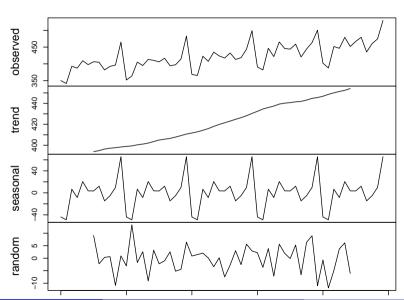
## Today's Agenda

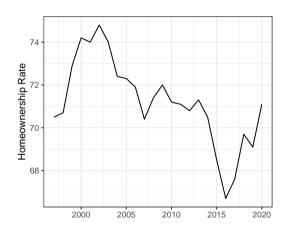
Comparing random variation models to linear trend models of time series data

Justin Leinaweaver (Spring 2022)

#### Decomposition of additive time series



# **Assignment for Today**

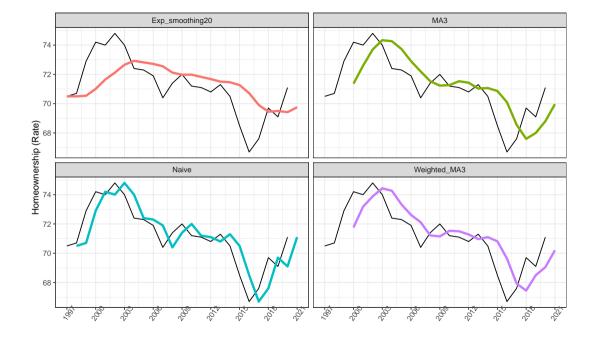


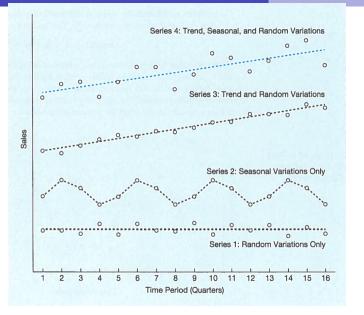
What is the best forecast model of homeownership rates in MO?

- Naïve
- MA (3)
- Weighted MA (3), or
- Exponential Smoothing (0.2)

Predict 2021 and calculate the MSE!

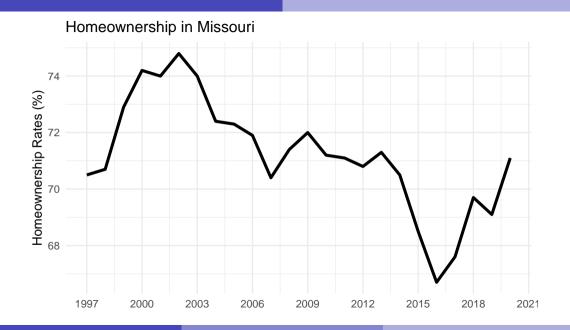
Forecast	MSE	Prediction
Naive	1.32	71.1
MA-3	2.46	70
WMA-3	1.96	70.2
Exp Smooth (.2)	3.15	69.8



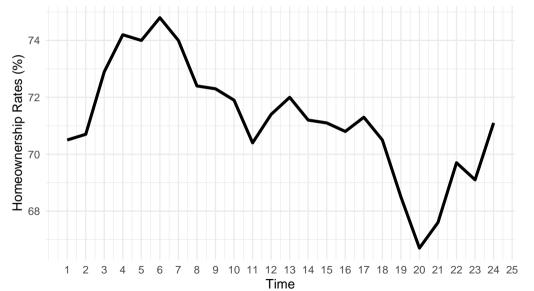


The Components of Time Series Data

(Render, Stair, Jr., Hanna and Hale 2018)



#### OLS on Time Series Data: Regress on Time Period



# **Using OLS on Time Series Data**

Regress homeownership rate on the time period

- Visualize the model as a line plot
- Calculate the MSE

### **Create Time Period Variable**

	Α	В	С	D
1	state	year	homeowner_rate	time
2	Missouri	1997	70.5	1
3	Missouri	1998	70.7	2
4	Missouri	1999	72.9	3
5	Missouri	2000	74.2	4
6	Missouri	2001	74	5
7	Missouri	2002	74.8	6
8	Missouri	2003	74	7
9	Missouri	2004	72.4	8
10	Missouri	2005	72.3	9
11	Missouri	2006	71.9	10
12	Missouri	2007	70.4	11
13	Missouri	2008	71.4	12

RESIDUAL OUTPUT			
Observation	Predicted homeowner_rate	Residuals	Error2
1	70.95	-0.45	0.20
2	71.83	-1.13	1.27
3	72.49	0.41	0.17
4	72.97	1.23	1.52
5	73.27	0.73	0.53
6	73.42	1.38	1.91
7	73.42	0.58	0.33
8	73.31	-0.91	0.83
9	73.09	-0.79	0.63
10	72.79	-0.89	0.79
11	72.41	-2.01	4.04
12	71.98	-0.58	0.34

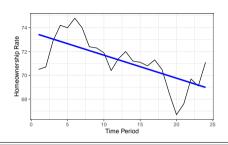
MSE = Average of the Squared Residuals

# **Using OLS on Time Series Data**

Regress homeownership rate on the time period

- Visualize the model as a line plot
- Calculate the MSE

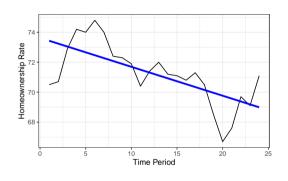
	homeowner_rate
time	-0.19*
	(0.04)
Constant	73.63*
	(0.64)
Observations	24
Adjusted R <sup>2</sup>	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)
Note:	*p < 0.05



Forecast	MSE	Prediction
Exp Smooth (.2)	3.15	69.8
MA-3	2.46	70
OLS	2.11	68.99
WMA-3	1.96	70.2
Naive	1.32	71.1

#### **Make Predictions**

	homeowner_rate
time	-0.19*
	(0.04)
Constant	73.63*
	(0.64)
Observations	24
Adjusted R <sup>2</sup>	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)
Note:	*p < 0.05

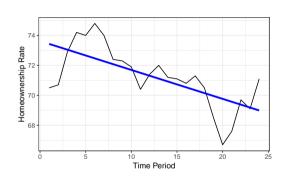


Prediction =  $73.63 + -0.19 \times Time$ 

Use the model to predict homeownership for the next two years.

#### **Make Predictions**

	homeowner_rate
time	-0.19*
	(0.04)
Constant	73.63*
	(0.64)
Observations	24
Adjusted R <sup>2</sup>	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)
Note:	*p < 0.05



Prediction = 
$$73.63 + -0.19 \times (Time = 25) = 68.88$$

Prediction = 
$$73.63 + -0.19 \times (Time = 26) = 68.69$$

## **Using OLS on Time Series Data**

Compare our results to two model transformations:

- Regress homeownership rate on a quadratic function of time period
- Regress homeownership rate on a cubic function of time period

	Α	В	С	D	Е	F
1	state	year	homeowner_rate	time	time2	time3
2	Missouri	1997	70.5	1	1	1
3	Missouri	1998	70.7	2	4	8
4	Missouri	1999	72.9	3	9	27
5	Missouri	2000	74.2	4	16	64
6	Missouri	2001	74	5	25	125
7	Missouri	2002	74.8	6	36	216
8	Missouri	2003	74	7	49	343
9	Missouri	2004	72.4	8	64	512
10	Missouri	2005	72.3	9	81	729
11	Missouri	2006	71.9	10	100	1000
12	Missouri	2007	70.4	11	121	1331
13	Missouri	2008	71.4	12	144	1728
14	Missouri	2009	72	13	169	2197

*time2* E2 = D2^2

time3 F2 = D2^3

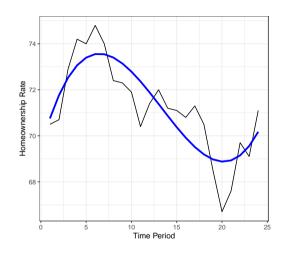
		Homeownership	
	(1)	(2)	(3)
Time	-0.19*	0.03	1.42*
	(0.04)	(0.18)	(0.37)
Squared		-0.01	-0.15*
		(0.01)	(0.03)
Cubed			0.004*
			(0.001)
Constant	73.63*	72.66*	69.48*
	(0.64)	(1.00)	(1.10)
Observations	24	24	24
Adjusted R <sup>2</sup>	0.43	0.45	0.68
Residual Std. Error	1.52 (df = 22)	1.50 (df = 21)	1.14 (df = 20)
F Statistic	18.61* (df = 1; 22)	$10.30^* \text{ (df} = 2; 21)$	17.18* (df = 3; 20
Note:			*n < 0.01

Note:

\*p < 0.05

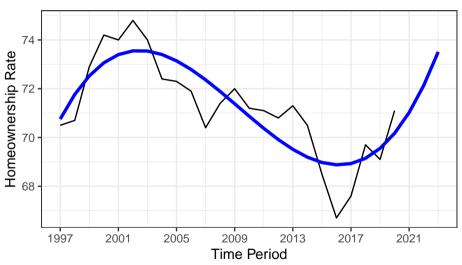
Forecast	MSE	Prediction
Exp Smooth (.2)	3.15	69.8
MA-3	2.46	70
OLS	2.11	68.99
<b>OLS</b> Quadratic	1.97	68.24
WMA-3	1.96	70.2
Naive	1.32	71.1
OLS Cubic	1.09	70.17

RESIDUAL OUTPUT	
Observation	Predicted homeowner_rate
1	70.95
2	71.83
3	72.49
4	72.97
5	73.27
6	73.42
7	73.42
8	73.31
9	73.09
10	72.79
11	72.41

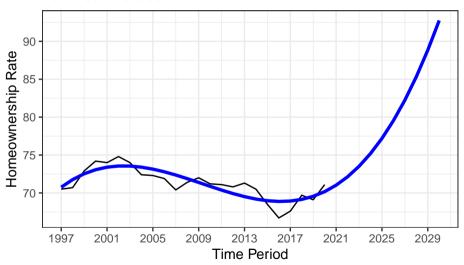


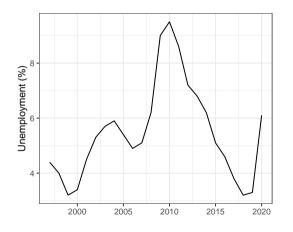
The model line is the "Predicted" column in the residual output.

#### Three Year Forecast



#### Ten Year Forecast





What is the best forecast model of unemployment rates in MO?

- Naïve
- Weighted MA (3)
- Linear model of time
- Quadratic function of time

Forecast	MSE
OLS	2.95
Weighted MA3	1.98
OLS (Quadratic)	1.67
Naive	1.14

