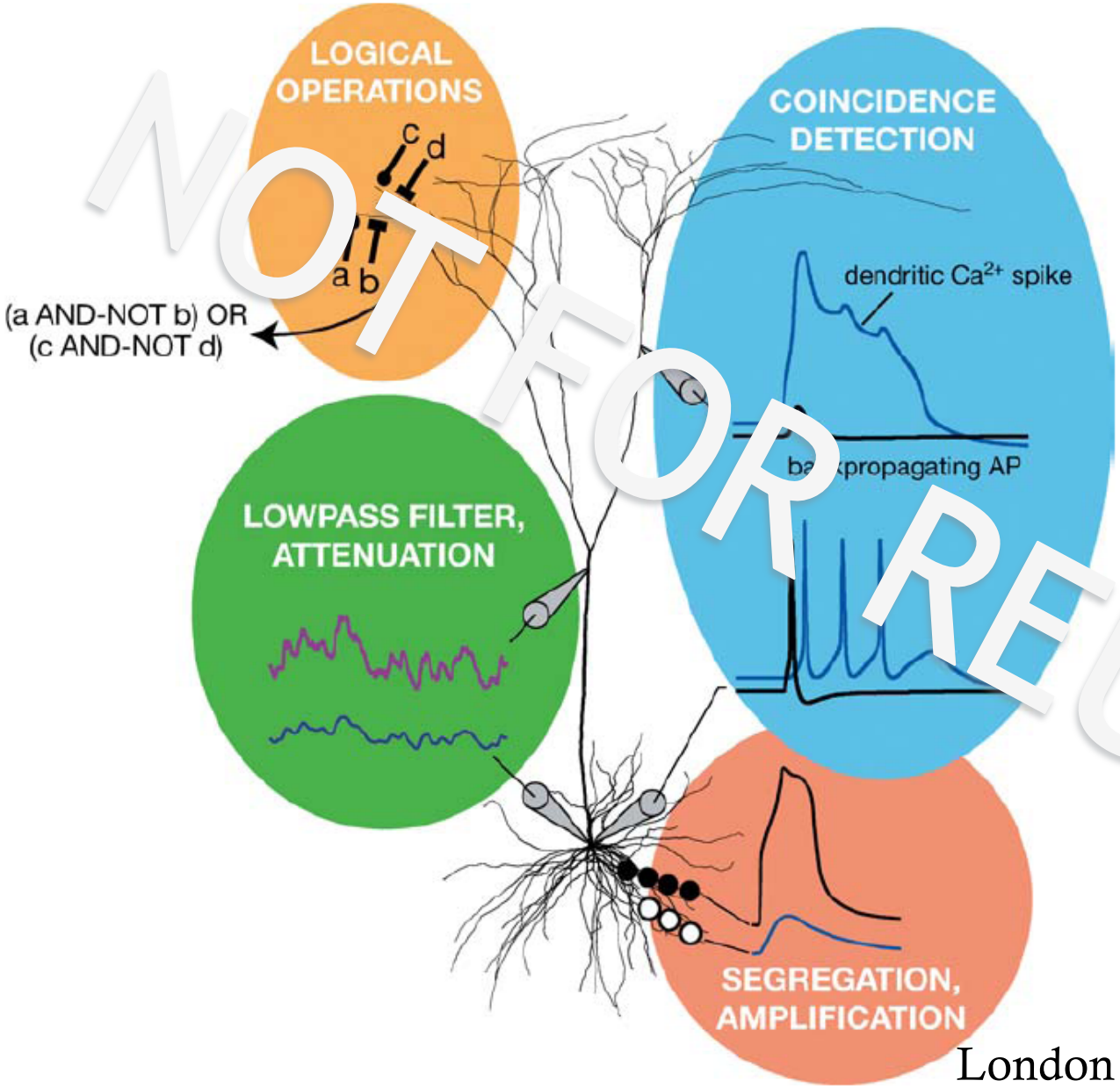


And now you see why Genesis and NEURON were developed—thank you!



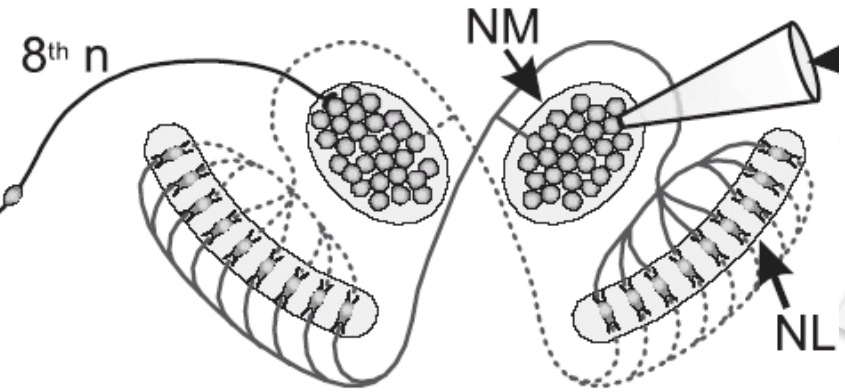
Dayan and Abbott

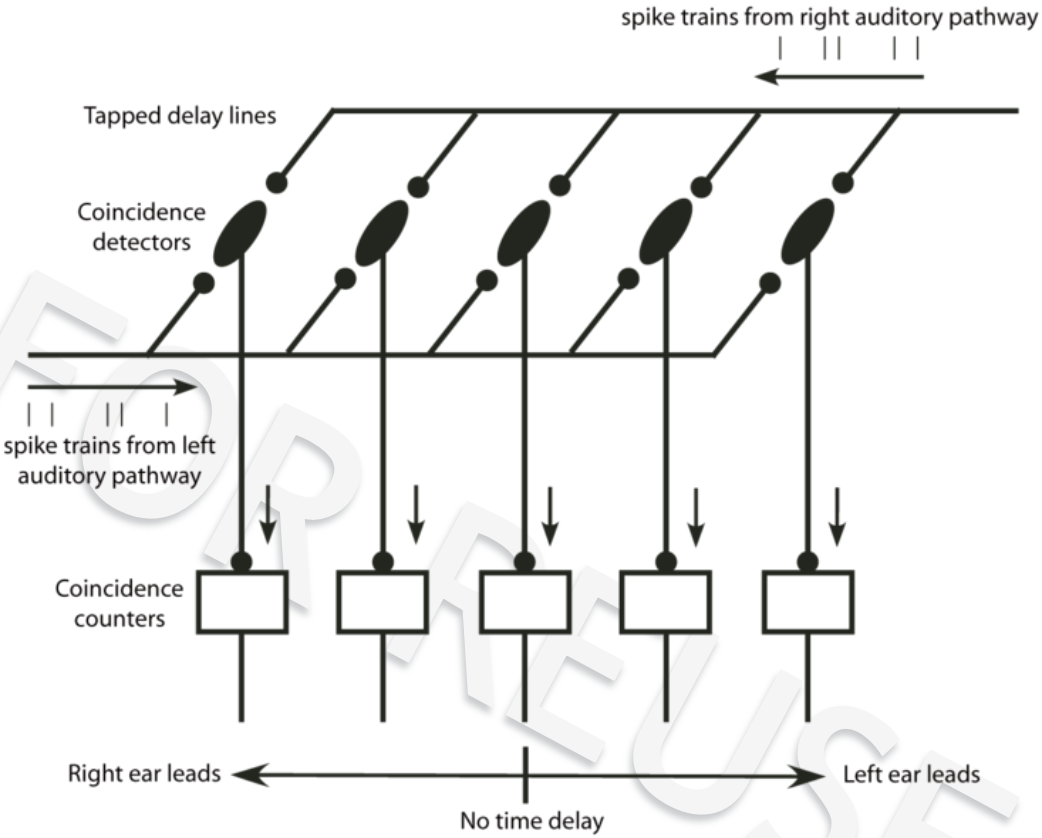
What do dendrites add to neuronal computation?



London and Hausser, 2005

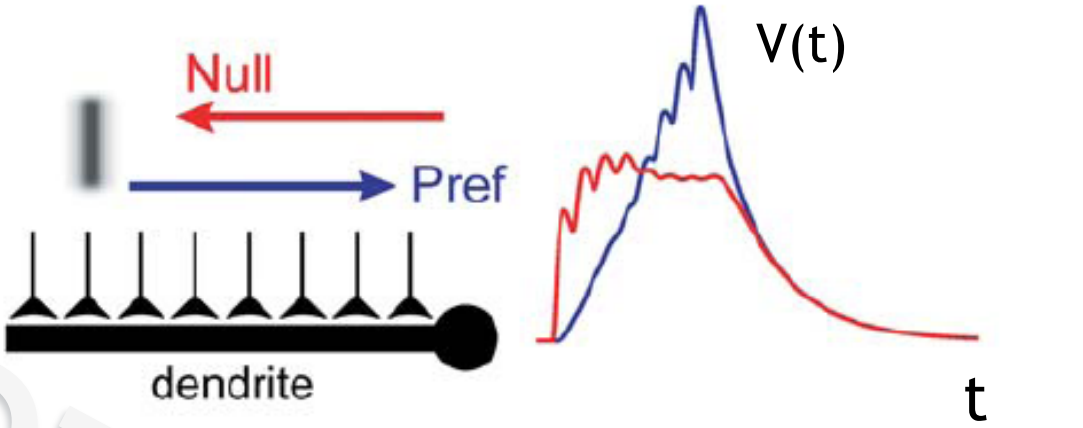
Delay lines in sound localization

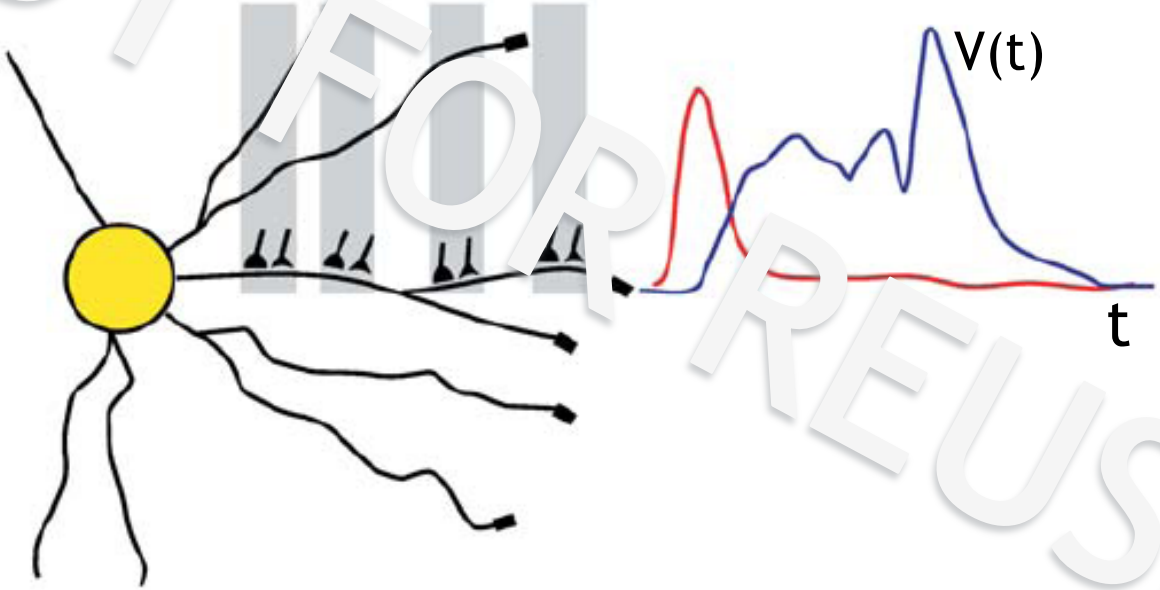




Spain; Scholarpedia

Direction selectivity





Rall; London and Hausser, 2005

Enthusiastically recommended references

- **Johnson and Wu, *Foundations of Cellular Neurophysiology*, Chap 4**

The classic textbook of biophysics and neurophysiology: lots of problems to work through. Good for HH, ion channels, cable theory.

- **Koch, *Biophysics of Computation***

Insightful compendium of ion channel contributions to neuronal computation

- **Izhikevich, *Dynamical Systems in Neuroscience***

An excellent primer on dynamical systems theory, applied to neuronal models

- **Magee, *Dendritic integration of excitatory synaptic input*,**

Nature Reviews Neuroscience, 2000
Review of interesting issues in dendritic integration

- **London and Hausser, *Dendritic Computation*,**

Annual Reviews in Neuroscience, 2005
Review of the possible computational space of dendritic processing