# Problem Solving as Search

CS161

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### What is search?

- Basic Al problem
- Long history, active topic
- Basis for games, SAT, advanced reasoning
- Used in many other fields
- UCLA plays key role in history of search ©

Graduate CS class offered by Prof. Korf

### What is search?

Structure: Search 'engine'



- Sensitive to
  - problem formulation (today)
  - choice of strategy (next lectures)

### Examples

- Puzzles
  - 8-puzzle
  - Missionaries and Cannibals
  - N-Queens
  - Crypto arithmetic
  - Rubik's cube
- Planning
  - Practical industry applications
     (e.g., Amazon delivery, Uber route and match, etc.)

How would you solve these?

### Search Problem Formulation

- Common elements:
  - Initial state
  - Final/goal state or goal test/predicate
  - Actions
  - Transition model/successors
  - (Costs)
- <u>Task</u>: find sequence of actions to move from initial to goal state.
- Optimal solution has lowest cost

### Search Problem Formulation

- Notions of state and action are not sharp!
- Design problem: art

Example: 8-puzzle?



- States are atomic (no internal structure)
- States are discrete
- No percepts
- Deterministic transitions
- How many unique states? 9! = 362,880
   15! = 10^12
- Choice of action space is important
  - Move tile x up, down, left, right?
  - Move blank up, down, left, right?
    More elegant, fewer actions!
- Actions may not be applicable to all states

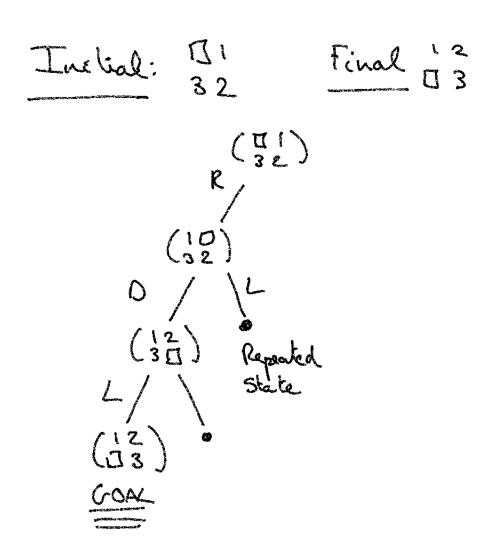
### **Search Trees**

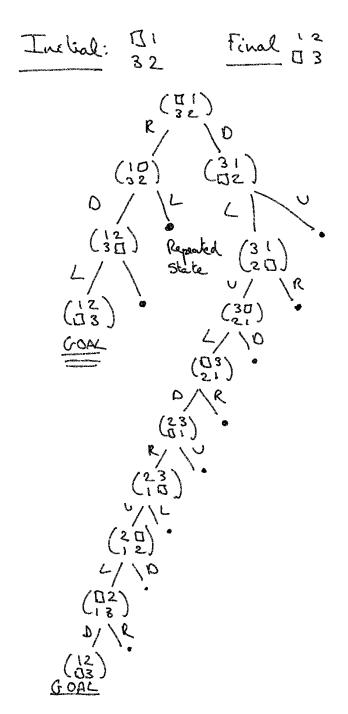
• Example: 8-puzzle?



- Some paths include the goal state
- Solving the search problem is finding such path
- Some paths are infinite (tree infinite)
- Beware: Repeated states
- Different solutions with different qualities
- Search space vs. search tree

Inclial: 31 Final 13

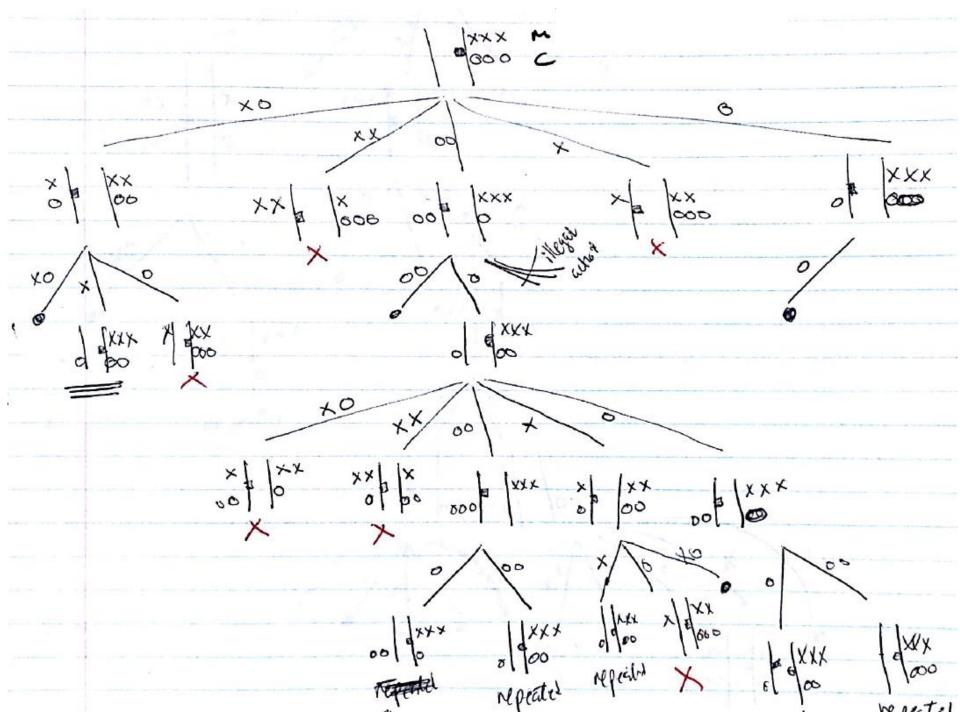


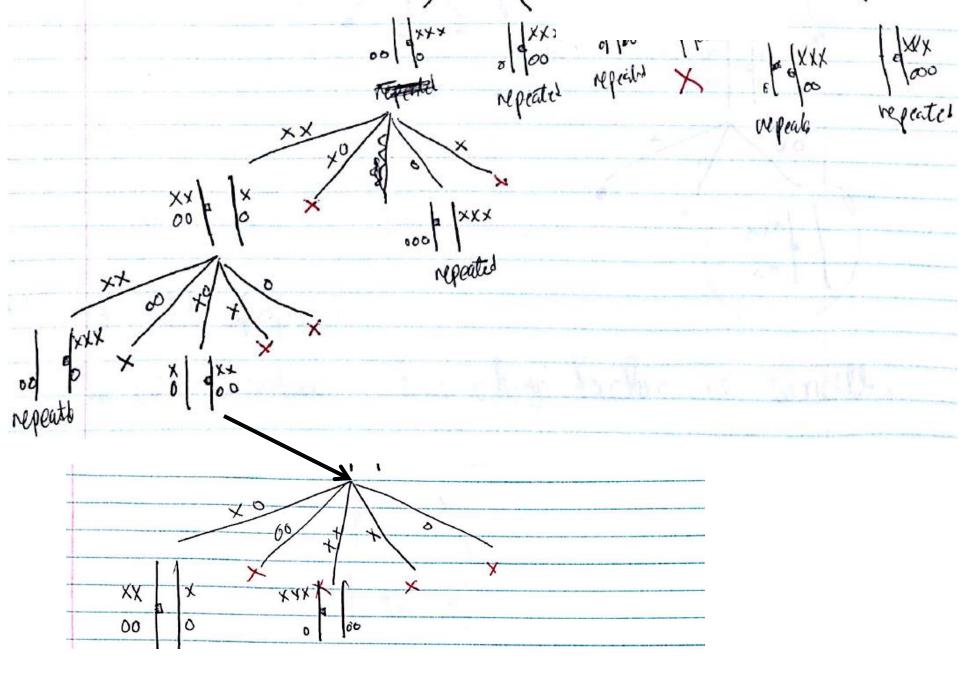


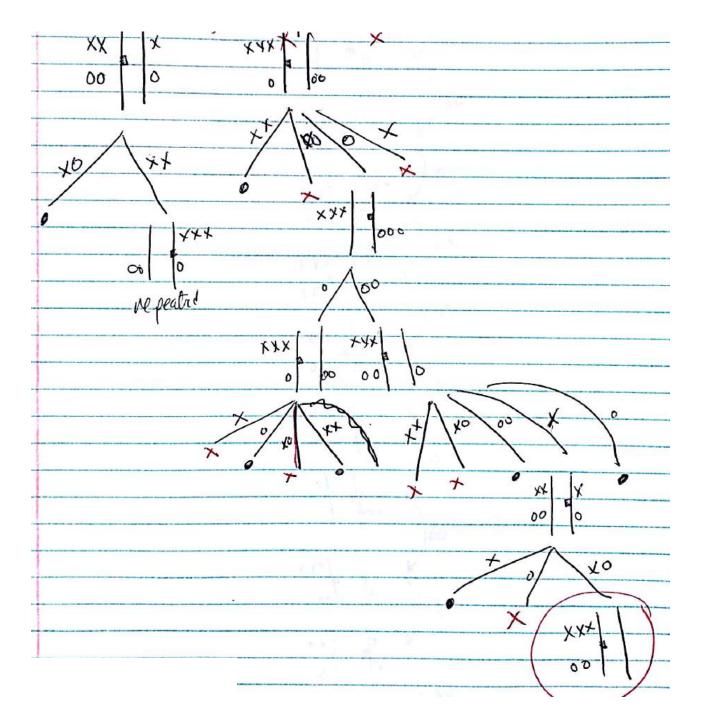
- Avoid repeated states or run into infinite loop
- Two solutions: cost 3 and cost 9
- Difficulty of problem: measured by parameters
  - Number of states
  - Branching factor
  - Solution depth
- 15-puzzle has 1.3 trillion states: few ms to solve
- 24-puzzle has 10^25 states: one day to solve
- Solving sliding block puzzles is NP-complete!

Example: Missionaries and Cannibals?

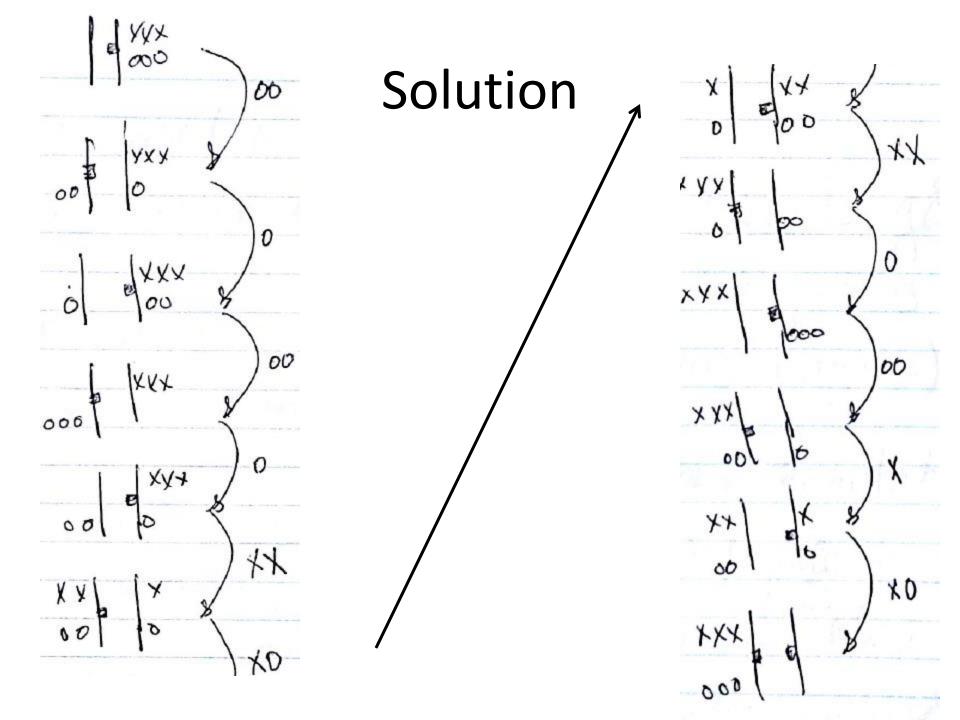




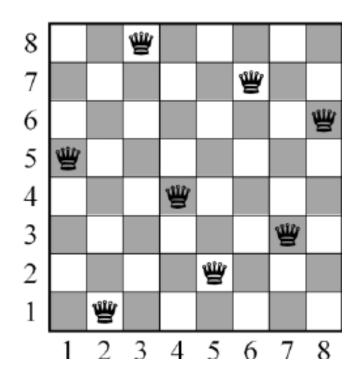




- Many choices for
  - State description
  - Actions
- Many correct, some better than others
- Find correct level of abstraction



• Example: 8-Queens?





- State formulation:
  - Incremental state
  - Complete state
- May or may not allow bad intermediate states
- No goal state => goal predicate
- Solution cost:
  - Incremental state: 8
  - Complete state: 0-8 (Can be solved in 0 moves!)

Example: Crypt-arithmetic?

FORTY	$\longrightarrow$	29786
TEN		850
TEN		850
+		+
SIXTY		31486



- Assign numbers to letters in fixed order (better: smallest number of remaining values)
- Incremental or complete state

- Example: Knut's Problem?
- Start: 4
- Actions
  - Factorial: x!
  - Sqrt:  $\sqrt{x}$
  - Floor: |x|
- Transitions: math
- Goal: 5 => HOW?



- Conjecture:
   Any positive integer can be reached
- No bound on intermediate representation
- Infinite state space

- Example of class of problems: recursively defined objects
  - Circuits, proofs, programs, etc.

### More Real-World Search Problems

Route finding

Amazon, computer networks, travel planning, airline planning, navigation systems

Traveling salesperson problems

Planning circuit board drill movements, mail delivery, street cleaning, etc.

What is a state?

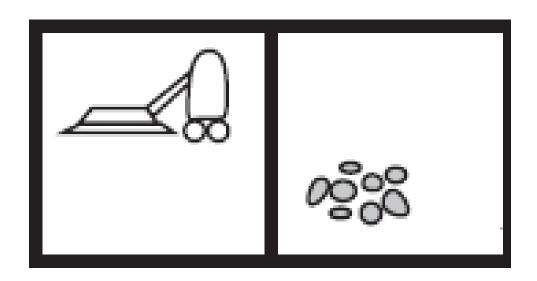
- Hardware layout
- Continuous robot navigation
- Scheduling
- Theorem proving

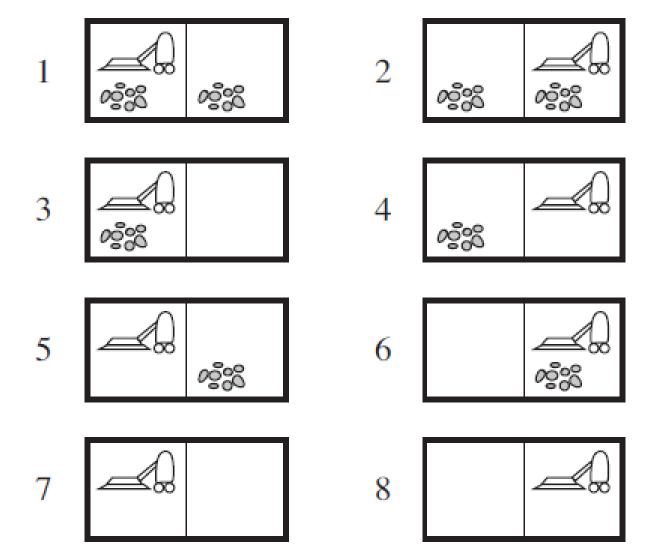
### Extensions/Complications

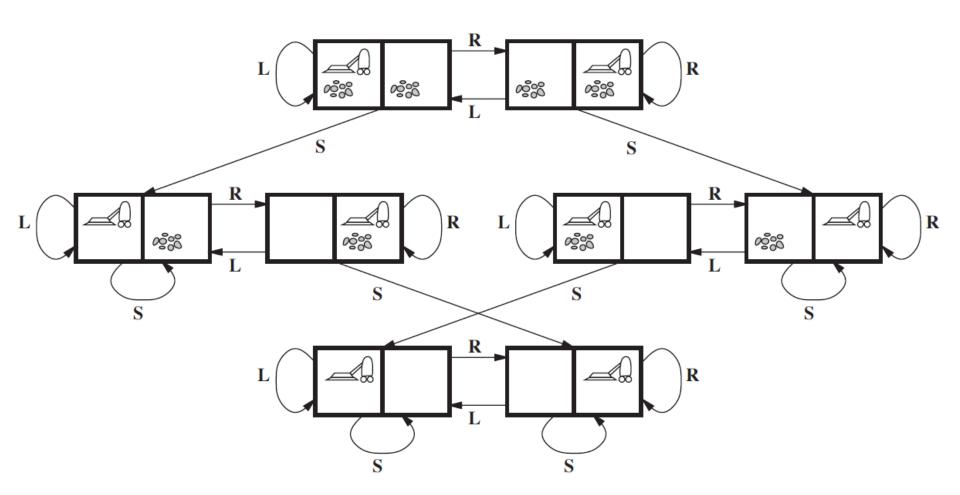
- Minimizing solution cost ('optimal solution')
  - Cost of solution is sum of action costs
- Note sure about effect of actions
  - Non-determinism (see probability later)
- Note sure about initial state

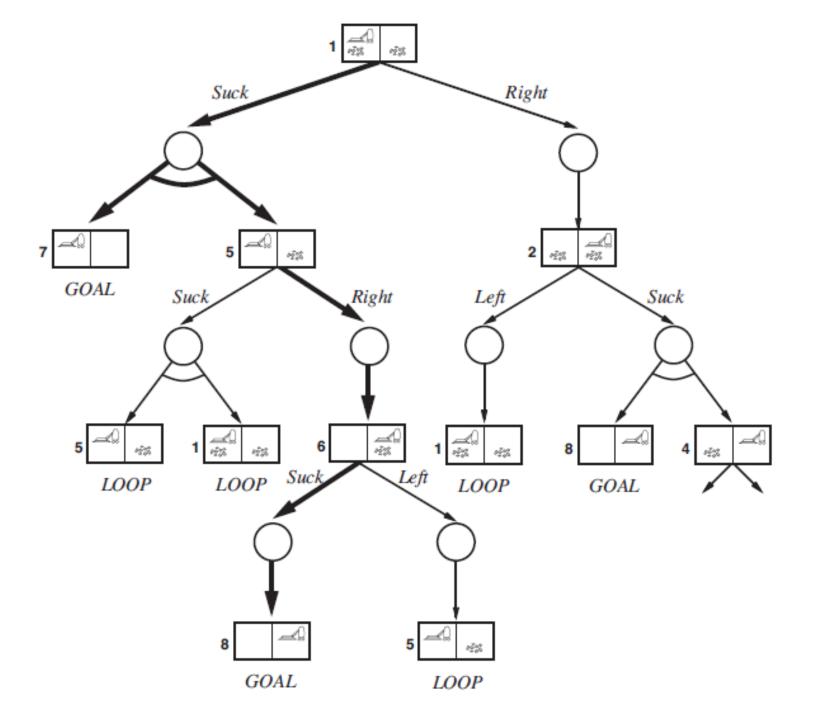
- Contingent planning: action based on sensing
- Conformant planning: plan without sensors
   Example: Not knowing initial state (see next)

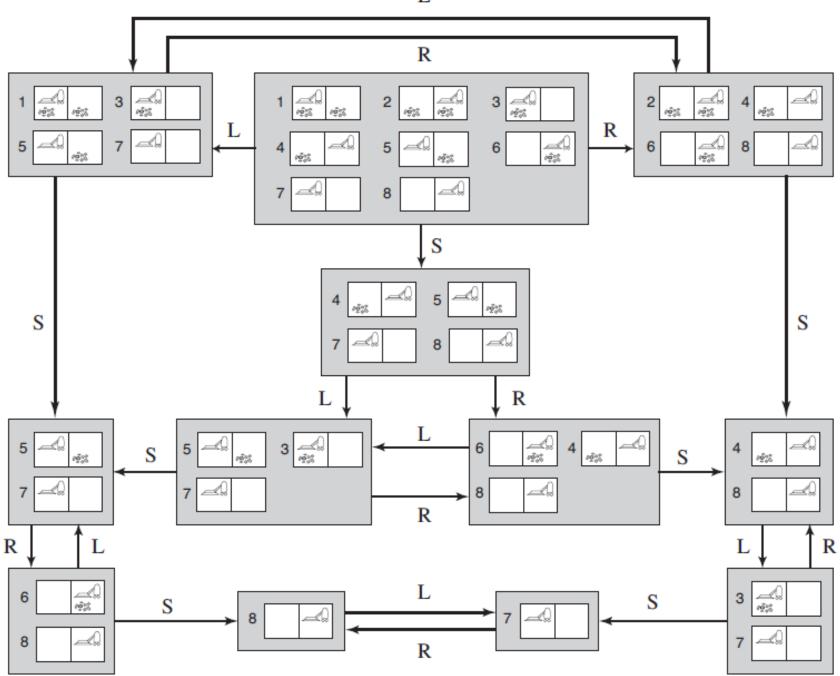
### Vacuum Cleaner World











- When uncertain about initial state, use belief states.
- Belief state is a set of deterministic states