#### Today's Agenda

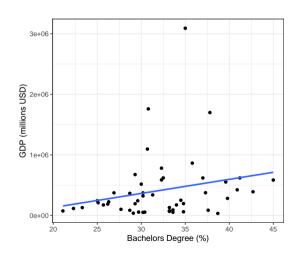
Extending the OLS Regression using Dataset 1

- Dummy predictors
- Categorical predictors
- Transforming the variables
- Transforming the model

Justin Leinaweaver (Spring 2022)

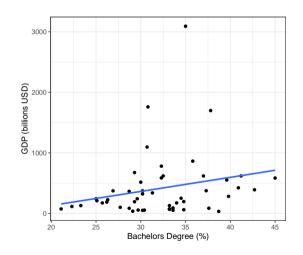
#### **Transforming the Variables**

	GDP (millions)
Bachelors (%)	23,271.42
	(14,124.28)
Intercept	-335,020.10
	(460,391.60)
Observations	50
Adjusted R <sup>2</sup>	0.03
Residual Std. Error	528,114.80 (df = 48)
F Statistic	2.71 (df = 1; 48)
Note:	*p<0.05



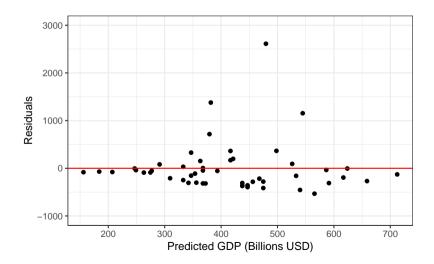
### **Transforming the Variables**

	GDP (billions)
Bachelors (%)	23.27
	(14.12)
Intercept	-335.02
	(460.39)
Observations	50
Adjusted R <sup>2</sup>	0.03
Residual Std. Error	528.11 (df = 48)
F Statistic	2.71 (df = 1; 48)
Note:	*p<0.05

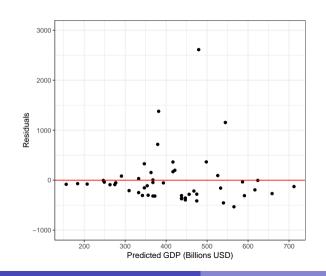


	GDP (millions) (1)	(billions) (2)	(10 billion) (3)	(100 billion) (4)
Bachelors (%)	23,271.42	23.27	2.33	0.23
	(14,124.28)	(14.12)	(1.41)	(0.14)
Intercept	-335,020.10	-335.02	-33.50	-3.35
	(460,391.60)	(460.39)	(46.04)	(4.60)
Observations Adjusted R <sup>2</sup>	50	50	50	50
	0.03	0.03	0.03	0.03
Residual Std. Error (df = 48)	528,114.80	528.11	52.81	5.28
F Statistic (df = 1; 48)	2.71	2.71	2.71	2.71
Note:				*p<0.05

#### **Transformation 1: Shift the Decimal Point**



#### **Transformation 1: Shift the Decimal Point**

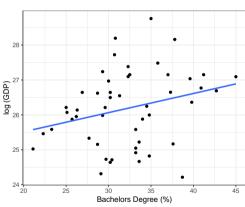


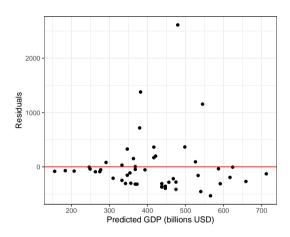
36 / 50 (72 %) are below the zero line.

Aim is 50%-50%

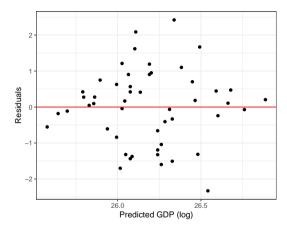
- Create a new variable: "log GDP"
  - Excel function for the natural log is = LN()
  - GDP in Dataset 1 is in millions so you have to convert it to dollars first!
  - = LN( GDP \* 1e6 )
- Practice: Regress log GDP on bachelors

	(billions) (1)	(log) (2)	
Bachelors (%)	23.27 (14.12)	0.05 (0.03)	-
Intercept	-335.02 (460.39)	24.42* (0.91)	log (GDP)
Observations	50	50	-
Adjusted R <sup>2</sup>	0.03	0.06	
Residual Std. Error ( $df = 48$ )	528.11	1.04	
F Statistic (df = 1; 48)	2.71	3.86	_
Note:		*p<0.05	-

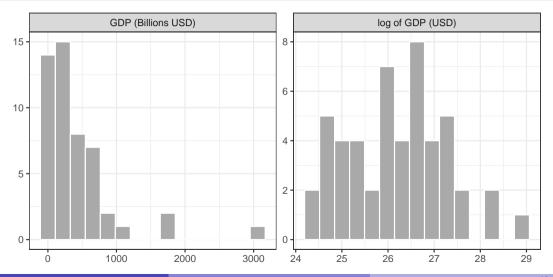


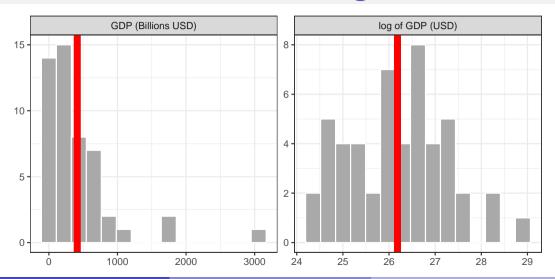


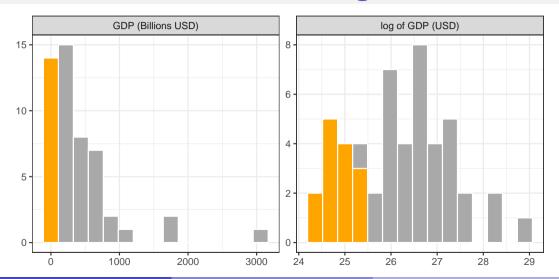
Above the line = 14 (28%)Below the line = 36 (72%)

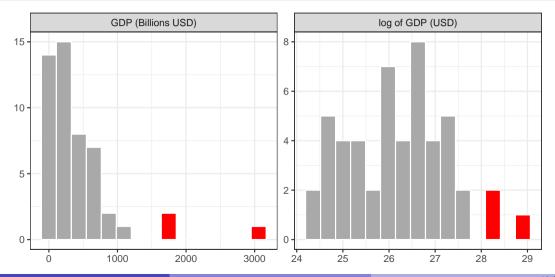


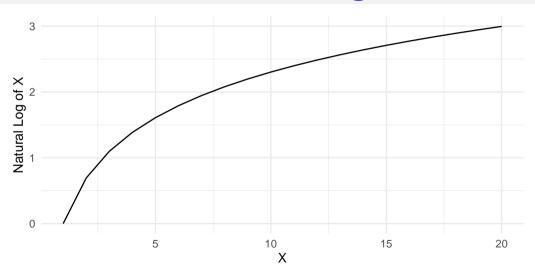
Above the line = 27 (54%)Below the line = 23 (46%)

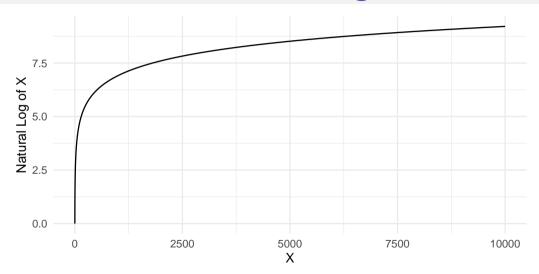












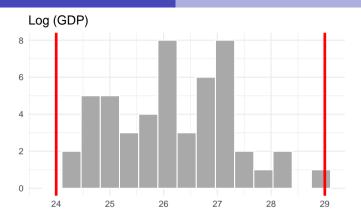
The natural log scale = multiplying by e

- *e* is Euler's Number (2.718282...)
- Typically written as  $log_e X$  or In X

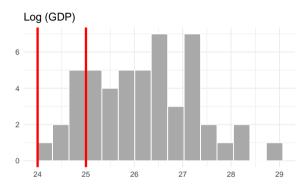
Transform back to linear scale using eX

GDP for State 
$$X = $5,000$$
 or 8.5 (In)

- $log_e$  5,000  $\approx$  8.5
- $e^{8.5} \approx 5,000$
- Excel function is = EXP()



- $e^{24}$  is approximately \$26 billion
- $e^{29}$  is approximately \$3.9 trillion



- $e^{24} \approx $26$  billion
- $e^{25} \approx $72$  billion

One unit on the LN scale:

• value x e

General rule of thumb:

value x 3

	(log GDP)
Bachelors (%)	0.05*
	(0.03)
Constant	24.42*
	(0.91)
Observations	50
Adjusted R <sup>2</sup>	0.06
Residual Std. Error	1.04 (df = 48)
F Statistic	3.86* (df = 1; 48)
Note:	*p<0.06

In (Outcome) = Intercept + Coefficient \* (Predictor)

	(log GDP)
Bachelors (%)	0.05*
	(0.03)
Constant	24.42*
	(0.91)
Observations	50
Adjusted R <sup>2</sup>	0.06
Residual Std. Error	1.04 (df = 48)
F Statistic	3.86* (df = 1; 48)
Note:	*p<0.06

In (GDP) = 
$$24.42 + 0.05 * (Bachelors)$$

	(log GDP)
Bachelors (%)	0.05*
	(0.03)
Constant	24.42*
	(0.91)
Observations	50
Adjusted R <sup>2</sup>	0.06
Residual Std. Error	1.04 (df = 48)
F Statistic	$3.86^* \text{ (df} = 1; 48)$
Note:	*p<0.06

In (GDP) = 
$$24.42 + 0.05 * 32.16 = 26.03$$

	(log GDP)
Bachelors (%)	0.05*
	(0.03)
Constant	24.42*
	(0.91)
Observations	50
Adjusted R <sup>2</sup>	0.06
Residual Std. Error	1.04 (df = 48)
F Statistic	$3.86^* (df = 1; 48)$
Note:	*p<0.06

$$GDP = 26.03 (In) = e^{26.03} = 201.7 Billion USD$$

$$In(Outcome) = Intercept + Coefficient * (Predictor)$$

$$Outcome = e^{Intercept + Coefficient*(Predictor)}$$

#### **Practice**

# Dataset 2: Do wealthier countries live longer?

- Regress life expectancy on GDP
- Regress life expectancy on log(GDP)

	Life Expectancy	
	(1)	(2)
GDP	0.00*	
	(0.00)	
log(GDP)		1.65*
log(GDT)		(0.22)
Constant	72.19*	32.07*
	(0.57)	(5.50)
Observations	173	173
Adjusted R <sup>2</sup>	0.03	0.24
Residual Std. Error ( $df = 171$ )	7.29	6.47
F Statistic (df = 1; 171)	6.53*	54.61*
Note:		*p<0.05

