

Ballasted Polar:

with the well known equation for lift:

$$mg = \frac{1}{2} \rho S V^2 C_a \quad (1)$$

and

$$o = m_b / m \quad (2)$$

o = ballast overload

m_b = ballasted mass

V = unballasted airspeed

S = wing area

ρ = air density constant

C_a = lift coefficient

m = unballasted mass as from reference polar

we can solve eq. (1) for V

$$V = \sqrt{m g / \frac{1}{2} \rho S C_a}$$

as we can consider everything except mass m as constant in the above expression we can conclude:

$$V_b / V = \sqrt{m_b / m} = \sqrt{o} \quad (2)$$

or

$$V = V_b / \sqrt{o} \quad (3)$$

with the second order approximation for sink:

$$\text{Sink}(V) = a_0 + a_1 V + a_2 V^2 \quad (4)$$

and (3) in (4), we get for the ballasted sink:

$$\text{Sink}_b(V_b / \sqrt{o}) = a_0 + a_1 (V_b / \sqrt{o}) + a_2 (V_b / \sqrt{o})^2$$

or

$$\text{Sink}_b(V_b) = \sqrt{o} (a_0 + (a_1 / \sqrt{o}) V_b + (a_2 / o) V_b^2)$$

or, further simplified:

$$\text{Sink}_b(V_b) = a_0 \sqrt{o} + a_1 V_b + (a_2 / \sqrt{o}) V_b^2$$

So finally we get the polar translated for the ballasted case and that's what we do today in XCS and also XCV when user increases ballast.