Lsn 8

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Power

Recall, in MA206 we tested Hypothesis such as:

 $H_0: \mu = \mu_0 \text{ vs } H_a: \mu \neq \mu_0$

Assuming that H_0 is true, we created a standardized statistic:

$$t = \frac{\bar{X} - \mu_0}{s/\sqrt{n}}$$

Which looks like:

Using $\alpha = 0.05$ our Rejection Region can be generated, which gives the values of t that we would conclude $\mu \neq \mu_0$ for. Note that if $\mu = \mu_a$ we should reject H_a , however there is a chance that we will not:

This region gives the probability of committing a Type-II error for $\mu = \mu_a$. Statistical power is 1-P(Type-II error) or the probability that the researchers find evidence for the alternative hypothesis when the alternative hypothesis is true.

Note that in order to actually find Power or Type-II error we need to specify a value of μ_a . Going back to our picture we see:

So the value chosen for μ_a impacts Power, another thing that impacts Power is n.

For a two-sample or one-sample t-test, finding power in R is straight forward with the command power.t.test. Here we have to input n, $\Delta = |\mu_0 - \mu_a|$ which can be thought of as how big of an effect do we want to observe, s, and/or power. Note that one of these must be blank and is solved for. For instance, if we want to observe an effect of 1 and we assume s = 1, and we have n = 10 observations for group and we are testing $H_0: \mu_1 = \mu_2$ vs $H_a: \mu_1 \neq \mu_2$ we can run

```
##
##
        Two-sample t test power calculation
##
##
                  n = 10
##
             delta = 1
##
                 sd = 1
         sig.level = 0.05
##
##
             power = 0.5619846
       alternative = two.sided
##
##
## NOTE: n is number in *each* group
```

And we see that the power associated with this test is 0.56, or the probability of committing a Type-II error in this instance is 0.44. If we wwant to determine how big of a sample we would need to have 80 % power we would run:

```
##
##
        Two-sample t test power calculation
##
                  n = 16.71477
##
##
             delta = 1
##
                 sd = 1
         sig.level = 0.05
##
##
             power = 0.8
       alternative = two.sided
##
##
## NOTE: n is number in *each* group
```

To see that we would need 17 people in each group.

The same thing can be done with ANOVA tests using library(pwr) which must be installed.

The function pwr.anova.test can then be used in a similar way. The only tricky thing is that it relies on an effect size not given by R^2 but rather given by $f = \sqrt{R^2/(1-R^2)}$. This value is called Cohen's f^2 , which is different than our F statistic. For two samples there's a similar value called Cohen's d statistic which is

```
found via \frac{\bar{x}_1 - \bar{x}_2}{s}. Using Cohen's f we can find power via:
library(pwr)
R2=.1
f = sqrt(R2/(1-R2))
pwr.anova.test(f=f,k=5,n=10)
##
##
        Balanced one-way analysis of variance power calculation
##
                  k = 5
##
##
                  n = 10
##
                  f = 0.3333333
##
          sig.level = 0.05
##
              power = 0.3968709
##
## NOTE: n is number in each group
Which matches Table 1.6.4. We can then change:
R2 = .3
f = sqrt(R2/(1-R2))
pwr.anova.test(f=f,k=5,n=10)
##
##
        Balanced one-way analysis of variance power calculation
##
##
                  k = 5
##
                  n = 10
##
                  f = 0.6546537
##
         sig.level = 0.05
##
              power = 0.9574163
##
## NOTE: n is number in each group
Or change People within group
R2 = .1
f = sqrt(R2/(1-R2))
pwr.anova.test(f=f,k=5,n=20)
##
        Balanced one-way analysis of variance power calculation
##
##
                  k = 5
##
##
                  n = 20
##
                  f = 0.3333333
##
         sig.level = 0.05
##
              power = 0.7431771
##
## NOTE: n is number in each group
```