k-means Clustering of the Iris Dataset

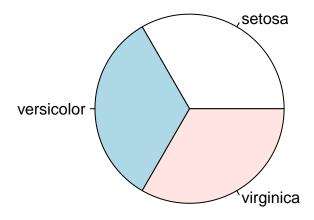
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```
# k-means is an unsupervised learning technique that deals with finding a
# structure (cluster) in a collection of unlabeled data. Clustering of the data
# involves organizing objects into k-groups whose members are similar in some way.
# Here, the similarity criterion is distance: two or more objects belong to the
# same cluster if they are "close" according to a given distance. The k-means
# approach utilizes an exclusive clustering algorithm.
# The algorithm of Hartigan and Wong (1979) is used by default. Note that some
# authors use k-means to refer to a specific algorithm rather than the general
# method: most commonly the algorithm given by MacQueen (1967) but sometimes that
# given by Lloyd (1957) and Forgy (1965). The Hartigan-Wong algorithm generally
# does a better job than either of those, but trying several random
# starts (nstart> 1) is often recommended. In rare cases, when some of the
# points (rows of x) are extremely close, the algorithm may not converge in the
# "Quick-Transfer" stage, signalling a warning (and returning ifault = 4).
# Slight rounding of the data may be advisable in that case.
# Hartigan, J. A. and Wong, M. A. (1979). A K-means clustering algorithm.
# Applied Statistics 28, 100-108.
# Prior to clustering data, you may want to remove or estimate missing data and
# rescale variables for comparability.
# mydata <- na.omit(mydata) # listwise deletion of missing
# mydata <- scale(mydata) # standardize variables</pre>
# some EDA first
dim(iris)
## [1] 150
names(iris) # variable names
## [1] "Sepal.Length" "Sepal.Width" "Petal.Length" "Petal.Width"
## [5] "Species"
str(iris) # structure
## 'data.frame':
                   150 obs. of 5 variables:
## $ Sepal.Length: num 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
## $ Sepal.Width : num 3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
## $ Petal.Length: num 1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
## $ Petal.Width : num 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
## $ Species : Factor w/ 3 levels "setosa", "versicolor", ..: 1 1 1 1 1 1 1 1 1 1 ...
```

```
## $names
## [1] "Sepal.Length" "Sepal.Width" "Petal.Length" "Petal.Width"
## [5] "Species"
##
## $row.names
   [1]
        1
             2
                3
                    4
                       5
                           6
                              7
                                  8
                                      9 10 11 12 13 14 15 16 17
##
   [18] 18 19 20
                   21 22
                          23 24
                                  25 26 27
                                             28
                                                29
                                                    30 31
                                                           32
## [35] 35 36 37
                   38
                       39
                           40 41
                                  42
                                     43
                                        44 45
                                                46
                                                    47 48
                                                           49
                                                               50
## [52] 52 53 54 55 56
                          57
                              58
                                  59
                                      60
                                         61
                                             62
                                                63
                                                    64
                                                       65
                                                           66 67
                                                                   68
   [69] 69
            70 71 72
                       73
                          74
                              75
                                  76
                                     77
                                         78
                                            79
                                                80
                                                    81
                                                       82 83 84
## [86] 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102
## [103] 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119
## [120] 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136
## [137] 137 138 139 140 141 142 143 144 145 146 147 148 149 150
##
## $class
## [1] "data.frame"
summary(iris)
                Sepal.Width
                               Petal.Length
                                            Petal.Width
##
    Sepal.Length
                             Min. :1.00 Min. :0.1
## Min. :4.30
               Min. :2.00
                             1st Qu.:1.60
## 1st Qu.:5.10
               1st Qu.:2.80
                                            1st Qu.:0.3
               Median :3.00
## Median :5.80
                             Median:4.35
                                            Median:1.3
                             Mean :3.76
## Mean
        :5.84
               Mean :3.06
                                            Mean :1.2
   3rd Qu.:6.40
                3rd Qu.:3.30
                             3rd Qu.:5.10
                                            3rd Qu.:1.8
##
## Max.
        :7.90
                 Max. :4.40 Max. :6.90
                                            Max. :2.5
##
        Species
##
   setosa
            :50
  versicolor:50
##
  virginica:50
##
##
##
table(iris$Species) # frequency
##
##
      setosa versicolor virginica
##
         50
                   50
                             50
pie(table(iris$Species)) # pie chart
```

attributes(iris) # attributes



#
cor(iris\$Sepal.Length, iris\$Petal.Length) # correlation between sepal, petal

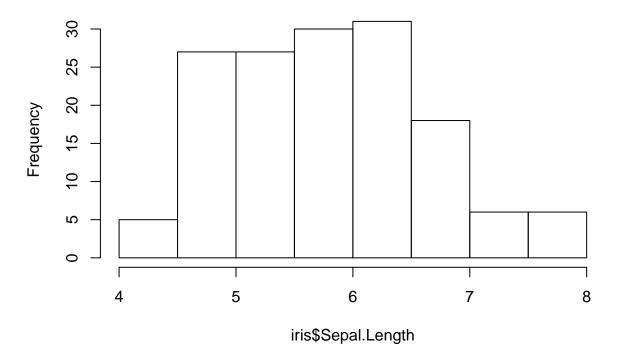
[1] 0.8718

cor(iris\$Sepal.Length, iris\$Sepal.Width)

[1] -0.1176

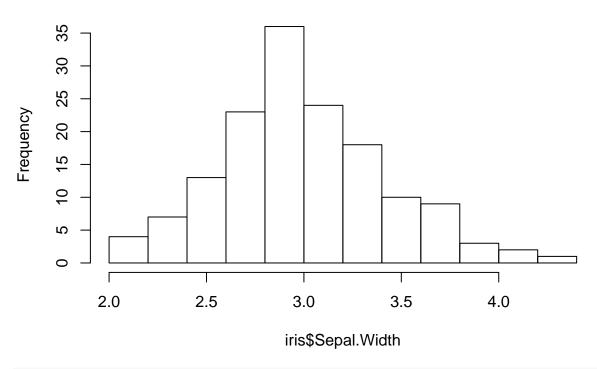
hist(iris\$Sepal.Length)

Histogram of iris\$Sepal.Length

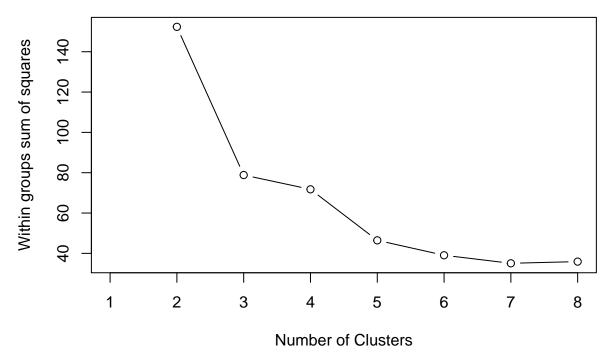


hist(iris\$Sepal.Width)

Histogram of iris\$Sepal.Width



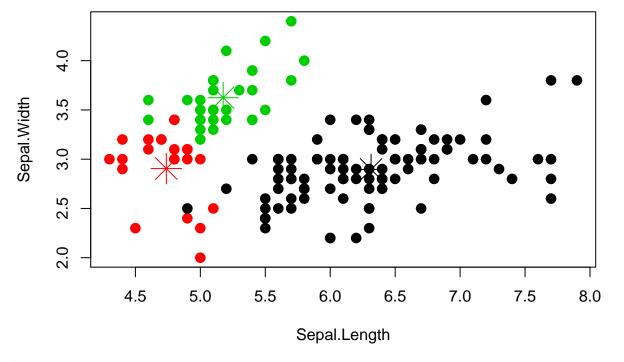
```
#
newiris <- iris
newiris$Species <- NULL # remove Species
#
# Below, we iterate through kmeans() with clusters argument varying from
# 1 to maxCluster and plot the within groups sum of squares for each iteration.
#
ssPlot <- function(data, maxCluster = 8) {
# Initialize within sum of squares
SSw <- (nrow(data) - 1) * sum(apply(data, 2, var))
SSw <- vector()
for (i in 2:maxCluster) {
    SSw[i] <- sum(kmeans(data, centers = i)$withinss)
}
plot(1:maxCluster, SSw, type = "b", xlab = "Number of Clusters", ylab = "Within groups sum of squares}
ssPlot(newiris)</pre>
```



```
# largest decrease going from 2 to 3 clusters. So, lets just go with 3.
# K-means clustering with 3 clusters of sizes 38, 50, 62
(kc <- kmeans(newiris, 3))</pre>
```

```
## K-means clustering with 3 clusters of sizes 96, 21, 33
##
## Cluster means:
   Sepal.Length Sepal.Width Petal.Length Petal.Width
## 1
        6.315
                2.896
                         4.974
                                1.7031
## 2
        4.738
                2.905
                         1.790
                                0.3524
        5.176
                3.624
## 3
                         1.473
                                0.2727
##
## Clustering vector:
   ## [141] 1 1 1 1 1 1 1 1 1 1
##
## Within cluster sum of squares by cluster:
## [1] 118.652 17.670
                 6.432
##
  (between_SS / total_SS = 79.0 %)
##
## Available components:
##
## [1] "cluster"
               "centers"
                         "totss"
                                   "withinss"
## [5] "tot.withinss" "betweenss"
                         "size"
                                   "iter"
 [9] "ifault"
# Compare the Species label with the clustering result
table(iris$Species, kc$cluster)
```

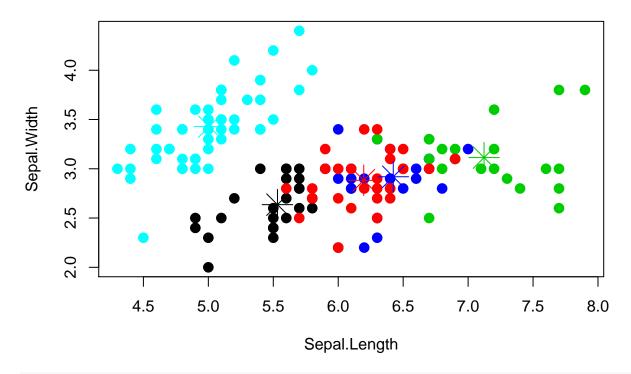
```
##
##
                   2 3
##
     setosa
                0 17 33
     versicolor 46 4 0
##
##
     virginica 50 0 0
# This result shows that cluster "setosa" can be easily separated from the other
# clusters, and that clusters "versicolor" and "virginica" are to a small degree
# overlapped with each other.
# Plot the clusters and their centres. Note that there are four dimensions in the data
# and that only the first two dimensions are used to draw the plot below.
# Some black points close to the green centre (asterisk) are actually closer
# to the black centre in the four dimensional space.
par(mfrow=c(1,1)) # make sure only 1 plot per page
plot(newiris[c("Sepal.Length", "Sepal.Width")], col=kc$cluster, pch=20,cex=2)
points(kc$centers[,c("Sepal.Length", "Sepal.Width")], col=1:3, pch=8, cex=3)
```



```
#
# Here are the exact locations of the cluster centers are.
# Note: just pay attention to Length and Width
kc$centers
```

```
Sepal.Length Sepal.Width Petal.Length Petal.Width
##
## 1
             6.315
                         2.896
                                        4.974
                                                    1.7031
## 2
             4.738
                          2.905
                                        1.790
                                                    0.3524
## 3
             5.176
                         3.624
                                        1.473
                                                    0.2727
# Lets try 5 clusters just for fun
(kc <- kmeans(newiris, 5))</pre>
```

```
## K-means clustering with 5 clusters of sizes 28, 29, 22, 21, 50
##
## Cluster means:
    Sepal.Length Sepal.Width Petal.Length Petal.Width
## 1
         5.532
                    2.636
                              3.961
                                        1.229
## 2
         6.197
                    2.883
                              5.183
                                        1.934
## 3
         7.123
                    3.114
                              6.032
                                        2.132
## 4
                    2.919
          6.424
                              4.605
                                        1.438
## 5
          5.006
                    3.428
                              1.462
                                        0.246
##
## Clustering vector:
    ## [141] 3 2 2 3 3 2 2 2 2 2
##
## Within cluster sum of squares by cluster:
## [1] 9.749 8.738 11.540 4.650 15.151
## (between_SS / total_SS = 92.7 %)
##
## Available components:
##
## [1] "cluster"
                              "totss"
                                           "withinss"
                  "centers"
## [5] "tot.withinss" "betweenss"
                              "size"
                                           "iter"
## [9] "ifault"
# Compare the Species label with the clustering result
table(iris$Species, kc$cluster)
##
##
              1 2 3 4 5
##
              0 0 0 0 50
    setosa
    versicolor 27 2 0 21 0
##
##
    virginica
             1 27 22 0 0
# This result shows that cluster "setosa" can be easily separated from the other
# clusters, and that clusters "versicolor" and "virginica" are to a small degree
# overlapped with each other.
# Plot the clusters and their centres. Note that there are four dimensions in the data
# and that only the first two dimensions are used to draw the plot below.
# Some black points close to the green centre (asterisk) are actually closer
# to the black centre in the four dimensional space.
par(mfrow=c(1,1)) # make sure only 1 plot per page
plot(newiris[c("Sepal.Length", "Sepal.Width")], col=kc$cluster, pch=20,cex=2)
points(kc$centers[,c("Sepal.Length", "Sepal.Width")], col=1:5, pch=8, cex=3)
```



#