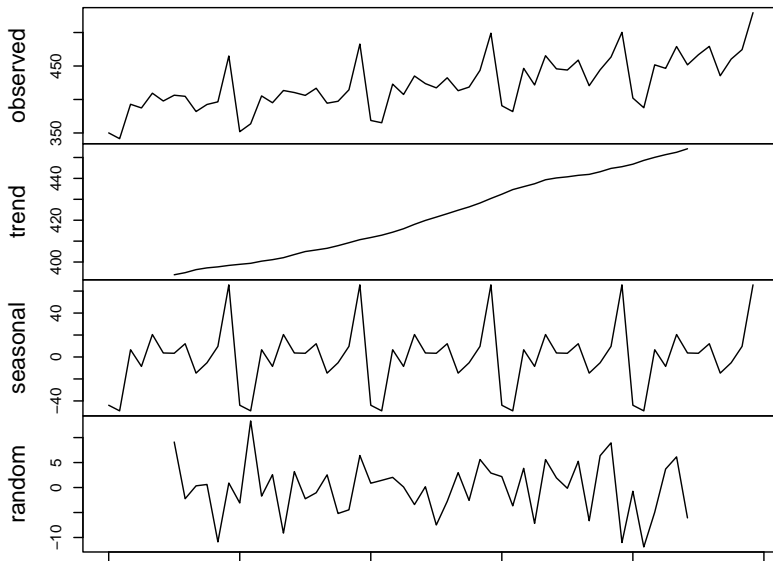


Today's Agenda

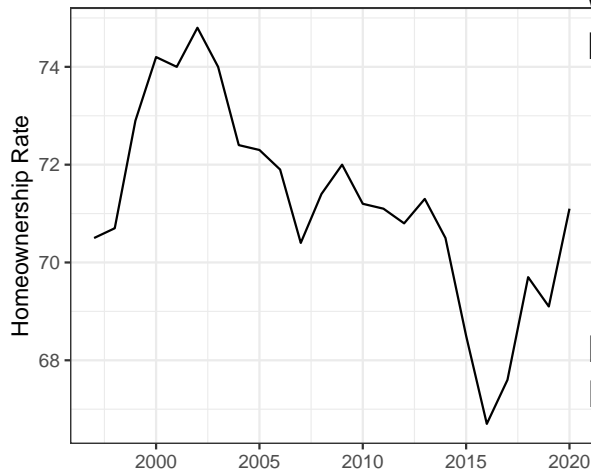
Comparing random variation models to linear trend models of time series data

Justin Leinaweaver (Spring 2022)

Decomposition of additive time series



Assignment for Today

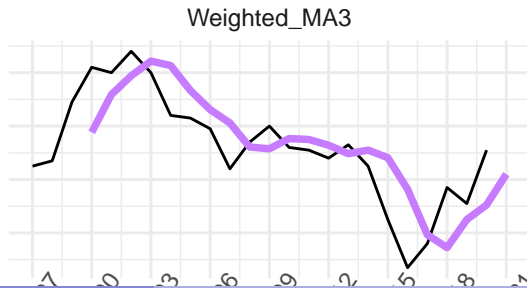
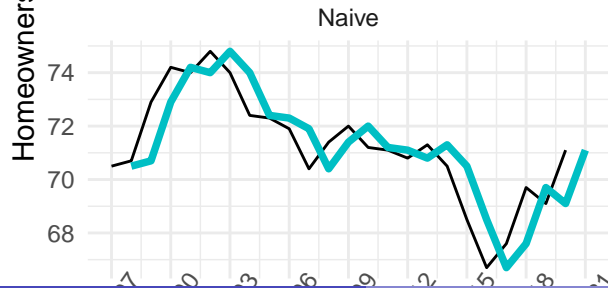
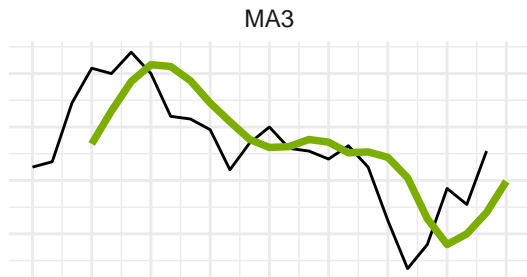
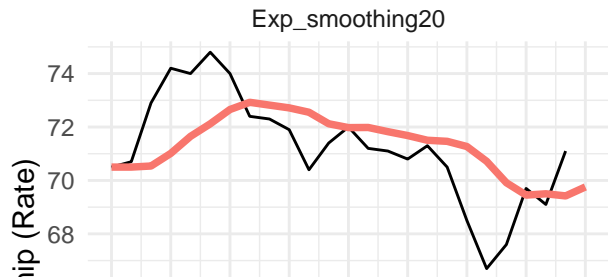


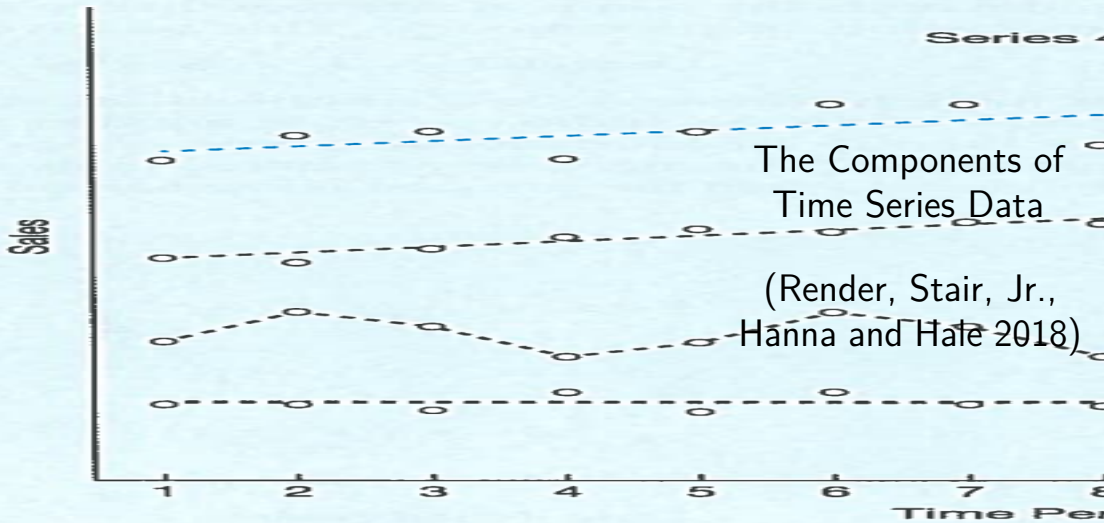
What is the best forecast model of homeownership rates in MO?

- Naïve
- MA (3)
- Weighted MA (3), or
- Exponential Smoothing (0.2)

Predict 2021 and calculate the MSE!

Forecast	MSE	Prediction
Naive	1.32	71.1
MA-3	2.46	70
WMA-3	1.96	70.2
Exp Smooth (.2)	3.15	69.8

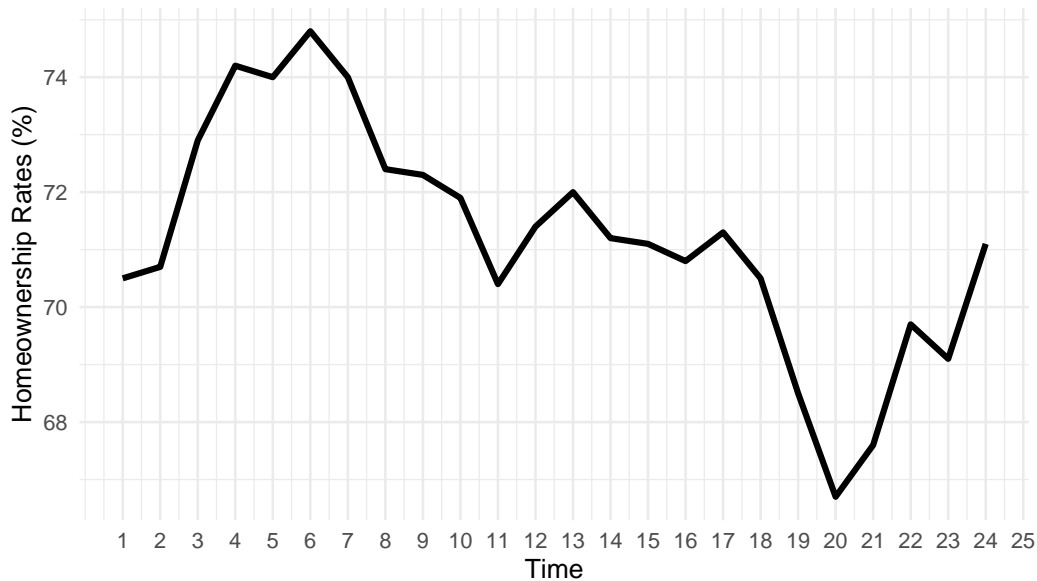




Homeownership in Missouri



OLS on Time Series Data: Regress on Time Period



Using OLS on Time Series Data

Regress homeownership rate on the time period

- Visualize the model as a line plot
- Calculate the MSE

Create Time Period Variable

	A	B	C	D
1	state	year	homeowner_rate	time
2	Missouri	1997	70.5	1
3	Missouri	1998	70.7	2
4	Missouri	1999	72.9	3
5	Missouri	2000	74.2	4
6	Missouri	2001	74	5
7	Missouri	2002	74.8	6
8	Missouri	2003	74	7
9	Missouri	2004	72.4	8
10	Missouri	2005	72.3	9
11	Missouri	2006	71.9	10
12	Missouri	2007	70.4	11
13	Missouri	2008	71.4	12
14	Missouri	2009	72	13

RESIDUAL OUTPUT		
<i>Observation</i>	<i>Predicted homeowner_rate</i>	<i>Residuals</i>
1	70.95	-0.45
2	71.83	-1.13
3	72.49	0.41
4	72.97	1.23
5	73.27	0.73
6	73.42	1.38
7	73.42	0.58
8	73.31	-0.91
9	73.09	-0.79
10	72.79	-0.89
11	72.41	-2.01
12	71.98	-0.58

MSE = Average of the Squared Residuals

Using OLS on Time Series Data

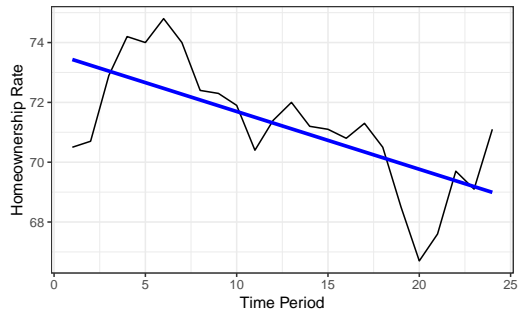
Regress homeownership rate on the time period

- Visualize the model as a line plot
- Calculate the MSE

	homeowner_rate
time	-0.19* (0.04)
Constant	73.63* (0.64)

Observations	24
Adjusted R ²	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)

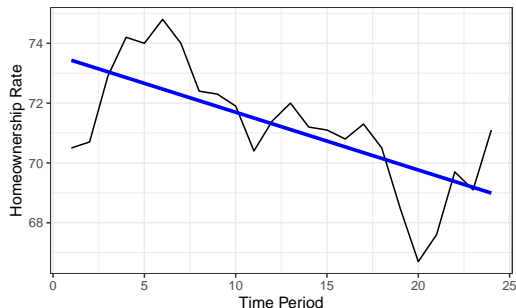
Note: *p < 0.05



Forecast	MSE	Prediction
Exp Smooth (.2)	3.15	69.8
MA-3	2.46	70
OLS	2.11	68.99
WMA-3	1.96	70.2
Naive	1.32	71.1

Make Predictions

	homeowner_rate
time	-0.19* (0.04)
Constant	73.63* (0.64)
Observations	24
Adjusted R ²	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)
Note: *p < 0.05	



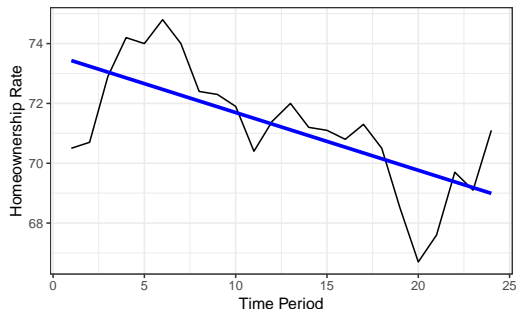
$$\text{Prediction} = 73.63 + -0.19 \times \text{Time}$$

Use the model to predict homeownership for the next two years.

Make Predictions

	homeowner_rate
time	-0.19* (0.04)
Constant	73.63* (0.64)
Observations	24
Adjusted R ²	0.43
Residual Std. Error	1.52 (df = 22)
F Statistic	18.61* (df = 1; 22)

Note: *p < 0.05



$$\text{Prediction} = 73.63 + -0.19 \times (\text{Time} = 25) = 68.88$$

$$\text{Prediction} = 73.63 + -0.19 \times (\text{Time} = 26) = 68.69$$

Using OLS on Time Series Data

Compare our results to two model transformations:

- 1 Regress homeownership rate on a quadratic function of time period
- 2 Regress homeownership rate on a cubic function of time period

	A	B	C	D	
1	state	year	homeowner_rate	time	
2	Missouri	1997	70.5	1	
3	Missouri	1998	70.7	2	
4	Missouri	1999	72.9	3	
5	Missouri	2000	74.2	4	
6	Missouri	2001	74	5	
7	Missouri	2002	74.8	6	
8	Missouri	2003	74	7	
9	Missouri	2004	72.4	8	
10	Missouri	2005	72.3	9	
11	Missouri	2006	71.9	10	
12	Missouri	2007	70.4	11	
13	Missouri	2008	71.4	12	
14	Missouri	2009	72	13	

time2

$$F2 = D2^2$$

$$F2$$

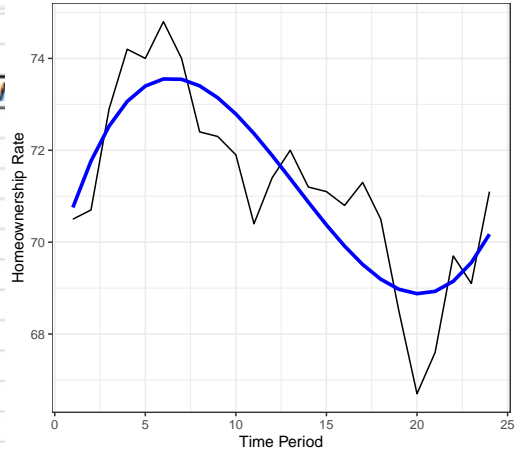
	Homeownership		
	(1)	(2)	(3)
Time	-0.19* (0.04)	0.03 (0.18)	1.42* (0.37)
Squared		-0.01 (0.01)	-0.15* (0.03)
Cubed			0.004* (0.001)
Constant	73.63* (0.64)	72.66* (1.00)	69.48* (1.10)
Observations	24	24	24
Adjusted R ²	0.43	0.45	0.68
Residual Std. Error	1.52 (df = 22)	1.50 (df = 21)	1.14 (df = 20)
F Statistic	18.61* (df = 1; 22)	10.30* (df = 2; 21)	17.18* (df = 3; 20)

Note:

*p < 0.05

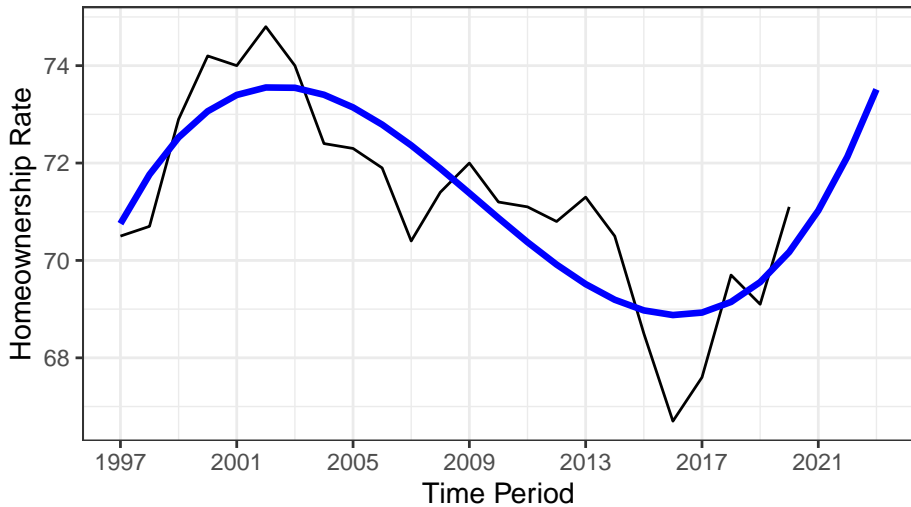
Forecast	MSE	Prediction
Exp Smooth (.2)	3.15	69.8
MA-3	2.46	70
OLS	2.11	68.99
OLS Quadratic	1.97	68.24
WMA-3	1.96	70.2
Naive	1.32	71.1
OLS Cubic	1.09	70.17

RESIDUAL OUTPUT	
Observation	Predicted
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	

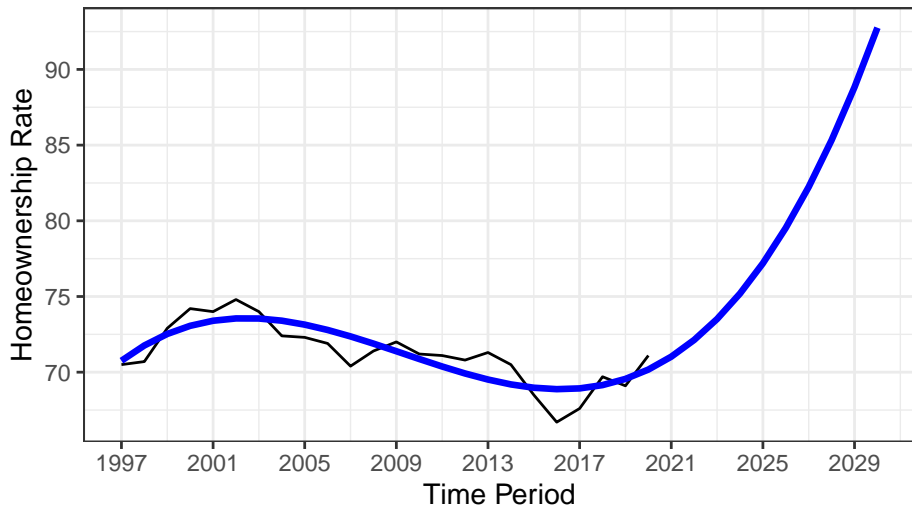


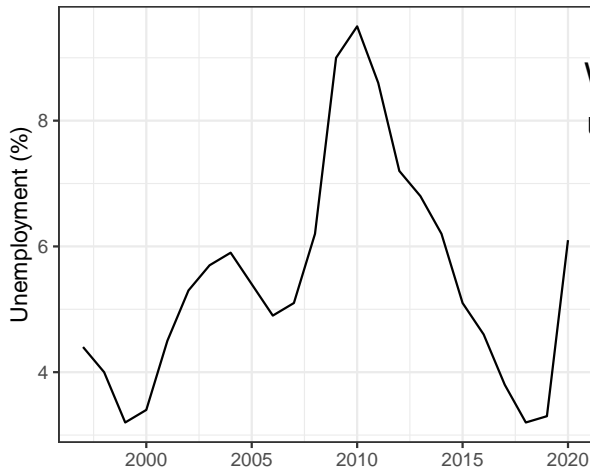
The model line is the "Predicted" column in the residual output.

Three Year Forecast



Ten Year Forecast

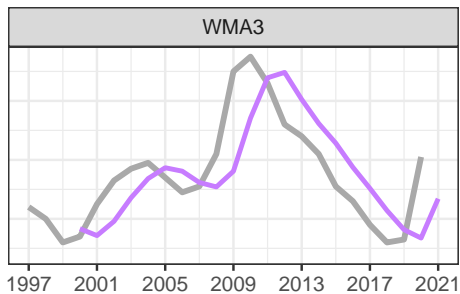
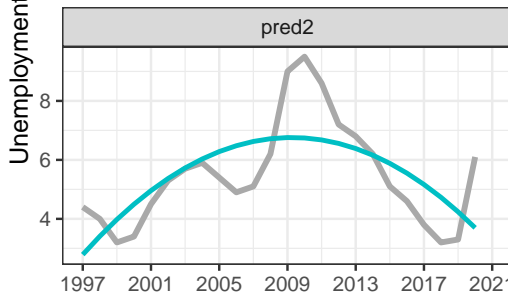
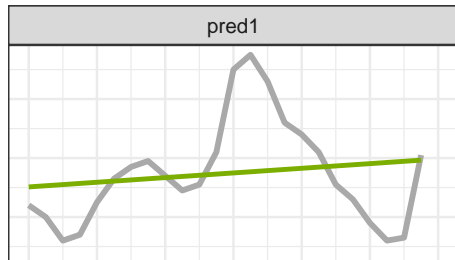
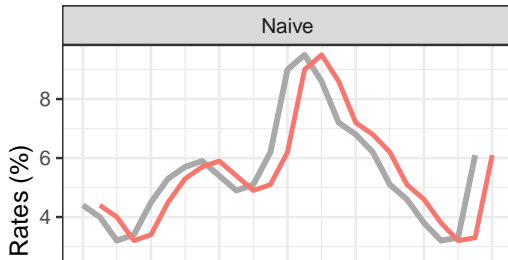




What is the best forecast model of unemployment rates in MO?

- Naïve
- Weighted MA (3)
- Linear model of time
- Quadratic function of time

Forecast	MSE
OLS	2.95
Weighted MA3	1.98
OLS (Quadratic)	1.67
Naive	1.14



Time