

Table 0.1: Simulations results, 10,000 iterations,  $\lambda_Z = 1$ . 22 November 2020.

| model  | n=100 |       |       |           |          | n=200 |       |       |           |          | n=500 |       |         |           |          | n=1000 |       |       |           |          |
|--|-------|-------|-------|-----------|----------|-------|-------|-------|-----------|----------|-------|-------|---------|-----------|----------|--------|-------|-------|-----------|----------|
|  | Bias  | MAE   | RMSE  | Cov. rate | $q_{95}$ | Bias  | MAE   | RMSE  | Cov. rate | $q_{95}$ | Bias  | MAE   | RMSE    | Cov. rate | $q_{95}$ | Bias   | MAE   | RMSE  | Cov. rate | $q_{95}$ |
| $\lambda_X=0.4, \alpha_Y=2 - b_2 + d_2=1.1$  |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.008 | 0.049 | 0.064 | 0.999     | 1.236    | 0.005 | 0.034 | 0.043 | 0.999     | 1.148    | 0.002 | 0.021 | 0.027   | 0.999     | 1.072    | 0.001  | 0.015 | 0.019 | 0.999     | 1.079    |
| smoothed                                     | 0.008 | 0.049 | 0.062 | 0.999     | 1.206    | 0.005 | 0.034 | 0.043 | 0.999     | 1.142    | 0.002 | 0.021 | 0.027   | 0.999     | 1.071    | 0.001  | 0.015 | 0.019 | 0.999     | 1.076    |
| $\lambda_X=0.4, \alpha_Y=3 - b_2 + d_2=0.93$ |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.005 | 0.028 | 0.036 | 0.996     | 0.693    | 0.002 | 0.02  | 0.025 | 0.996     | 0.662    | 0.001 | 0.012 | 0.015   | 0.995     | 0.605    | 0.0    | 0.009 | 0.011 | 0.991     | 0.609    |
| smoothed                                     | 0.005 | 0.028 | 0.036 | 0.996     | 0.684    | 0.002 | 0.02  | 0.025 | 0.997     | 0.66     | 0.001 | 0.012 | 0.015   | 0.995     | 0.607    | 0.0    | 0.009 | 0.011 | 0.991     | 0.607    |
| $\lambda_X=0.4, \alpha_Y=4 - b_2 + d_2=0.85$ |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.003 | 0.02  | 0.025 | 0.994     | 0.483    | 0.002 | 0.014 | 0.018 | 0.993     | 0.456    | 0.001 | 0.009 | 0.011   | 0.989     | 0.443    | 0.0    | 0.006 | 0.008 | 0.986     | 0.424    |
| smoothed                                     | 0.003 | 0.02  | 0.025 | 0.995     | 0.478    | 0.002 | 0.014 | 0.017 | 0.993     | 0.457    | 0.001 | 0.009 | 0.011   | 0.989     | 0.443    | 0.0    | 0.006 | 0.008 | 0.987     | 0.425    |
| $\lambda_X=0.4, \alpha_Y=5 - b_2 + d_2=0.8$  |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.003 | 0.015 | 0.019 | 0.993     | 0.376    | 0.001 | 0.011 | 0.013 | 0.99      | 0.344    | 0.0   | 0.007 | 0.008   | 0.986     | 0.33     | 0.0    | 0.005 | 0.006 | 0.984     | 0.324    |
| smoothed                                     | 0.003 | 0.015 | 0.019 | 0.993     | 0.374    | 0.001 | 0.011 | 0.013 | 0.99      | 0.344    | 0.0   | 0.007 | 0.008   | 0.986     | 0.331    | 0.0    | 0.005 | 0.006 | 0.984     | 0.324    |
| $\lambda_X=0.4, \alpha_Y=8 - b_2 + d_2=0.72$ |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.001 | 0.009 | 0.011 | 0.991     | 0.217    | 0.001 | 0.006 | 0.008 | 0.989     | 0.201    | 0.0   | 0.004 | 0.005   | 0.983     | 0.197    | 0.0    | 0.003 | 0.004 | 0.98      | 0.196    |
| smoothed                                     | 0.002 | 0.009 | 0.011 | 0.991     | 0.218    | 0.001 | 0.006 | 0.008 | 0.989     | 0.201    | 0.0   | 0.004 | 0.005   | 0.983     | 0.196    | 0.0    | 0.003 | 0.004 | 0.98      | 0.197    |
| $\lambda_X=0.5, \alpha_Y=2 - b_2 + d_2=1.0$  |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.013 | 0.068 | 0.092 | 0.995     | 1.74     | 0.006 | 0.048 | 0.062 | 0.993     | 1.611    | 0.002 | 0.029 | 0.038   | 0.994     | 1.473    | 0.002  | 0.021 | 0.027 | 0.993     | 1.501    |
| smoothed                                     | 0.01  | 0.066 | 0.089 | 0.995     | 1.661    | 0.005 | 0.047 | 0.061 | 0.994     | 1.57     | 0.001 | 0.029 | 0.037   | 0.995     | 1.451    | 0.002  | 0.021 | 0.026 | 0.993     | 1.483    |
| $\lambda_X=0.5, \alpha_Y=3 - b_2 + d_2=0.83$ |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.006 | 0.037 | 0.047 | 0.991     | 0.888    | 0.003 | 0.026 | 0.032 | 0.988     | 0.846    | 0.001 | 0.016 | 0.02    | 0.986     | 0.79     | 0.0    | 0.011 | 0.014 | 0.979     | 0.783    |
| smoothed                                     | 0.005 | 0.036 | 0.046 | 0.992     | 0.852    | 0.003 | 0.025 | 0.032 | 0.989     | 0.83     | 0.001 | 0.016 | 0.02    | 0.986     | 0.781    | 0.0    | 0.011 | 0.014 | 0.979     | 0.778    |
| $\lambda_X=0.5, \alpha_Y=4 - b_2 + d_2=0.75$ |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.004 | 0.025 | 0.032 | 0.987     | 0.611    | 0.002 | 0.018 | 0.022 | 0.981     | 0.587    | 0.001 | 0.011 | 0.014   | 0.979     | 0.546    | 0.001  | 0.008 | 0.009 | 0.977     | 0.52     |
| smoothed                                     | 0.003 | 0.025 | 0.031 | 0.988     | 0.596    | 0.002 | 0.018 | 0.022 | 0.981     | 0.575    | 0.001 | 0.011 | 0.014   | 0.979     | 0.542    | 0.0    | 0.008 | 0.009 | 0.977     | 0.517    |
| $\lambda_X=0.5, \alpha_Y=5 - b_2 + d_2=0.7$  |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.003 | 0.019 | 0.024 | 0.984     | 0.454    | 0.001 | 0.013 | 0.017 | 0.982     | 0.441    | 0.001 | 0.008 | 0.01    | 0.977     | 0.409    | 0.0    | 0.006 | 0.007 | 0.97      | 0.404    |
| smoothed                                     | 0.002 | 0.019 | 0.024 | 0.984     | 0.445    | 0.001 | 0.013 | 0.017 | 0.983     | 0.436    | 0.001 | 0.008 | 0.01    | 0.977     | 0.407    | 0.0    | 0.006 | 0.007 | 0.97      | 0.403    |
| $\lambda_X=0.5, \alpha_Y=8 - b_2 + d_2=0.62$ |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.002 | 0.011 | 0.014 | 0.981     | 0.257    | 0.001 | 0.008 | 0.01  | 0.979     | 0.248    | 0.0   | 0.005 | 0.006   | 0.972     | 0.232    | 0.0    | 0.003 | 0.004 | 0.969     | 0.231    |
| smoothed                                     | 0.002 | 0.011 | 0.014 | 0.981     | 0.253    | 0.001 | 0.008 | 0.01  | 0.98      | 0.245    | 0.0   | 0.005 | 0.006   | 0.972     | 0.23     | 0.0    | 0.003 | 0.004 | 0.969     | 0.23     |
| $\lambda_X=0.6, \alpha_Y=2 - b_2 + d_2=0.9$  |       |       |       |           |          |       |       |       |           |          |       |       |         |           |          |        |       |       |           |          |
| standard                                     | 0.015 | 0.092 | 0.125 | 0.984     | 2.353    | 0.007 | 0.062 | 0.083 | 0.985     | 2.102    | 0.003 | 0.04  | 0.052   | 0.984     | 2.042    | 0.001  | 0.028 | 0.036 | 0.981     | 1.958    |
| smoothed                                     | 0.007 | 0.088 | 0.118 | 0.984     | 2.141    | 0.003 | 0.061 | 0.08  | 0.985     | 1.98     | 0.002 | 0.04  | 0.051</ |           |          |        |       |       |           |          |

|  |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
|--|--------|-------|-------|-------|-------|--------|-------|-------|-------|-------|--------|-------|-------|-------|-------|--------|-------|-------|-------|-------|
| standard                                     | 0.002  | 0.013 | 0.016 | 0.972 | 0.304 | 0.001  | 0.009 | 0.011 | 0.968 | 0.29  | 0.0    | 0.006 | 0.007 | 0.965 | 0.277 | 0.0    | 0.004 | 0.005 | 0.962 | 0.272 |
| smoothed                                     | 0.001  | 0.013 | 0.016 | 0.972 | 0.295 | 0.0    | 0.009 | 0.011 | 0.969 | 0.284 | 0.0    | 0.006 | 0.007 | 0.965 | 0.274 | 0.0    | 0.004 | 0.005 | 0.962 | 0.27  |
| $\lambda_X=0.7, \alpha_Y=2 - b_2 + d_2=0.8$  |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.015  | 0.121 | 0.173 | 0.964 | 3.077 | 0.008  | 0.084 | 0.114 | 0.971 | 2.961 | 0.001  | 0.054 | 0.071 | 0.966 | 2.696 | 0.0    | 0.038 | 0.049 | 0.964 | 2.62  |
| smoothed                                     | 0.002  | 0.115 | 0.164 | 0.964 | 2.745 | -0.0   | 0.082 | 0.11  | 0.971 | 2.686 | -0.003 | 0.053 | 0.07  | 0.966 | 2.532 | -0.002 | 0.037 | 0.048 | 0.965 | 2.502 |
| $\lambda_X=0.7, \alpha_Y=3 - b_2 + d_2=0.63$ |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.006  | 0.056 | 0.074 | 0.965 | 1.362 | 0.004  | 0.04  | 0.051 | 0.966 | 1.306 | 0.001  | 0.025 | 0.032 | 0.959 | 1.256 | 0.0    | 0.018 | 0.022 | 0.958 | 1.225 |
| smoothed                                     | 0.001  | 0.054 | 0.07  | 0.964 | 1.256 | 0.001  | 0.039 | 0.05  | 0.967 | 1.23  | -0.0   | 0.025 | 0.032 | 0.96  | 1.209 | -0.0   | 0.018 | 0.022 | 0.959 | 1.188 |
| $\lambda_X=0.7, \alpha_Y=4 - b_2 + d_2=0.55$ |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.004  | 0.037 | 0.047 | 0.962 | 0.869 | 0.001  | 0.025 | 0.032 | 0.961 | 0.804 | 0.001  | 0.016 | 0.02  | 0.958 | 0.784 | 0.0    | 0.011 | 0.014 | 0.958 | 0.777 |
| smoothed                                     | 0.001  | 0.036 | 0.045 | 0.963 | 0.814 | -0.0   | 0.025 | 0.032 | 0.962 | 0.764 | -0.0   | 0.016 | 0.02  | 0.958 | 0.761 | -0.0   | 0.011 | 0.014 | 0.958 | 0.759 |
| $\lambda_X=0.7, \alpha_Y=5 - b_2 + d_2=0.5$  |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.003  | 0.027 | 0.035 | 0.96  | 0.629 | 0.001  | 0.019 | 0.024 | 0.96  | 0.612 | 0.0    | 0.012 | 0.015 | 0.958 | 0.577 | 0.0    | 0.009 | 0.011 | 0.951 | 0.585 |
| smoothed                                     | 0.001  | 0.026 | 0.034 | 0.962 | 0.596 | 0.0    | 0.019 | 0.024 | 0.961 | 0.583 | -0.0   | 0.012 | 0.015 | 0.959 | 0.56  | 0.0    | 0.008 | 0.011 | 0.951 | 0.575 |
| $\lambda_X=0.7, \alpha_Y=8 - b_2 + d_2=0.43$ |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.001  | 0.015 | 0.019 | 0.958 | 0.35  | 0.001  | 0.011 | 0.013 | 0.957 | 0.343 | 0.0    | 0.007 | 0.008 | 0.957 | 0.32  | 0.0    | 0.005 | 0.006 | 0.954 | 0.316 |
| smoothed                                     | 0.0    | 0.015 | 0.019 | 0.959 | 0.332 | 0.0    | 0.01  | 0.013 | 0.957 | 0.329 | 0.0    | 0.007 | 0.008 | 0.957 | 0.313 | -0.0   | 0.005 | 0.006 | 0.954 | 0.312 |
| $\lambda_X=0.8, \alpha_Y=2 - b_2 + d_2=0.7$  |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.006  | 0.153 | 0.222 | 0.935 | 3.716 | -0.002 | 0.112 | 0.161 | 0.93  | 3.673 | -0.001 | 0.074 | 0.106 | 0.932 | 3.644 | -0.002 | 0.053 | 0.073 | 0.919 | 3.711 |
| smoothed                                     | -0.014 | 0.147 | 0.208 | 0.931 | 3.28  | -0.015 | 0.109 | 0.154 | 0.927 | 3.339 | -0.008 | 0.072 | 0.102 | 0.929 | 3.356 | -0.007 | 0.053 | 0.071 | 0.918 | 3.422 |
| $\lambda_X=0.8, \alpha_Y=3 - b_2 + d_2=0.53$ |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.004  | 0.068 | 0.091 | 0.943 | 1.678 | 0.001  | 0.049 | 0.063 | 0.947 | 1.593 | 0.0    | 0.031 | 0.04  | 0.942 | 1.551 | -0.0   | 0.022 | 0.028 | 0.938 | 1.517 |
| smoothed                                     | -0.004 | 0.066 | 0.087 | 0.942 | 1.525 | -0.003 | 0.048 | 0.061 | 0.946 | 1.46  | -0.002 | 0.031 | 0.039 | 0.943 | 1.464 | -0.002 | 0.022 | 0.027 | 0.939 | 1.442 |
| $\lambda_X=0.8, \alpha_Y=4 - b_2 + d_2=0.45$ |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.003  | 0.043 | 0.056 | 0.946 | 0.998 | 0.002  | 0.03  | 0.039 | 0.951 | 0.998 | -0.0   | 0.019 | 0.025 | 0.943 | 0.937 | -0.0   | 0.014 | 0.017 | 0.943 | 0.919 |
| smoothed                                     | -0.001 | 0.042 | 0.054 | 0.946 | 0.915 | -0.001 | 0.03  | 0.038 | 0.951 | 0.929 | -0.001 | 0.019 | 0.024 | 0.945 | 0.892 | -0.001 | 0.014 | 0.017 | 0.945 | 0.885 |
| $\lambda_X=0.8, \alpha_Y=5 - b_2 + d_2=0.4$  |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.002  | 0.031 | 0.04  | 0.948 | 0.732 | 0.001  | 0.022 | 0.028 | 0.948 | 0.716 | 0.0    | 0.014 | 0.017 | 0.951 | 0.68  | -0.0   | 0.01  | 0.013 | 0.944 | 0.673 |
| smoothed                                     | -0.001 | 0.03  | 0.039 | 0.949 | 0.675 | -0.0   | 0.022 | 0.028 | 0.95  | 0.674 | -0.0   | 0.014 | 0.017 | 0.95  | 0.656 | -0.0   | 0.01  | 0.012 | 0.945 | 0.657 |
| $\lambda_X=0.8, \alpha_Y=8 - b_2 + d_2=0.32$ |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |        |       |       |       |       |
| standard                                     | 0.001  | 0.017 | 0.022 | 0.95  | 0.389 | 0.001  | 0.012 | 0.015 | 0.954 | 0.379 | -0.0   | 0.008 | 0.01  | 0.95  | 0.361 | 0.0    | 0.005 | 0.007 | 0.949 | 0.37  |
| smoothed                                     | -0.0   | 0.017 | 0.021 | 0.952 | 0.362 | -0.0   | 0.012 | 0.015 | 0.954 | 0.359 | -0.0   | 0.007 | 0.009 | 0.95  | 0.349 | -0.0   | 0.005 | 0.007 | 0.949 | 0.359 |