

Scalar Quartic Couplings in the Left-Right Symmetric Models

Higgs Quartic Coupling Vertices: LR triplet model

Here, we have encoded the possible non-zero quartic couplings that appear in this model in terms of the physical Higgs fields.

$$\begin{aligned}
H_0^0 H_0^0 H_0^0 H_0^0 &: \left[\frac{6 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 (\lambda_4 (k_1^2 + k_2^2) + (2\lambda_2 + \lambda_3) k_1 k_2) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^0 H_0^0 H_0^0 H_0^0 &: \left[\frac{6(k_1 - k_2)(k_1 + k_2) (\lambda_4 (k_1^2 + k_2^2) + 2(2\lambda_2 + \lambda_3) k_1 k_2)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^0 H_1^0 H_0^0 H_0^0 &: \left[\frac{2 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 2(2\lambda_2 + \lambda_3) (k_1^4 - 4k_1^2 k_2^2 + k_2^4) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_2^0 H_2^0 H_0^0 H_0^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (4\alpha_2 k_1 + \alpha_3 k_2)}{k_1^2 + k_2^2} \right] \\
H_3^0 H_3^0 H_0^0 H_0^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (4\alpha_2 k_1 + \alpha_3 k_2)}{k_1^2 + k_2^2} \right] \\
H_1^- H_1^+ H_0^0 H_0^0 &: \left[\alpha_1 + \frac{\alpha_3}{2} + \frac{4\alpha_2 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_2^- H_2^+ H_0^0 H_0^0 &: \left[\frac{2 \left(\lambda_1 (k_1^2 + k_2^2)^2 - 4(2\lambda_2 + \lambda_3) k_1^2 k_2^2 \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^{--} H_1^{++} H_0^0 H_0^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 + 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_2^{--} H_2^{++} H_0^0 H_0^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 + 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
A_1^0 A_1^0 H_0^0 H_0^0 &: \left[\frac{2 \left(2\lambda_3 (k_1^4 + k_2^4) + \lambda_1 (k_1^2 + k_2^2)^2 - 4\lambda_2 (k_1^4 + 4k_1^2 k_2^2 + k_2^4) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^0 H_1^0 H_1^0 H_0^0 &: \left[\frac{6(k_1 - k_2)(k_1 + k_2) (\lambda_4 (k_1^2 + k_2^2) - 2(2\lambda_2 + \lambda_3) k_1 k_2)}{(k_1^2 + k_2^2)^2} \right] \\
H_2^0 H_2^0 H_1^0 H_0^0 &: \left[\frac{2\alpha_2 (k_1 - k_2)(k_1 + k_2) + \alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_3^0 H_3^0 H_1^0 H_0^0 &: \left[\frac{2\alpha_2 (k_1 - k_2)(k_1 + k_2) + \alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right]
\end{aligned}$$

$$\begin{aligned}
H_1^- H_1^+ H_1^0 H_0^0 &: \left[\frac{2\alpha_2(k_1 - k_2)(k_1 + k_2)}{k_1^2 + k_2^2} \right] \\
H_2^- H_2^+ H_1^0 H_0^0 &: \left[\frac{2(k_1 - k_2)(k_1 + k_2)(\lambda_4(k_1^2 + k_2^2) - 2(2\lambda_2 + \lambda_3)k_1 k_2)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^{--} H_1^{++} H_1^0 H_0^0 &: \left[\frac{2\alpha_2(k_1 - k_2)(k_1 + k_2) - \alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_2^{--} H_2^{++} H_1^0 H_0^0 &: \left[\frac{2\alpha_2(k_1 - k_2)(k_1 + k_2) - \alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right] \\
A_1^0 A_1^0 H_1^0 H_0^0 &: \left[\frac{2(k_1 - k_2)(k_1 + k_2)(\lambda_4(k_1^2 + k_2^2) - 2(2\lambda_2 + \lambda_3)k_1 k_2)}{(k_1^2 + k_2^2)^2} \right] \\
H_2^- H_1^+ H_3^0 H_0^0 &: \left[\frac{\alpha_3 k_1 k_2}{\sqrt{2}(k_1^2 + k_2^2)} \right] \\
H_2^+ H_1^- H_3^0 H_0^0 &: \left[\frac{\alpha_3 k_1 k_2}{\sqrt{2}(k_1^2 + k_2^2)} \right] \\
H_1^{--} H_2^+ H_1^+ H_0^0 &: \left[-\frac{\alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_1^{++} H_2^- H_1^- H_0^0 &: \left[-\frac{\alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_1^0 H_1^0 H_1^0 H_1^0 &: \left[\frac{6 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 ((2\lambda_2 + \lambda_3)k_1 k_2 - \lambda_4(k_1^2 + k_2^2)) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_2^0 H_2^0 H_1^0 H_1^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_3^0 H_3^0 H_1^0 H_1^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_1^- H_1^+ H_1^0 H_1^0 &: \left[\alpha_1 + \frac{\alpha_3}{2} - \frac{4\alpha_2 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_2^- H_2^+ H_1^0 H_1^0 &: \left[\frac{2 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 ((2\lambda_2 + \lambda_3)k_1 k_2 - \lambda_4(k_1^2 + k_2^2)) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^{--} H_1^{++} H_1^0 H_1^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
H_2^{--} H_2^{++} H_1^0 H_1^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
A_1^0 A_1^0 H_1^0 H_1^0 &: \left[\frac{2 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 ((2\lambda_2 + \lambda_3)k_1 k_2 - \lambda_4(k_1^2 + k_2^2)) \right)}{(k_1^2 + k_2^2)^2} \right]
\end{aligned}$$

$$\begin{aligned}
H_2^- H_1^+ H_3^0 H_1^0 &: \left[\frac{\alpha_3 (k_1 - k_2)(k_1 + k_2)}{2\sqrt{2} (k_1^2 + k_2^2)} \right] \\
H_2^+ H_1^- H_3^0 H_1^0 &: \left[\frac{\alpha_3 (k_1 - k_2)(k_1 + k_2)}{2\sqrt{2} (k_1^2 + k_2^2)} \right] \\
H_1^{--} H_2^+ H_1^+ H_1^0 &: \left[\frac{\alpha_3 (k_2^2 - k_1^2)}{2 (k_1^2 + k_2^2)} \right] \\
H_1^{++} H_2^- H_1^- H_1^0 &: \left[\frac{\alpha_3 (k_2^2 - k_1^2)}{2 (k_1^2 + k_2^2)} \right] \\
H_2^0 H_2^0 H_2^0 H_2^0 &: [6\rho_1] \\
H_3^0 H_3^0 H_2^0 H_2^0 &: [\rho_3] \\
H_1^- H_1^+ H_2^0 H_2^0 &: [\rho_3] \\
H_2^- H_2^+ H_2^0 H_2^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_1^{--} H_1^{++} H_2^0 H_2^0 &: [\rho_3] \\
H_2^{--} H_2^{++} H_2^0 H_2^0 &: [2(\rho_1 + 2\rho_2)] \\
A_1^0 A_1^0 H_2^0 H_2^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_2^{--} H_1^{++} H_3^0 H_2^0 &: [2\rho_4] \\
H_2^{++} H_1^{--} H_3^0 H_2^0 &: [2\rho_4] \\
H_2^{--} H_1^+ H_1^+ H_2^0 &: [2\sqrt{2}\rho_4] \\
H_2^{++} H_1^- H_1^- H_2^0 &: [2\sqrt{2}\rho_4] \\
H_3^0 H_3^0 H_3^0 H_3^0 &: [6\rho_1] \\
H_1^- H_1^+ H_3^0 H_3^0 &: [2\rho_1] \\
H_2^- H_2^+ H_3^0 H_3^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
H_1^{--} H_1^{++} H_3^0 H_3^0 &: [2(\rho_1 + 2\rho_2)] \\
H_2^{--} H_2^{++} H_3^0 H_3^0 &: [\rho_3] \\
A_1^0 A_1^0 H_3^0 H_3^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_1^{--} H_1^+ H_1^+ H_3^0 &: [2\sqrt{2}\rho_2] \\
A_1^0 H_2^- H_1^+ H_3^0 &: \left[-\frac{i\alpha_3 (k_1 - k_2)(k_1 + k_2)}{2\sqrt{2} (k_1^2 + k_2^2)} \right]
\end{aligned}$$

$$\begin{aligned}
H_1^{++} H_1^- H_1^- H_3^0 &: \left[2\sqrt{2}\rho_2 \right] \\
A_1^0 H_2^+ H_1^- H_3^0 &: \left[\frac{i\alpha_3(k_1 - k_2)(k_1 + k_2)}{2\sqrt{2}(k_1^2 + k_2^2)} \right] \\
H_1^- H_1^- H_1^+ H_1^+ &: \left[4(\rho_1 + \rho_2) \right] \\
H_2^- H_2^+ H_1^- H_1^+ &: \left[\alpha_1 + \frac{\alpha_3}{2} - \frac{4\alpha_2 k_1 k_2}{k_1^2 + k_2^2} \right] \\
H_1^{--} H_1^{++} H_1^- H_1^+ &: \left[2\rho_1 \right] \\
H_2^- H_2^{++} H_1^- H_1^+ &: \left[\rho_3 \right] \\
A_1^0 A_1^0 H_1^- H_1^+ &: \left[\alpha_1 + \frac{\alpha_3}{2} - \frac{4\alpha_2 k_1 k_2}{k_1^2 + k_2^2} \right] \\
A_1^0 H_1^{--} H_2^+ H_1^+ &: \left[-\frac{i\alpha_3(k_1 - k_2)(k_1 + k_2)}{2(k_1^2 + k_2^2)} \right] \\
A_1^0 H_1^{++} H_2^- H_1^- &: \left[\frac{i\alpha_3(k_1 - k_2)(k_1 + k_2)}{2(k_1^2 + k_2^2)} \right] \\
H_2^- H_2^- H_2^+ H_2^+ &: \left[\frac{4 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 ((2\lambda_2 + \lambda_3) k_1 k_2 - \lambda_4 (k_1^2 + k_2^2)) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^{--} H_1^{++} H_2^- H_2^+ &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
H_2^{--} H_2^{++} H_2^- H_2^+ &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
A_1^0 A_1^0 H_2^- H_2^+ &: \left[\frac{2 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 ((2\lambda_2 + \lambda_3) k_1 k_2 - \lambda_4 (k_1^2 + k_2^2)) \right)}{(k_1^2 + k_2^2)^2} \right] \\
H_1^{--} H_1^{--} H_1^{++} H_1^{++} &: \left[4\rho_1 \right] \\
H_2^{--} H_2^{++} H_1^{--} H_1^{++} &: \left[\rho_3 \right] \\
A_1^0 A_1^0 H_1^{--} H_1^{++} &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
H_2^{--} H_2^{--} H_2^{++} H_2^{++} &: \left[4\rho_1 \right] \\
A_1^0 A_1^0 H_2^{--} H_2^{++} &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
A_1^0 A_1^0 A_1^0 A_1^0 &: \left[\frac{6 \left(\lambda_1 (k_1^2 + k_2^2)^2 + 4k_1 k_2 ((2\lambda_2 + \lambda_3) k_1 k_2 - \lambda_4 (k_1^2 + k_2^2)) \right)}{(k_1^2 + k_2^2)^2} \right]
\end{aligned}$$

$$\begin{aligned}
A_2^0 A_2^0 H_0^0 H_0^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (4\alpha_2 k_1 + \alpha_3 k_2)}{k_1^2 + k_2^2} \right] \\
A_2^0 A_2^0 H_1^0 H_0^0 &: \left[\frac{2\alpha_2 (k_1 - k_2)(k_1 + k_2) + \alpha_3 k_1 k_2}{k_1^2 + k_2^2} \right] \\
A_2^0 H_2^- H_1^+ H_0^0 &: \left[-\frac{i\alpha_3 k_1 k_2}{\sqrt{2} (k_1^2 + k_2^2)} \right] \\
A_2^0 H_2^+ H_1^- H_0^0 &: \left[\frac{i\alpha_3 k_1 k_2}{\sqrt{2} (k_1^2 + k_2^2)} \right] \\
A_2^0 A_2^0 H_1^0 H_1^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
A_2^0 H_2^- H_1^+ H_1^0 &: \left[-\frac{i\alpha_3 (k_1 - k_2)(k_1 + k_2)}{2\sqrt{2} (k_1^2 + k_2^2)} \right] \\
A_2^0 H_2^+ H_1^- H_1^0 &: \left[\frac{i\alpha_3 (k_1 - k_2)(k_1 + k_2)}{2\sqrt{2} (k_1^2 + k_2^2)} \right] \\
A_2^0 A_2^0 H_2^0 H_2^0 &: [\rho_3] \\
A_2^0 H_2^{--} H_1^{++} H_2^0 &: [2i\rho_4] \\
A_2^0 A_2^0 H_3^0 H_3^0 &: [2\rho_1] \\
A_2^0 H_1^{--} H_1^+ H_1^+ &: [-2i\sqrt{2}\rho_2] \\
A_2^0 A_2^0 H_1^- H_1^+ &: [2\rho_1] \\
A_2^0 A_1^0 H_2^- H_1^+ &: \left[\frac{\alpha_3 (k_2^2 - k_1^2)}{2\sqrt{2} (k_1^2 + k_2^2)} \right] \\
A_2^0 H_1^{++} H_1^- H_1^- &: [2i\sqrt{2}\rho_2] \\
A_2^0 A_2^0 H_2^- H_2^+ &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_2 (\alpha_3 k_2 - 4\alpha_2 k_1)}{k_1^2 + k_2^2} \right] \\
A_2^0 A_2^0 H_1^{--} H_1^{++} &: [2(\rho_1 + 2\rho_2)] \\
A_2^0 A_2^0 H_2^{--} H_2^{++} &: [\rho_3] \\
A_2^0 A_2^0 A_1^0 A_1^0 &: \left[\frac{\alpha_1 (k_1^2 + k_2^2) + k_1 (\alpha_3 k_1 - 4\alpha_2 k_2)}{k_1^2 + k_2^2} \right] \\
A_2^0 A_2^0 A_2^0 A_2^0 &: [6\rho_1]
\end{aligned}$$