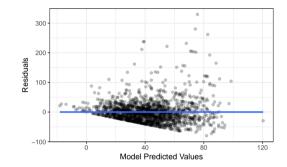
## Today's Agenda

Practice fitting, evaluating and making point estimates using multiple linear regression models (ch 6)

Justin Leinaweaver (Spring 2022)

	Earnings (2021 USD)	
Age	0.47*	
	(0.05)	
	` ,	
Education	5.42*	
	(0.35)	
Exercise	0.95*	
	(0.41)	
Height	2.84*	
	(0.24)	
	2.4.27	
Mother's Education	-241.27*	
	(16.34)	
Observations	1,813	
Adjusted R <sup>2</sup>	0.21	
Residual Std. Error	37.43 (df = 1808)	
F Statistic	118.04* (df = 4; 1808)	
Note:	*p < 0.05	
	•	



	age	education	exercise	height
age education exercise height	1 -0.15 -0.33 -0.14	-0.15 1 0.18 0.11	-0.33 0.18 1 0.22	-0.14 0.11 0.22

## For Today - Make Predictions (w/ 95% Pls)

Establish a baseline prediction for a hypothetical person who is 25 (Age), Education 13, Exercise 1, Height 67

Then calculate the predicted income if:

- Finish college? (16)
- Finish grad school? (18)
- Increase exercise to 1x / week? (4)
- Increase exercise to 3x / week? (7)

	Earnings (2021 USD)		
Age	0.47*		
7.65	(0.05)		
	(5.55)		
Education	5.42*		
	(0.35)		
	` '		
Exercise	0.95*		
	(0.41)		
Height	2.84*		
	(0.24)		
Mother's Education	-241.27*		
	(16.34)		
Observations	1,813		
Adjusted R <sup>2</sup>	0.21		
Residual Std. Error	37.43 (df = 1808)		
F Statistic	118.04* (df = 4; 1808)		
Note:	*p < 0.05		
	P < 0.05		

Prediction	Low	Estimate	High
Baseline	-44.9	29.9	104.7
Finish College	-28.7	46.1	120.9
Finish Grad School	-17.9	56.9	131.7

Prediction	Low	Estimate	High
Baseline	-44.9	29.9	104.7
Exercise $1x / week$	-42.2	32.6	107.4
Exercise >3x	-39.5	35.3	110.1

	Earnings (2021 USD)	
Age	0.47*	
	(0.05)	
Education	5.42*	
	(0.35)	
Exercise	0.95*	
	(0.41)	
Height	2.84*	
	(0.24)	
Mother's Education	$-241.27^{*}$	
	(16.34)	
Observations	1,813	
Adjusted R <sup>2</sup>	0.21	
Residual Std. Error	37.43  (df = 1808)	
F Statistic	118.04* (df = 4; 1808)	
Note:	*p < 0.05	

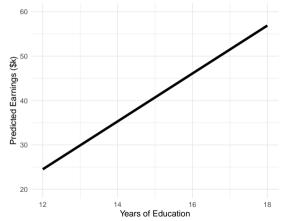
Education	Prediction
12	
13	
14	
15	
16	\$46.1k
17	
18	\$56.9k

	Earnings (2021 USD)	
Age	0.47*	
	(0.05)	
Education	5.42*	
Education	(0.35)	
	(0.33)	
Exercise	0.95*	
	(0.41)	
	, ,	
Height	2.84*	
	(0.24)	
	041.07*	
Mother's Education	-241.27*	
	(16.34)	
Observations	1 012	
Adjusted R <sup>2</sup>	1,813 0.21	
Residual Std. Error	*	
F Statistic	$118.04^* \text{ (df} = 4; 1808)$	
	110.04 (41 = 4, 1000)	
Note:	*p < 0.05	

Education	Prediction
12	\$24.5k
13	\$29.9k
14	\$35.3k
15	\$40.7k
16	\$46.1k
17	\$51.5k
18	\$56.9k

Education	Prediction	
12	\$24.5k	
13	\$29.9k	
14	\$35.3k	
15	\$40.7k	
16	\$46.1k	
17	\$51.5k	
18	\$56.9k	

## The Marginal Effect of Education on Earnings Assumes a 25 year old who is 5ft 7in and doesn't exercise

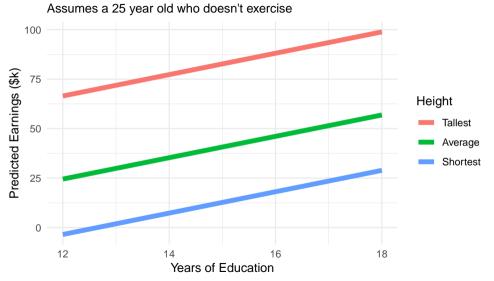


## Average Height (5'7")

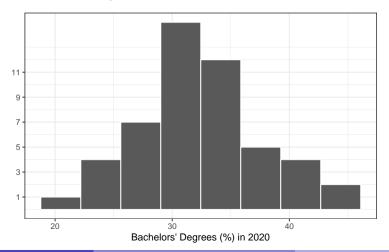
### Tallest Height (6'10")

Education	Prediction	Education	Prediction
12	\$24.5	12	\$66.5
13	\$29.9	13	\$71.9
14	\$35.3	14	\$77.3
15	\$40.7	15	\$82.7
16	\$46.1	16	\$88.1
17	\$51.5	17	\$93.5
18	\$56.9	18	\$98.9

The Marginal Effect of Education on Earnings



## What is the "best" model of bachelor's degree completion in dataset 1?



## What is the "best" model of bachelor's degree completion in dataset 1?

- Choose the logical predictors
- Fit a simple OLS regression to each predictor
- Fit a multiple regression with the "best" of those
- Evaluate the model using all five steps
- Use the model to make predictions

# What is the "best" model of bachelor's degree completion in dataset 1?

#### **Outcome**

Bachelors' Degrees

#### **Predictors to Consider**

• GDP (Billions), GDP (Rate), Homeownership, Manufacturing employment, Minimum wage, Population, Rental Vacancy Rate, State Tax Rate on Wages, Unemployment

### Common Regression Mistakes (Wheelan ch12)

- Linear regression on nonlinear relationships
- Correlation does not equal causation
- Reverse causality
- Omitted variable bias (too few variables)
- Highly correlated explanatory variables (multicollinearity)
- Extrapolating beyond the data
- Data mining (too many variables)