

Our goal in this notebook is to calculate the hyperfine splitting for $^{87}\text{Sr}^+$. This will be given by

$$E_{\text{hfs}} = \frac{1}{2}AC + BC(C + 1),$$

where C is given by

$$C = F(F + 1) - J(J + 1) - I(I + 1).$$

First, we will store the values of A and B given by Safronova's paper. Both of these values are in MHz

```
In [1]: AP=-35.3  
        BP=88.68
```

```
In [2]: def hyperfine_split(F,J=3.00/2,I=9.00/2):  
        C=F*(F+1)-J*(J+1)-I*(I+1)  
        #print "C=",C,"I=",I,"F=",F,"A=",AP,"B=",BP  
        return (1.0/2)*AP*C+BP*C*(C+1)
```

```
In [3]: AP=-35.3  
        BP=88.68  
  
        print "F=3 gives", hyperfine_split(3),"MHz"  
        print "F=4 gives", hyperfine_split(4),"MHz"  
        print "F=5 gives", hyperfine_split(5),"MHz"  
        print "F=6 gives", hyperfine_split(6),"MHz"
```

```
F=3 gives 22971.135 MHz  
F=4 gives 5803.375 MHz  
F=5 gives 306.075 MHz  
F=6 gives 17120.835 MHz
```

Now, we look at the S state. $A = 1000$ MHz, $B = 0$ MHz while $J = \frac{1}{2}$ and I is still $\frac{9}{2}$.

```
In [4]: AP=1000  
        BP=0  
  
        print "F=4 gives", hyperfine_split(4,J=1.0/2)  
        print "F=5 gives", hyperfine_split(5,J=1.0/2)
```

```
F=4 gives -2750.0  
F=5 gives 2250.0
```

The difference between these is clearly 5 GHz.

```
In [5]: #A version table.  
#This notebook does not use anything else from the qutip package.  
from qutip.ipynbtools import version_table  
version_table()
```

```
/home/jlarchibald/anaconda/lib/python2.7/site-packages/IPython/parallel.py:13:  
ShimWarning: The `IPython.parallel` package has been deprecated. You should imp  
ort from ipyparallel instead.  
"You should import from ipyparallel instead.", ShimWarning)
```

Out[5]:

Software	Version
Cython	0.22.1
SciPy	0.15.1
QuTiP	3.1.0
Python	2.7.10 Anaconda 2.3.0 (64-bit) (default, Oct 19 2015, 18:04:42) [GCC 4.4.7 20120313 (Red Hat 4.4.7-1)]
IPython	4.0.0
OS	posix [linux2]
Numpy	1.9.2
matplotlib	1.4.3
Mon Nov 23 22:59:56 2015 CST	