k-means Clustering of the Old Faithful Dataset

Jon Kinsey

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```
# Old Faithful Geyser Data
# Waiting time between eruptions and the duration of the eruption for the
# Old Faithful geyser in Yellowstone National Park, Wyoming, USA.
# The dataset contains 272 observations on 2 variables.
# [,1] eruptions numeric Eruption time in mins
# [,2] waiting numeric Waiting time to next eruption (in mins)
names (faithful)
## [1] "eruptions" "waiting"
str(faithful) # structure
## 'data.frame':
                    272 obs. of 2 variables:
## $ eruptions: num 3.6 1.8 3.33 2.28 4.53 ...
   $ waiting : num 79 54 74 62 85 55 88 85 51 85 ...
attributes(faithful) # attributes
## $names
## [1] "eruptions" "waiting"
##
## $row.names
##
    [1]
          1
                  3
                       4
                              6
                                 7
                                      8
                                           9 10 11 12 13 14
                                                                  15 16
                           5
    [18]
         18
             19
                 20
                     21
                          22
                              23
                                 24
                                      25
                                          26
                                              27
                                                  28
                                                      29
                                                          30
                                                              31
                                                                  32
##
  [35] 35
              36
                 37
                     38
                         39
                              40 41
                                      42
                                          43
                                              44
                                                  45
                                                      46
                                                          47
                                                              48
                                                                  49
  [52] 52
              53
                 54
                     55
                         56
                              57
                                  58
                                      59
                                          60
                                              61
                                                  62
                                                      63
                                                              65
                                                                  66
                 71
                             74
   [69] 69
              70
                     72
                         73
                                 75
                                      76
                                         77
                                              78
                                                  79
                                                      80
                                                          81
                                                              82
                                                                  83
   [86] 86
              87
                 88
                     89
                         90
                             91
                                 92
                                      93
                                         94
                                              95
                                                  96
                                                      97
                                                          98
                                                              99 100 101 102
## [103] 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119
## [120] 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136
## [137] 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153
## [154] 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170
## [171] 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187
## [188] 188 189 190 191 192 193 194 195 196 197 198 199 200 201 202 203 20<del>4</del>
## [205] 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221
## [222] 222 223 224 225 226 227 228 229 230 231 232 233 234 235 236 237 238
## [239] 239 240 241 242 243 244 245 246 247 248 249 250 251 252 253 254 255
## [256] 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272
##
## $class
## [1] "data.frame"
summary(faithful)
```

```
##
      eruptions
                        waiting
##
    Min.
            :1.60
                            :43.0
                    Min.
                     1st Qu.:58.0
    1st Qu.:2.16
   Median:4.00
                    Median:76.0
##
##
    Mean
            :3.49
                    Mean
                            :70.9
    3rd Qu.:4.45
                     3rd Qu.:82.0
##
    Max.
            :5.10
                    Max.
                            :96.0
ssPlot <- function(data, maxCluster = 4) {</pre>
  # Initialize within sum of squares
  SSw <- (nrow(data) - 1) * sum(apply(data, 2, var))
  SSw <- vector()
  for (i in 1:maxCluster) {
    SSw[i] <- sum(kmeans(data, centers = i)$withinss)</pre>
  }
  plot(1:maxCluster, SSw, type = "b", xlab = "Number of Clusters", ylab = "Within groups sum of squares
ssPlot(faithful)
      50000
Within groups sum of squares
      30000
      10000
             1.0
                         1.5
                                      2.0
                                                  2.5
                                                                           3.5
                                                                                       4.0
                                                              3.0
                                         Number of Clusters
(kf <- kmeans(faithful, 2))</pre>
## K-means clustering with 2 clusters of sizes 100, 172
##
## Cluster means:
     eruptions waiting
##
## 1
         2.094
                  54.75
```

2

##

4.298

Clustering vector:

80.28

```
##
              3
                  4
                      5
                           6
                               7
                                    8
                                        9
                                           10
                                                11
                                                   12
                                                        13
                                                            14
                                                                 15
                                                                      16
                                                                          17
##
     2
         1
              2
                  1
                      2
                           1
                               2
                                    2
                                        1
                                            2
                                                 1
                                                     2
                                                          2
                                                              1
                                                                  2
                                                                      1
                                                                           1
                                                                               2
##
    19
        20
             21
                 22
                     23
                          24
                              25
                                   26
                                       27
                                           28
                                                29
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                                                        31
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                                                                      34
                                                                          35
                                                                              36
         2
                                                 2
##
     1
              1
                  1
                      2
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                                    2
                                        1
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##
    37
        38
             39
                 40
                     41
                          42
                              43
                                   44
                                       45
                                           46
                                                47
                                                    48
                                                        49
                                                             50
                                                                 51
                                                                      52
                                                                          53
                                                                              54
         2
                  2
                      2
                           1
                               2
                                        2
                                            2
                                                          2
                                                                  2
                                                                       2
                                                                                2
##
     1
              1
                                    1
                                                 1
                                                     1
                                                              1
                                                                           1
            57
                 58
                     59
                          60
                                  62
                                       63
                                                65
                                                        67
##
    55
        56
                              61
                                           64
                                                    66
                                                             68
                                                                 69
                                                                      70
                                                                          71
##
     1
         2
              2
                  1
                      2
                           2
                               1
                                    2
                                        1
                                            2
                                                 1
                                                     2
                                                          2
                                                              2
                                                                   1
                                                                       2
                                                                           2
                                                                                1
##
    73
        74
             75
                 76
                     77
                          78
                              79
                                   80
                                       81
                                           82
                                                83
                                                    84
                                                        85
                                                             86
                                                                 87
                                                                      88
                                                                          89
                                                                              90
         2
                  2
                           2
                               2
                                    2
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                                                 2
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                                                                       2
                                                                                2
##
     2
              1
                      1
                                             2
                                                     1
                                                              2
                                                                           1
    91
        92
            93
                 94
                     95
                          96
                              97
                                  98
                                       99 100 101 102 103 104 105 106 107 108
                  2
                           2
         2
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                                    2
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                                                                   2
##
              1
                      1
                                        1
                                             2
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                                                                       1
## 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126
##
     2
              2
                  1
                      2
                           2
                               1
                                    2
                                        1
                                             2
                                                 1
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                                                              2
## 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144
         2
              1
                  2
                      1
                           2
                               1
                                    2
                                        1
                                            2
                                                 1
                                                     2
                                                          1
                                                              2
                                                                  2
                                                                       1
                                                                           2
## 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162
                           1
                               2
                                    2
                                        1
                                             2
                                                 2
                                                          2
## 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180
                  2
                      1
                           2
                               1
                                    2
                                        1
                                             1
                                                 2
                                                     2
                                                          2
                                                              2
## 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198
                           2
                               2
                                        2
                                                 2
                                                              2
                      1
                                    1
## 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216
         2
                  2
                      2
                           1
                               2
                                        2
                                             2
                                                 1
                                                     2
                                                          2
                                                              2
                                                                       2
              1
                                    1
                                                                   1
## 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234
         2
              1
                  2
                      1
                           2
                               1
                                    2
                                        2
                                             2
                                                 2
                                                     2
                                                          2
                                                              2
                                                                   2
                                                                       1
                                                                           2
## 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252
                                        2
                                                 2
         1
              1
                  2
                      2
                           1
                               2
                                    1
                                            1
                                                     2
                                                          1
                                                              2
                                                                   1
                                                                       2
                                                                           1
## 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270
     2
         2
              2
                  2
                      2
                           2
                               1
                                    2
                                        2
                                             2
                                                 1
                                                     2
                                                          1
                                                              1
                                                                   2
                                                                       2
## 271 272
##
     1
         2
##
## Within cluster sum of squares by cluster:
## [1] 3456 5446
   (between_SS / total_SS = 82.4 %)
##
## Available components:
##
## [1] "cluster"
                        "centers"
                                        "totss"
                                                         "withinss"
## [5] "tot.withinss" "betweenss"
                                        "size"
                                                         "iter"
## [9] "ifault"
# Compare the eruptions label with the clustering result
table(faithful$eruptions, kf$cluster)
##
##
           1 2
##
           1 0
     1.6
##
     1.667 1 0
```

##

##

##

1.7

1.733 1 0

1.75 6 0

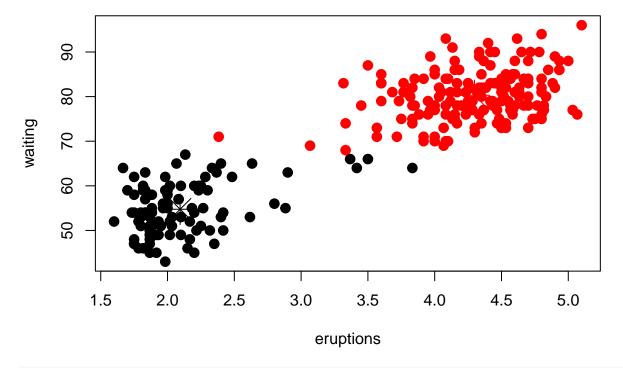
1 0

```
1.783 2 0
##
     1.8 40
##
##
     1.817 3 0
##
     1.833 7 0
     1.85 2 0
##
##
     1.867 8 0
     1.883 4 0
##
##
     1.917 2 0
##
     1.933 2 0
##
     1.95 1 0
##
     1.967 3 0
##
     1.983 3 0
     2 4 0
##
##
     2.017 3 0
##
     2.033 2 0
     2.067 1 0
##
##
     2.083 2 0
##
     2.1 3 0
##
     2.133 1 0
     2.15 1 0
##
     2.167 2 0
##
     2.183 1 0
##
##
     2.2 3 0
     2.217 1 0
##
##
     2.233 2 0
##
     2.25 2 0
##
     2.267 1 0
##
     2.283 1 0
##
     2.3 1 0
##
     2.317 1 0
     2.333 1 0
##
##
     2.35 1 0
##
     2.367 1 0
##
     2.383 0 1
     2.4 2 0
##
##
     2.417 2 0
     2.483 1 0
##
##
     2.617 1 0
     2.633 1 0
##
##
     2.8 1 0
##
     2.883 1 0
##
     2.9 1 0
##
     3.067 0 1
##
     3.317 0 1
##
     3.333 0 2
##
     3.367 1 0
##
     3.417 1 0
##
     3.45 0 1
##
     3.5 1 1
##
     3.567 0 2
##
     3.6 0 4
     3.683 0 1
##
##
     3.717 0 1
##
     3.733 0 1
```

```
3.75 0 1
##
     3.767 0 2
##
##
     3.817 0 1
##
     3.833 1 4
     3.85 0 2
##
##
     3.883 0 1
     3.917 0 3
##
     3.95 0 2
##
##
     3.966 0 1
##
     3.967 0 1
##
     4 0 6
##
     4.033 0 2
##
     4.05 0 1
     4.067 0 2
##
##
     4.083 0 5
     4.1 0 2
##
##
     4.117 0 2
     4.133 0 2
##
     4.15 0 4
##
     4.167 0 4
##
     4.183 0 1
##
##
     4.2 0 1
##
     4.233 0 3
     4.25 0 4
##
##
     4.267 0 2
     4.283 0 2
##
##
     4.3 0 2
##
     4.317 0 1
     4.333 0 5
##
##
     4.35 0 4
     4.366 0 1
##
##
     4.367 0 3
##
     4.383 0 1
     4.4 0 1
##
     4.417 0 4
##
##
     4.433 0 2
     4.45 0 3
##
##
     4.467 0 2
     4.483 0 1
##
     4.5 08
##
     4.517 0 1
##
     4.533 0 5
##
##
     4.55 0 1
##
     4.567 0 3
     4.583 0 4
##
     4.6 0 4
##
     4.617 0 1
##
     4.633 0 3
##
##
     4.65 0 1
##
     4.667 0 2
     4.7 0 6
##
     4.716 0 1
##
##
     4.733 0 1
     4.75 0 1
##
```

```
##
     4.767 0 1
##
     4.783 0 1
     4.8 0 6
##
##
     4.817 0 2
     4.833 0 2
##
     4.85 0 1
##
     4.883 0 1
##
##
     4.9
           0 2
     4.933 0 3
##
##
           0 1
     5.033 0 1
##
##
     5.067 0 1
     5.1 0 1
```

```
#
par(mfrow=c(1,1)) # make sure only 1 plot per page
# plot of waiting time between eruptions and the duration of the eruption
plot(faithful[c("eruptions", "waiting")], col=kf$cluster, pch=20,cex=2)
points(kf$centers[,c("eruptions", "waiting")], col=1:3, pch=8, cex=3)
```



```
#
# cluster centers:
kf$centers
```

```
## 1 eruptions waiting
## 1 2.094 54.75
## 2 4.298 80.28
```