

Array Rotation Solution with formula

As we know, how we translate 1-d array index into 2-d array index

```
row_index = (1d_index) / 2d_arr[0].length
col_index = (1d_index) % 2d_arr[0].length
```

And vice versa: $1d_index = row_index * 2d_arr[0].length + col_index$

Post right rotation array will follow the `col_index` formula as it is similar to occupy space in next row at `k`th column.

```
(i+k) % n = col_index
(i+k) % n = r
```

```
(0+k)%n = k
(1+k)%n = k+1
(2+k)%n = k+2
```

```
...
(x+k)%n = 0; when x+k = n
...
(n-1+k)%n = k-1;
```

formula : $r = (i+k)\%n$
`i` - represents index of array
`k` - represents rotation count
`n` - represents size of the array
`r` - represents index post rotation

CASE_A: Single transitive-iteration-cycle, i.e. when $GCD(n,k) = 1$

lets say array size is 5 and $k=2$

```
(i+k)% n = r
(0+2)%5 = 2
(1+2)%5 = 3
(2+2)%5 = 4
(3+2)%5 = 0
(4+2)%5 = 1
```

0 -> 2 -> 4 -> 1 -> 3 -> 0

There is single transitive-iteration-cycle starting at 0.

CASE_B: Multiple transitive-iteration-cycle i.e when $GCD(n,k) > 1$

lets say array size is 6 and $k=2$

```
(i+k)% n = r
(0+2)%6 = 2
(1+2)%6 = 3
(2+2)%6 = 4
(3+2)%6 = 5
(4+2)%6 = 0
(5+2)%6 = 1
```

There are two contiguous transitive-iteration-cycle starting at contiguous indices 0, 1

0 -> 2 -> 4 -> 0

1 -> 3 -> 5 -> 1

This method works by rotating an array in-place by using cyclic replacements. This approach involves repeatedly moving elements to their correct positions one step at a time until all elements are in their correct positions.

Juggling algorithm for array-rotation

Total number of transitive-iteration-cycles : $\text{GCD}(n,k)$
Total elements in a transitive-iteration-cycle : $n/\text{GCD}(n,k)$
Each transitive-iteration-cycle is mutually exclusive.

Why is it that once we finish a cycle, we start the new cycle from the next element i.e. can't the next element be already a part of a processed cycle?
<https://leetcode.com/problems/rotate-array/solutions/259418/clear-cyclic-replacement-java-solution-with-proof-o-n-in-time-o-1-in-space/>

Time complexity: $O(n)$, because loop is getting iterated only once, that is we scan each element once combined inner+outer loop.

formula : $r = (i+k)\%n$
 i - represents index of array
 k - represents rotation count
 n - represents size of the array
 r - represents index post rotation

Let's try to figure-out iteration pattern for case $\text{GCD}(n,k) > 1$

3 iterations cycles starting at 0, 1, 2

$(0+3)\%6 = 3$
$(1+3)\%6 = 4$
$(2+3)\%6 = 5$
$(3+3)\%6 = 0$
$(4+3)\%6 = 1$
$(5+3)\%6 = 2$

Here, there will be 3 transitive-iteration cycles which covers all the elements:

1. $0 \rightarrow 3 : 3 \rightarrow 0$
2. $1 \rightarrow 4 : 4 \rightarrow 1$
3. $2 \rightarrow 5 : 5 \rightarrow 2$

Note: Iteration cycle start nodes are sequential. 0,1,2

Two iterations cycles starting at 0, 1

$(0+2)\%6 = 2$
$(1+2)\%6 = 3$
$(2+2)\%6 = 4$
$(3+2)\%6 = 5$
$(4+2)\%6 = 0$
$(5+2)\%6 = 1$

Here, there will be 2 transitive-iteration cycles which covers all the elements:

1. $0 \rightarrow 2 : 2 \rightarrow 4 : 4 \rightarrow 0$
2. $1 \rightarrow 3 : 3 \rightarrow 5 : 5 \rightarrow 1$

Note: Iteration cycle start nodes are sequential. 0,1

So, finally for case when $\text{GCD}(n,k) > 1$, outer loop needs to start the transitive-iteration cycles in sequence until we reach to the total count of elements. Since, for case when $\text{GCD}(n,k) = 1$ there will be only single transitive-iteration cycle, means we need to put the total count calculation for inner loop as well.

```

public static void rotate(int[] nums, int k) {
    int n = nums.length;
    k %= n; // to handle cases where k is greater than the length of the array
    int count = 0;
    for (int startIndex = 0; count < n; startIndex++) {
        count = iterateTransitiveCycle(nums, n, k, startIndex, count);
    }
}

```

```

/**
 * A transitive cycle ends when it reaches the same index where it started.
 *
 */
private static int iterateTransitiveCycle(int[] nums, final int n, final int k, final int startIndex, int count) {
    int idx = startIndex;
    int nextIdx = Integer.MIN_VALUE;

    int prevElement = nums[idx];

    while (nextIdx != startIndex) {
        nextIdx = (idx + k) % n;

        // rotate the element
        int temp = nums[nextIdx];
        nums[nextIdx] = prevElement;
        prevElement = temp;

        idx = nextIdx;
        count++;
    }

    return count;
}

```
