

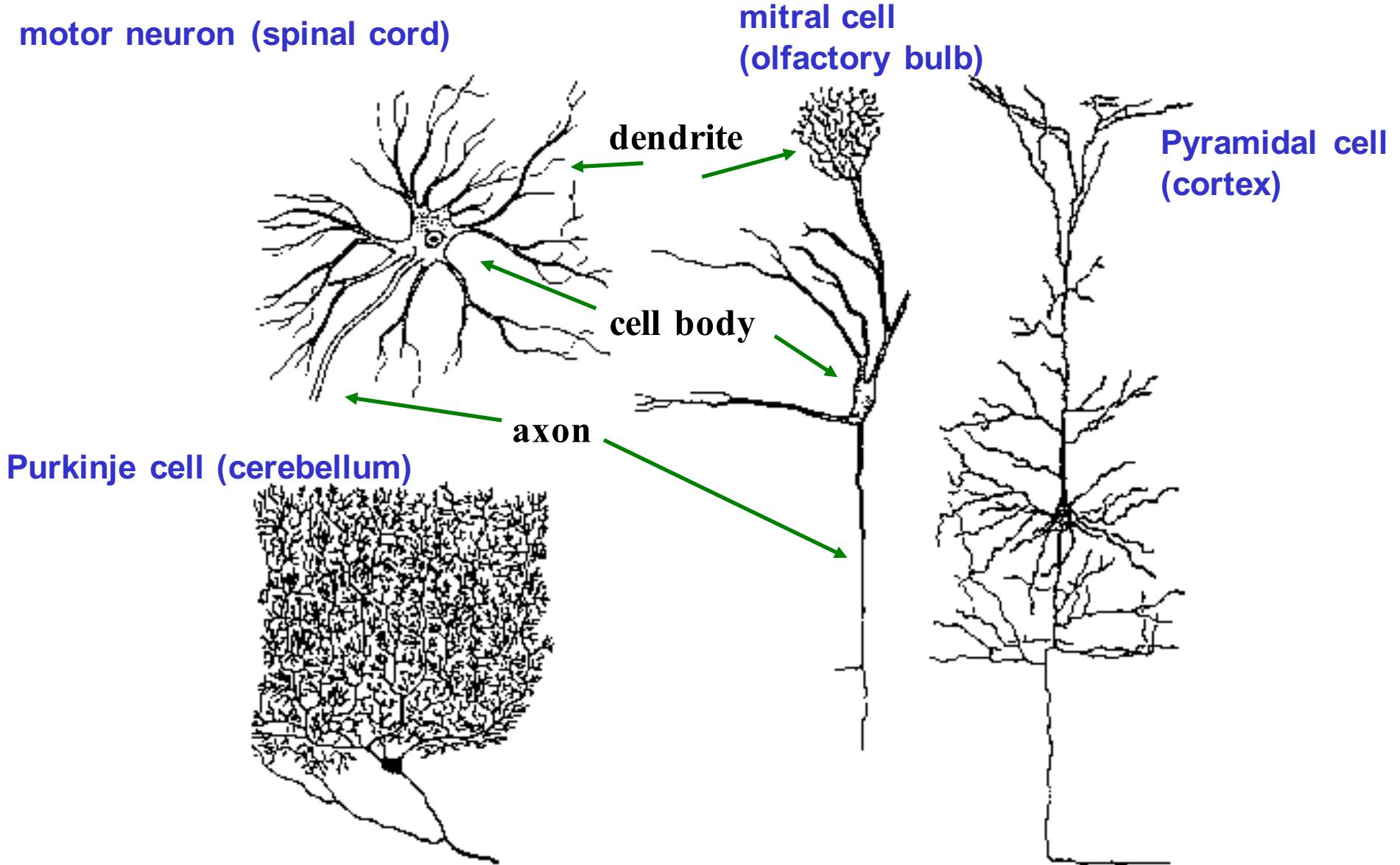
**$10^{11}$  neurons**

**( $10^5$  per mm<sup>3</sup>)**

**$10^{15}$  synapses**

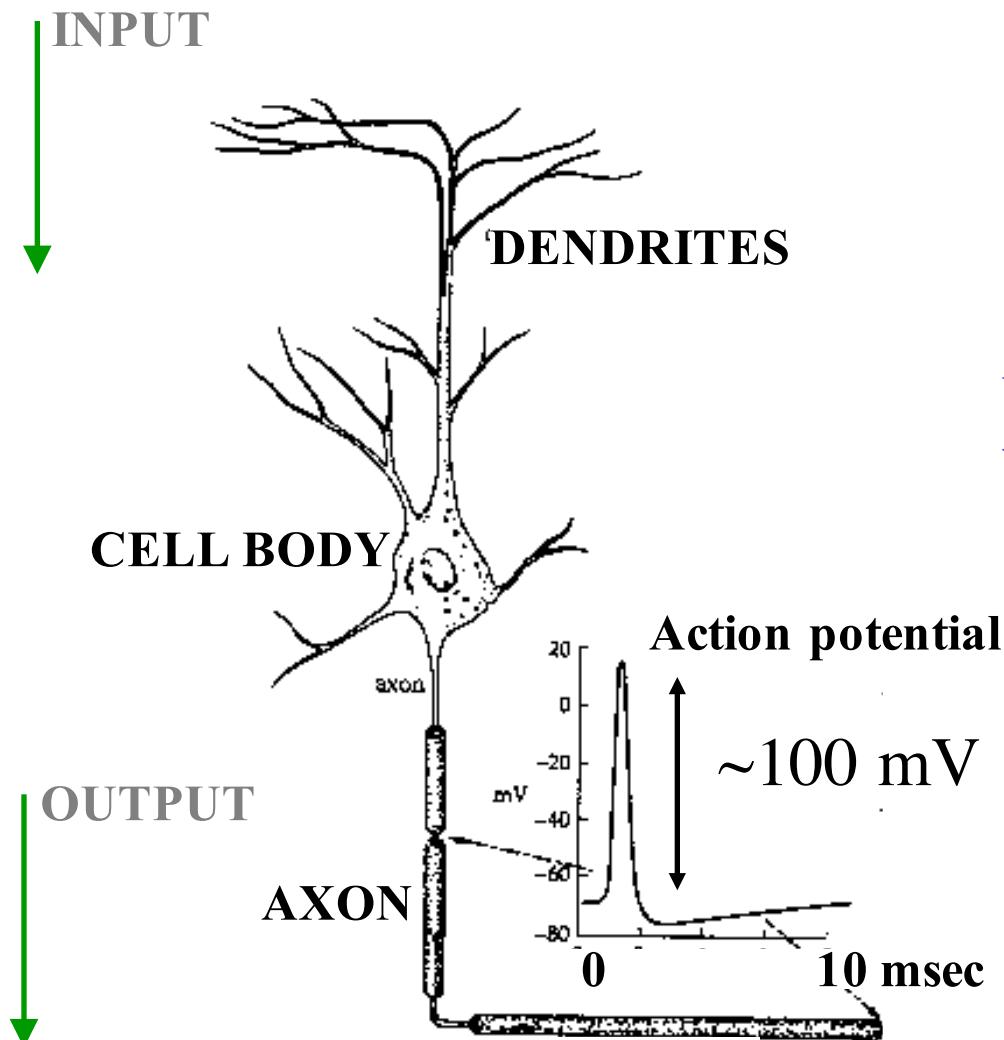
from *Neuroscience: Exploring the Brain* by M.F. Bear, B.W. Connors, and M.A. Paradiso, 2001

Electrical signals come IN to dendrites, are “integrated” in cell body, result goes OUT axon



From Nicholls et al, 1992, Fisher and Boycott, 1974, Johnston and Wu, 1997

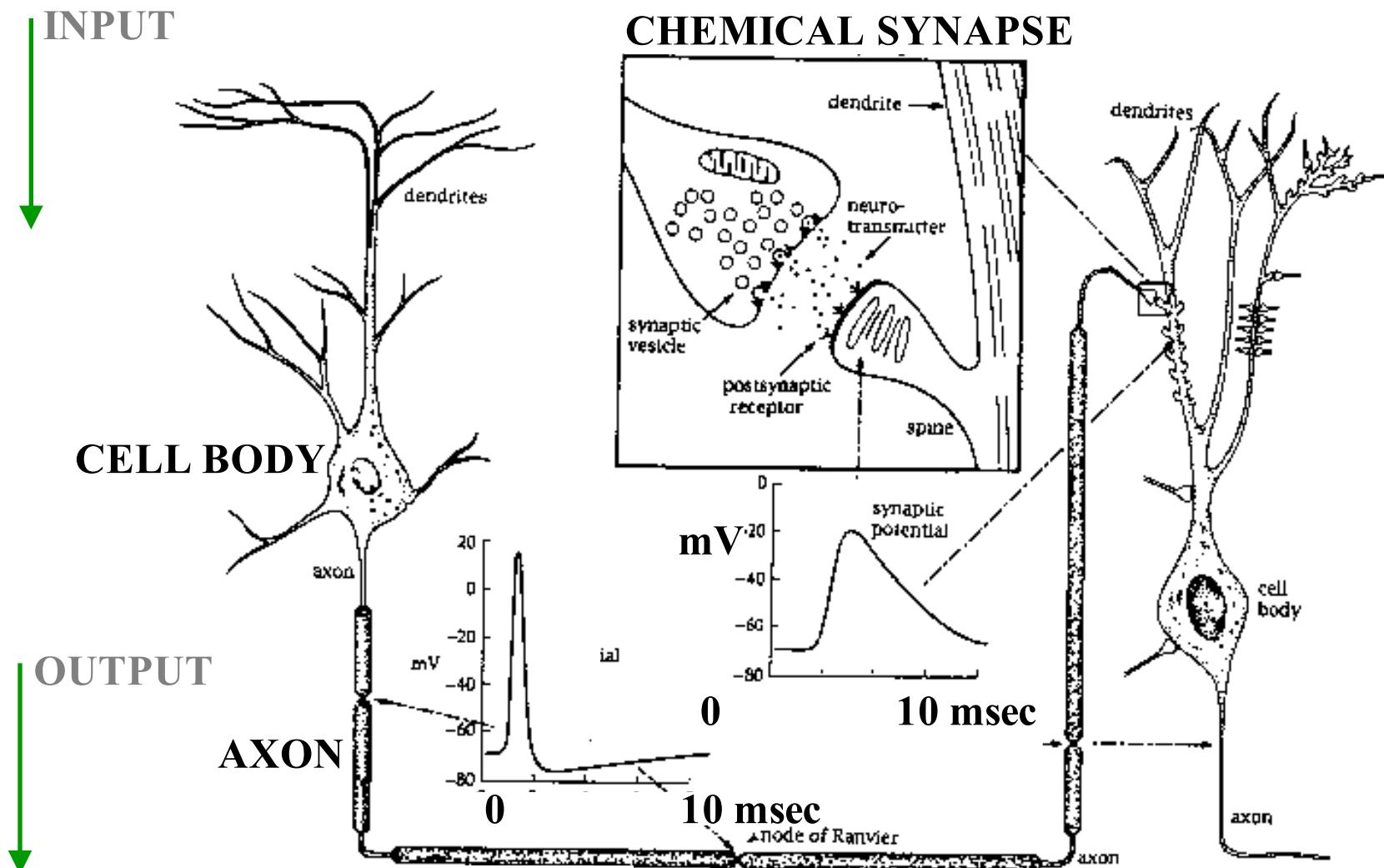
Given sufficient input, neurons “fire action potentials” – fast voltage transients



Voltage V: set by "excess charge" inside vs outside membrane (more later)

Given sufficient input, neurons “fire action potentials” – fast voltage transients

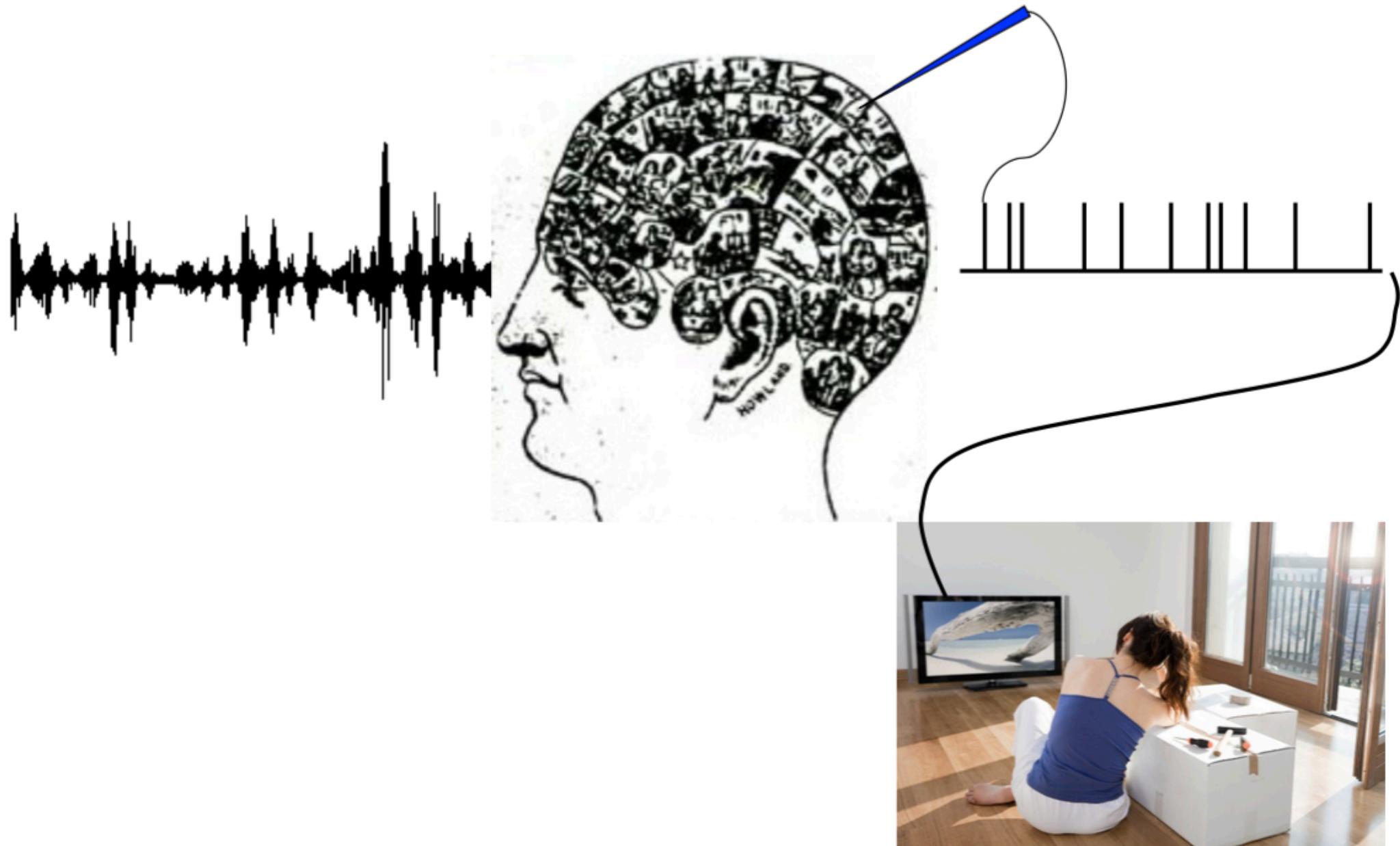
...which are communicated to downstream neurons via synapses



- Overview (blackboard)

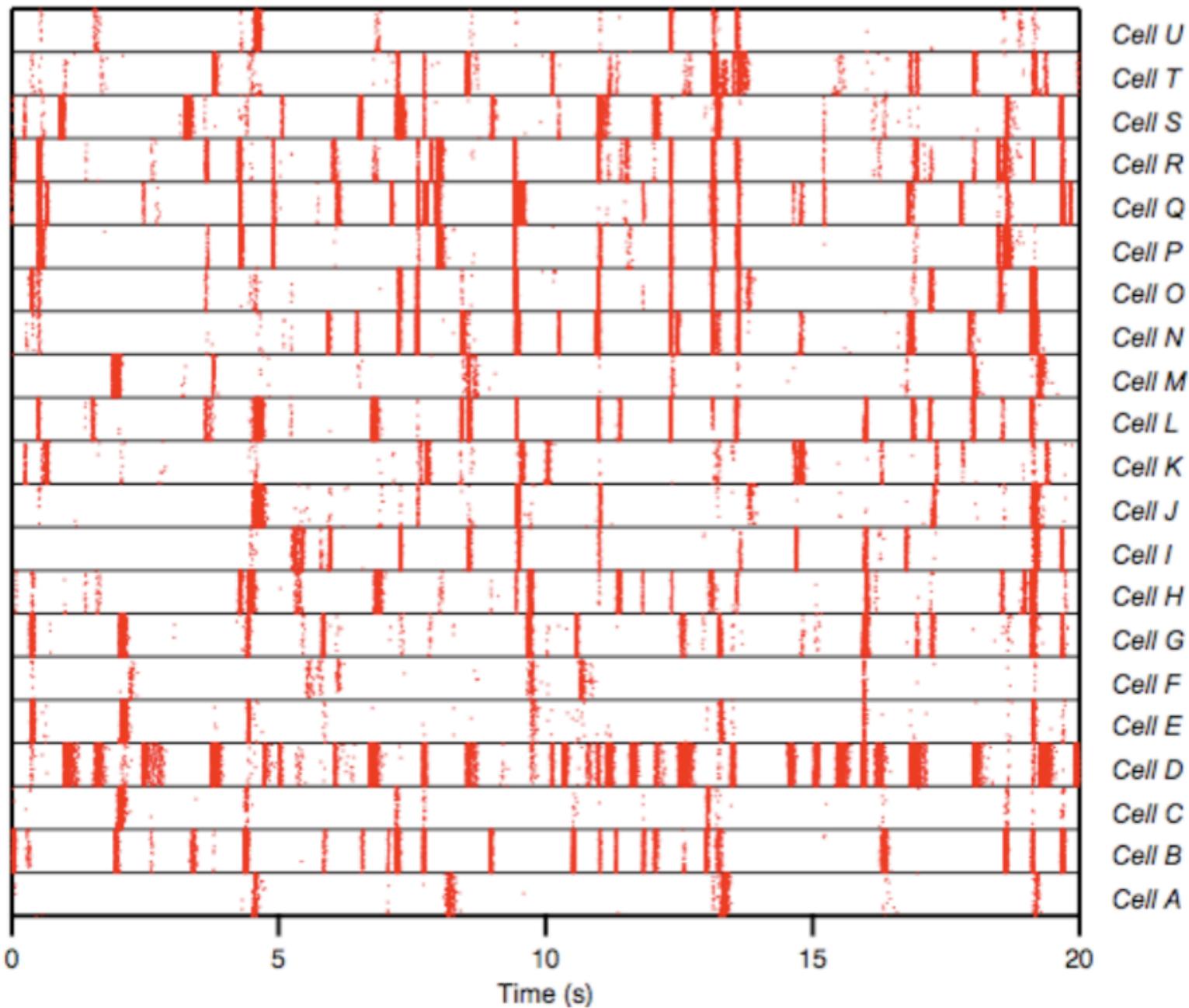
- Thanks to Prof. Adrienne Fairhall for many slides, materials, and ideas!

# Neural coding



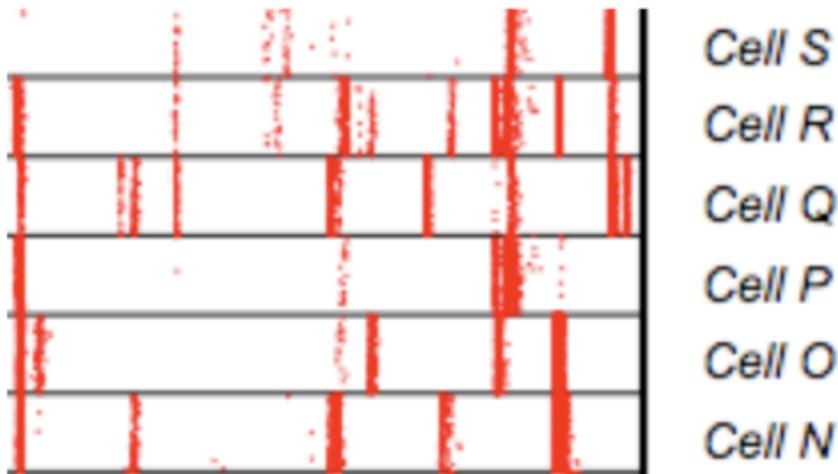
# What is the neural code?

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*Encoding:* how does a stimulus cause a pattern of responses?

- what are “responses” and what are their characteristics?
- how much is deterministic and how much stochastic?
- neural models:
  - what takes us from stimulus to response;
  - descriptive and mechanistic models, and the relation between them.

*Decoding:* what do these responses tell us about the stimulus?

- Implies some kind of decoding algorithm
- How do we evaluate how good our algorithm is?

# Neural coding

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More generally, we are interested in determining the relationship:

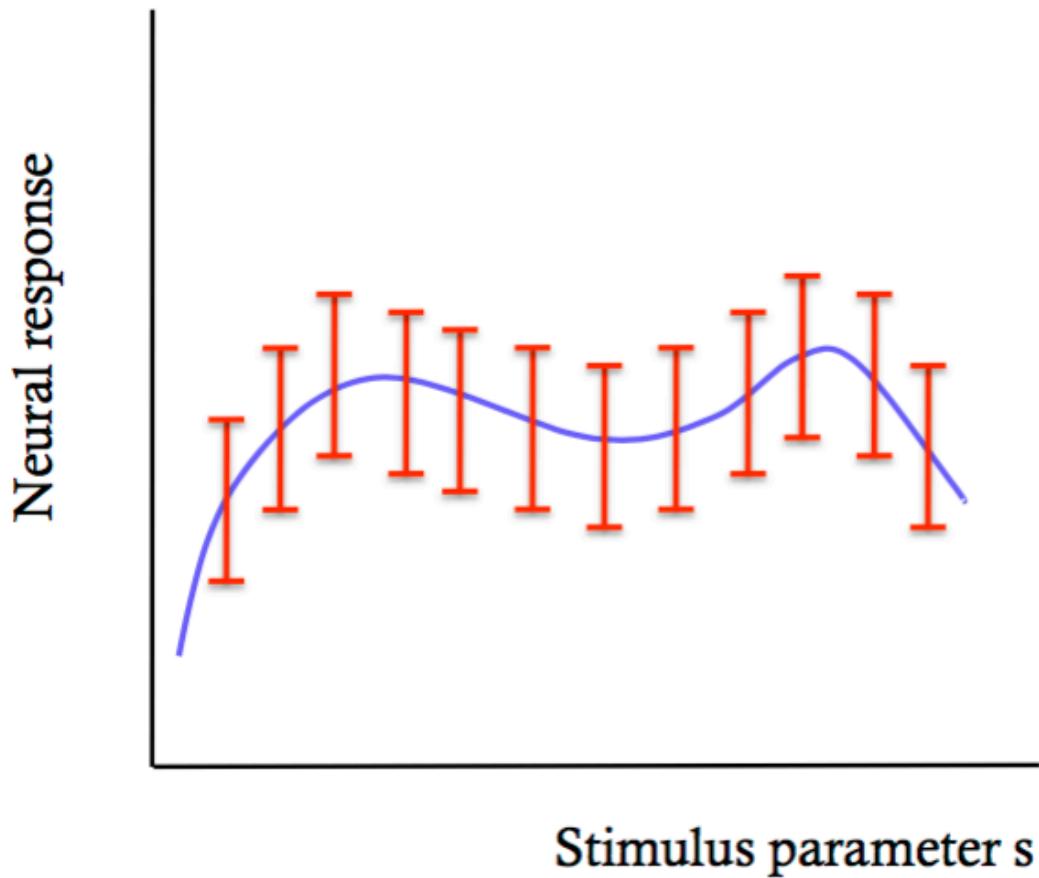
$$P(\text{response} \mid \text{stimulus})$$

*encoding*

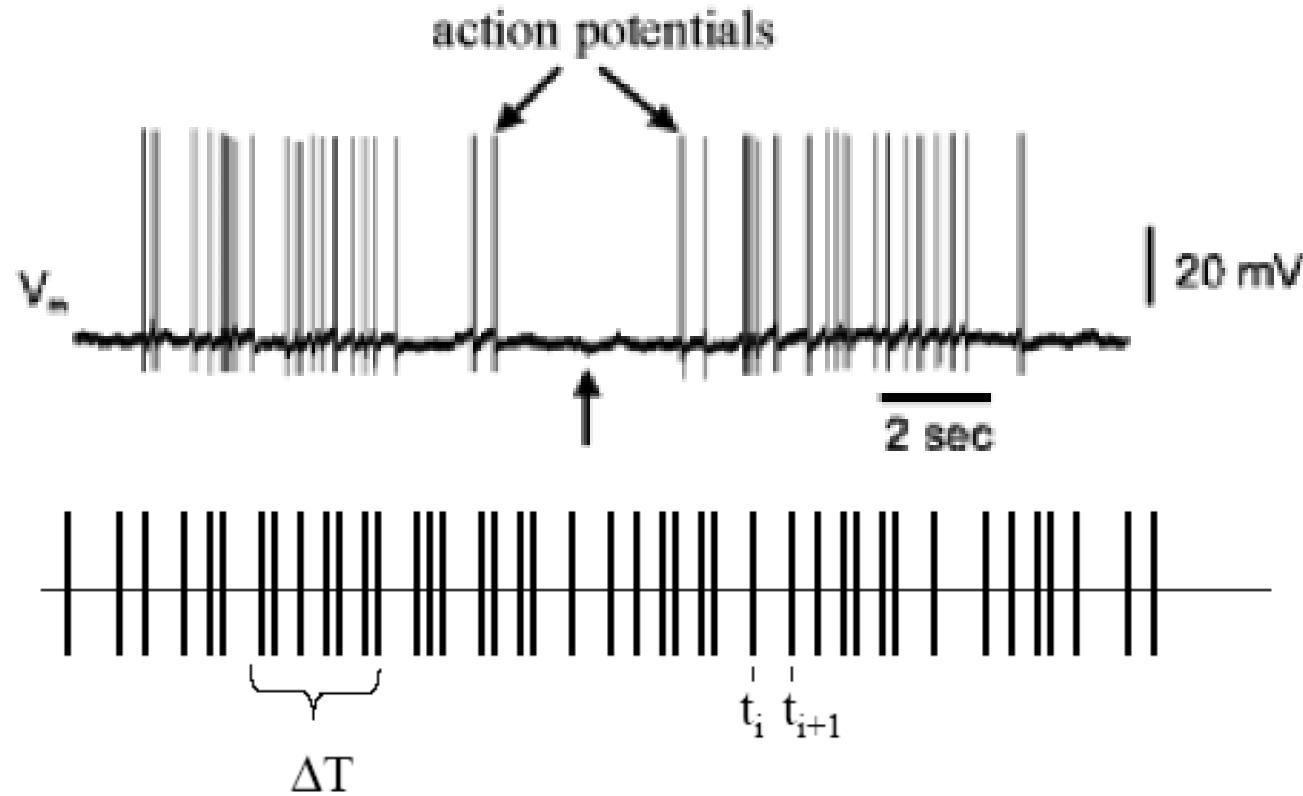
$$P(\text{stimulus} \mid \text{response})$$

*decoding*

# Neuronal representation of information



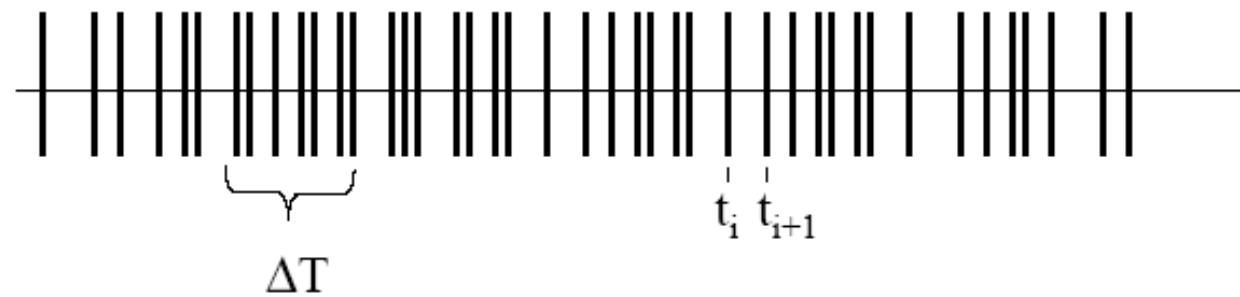
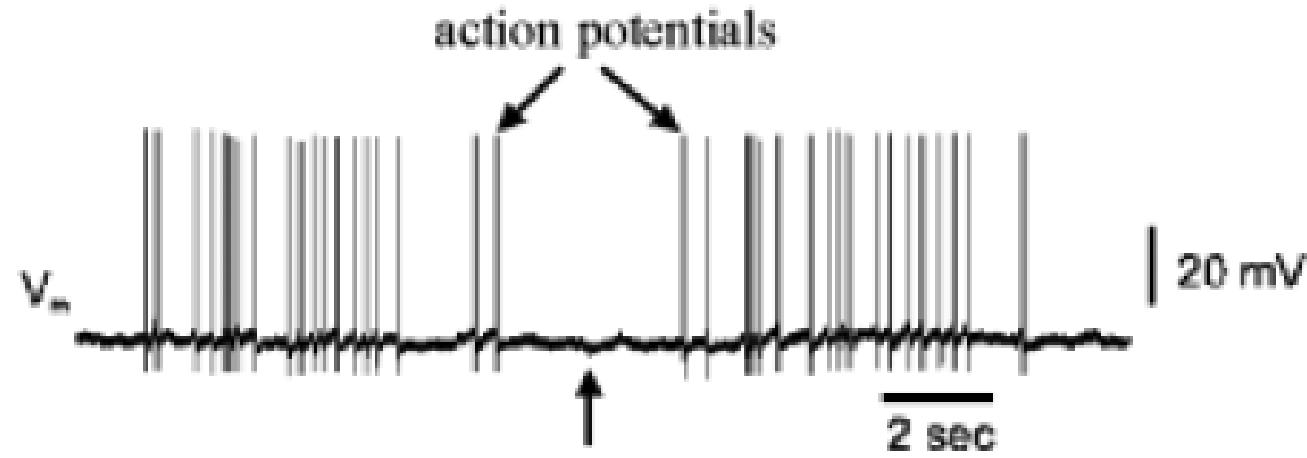
Simplest definition of neural response: *firing rates*



$$\text{Firing rate} = (\# \text{ spikes}) / (\Delta T)$$

(Other possibilities: spike timing, synchrony among multiple spikes, ...)

(Board ... definition of delta function)



David Tank

SPIKE TRAIN

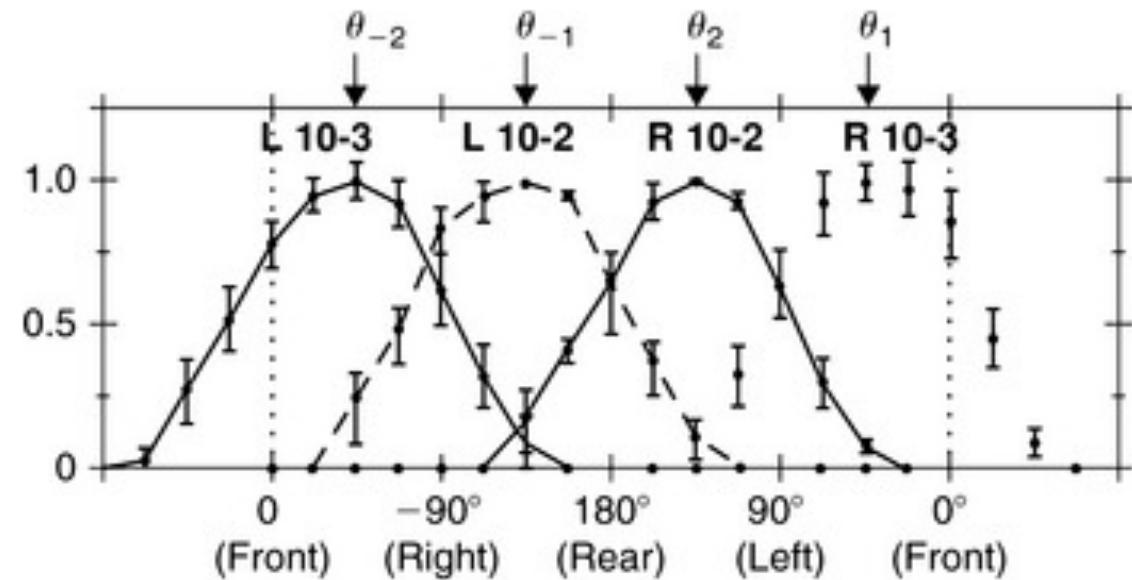
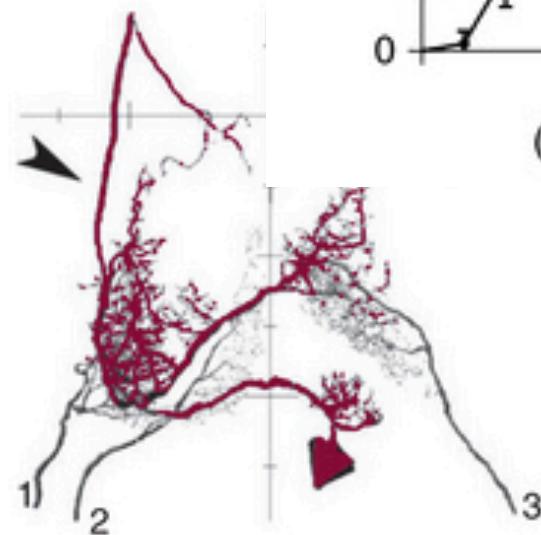
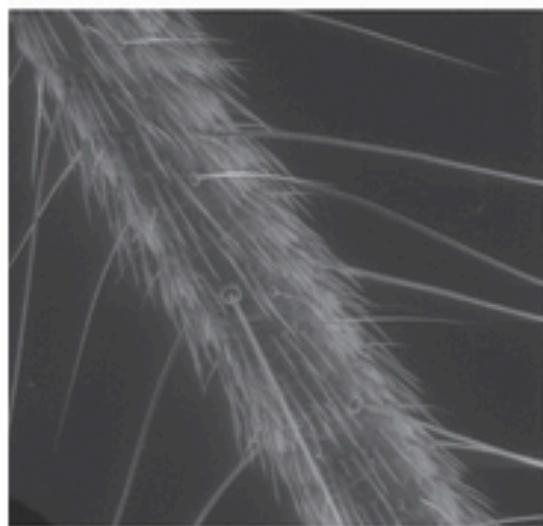
$$\rho(t) = \sum_{t_i} \delta(t - t_i)$$

FIRING RATE

$$r(t) = \frac{1}{\Delta T} \int_t^{t+\Delta T} \rho(t) dt$$

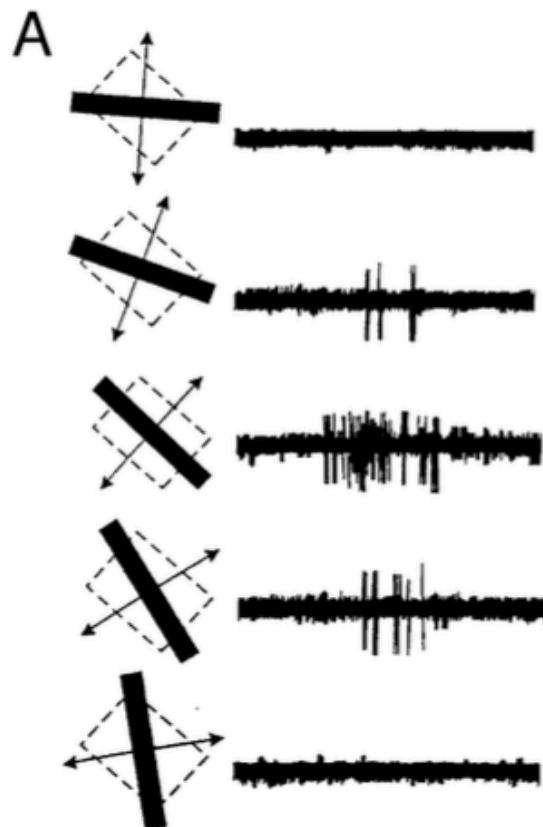
# Starting “simple:” Stimulus ENcoding in the cricket cercal system

Response = firing rate  
Stimulus = wind direction

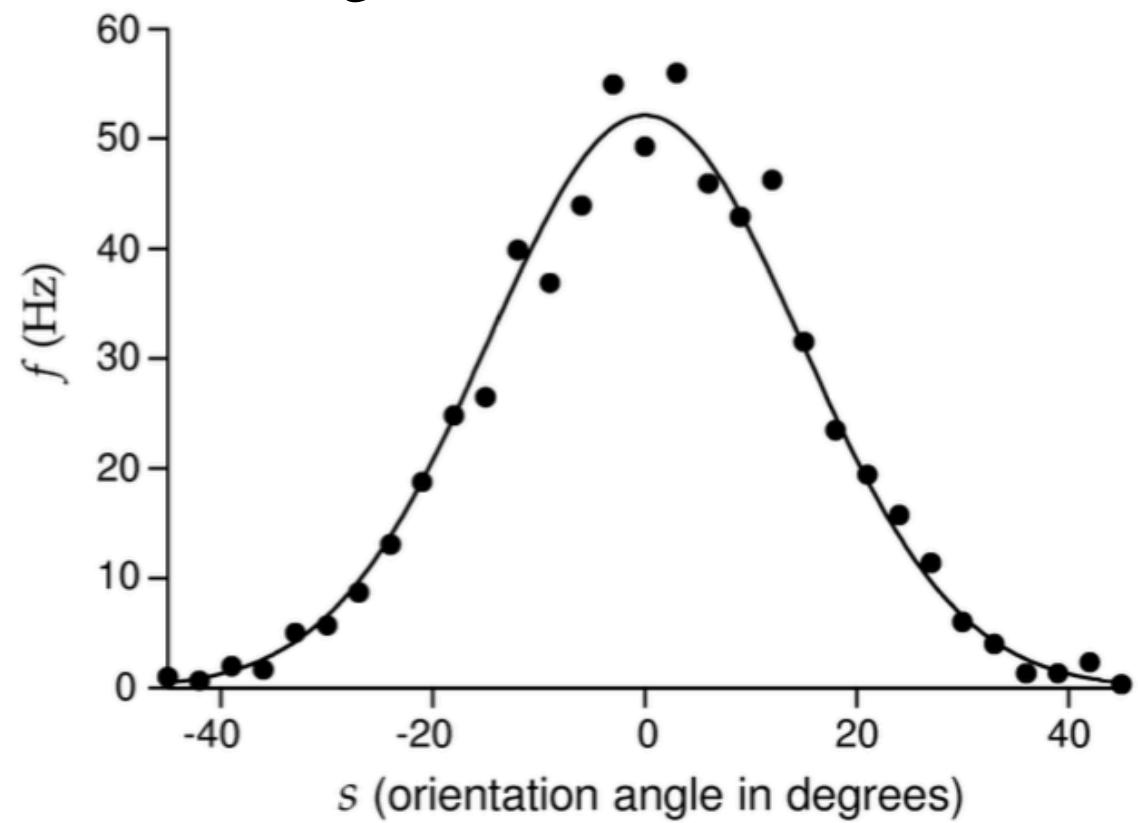


# Receptive fields and tuning curves

Tuning curve:  $r = f(s)$



B Firing rate (Hz) vs. stimulus  $s$



Gaussian tuning curve of a cortical (V1) neuron

(Board –  
Modeling spike trains and the Poisson process  
Random variables  
Generating spike trains in MATLAB)

## Code 1: generate\_simple\_spiketrain.m

```
%Generate single spiketrain  
  
rand('state',sum(100*clock));  
  
nsec=1 ;  
T=1;  
deltat=0.001;  
r=100;  
p=r*deltat;  
numbins=round(T/deltat);  
spiketrain=round(rand(1,numbins) + (p-1/2))  
  
figure;  
imagesc(spiketrain)  
...
```

(Board – Mean, variance, std dev)

# Code 1, continued: Generating and analyzing multiple trials of a spike train

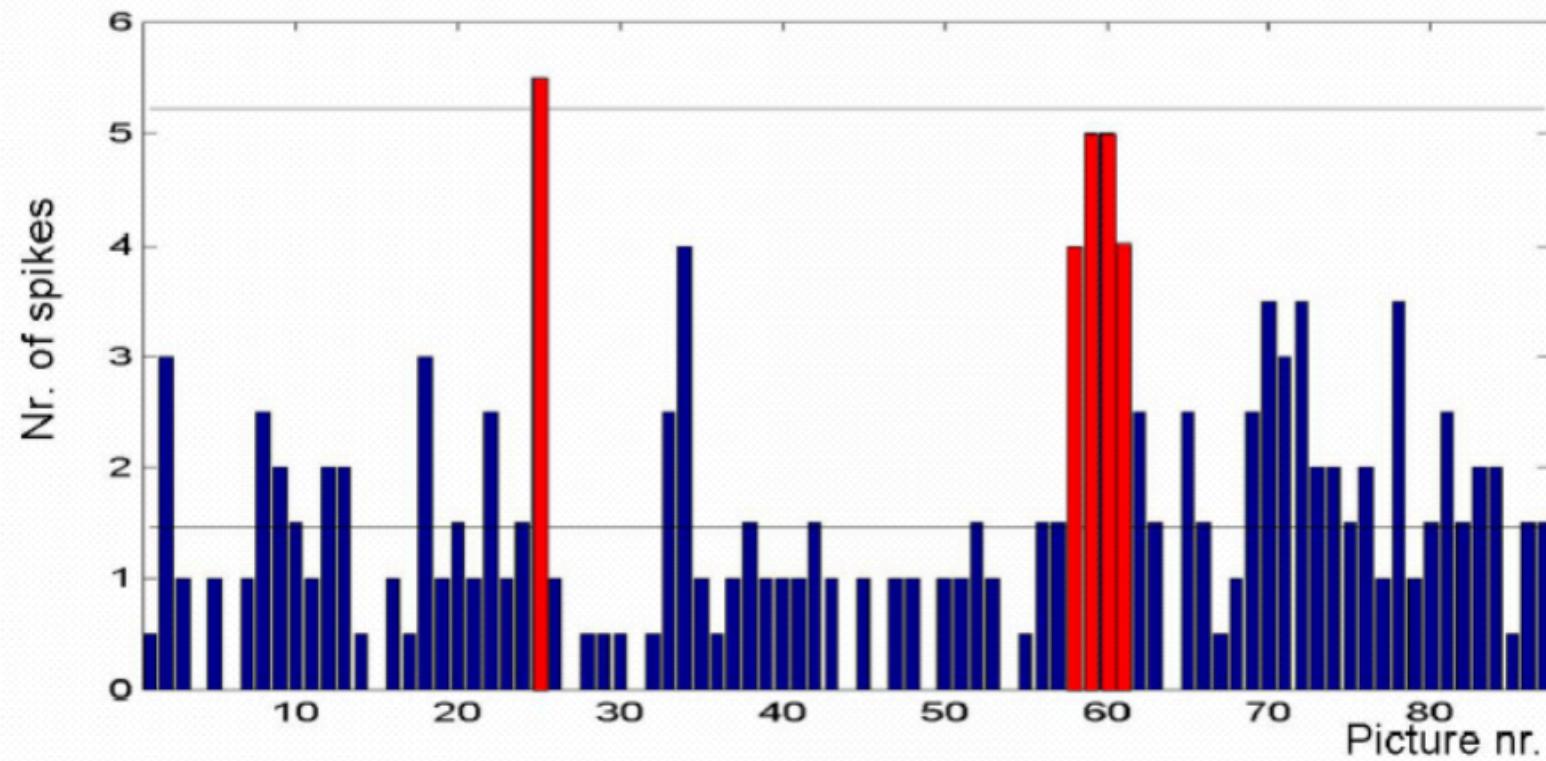
```
%Generate many "trials" of spiketrains
numtrials=10;
spiketrain=round(rand(numtrials,numbins) +
(p-1/2));

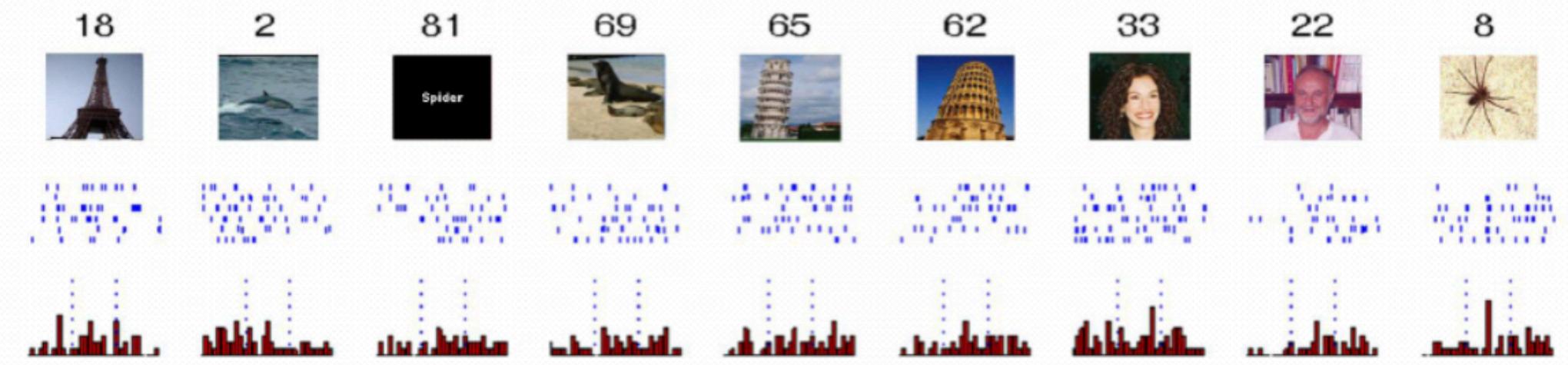
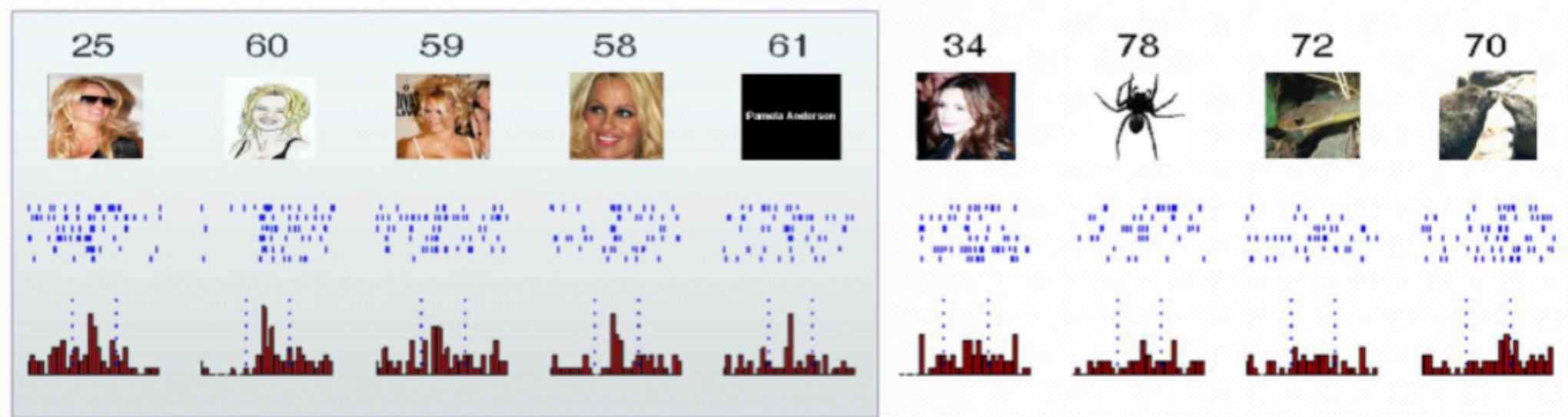
figure;
imagesc(spiketrain)
xlabel('time')
ylabel('trial')

%Compute the average spike rate, and standard
deviation
rate_per_trial=1/T * sum(spiketrain,2)
mean_rate_per_trial = mean(rate_per_trial)
std_dev_rate_per_trial = std(rate_per_trial)
```

Hand out HW

## Complex feature representation





25



60



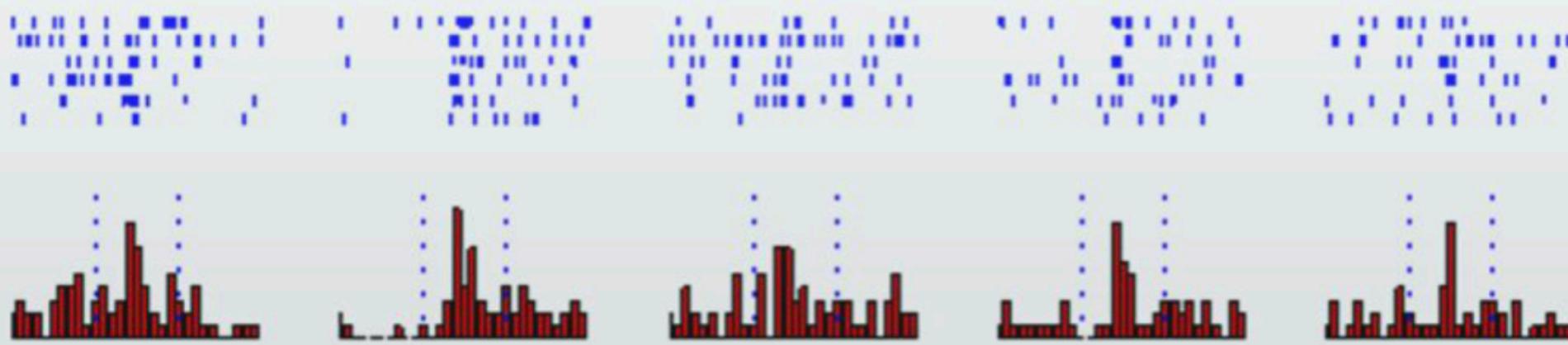
59



58



61



nature

Vol 435 | 23 June 2005 | doi:10.1038/nature03687

## LETTERS

### Invariant visual representation by single neurons in the human brain

R. Quian Quiroga<sup>1,2</sup>†, L. Reddy<sup>1</sup>, G. Kreiman<sup>3</sup>, C. Koch<sup>1</sup> & I. Fried<sup>2,4</sup>