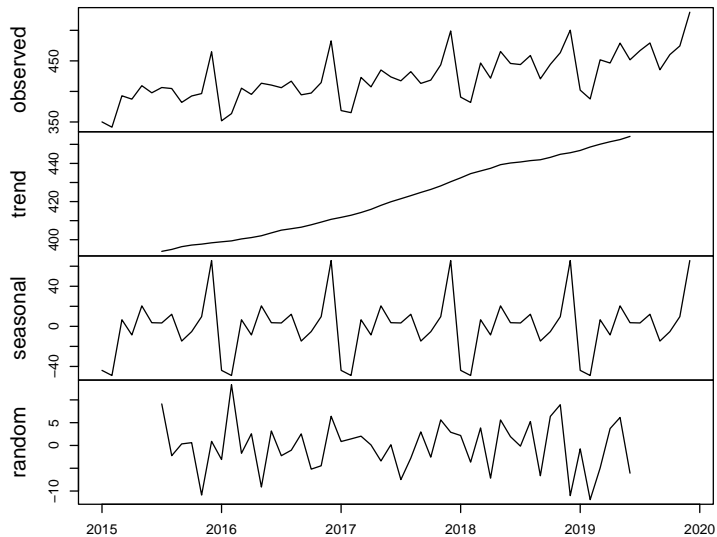


# Today's Agenda

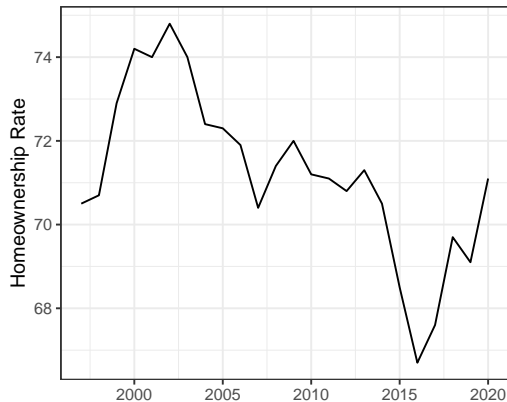
Comparing random variation models to linear trend models of time series data

Justin Leinaweaver (Spring 2022)

## Decomposition of additive time series



# Assignment for Today

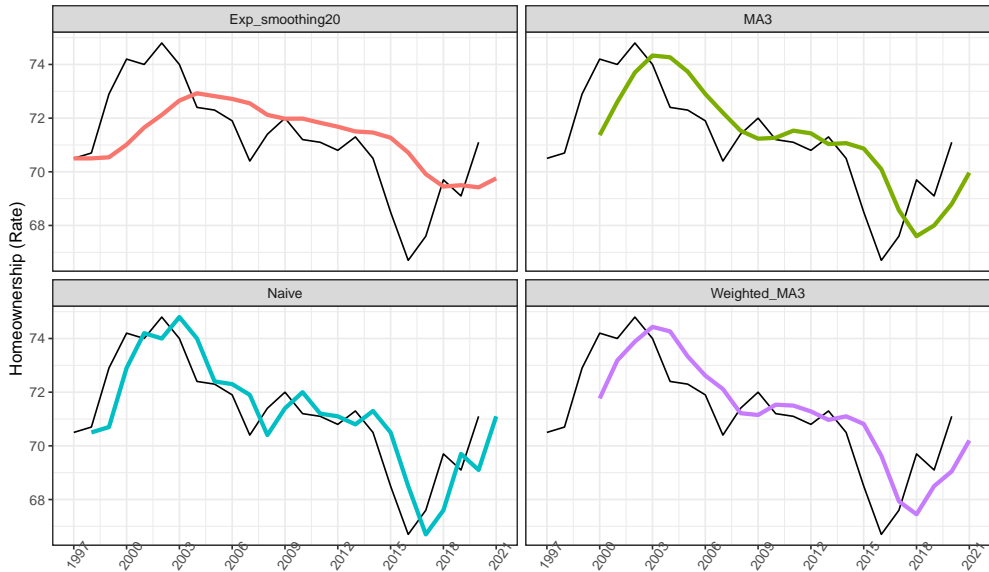


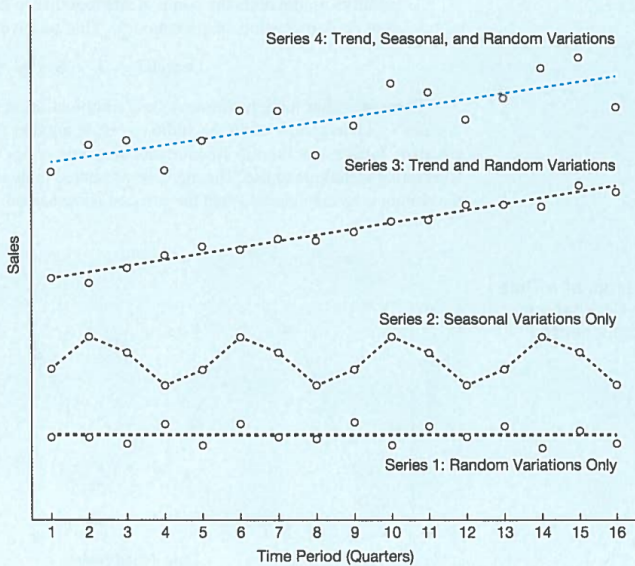
What is the best forecast model of homeownership rates in MO?

- Naïve
- MA (3)
- Weighted MA (3), or
- Exponential Smoothing (0.2)

Predict 2021 and calculate the MSE!

Forecast	MSE	Prediction
Naive	1.32	71.1
MA-3	2.46	70
WMA-3	1.96	70.2
Exp Smooth (.2)	3.15	69.8





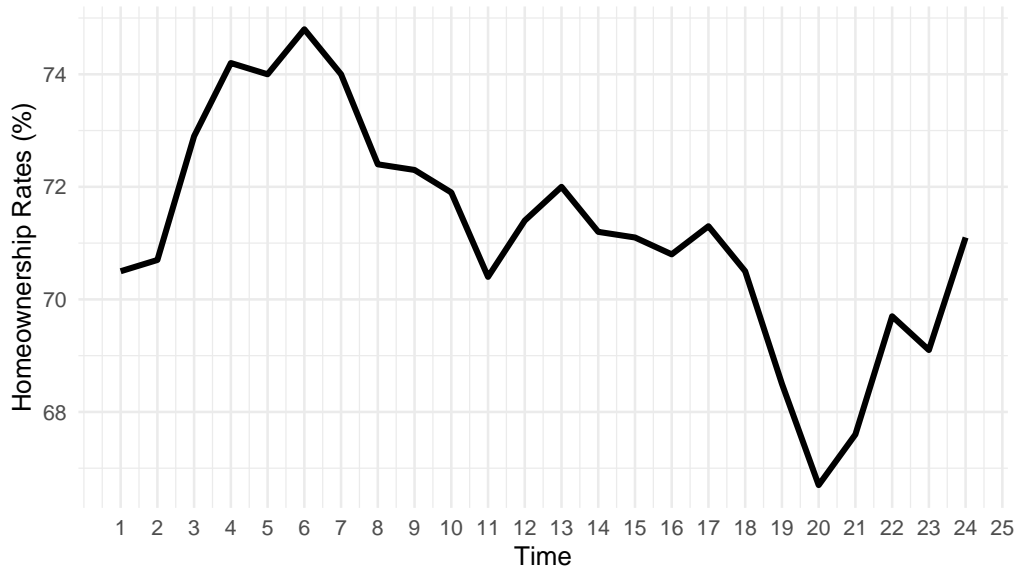
## The Components of Time Series Data

(Render, Stair, Jr.,  
Hanna and Hale 2018)

## Homeownership in Missouri



## OLS on Time Series Data: Regress on Time Period





# Create Time Period Variable

	A	B	C	D
1	state	year	homeowner_rate	time
2	Missouri	1997	70.5	1
3	Missouri	1998	70.7	2
4	Missouri	1999	72.9	3
5	Missouri	2000	74.2	4
6	Missouri	2001	74	5
7	Missouri	2002	74.8	6
8	Missouri	2003	74	7
9	Missouri	2004	72.4	8
10	Missouri	2005	72.3	9
11	Missouri	2006	71.9	10
12	Missouri	2007	70.4	11
13	Missouri	2008	71.4	12
14	Missouri	2009	72	13

# Practice Using OLS on Time Series Data

- 1 Regress homeownership rate on the time period
- 2 Visualize the forecast as a line plot
- 3 Calculate the MSE

RESIDUAL OUTPUT		
<i>Observation</i>	<i>Predicted homeowner_rate</i>	<i>Residuals</i>
1	70.95	-0.45
2	71.83	-1.13
3	72.49	0.41
4	72.97	1.23
5	73.27	0.73
6	73.42	1.38
7	73.42	0.58
8	73.31	-0.91
9	73.09	-0.79
10	72.79	-0.89
11	72.41	-2.01
12	71.98	-0.58

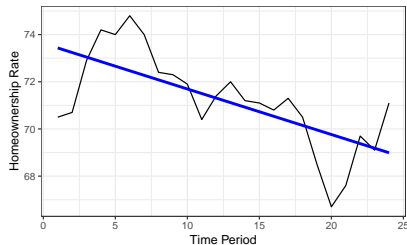
RESIDUAL OUTPUT			
<i>Observation</i>	<i>Predicted homeowner_rate</i>	<i>Residuals</i>	<i>Error2</i>
1	70.95	-0.45	0.20
2	71.83	-1.13	1.27
3	72.49	0.41	0.17
4	72.97	1.23	1.52
5	73.27	0.73	0.53
6	73.42	1.38	1.91
7	73.42	0.58	0.33
8	73.31	-0.91	0.83
9	73.09	-0.79	0.63
10	72.79	-0.89	0.79
11	72.41	-2.01	4.04
12	71.98	-0.58	0.34

**MSE = Average of the Squared Residuals**

# Practice Using OLS on Time Series Data

- 1 Regress homeownership rate on the time period
- 2 Visualize the forecast as a line plot
- 3 Calculate the MSE

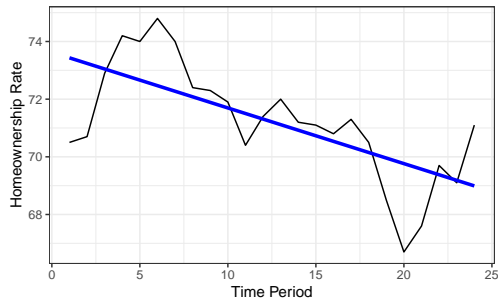
	homeowner_rate
time	-0.19* (0.04)
Constant	73.63* (0.64)
Observations	24
Adjusted R <sup>2</sup>	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)
Note:	*p < 0.05



Forecast	MSE	Prediction
Exp Smooth (.2)	3.15	69.8
MA-3	2.46	70
OLS	2.11	68.99
WMA-3	1.96	70.2
Naive	1.32	71.1

# Make Predictions

	homeowner_rate
time	-0.19* (0.04)
Constant	73.63* (0.64)
Observations	24
Adjusted R <sup>2</sup>	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)
Note: *p < 0.05	



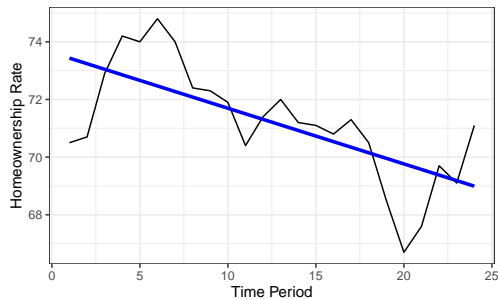
$$\text{Prediction} = 73.63 + -0.19 \times \text{Time}$$

Use the model to predict homeownership for the next two years.

# Make Predictions

	homeowner_rate
time	-0.19* (0.04)
Constant	73.63* (0.64)
Observations	24
Adjusted R <sup>2</sup>	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)

Note: \*p < 0.05



$$\text{Prediction} = 73.63 + -0.19 \times (\text{Time} = 25) = 68.88$$

$$\text{Prediction} = 73.63 + -0.19 \times (\text{Time} = 26) = 68.69$$



# Using OLS on Time Series Data

Compare our results to two model transformations:

- 1 Regress homeownership rate on a quadratic function of time period
- 2 Regress homeownership rate on a cubic function of time period

	A	B	C	D	E	F
1	state	year	homeowner_rate	time	time2	time3
2	Missouri	1997	70.5	1	1	1
3	Missouri	1998	70.7	2	4	8
4	Missouri	1999	72.9	3	9	27
5	Missouri	2000	74.2	4	16	64
6	Missouri	2001	74	5	25	125
7	Missouri	2002	74.8	6	36	216
8	Missouri	2003	74	7	49	343
9	Missouri	2004	72.4	8	64	512
10	Missouri	2005	72.3	9	81	729
11	Missouri	2006	71.9	10	100	1000
12	Missouri	2007	70.4	11	121	1331
13	Missouri	2008	71.4	12	144	1728
14	Missouri	2009	72	13	169	2197

*time2*

$$E2 = D2^2$$

*time3*

$$F2 = D2^3$$

	Homeownership		
	(1)	(2)	(3)
Time	-0.19* (0.04)	0.03 (0.18)	1.42* (0.37)
Squared		-0.01 (0.01)	-0.15* (0.03)
Cubed			0.004* (0.001)
Constant	73.63* (0.64)	72.66* (1.00)	69.48* (1.10)
Observations	24	24	24
Adjusted R <sup>2</sup>	0.43	0.45	0.68
Residual Std. Error	1.52 (df = 22)	1.50 (df = 21)	1.14 (df = 20)
F Statistic	18.61* (df = 1; 22)	10.30* (df = 2; 21)	17.18* (df = 3; 20)

Note:

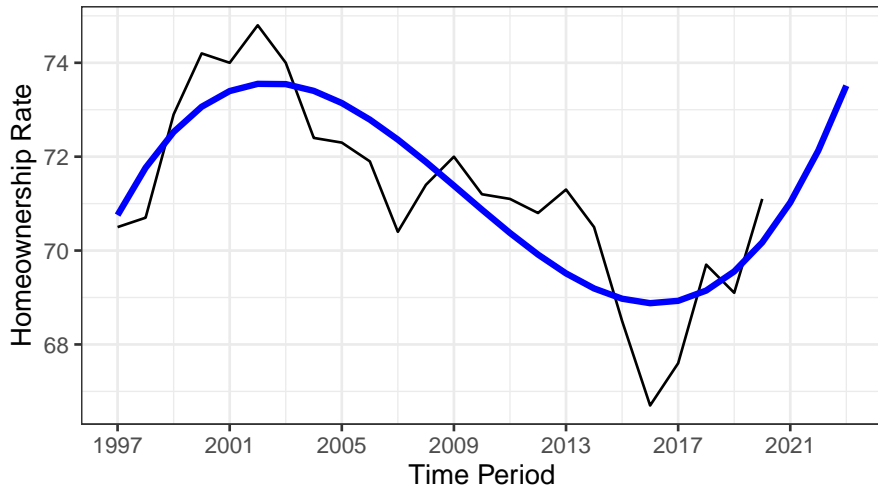
\*p < 0.05

Forecast	MSE	Prediction
Exp Smooth (.2)	3.15	69.8
MA-3	2.46	70
OLS	2.11	68.99
OLS Quadratic	1.97	68.24
WMA-3	1.96	70.2
Naive	1.32	71.1
OLS Cubic	1.09	70.17

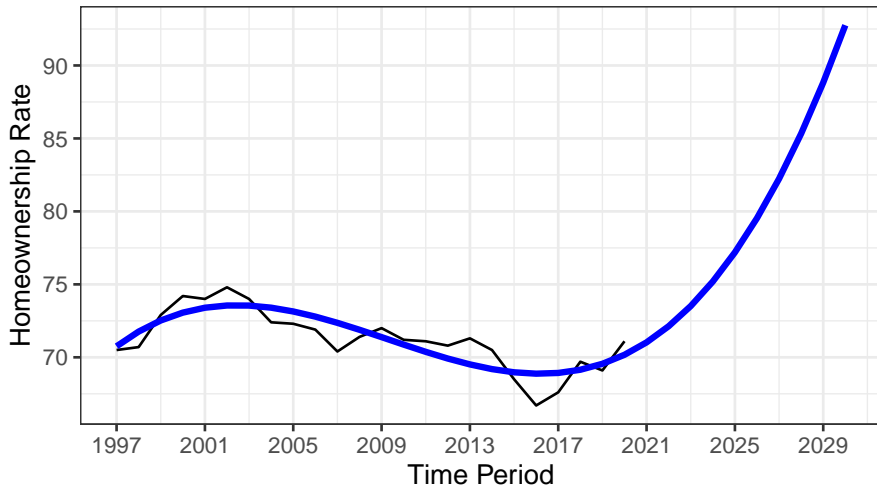
# Predict the Future!

- 1 Use the quadratic model fit to predict the next three years (2021, 2022, 2023), and
- 2 Visualize the actual data and your model fit.

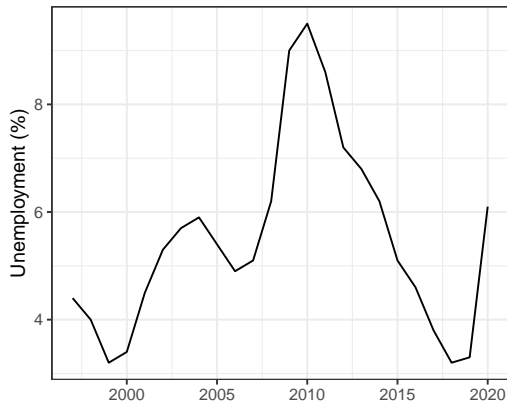
## Three Year Forecast



## Ten Year Forecast



# Forecast Unemployment Rates



What is the best forecast model of unemployment rates in MO?

- Naïve
- Weighted MA (3)
- Linear model of time
- Quadratic function of time



Forecast	MSE
OLS	2.95
Weighted MA3	1.98
OLS (Quadratic)	1.67
Naive	1.14

