

$$\begin{aligned} \frac{dH}{dt} = & -2 \int_S (\mathbf{A}_p \cdot \mathbf{V}_h) B_z dS \\ & + 2 \int_S (\mathbf{A}_p \cdot \mathbf{B}_h) v_z dS \end{aligned}$$