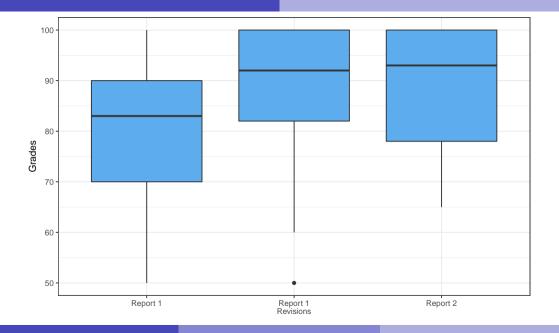
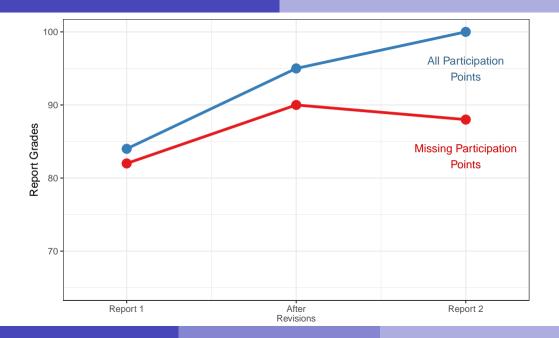
### **Today's Agenda**

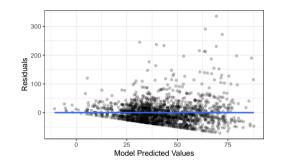
# Practicing Multiple Linear Regressions (Adding marginal effects plots)

Justin Leinaweaver (Spring 2022)





	Earnings (2021 USD)
Age	0.42*
	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
Constant	-56.86*
	(5.86)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05



	age	education	exercise
age	1.00	-0.15	-0.33
education	-0.15	1.00	0.18
exercise	-0.33	0.18	1.00

	Earnings (2021 USD)
Age	0.42*
3	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
Constant	-56.86*
	(5.86)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05

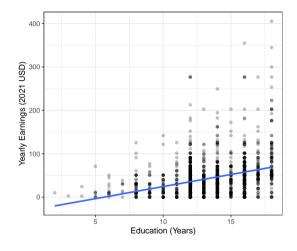
### Baseline: Age 20, Education 13, Exercise 1

	High
27	104.8
44.1	121.9
55.5	133.3
	44.1

Prediction	Low	Estimate	High
Baseline	-50.8	27	104.8
Exercise 1x / week	-45.4	32.4	110.2
Exercise >3x	-40	37.8	115.6

	Earnings (2021 USD)
Education	5.57*
	(0.36)
Constant	-31.34*
	(4.89)
Observations	1,813
Adjusted R <sup>2</sup>	0.11
Residual Std. Error	39.50 (df = 1811)
F Statistic	235.79* (df = 1; 1811)
Note:	*p < 0.05

	Earnings (2021 USD)
Education	5.57*
	(0.36)
Constant	-31.34*
	(4.89)
Observations	1,813
Adjusted R <sup>2</sup>	0.11
Residual Std. Error	$39.50 \; (df = 1811)$
F Statistic	235.79* (df = 1; 1811)
Note:	*p < 0.05



	Earnings (2021 USD)
Age	0.42*
O ·	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
<b>C</b>	FC 0C*
Constant	-56.86*
	(5.86)
Observations	1 012
	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05
	l

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	Earnings (2021 USD)
Age	0.42*
	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
Constant	-56.86*
	(5.86)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05

Prediction	Estimate
Baseline	\$27k
Finish College	\$44.1k
Finish Grad School	\$55.5k

Prediction	Estimate
Baseline Exercise 1x / week	\$27k \$32.4k
Exercise >3x	\$37.8k

	Earnings (2021 USD)
Age	0.42*
	(0.06)
E	E 71*
Education	5.71*
	(0.36)
Exercise	1.80*
Exercise	
	(0.42)
Constant	-56.86*
	(5.86)
	(3.00)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
- Statistic	101.17 (47 = 3, 1009)
Note:	*p < 0.05

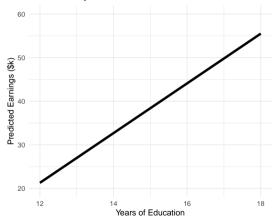
Education	Prediction
12	
13	
14	
15	
16	\$44.1k
17	
18	\$55.5k

Earnings (2021 USD)
0.42*
(0.06)
5.71*
(0.36)
1.80*
(0.42)
-56.86* (5.86)
(5.60)
1,813
0.14
38.88 (df = 1809)
101.17* (df = 3; 1809)
*p < 0.05

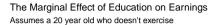
Education	Prediction
12	\$21.3k
13	\$27k
14	\$32.7k
15	\$38.4k
16	\$44.1k
17	\$49.8k
18	\$55.5k

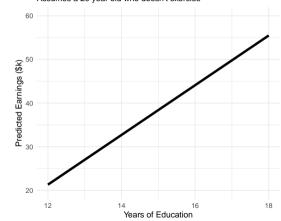
Education	Prediction
12	\$21.3k
13	\$27k
14	\$32.7k
15	\$38.4k
16	\$44.1k
17	\$49.8k
18	\$55.5k

#### The Marginal Effect of Education on Earnings Assumes a 20 year old who doesn't exercise



	Earnings (2021 USD)
Age	0.42*
	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
Constant	-56.86*
	(5.86)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	$101.17^* \text{ (df} = 3; 1809)$
Note:	*p < 0.05





	Earnings (2021 USD)
Age	0.42*
	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
Constant	-56.86*
	(5.86)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05

#### **Practice**

Make a marginal effects plot of exercise for a 22 year old who has finished their undergraduate degree (education = 16)

	Earnings (2021 USD)
Age	0.42*
-	(0.06)
Education	C 71*
Education	5.71*
	(0.36)
Exercise	1.80*
Exercise	(0.42)
	(0.42)
Constant	-56.86*
	(5.86)
	(0.00)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05
A VOLC.	p < 0.03

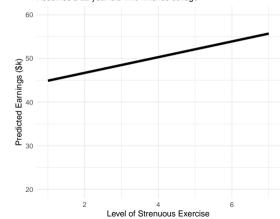
Exercise	Prediction
1	
2	
3	
4	
5	
6	
7	

	Earnings (2021 USD)
Age	0.42*
	(0.06)
Education	5.71*
	(0.36)
Exercise	1.80*
	(0.42)
Constant	-56.86*
	(5.86)
Observations	1,813
Adjusted R <sup>2</sup>	0.14
Residual Std. Error	38.88 (df = 1809)
F Statistic	101.17* (df = 3; 1809)
Note:	*p < 0.05

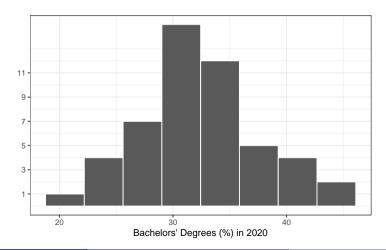
Exercise	Prediction
1	\$44.9k
2	\$46.7k
3	\$48.5k
4	\$50.3k
5	\$52.1k
6	\$53.9k
7	\$55.7k

Earnings (2021 USD)
0.42*
(0.06)
5.71*
(0.36)
1.80*
(0.42)
F6 06*
-56.86*
(5.86)
1.813
,
0.14
38.88 (df = 1809)
101.17* (df = 3; 1809)
*p < 0.05

The Marginal Effect of Exercise on Earnings Assumes a 22 year old who finishes college



# What is the "best" model of bachelor's degree completion in dataset 1?



## What is the "best" model of bachelor's degree completion in dataset 1?

- Choose the logical predictors
- Fit a simple OLS regression to each predictor
- Fit a multiple regression with the "best" of those
- Evaluate the model using all five steps
- Use the model to make predictions

# What is the "best" model of bachelor's degree completion in dataset 1?

#### **Outcome**

Bachelors' Degrees

#### **Predictors to Consider**

• GDP (Billions), GDP (Rate), Homeownership, Manufacturing employment, Minimum wage, Population, Rental Vacancy Rate, State Tax Rate on Wages, Unemployment

### Common Regression Mistakes (Wheelan ch12)

- Linear regression on nonlinear relationships
- Correlation does not equal causation
- Reverse causality
- Omitted variable bias (too few variables)
- Highly correlated explanatory variables (multicollinearity)
- Extrapolating beyond the data
- Data mining (too many variables)