

# A MC-AIXI-CTW Implementation Group Project

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## 1 INTRODUCTION

The AIXI model [Hut05] is an attempt to solve the general AI problem. The AIXI agent interacts with an environment in cycles. Denote by  $\mathcal{A}$ ,  $\mathcal{O}$  and  $\mathcal{R}$  an action, observation and reward space respectively. In each cycle, AIXI takes an action  $a \in \mathcal{A}$  and receives an observation  $o \in \mathcal{O}$  and a reward  $r \in \mathcal{R}$ . The goal of the agent is to maximize the total future reward. AIXI does not require any previous knowledge of an environment, actions are chosen based on past perceptions, which are used to build a model of the environment. More specifically, AIXI chooses in cycle  $k$  an action

$$a_k = \arg \max_{a_k} \sum_{o_k r_k} \dots \max_{a_m} \sum_{o_m r_m} (r_k + \dots + r_m) \sum_{\rho \in \mathcal{M}} 2^{-K(\rho)} \rho(o_1 r_1 \dots o_m r_m | a_1 \dots a_m, \rho)$$

Where  $\mathcal{M}$  is the model class of all chronological semi-computable semi-measures and  $K(\rho)$  is the Kolmogorov Complexity of  $\rho$ .

Unfortunately the AIXI model is uncomputable. For all practical applications, the agent must be approximated. One approach in approximating AIXI is the MC-AIXI-CTW [VNHS09] model. Here the expectimax search is solved by an Monte-Carlo approach. The UTC [KS06] algorithm is used to balance exploration and exploitation. The class of

environment models used in the implementation is a mixture of  $d$ -th order Markov Decision Process. Notably, Context Tree Weighting allows efficient linear time computation of this rather general class of models [WST95].

In comparison to AIXI, at cycle  $k$  MC-AIXI-CTW selects an action

$$a_k = \arg \max_{a_k} \sum_{o_k r_k} \dots \max_{a_m} \sum_{o_m r_m} (r_k + \dots + r_m) \sum_{M \in \mathcal{C}_D} 2^{-\Gamma_D(M)} \rho(o_1 r_1 \dots o_m r_m | a_1 \dots a_m, M)$$

Here  $\mathcal{C}_D$  is the class of all prediction suffix trees of maximum depth  $D$ , and  $\Gamma_D(M)$  is the description length of a context tree  $M$ .

In the following we present our implementation of the MC-AIXI-CTW model. In Section 2 we explain how to use the program and specify different options. Section 3 describes the results of the model on several experimental environments.

## 2 USER MANUAL

Our approximation of aixi is written in C++ and requires g++ for compilation.

### 2.1 SETUP

Compile:

```
cd aixi
make
```

Run:

```
./aixi file.conf [--option1=value1 --option2=value2 ...]
```

Include trained ctw data?? I think this is a good idea Johannes

### 2.2 CONFIGURATION OPTIONS

Options can be either specified in the configuration file or passed directly as `--option=value` to the program. Several configuration files are available, each specifies a particular environment and a set of default options.

#### AVAILABLE OPTIONS

`--ENVIRONMENT=ENV` Specifies the environment. Available environments are

- biased\_rock\_paper\_scissor
- coinflip
- kuhn\_poker
- pacman
- tiger

--MC-TIMELIMIT= $N$  The number  $N$  of MC simulations per cycle.

--WRITE-CT=FILE Write CTW to file before agent termination.

--LOAD-CT=FILE Specifies a (trained) CTW for the agent to load at initialisation.

--LOG=FILE

--TERMINATE-AGE= $N$  The number  $N$  of agent/environment interaction cycles.

--EXPLORATION= $P$  Probability  $0 \leq P \leq 1$  that a action is chosen randomly.

--EXPLORE-DECAY= $D$  Decay  $0 \leq D \leq 1$  of exploration constant.  $P$  is multiplied by  $D$  in each cycle.

--INTERMEDIATE-CT=[1|0] If set to 0 , no intermediate context tree at time  $t = 2^k$  is written. Default is 1. (TODO: I actually would prefer default 0 but that's not so important :) Johannes)

### 3 EXPERIMENTAL RESULTS

#### 3.1 EXPERIMENTAL SETUP

TODO: reword the following paragraphs

We evaluate the performance of our agent on five sample environments. For each environment the agent was allowed 100000 cycles to learn a model. During the learning process an exploratory constant was used. The performance of the model after various amounts of experience was then evaluated by running the agent without exploration for 5000 cycles, and the average reward per cycle reported.

The parameters used for each environment are shown in Figure 3.1. The experiments themselves were performed using a 3.47GHz CPU with 4GB of RAM.

Domain	CTW depth	$m$	$\epsilon$	$\gamma$	$\rho$ UCT Simulations
Biased Rock-Paper-Scissor	32	4	0.999	0.99999	500
Coinflip	x	x	x	x	x00
Kuhn-Poker	42	2	0.99	0.9999	500
Partial Observable Pacman	96	4	0.9999	0.99999	500
Tiger	96	5	0.99	0.9999	500

Figure 3.1: MC-AIXI-CTW model learning configuration

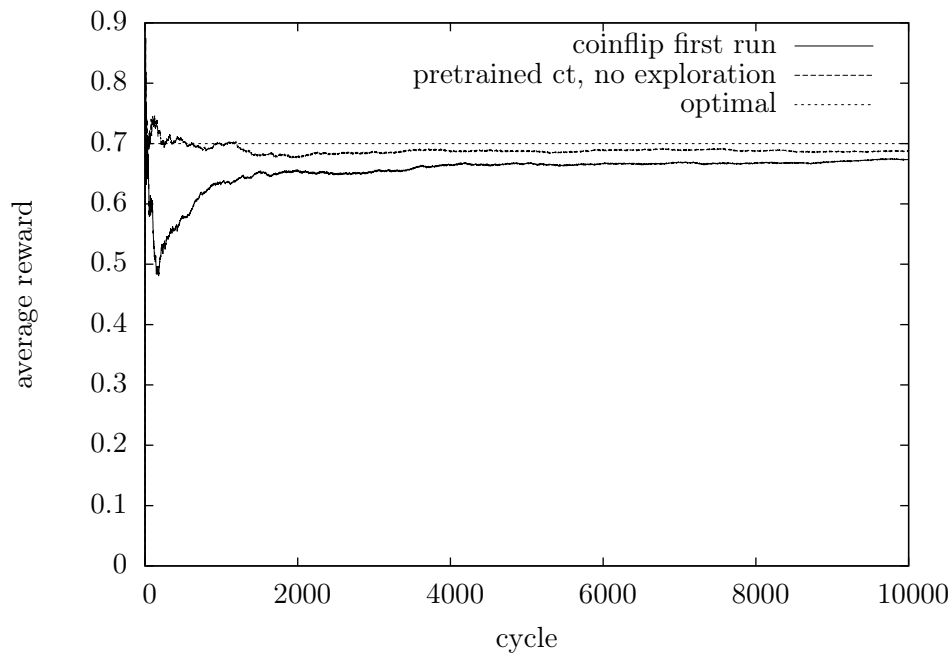


Figure 3.2: Results on the coinflip environment

## 3.2 RESULTS

Present Results/Graphs of each environment. Maybe mention optimal result and/or scale results accordingly

All environments except for Pacman have a known optimal policy and reward.

## 3.3 FURTHER EXPERIMENTS

Include results to do with forgetting past model - changing environments

How does the exploration constant affect learning? (tiger env)

How does aixi handle a change of the environment?

– Compare 0.3 coinflip to 0.7 coinflip

– biased rps vs tiger

## 3.4 DISCUSSION

How well did it do.

Include statistics about cycles required for optimal performance, time per cycle as in the VNHS paper [VNHS09]. Also note the number of simulations required at each cycle for near optimal performance.



Figure 3.3: Average Reward per Cycle vs Experience

## REFERENCES

- [Hut05] Marcus Hutter. *Universal Artificial Intelligence: Sequential Decisions based on Algorithmic Probability*. Springer, Berlin, 2005.
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- [VNHS09] Joel Veness, Kee Siong Ng, Marcus Hutter, and David Silver. A monte carlo aixo approximation. *CoRR*, abs/0909.0801, 2009.
- [WST95] Frans M. J. Willems, Yuri M. Shtarkov, and Tjalling J. Tjalkens. The context tree weighting method: Basic properties. *IEEE Transactions on Information Theory*, 41:653–664, 1995.