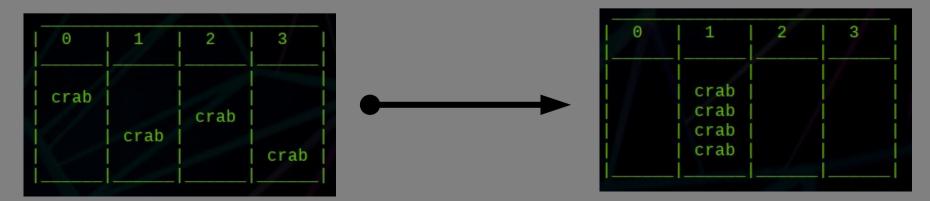
Advent of Code 2021

- Problem description: https://adventofcode.com/2021/day/7
- A "swarm" of crabs arranged with various non-negative integer horizontal positions (ex: 0, 7, 3)
- The crabs can move and they burn fuel proportional to the distance traveled (1 unit of fuel to move 1 unit of distance)
- Task: move all crabs to the same horizontal position while minimizing the total amount of fuel spent. Submit the sum of the fuel spent by all crabs.



- Proposed consolidation point: \hat{y}
- Crab horizontal position: χ
- Fuel function for single crab: $f(\hat{y}) = |\hat{y} x|$
- Fuel function for all crabs: $f(\hat{y}) = \sum_{i} |\hat{y} x_{i}|$

Day 7 - Part 1: Brute Force Technique

- For every horizontal position y between the minimum and maximum crab positions
 - For every crab x
 - Add abs(y x) to the sum
 - Return the minimum fuel cost.
- Is brute force feasible?
 - 1841 iterations of the outer loop
 - 1000 iterations of the inner loop
- Yes brute force is trivial

```
>>> data.shape
(1000,)
>>> data.min()
0
>>> data.max()
1840_
```

The End.

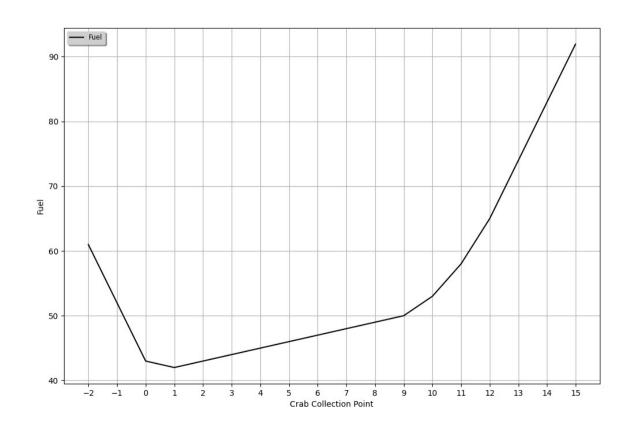
JK

Crab positions:

[0, 0, 0, 0, 1, 9, 10, 11, 12]

It's a convex function, which means it's easy to minimize

Part 1: Fuel Required vs Crab Collection Point (CCP)

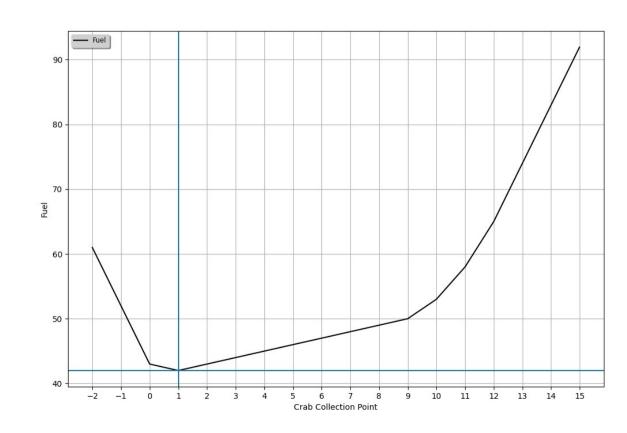


Crab positions:

[0, 0, 0, 0, 1, 9, 10, 11, 12]

Minimum fuel cost occurs when the slope of the fuel function is zero*.

Part 1: Fuel Required vs Crab Collection Point (CCP)



^{*}for this function, the slope is technically not defined at this point

Day 7 - Part 1: Math

 $X = \{x_0, x_1, ...\}$, initial crab positions $f(X, \hat{y}) = \sum_i |\hat{y} - x_i|$, fuel cost to move all crabs to position \hat{y}

Goal: minimize $f(\hat{y})$ by finding where derivative is 0 Trick question, $f(\hat{y})$ is only piece-wise differentiable.

Equivalent fuel function:

$$f(X, \hat{y}) = \begin{cases} \sum_{i} \hat{y} - x_{i}, & \text{where } \hat{y} \ge x_{i} \\ \sum_{i} x_{i} - \hat{y}, & \text{where } x_{i} > \hat{y} \end{cases}$$

Equivalent fuel derivative:

$$f'(X, \hat{y}) = \begin{cases} \sum_{i} 1, \text{ where } \hat{y} \ge x_{i} \\ \sum_{i} 1, \text{ where } x_{i} > \hat{y} \end{cases}$$

Another way to view the fuel function:

$$f'(X, \hat{y}) = \sum \hat{y} \ge x_i - \sum_i \hat{y} < x$$

- In the basic form, the function is only piece-wise differentiable and undefined at 0
- By rearranging, the fuel function derivative is minimized when then number of crabs to the right of y is equal to the number of crabs to the left of y
- This central location is the median.

Day 7 - Part 1: Implementation

```
1 #!/usr/bin/python3
2
3 import numpy as np
4
5 with open("input", "r") as in_file:
6    data = np.asarray(in_file.read().strip().split(','), np.int64)
7    print(np.absolute(data - np.round(np.median(data))).sum())
```

• The same crab layout and objective as before, but with a different fuel function.

As it turns out, crab submarine engines don't burn fuel at a constant rate. Instead, each change of 1 step in horizontal position costs 1 more unit of fuel than the last: the first step costs 1, the second step costs 2, the third step costs 3, and so on.

Crab Fuel	Function	
Distance	Total Fuel	
1	1	
2	3	
3	6	
4	10	
5	15	
6	21	

Recursive Definition:

$$f(1) = 1$$

$$f(x) = x + f(x - 1)$$

- The individual crab fuel function is the sum of every number between 1 and the distance traveled.
- Can be calculated directly:

$$f(d) = \frac{d \cdot (d+1)}{2}$$

• Overall crab fuel function:

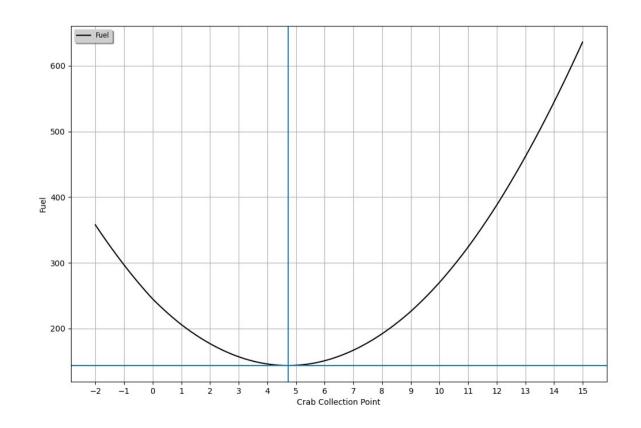
$$f(\hat{y}) = \sum_{i} \frac{d_i \cdot (d_i + 1)}{2}$$
, where $d_i = |\hat{y} - x_i|$

Crab positions:

[0, 0, 0, 0, 1, 9, 10, 11, 12]

Minimum fuel cost occurs when the slope of the fuel function is zero.

Part 2: Fuel Required vs Crab Collection Point (CCP)

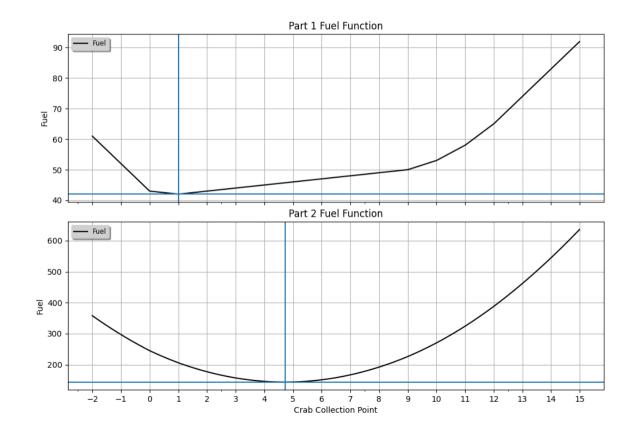


Crab positions:

[0, 0, 0, 0, 1, 9, 10, 11, 12]

The optimal crab collection point is dependent on the fuel function.





$$X = \{x_0, x_1, ...\}$$
, initial crab positions $d_i = |\hat{y} - x_i|$

Fuel cost to move all crabs to position \hat{y}

$$f(X, \hat{y}) = \sum_{i} \frac{d_i(d_i + 1)}{2} = \frac{1}{2} \sum_{i} [d_i^2 + d_i]$$

$$f(X, \hat{y}) = \frac{1}{2} \sum_{i} \left[d_i^2 + d_i \right]$$

$$f'(X, \hat{y}) = \frac{1}{2} \sum_{i} 2d_{i} + \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$f'(X, \hat{y}) = \sum_{i} d_{i} + \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$f'(X, \hat{y}) = \sum_{i} [\hat{y} - x_{i}] + \frac{1}{2} [\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y}]$$

$$f'(X, \hat{y}) = \sum_{i} [\hat{y} - x_{i}] + \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$f'(X, \hat{y}) = \sum_{i} \hat{y} - \sum_{i} x_{i} + \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$
$$f'(X, \hat{y}) = N \cdot \hat{y} - \sum_{i} x_{i} + \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$0 = N \cdot \hat{y} - \sum_{i} x_{i} + \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$N \cdot \hat{y} = \sum_{i} x_{i} - \frac{1}{2} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$\hat{y} = \frac{1}{N} \sum_{i} x_{i} - \frac{1}{2N} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$

$$\hat{y} = \frac{1}{N} \sum_{i} x_{i} - \frac{1}{2N} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$
What is this? What is the min/max of this expression?

$$\hat{y} = \frac{1}{N} \sum_{i} x_{i} - \frac{1}{2N} \left[\sum_{i} \hat{y} \ge x_{i} - \sum_{i} x_{i} > \hat{y} \right]$$
Average of all crab positions

Average of all crab positions

$$\hat{y} = \frac{1}{N} \sum_{i} x_{i} - \frac{1}{2} \cdot \frac{\pm N}{N}$$
Average of all crab positions

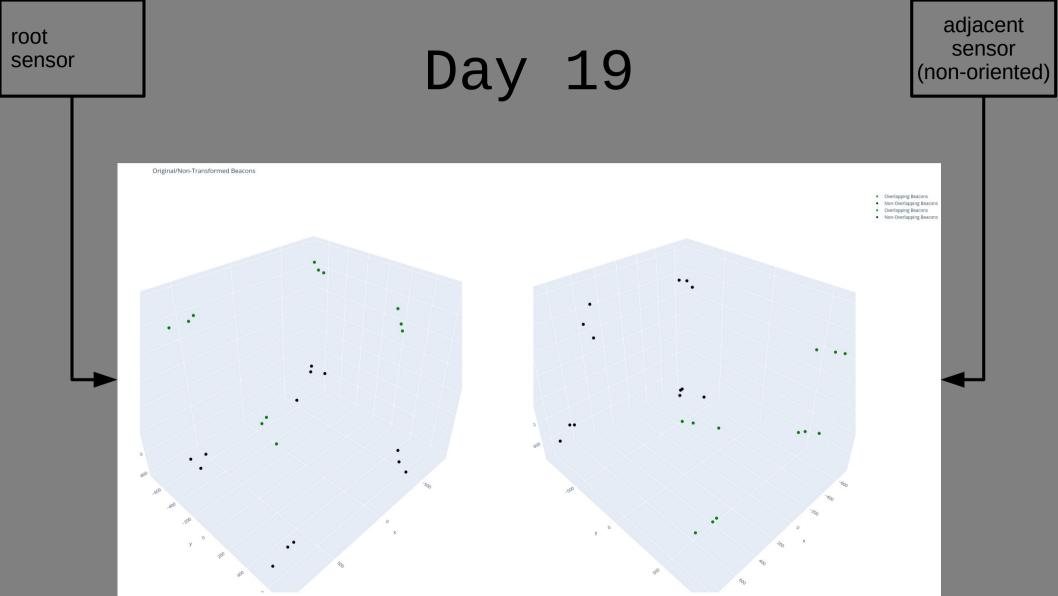
$$\hat{y} = \frac{1}{N} \sum_{i} x_{i} \pm \frac{1}{2}$$
Average of all crab positions

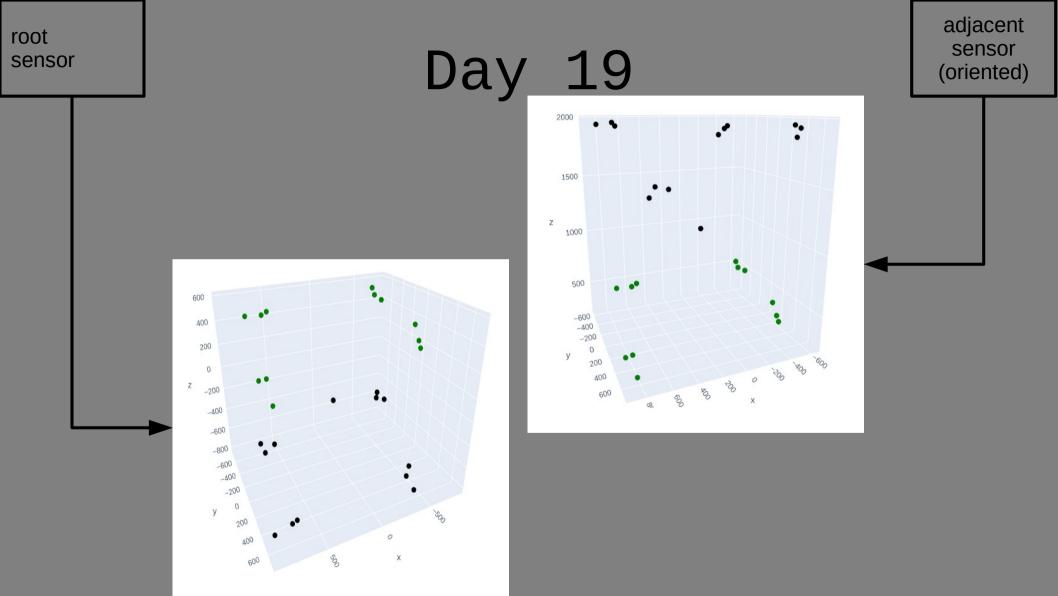
Day 7 - Part 2: Implementation

```
1 #!/usr/bin/python3
 3 import numpy as np
 5 from code import interact
 6
 7 def get_fuel(dist):
       return (dist * (dist + 1)) / 2
10 with open("input", "r") as in_file:
       data = np.asarray(in_file.read().strip().split(','), np.int64)
11
12
       ccp_0 = np.round(data.mean() - 0.5) #crab collection point
       ccp 1 = np.round(data.mean() + 0.5) #crab collection point
13
14
15
       abs_diff = np.absolute(data - ccp_0)
       min_fuel = np.vectorize(get_fuel)(abs_diff).sum()
16
17
       print("%d %d" % (ccp_0, min_fuel))
18
       abs_diff = np.absolute(data - ccp_1)
19
       min_fuel = np.vectorize(get_fuel)(abs_diff).sum()
20
21
       print("%d %d" % (ccp_1, min_fuel))
```

- Problem description: https://adventofcode.com/2021/day/19
- ~35 sensors
- ~25 beacons per sensor
- Beacon positions relative to the sensor are known, but the orientation of the beacons may be reflected and rotated about any axis any number of times
- Adjacent sensors share 12 beacons
- Tasks:
 - task 1: find the number of unique beacons
 - task 2: find the maximum manhattan distance between sensor centers
- Determining the correct orientation of each sensor will essentially solve both tasks

Day 19 original orientation true orientation >>> sensors[1].original_beacons sensors[1].original_beacons @ sensors[1].transform array([[670, 487, -847], 847, -670, 487], -432, 537, -3951, 395, 432, 537], -359, -521, 374, 359], 521, 374], -666, 441, 313], -313, 666, 441], 740, 701, 863] -863, -740, 701], -432, -383] 383, 432. 701], 721, -623] -698] -871, 818 605, 871] -818, 605] 496, -282, -496] 282, -564] 766, 577, 737] -737, 577], 489 375, -375. -489] -5961. -427] -537], 745, -562. -653] 650, 785] -523], 24, 36, 8] 36] -417, 608. 733] -386. -616, 490] -460], 453, -460, 776], 648, -745, -802], 745. -802, -648] 472, 454, 633], -454 -472] -596, 403. -500], -403, -500, 596] 710, -693, 557], 693, 557. -710] 874, -669 547], 669 -874], -508, -462, 508] -346, 529, 539]] -529, 346]], dtype=int32)





General approach:

- 1 The root node is oriented correctly
- 2 Calculate inter-beacon pairwise distances for each sensor
- 3 While unoriented sensors remain:
 - From an oriented sensor s1, consider an unoriented sensor s2
 - If 12 matching inter-beacon distances:
 - While s2 not oriented:
 - Rotate/reflect s2 beacons using one of 24 projection matrices
 - For each pair of overlapping beacons b1, b2
 - s2 center = b1 b2
 - If s2 center is equal for all overlapping pairs of beacons, s2 is oriented

Generate inter-beacon pairwise distances for each sensor:

```
26
           #get pairwise beacon-to-beacon distances
           self.dist = np.zeros(shape=(self.beacons.shape[0], self.beacons.shape[0]), dtype=np.float64)
28
           for idx in range(self.beacons.shape[0]):
29
30
               for jdx in range(self.beacons.shape[0]):
31
                   if idx == jdx:
32
                       continue
34
                   self.dist[idx, jdx] = (
36
                        (self.beacons[idx][0] - self.beacons[jdx][0])**2 +
                        (self.beacons[idx][1] - self.beacons[jdx][1])**2 +
38
                        (self.beacons[idx][2] - self.beacons[jdx][2])**2) ** 0.5
```

```
66.4, 1350.6, 1531.9, 1996.8, 1207.1, 1431.8, 1515.5, 2137.4, 1494.5, 1743.5, 1493.4, 187.8, 1272.9, 1249.2, 1779.3, 1112.1, 1980.7, 2375.4, 1608.5, 1492.9, 2258.5, 2306.2
array([[ 0. , 1512. , 1906. ,
       [1512., 0., 1831.5, 1520.1, 1550.3, 990., 1005.5, 1542., 95.5, 151.8, 1157.4, 1605.8, 1752.7, 939.4, 1333.4, 859.5, 1603.5, 1755.2, 1554.4, 963.4, 1502.9, 1099.6, 1521.3, 1337.3, 1450.6]
                        0., 1941.8, 1327.3, 1504.6, 1571.7, 1266.6, 1815.8, 1963.1, 1607.5, 1249., 204.4, 1529.1, 1872.9, 1005.1, 1261.1, 148.8, 1374.4, 1559.2, 1058.5, 1461.1, 1284.4, 1085.7, 1016.4
                                 0. 1338.1, 1578.6, 1994.8, 1269.6, 1441.6, 1518.2, 2134.9, 1485.6, 1783.2, 1538.7, 207. 1298.7, 1312.2, 1817.5, 1176.1, 1979.9, 2404.8, 1657.6, 1482.5, 2284.6, 2336.
                                        0., 1876.3, 1201.6, 1718.9, 1539.2, 1594., 1264.3, 164.8, 1309., 1853., 1337.2, 1020.5, 1751.9, 1298.1, 1734.2, 1218.1, 1766.3, 1927.3, 182.1, 1645.3, 1719.2
      [1531.9, 990. , 1504.6, 1578.6, 1876.3,
                                                0, 1640.1, 817.1, 934.2, 1108.4, 1769.6, 1914.7, 1366.2, 62.8, 1390.7, 885.7, 863.7, 1392.6, 866.2, 1593.3, 1394.., 126.9, 1878.., 1326.., 1330.1
       [1996.8, 1005.5, 1571.7, 1994.8, 1201.6, 1640.1,
                                                        0., 2001.9, 1070., 1065.4, 159.3, 1160.8, 1605.3, 1616.7, 1871.5, 991.1, 2048.4, 1574.9, 2055.8, 52.4, 1145.7, 1697.8, 1063.4, 967.7, 1122.8
      [1207.1, 1542. , 1266.6, 1269.6, 1718.9, 817.1, 2001.9,
                                                               0., 1468.7, 1644.6, 2124.3, 1768.9, 1067.5, 832.6, 1159.1, 1016.2, 65., 1120.2, 135.8, 1968.2, 1730.3, 791.5, 1778.5, 1694.3, 1661.6
      [1431.8, 95.5, 1815.8, 1441.6, 1539.2, 934.2, 1070. , 1468.7, 0. , 183.2, 1224.3, 1601.2, 1727.3, 881. , 1251.7, 832.6, 1531. , 1732.9, 1476. , 1028.5, 1535. , 1048. , 1520.6, 1373.5, 1479.8]
       [1515.5, 151.8, 1963.1, 1518.2, 1594. , 1108.4, 1065.4, 1644.6, 183.2,
                                                                            0., 1216.7, 1658.9, 1882.8, 1054.7, 1334.9, 978.8, 1707.5, 1885.8, 1647.2, 1027.1, 1643.9, 1222.9, 1571.2, 1475., 1592.9
      [2137.4, 1157.4, 1607.5, 2134.9, 1264.3, 1769.6, 159.3, 2124.3, 1224.3, 1216.7,
                                                                                     0, 1206.3, 1660, 1749.3, 2017, 1115.5, 2168.6, 1624.9, 2183.3, 197.2, 1146.1, 1821.1, 1112.3, 977.9, 1132.4
      [1494.5, 1605.8, 1249. , 1485.6, 164.8, 1914.7, 1160.8, 1768.9, 1601.2, 1658.9, 1206.3,
                                                                                            0., 1254.6, 1895.3, 1477.9, 1040.7, 1799.1, 1237.1, 1795.8, 1180.4, 1683.3, 1958.2, 110.9, 1569.8, 1640.4
      [1743.5, 1752.7, 204.4, 1783.2, 1309. , 1366.2, 1605.3, 1067.5, 1727.3, 1882.8, 1660. , 1254.6,
                                                                                                    0., 1390.3, 1712.5, 913.8, 1061.1, 59.8, 1173.5, 1588.9, 1136.9, 1323.4, 1289.6, 1149.5, 1085.7
      [1493.4, 939.4, 1529.1, 1538.7, 1853.
                                              62.8, 1616.7, 832.6, 881. , 1054.7, 1749.3, 1895.3, 1390.3, 0. , 1348.2, 868.9, 882.4, 1416.3, 874.1, 1570. , 1417. , 189.5, 1856.6, 1341.4, 1352.7
       187.8, 1333.4, 1872.9, 207., 1337.2, 1390.7, 1871.5, 1159.1, 1251.7, 1334.9, 2017., 1477.9, 1712.5, 1348.2,
                                                                                                                     0., 1158.6, 1208.2, 1746.2, 1069.9, 1852.4, 2263.5, 1475.6, 1463.8, 2140.6, 2194.3
                                                     991.1, 1016.2, 832.6, 978.8, 1115.5, 1040.7, 913.8, 868.9, 1158.6,
                                                                                                                             0. 1062.8 918.3 1069.6 961 1110.5 931.7 999.9 985.9 1042.8
       1249.2, 1603.5, 1261.1, 1312.2, 1751.9, 863.7, 2048.4, 65., 1531., 1707.5, 2168.6, 1799.1, 1061.1, 882.4, 1208.2, 1062.8,
                                                                                                                                     0., 1115.1, 166.4, 2015.2, 1749.9, 830.9, 1811.8, 1720.2, 1682.
      [1779.3, 1755.2, 148.8, 1817.5, 1298.1, 1392.6, 1574.9, 1120.2, 1732.9, 1885.8, 1624.9, 1237.1, 59.8, 1416.3, 1746.2, 918.3, 1115.1,
                                                                                                                                             0. . 1226.5. 1559.4. 1099.8. 1350.6. 1271.1. 1114.1. 1050.4
      [1112.1, 1554.4, 1374.4, 1176.1, 1734.2, 866.2, 2055.8, 135.8, 1476. , 1647.2, 2183.3, 1795.8, 1173.5, 874.1, 1069.9, 1069.6, 166.4, 1226.5,
                                                                                                                                                    0. , 2022.7, 1844.1, 855.3, 1805.2, 1800. , 1774.7
       [1980.7, 963.4, 1559.2, 1979.9, 1218.1, 1593.3,
                                                      52.4, 1968.2, 1028.5, 1027.1, 197.2, 1180.4, 1588.9, 1570., 1852.4,
                                                                                                                           961. , 2015.2, 1559.4, 2022.7,
                                                                                                                                                            0. , 1117.8, 1651.2, 1083.7, 937.6, 1093.5]
      [2375.4, 1502.9, 1058.5, 2404.8, 1766.3, 1394. , 1145.7, 1730.3, 1535. , 1643.9, 1146.1, 1683.3, 1136.9, 1417. , 2263.5, 1110.5, 1749.9, 1099.8, 1844.1, 1117.8,
       [1608.5, 1099.6, 1461.1, 1657.6, 1927.3, 126.9, 1697.8, 791.5, 1048. , 1222.9, 1821.1, 1958.2, 1323.4, 189.5, 1475.6, 931.7, 830.9, 1350.6, 855.3, 1651.2, 1360.9,
      [1492.9, 1521.3, 1284.4, 1482.5, 182.1, 1878. , 1063.4, 1778.5, 1520.6, 1571.2, 1112.3, 110.9, 1289.6, 1856.6, 1463.8, 999.9, 1811.8, 1271.1, 1805.2, 1083.7, 1647. , 1926.2,
       [2258.5, 1337.3, 1085.7, 2284.6, 1645.3, 1326. , 967.7, 1694.3, 1373.5, 1475. , 977.9, 1569.8, 1149.5, 1341.4, 2140.6, 985.9, 1720.2, 1114.1, 1800. , 937.6, 187. , 1309.1, 1524.3,
      [2306.2, 1450.6, 1016.4, 2336. , 1719.2, 1330.1, 1122.8, 1661.6, 1479.8, 1592.9, 1132.4, 1640.4, 1085.7, 1352.7, 2194.3, 1042.8, 1682. , 1050.4, 1774.7, 1093.5, 71.6, 1298. , 1604.3, 163.2, 0. ]]
```

40

Generate projection matrices:

```
def get_transforms(self):
           Generate the 24 unique transformation matricies
43
45
46
           #define the basic identity and rotation matrices
           ident = np.asarray([[1, 0, 0],
                                [ 0, 1, 0],
                               [0, 0, 1]])
49
           rot_y = np.asarray([[0, 0, 1],
51
52
53
54
55
56
                               [-1, 0, 0]])
           rot_x = np.asarray([[1, 0, 0],
                               [ 0, 0, -1],
           rot_z = np.asarray([[0, -1, 0],
59
                                [ 1, 0, 0],
60
                               [ 0, 0, 1]])
61
62
           #generate the 24 unique transformation matrices
63
           transforms = list()
           #generate every possible combination of 0-3 rotations about each axis
66
           for x in range(4):
              for y in range(4):
                   for z in range(4):
69
                       transform = ident.copy()
                       for _ in range(x):
                           transform = rot_x @ transform
74
                       for _ in range(y):
                           transform = rot y @ transform
                       for _ in range(z):
                           transform = rot_z @ transform
80
                       transforms.append(transform.copy())
           #convert to numpy array and retain only the 24 unique transfomation matrices
84
           transforms = np.asarray(transforms)
           transforms = np.unique(transforms, axis=0)
86
           return transforms
```

>>> Sensor.transforms[:12]

[0, -1, 0],

[0, 0, 1]],

array([[[-1, 0, 0],

Projection matrix examples:

```
[ 0, 0, -1],
                         [ 1, 0, 0]],
 [ 0, -1, 0]],
                        [[ 0, 0, 1],
[[-1, 0, 0],
                                          >>> Sensor.transforms
                                                                          (1, 2, 3)
                         [ 0, 1, 0],
                         [-1, 0, 0]],
 [ 0, 1, 0]],
                                          array([[-1, -2,
                                                                3],
                                                    [-1, -3,
                                                               -2],
                         [ 1, 0, 0],
                                                           3,
                                                                2],
                         [ 0, 1, 0]],
 [ 0, 0, -1]],
                                                               -3],
                                                          2,
[[ 0, -1, 0],
                                                          -1,
                                                               -3],
                         [-1, 0, 0],
                          0, 0, 1]],
                                                    [-2, -3,
                                                           3,
                        [[ 0, 1, 0],
[[ 0, -1, 0],
                                                                3],
 [ 0,
                         [-1, 0, 0]],
[ 1, 0, 0]],
                                                    [-3, -1,
                                                                2],
[[ 0, -1, 0],
                                                           2,
 [-1, 0, 0]],
                                                    [-3,
                        [[ 0, 1, 0],
                                                               -2],
                         [ 1, 0, 0],
                         [ 0, 0, -1]],
                                                          -2,
                                                                1],
                                                           2,
[[ 0, 0, -1],
                                                                2],
                             0, -1]],
 [ 0, 1, 0]],
                                                                3],
                                                          -1,
[[ 0, 0, -1],
                         [ 0, 0, -1],
                         [ 0, 1, 0]],
                                                      2,
                                                           3,
                                                                1],
 [-1, 0, 0]],
                                                                -3],
[[ 0, 0, -1],
                         [ 0, 0, 1],
                                                               -3],
 [ 1, 0, 0]],
                         0, -1, 0]],
                                                                2],
                                                          -3,
                                                           3,
                                                               -2],
                                                           2,
                                                                3]])
                         [ 0, 0, 1]]])
 [ 0, -1, 0]]])
```

>>> Sensor.transforms[12:] array([[[0, 0, 1],

[0, -1, 0]],

Find overlapping beacons based on pairwise inter-beacon distances:

```
88
       def get_pairs(self, dst):
           #determine the mapping from source-sensor-beacon-index to destination-sensor-beacon-index
89
           pairs = list()
90
91
92
           #intersect1d returns the values shared between the 3D arrays
93
           intersection_set = np.intersect1d(self.dist, dst.dist)
94
           #a shape of 67 implies the self sensor and the destination sensor have 12 overlapping beacons
95
           #(12 * 11) / 2 unique pairwise distances
96
           #this check is optional, but speeds up execution quite a bit because it skips the pairwise comparisons below on
97
           #non-overlapping sensors
98
99
           if intersection set.shape[0] == 67:
               for idx in range(self.dist.shape[0]):
L00
101
                   for jdx in range(dst.dist.shape[0]):
102
                       #check for 12 identical pairwise-distances using src-beacon-idx and dest-beacon-jdx as the base of
L03
                       #measurement
L04
                       #this indicates src.beacons[idx] and dst.beacons[jdx] are the same beacon
                       tmp = np.intersect1d(self.dist[idx], dst.dist[jdx])
L05
                       if tmp.shape[0] == 12:
L06
L07
                           pairs.append((idx, jdx))
L08
L09
           return pairs
```

Core logic of brute forcing the transforms and traversing the graph.

```
def orient peers(self):
111
112
            if self.visited:
113
                return
114
115
           self.visited = True
116
117
            for dst in Sensor.sensors:
118
                if dst.visited:
119
                    continue
120
121
                pairs = self.get_pairs(dst)
122
123
               if len(pairs) != 12:
124
                    continue
125
126
                for transform in Sensor.transforms:
127
                    #apply a transform to dst
128
                    tmp = dst.beacons @ transform
129
130
                   #calculate dst center relative to src based on each beacon
131
                   dst_centers = set()
132
133
                   for idx, jdx in pairs:
                        dst_centers.add(tuple(self.beacons[idx] - tmp[jdx]))
134
135
136
                   #if the number of dst_centers is 1, this indicates the transform was correct
137
                   if len(dst_centers) == 1:
138
                        #add the scanner_center to the list of scanner centers
139
                        Sensor.sensor_centers.append(dst_centers.pop())
140
141
                        #set the beacons to the transformed orientation and apply the linear offset of the scanner center
                        dst.beacons = tmp + Sensor.sensor_centers[-1]
                        dst.orient_peers()
144
                        break
```

Final logic to determine the number of unique beacons (part 1), and the maximal manhattan distance between sensor centers.

```
147 with open(file_name, "r") as in file:
148
        sensors = list()
149
        sensor_datas = in_file.read().split("\n\n")
150
151
        for sensor data in sensor datas:
152
            beacons = [coord.split(',') for coord in sensor data.strip().split('\n')[1:]]
153
154
155
156
157
            sensors.append(Sensor(beacons))
        sensors[0].orient_peers()
        concatenated = np.concatenate([sensors[idx].beacons for idx in range(len(Sensor.sensors))])
        concat uniq = np.unique(concatenated, axis=0)
158
159
160
161
        print(concat uniq.shape)
        max dist = 0
        for idx in range(len(sensors) - 1):
162
            for jdx in range(idx + 1, len(sensors)):
163
164
165
                dist = abs(Sensor_sensor_centers[idx][0] - Sensor.sensor_centers[jdx][0]) + \
                        abs(Sensor.sensor_centers[idx][1] - Sensor.sensor_centers[jdx][1]) + \
                        abs(Sensor.sensor_centers[idx][2] - Sensor.sensor_centers[jdx][2])
166
167
                if dist > max dist:
168
                     max dist = dist
169
170
        print(max_dist)
```

Visualization of oriented and arranged sensors/beacons.

