Third-party maxima software

John Lapeyre

August 20, 2013

Contents

1 Array Representation For Expressions

Maxima expressions are normally implemented internally as lisp lists, but they may also be represented by lisp arrays. Each representation has advantages.

2 Attributes

A function may possess a list of attributes. The attributes control how the arguments to the function are evaluated and how errors are handled.

- attributes
- set_match_form
- set_nowarn
- unset_match_form
- unset_nowarn

2.1 Function: attributes

attributes(name)

Description Returns a list of the 'attributes' of function *name*.

Arguments attributes requires one argument *name*, which must be a string or a symbol.

See also unset_match_form, set_match_form, set_nowarn, and unset_nowarn.

2.2 Function: set_match_form

 $set_match_form(names)$

Description Set the 'match_form' attribute for function(s) *names*. If the argument checks for a function call fail, and the attribute 'match_form' is set, then rather than signaling an error, the unevaluated form is returned. Furthemore, if the attribute 'nowarn' is not set, then a warning message is printed.

Arguments set_match_form requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also unset_match_form, set_nowarn, unset_nowarn, and attributes.

2.3 Function: set_nowarn

 $set_nowarn(names)$

Description Set the 'nowarn' attribute for function(s) *names*. If the argument checks for a function call fail, and the attribute 'match_form' is set, and the attribute 'nowarn' is set, then rather than signaling an error, the unevaluated form is returned and no warning message is printed.

Arguments set_nowarn requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also unset_match_form, set_match_form, unset_nowarn, and attributes.

2.4 Function: unset_match_form

 $unset_match_form(names)$

Description Unset the 'match_form' attribute for function(s) names. If the argument checks for a function call fail, and the attribute 'match_form' is set, then rather than signaling an error, the unevaluated form is returned. Furthemore, if the attribute 'nowarn' is not set, then a warning message is printed.

Arguments unset_match_form requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also set_match_form, set_nowarn, unset_nowarn, and attributes.

2.5 Function: unset_nowarn

 $unset_nowarn(names)$

Description Unset the 'nowarn' attribute for function(s) *names*. If the argument checks for a function call fail, and the attribute 'match_form' is set, and the attribute 'nowarn' is set, then rather than signaling an error, the unevaluated form is returned and no warning message is printed.

Arguments unset_nowarn requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also unset_match_form, set_match_form, set_nowarn, and attributes.

3 Functions and Variables for Array Represention for Expressions

These functions operate on the the array expression data structure.

- aeop
- aex
- aex_cp
- aex_get
- aex_new
- aex_set
- aex_shift
- aex_unshift

- aexg
- aexs
- copy_aex_type
- iapply
- ilength
- ipart
- ipart_set
- ireverse
- lex

3.1 Function: aeop

aeop(expr)

mext package: aex

Description op function for aex. returns op if e is not an aex.

Arguments aeop requires one argument *expr*, which must be non-atomic.

3.2 Function: aex

 $\mathbf{aex}(:$ optional x) mext package: aex

Calling

 $\mathbf{aex}(e)$ Converts expression e to an array representation. The input expression e is returned unchanged if it is already an array expression or is a symbol or number or specially represented maxima expression. This function converts only at the first level.

Arguments aex requires either zero or one arguments.

Options aex takes options with default values: adj->true.

3.3 Function: aex_cp

 $\mathbf{aex_cp}(e : \mathbf{optional} \ head)$ mext package: \mathbf{aex}

Calling

 $\mathbf{aex_cp}(e)$ Returns an aex form copy of e. e may be in either lex or aex form. Conversion to aex representation occurs only on the first level.

Arguments aex_cp requires either one or two arguments. The first argument e must be non-atomic.

Options aex_cp takes options with default values: adj->true.

3.4 Function: aex_get

Description Returns the n-1th part of aexpr e. A value of n less than 0 is not allowed. This is more efficient than aexg, which returns the head of the expression when n is equal to zero.

Examples

```
(%i1) a : aex([5,6,7]), aex_get(a,2);
(%o1) 7
```

3.5 Function: aex new

```
aex_new(n :optional head)
mext package: aex
```

Arguments aex_new requires either one or two arguments. The first argument n must be a non-negative integer.

3.6 Function: aex_set

Description Destructively sets the nth part of aexpr e to value v. A value of 0 for n is not allowed. This is more efficient than aexs. No argument checking is done.

Examples

Destructively assign to a part of an expression.

```
(%i1) a : aex([1,2,3]), aex_set(a,1,x), a;
(%o1) <[1,x,3]>
```

See also aexs and ipart.

3.7 Function: aex_shift

```
\mathbf{aex\_shift}(e) mext package: aex
```

Description destructively removes an element from the end of e. For array representation of expressions we use the words 'push' and 'pop' for the beginning of and expression, and 'shift' and 'unshift' for the end of an expression, whether the representation is an array or a list. This is consistent with maxima, but the reverse of the meaning of the terms in perl.

Arguments aex_shift requires one argument e, which must be an adjustable array expression.

Examples

```
(%i1) a : lrange(10,ot->ar);
(%o1) <[1,2,3,4,5,6,7,8,9,10]>
(%i1) b : aex_shift(a);
(%o1) 10
(%i2) a;
(%o2) <[1,2,3,4,5,6,7,8,9]>
```

3.8 Function: aex_unshift

 $\mathbf{aex_unshift}(v, e)$ mext package: aex

Description Destructively pushes an element v onto the end of e. The return value is v. For array representation of expressions we use the words 'push' and 'pop' for the beginning of and expression, and 'shift' and 'unshift' for the end of an expression, whether the representation is an array or a list. This is consistent with maxima, but the reverse of the meaning of the terms in perl.

Arguments aex_unshift requires two arguments. The second argument e must be an adjustable array expression.

Examples

```
(%i1) a : lrange(10,ot->ar), aex_unshift("dog",a), a;
(%o1) <[1,2,3,4,5,6,7,8,9,10,"dog"]>
```

3.9 Function: aexg

Description aexg(e,n) returns the nth part of aexpr e. If n is 0, the head of e is returned. No argument checking is performed.

See also aex_get, ipart, inpart, and part.

3.10 Function: aexs

Description destructively sets the nth part of aexpr e to value v. A value of 0 for n returns the head (or op) of e.

3.11 Function: copy_aex_type

copy_aex_type(ein)
mext package: aex

Description Create a new aex with same head, length, adjustability, etc. but contents of expression are not copied.

Arguments copy_aex_type requires one argument *ein*, which must be an array-representation expression.

3.12 Function: iapply

iapply(fun, arg)
mext package: aex

Description iapply is like maxima apply, but it supports aex lists. *arg* is converted to an ml if it is an aex expression. By default, output is ml regardless of the input representation.

Arguments iapply requires two arguments. The first argument fun must be a function. The second argument arg must be non-atomic.

Options iapply takes options with default values: adj->true, ot->ml.

Examples

```
(%i1) iapply(%%ff,lrange(4));
(%o1) %%ff(1,2,3,4)
```

```
(%i1) iapply(%%ff,lrange(4,[ot->ar]));
(%o1) %%ff(1,2,3,4)
```

```
(%i1) iapply(%%ff,lrange(4,[ot->ar]), [ot->ar]);
(%o1) %%ff<1,2,3,4>
```

```
(%i1) iapply(%%ff,lrange(4), [ot->ar]);
(%o1) %%ff<1,2,3,4>
```

3.13 Function: ilength

ilength(e)

mext package: aex

Description Returns the length of the expression e. This is like maxima length, but here, e can be either an aex or a lex.

Arguments ilength requires one argument *e*, which must be a subscripted variable or non-atomic.

3.14 Function: ipart

Calling

ipart(e, ind1, ind2, ...) Returns the part of expression e specified by indices. e may be a mixed (lex and aex) representation expression. When used as an lvalue, ipart can be used to assign to a part of an expression. If an index is negative, then it counts from the end of the list. If e is an ordinary maxima list (lex), then using a negative index is potentially slower than using a positive index because the entire list must first be traversed in order to determine it's length. If e is in aex representation, then this inefficiency is not present.

Examples

Destructively assign to a part of an exression.

```
(%i1) (a : [1,2,3], ipart(a,1) : 7, a);
(%o1) [7,2,3]
```

Implementation Some tests were performed with large lists of numbers. If we set a:lrange(10^7), then the times required for ipart(a,10^7), ipart(a,-1), inpart(a,10^7), and part(a,10^7) were 30, 60, 90, and 90 ms.

3.15 Function: ipart_set

Calling

 $ipart_set(e, val, ind1, ind2, ...)$ Set part of e specified by the final arguments to val. e is a mixed representation expression.

3.16 Function: ireverse

ireverse(e)

mext package: aex

Description ireverse is like maxima reverse, but is works on both aex and list objects. ireverse is tries to be identical to maxima reverse for a non-aex argument.

Arguments ireverse requires one argument e, which must be non-atomic.

Options ireverse takes options with default values: adj->true, ot->ml.

Examples

```
(%i1) ireverse(lrange(4));
(%o1) [4,3,2,1]
```

```
(%i1) ireverse(lrange(4), [ot->ar]);
(%o1) <[4,3,2,1]>
```

```
(%i1) ireverse(lrange(4, [ot->ar]));
(%o1) <[4,3,2,1]>
```

```
(%i1) ireverse(lrange(4, [ot->ar]), [ot->ml]);
(%o1) [4,3,2,1]
```

3.17 Function: lex

Calling

lex(e) converts the aex expression e to lex. If e is not an aex expression, e is returned. Conversion is only done on the first level.

4 Functions and Variables for Combinatorics

- ae_random_permutation
- cycles_to_perm
- ullet inverse_permutation
- perm_to_cycles
- perm_to_transpositions
- permutation_p
- permutation_p1
- random_cycle
- random_permutation_sym
- signature_permutation
- transpositions_to_perm

4.1 Function: ae_random_permutation

$ae_random_permutation(a)$

mext package: discrete_aex

Description returns a with subexpressions permuted randomly.

Arguments ae_random_permutation requires one argument a, which must be non-atomic.

Options ae_random_permutation takes options with default values: adj->true, ot->ml.

See also random_cycle, random_permutation_sym, signature_permutation, perm_to_cycles, and cycles_to_perm.

4.2 Function: cycles_to_perm

cycles_to_perm(cycles)
mext package: discrete_aex

Description Returns a permutation from its cycle decomposition cycles, which is a list of lists. Here 'permutation' means a permutation of a list of the integers from 1 to some number n. The default output representation is aex.

Arguments cycles_to_perm requires one argument cycles, which must be a list (lex or aex).

Options cycles_to_perm takes options with default values: adj->true, ot->ml.

See also random_cycle, random_permutation_sym, ae_random_permutation, signature_permutation, and perm_to_cycles.

4.3 Function: inverse_permutation

inverse_permutation(perm)

mext package: discrete_aex

Description Returns the inverse permutation of *perm*.

Arguments inverse_permutation requires one argument *perm*, which must be a list (lex or aex).

Options inverse_permutation takes options with default values: adj->true, ot->ml.

Examples

```
(%i1) inverse_permutation([5,1,4,2,6,8,7,3,10,9]);

(%o1) <[2,4,8,3,1,5,7,6,10,9]>

(%i1) inverse_permutation(inverse_permutation([5,1,4,2,6,8,7,3,10,9]),ot->ml);

(%o1) [5,1,4,2,6,8,7,3,10,9]
```

4.4 Function: perm_to_cycles

perm_to_cycles(ain)

mext package: discrete_aex

Description Returns a cycle decomposition of the input permutation ain. The input must be a permutation of n integers from 1 through n.

Arguments perm_to_cycles requires one argument *ain*, which must be a list (lex or aex).

Options perm_to_cycles takes options with default values: adj->true, ot->ml.

Examples

```
(%i1) perm_to_cycles([5,4,3,2,1,10,6,7,8,9]);
(%o1) [[7,8,9,10,6],[3],[4,2],[5,1]]
```

See also random_cycle, random_permutation_sym, ae_random_permutation, signature_permutation, and cycles_to_perm.

4.5 Function: perm_to_transpositions

perm_to_transpositions(ain) mext package: discrete_aex

Description Returns a list representing the permutation *ain* as a product of transpositions. The output representation type is applied at both levels.

Arguments perm_to_transpositions requires one argument *ain*, which must be a list (lex or aex).

Options perm_to_transpositions takes options with default values: adj->true, ot->ml.

4.6 Function: permutation_p

$permutation_p(ain)$

 \max package: discrete_aex

Calling

permutation_p(list) Returns true if the list list of length n is a permutation of the integers from 1 through n. Otherwise returns false.

Arguments permutation_p requires one argument.

Implementation Separate routines for aex and lex input are used.

4.7 Function: permutation_p1

$permutation_p1(ain)$

mext package: discrete_aex

Description This is the same as permutation_p, but, if the input is a list, it assumes all elements in the input list are fixnum integers, while permutation_p does not.

Arguments permutation_p1 requires one argument.

Implementation Some variables are declared fixnum, but this does not seem to improve performance with respect to permutationp.

4.8 Function: random_cycle

$random_cvcle(n)$

mext package: discrete_aex

Calling

 $random_cycle(n)$ Returns a random cycle of length n. The return value is a list of the integers from 1 through n, representing an element of the symmetric group S_n that is a cycle.

Arguments random_cycle requires one argument n, which must be a positive integer.

Options random_cycle takes options with default values: adj->true, ot->ml.

See also random_permutation_sym, ae_random_permutation, signature_permutation, perm_to_cycles, and cycles_to_perm.

Implementation This function uses Sattolo's algorithm.

4.9 Function: random_permutation_sym

$random_permutation_sym(n)$

mext package: discrete_aex

Calling

random_permutation_sym(n) Returns a random permutation of the integers from 1 through n. This represents a random element of the symmetric group S_n .

Arguments random_permutation_sym requires one argument n, which must be a positive integer.

Options random_permutation_sym takes options with default values: adj->true, ot->ml.

See also random_cycle, ae_random_permutation, signature_permutation, perm_to_cycles, and cycles_to_perm.

4.10 Function: signature_permutation

${\bf signature_permutation}(\mathit{ain})$

mext package: discrete_aex

Calling

signature_permutation(list) returns the sign, or signature, of the symmetric permutation list, which must be represented by a permutation the integers from 1 through n, where n is the length of the list.

Arguments signature permutation requires one argument *ain*, which must be a list (lex or aex).

See also random_cycle, random_permutation_sym, ae_random_permutation, perm_to_cycles, and cycles_to_perm.

4.11 Function: transpositions_to_perm

$transpositions_to_perm(ain)$

mext package: discrete_aex

Description Returns the permutation specified by the list of transpositions ain.

Arguments transpositions_to_perm requires one argument ain, which must be a list (lex or aex).

Options transpositions_to_perm takes options with default values: adj->true, ot->ml.

Implementation Input is converted to lex on both levels. Default output is aex.

5 Functions and Variables for Documentation

- doc_system_list
- error_code
- maxdoc

- maxdoc_author
- maxdoc_copyright
- maxdoc_examples
- maxdoc_set_cur_sec
- maxdoc_set_mext_package
- maxdoc_split_text
- mext_package_record
- pager_command
- print_authors
- \bullet print_copyrights
- print_entry_latex
- print_implementation
- print_maxdoc_entry
- print_maxdoc_sections
- print_sections_latex
- read_docs_with_pager
- set_all_doc_systems
- simple_doc_add
- simple_doc_delete
- simple_doc_get
- simple_doc_init
- simple_doc_print

5.1 Variable: doc_system_list

default value false.

Description A list of the documentation systems that will be searched by ? and ??. This can be set to all avaliable systems with the function set_all_doc_systems. If this variable is false, then all documentation is enabled.

5.2 Variable: error_code

default value false.

Description This is an error code set by merror1.

5.3 Function: maxdoc

maxdoc(name, docs) mext package: defmfun1

Description Add maxdoc documentation entry for item *name* specified by *docs*.

Arguments maxdoc requires two arguments. The first argument name must be a string.

Attributes maxdoc has attributes: [hold_all]

5.4 Function: maxdoc_author

maxdoc_author(name, author)

mext package: defmfun1

Description Set the author(s) for the documentation item *name*.

Arguments maxdoc_author requires two arguments. The first argument *name* must be a string. The second argument *author* must be a string or a list of strings.

5.5 Function: maxdoc_copyright

maxdoc_copyright(name, copyright)

mext package: defmfun1

Description Set the copyright information for the documentation item *name*. *copyright* should typically be a list whose first element is an integer (the year), with the remaining strings naming the copyright holder. This copyright information will not be printed with documentation, unless *print_copyrights* is true.

Arguments maxdoc_copyright requires two arguments. The first argument name must be a string.

5.6 Function: maxdoc_examples

maxdoc_examples(name :rest examples)

mext package: defmfun1

Description Add maxdoc examples entry for item name specified by examples.

Arguments maxdoc_examples requires one or more arguments. The first argument name must be a string.

Attributes maxdoc_examples has attributes: [hold_all]

5.7 Function: maxdoc_set_cur_sec

 $maxdoc_set_cur_sec(shortname)$

mext package: defmfun1

Description Set the current section for maxdoc to *shortname*. This section will be used by functions such as maxdoc, and maxdoc_author.

Arguments maxdoc_set_cur_sec requires one argument *shortname*, which must be a string.

5.8 Function: maxdoc_set_mext_package

maxdoc_set_mext_package(packagename)

mext package: defmfun1

Description Set the current mext package name for maxdoc to *packagename*. This name will be used by functions specifying documentation for functions until the name is set to another value. When documenting functions written in maxima code, calling mext_record_package is probably more useful.

Arguments maxdoc_set_mext_package requires one argument packagename, which must be a string.

5.9 Function: maxdoc_split_text

maxdoc_split_text(text)
mext package: defmfun1

Description Split the string *text* into a list of strings, using a sequence of one or more spaces as the delimeter. Single newlines are removed.

Arguments maxdoc_split_text requires one argument text, which must be a string.

5.10 Function: mext_package_record

mext_package_record(docitem, packagename)

mext package: defmfun1

Description Set the mext packagename for the function or variable *docitem* to *packagename*. This name will be used when displaying documentation. The function maxdoc_set_mext_package is useful for setting the package name of a group of functions, but there is currently no maxima hook for doing this.

Arguments mext_package_record requires two arguments. The first argument *docitem* must be a string or a symbol. The second argument *packagename* must be a string.

5.11 Variable: pager_command

default value /usr/bin/less.

Description The pathname to the system command used for paged output, for instance, for reading documentation.

5.12 Variable: print_authors

default value true.

Description If true, then print the names of the authors with maxdoc documentation.

5.13 Variable: print_copyrights

default value false.

Description If true, then print copyright information with maxdoc documentation.

5.14 Function: print_entry_latex

print_entry_latex(item)
mext package: defmfun1

Arguments print_entry_latex requires one argument *item*, which must be a string.

5.15 Variable: print_implementation

default value true.

Description If true, then print implementation information with maxdoc documentation.

5.16 Function: print_maxdoc_entry

print_maxdoc_entry(item)
mext package: defmfun1

Arguments print_maxdoc_entry requires one argument *item*, which must be a string.

5.17 Function: print_maxdoc_sections

print_maxdoc_sections()
mext package: defmfun1

Description Print all sections of maxdoc documentation. This does not include other documentation databases, such as the main maxima documentation.

Arguments print_maxdoc_sections requires zero arguments.

5.18 Function: print_sections_latex

print_sections_latex(:optional filename)

mext package: defmfun1

Description Print all sections of maxdoc documentation currently loaded in latex format to the file *file-name*. This does not include other documentation databases, such as the main maxima documentation.

Arguments print_sections_latex requires either zero or one arguments. If present, the argument *file-name* must be a a string.

5.19 Variable: read_docs_with_pager

default value false.

Description If true, then documenation printed by describe or ? or ?? is sent through the pager specified by pager_command. This will most likely only work with a command line interface under linux/unix with certain lisp implementations.

5.20 Function: set_all_doc_systems

set_all_doc_systems() mext package: defmfun1

Description Enable all documentation databases for describe, ? and ??. This sets doc_system_list to a list of all doc systems.

Arguments set_all_doc_systems requires zero arguments.

5.21 Function: simple_doc_add

simple_doc_add(name, content)

mext package: defmfun1

Description Adds documentation string *content* for item *name*. These documentation strings are accessible via '?' and '??'.

Arguments simple_doc_add requires two arguments. The first argument name must be a string. The second argument *content* must be a string.

See also simple_doc_init, simple_doc_delete, simple_doc_get, and simple_doc_print.

$Function: simple_doc_delete$ 5.22

 $simple_doc_delete(name)$ mext package: defmfun1

Description Deletes the simple_doc documentation string for item *name*.

Arguments simple_doc_delete requires one argument *name*, which must be a string.

See also simple_doc_init, simple_doc_add, simple_doc_get, and simple_doc_print.

5.23Function: simple_doc_get

 $simple_doc_get(name)$ mext package: defmfun1

Description Returns the simple_doc documentation string for item *name*.

Arguments simple_doc_get requires one argument *name*, which must be a string.

See also simple_doc_init, simple_doc_add, simple_doc_delete, and simple_doc_print.

5.24Function: simple_doc_init

simple_doc_init() mext package: defmfun1

Description Initialize the simple_doc documentation database.

Arguments simple_doc_init requires zero arguments.

See also simple_doc_add, simple_doc_delete, simple_doc_get, and simple_doc_print.

5.25Function: simple_doc_print

 $simple_doc_print(name)$ mext package: defmfun1

Description Prints the simple_doc documentation string for item *name*.

Arguments simple_doc_print requires one argument *name*, which must be a string.

See also simple_doc_init, simple_doc_add, simple_doc_delete, and simple_doc_get.

6 Functions and Variables for Equations

- alt_eigen
- nelder_mead

6.1 Function: alt_eigen

mext package: alt_eigen

```
Description alt_eigen(mat, ['var=x, 'maxdegree=n, 'orthogonal=boolean])
```

Express the eigenvectors of the matrix mat as a polynomial in the eigenvalue var. When the degree of a factor of the characteristic polynomial has degree maxdegree or less, the code attempts to find all the roots of the factor. The optional variables var, maxdegree (default 1), and orthogonal (default false) can be in any order. When the dimension of an eigenspace is greater than one and orthogonal is true, the list of eigenvectors is orthogonal.

Examples The eigenvectors of matrix([1,2],[4,5]), are

```
(%i1) alt_eigen(matrix([1,2],[4,5]),'var=z);
(%o1) [z^2=6*z+3,[matrix([2],[z-1])]]
```

Substituting the two roots of $z^2=6*z+3$ in to the column vector matrix([2],[z-1]) gives the two eigenvectors. To find explicit expressions for these eigenvectors, set maxdegree to 2; thus

Here is a matrix with a degenerate eigenvalue:

```
(%i3) m : matrix([5,6,5,6,5,6],[6,5,6,5,6,5],[5,6,5,6,5,6],[6,5,6,5,6,5],
       [5,6,5,6,5,6],[6,5,6,5,6,5])$
(%i4) alt_eigen(m,'var=z);
(%o4) [z=-3,[matrix([-1],[1],[-1],[1],[-1],[1])],z=0,[matrix([0],[-1],[0],[1],[0]),
       matrix([0],[0],[0],[-1],[0],[1]), matrix([0],[0],[1],[0],[-1],[0]),
       matrix([1],[0],[-1],[0],[0])],z=33,[matrix([-1],[-1],[-1],[-1],[-1])]]
```

There are four eigenvectors with eigenvalue 0. To find an orthogonal basis for this eigenspace, set the optional variable *orthogonal* to true; thus

```
(%i5) alt_eigen(m,'var=z, 'orthogonal=true);

(%o5) [z=-3,[matrix([-1],[1],[-1],[1],[-1],[1])],z=0,[matrix([1],[0],[-1/2],[0],

[-1/2],[0]), matrix([0],[0],[1],[0],[-1],[0]),matrix([0],[-1/2],[0],[-1/2],[0],[1]),

matrix([0],[-1],[0],[1],[0],[0])],z=33,[matrix([-1],[-1],[-1],[-1],[-1])]]
```

Author Barton Willis.

6.2 Function: nelder_mead

nelder_mead(*expr*, *vars*, *init*) mext package: nelder_mead

Description The Nelder-Mead optimization algorithm.

Arguments nelder_mead requires three arguments. The second argument *vars* must be a list of symbols. The third argument *init* must be a list of numbers.

Examples

Find the minimum of a function at a non-analytic point.

```
(%i1) nelder_mead(if x<0 then -x else x^2, [x], [4]);
(%o1) [x = 9.536387892694629e-11]
```

```
(%i1) f(x) := if x<0 then -x else x^2$
(%i2) nelder_mead(f, [x], [4]);
(%o2) [x = 9.536387892694628e-11]
(%i3) nelder_mead(f(x), [x], [4]);
(%o3) [x = 9.536387892694628e-11]
```

```
(%i1) nelder_mead(x^4+y^4-2*x*y-4*x-3*y, [x,y], [2,2]); (%o1) [x = 1.157212489168102,y = 1.099342680267472]
```

Author Mario S. Mommer.

7 Functions and Variables for Function Definition

- comp_load
- compile_file1

7.1 Function: comp_load

comp_load(fname :optional pathlist)
mext package: aex

Description Compile and load a lisp file. Maxima does not load it by default with compile_file. If the input filename does not end with ".lisp", it will be appended. If *pathlist* is specified, then *fname* is only searched for in directories in *pathlist*.

Arguments comp_load requires either one or two arguments. The first argument *fname* must be a string. The second argument *pathlist* must be a string or a list of strings.

7.2 Function: compile_file1

compile_file1(input-file :optional bin-file, translation-output-file) mext package: aex

Description This is copied from maxima compile_file, with changes. Sometimes a loadable binary file is apparently compiled, but an error flag is set and compile_file returns false for the output binary filename. Here we return the binary filename in any case.

Arguments compile_file1 requires between one and three arguments. The first argument *input-file* must be a string.

8 Functions and Variables for Input and Output

- pager_string
- restore
- restore_fast
- store
- store_fast

8.1 Function: pager_string

$\mathbf{pager_string}(s)$ mext package: aex

Description Read the string s in the pager given by the maxima variable pager_command. This works at least with gcl under linux.

Arguments pager_string requires one argument s, which must be a string.

8.2 Function: restore

restore(file)

mext package: store

Calling

restore(file) Reads and returns expressions from the file file.

Description Reads maxima expressions from file *file* created by the function store.

Arguments restore requires one argument *file*, which must be a string.

See also store, store_fast, and restore_fast.

8.3 Function: restore_fast

restore_fast(file) mext package: store

Calling

 $\mathbf{restore_fast}(file)$ Reads and returns expression from the file file. No checking for circular references is done.

Description Reads maxima expressions from file *file* created by the function store, or store_fast. No checks for circular references are done.

Arguments restore_fast requires one argument *file*, which must be a string.

See also store, restore, and store_fast.

8.4 Function: store

```
store(file :rest exprs) mext package: store
```

Calling

store(file, expr1, expr2, ...) stores the expressions to the file file.

Description Stores maxima expressions *exprs* in *file* in binary format. Many types of lisp expressions and subexpressions are supported: numbers, strings, list, arrays, hashtables, structures,....

Arguments store requires one or more arguments. The first argument file must be a string.

Examples

Save a graph to a file. This cannot be done with the command ¡save¿.

```
(%i1) load(graphs)$
(%i2) c : petersen_graph();
(%o2) GRAPH(10 vertices, 15 edges)
(%i3) factor(graph_charpoly(c,x));
(%o3) (x-3)*(x-1)^5*(x+2)^4
(%i4) store("graph.cls",c)$
(%i5) factor(graph_charpoly( restore("graph.cls"), x));
(%o5) (x-3)*(x-1)^5*(x+2)^4
```

See also restore, store_fast, and restore_fast.

Implementation store uses the cl-store library. See the cl-store documentation for more information.

8.5 Function: store_fast

```
\begin{array}{l} \mathbf{store\_fast}(file: \mathrm{rest}\ exprs) \\ \mathrm{mext}\ \mathrm{package:}\ \mathrm{store} \end{array}
```

Calling

store_fast(*file*, *expr1*, *expr2*, ...) stores the expressions to the file *file*. No checking for circular references is done.

Description Stores maxima expressions *exprs* in *file* in binary format. This is like **store**, except that no checks for circular references are done.

Arguments store_fast requires one or more arguments. The first argument file must be a string.

See also store, restore, and restore_fast.

9 Functions and Variables for Lists

These functions manipulate lists. They build lists, take them apart, select elements, etc.

- aelistp
- constant_list
- count
- drop_while

- every1
- fold
- fold_list
- icons
- \bullet imap
- length_while
- lrange
- nest
- nest_list
- nest_while
- nreverse
- partition_list
- select
- sequence specifier
- table
- take
- take_while
- tuples

9.1 Function: aelistp

Description Returns true if e is a list, either ml or ar representation.

Examples

```
(%i1) aelistp([1,2,3]);
(%o1) true
(%i1) aelistp( aex([1,2,3]));
(%o1) true
(%i2) aelistp(3);
(%o2) false
(%i3) aelistp(x);
(%o3) false
(%i4) x:lrange(10),aelistp(x);
(%o4) true
(%i5) aelistp(%%f(y));
(%o5) false
(%i6) aelistp( aex( %%f(y) ));
(%o6) false
```

9.2 Function: constant_list

```
constant_list(expr, list) mext package: lists_aex
```

Description Returns a list of n elements, each of which is an independent copy of expr. constant_list(expr,[n,m,..]) returns a nested list of dimensions n,m,... where each leaf is an independent copy of expr and the copies of each list at each level are independent. If a third argument is given, then it is used as the op, rather than 'list', at every level.

Arguments constant_list requires either two or three arguments. The second argument *spec* must be a positive integer or a list of positive integers.

Options constant_list takes options with default values: adj->true, ot->ml.

See also makelist, lrange, and table.

9.3 Function: count

```
count(expr, item)
mext package: lists_aex
```

Description Counts the number of items in *expr* matching *item*. If *item* is a lambda function then *compile* must be true.

Arguments count requires two arguments. The first argument *expr* must be non-atomic and either aex or represented by a lisp list.

Options count takes options with default values: compile->true.

Examples

```
(%i1) count([1,2,"dog"], 'numberp);
(%o1) 2
(%i1) count([1,2,"dog"], "dog");
(%o1) 1
(%i2) count(lrange(10^4), lambda([x], is(mod(x,3) = 0)));
(%o2) 3333
(%i3) count( %%ff(1,2,"dog"), "dog");
(%o3) 1
(%i4) count(lrange(100,ot->ar), 'evenp);
(%o4) 50
```

9.4 Function: drop_while

```
drop_while(expr, test)
mext package: lists_aex
```

Calling

 $drop_while(expr, test)$ Tests the elements of expr in order, dropping them until test fails. The remaining elements are returned in an expression with the same op as that expr.

Arguments drop_while requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options drop_while takes options with default values: adj->true, ot->ml, compile->true.

Examples

Drop elements as long as they are negative.

```
(%i1) drop_while([-3,-10,-1,3,6,7,-4], lambda([x], is(x<0)));
(%o1) [3,6,7,-4]
```

9.5 Function: every1

every1(expr, test)
mext package: lists_aex

Calling

every1(expr, test) Returns true if test is true for each element in expr. Otherwise, false is returned. This is like **every** but allow a test that takes only one argument. For some inputs, every1 is much faster than every.

Arguments every1 requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options every1 takes options with default values: compile->true.

9.6 Function: fold

mext package: lists_aex

Description fold(f,x,[a,b,c]) returns f(f(f(x,a),b),c).

Arguments fold requires three arguments. The third argument v must be non-atomic.

Options fold takes options with default values: adj->true, ot->ml, compile->true.

See also fold_list and nest.

9.7 Function: fold_list

mext package: lists_aex

Description fold_list(f,x,[a,b,c]) returns [f(x,a),f(f(x,a),b),f(f(f(x,a),b),c)].

Arguments fold_list requires three arguments. The third argument v must be non-atomic.

Options fold_list takes options with default values: adj->true, ot->ml, compile->true.

See also fold and nest.

9.8 Function: icons

icons(x, e)

Description icons is like maxima cons, but less general, and much, much faster. x is a maxima object. e is a maxima list or list-like object, such as [a], or f(a). It is suitable at a minimum, for pushing a number or list or string onto a list of numbers, or strings or lists. If you find icons gives buggy behavior that you are not interested in investigating, use cons instead.

Implementation In a function that mostly only does icons in a loop, icons defined with defmfun rather than defmfun1 runs almost twice as fast. So icons is defined with defmfun rather than defmfun1. icons does no argument checking.

9.9 Function: imap

```
imap(f, expr)
```

mext package: lists_aex

Description Maps functions of a single argument. I guess that map handles more types of input without error. But imap can be much faster for some inputs.

Arguments imap requires two arguments. The second argument *expr* must be non-atomic.

Options imap takes options with default values: compile->true.

Examples

Map sort efficiently over a list of floats

With aex expression, no conversions to lex are done.

9.10 Function: length_while

length_while(expr, test) mext package: lists_aex

Description Computes the length of expr while test is true.

Arguments length_while requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options length_while takes options with default values: compile->true.

Examples

```
(%i1) length_while([-3,-10,-1,3,6,7,-4], lambda([x], is(x<0)));
(%o1) 3
```

9.11 Function: lrange

mext package: lists_aex

Calling

lrange(stop) returns a list of numbers from 1 through stop.

lrange(start, stop) returns a list of expressions from start through stop.

lrange(start, stop, incr) returns a list of expressions from start through stop in steps of incr.

Description lrange is much more efficient than makelist for creating ranges, particularly for large lists (e.g. 10^5 or more items.) Functions for creating a list of numbers, in order of decreasing speed, are: lrange, table, create_list,makelist.

Arguments lrange requires between one and three arguments. The third argument *incr* must be an expression that is not zero.

Options lrange takes options with default values: adj->true, ot->ml.

Examples

```
(%i1) lrange(6);
(%o1) [1,2,3,4,5,6]
(%i1) lrange(2,6);
(%o1) [2,3,4,5,6]
(%i2) lrange(2,6,2);
(%o2) [2,4,6]
(%i3) lrange(6,1,-1);
(%o3) [6,5,4,3,2,1]
(%i4) lrange(6,1,-2);
(%o4) [6,4,2]
(%i5) lrange(6,ot->ar);
(%o5) <[1,2,3,4,5,6]>
```

The type of the first element and increment determine the type of the elements.

```
(%i1) lrange(1.0,6);

(%o1) [1.0,2.0,3.0,4.0,5.0,6.0]

(%i1) lrange(1.0b0,6);

(%o1) [1.0b0,2.0b0,3.0b0,4.0b0,5.0b0,6.0b0]

(%i2) lrange(1/2,6);

(%o2) [1/2,3/2,5/2,7/2,9/2,11/2]

(%i3) lrange(6.0,1,-1);

(%o3) [6.0,5.0,4.0,3.0,2.0,1.0]
```

Symbols can be used for limits or increments.

```
(%i1) lrange(x,x+4);

(%o1) [x,x+1,x+2,x+3,x+4]

(%i1) lrange(x,x+4*a,a);

(%o1) [x,x+a,x+2*a,x+3*a,x+4*a]
```

 $\mathbf{See} \ \mathbf{also} \ \ \mathtt{makelist}, \ \mathsf{table}, \ \mathrm{and} \ \mathtt{constant_list}.$

9.12 Function: nest

mext package: lists_aex

Description nest(f,x,n) returns f(...f(f(f(x)))...) where there are n nested calls of f.

Arguments nest requires three arguments. The first argument f must be a function. The third argument n must be a non-negative integer.

Options nest takes options with default values: adj->true, ot->ml, compile->true.

9.13 Function: nest_list

```
\mathbf{nest\_list}(f, x, n)
mext package: lists_aex
```

Arguments nest_list requires three arguments. The third argument n must be a non-negative integer.

Options nest_list takes options with default values: adj->true, ot->m1, compile->true.

Examples

Find the first 10 primes after 100.

```
(%i1) nest_list(next_prime,100,10);
(%o1) [101,103,107,109,113,127,131,137,139,149]
```

See also nest, fold, and fold_list.

9.14 Function: nest_while

```
\mathbf{nest\_while}(f, x, test : optional min, max) mext package: lists_aex
```

Calling

 $\mathbf{nest_while}(f,\ x,\ test)$ applies f to x until test fails to return true when called on the nested result.

 $\mathbf{nest_while}(f, x, test, min)$ applies f at least min times.

 $\mathbf{nest_while}(f, x, test, min, max)$ applies f not more than max times.

Arguments nest_while requires between three and five arguments. The fourth argument *min* must be a non-negative integer. The fifth argument *max* must be a non-negative integer.

Options nest_while takes options with default values: adj->true, ot->ml, compile->true.

Implementation This should be modified to allow applying test to more than just the most recent result.

9.15 Function: nreverse

nreverse(e)

mext package: lists_aex

Description Destructively reverse the arguments of expression e. This is more efficient than using reverse.

Arguments nreverse requires one argument e, which must be non-atomic.

Examples

Be careful not to use a after applying neverse. Do assign the result to another variable.

```
(%i1) a : lrange(10), b : nreverse(a);

(%o1) [10,9,8,7,6,5,4,3,2,1]

(%i1) a : lrange(10,ot->ar), b : nreverse(a);

(%o1) <[10,9,8,7,6,5,4,3,2,1]>
```

See also reverse.

9.16 Function: partition_list

```
partition_list(e, nlist:optional dlist)
mext package: lists_aex
```

Calling

```
partition\_list(e, n) partitions e into sublists of length n partition\_list(e, n, d) partitions e into sublists of length n with offsets d.
```

Description Omitting d is equivalent to giving d equal to n. e can be any expression, not only a list. If n is a list, then partition_list partitions at successively deeper levels with elements of n. If n and d are lists, the first elements of n and d apply at the highest level and so on. If n is a list and d is a number, then the offset d is used with each of the n.

Arguments partition_list requires either two or three arguments. The first argument e must be non-atomic. The second argument nlist must be an integer or a list of integers. The third argument dlist must be an integer or a list of integers.

Examples

Partition the numbers from 1 through 10 into pairs.

```
(%i1) partition_list([1,2,3,4,5,6,7,8,9,10],2);
(%o1) [[1,2],[3,4],[5,6],[7,8],[9,10]]
```

9.17 Function: select

```
\mathbf{select}(expr,\ test: optional\ n) mext package: lists_aex
```

Description Returns a list of all elements of expr for which test is true. expr may have any op. If n is supplied, then at most n elements are examined.

Arguments select requires either two or three arguments. The first argument expr must be non-atomic and represented by a lisp list. The third argument n must be a positive integer.

Options select takes options with default values: adj->true, ot->ml, compile->true.

Examples

Select elements less than 3

```
(%i1) select([1,2,3,4,5,6,7], lambda([x], is(x<3)));
(%o1) [1,2]
```

9.18 Argument type: sequence specifier

Description A sequence specification specifies a subsequence of the elements in an expression. A single positive number n means the first n elements. -n means the last n elements. A list of three numbers [i1,i2,i3] means the i1th through the i2th stepping by i3. If i1 or i2 are negative, they count from the end. If i3 is negative, stepping is down and i1 must be greater than or equal to i2. If i3 is omitted, it is taken to be 1. A sequence specifier can also be one of 'all 'none or 'reverse, which mean all elements, no elements or all elements in reverse order respectively.

See also take and string_take.

9.19 Function: table

mext package: lists_aex

Calling

table(expr, [n]) Evaluates expression *number* times. If *number* is not an integer or a floating point number, then float is called. If we have a floating point number, it is truncated into an integer. This type of iterator is the fastest, since no variable is bound.

table(expr, [variable, initial, end, step]) Returns a list of evaluated expressions where variable (a symbol) is set to a value. The first element of the returned list is expression evaluated with variable set to initial. The i-th element of the returned list is expression evaluated with variable set to initial+(i-1)step. The iteration stops once the value is greater (if step is positive) or smaller (if step is negative) than end. Requirement: The difference between end and initial must return a numberp number. step must be a nonzero numberp number. This allows for iterators of rather general forms like [i, %i - 2, %i, 0.1b0] ...

table(expr, [variable, initial, end]) This iterator uses a step of 1 and is equal to [variable,initial, end, 1].

Arguments table requires two or more arguments. The second argument *iterator1* must be a list. Each of the remaining arguments must be a list.

Options table takes options with default values: adj->true, ot->ml.

Attributes table has attributes: [hold_all]

Examples

Make a list of function values

```
(%i1) table(sin(x),[x,0,2*%pi,%pi/4]);
(%o1) [0,1/sqrt(2),1,1/sqrt(2),0,-1/sqrt(2),-1,-1/sqrt(2),0]
```

Make a nested list.

```
(%i1) table(x^y, [x,1,2], [y,1,2]);
(%o1) [[1,1],[2,4]]
```

See also makelist, lrange, and constant_list.

Author Ziga Lenarcic.

9.20 Function: take

```
take(e : rest v)
mext package: lists_aex
```

Calling

take(e, n) returns a list of the first n elements of list or expression e.

take(e, [n1, n2]) returns a list of the n1th through n2th elements of list or expression e.

take(e, [n1, n2, step]) returns a list of the n1th through n2th elements stepping by step of list or expression e.

take(e, -n) returns the last n elements.

take(e, spec1, spec2, ...) applies the sequence specifications at successively deeper levels in e.

Description e can have mixed lex and aex expressions on different levels. If more sequence specifications are given, they apply to successively deeper levels in e.

Arguments take requires one or more arguments. The first argument e must be non-atomic. Each of the remaining arguments must be a sequence specification.

Examples

Take the first 3 elements of a list.

```
(%i1) take([a,b,c,d,e],3);
(%o1) [a,b,c]
```

Take the last 3 elements of a list.

```
(%i1) take([a,b,c,d,e],-3);
(%o1) [c,d,e]
```

Take the second through third elements of a list.

```
(%i1) take([a,b,c,d,e],[2,3]);
(%o1) [b,c]
```

Take the second through tenth elements of a list counting by two.

```
(%i1) take([1,2,3,4,5,6,7,8,9,10],[2,10,2]);
(%o1) [2,4,6,8,10]
```

Take the last through first elements of a list counting backwards by one.

```
(%i1) take([a,b,c,d],[-1,1,-1]);
(%o1) [d,c,b,a]
```

Shorthand for the previous example is 'reverse.

```
(%i1) take([a,b,c,d],'reverse);
(%o1) [d,c,b,a]
```

Take the second through third elements at the first level and the last 2 elements at the second level.

```
(%i1) take([[a,b,c], [d,e,f], [g,h,i]], [2,3],-2);
(%o1) [[e,f],[h,i]]
```

9.21 Function: take_while

```
take_while(expr, test)
mext package: lists_aex
```

Calling

 $take_while(expr, test)$ collects the elements in expr until test fails on one of them. The op of the returned expression is the same as the op of expr.

Arguments take_while requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options take_while takes options with default values: adj->true, ot->ml, compile->true.

Examples

Take elements as long as they are negative.

```
(%i1) take_while([-3,-10,-1,3,6,7,-4], lambda([x], is(x<0)));
(%o1) [-3,-10,-1]
```

9.22 Function: tuples

```
\mathbf{tuples}(list\text{-}or\text{-}lists : optional } n) mext package: lists_aex
```

Calling

tuples (list, n) Return a list of all lists of length n whose elements are chosen from list.

tuples([list1, list2, ...]) Return a list of all lists whose i-th element is chosen from listi.

Arguments tuples requires either one or two arguments. The first argument list-or-lists must be non-atomic and represented by a lisp list. The second argument n must be a non-negative integer.

Options tuples takes options with default values: adj->true, ot->ml.

Examples

Make all three letter words in the alphabet 'a,b'.

```
(%i1) tuples([a,b],3);
(%o1) [[a,a,a],[a,a,b],[a,b,a],[a,b,b],[b,a,a],[b,a,b],[b,b,a],[b,b,b]]
```

Take all pairs chosen from two lists.

```
(%i1) tuples([[0,1], [x,y,z]]);
(%o1) [[0,x],[0,y],[0,z],[1,x],[1,y],[1,z]]
```

tuples works for expressions other than lists.

```
(%i1) tuples(f(0,1),3);
(%o1) [f(0,0,0),f(0,0,1),f(0,1,0),f(0,1,1),f(1,0,0),f(1,0,1),f(1,1,0),f(1,1,1)]
```

10 Functions and Variables for Number Theory

- \bullet abundant_p
- aliquot_sequence
- aliquot_sum
- amicable_p
- catalan_number

- divisor_function
- divisor_summatory
- from_digits
- integer_digits
- integer_string
- oeis_A092143
- perfect_p
- prime_pi
- prime_pi_soe
- prime_twins
- primes1

10.1 Function: abundant_p

$abundant_p(n)$

mext package: discrete_aex

Description Returns true if n is an abundant number. Otherwise, returns false.

Arguments abundant_p requires one argument n, which must be a positive integer.

Examples

The abundant numbers between 1 and 100

```
(%i1) select(lrange(100),abundant_p);
(%o1) [12,18,20,24,30,36,40,42,48,54,56,60,66,70,72,78,80,84,88,90,96,100]
```

See also divisor_function, aliquot_sum, aliquot_sequence, divisor_summatory, and perfect_p.

10.2 Function: aliquot_sequence

$aliquot_sequence(k, n)$ mext package: discrete_aex

Description The aliquot sequence is a recursive sequence in which each term is the sum of the proper divisors of the previous term. This function returns the first n elements (counting from zero) in the aliquot sequence whose first term is k. The sequence is truncated at an element if it is zero or repeats the previous element.

Arguments aliquot_sequence requires two arguments. The first argument k must be a positive integer. The second argument n must be a non-negative integer.

Examples

Perfect numbers give a repeating sequence of period 1.

```
(%i1) imap(lambda([x],aliquot_sequence(x,100)),[6,28,496,8128]);
(%o1) [[6],[28],[496],[8128]]
```

Aspiring numbers are those which are not perfect, but terminate with a repeating perfect number.

```
(%i1) imap(lambda([x],aliquot_sequence(x,100)),[25, 95, 119, 143, 417, 445, 565, 608, 650, 652, 675, 68 (%o1) [[25,6],[95,25,6],[119,25,6],[143,25,6],[417,143,25,6],[445,95,25,6],[565,119,25,6],[608,652,496]
```

See also divisor_function, aliquot_sum, divisor_summatory, perfect_p, and abundant_p.

10.3 Function: aliquot_sum

$aliquot_sum(n)$

mext package: discrete_aex

Description Returns the aliquot sum of n. The aliquot sum of n is the sum of the proper divisors of n.

Arguments aliquot_sum requires one argument n, which must be a positive integer.

Attributes aliquot_sum has attributes: [match_form]

See also divisor_function, aliquot_sequence, divisor_summatory, perfect_p, and abundant_p.

10.4 Function: amicable_p

$\mathbf{amicable_p}(n, m)$

mext package: discrete_aex

Description Returns true if n and m are amicable, and false otherwise.

Arguments amicable_p requires two arguments. The first argument n must be a positive integer. The second argument m must be a positive integer.

Examples

The first few amicable pairs.

10.5 Function: catalan_number

$catalan_number(n)$

mext package: discrete_aex

Description Returns the *n*th catalan number.

Arguments catalan_number requires one argument.

Examples

The catalan number for n from 1 through 12.

```
(%i1) map(catalan_number,lrange(12));
(%o1) [1,2,5,14,42,132,429,1430,4862,16796,58786,208012]
```

The n'th catalan number.

```
(%i1) catalan_number(n);
(%o1) binomial(2*n,n)/(n+1)
```

OEIS number: A000108.

10.6 Function: divisor_function

divisor_function(n :optional x) mext package: discrete_aex

Description Returns the divisor function, or sum of positive divisors function

$$\sigma_x(n) = \sum_{d|n} d^x,$$

where d|x means d divides n. If x is omitted it takes the default value 0. Currently, complex values for x are not supported. After writing this, I noticed that the function is implemented in the maxima core and is callled divsum.

Arguments divisor_function requires either one or two arguments. The first argument n must be a non-negative integer. The second argument x must be a number.

Attributes divisor_function has attributes: [match_form]

OEIS number: A000005 for x=0 and A000203 for x=1.

See also aliquot_sum, aliquot_sequence, divisor_summatory, perfect_p, and abundant_p.

10.7 Function: divisor_summatory

 $divisor_summatory(x)$

mext package: discrete_aex

Description Returns the divisor summatory function D(x) for x. The divisor_function $\sigma_0(n)$ counts the number of unique divisors of the natural number n. D(x) is the sum of $\sigma_0(n)$ over $n \le x$.

Arguments divisor_summatory requires one argument x, which must be a non-negative number.

Attributes divisor_summatory has attributes: [match_form]

Examples

D(n) for n from 1 through 12

```
(%i1) map(divisor_summatory,lrange(12));
(%o1) [1,3,5,8,10,14,16,20,23,27,29,35]
```

OEIS number: A006218.

See also divisor_function, aliquot_sum, aliquot_sequence, perfect_p, and abundant_p.

10.8 Function: from_digits

from_digits(digits :optional base)

mext package: discrete_aex

Calling

from_digits(digits) returns the integer represented by the decimal digits in the list digits.

from_digits(digits, base) returns the integer represented by the base base digits in the list digits.

Description base need not be number, but may be, for instance, a symbol. If base is a number it must be an integer between 2 and 36. digits may be a string rather than a list.

Arguments from digits requires either one or two arguments. The first argument digits must be a list (lex or aex) or a string.

See also integer_digits and integer_string.

10.9 Function: integer_digits

integer_digits(n :optional base, len)

mext package: discrete_aex

Calling

 $integer_digits(n)$ returns a list of the base 10 digits of n.

 $integer_digits(n, base)$ returns a list of the base base digits of n.

integer_digits(n, base, len) returns a list of the base base digits of n padded with 0's so that the total length of the list is len.

Arguments integer_digits requires between one and three arguments. The first argument *n* must be an integer. The second argument *base* must be a valid radix (an integer between 2 and 36). The third argument *len* must be a non-negative integer.

Options integer_digits takes options with default values: adj->true, ot->ml.

See also from_digits and integer_string.

Implementation gcl is much faster than the others. integer_digits($2^(10^6)$): typical times for lisps: ccl-1.7-r15184M = 65s, sbcl-1.0.52.0.debian = 1.5s, allegro-8.2 = 23s, Mma-3.0 = 5s, gcl-2.6.7 = 0.11s, Mma-8 = 0.04s. The base is limited to 36 only because we call write-to-string.

10.10 Function: integer_string

 $integer_string(n : optional base, pad)$

mext package: discrete_aex

Calling

 $integer_string(n)$ returns a string containing the decimal digits of the integer n.

 $integer_string(n, base)$ returns a string containing the base base digits of the integer n.

integer_string(n, base, pad) pads the string on the left with 0's so that the length of the string is pad.

 $integer_string(n, "roman")$ returns a string containing the roman-numeral form of the integer n.

 $integer_string(n, "cardinal")$ returns a string containing the english word form of the integer (cardinal number) n.

 $integer_string(n, "ordinal")$ returns a string containing the english word form of the ordinal (counting) number n.

Arguments integer_string requires between one and three arguments. The first argument n must be an integer. The second argument base must be a valid radix (an integer between 2 and 36) or a string. The third argument pad must be a positive integer.

See also integer_digits and from_digits.

10.11 Function: oeis_A092143

 $oeis_A092143(n)$

mext package: discrete_aex

Description Returns the cumulative product of all divisors of integers from 1 to n.

Arguments oeis_A092143 requires one argument n, which must be a positive integer.

10.12 Function: perfect_p

 $\mathbf{perfect}_{-}\mathbf{p}(n)$

mext package: discrete_aex

Description Returns true if n is a perfect number. Otherwise, returns false.

Arguments perfect_p requires one argument n, which must be a positive integer.

See also divisor_function, aliquot_sum, aliquot_sequence, divisor_summatory, and abundant_p.

Implementation This function computes divisors. It would be far more efficient to use a table of known perfect numbers, as very few of them are accessible by current computer hardware.

10.13 Function: prime_pi

 $prime_pi(n)$

mext package: prime_pi

Calling

 $\mathbf{prime_pi}(n)$ returns the number of primes less than or equal to n.

Description Computes the prime counting function. The option threads specifies the maximum number of cpu threads to use. The routine may use fewer threads, depending on the value of n. The percent of the calculation that is finished is printed during the calculation if the option status is true. The status will only work under some terminals.

Arguments prime_pi requires one argument n, which must be equivalent to an unsigned 64 bit integer (that is, an integer between 0 and 2 to the power 64) (We need to modify the doc system so we can use notation for powers in arg check strings.

Options prime_pi takes options with default values: status->false, threads->1.

See also prime_pi_soe, next_prime, and prev_prime.

Implementation This algorithm is fast, for a general purpose mathematics program. It combines a segmented sieve implemented as a C library with tables.

Authors Kim Walisch (C library), Tomas Oliveira e Silva (tables), and John Lapevre (lisp).

10.14 Function: prime_pi_soe

 $\mathbf{prime_pi_soe}(n)$

mext package: discrete_aex

Description The prime counting function. The algorithm is the sieve of Eratosthenes. Internally an array of n bits is used.

Arguments prime_pi_soe requires one argument n, which must be a non-negative integer.

See also prime_pi, next_prime, and prev_prime.

Implementation This is not the most efficient way to compute primes.

10.15 Function: prime_twins

prime_twins(*min* :optional *max*)

mext package: prime_pi

Calling

prime_twins(n) returns the number of prime twins less than or equal to n.

prime_twins(nmin, nmax) returns the number of prime twins between nmin and max.

Description The option *ktuplet* counts the *ktuplet*-constellation rather than the twins. *ktuplet* must be an integer between 1 and 7.

Arguments prime_twins requires either one or two arguments. The first argument min must be equivalent to an unsigned 64 bit integer (that is, an integer between 0 and 2 to the power 64) (We need to modify the doc system so we can use notation for powers in arg check strings. The second argument max must be equivalent to an unsigned 64 bit integer (that is, an integer between 0 and 2 to the power 64) (We need to modify the doc system so we can use notation for powers in arg check strings.

Options prime_twins takes options with default values: ktuplet->2, status->false, threads->1.

 $\mathbf{See} \ \mathbf{also} \ \ \mathsf{prime_pi}, \ \mathsf{next_prime}, \ \mathsf{prev_prime}, \ \mathrm{and} \ \mathsf{primep}.$

Implementation No tables are used in this algorithm.

10.16 Function: primes1

primes1(*n1* :optional *n2*) mext package: discrete_aex

Calling

primes1(max) returns a list of the primes less than or equal to max.

primes1(min, max) returns a list of the primes between min and max.

Description The algorithm is the sieve of Eratosthenes. This is not an efficient algorithm.

Arguments primes 1 requires either one or two arguments. The first argument n1 must be a non-negative integer. The second argument n2 must be a non-negative integer.

Options primes1 takes options with default values: adj->true, ot->ml.

11 Functions and Variables for Numerics

These are mathematical functions—cos,sin,etc. —that accept only numerical arguments. Tests of loops in untranslated code show that these are much more efficient than using the standard maxima versions. But, for most applications, the standard maxima versions are probably ok.

- n_abs
- n_acos
- n_acosh
- n_asin
- n_asinh
- n_atan
- n_atanh
- n_cos

- n_cosh
- n_exp
- n_expt
- n_log
- n_sin
- n_sinh
- n_sqrt
- n_tan
- n_tanh

11.1 Function: n_abs

Description n_abs calls the lisp numeric function ?abs. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_abs may be considerably faster in some code, particularly untranslated code.

11.2 Function: n_acos

Description n₋acos calls the lisp numeric function ?acos. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n₋acos may be considerably faster in some code, particularly untranslated code.

11.3 Function: n acosh

Description n_acosh calls the lisp numeric function ?acosh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_acosh may be considerably faster in some code, particularly untranslated code.

11.4 Function: n_asin

Description n_asin calls the lisp numeric function ?asin. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_asin may be considerably faster in some code, particularly untranslated code.

11.5 Function: n_asinh

Description n_asinh calls the lisp numeric function ?asinh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_asinh may be considerably faster in some code, particularly untranslated code.

11.6 Function: n_atan

Description n_atan calls the lisp numeric function ?atan. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_atan may be considerably faster in some code, particularly untranslated code.

11.7 Function: n_atanh

Description n_atanh calls the lisp numeric function ?atanh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_atanh may be considerably faster in some code, particularly untranslated code.

11.8 Function: n_cos

Description n_cos calls the lisp numeric function ?cos. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_cos may be considerably faster in some code, particularly untranslated code.

11.9 Function: n_cosh

Description n_cosh calls the lisp numeric function ?cosh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_cosh may be considerably faster in some code, particularly untranslated code.

11.10 Function: n_exp

Description n_exp calls the lisp numeric function ?exp. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_exp may be considerably faster in some code, particularly untranslated code.

11.11 Function: n_expt

Description n_expt calls the lisp numeric function ?expt. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_expt may be considerably faster in some code, particularly untranslated code.

11.12 Function: n₋log

Description n_log calls the lisp numeric function ?log. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_log may be considerably faster in some code, particularly untranslated code.

11.13 Function: n_sin

Description n_sin calls the lisp numeric function ?sin. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_sin may be considerably faster in some code, particularly untranslated code.

11.14 Function: n_sinh

Description n_sinh calls the lisp numeric function ?sinh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_sinh may be considerably faster in some code, particularly untranslated code.

11.15 Function: n_sqrt

Description n_sqrt calls the lisp numeric function ?sqrt. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_sqrt may be considerably faster in some code, particularly untranslated code.

11.16 Function: n_tan

Description n_tan calls the lisp numeric function ?tan. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_tan may be considerably faster in some code, particularly untranslated code.

11.17 Function: n_tanh

Description n_tanh calls the lisp numeric function ?tanh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n_tanh may be considerably faster in some code, particularly untranslated code.

12 Functions and Variables for Predicates

- cmplength
- lengthOp
- length1p
- length_eq
- type_of

12.1 Function: cmplength

 $\mathbf{cmplength}(e, n)$ mext package: aex

Description return the smaller of n and length(e). This is useful if e is very large and n is small, so that computing the entire length of e is inefficient. Expression e can be either a lex of aex expression.

Arguments cmplength requires two arguments. The second argument n must be a non-negative integer.

See also length0p, length_eq, and length1p.

Implementation complength is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

12.2 Function: length0p

length0p(e)

mext package: aex

Description Returns true if je; is of length 0, false otherwise. This implementation traverse no more elements of je; than necessary to return the result.

Arguments length0p requires one argument e, which must be a string or non-atomic.

See also cmplength, length_eq, and length1p.

Implementation length0p is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

12.3 Function: length1p

length1p(e)

mext package: aex

Description Returns true if e is of length 1, false otherwise. This implementation traverse no more elements of e than necessary to return the result.

Arguments length1p requires one argument e, which must be a string or non-atomic.

See also lengthOp, cmplength, and length_eq.

Implementation length1p is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

12.4 Function: length_eq

$\mathbf{length_eq}(\mathit{e},\;\mathit{n})$

mext package: aex

Description Returns true if e is of length n, false otherwise. This implementation traverses no more elements of e than necessary to return the result.

Arguments length_eq requires two arguments. The first argument e must be a string or non-atomic. The second argument n must be a non-negative integer.

See also length0p, cmplength, and length1p.

Implementation length_eq is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

12.5 Function: type_of

 $\mathbf{type_of}(e : optional \ verbose)$

mext package: aex

Description Return something like the 'type' of a maxima expression. This is a bit ill defined currently. type_of uses the lisp function type-of.

Arguments type_of requires either one or two arguments.

Examples

```
(%i1) type_of(1);
(%o1) ?bit
```

```
(%i1) type_of(1.0);
(%o1) ?double\-float
(%i2) type_of(1.0b0);
(%o2) ?bfloat
(%i3) type_of(1/3);
(%03) /
(%i4) type_of("dog");
(%o4) ?string
(%i5) type_of([1,2,3]);
(%o5) [
(%i6) type_of(aex([1,2,3]));
(%06) [
(%i7) type_of(%e);
(%o7) ?symbol
(%i8) type_of(%i);
(%o8) ?symbol
(%i9) type_of(%i+1);
(\%09) +
```

type_of returns the type of the lisp struct corresponding to a maxima object.

```
(%i1) load(graphs)$
(%i2) type_of(new_graph());
(%o2) graph
```

13 Functions and Variables for Program Flow

• error_str

13.1 Function: error_str

```
error_str()
mext package: aex
```

Description Returns the last error message as a string.

Arguments error_str requires zero arguments.

See also error and errormsg.

14 Functions and Variables for Quicklisp

- quicklisp_apropos
- quicklisp_install
- quicklisp_load
- quicklisp_start

14.1 Function: quicklisp_apropos

quicklisp_apropos(term)
mext package: quicklisp

Description Search quicklisp for lisp 'systems' (packages) matching term.

Arguments quicklisp_apropos requires one argument term, which must be a string.

14.2 Function: quicklisp_install

quicklisp_install()
mext package: quicklisp

Description Download and install quicklisp from the internet. This is usually done automatically as the final step of building and installing the maxima interface to quicklisp.

Arguments quicklisp_install requires zero arguments.

14.3 Function: quicklisp_load

quicklisp_load(package_name)

mext package: quicklisp

Description Load the asdf lisp package *package_name*, or, if not installed, install from the internet and

then load.

Arguments quicklisp_load requires one argument package_name, which must be a string.

14.4 Function: quicklisp_start

quicklisp_start()

mext package: quicklisp

Description Load (setup) quicklisp. It must already be installed.

Arguments quicklisp_start requires zero arguments.

15 Functions and Variables for Runtime Environment

- chdir
- dir_exists
- dirstack
- dont_kill
- dont_kill_share
- get_dont_kill
- homedir
- mext_clear
- mext_info

- mext_list
- mext_test
- popdir
- probe_file
- pwd
- require
- truename

15.1 Function: chdir

chdir(:optional *dir*)

mext package: mext_defmfun1

Calling

chdir() Set the working directory to the value it had when mext was loaded.

chdir(dir) Set the working directory to dir.

Description Set the working directory for maxima/lisp. With some lisps, such as cmu lisp the system directory is changed as well. This should be made uniform across lisp implementations.

Arguments chdir requires either zero or one arguments. If present, the argument dir must be a a string.

15.2 Function: dir_exists

 $dir_exists(dir)$

mext package: mext_defmfun1

Description Returns the pathname as a string if *dir* exists, and false otherwise.

Arguments dir_exists requires one argument dir, which must be a string.

15.3 Function: dirstack

dirstack()

mext package: mext_defmfun1

Description Return a list of the directories on the directory stack. This list is manipulated with chdir, updir, and popdir.

Arguments dirstack requires zero arguments.

15.4 Function: dont_kill

dont_kill(:rest item)

mext package: mext_defmfun1

Description Add the *items* to the list of symbols that are not killed by kill(all). This facility is part of the maxima core, but is apparantly unused. Maybe putting a property in the symbol's property list would be better.

Arguments dont_kill requires zero or more arguments.

Attributes dont_kill has attributes: [hold_all]

15.5 Function: dont_kill_share

dont_kill_share(package)
mext package: mext_defmfun1

Description Prevent symbols in maxima share package package from being killed by kill.

Arguments dont_kill_share requires one argument *package*, which must be a string or a symbol.

15.6 Function: get_dont_kill

get_dont_kill()

mext package: mext_defmfun1

Description Returns the list of symbols that are not killed by kill(all). Items are added to this list with dont_kill.

Arguments get_dont_kill requires zero arguments.

15.7 Variable: homedir

default value (NAMESTRING *HOMEDIR-PATHNAME*).

Description The user's home directory.

15.8 Function: mext_clear

 $mext_clear()$

mext package: mext_defmfun1

Description Clears the list of mext packages that have been loaded with require. Subsequent calls to require will reload the packages.

Arguments mext_clear requires zero arguments.

15.9 Function: mext_info

mext_info(distname)

mext package: mext_defmfun1

Description Print information about installed mext distribution distname. The list of installed distributions is built by calling mext_list.

Arguments mext_info requires one argument *distname*, which must be a string or a symbol.

15.10 Function: mext_list

mext_list()

mext package: mext_defmfun1

Description Returns a list of all installed mext distributions.

Arguments mext_list requires zero arguments.

15.11 Function: mext_test

mext_test(:optional dists)
mext package: mext_defmfun1

Description Run the test suites for a mext distribution or list of distributions. With no argument, a subfolder named **rtests** is searched for in the current directory.

Arguments mext_test requires either zero or one arguments. If present, the argument *dists* must be a a string, a symbol, or a list of strings or symbols.

15.12 Function: popdir

popdir(:optional n)

mext package: mext_defmfun1

Description Pop a value from the current directory stack and chdir to this value. If n is given, pop n values and chdir to the last value popped.

Arguments popdir requires either zero or one arguments. If present, the argument n must be a a non-negative integer.

15.13 Function: probe_file

Calling

probe_file(filespec) returns a string representing a canonical pathname to the file specified by filespec. False is returned if the file can't be found.

Description Probe_File tries to find a canonical pathname for a file specified by the string *filespec*.

Examples

```
(%i1) probe_file("a/b.txt");
(%o1) "/home/username/c/a/b.txt"
```

15.14 Function: pwd

pwd()

mext package: mext_defmfun1

Description Return the current working directory.

Arguments pwd requires zero arguments.

15.15 Function: require

require(distname :optional force)
mext package: mext_defmfun1

Description Load the mext package *distname* and register that it has been loaded. require('all) will load all installed mext packages. If *force* is true, then *distname* is loaded even if it has been loaded previously.

Arguments require requires either one or two arguments. The first argument *distname* must be a string or a symbol.

15.16 Function: truename

Calling

truename(*filespec*) returns a string representing a canonical pathname to the file specified by *filespec* **Description** Truename tries to find a canonical pathname for a file specified by the string *filespec*.

16 Functions and Variables for Strings

- string_drop
- string_reverse
- \bullet string_take
- with_output_to_string

16.1 Function: string_drop

```
string\_drop(s, spec)
mext package: lists_aex
```

Arguments string_drop requires two arguments. The first argument s must be a string. The second argument spec must be a sequence specification.

Examples

```
(%i1) string_drop("abracadabra",1);
(%o1) bracadabra
```

```
(%i1) string_drop("abracadabra",-1);
(%o1) abracadabr
```

```
(%i1) string_drop("abracadabra",[2,10]);
(%o1) aa
```

16.2 Function: string_reverse

```
string_reverse(s)
mext package: lists_aex
```

Calling

 $string_reverse(s)$ returns a copy of string s with the characters in reverse order.

Arguments string_reverse requires one argument s, which must be a string.

16.3 Function: string_take

```
string\_take(s, spec)
mext package: lists_aex
```

Calling

```
string\_take(s, n) returns a string of the first n characters of the string s. string\_take(s, -n) returns a string of the last n characters of s.
```

Arguments string_take requires two arguments. The first argument s must be a string. The second argument spec must be a sequence specification.

Examples

```
(%i1) string_take("dog-goat-pig-zebra",[5,12]);
(%o1) goat-pig
```

16.4 Function: with_output_to_string

Description Evaluates $expr_1, expr_2, expr_3, \dots$

Examples

```
(%i1) sreverse(with_output_to_string(for i:5 thru 10 do print("i! for i=",i,i!)));
(%o1)
0088263 01 =i rof !i
088263 9 =i rof !i
02304 8 =i rof !i
0405 7 =i rof !i
027 6 =i rof !i
021 5 =i rof !i
```

See also with_stdout.

17 Miscellaneous Functions

- examples
- examples_add

17.1 Function: examples

```
examples(item) mext package: defmfun1
```

Calling

examples(*item*) Print examples for the topic *item*. Note these examples are different from those extracted from the maxima manual with the command **example**.

Arguments examples requires one argument *item*, which must be a string or a symbol.

17.2 Function: examples_add

examples_add(item, text, protected-var-list, code) mext package: defmfun1

Calling

examples_add(*item*, *text*, *protected-var-list*, *code*) Add an example for item *item*. *text* will be printed before the example is displayed. *protected-var-list* is string giving a list of variables such as "[x,y]" that appear in the example code. The example code will be wrapped in a block that makes *protected-var-list* local. *code* may be a string or list of strings that is/are the example code.

Arguments examples_add requires four arguments. The first argument *item* must be a string or a symbol. The second argument *text* must be a string. The third argument *protected-var-list* must be a string. The fourth argument *code* must be a string or a list of strings.

Examples

Add an example for the function 'last'.

```
(%i1) examples_add("last", "Return the last item in a list.", "[a,b,c,d]", "last([a,b,c,d])");
(%o1) done
```

18 Miscellaneous utilities

• compile_lambda_verbose

18.1 Variable: compile_lambda_verbose

default value false.

Description If this is true, then print translated code when automatically compiling lambda functions passed as arguments. This is done in the macro option-compile-lambda.

19 Options

Options to a function in the aex-maxima distribution are passed as follows:

funcname(x,y, [optname -; optval, optname2 -; optval2]) or funcname(x,y, optname -; optval, optname2 -; optval2)

The standard options described in this section are some options that are supported by many functions in the aex-maxima distribution.

- adj
- compile
- foptions
- ot

19.1 Option: adj

Description This option takes values of true or false. If true, then the output aex expression is adjustable, that is, the underlying array can be extended in size. If false, then the output aex expression is not adjustable. The non-adjustable array may have some advantanges in efficiency, but I have not observed them, and this may be lisp-implementation dependent.

19.2 Option: compile

Description If this option is true, then lambda functions passed as arguments to a function will be automatically translated or compiled. If it is false they will used as interpreted maxima code. Compiling lambda functions usually greatly deceases the execution time of the function if the lambda function is called many times.

19.3 Function: foptions

foptions(name)

Description Return a list of allowed options to defmfun1 function *name*. I would prefer to call this options, but that name is taken by an unused, undocumented function.

Arguments foptions requires one argument *name*, which must be a string or a symbol.

19.4 Option: ot

Description With a value ar this option causes the function to return an array-representation expression. With a value ml a standard lisp list representation is returned. The array-representation is not a maxima array, but rather a more-or-less arbitrary maxima expression that is stored internally as an array. For certain operations, such as random access to elements of the expression, an array representation is faster than the standard list representation. One disadvantange of the array representations is that creating an array is relatively slow. For instance, execution time may be large if a function returns an expression with many small subexpressions that are in the array-representation. The majority of the maxima system does not understand array-representation, so conversion back to list-representation at may be necessary.