# Third-party maxima software

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# 1 Array Representation For Expressions

Maxima expressions are normally implemented internally as lisp lists, but they may also be represented by lisp arrays. Each representation has advantages.

# 2 Attributes

A function may possess a list of attributes. The attributes control how the arguments to the function are evaluated and how errors are handled.

- attributes
- set\_match\_form
- set\_nowarn
- unset\_match\_form
- unset\_nowarn

## 2.1 Function: attributes

attributes(name)

**Description** Returns a list of the 'attributes' of function *name*.

**Arguments** attributes requires one argument *name*, which must be a string or a symbol.

See also unset\_match\_form, set\_match\_form, set\_nowarn, and unset\_nowarn.

#### 2.2 Function: set\_match\_form

 $set_match_form(names)$ 

**Description** Set the 'match\_form' attribute for function(s) names. If the argument checks for a function call fail, and the attribute 'match\_form' is set, then rather than signaling an error, the unevaluated form is returned. Furthemore, if the attribute 'nowarn' is not set, then a warning message is printed. Currently, only automatic argument checks generated from the defmfun1 protocol are controlled. Argument checks and errors written within the body of the functions occur regardless of function attributes.

**Arguments** set\_match\_form requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also unset\_match\_form, set\_nowarn, unset\_nowarn, and attributes.

## 2.3 Function: set\_nowarn

 $set_nowarn(names)$ 

**Description** Set the 'nowarn' attribute for function(s) names. If the argument checks for a function call fail, and the attribute 'match\_form' is set, and the attribute 'nowarn' is set, then rather than signaling an error, the unevaluated form is returned and no warning message is printed.

**Arguments** set\_nowarn requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also unset\_match\_form, set\_match\_form, unset\_nowarn, and attributes.

#### 2.4 Function: unset\_match\_form

unset\_match\_form(names)

**Description** Unset the 'match\_form' attribute for function(s) *names*. If the argument checks for a function call fail, and the attribute 'match\_form' is set, then rather than signaling an error, the unevaluated form is returned. Furthemore, if the attribute 'nowarn' is not set, then a warning message is printed. Currently, only automatic argument checks generated from the defmfun1 protocol are controlled. Argument checks and errors written within the body of the functions occur regardless of function attributes.

**Arguments** unset\_match\_form requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also set\_match\_form, set\_nowarn, unset\_nowarn, and attributes.

#### 2.5 Function: unset\_nowarn

 $unset\_nowarn(names)$ 

**Description** Unset the 'nowarn' attribute for function(s) names. If the argument checks for a function call fail, and the attribute 'match\_form' is set, and the attribute 'nowarn' is set, then rather than signaling an error, the unevaluated form is returned and no warning message is printed.

**Arguments** unset\_nowarn requires one argument *names*, which must be a string, a symbol, or a list of strings or symbols.

See also unset\_match\_form, set\_match\_form, set\_nowarn, and attributes.

## 3 Functions and Variables for Array Represention for Expressions

These functions operate on the the array expression data structure.

- aeop
- aex
- aex\_cp
- aex\_get
- aex\_new
- aex\_set
- aex\_shift
- aex\_unshift
- aexg
- aexs
- copy\_aex\_type
- deep\_copy
- faex
- flex
- iapply
- iargs
- ilength
- iop
- ipart
- $\bullet \ \mathtt{ipart\_set}$
- ireverse
- lex
- raex
- rlex

## 3.1 Function: aeop

 $\mathbf{aeop}(\mathit{expr})$ 

mext package: aex

**Description** op function for aex. returns op if e is not an aex.

**Arguments** aeop requires one argument *expr*, which must be non-atomic.

## 3.2 Function: aex

 $\mathbf{aex}$ (:optional x) mext package: aex

#### Calling

 $\mathbf{aex}(e)$  Converts expression e to an array representation. The input expression e is returned unchanged if it is already an array expression or is a symbol or number or specially represented maxima expression. This function converts only at the first level.

**Arguments** aex requires either zero or one arguments.

Options aex takes options with default values: adj->true.

## 3.3 Function: aex\_cp

 $\mathbf{aex\_cp}(e : \mathbf{optional} \ head)$ mext package:  $\mathbf{aex}$ 

#### Calling

 $\mathbf{aex\_cp}(e)$  Returns an aex form copy of e. e may be in either lex or aex form. Conversion to aex representation occurs only on the first level.

**Arguments** aex\_cp requires either one or two arguments. The first argument e must be non-atomic.

Options aex\_cp takes options with default values: adj->true.

## 3.4 Function: aex\_get

**Description** Returns the n-1th part of aexpr e. A value of n less than 0 is not allowed. This is more efficient than aexg, which returns the head of the expression when n is equal to zero.

## Examples

```
(%i1) a : aex([5,6,7]), aex_get(a,2);
(%o1) 7
```

#### 3.5 Function: aex\_new

 $\mathbf{aex\_new}(n : optional \ head)$ 

mext package: aex

**Arguments** aex\_new requires either one or two arguments. The first argument n must be a non-negative integer.

#### 3.6 Function: aex\_set

**Description** Destructively sets the nth part of aexpr e to value v. A value of 0 for n is not allowed. This is more efficient than aexs. No argument checking is done.

#### Examples

Destructively assign to a part of an expression.

```
(%i1) a : aex([1,2,3]), aex_set(a,1,x), a;
(%o1) <[1,x,3]>
```

See also aexs and ipart.

#### 3.7 Function: aex shift

```
\mathbf{aex\_shift}(e) mext package: \mathbf{aex}
```

**Description** destructively removes an element from the end of e. For array representation of expressions we use the words 'push' and 'pop' for the beginning of and expression, and 'shift' and 'unshift' for the end of an expression, whether the representation is an array or a list. This is consistent with maxima, but the reverse of the meaning of the terms in perl.

**Arguments**  $aex_shift$  requires one argument e, which must be an adjustable array expression.

## Examples

```
(%i1) a : lrange(10,ot->ar);
(%o1) <[1,2,3,4,5,6,7,8,9,10]>
(%i1) b : aex_shift(a);
(%o1) 10
(%i2) a;
(%o2) <[1,2,3,4,5,6,7,8,9]>
```

#### 3.8 Function: aex unshift

```
\mathbf{aex\_unshift}(v, e) mext package: aex
```

**Description** Destructively pushes an element v onto the end of e. The return value is v. For array representation of expressions we use the words 'push' and 'pop' for the beginning of and expression, and 'shift' and 'unshift' for the end of an expression, whether the representation is an array or a list. This is consistent with maxima, but the reverse of the meaning of the terms in perl.

**Arguments** aex\_unshift requires two arguments. The second argument e must be an adjustable array expression.

#### Examples

```
(%i1) a : lrange(10,ot->ar), aex_unshift("dog",a), a;
(%o1) <[1,2,3,4,5,6,7,8,9,10,"dog"]>
```

## 3.9 Function: aexg

**Description** aexg(e,n) returns the nth part of aexpr e. If n is 0, the head of e is returned. No argument checking is performed.

See also aex\_get, ipart, inpart, and part.

#### 3.10 Function: aexs

**Description** destructively sets the nth part of aexpr e to value v. A value of 0 for n returns the head (or op) of e.

## 3.11 Function: copy\_aex\_type

copy\_aex\_type(ein)
mext package: aex

**Description** Create a new aex with same head, length, adjustability, etc. but contents of expression are not copied.

**Arguments** copy\_aex\_type requires one argument *ein*, which must be an array-representation expression.

## 3.12 Function: deep\_copy

 $\mathbf{deep\_copy}(e)$  mext package: aex

**Description** Deep copy expression e which may be of mixed lex/aex representation. An exact copy is made; that is, the representation is preserved at all levels.

**Arguments** deep\_copy requires one argument.

## 3.13 Function: faex

faex(e)

mext package: aex

**Description** deep copy e converting to aex representation at all levels.

**Arguments** faex requires one argument.

#### 3.14 Function: flex

 $\mathbf{flex}(e)$ 

mext package: aex

**Description** deep copy e converting to lex representation at all levels.

Arguments flex requires one argument.

## 3.15 Function: iapply

iapply(fun, arg)
mext package: aex

**Description** iapply is like maxima apply, but it supports aex lists. *arg* is converted to an ml if it is an aex expression. By default, output is ml regardless of the input representation.

**Arguments** iapply requires two arguments. The first argument fun must be a function. The second argument arg must be non-atomic.

Options iapply takes options with default values: adj->true, ot->ml.

#### Examples

```
(%i1) iapply(%%ff,lrange(4));
(%o1) %%ff(1,2,3,4)
```

```
(%i1) iapply(%%ff,lrange(4,[ot->ar]));
(%o1) %%ff(1,2,3,4)
```

```
(%i1) iapply(%%ff,lrange(4,[ot->ar]), [ot->ar]);
(%o1) %%ff<1,2,3,4>
```

```
(%i1) iapply(%%ff,lrange(4), [ot->ar]);
(%o1) %%ff<1,2,3,4>
```

## 3.16 Function: iargs

iargs(e)

mext package: aex

**Description** returns a list of the arguments of e, which may be either a lex or aex expression. This works like 'args', but is more general.

**Arguments** iargs requires one argument e, which must be a subscripted variable or non-atomic.

Options iargs takes options with default values: adj->true, ot->ml.

## 3.17 Function: ilength

ilength(e)

mext package: aex

**Description** Returns the length of the expression e. This is like maxima length, but here, e can be either an aex or a lex.

**Arguments** ilength requires one argument *e*, which must be a subscripted variable or non-atomic.

## 3.18 Function: iop

iop(expr)

mext package: aex

**Description** returns the main operator of the expression *expr*, which may be either a lex or aex expression. This works like 'op', but is more general.

**Arguments** iop requires one argument *expr*, which must be a subscripted variable or non-atomic.

## 3.19 Function: ipart

#### Calling

ipart(e, ind1, ind2, ...) Returns the part of expression e specified by indices. e may be a mixed (lex and aex) representation expression. When used as an Ivalue, ipart can be used to assign to a part of an expression. If an index is negative, then it counts from the end of the list. If e is an ordinary maxima list (lex), then using a negative index is potentially slower than using a positive index because the entire list must first be traversed in order to determine it's length. If e is in aex representation, then this inefficiency is not present.

#### Examples

Destructively assign to a part of an exression.

```
(%i1) (a : [1,2,3], ipart(a,1) : 7, a);
(%o1) [7,2,3]
```

Implementation Some tests were performed with large lists of numbers. If we set a:lrange(10^7), then the times required for ipart(a,10^7), ipart(a,-1), inpart(a,10^7), and part(a,10^7) were 30, 60, 90, and 90 ms.

## 3.20 Function: ipart\_set

#### Calling

 $ipart\_set(e, val, ind1, ind2, ...)$  Set part of e specified by the final arguments to val. e is a mixed representation expression.

#### 3.21 Function: ireverse

#### ireverse(e)

mext package: aex

**Description** ireverse is like maxima reverse, but is works on both aex and list objects. ireverse is tries to be identical to maxima reverse for a non-aex argument.

**Arguments** ireverse requires one argument e, which must be non-atomic.

Options ireverse takes options with default values: adj->true, ot->ml.

## Examples

```
(%i1) ireverse(lrange(4));
(%o1) [4,3,2,1]
```

```
(%i1) ireverse(lrange(4), [ot->ar]);
(%o1) <[4,3,2,1]>
```

```
(%i1) ireverse(lrange(4, [ot->ar]));
(%o1) <[4,3,2,1]>
```

```
(%i1) ireverse(lrange(4, [ot->ar]), [ot->ml]);
(%o1) [4,3,2,1]
```

## 3.22 Function: lex

## Calling

lex(e) converts the aex expression e to lex. If e is not an aex expression, e is returned. Conversion is only done on the first level.

## 3.23 Function: raex

raex(e :optional spec)
mext package: aex

**Description** Convert e to aex representation at the specified levels.

**Arguments** raex requires either one or two arguments.

## 3.24 Function: rlex

 $\mathbf{rlex}(e : \text{optional } spec)$ mext package: aex

**Description** Deep copy, converting e to lex representation at the specified levels.

**Arguments** rlex requires either one or two arguments.

## 4 Functions and Variables for Combinatorics

- ae\_random\_permutation
- cycles\_to\_perm
- inverse\_permutation
- perm\_to\_cycles
- perm\_to\_transpositions
- permutation\_p
- $\bullet$  permutation\_p1
- random\_cycle
- random\_permutation\_sym
- signature\_permutation
- transpositions\_to\_perm

## 4.1 Function: ae\_random\_permutation

## $ae\_random\_permutation(a)$

mext package: discrete\_aex

**Description** returns a with subexpressions permuted randomly.

**Arguments** ae\_random\_permutation requires one argument a, which must be non-atomic.

Options ae\_random\_permutation takes options with default values: adj->true, ot->ml.

See also random\_cycle, random\_permutation\_sym, signature\_permutation, perm\_to\_cycles, and cycles\_to\_perm.

## 4.2 Function: cycles\_to\_perm

cycles\_to\_perm(cycles)
mext package: discrete\_aex

**Description** Returns a permutation from its cycle decomposition cycles, which is a list of lists. Here 'permutation' means a permutation of a list of the integers from 1 to some number n. The default output representation is aex.

**Arguments** cycles\_to\_perm requires one argument cycles, which must be a list (lex or aex).

Options cycles\_to\_perm takes options with default values: adj->true, ot->ml.

See also random\_cycle, random\_permutation\_sym, ae\_random\_permutation, signature\_permutation, and perm\_to\_cycles.

## 4.3 Function: inverse\_permutation

#### $inverse\_permutation(perm)$

mext package: discrete\_aex

**Description** Returns the inverse permutation of *perm*.

**Arguments** inverse\_permutation requires one argument *perm*, which must be a list (lex or aex).

Options inverse\_permutation takes options with default values: adj->true, ot->ml.

#### Examples

```
(%i1) inverse_permutation([5,1,4,2,6,8,7,3,10,9]);

(%o1) <[2,4,8,3,1,5,7,6,10,9]>

(%i1) inverse_permutation(inverse_permutation([5,1,4,2,6,8,7,3,10,9]),ot->ml);

(%o1) [5,1,4,2,6,8,7,3,10,9]
```

## 4.4 Function: perm\_to\_cycles

#### perm\_to\_cycles(ain)

mext package: discrete\_aex

**Description** Returns a cycle decomposition of the input permutation ain. The input must be a permutation of n integers from 1 through n.

**Arguments** perm\_to\_cycles requires one argument *ain*, which must be a list (lex or aex).

Options perm\_to\_cycles takes options with default values: adj->true, ot->ml.

## Examples

```
(%i1) perm_to_cycles([5,4,3,2,1,10,6,7,8,9]);
(%o1) [[7,8,9,10,6],[3],[4,2],[5,1]]
```

See also random\_cycle, random\_permutation\_sym, ae\_random\_permutation, signature\_permutation, and cycles\_to\_perm.

## 4.5 Function: perm\_to\_transpositions

# perm\_to\_transpositions(ain) mext package: discrete\_aex

**Description** Returns a list representing the permutation *ain* as a product of transpositions. The output representation type is applied at both levels.

**Arguments** perm\_to\_transpositions requires one argument ain, which must be a list (lex or aex).

Options perm\_to\_transpositions takes options with default values: adj->true, ot->ml.

## 4.6 Function: permutation\_p

#### $permutation_p(ain)$

 $\max$  package: discrete\_aex

#### Calling

**permutation\_p**(list) Returns true if the list list of length n is a permutation of the integers from 1 through n. Otherwise returns false.

**Arguments** permutation\_p requires one argument.

Implementation Separate routines for aex and lex input are used.

## 4.7 Function: permutation\_p1

## $permutation_p1(ain)$

mext package: discrete\_aex

**Description** This is the same as permutation\_p, but, if the input is a list, it assumes all elements in the input list are fixnum integers, while permutation\_p does not.

Arguments permutation\_p1 requires one argument.

**Implementation** Some variables are declared fixnum, but this does not seem to improve performance with respect to permutationp.

## 4.8 Function: random\_cycle

#### $random\_cvcle(n)$

mext package: discrete\_aex

#### Calling

 $random\_cycle(n)$  Returns a random cycle of length n. The return value is a list of the integers from 1 through n, representing an element of the symmetric group  $S_n$  that is a cycle.

**Arguments** random\_cycle requires one argument n, which must be a positive integer.

Options random\_cycle takes options with default values: adj->true, ot->ml.

See also random\_permutation\_sym, ae\_random\_permutation, signature\_permutation, perm\_to\_cycles, and cycles\_to\_perm.

**Implementation** This function uses Sattolo's algorithm.

## 4.9 Function: random\_permutation\_sym

## $random\_permutation\_sym(n)$

mext package: discrete\_aex

## Calling

**random\_permutation\_sym**(n) Returns a random permutation of the integers from 1 through n. This represents a random element of the symmetric group  $S_n$ .

**Arguments** random\_permutation\_sym requires one argument n, which must be a positive integer.

Options random\_permutation\_sym takes options with default values: adj->true, ot->ml.

See also random\_cycle, ae\_random\_permutation, signature\_permutation, perm\_to\_cycles, and cycles\_to\_perm.

## 4.10 Function: signature\_permutation

## ${\bf signature\_permutation}(\mathit{ain})$

mext package: discrete\_aex

#### Calling

**signature\_permutation**(list) returns the sign, or signature, of the symmetric permutation list, which must be represented by a permutation the integers from 1 through n, where n is the length of the list.

**Arguments** signature permutation requires one argument *ain*, which must be a list (lex or aex).

See also random\_cycle, random\_permutation\_sym, ae\_random\_permutation, perm\_to\_cycles, and cycles\_to\_perm.

## 4.11 Function: transpositions\_to\_perm

#### $transpositions\_to\_perm(ain)$

mext package: discrete\_aex

**Description** Returns the permutation specified by the list of transpositions ain.

**Arguments** transpositions\_to\_perm requires one argument ain, which must be a list (lex or aex).

Options transpositions\_to\_perm takes options with default values: adj->true, ot->ml.

Implementation Input is converted to lex on both levels. Default output is aex.

## 5 Functions and Variables for Documentation

- doc\_system\_list
- error\_code
- maxdoc

- maxdoc\_author
- maxdoc\_copyright
- maxdoc\_examples
- maxdoc\_set\_cur\_sec
- maxdoc\_set\_mext\_package
- maxdoc\_split\_text
- mext\_package\_record
- pager\_command
- print\_authors
- $\bullet$  print\_copyrights
- print\_entry\_latex
- print\_implementation
- print\_maxdoc\_entry
- print\_maxdoc\_sections
- print\_sections\_latex
- read\_docs\_with\_pager
- set\_all\_doc\_systems
- simple\_doc\_add
- simple\_doc\_delete
- simple\_doc\_get
- simple\_doc\_init
- simple\_doc\_print

# 5.1 Variable: doc\_system\_list

default value false.

**Description** A list of the documenatation systems that will be searched by ? and ??. This can be set to all avaliable systems with the function set\_all\_doc\_systems. If this variable is false, then all documentation is enabled.

## 5.2 Variable: error\_code

default value false.

**Description** This is an error code set by merror1.

## 5.3 Function: maxdoc

maxdoc(name, docs) mext package: defmfun1

**Description** Add maxdoc documentation entry for item *name* specified by *docs*.

**Arguments** maxdoc requires two arguments. The first argument name must be a string.

Attributes maxdoc has attributes: [hold\_all]

#### 5.4 Function: maxdoc\_author

**maxdoc\_author**(name, author)

mext package: defmfun1

**Description** Set the author(s) for the documentation item *name*.

**Arguments** maxdoc\_author requires two arguments. The first argument *name* must be a string. The second argument *author* must be a string or a list of strings.

## 5.5 Function: maxdoc\_copyright

maxdoc\_copyright(name, copyright)

mext package: defmfun1

**Description** Set the copyright information for the documentation item *name*. *copyright* should typically be a list whose first element is an integer (the year), with the remaining strings naming the copyright holder. This copyright information will not be printed with documentation, unless *print\_copyrights* is true.

**Arguments** maxdoc\_copyright requires two arguments. The first argument name must be a string.

## 5.6 Function: maxdoc\_examples

maxdoc\_examples(name :rest examples)

mext package: defmfun1

**Description** Add maxdoc examples entry for item name specified by examples.

**Arguments** maxdoc\_examples requires one or more arguments. The first argument name must be a string.

Attributes maxdoc\_examples has attributes: [hold\_all]

## 5.7 Function: maxdoc\_set\_cur\_sec

 $maxdoc\_set\_cur\_sec(shortname)$ 

mext package: defmfun1

**Description** Set the current section for maxdoc to *shortname*. This section will be used by functions such as maxdoc, and maxdoc\_author.

**Arguments** maxdoc\_set\_cur\_sec requires one argument *shortname*, which must be a string.

## 5.8 Function: maxdoc\_set\_mext\_package

maxdoc\_set\_mext\_package(packagename)

mext package: defmfun1

**Description** Set the current mext package name for maxdoc to *packagename*. This name will be used by functions specifying documentation for functions until the name is set to another value. When documenting functions written in maxima code, calling mext\_record\_package is probably more useful.

**Arguments** maxdoc\_set\_mext\_package requires one argument packagename, which must be a string.

## 5.9 Function: maxdoc\_split\_text

maxdoc\_split\_text(text)
mext package: defmfun1

**Description** Split the string *text* into a list of strings, using a sequence of one or more spaces as the delimeter. Single newlines are removed.

**Arguments** maxdoc\_split\_text requires one argument text, which must be a string.

## 5.10 Function: mext\_package\_record

mext\_package\_record(docitem, packagename)

mext package: defmfun1

**Description** Set the mext packagename for the function or variable *docitem* to *packagename*. This name will be used when displaying documentation. The function maxdoc\_set\_mext\_package is useful for setting the package name of a group of functions, but there is currently no maxima hook for doing this.

**Arguments** mext\_package\_record requires two arguments. The first argument *docitem* must be a string or a symbol. The second argument *packagename* must be a string.

## 5.11 Variable: pager\_command

default value /usr/bin/less.

**Description** The pathname to the system command used for paged output, for instance, for reading documentation.

## 5.12 Variable: print\_authors

default value true.

**Description** If true, then print the names of the authors with maxdoc documentation.

## 5.13 Variable: print\_copyrights

default value false.

**Description** If true, then print copyright information with maxdoc documentation.

## 5.14 Function: print\_entry\_latex

print\_entry\_latex(item)
mext package: defmfun1

**Arguments** print\_entry\_latex requires one argument *item*, which must be a string.

## 5.15 Variable: print\_implementation

default value true.

**Description** If true, then print implementation information with maxdoc documentation.

## 5.16 Function: print\_maxdoc\_entry

print\_maxdoc\_entry(item)
mext package: defmfun1

**Arguments** print\_maxdoc\_entry requires one argument *item*, which must be a string.

## 5.17 Function: print\_maxdoc\_sections

print\_maxdoc\_sections()
mext package: defmfun1

**Description** Print all sections of maxdoc documentation. This does not include other documentation databases, such as the main maxima documentation.

Arguments print\_maxdoc\_sections requires zero arguments.

#### 5.18 Function: print\_sections\_latex

print\_sections\_latex( :optional filename)

mext package: defmfun1

**Description** Print all sections of maxdoc documentation currently loaded in latex format to the file *file-name*. This does not include other documentation databases, such as the main maxima documentation.

**Arguments** print\_sections\_latex requires either zero or one arguments. If present, the argument *file-name* must be a a string.

## 5.19 Variable: read\_docs\_with\_pager

default value false.

**Description** If true, then documenation printed by describe or ? or ?? is sent through the pager specified by pager\_command. This will most likely only work with a command line interface under linux/unix with certain lisp implementations.

## 5.20 Function: set\_all\_doc\_systems

set\_all\_doc\_systems()
mext package: defmfun1

**Description** Enable all documentation databases for describe, ? and ??. This sets doc\_system\_list to a list of all doc systems.

Arguments set\_all\_doc\_systems requires zero arguments.

## 5.21 Function: simple\_doc\_add

 $simple\_doc\_add(name, content)$ 

mext package: defmfun1

**Description** Adds documentation string *content* for item *name*. These documentation strings are accessible via '?' and '??'.

**Arguments** simple\_doc\_add requires two arguments. The first argument *name* must be a string. The second argument *content* must be a string.

See also simple\_doc\_init, simple\_doc\_delete, simple\_doc\_get, and simple\_doc\_print.

## 5.22 Function: simple\_doc\_delete

simple\_doc\_delete(name)
mext package: defmfun1

**Description** Deletes the simple\_doc documentation string for item *name*.

Arguments simple\_doc\_delete requires one argument name, which must be a string.

See also simple\_doc\_init, simple\_doc\_add, simple\_doc\_get, and simple\_doc\_print.

## 5.23 Function: simple\_doc\_get

simple\_doc\_get(name)
mext package: defmfun1

**Description** Returns the simple\_doc documentation string for item *name*.

**Arguments** simple\_doc\_get requires one argument *name*, which must be a string.

See also simple\_doc\_init, simple\_doc\_add, simple\_doc\_delete, and simple\_doc\_print.

## 5.24 Function: simple\_doc\_init

simple\_doc\_init()
mext package: defmfun1

**Description** Initialize the simple\_doc documentation database.

**Arguments** simple\_doc\_init requires zero arguments.

See also simple\_doc\_add, simple\_doc\_delete, simple\_doc\_get, and simple\_doc\_print.

## 5.25 Function: simple\_doc\_print

simple\_doc\_print(name)
mext package: defmfun1

**Description** Prints the simple\_doc documentation string for item *name*.

**Arguments** simple\_doc\_print requires one argument *name*, which must be a string.

See also simple\_doc\_init, simple\_doc\_add, simple\_doc\_delete, and simple\_doc\_get.

## 6 Functions and Variables for Equations

- alt\_eigen
- nelder\_mead

## 6.1 Function: alt\_eigen

mext package: alt\_eigen

```
Description alt_eigen(mat, ['var=x, 'maxdegree=n, 'orthogonal=boolean])
```

Express the eigenvectors of the matrix mat as a polynomial in the eigenvalue var. When the degree of a factor of the characteristic polynomial has degree maxdegree or less, the code attempts to find all the roots of the factor. The optional variables var, maxdegree (default 1), and orthogonal (default false) can be in any order. When the dimension of an eigenspace is greater than one and orthogonal is true, the list of eigenvectors is orthogonal.

Examples The eigenvectors of matrix([1,2],[4,5]), are

```
(%i1) alt_eigen(matrix([1,2],[4,5]),'var=z);
(%o1) [z^2=6*z+3,[matrix([2],[z-1])]]
```

Substituting the two roots of  $z^2=6*z+3$  in to the column vector matrix([2],[z-1]) gives the two eigenvectors. To find explicit expressions for these eigenvectors, set maxdegree to 2; thus

Here is a matrix with a degenerate eigenvalue:

```
(%i3) m : matrix([5,6,5,6,5,6],[6,5,6,5,6,5],[5,6,5,6,5,6],[6,5,6,5,6,5],
      [5,6,5,6,5,6],[6,5,6,5,6,5])$
(%i4) alt_eigen(m,'var=z);
(%o4) [z=-3,[matrix([-1],[1],[-1],[1],[-1],[1])],z=0,[matrix([0],[-1],[0],[1],[0],[0]),
      matrix([0],[0],[0],[-1],[0],[1]), matrix([0],[0],[1],[0],[-1],[0]),
      matrix([1],[0],[-1],[0],[0])],z=33,[matrix([-1],[-1],[-1],[-1],[-1])]]
```

There are four eigenvectors with eigenvalue 0. To find an orthogonal basis for this eigenspace, set the optional variable *orthogonal* to true; thus

```
(%i5) alt_eigen(m,'var=z, 'orthogonal=true);

(%o5) [z=-3,[matrix([-1],[1],[-1],[1],[-1],[1])],z=0,[matrix([1],[0],[-1/2],[0],

[-1/2],[0]), matrix([0],[0],[1],[0],[-1],[0]),matrix([0],[-1/2],[0],[-1/2],[0],[1]),

matrix([0],[-1],[0],[1],[0],[0])],z=33,[matrix([-1],[-1],[-1],[-1],[-1])]]
```

Author Barton Willis.

## 6.2 Function: nelder\_mead

**nelder\_mead**(*expr*, *vars*, *init*) mext package: nelder\_mead

**Description** The Nelder-Mead optimization algorithm.

**Arguments** nelder\_mead requires three arguments. The second argument *vars* must be a list of symbols. The third argument *init* must be a list of numbers.

#### Examples

Find the minimum of a function at a non-analytic point.

```
(%i1) nelder_mead(if x<0 then -x else x^2, [x], [4]);
(%o1) [x = 9.5364e-11]
```

```
(%i1) f(x) := if x<0 then -x else x^2$
(%i2) nelder_mead(f, [x], [4]);
(%o2) [x = 9.536387892694628e-11]
(%i3) nelder_mead(f(x), [x], [4]);
(%o3) [x = 9.536387892694628e-11]</pre>
```

```
(%i1) nelder_mead(x^4+y^4-2*x*y-4*x-3*y, [x,y], [2,2]); (%o1) [x = 1.1572,y = 1.0993]
```

Author Mario S. Mommer.

## 7 Functions and Variables for Function Definition

- comp\_load
- compile\_file1

## 7.1 Function: comp\_load

comp\_load(fname :optional pathlist)

mext package: aex

**Description** Compile and load a lisp file. Maxima does not load it by default with compile\_file. If the input filename does not end with ".lisp", it will be appended. If *pathlist* is specified, then *fname* is only searched for in directories in *pathlist*.

**Arguments** comp\_load requires either one or two arguments. The first argument *fname* must be a string. The second argument *pathlist* must be a string or a list of strings.

## 7.2 Function: compile\_file1

 $\mathbf{compile\_file1}(input\text{-}\mathit{file}: \mathbf{optional}\ \mathit{bin-file},\ \mathit{translation-output\text{-}\mathit{file}})$  mext package: aex

**Description** This is copied from maxima compile\_file, with changes. Sometimes a loadable binary file is apparently compiled, but an error flag is set and compile\_file returns false for the output binary filename. Here we return the binary filename in any case.

**Arguments** compile\_file1 requires between one and three arguments. The first argument *input-file* must be a string.

## 8 Functions and Variables for Input and Output

- pager\_string
- restore
- restore\_fast
- store
- store\_fast

## 8.1 Function: pager\_string

# $pager\_string(s)$ mext package: aex

**Description** Read the string s in the pager given by the maxima variable pager\_command. This works at least with gcl under linux.

**Arguments** pager\_string requires one argument s, which must be a string.

#### 8.2 Function: restore

## restore(file)

mext package: store

#### Calling

restore(file) Reads and returns expressions from the file file.

**Description** Reads maxima expressions from file *file* created by the function store.

**Arguments** restore requires one argument *file*, which must be a string.

See also store, store\_fast, and restore\_fast.

#### 8.3 Function: restore\_fast

# restore\_fast(file) mext package: store

#### Calling

 $\mathbf{restore\_fast}(file)$  Reads and returns expression from the file file. No checking for circular references is done.

**Description** Reads maxima expressions from file *file* created by the function store, or store\_fast. No checks for circular references are done.

**Arguments** restore\_fast requires one argument *file*, which must be a string.

See also store, restore, and store\_fast.

## 8.4 Function: store

```
store(file :rest exprs) mext package: store
```

#### Calling

**store**(file, expr1, expr2, ...) stores the expressions to the file file.

**Description** Stores maxima expressions *exprs* in *file* in binary format. Many types of lisp expressions and subexpressions are supported: numbers, strings, list, arrays, hashtables, structures,....

**Arguments** store requires one or more arguments. The first argument file must be a string.

## Examples

Save a graph to a file. This cannot be done with the command ¡save¿.

```
(%i1) load(graphs)$
(%i2) c : petersen_graph();
(%o2) GRAPH(10 vertices, 15 edges)
(%i3) factor(graph_charpoly(c,x));
(%o3) (x-3)*(x-1)^5*(x+2)^4
(%i4) store("graph.cls",c)$
(%i5) factor(graph_charpoly( restore("graph.cls"), x));
(%o5) (x-3)*(x-1)^5*(x+2)^4
```

See also restore, store\_fast, and restore\_fast.

Implementation store uses the cl-store library. See the cl-store documentation for more information.

## 8.5 Function: store\_fast

```
store\_fast(file : rest \ exprs) mext package: store
```

#### Calling

**store\_fast**(*file*, *expr1*, *expr2*, ...) stores the expressions to the file *file*. No checking for circular references is done.

**Description** Stores maxima expressions *exprs* in *file* in binary format. This is like **store**, except that no checks for circular references are done.

Arguments store\_fast requires one or more arguments. The first argument file must be a string.

See also store, restore, and restore\_fast.

## 9 Functions and Variables for Lists

These functions manipulate lists. They build lists, take them apart, select elements, etc.

- aelistp
- constant\_list
- count
- drop\_while

- every1
- fold
- fold\_list
- icons
- $\bullet$  imap
- length\_while
- lrange
- nest
- nest\_list
- nest\_while
- nreverse
- partition\_list
- select
- sequence specifier
- table
- take
- take\_while
- tuples

## 9.1 Function: aelistp

**Description** Returns true if e is a list, either ml or ar representation.

## Examples

```
(%i1) aelistp([1,2,3]);
(%o1) true
(%i1) aelistp( aex([1,2,3]));
(%o1) true
(%i2) aelistp(3);
(%o2) false
(%i3) aelistp(x);
(%o3) false
(%i4) x:lrange(10),aelistp(x);
(%o4) true
(%i5) aelistp(%%f(y));
(%o5) false
(%i6) aelistp( aex( %%f(y) ));
(%o6) false
```

## 9.2 Function: constant\_list

```
constant_list(expr, list) mext package: lists_aex
```

**Description** Returns a list of n elements, each of which is an independent copy of expr. constant\_list(expr,[n,m,..]) returns a nested list of dimensions n,m,... where each leaf is an independent copy of expr and the copies of each list at each level are independent. If a third argument is given, then it is used as the op, rather than 'list', at every level.

**Arguments** constant\_list requires either two or three arguments. The second argument *spec* must be a positive integer or a list of positive integers.

Options constant\_list takes options with default values: adj->true, ot->ml.

See also makelist, lrange, and table.

## 9.3 Function: count

```
count(expr, item)
mext package: lists_aex
```

**Description** Counts the number of items in *expr* matching *item*. If *item* is a lambda function then *compile* must be true.

**Arguments** count requires two arguments. The first argument *expr* must be non-atomic and either aex or represented by a lisp list.

Options count takes options with default values: compile->true.

#### Examples

```
(%i1) count([1,2,"dog"], 'numberp);
(%o1) 2
(%i1) count([1,2,"dog"], "dog");
(%o1) 1
(%i2) count(lrange(10^4), lambda([x], is(mod(x,3) = 0)));
(%o2) 3333
(%i3) count( %%ff(1,2,"dog"), "dog");
(%o3) 1
(%i4) count(lrange(100,ot->ar), 'evenp);
(%o4) 50
```

## 9.4 Function: drop\_while

```
drop_while(expr, test)
mext package: lists_aex
```

#### Calling

 $drop\_while(expr, test)$  Tests the elements of expr in order, dropping them until test fails. The remaining elements are returned in an expression with the same op as that expr.

**Arguments** drop\_while requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options drop\_while takes options with default values: adj->true, ot->ml, compile->true.

#### Examples

Drop elements as long as they are negative.

```
(%i1) drop_while([-3,-10,-1,3,6,7,-4], lambda([x], is(x<0)));
(%o1) [3,6,7,-4]
```

## 9.5 Function: every1

every1(expr, test)
mext package: lists\_aex

#### Calling

**every1**(*expr*, *test*) Returns true if *test* is true for each element in *expr*. Otherwise, false is returned. This is like **every** but allow a test that takes only one argument. For some inputs, every1 is much faster than every.

**Arguments** every1 requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options every1 takes options with default values: compile->true.

#### 9.6 Function: fold

mext package: lists\_aex

**Description** fold(f,x,[a,b,c]) returns f(f(f(x,a),b),c).

**Arguments** fold requires three arguments. The third argument v must be non-atomic.

Options fold takes options with default values: adj->true, ot->ml, compile->true.

See also fold\_list and nest.

## 9.7 Function: fold\_list

mext package: lists\_aex

**Description** fold\_list(f,x,[a,b,c]) returns [f(x,a),f(f(x,a),b),f(f(f(x,a),b),c)].

**Arguments** fold\_list requires three arguments. The third argument v must be non-atomic.

Options fold\_list takes options with default values: adj->true, ot->ml, compile->true.

See also fold and nest.

## 9.8 Function: icons

icons(x, e)

**Description** icons is like maxima cons, but less general, and much, much faster. x is a maxima object. e is a maxima list or list-like object, such as [a], or f(a). It is suitable at a minimum, for pushing a number or list or string onto a list of numbers, or strings or lists. If you find icons gives buggy behavior that you are not interested in investigating, use cons instead.

**Implementation** In a function that mostly only does icons in a loop, icons defined with defmfun rather than defmfun1 runs almost twice as fast. So icons is defined with defmfun rather than defmfun1. icons does no argument checking.

## 9.9 Function: imap

imap(f, expr)

mext package: lists\_aex

**Description** Maps functions of a single argument. I guess that map handles more types of input without error. But imap can be much faster for some inputs. This is especially true if a lambda function is passed to imap, as it can be compiled.

**Arguments** imap requires two arguments. The second argument *expr* must be non-atomic.

Options imap takes options with default values: compile->true.

#### Examples

Map sqrt efficiently over a list of floats

With aex expression, no conversions to lex are done.

## 9.10 Function: length\_while

length\_while(expr, test) mext package: lists\_aex

**Description** Computes the length of *expr* while *test* is true.

**Arguments** length\_while requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options length\_while takes options with default values: compile->true.

#### Examples

```
(%i1) length_while([-3,-10,-1,3,6,7,-4], lambda([x], is(x<0)));
(%o1) 3
```

## 9.11 Function: lrange

mext package: lists\_aex

#### Calling

**lrange**(*stop*) returns a list of numbers from 1 through *stop*.

**lrange**(start, stop) returns a list of expressions from start through stop.

**lrange**(start, stop, incr) returns a list of expressions from start through stop in steps of incr.

**Description** lrange is much more efficient than makelist for creating ranges, particularly for large lists (e.g. 10<sup>5</sup> or more items.) Functions for creating a list of numbers, in order of decreasing speed, are: lrange, table, create\_list\_makelist.

**Arguments** lrange requires between one and three arguments. The third argument *incr* must be an expression that is not zero.

Options lrange takes options with default values: adj->true, ot->ml.

#### Examples

```
(%i1) lrange(6);
(%o1) [1,2,3,4,5,6]
(%i1) lrange(2,6);
(%o1) [2,3,4,5,6]
(%i2) lrange(2,6,2);
(%o2) [2,4,6]
(%i3) lrange(6,1,-1);
(%o3) [6,5,4,3,2,1]
(%i4) lrange(6,1,-2);
(%o4) [6,4,2]
(%i5) lrange(6,ot->ar);
(%o5) <[1,2,3,4,5,6]>
```

The type of the first element and increment determine the type of the elements.

```
(%i1) lrange(1.0,6);

(%o1) [1.0,2.0,3.0,4.0,5.0,6.0]

(%i1) lrange(1.0b0,6);

(%o1) [1.0b0,2.0b0,3.0b0,4.0b0,5.0b0,6.0b0]

(%i2) lrange(1/2,6);

(%o2) [1/2,3/2,5/2,7/2,9/2,11/2]

(%i3) lrange(6.0,1,-1);

(%o3) [6.0,5.0,4.0,3.0,2.0,1.0]
```

Symbols can be used for limits or increments.

```
(%i1) lrange(x,x+4);

(%o1) [x,x+1,x+2,x+3,x+4]

(%i1) lrange(x,x+4*a,a);

(%o1) [x,x+a,x+2*a,x+3*a,x+4*a]
```

See also makelist, table, and constant\_list.

#### 9.12 Function: nest

 $mext\ package:\ lists\_aex$ 

**Description** nest(f,x,n) returns f(...f(f(f(x)))...) where there are n nested calls of f.

**Arguments** nest requires three arguments. The first argument f must be a function. The third argument n must be a non-negative integer.

Options nest takes options with default values: adj->true, ot->ml, compile->true.

#### 9.13 Function: nest\_list

```
\mathbf{nest\_list}(f, x, n)
mext package: lists_aex
```

**Arguments** nest\_list requires three arguments. The third argument n must be a non-negative integer.

Options nest\_list takes options with default values: adj->true, ot->m1, compile->true.

#### Examples

Find the first 10 primes after 100.

```
(%i1) nest_list(next_prime,100,10);
(%o1) [101,103,107,109,113,127,131,137,139,149]
```

See also nest, fold, and fold\_list.

#### 9.14 Function: nest\_while

```
\mathbf{nest\_while}(f, x, test : optional min, max) mext package: lists_aex
```

## Calling

 $\mathbf{nest\_while}(f,\ x,\ test)$  applies f to x until test fails to return true when called on the nested result.

 $\mathbf{nest\_while}(f, x, test, min)$  applies f at least min times.

 $\mathbf{nest\_while}(f, x, test, min, max)$  applies f not more than max times.

**Arguments** nest\_while requires between three and five arguments. The fourth argument *min* must be a non-negative integer. The fifth argument *max* must be a non-negative integer.

Options nest\_while takes options with default values: adj->true, ot->ml, compile->true.

**Implementation** This should be modified to allow applying test to more than just the most recent result.

## 9.15 Function: nreverse

#### nreverse(e)

mext package: lists\_aex

**Description** Destructively reverse the arguments of expression e. This is more efficient than using reverse.

**Arguments** nreverse requires one argument e, which must be non-atomic.

## Examples

Be careful not to use a after applying neverse. Do assign the result to another variable.

```
(%i1) a : lrange(10), b : nreverse(a);

(%o1) [10,9,8,7,6,5,4,3,2,1]

(%i1) a : lrange(10,ot->ar), b : nreverse(a);

(%o1) <[10,9,8,7,6,5,4,3,2,1]>
```

See also reverse.

## 9.16 Function: partition\_list

```
partition_list(e, nlist:optional dlist)
mext package: lists_aex
```

#### Calling

```
partition\_list(e, n) partitions e into sublists of length n partition\_list(e, n, d) partitions e into sublists of length n with offsets d.
```

**Description** Omitting d is equivalent to giving d equal to n. e can be any expression, not only a list. If n is a list, then partition\_list partitions at successively deeper levels with elements of n. If n and d are lists, the first elements of n and d apply at the highest level and so on. If n is a list and d is a number, then the offset d is used with each of the n.

**Arguments** partition\_list requires either two or three arguments. The first argument e must be non-atomic. The second argument nlist must be an integer or a list of integers. The third argument dlist must be an integer or a list of integers.

## Examples

Partition the numbers from 1 through 10 into pairs.

```
(%i1) partition_list([1,2,3,4,5,6,7,8,9,10],2);
(%o1) [[1,2],[3,4],[5,6],[7,8],[9,10]]
```

## 9.17 Function: select

```
\mathbf{select}(expr,\ test: optional\ n) mext package: lists_aex
```

**Description** Returns a list of all elements of expr for which test is true. expr may have any op. If n is supplied, then at most n elements are examined.

**Arguments** select requires either two or three arguments. The first argument expr must be non-atomic and represented by a lisp list. The third argument n must be a positive integer.

Options select takes options with default values: adj->true, ot->ml, compile->true.

#### Examples

Select elements less than 3

```
(%i1) select([1,2,3,4,5,6,7], lambda([x], is(x<3)));
(%o1) [1,2]
```

#### 9.18 Argument type: sequence specifier

**Description** A sequence specification specifies a subsequence of the elements in an expression. A single positive number n means the first n elements. -n means the last n elements. A list of three numbers [i1,i2,i3] means the i1th through the i2th stepping by i3. If i1 or i2 are negative, they count from the end. If i3 is negative, stepping is down and i1 must be greater than or equal to i2. If i3 is omitted, it is taken to be 1. A sequence specifier can also be one of 'all 'none or 'reverse, which mean all elements, no elements or all elements in reverse order respectively.

See also take and string\_take.

## 9.19 Function: table

mext package: lists\_aex

#### Calling

table(expr, [n]) Evaluates expression number times. If number is not an integer or a floating point number, then float is called. If we have a floating point number, it is truncated into an integer. This type of iterator is the fastest, since no variable is bound.

table(expr, [variable, initial, end, step]) Returns a list of evaluated expressions where variable (a symbol) is set to a value. The first element of the returned list is expression evaluated with variable set to initial. The i-th element of the returned list is expression evaluated with variable set to initial+(i-1)step. The iteration stops once the value is greater (if step is positive) or smaller (if step is negative) than end. Requirement: The difference between end and initial must return a numberp number. step must be a nonzero numberp number. This allows for iterators of rather general forms like [i, %i - 2, %i, 0.1b0] ...

table(expr, [variable, initial, end]) This iterator uses a step of 1 and is equal to [variable,initial, end, 1].

**Arguments** table requires two or more arguments. The second argument *iterator1* must be a list. Each of the remaining arguments must be a list.

Options table takes options with default values: adj->true, ot->ml.

Attributes table has attributes: [hold\_all]

#### Examples

Make a list of function values

```
(%i1) table(sin(x),[x,0,2*%pi,%pi/4]);
(%o1) [0,1/sqrt(2),1,1/sqrt(2),0,-1/sqrt(2),-1,-1/sqrt(2),0]
```

Make a nested list.

```
(%i1) table(x^y, [x,1,2], [y,1,2]);
(%o1) [[1,1],[2,4]]
```

See also makelist, lrange, and constant\_list.

Author Ziga Lenarcic.

#### 9.20 Function: take

```
take(e : rest v)
mext package: lists_aex
```

#### Calling

take(e, n) returns a list of the first n elements of list or expression e.

take(e, [n1, n2]) returns a list of the n1th through n2th elements of list or expression e.

 $\mathbf{take}(e, [n1, n2, step])$  returns a list of the n1th through n2th elements stepping by step of list or expression e.

take(e, -n) returns the last n elements.

take(e, spec1, spec2, ...) applies the sequence specifications at successively deeper levels in e.

**Description** e can have mixed lex and aex expressions on different levels. If more sequence specifications are given, they apply to successively deeper levels in e.

**Arguments** take requires one or more arguments. The first argument e must be non-atomic. Each of the remaining arguments must be a sequence specification.

#### Examples

Take the first 3 elements of a list.

```
(%i1) take([a,b,c,d,e],3);
(%o1) [a,b,c]
```

Take the last 3 elements of a list.

```
(%i1) take([a,b,c,d,e],-3);
(%o1) [c,d,e]
```

Take the second through third elements of a list.

```
(%i1) take([a,b,c,d,e],[2,3]);
(%o1) [b,c]
```

Take the second through tenth elements of a list counting by two.

```
(%i1) take([1,2,3,4,5,6,7,8,9,10],[2,10,2]);
(%o1) [2,4,6,8,10]
```

Take the last through first elements of a list counting backwards by one.

```
(%i1) take([a,b,c,d],[-1,1,-1]);
(%o1) [d,c,b,a]
```

Shorthand for the previous example is 'reverse.

```
(%i1) take([a,b,c,d],'reverse);
(%o1) [d,c,b,a]
```

Take the second through third elements at the first level and the last 2 elements at the second level.

```
(%i1) take([[a,b,c], [d,e,f], [g,h,i]], [2,3],-2);
(%o1) [[e,f],[h,i]]
```

## 9.21 Function: take\_while

```
take_while(expr, test)
mext package: lists_aex
```

#### Calling

 $take\_while(expr, test)$  collects the elements in expr until test fails on one of them. The op of the returned expression is the same as the op of expr.

**Arguments** take\_while requires two arguments. The first argument *expr* must be non-atomic and represented by a lisp list.

Options take\_while takes options with default values: adj->true, ot->ml, compile->true.

#### Examples

Take elements as long as they are negative.

```
(%i1) take_while([-3,-10,-1,3,6,7,-4], lambda([x], is(x<0)));
(%o1) [-3,-10,-1]
```

## 9.22 Function: tuples

```
 \begin{array}{l} \mathbf{tuples}(\mathit{list-or-lists}: \mathtt{optional}\ \mathit{n}) \\ \mathtt{mext}\ \mathtt{package:}\ \mathtt{lists\_aex} \end{array}
```

## Calling

tuples (list, n) Return a list of all lists of length n whose elements are chosen from list.

tuples([list1, list2, ...]) Return a list of all lists whose i-th element is chosen from listi.

**Arguments** tuples requires either one or two arguments. The first argument list-or-lists must be non-atomic and represented by a lisp list. The second argument n must be a non-negative integer.

Options tuples takes options with default values: adj->true, ot->ml.

#### Examples

Make all three letter words in the alphabet 'a,b'.

```
(%i1) tuples([a,b],3);
(%o1) [[a,a,a],[a,a,b],[a,b,a],[a,b,b],[b,a,a],[b,a,b],[b,b,a],[b,b,b]]
```

Take all pairs chosen from two lists.

```
(%i1) tuples([[0,1], [x,y,z]]);
(%o1) [[0,x],[0,y],[0,z],[1,x],[1,y],[1,z]]
```

tuples works for expressions other than lists.

```
(%i1) tuples(f(0,1),3);
(%o1) [f(0,0,0),f(0,0,1),f(0,1,0),f(0,1,1),f(1,0,0),f(1,0,1),f(1,1,0),f(1,1,1)]
```

## 10 Functions and Variables for Number Theory

- $\bullet \ abundant\_p$
- aliquot\_sequence
- aliquot\_sum
- amicable\_p
- catalan\_number

- divisor\_function
- divisor\_summatory
- from\_digits
- integer\_digits
- integer\_string
- oeis\_A092143
- perfect\_p
- prime\_pi
- prime\_pi\_soe
- prime\_twins
- primes1

## 10.1 Function: abundant\_p

## $abundant_p(n)$

mext package: discrete\_aex

**Description** Returns true if n is an abundant number. Otherwise, returns false.

**Arguments** abundant\_p requires one argument n, which must be a positive integer.

#### Examples

The abundant numbers between 1 and 100

```
(%i1) select(lrange(100),abundant_p);
(%o1) [12,18,20,24,30,36,40,42,48,54,56,60,66,70,72,78,80,84,88,90,96,100]
```

See also divisor\_function, aliquot\_sum, aliquot\_sequence, divisor\_summatory, and perfect\_p.

## 10.2 Function: aliquot\_sequence

# $aliquot\_sequence(k, n)$ mext package: discrete\_aex

**Description** The aliquot sequence is a recursive sequence in which each term is the sum of the proper divisors of the previous term. This function returns the first n elements (counting from zero) in the aliquot sequence whose first term is k. The sequence is truncated at an element if it is zero or repeats the previous element.

**Arguments** aliquot\_sequence requires two arguments. The first argument k must be a positive integer. The second argument n must be a non-negative integer.

#### Examples

Perfect numbers give a repeating sequence of period 1.

```
(%i1) imap(lambda([x],aliquot_sequence(x,100)),[6,28,496,8128]);
(%o1) [[6],[28],[496],[8128]]
```

Aspiring numbers are those which are not perfect, but terminate with a repeating perfect number.

```
(%i1) imap(lambda([x],aliquot_sequence(x,100)),[25, 95, 119, 143, 417, 445, 565, 608, 650, 652, 675, 68 (%o1) [[25,6],[95,25,6],[119,25,6],[143,25,6],[417,143,25,6],[445,95,25,6],[565,119,25,6],[608,652,496]
```

See also divisor\_function, aliquot\_sum, divisor\_summatory, perfect\_p, and abundant\_p.

## 10.3 Function: aliquot\_sum

#### $aliquot\_sum(n)$

mext package: discrete\_aex

**Description** Returns the aliquot sum of n. The aliquot sum of n is the sum of the proper divisors of n.

**Arguments** aliquot\_sum requires one argument n, which must be a positive integer.

Attributes aliquot\_sum has attributes: [match\_form]

See also divisor\_function, aliquot\_sequence, divisor\_summatory, perfect\_p, and abundant\_p.

## 10.4 Function: amicable\_p

### $\mathbf{amicable\_p}(n, m)$

mext package: discrete\_aex

**Description** Returns true if n and m are amicable, and false otherwise.

**Arguments** amicable\_p requires two arguments. The first argument n must be a positive integer. The second argument m must be a positive integer.

#### Examples

The first few amicable pairs.

#### 10.5 Function: catalan\_number

### $catalan\_number(n)$

mext package: discrete\_aex

**Description** Returns the *n*th catalan number.

Arguments catalan\_number requires one argument.

#### Examples

The catalan number for n from 1 through 12.

```
(%i1) map(catalan_number,lrange(12));
(%o1) [1,2,5,14,42,132,429,1430,4862,16796,58786,208012]
```

The n'th catalan number.

```
(%i1) catalan_number(n);
(%o1) binomial(2*n,n)/(n+1)
```

OEIS number: A000108.

#### 10.6 Function: divisor\_function

**divisor\_function**(n :optional x) mext package: discrete\_aex

**Description** Returns the divisor function, or sum of positive divisors function

$$\sigma_x(n) = \sum_{d|n} d^x,$$

where d|x means d divides n. If x is omitted it takes the default value 0. Currently, complex values for x are not supported. After writing this, I noticed that the function is implemented in the maxima core and is callled divsum.

**Arguments** divisor\_function requires either one or two arguments. The first argument n must be a non-negative integer. The second argument x must be a number.

Attributes divisor\_function has attributes: [match\_form]

OEIS number: A000005 for x=0 and A000203 for x=1.

See also aliquot\_sum, aliquot\_sequence, divisor\_summatory, perfect\_p, and abundant\_p.

## 10.7 Function: divisor\_summatory

 $\mathbf{divisor\_summatory}(x)$ 

mext package: discrete\_aex

**Description** Returns the divisor summatory function D(x) for x. The divisor\_function  $\sigma_0(n)$  counts the number of unique divisors of the natural number n. D(x) is the sum of  $\sigma_0(n)$  over  $n \le x$ .

**Arguments** divisor\_summatory requires one argument x, which must be a non-negative number.

Attributes divisor\_summatory has attributes: [match\_form]

Examples

D(n) for n from 1 through 12

```
(%i1) map(divisor_summatory,lrange(12));
(%o1) [1,3,5,8,10,14,16,20,23,27,29,35]
```

OEIS number: A006218.

See also divisor function, aliquot\_sum, aliquot\_sequence, perfect\_p, and abundant\_p.

# 10.8 Function: from\_digits

 $\mathbf{from\_digits}(\mathit{digits}: \mathtt{optional}\ \mathit{base})$ 

mext package: discrete\_aex

Calling

from\_digits(digits) returns the integer represented by the decimal digits in the list or string digits.

from\_digits(digits, base) returns the integer represented by the base base digits in the list or string digits.

**Description** base need not be number, but may be, for instance, a symbol. If base is a number it must be an integer between 2 and 36. digits may be a string rather than a list.

**Arguments** from digits requires either one or two arguments. The first argument digits must be a list (lex or aex) or a string.

See also integer\_digits and integer\_string.

# 10.9 Function: integer\_digits

integer\_digits(n :optional base, len)

mext package: discrete\_aex

# Calling

 $integer\_digits(n)$  returns a list of the base 10 digits of n.

 $integer\_digits(n, base)$  returns a list of the base base digits of n.

**integer\_digits**(n, base, len) returns a list of the base base digits of n padded with 0's so that the total length of the list is len.

**Arguments** integer\_digits requires between one and three arguments. The first argument *n* must be an integer. The second argument *base* must be a valid radix (an integer between 2 and 36). The third argument *len* must be a non-negative integer.

Options integer\_digits takes options with default values: adj->true, ot->ml.

See also from\_digits and integer\_string.

Implementation gcl is much faster than the others. integer\_digits( $2^(10^6)$ ): typical times for lisps: ccl-1.7-r15184M = 65s, sbcl-1.0.52.0.debian = 1.5s, allegro-8.2 = 23s, Mma-3.0 = 5s, gcl-2.6.7 = 0.11s, Mma-8 = 0.04s. The base is limited to 36 only because we call write-to-string.

# 10.10 Function: integer\_string

 $integer\_string(n : optional base, pad)$ 

mext package: discrete\_aex

#### Calling

 $integer\_string(n)$  returns a string containing the decimal digits of the integer n.

 $integer\_string(n, base)$  returns a string containing the base base digits of the integer n.

integer\_string(n, base, pad) pads the string on the left with 0's so that the length of the string is pad.

 $integer\_string(n, "roman")$  returns a string containing the roman-numeral form of the integer n.

 $integer\_string(n, "cardinal")$  returns a string containing the english word form of the integer (cardinal number) n.

 $integer\_string(n, "ordinal")$  returns a string containing the english word form of the ordinal (counting) number n.

**Arguments** integer\_string requires between one and three arguments. The first argument n must be an integer. The second argument base must be a valid radix (an integer between 2 and 36) or a string. The third argument pad must be a positive integer.

See also integer\_digits and from\_digits.

#### 10.11 Function: oeis\_A092143

 $oeis\_A092143(n)$ 

mext package: discrete\_aex

**Description** Returns the cumulative product of all divisors of integers from 1 to n.

**Arguments** oeis\_A092143 requires one argument n, which must be a positive integer.

# 10.12 Function: perfect\_p

 $\mathbf{perfect}_{-}\mathbf{p}(n)$ 

mext package: discrete\_aex

**Description** Returns true if n is a perfect number. Otherwise, returns false.

**Arguments** perfect\_p requires one argument n, which must be a positive integer.

See also divisor\_function, aliquot\_sum, aliquot\_sequence, divisor\_summatory, and abundant\_p.

**Implementation** This function computes divisors. It would be far more efficient to use a table of known perfect numbers, as very few of them are accessible by current computer hardware.

# 10.13 Function: prime\_pi

 $prime_pi(n)$ 

mext package: prime\_pi

Calling

 $\mathbf{prime\_pi}(n)$  returns the number of primes less than or equal to n.

**Description** Computes the prime counting function. The option threads specifies the maximum number of cpu threads to use. The routine may use fewer threads, depending on the value of n. The percent of the calculation that is finished is printed during the calculation if the option status is true. The status will only work under some terminals.

**Arguments** prime\_pi requires one argument n, which must be equivalent to an unsigned 64 bit integer (that is, an integer between 0 and 2 to the power 64) (We need to modify the doc system so we can use notation for powers in arg check strings.

Options prime\_pi takes options with default values: status->false, threads->1.

See also prime\_pi\_soe, next\_prime, and prev\_prime.

**Implementation** This algorithm is fast, for a general purpose mathematics program. It combines a segmented sieve implemented as a C library with tables.

Authors Kim Walisch (C library), Tomas Oliveira e Silva (tables), and John Lapevre (lisp).

# 10.14 Function: prime\_pi\_soe

 $\mathbf{prime\_pi\_soe}(n)$ 

mext package: discrete\_aex

**Description** The prime counting function. The algorithm is the sieve of Eratosthenes. Internally an array of n bits is used.

**Arguments** prime\_pi\_soe requires one argument n, which must be a non-negative integer.

See also prime\_pi, next\_prime, and prev\_prime.

**Implementation** This is not the most efficient way to compute primes.

# 10.15 Function: prime\_twins

**prime\_twins**(min :optional max)

mext package: prime\_pi

Calling

 $\mathbf{prime\_twins}(n)$  returns the number of prime twins less than or equal to n.

**prime\_twins**(nmin, nmax) returns the number of prime twins between nmin and max.

**Description** The option *ktuplet* counts the *ktuplet*-constellation rather than the twins. *ktuplet* must be an integer between 1 and 7.

**Arguments** prime\_twins requires either one or two arguments. The first argument min must be equivalent to an unsigned 64 bit integer (that is, an integer between 0 and 2 to the power 64) (We need to modify the doc system so we can use notation for powers in arg check strings. The second argument max must be equivalent to an unsigned 64 bit integer (that is, an integer between 0 and 2 to the power 64) (We need to modify the doc system so we can use notation for powers in arg check strings.

Options prime\_twins takes options with default values: ktuplet->2, status->false, threads->1.

 $\mathbf{See} \ \mathbf{also} \ \ \mathsf{prime\_pi}, \ \mathsf{next\_prime}, \ \mathsf{prev\_prime}, \ \mathrm{and} \ \mathsf{primep}.$ 

Implementation No tables are used in this algorithm.

# 10.16 Function: primes1

**primes1**(*n1* :optional *n2*) mext package: discrete\_aex

### Calling

primes1(max) returns a list of the primes less than or equal to max.

primes1(min, max) returns a list of the primes between min and max.

**Description** The algorithm is the sieve of Eratosthenes. This is not an efficient algorithm.

**Arguments** primes 1 requires either one or two arguments. The first argument n1 must be a non-negative integer. The second argument n2 must be a non-negative integer.

Options primes1 takes options with default values: adj->true, ot->ml.

# 11 Functions and Variables for Numerical Computation

Functions for numerical computations: Numeric integration; Mathematical functions—cos,sin,etc. —that accept only numerical arguments. Tests of loops in untranslated code show that these are much more efficient than using the standard maxima versions. But, for most applications, the standard Maxima versions are probably ok.

- n\_abs
- n\_acos
- n\_acosh
- n\_asin
- n\_asinh
- n\_atan
- n\_atanh
- n\_cos

- n\_cosh
- n\_exp
- n\_expt
- n\_log
- n\_sin
- n\_sinh
- n\_sqrt
- n\_tan
- n\_tanh
- nintegrate

#### 11.1 Function: n\_abs

**Description** n\_abs calls the lisp numeric function ?abs. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_abs may be considerably faster in some code, particularly untranslated code.

#### 11.2 Function: n\_acos

**Description** n<sub>a</sub>cos calls the lisp numeric function ?acos. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n<sub>a</sub>cos may be considerably faster in some code, particularly untranslated code.

#### 11.3 Function: n\_acosh

**Description** n\_acosh calls the lisp numeric function ?acosh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_acosh may be considerably faster in some code, particularly untranslated code.

#### 11.4 Function: n asin

**Description** n\_asin calls the lisp numeric function ?asin. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_asin may be considerably faster in some code, particularly untranslated code.

# 11.5 Function: n\_asinh

**Description** n\_asinh calls the lisp numeric function ?asinh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_asinh may be considerably faster in some code, particularly untranslated code.

#### 11.6 Function: n\_atan

**Description** n\_atan calls the lisp numeric function ?atan. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_atan may be considerably faster in some code, particularly untranslated code.

#### 11.7 Function: n\_atanh

**Description** n\_atanh calls the lisp numeric function ?atanh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_atanh may be considerably faster in some code, particularly untranslated code.

#### 11.8 Function: n\_cos

**Description** n\_cos calls the lisp numeric function ?cos. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_cos may be considerably faster in some code, particularly untranslated code.

#### 11.9 Function: n\_cosh

**Description** n\_cosh calls the lisp numeric function ?cosh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_cosh may be considerably faster in some code, particularly untranslated code.

# 11.10 Function: n\_exp

**Description** n\_exp calls the lisp numeric function ?exp. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_exp may be considerably faster in some code, particularly untranslated code.

# 11.11 Function: n\_expt

**Description** n\_expt calls the lisp numeric function ?expt. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_expt may be considerably faster in some code, particularly untranslated code.

#### 11.12 Function: n<sub>-</sub>log

**Description** n\_log calls the lisp numeric function ?log. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_log may be considerably faster in some code, particularly untranslated code.

# 11.13 Function: n\_sin

**Description** n\_sin calls the lisp numeric function ?sin. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_sin may be considerably faster in some code, particularly untranslated code.

#### 11.14 Function: n\_sinh

**Description** n\_sinh calls the lisp numeric function ?sinh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_sinh may be considerably faster in some code, particularly untranslated code.

#### 11.15 Function: n\_sqrt

**Description** n\_sqrt calls the lisp numeric function ?sqrt. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_sqrt may be considerably faster in some code, particularly untranslated code.

#### 11.16 Function: n\_tan

**Description** n\_tan calls the lisp numeric function ?tan. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_tan may be considerably faster in some code, particularly untranslated code.

#### 11.17 Function: n\_tanh

**Description** n\_tanh calls the lisp numeric function ?tanh. This function accepts only float or integer arguments from maxima (lisp complex and rationals, as well.). n\_tanh may be considerably faster in some code, particularly untranslated code.

# 11.18 Function: nintegrate

nintegrate(expr, varspec :optional singlist)
mext package: numerical

**Description** Numerically integrate expr, with the variable and limits supplied in the list varspec as [var, lo, hi]. Only one-dimensional integrals are implemented. nintegrate automatically chooses and combines qags,qagp, and qagi. Some support for complex numbers is implemented. Some integrable singularities are found automatically. See the Maxima documentation for quadpack.

**Arguments** nintegrate requires either two or three arguments. The second argument *varspec* must be a list. The third argument *singlist* must be a list.

Options nintegrate takes options with default values: calls->false, epsrel->1.e-8, epsabs->0, subint->200, words->true.

#### Examples

```
(%i1) nintegrate(sin(sin(x)), [x,0,2]);
(%o1) [1.24706, 1.38451e-14, 21, no problems]
```

Integrate over a semi-infinite interval with an internal singularity. The location of the singularity is supplied. This cannot be done with a single call to quadpack routines.

```
(%i2) nintegrate(1/sqrt(abs(1-x))*exp(-x),[x,0,inf], [1]);
(%o2) [1.72821, 1.87197e-10, 660, no problems]
```

If a list of possible singular points is not supplied, then they will be searched for using solve.

```
(%i3) nintegrate(1/sqrt(abs(1-x))*exp(-x),[x,0,inf]);
(%o3) [1.72821, 1.87197e-10, 660, no problems]
```

In some cases, complex numbers are treated correctly. (The simplifier replaces cos(%i\*x) with cosh(x) before the routine is called. So this works with quad\_qags as well.)

```
(%i4) nintegrate( cos(%i*x), [x,0,1]);
(%o4) [1.1752, 1.30474e-14, 21, no problems]
```

```
(%i5) sinh(1.0);
(%o5) 1.1752
```

But, the quadpack routines cannot handle the complex numbers in this example.

```
(%i6) nintegrate(exp(%i*x) * exp(-x*x), [x,0,inf]);
(%o6) [.424436 %i + .690194, 4.988325e-9, 300, no problems]
```

Return quadpack error code rather than error text.

```
(%i7) nintegrate(sin(sin(x)), [x,0,2], words->false);
(%o7) [1.24706, 1.38451e-14, 21, 0]
```

Request a relative error.

```
(%i8) nintegrate(exp(%i*x) * exp(-x*x), [x,0,inf], epsrel -> 1e-12);
(%o8) [.424436 %i + .690194, 1.06796e-13, 480, no problems]
```

Trying to do the integral with too few sub-intervals fails.

```
(%i9) nintegrate(1/(1+x^2), [x, 0, inf], subint -> 2, epsrel -> 1e-10);
(%o9) [1.5708, 2.57779e-10, 45, too many sub-intervals]
```

This integral is not handled well. Giving limits of minf and inf fails.

```
(%i10) nintegrate(exp(%i*x*x),[x,-200,200],subint->10000);
(%o10) [1.25170114 %i + 1.25804682, 2.507635982e-8, 760578, no problems]
```

```
(%i11) integrate(exp(%i*x*x),x,minf,inf);
(%o11) sqrt(%pi)*(%i/sqrt(2)+1/sqrt(2))
```

```
(%i12) rectform(float(%));
(%o12) 1.25331414*%i+1.25331414
```

Return a list of calls made to quadpack.

```
(%i13) nintegrate(1/sqrt(abs(1-x)) * exp(-x),[x,0,inf], calls->true);
(%o13) [1.72821,1.87197e-10,660, no problems,
[quad_qagi(%e^-x/sqrt(abs(x-1)),x,1.0,inf,epsrel = 1.e-8,epsabs = 0,limit = 200),
   quad_qagp(%e^-x/sqrt(abs(x-1)),x,0,1.0,[],epsrel = 1.e-8,epsabs = 0,limit = 200)]]
```

Here we must supply the roots of sin(x) within the range of integration.

```
(%i14) nintegrate(1/(sqrt(sin(x))),[x,0,10], [%pi,2*%pi,3*%pi]);
(%o14) [10.48823021716687 - 6.769465521725385 %i, 9.597496930524585e-8, 1596, no problems]
```

See also quad\_qags, quad\_qagi, and quad\_qagp.

# 12 Functions and Variables for Numerics

These are mathematical functions—cos,sin,etc. —that accept only numerical arguments. Tests of loops in untranslated code show that these are much more efficient than using the standard maxima versions. But, for most applications, the standard maxima versions are probably ok.

## 13 Functions and Variables for Predicates

- aex\_p
- cmplength
- lengthOp
- length1p
- length\_eq
- type\_of

### 13.1 Function: aex\_p

 $\mathbf{aex}_{\mathbf{p}}(e)$ 

mext package: aex

**Description** Returns true if e is an aex expression, otherwise false.

**Arguments** aex\_p requires one argument.

### 13.2 Function: cmplength

```
\mathbf{cmplength}(e, n) mext package: aex
```

**Description** return the smaller of n and length(e). This is useful if e is very large and n is small, so that computing the entire length of e is inefficient. Expression e can be either a lex of aex expression.

**Arguments** cmplength requires two arguments. The second argument n must be a non-negative integer.

See also length0p, length\_eq, and length1p.

**Implementation** complength is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

# 13.3 Function: length0p

#### length0p(e)

mext package: aex

**Description** Returns true if je; is of length 0, false otherwise. This implementation traverse no more elements of je; than necessary to return the result.

**Arguments** length0p requires one argument e, which must be a string or non-atomic.

See also cmplength, length\_eq, and length1p.

**Implementation** length0p is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

# 13.4 Function: length1p

#### length1p(e)

mext package: aex

**Description** Returns true if e is of length 1, false otherwise. This implementation traverse no more elements of e than necessary to return the result.

**Arguments** length1p requires one argument e, which must be a string or non-atomic.

See also lengthOp, cmplength, and length\_eq.

**Implementation** length1p is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

# 13.5 Function: length\_eq

# $\mathbf{length\_eq}(\mathit{e}, \mathit{n})$

mext package: aex

**Description** Returns true if e is of length n, false otherwise. This implementation traverses no more elements of e than necessary to return the result.

**Arguments** length\_eq requires two arguments. The first argument e must be a string or non-atomic. The second argument n must be a non-negative integer.

See also length0p, cmplength, and length1p.

**Implementation** length\_eq is implemented with defmfun1, which slows things down a bit. So be cautious using it in a tight loop.

# 13.6 Function: type\_of

 $\mathbf{type\_of}(e : optional \ verbose)$ 

mext package: aex

**Description** Return something like the 'type' of a maxima expression. This is a bit ill defined currently. type\_of uses the lisp function type-of.

Arguments type\_of requires either one or two arguments.

# Examples

```
(%i1) type_of(1);
(%o1) ?bit
```

```
(%i1) type_of(1.0);
(%o1) ?double\-float
(%i2) type_of(1.0b0);
(%o2) ?bfloat
(%i3) type_of(1/3);
(%03) /
(%i4) type_of("dog");
(%o4) ?string
(%i5) type_of([1,2,3]);
(%o5) [
(%i6) type_of(aex([1,2,3]));
(%06) [
(%i7) type_of(%e);
(%o7) ?symbol
(%i8) type_of(%i);
(%o8) ?symbol
(%i9) type_of(%i+1);
(\%09) +
```

type\_of returns the type of the lisp struct corresponding to a maxima object.

```
(%i1) load(graphs)$
(%i2) type_of(new_graph());
(%o2) graph
```

# 14 Functions and Variables for Program Flow

• error\_str

### 14.1 Function: error\_str

```
\begin{array}{l} \mathbf{error\_str}() \\ \mathbf{mext} \ \mathbf{package:} \ \mathbf{aex} \end{array}
```

**Description** Returns the last error message as a string.

Arguments error\_str requires zero arguments.

See also error and errormsg.

# 15 Functions and Variables for Quicklisp

- quicklisp\_apropos
- quicklisp\_install
- quicklisp\_load
- quicklisp\_start

# 15.1 Function: quicklisp\_apropos

quicklisp\_apropos(term)
mext package: quicklisp

**Description** Search quicklisp for lisp 'systems' (packages) matching term.

**Arguments** quicklisp\_apropos requires one argument *term*, which must be a string.

# 15.2 Function: quicklisp\_install

quicklisp\_install()
mext package: quicklisp

**Description** Download and install quicklisp from the internet. This is usually done automatically as the final step of building and installing the maxima interface to quicklisp.

Arguments quicklisp\_install requires zero arguments.

# 15.3 Function: quicklisp\_load

quicklisp\_load(package\_name)

mext package: quicklisp

Description Load the asdf lisp package package\_name, or, if not installed, install from the internet and

then load.

**Arguments** quicklisp\_load requires one argument *package\_name*, which must be a string.

# 15.4 Function: quicklisp\_start

quicklisp\_start()

mext package: quicklisp

**Description** Load (setup) quicklisp. It must already be installed.

Arguments quicklisp\_start requires zero arguments.

# 16 Functions and Variables for Runtime Environment

- chdir
- dir\_exists
- dirstack
- dont\_kill
- dont\_kill\_share
- get\_dont\_kill
- homedir
- list\_directory
- mext\_clear

- mext\_info
- mext\_list
- mext\_list\_loaded
- mext\_test
- popdir
- probe\_file
- pwd
- require
- truename
- updir

#### 16.1 Function: chdir

chdir( :optional dir)

mext package: mext\_defmfun1

### Calling

**chdir**() Set the working directory to the value it had when mext was loaded.

**chdir**(dir) Set the working directory to dir.

**Description** Set the working directory for maxima/lisp. With some lisps, such as cmu lisp the system directory is changed as well. This should be made uniform across lisp implementations.

**Arguments** chdir requires either zero or one arguments. If present, the argument dir must be a a string.

## 16.2 Function: dir\_exists

 $dir_exists(dir)$ 

mext package: mext\_defmfun1

**Description** Returns the pathname as a string if dir exists, and false otherwise.

**Arguments** dir\_exists requires one argument *dir*, which must be a string.

### 16.3 Function: dirstack

dirstack()

mext package: mext\_defmfun1

**Description** Return a list of the directories on the directory stack. This list is manipulated with chdir, updir, and popdir.

**Arguments** dirstack requires zero arguments.

#### 16.4 Function: dont\_kill

dont\_kill( :rest item)

mext package: mext\_defmfun1

**Description** Add the *items* to the list of symbols that are not killed by kill(all). This facility is part of the maxima core, but is apparantly unused. Maybe putting a property in the symbol's property list would be better.

**Arguments** dont\_kill requires zero or more arguments.

Attributes dont\_kill has attributes: [hold\_all]

#### 16.5 Function: dont\_kill\_share

dont\_kill\_share(package)

mext package: mext\_defmfun1

**Description** Prevent symbols in maxima share package package from being killed by kill.

Arguments dont\_kill\_share requires one argument package, which must be a string or a symbol.

# 16.6 Function: get\_dont\_kill

get\_dont\_kill()

mext package: mext\_defmfun1

**Description** Returns the list of symbols that are not killed by kill(all). Items are added to this list with dont\_kill.

Arguments get\_dont\_kill requires zero arguments.

#### 16.7 Variable: homedir

default value /home/jlapeyre/.

**Description** The user's home directory.

# 16.8 Function: list\_directory

list\_directory( :optional dir)
mext package: mext\_defmfun1

**Description** Returns a directory listing for *dir* or the current directory if no argument is given.

**Arguments** list\_directory requires either zero or one arguments. If present, the argument *dir* must be a a string.

# 16.9 Function: mext\_clear

mext\_clear()

mext package: mext\_defmfun1

**Description** Clears the list of mext packages that have been loaded with require. Subsequent calls to require will reload the packages.

Arguments mext\_clear requires zero arguments.

See also mext\_list\_loaded, mext\_list, and mext\_info.

#### 16.10 Function: mext\_info

 $mext\_info(distname)$ 

mext package: mext\_defmfun1

**Description** Print information about installed mext distribution distname. The list of installed distributions is built by calling mext\_list.

**Arguments** mext\_info requires one argument *distname*, which must be a string or a symbol.

See also mext\_list\_loaded, mext\_list, and mext\_clear.

#### 16.11 Function: mext\_list

mext\_list()

mext package: mext\_defmfun1

**Description** Returns a list of all installed mext distributions. These are installed, but not necessarily loaded.

Arguments mext\_list requires zero arguments.

See also mext\_list\_loaded, mext\_info, and mext\_clear.

#### 16.12 Function: mext\_list\_loaded

mext\_list\_loaded()

mext package: mext\_defmfun1

**Description** Returns a list of mext packages currently loaded.

Arguments mext\_list\_loaded requires zero arguments.

See also mext\_list, mext\_info, and mext\_clear.

#### 16.13 Function: mext\_test

mext\_test( :optional dists)
mext package: mext\_defmfun1

**Description** Run the test suites for a mext distribution or list of distributions. If the argument all is given, then all tests are run for all installed mext distributions. If no argument is given, a subfolder named rtests is searched for in the current directory.

**Arguments** mext\_test requires either zero or one arguments. If present, the argument *dists* must be a a string, a symbol, or a list of strings or symbols.

# 16.14 Function: popdir

 $\mathbf{popdir}(: optional \ n)$ 

mext package: mext\_defmfun1

**Description** Pop a value from the current directory stack and chdir to this value. If n is given, pop n values and chdir to the last value popped.

**Arguments** popdir requires either zero or one arguments. If present, the argument n must be a a non-negative integer.

# 16.15 Function: probe\_file

# Calling

**probe\_file**(filespec) returns a string representing a canonical pathname to the file specified by filespec. False is returned if the file can't be found.

**Description** Probe\_File tries to find a canonical pathname for a file specified by the string *filespec*.

#### Examples

```
(%i1) probe_file("a/b.txt");
(%o1) "/home/username/c/a/b.txt"
```

# 16.16 Function: pwd

pwd()

mext package: mext\_defmfun1

**Description** Return the current working directory.

**Arguments** pwd requires zero arguments.

# 16.17 Function: require

require(distname :optional force)
mext package: mext\_defmfun1

**Description** Load the mext pacakge *distname* and register that it has been loaded. require('all) will load all installed mext packages. If *force* is true, then *distname* is loaded even if it has been loaded previously.

**Arguments** require requires either one or two arguments. The first argument *distname* must be a string or a symbol.

#### 16.18 Function: truename

#### Calling

**truename**(filespec) returns a string representing a canonical pathname to the file specified by filespec

**Description** Truename tries to find a canonical pathanme for a file specified by the string *filespec*.

#### 16.19 Function: updir

updir( :optional n)

mext package: mext\_defmfun1

**Description** Change the working directory to be n (or 1 if n is not given) subdirectories higher than the current working directory.

**Arguments** updir requires either zero or one arguments. If present, the argument n must be a a non-negative integer.

# 17 Functions and Variables for Strings

- string\_drop
- string\_reverse
- string\_take
- with\_output\_to\_string

# 17.1 Function: string\_drop

```
string\_drop(s, spec)
mext package: lists_aex
```

**Arguments** string\_drop requires two arguments. The first argument s must be a string. The second argument spec must be a sequence specification.

# Examples

```
(%i1) string_drop("abracadabra",1);
(%o1) bracadabra
```

```
(%i1) string_drop("abracadabra",-1);
(%o1) abracadabr
```

```
(%i1) string_drop("abracadabra",[2,10]);
(%o1) aa
```

# 17.2 Function: string\_reverse

```
string_reverse(s)
mext package: lists_aex
```

#### Calling

 $string\_reverse(s)$  returns a copy of string s with the characters in reverse order.

**Arguments** string\_reverse requires one argument s, which must be a string.

# 17.3 Function: string\_take

```
string\_take(s, spec)
mext package: lists_aex
```

#### Calling

 $string\_take(s, n)$  returns a string of the first n characters of the string s.

 $string\_take(s, -n)$  returns a string of the last n characters of s.

**Arguments** string\_take requires two arguments. The first argument s must be a string. The second argument spec must be a sequence specification.

#### **Examples**

```
(%i1) string_take("dog-goat-pig-zebra",[5,12]);
(%o1) goat-pig
```

# 17.4 Function: with\_output\_to\_string

**Description** Evaluates  $expr_1, expr_2, expr_3, \dots$ 

### Examples

```
(%i1) sreverse(with_output_to_string(for i:5 thru 10 do print("i! for i=",i,i!)));
(%o1)
0088263 01 =i rof !i
088263 9 =i rof !i
02304 8 =i rof !i
0405 7 =i rof !i
027 6 =i rof !i
021 5 =i rof !i
```

See also with\_stdout.

### 18 Miscellaneous Functions

- examples
- examples\_add

# 18.1 Function: examples

```
examples(item)
mext package: defmfun1
```

#### Calling

**examples**(*item*) Print examples for the topic *item*. Note these examples are different from those extracted from the maxima manual with the command **example**.

**Arguments** examples requires one argument *item*, which must be a string or a symbol.

# 18.2 Function: examples\_add

```
examples_add(item, text, protected-var-list, code) mext package: defmfun1
```

#### Calling

**examples\_add**(*item*, *text*, *protected-var-list*, *code*) Add an example for item *item*. *text* will be printed before the example is displayed. *protected-var-list* is string giving a list of variables such as "[x,y]" that appear in the example code. The example code will be wrapped in a block that makes *protected-var-list* local. *code* may be a string or list of strings that is/are the example code.

**Arguments** examples\_add requires four arguments. The first argument *item* must be a string or a symbol. The second argument *text* must be a string. The third argument *protected-var-list* must be a string. The fourth argument *code* must be a string or a list of strings.

#### Examples

Add an example for the function 'last'.

```
(%i1) examples_add("last", "Return the last item in a list.", "[a,b,c,d]", "last([a,b,c,d])");
(%o1) done
```

# 19 Miscellaneous utilities

• compile\_lambda\_verbose

## 19.1 Variable: compile\_lambda\_verbose

default value false.

**Description** If this is true, then print translated code when automatically compiling lambda functions passed as arguments. This is done in the macro option-compile-lambda.

# 20 Options

Options to a function in the aex-maxima distribution are passed as follows:

funcname(x,y, [optname - $\dot{i}$  optval, optname2 - $\dot{i}$  optval2]) or funcname(x,y, optname - $\dot{i}$  optval, optname2 - $\dot{i}$  optval2)

The standard options described in this section are some options that are supported by many functions in the aex-maxima distribution.

- adj
- compile
- foptions
- ot

# 20.1 Option: adj

**Description** This option takes values of true or false. If true, then the output aex expression is adjustable, that is, the underlying array can be extended in size. If false, then the output aex expression is not adjustable. The non-adjustable array may have some advantanges in efficiency, but I have not observed them, and this may be lisp-implementation dependent.

#### 20.2 Option: compile

**Description** If this option is true, then lambda functions passed as arguments to a function will be automatically translated or compiled. If it is false they will used as interpreted maxima code. Compiling lambda functions usually greatly deceases the execution time of the function if the lambda function is called many times.

### 20.3 Function: foptions

foptions(name)

**Description** Return a list of allowed options to defmfun1 function *name*. I would prefer to call this options, but that name is taken by an unused, undocumented function.

**Arguments** foptions requires one argument *name*, which must be a string or a symbol.

# 20.4 Option: ot

**Description** With a value ar this option causes the function to return an array-representation expression. With a value ml a standard lisp list representation is returned. The array-representation is not a maxima array, but rather a more-or-less arbitrary maxima expression that is stored internally as an array. For certain operations, such as random access to elements of the expression, an array representation is faster than the standard list representation. One disadvantange of the array representations is that creating an array is relatively slow. For instance, execution time may be large if a function returns an expression with many small subexpressions that are in the array-representation. The majority of the maxima system does not understand array-representation, so conversion back to list-representation at may be necessary.