PlanetsHW3

November 4, 2020

1 ASTR 5490 Homework 3

```
[36]: # Import relevant modules/packages
      import numpy as np
      import matplotlib.pyplot as plt
      from astropy import units as u
      from astropy import constants as const
      from astropy.timeseries import LombScargle
      from PeriodicityTools import Periodicity
      from GrazingTransit import GrazingTransit
      from LimbDarkening import LimbDarkening
      from Spectra import SpectralFeatures, Accuracy
      from MathTools import Gaussian, NonRelDoppler
      from TransitPlotter import LightCurveCompare
      from Batman import BatmanModel
      # Reload PeriodicityTools to acknowledge changes made in the script
      %load_ext autoreload
      %autoreload 2
```

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

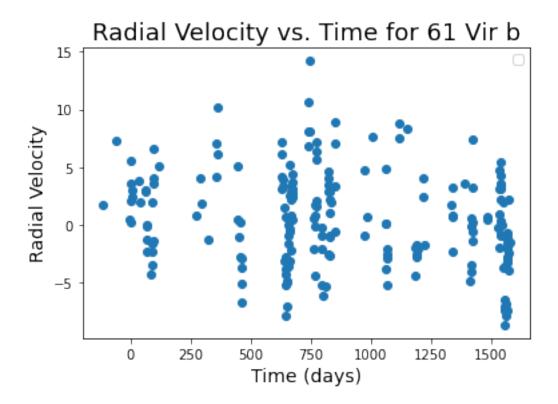
2 1) Exploring Radial Velocity Curve of 61 Vir b from Vogt et al. (2009)

2.0.1 https://iopscience.iop.org/article/10.1088/0004-637X/708/2/1366#apj330338s2

```
[9]: # Create instance of class
Virb = Periodicity('Vogt2009_61Virb_vels.dat','61 Vir b',None)

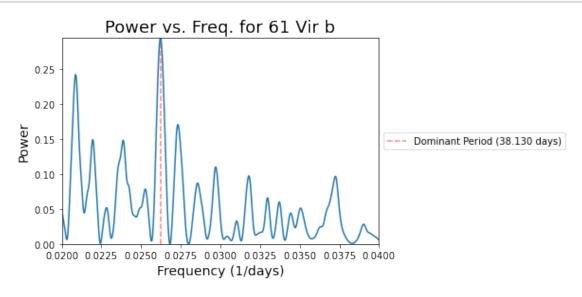
# Generate light curve for data
times,RVs,errors = Virb.LightCurve(curve='Radial Velocity')
```

No handles with labels found to put in legend.



2.1 1a) Make a periodogram of the whole dataset

```
[45]: # Make a Lomb Scargle Periodogram of the data original_maxPower = Virb.LS(25,50,1000,1,flux=[],plot=True)
```



- 2.1.1 Looks quite similar to upper panel of Vogt et al. Figure 3, but my x-axis is the inverse of their's so mine's not exactly the same. I find the same as they do (38.13 d)
- 2.2 1b) Compute the false alarm probability considering the 38 day planet
- 2.2.1 The F.A.P. is defined as "the fraction of trials for which the periodogram power exceeds the observed value" (Page 3 of Cumming 2004 https://academic.oup.com/mnras/article/354/4/1165/1052087)

```
[15]: fap = Virb.FAP(10000)
```

FAP = 0.000e+00

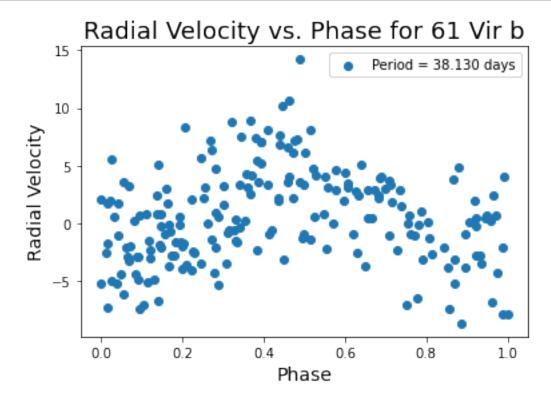
2.3 1c) Fold the RV data at the period determined from the periodogram

```
[47]: Virb_folded = Periodicity('Vogt2009_61Virb_vels.dat','61 Vir b',None,period=38.

→13)

new_times,new_RVs,new_errors = Virb_folded.

→LightCurve(xaxis='Phase',curve='Radial Velocity')
```



2.4 1d) Pick a _____ interval and find the FAP

2.4.1 i) contiguous 100d

```
[13]: # Find FAP over first 100 days of data

Virb_contig = Periodicity('Vogt2009_61Virb_vels.dat','61 Vir b',100,period=38.

→13)

contiguous_fap = Virb_contig.FAP(10000)
```

FAP = 0.000e+00

2.4.2 ii) sparsed 100d

```
[14]: # Find FAP using first 50 and last 50 days of data

Virb_sparsed = Periodicity('Vogt2009_61Virb_vels.dat','61 Viru

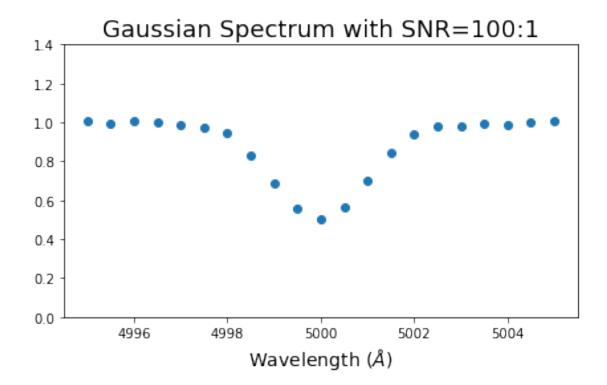
b',50,contiguous=False,period=38.13)

sparsed_FAP = Virb_sparsed.FAP(10000)
```

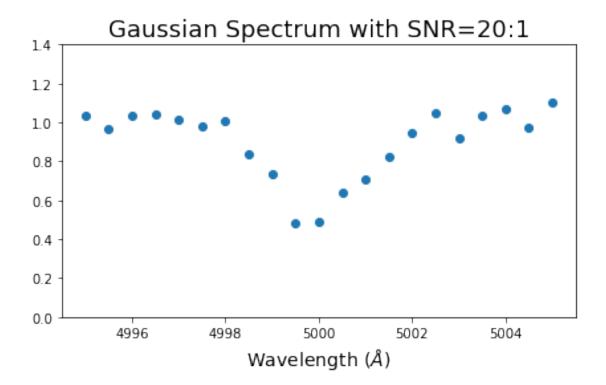
FAP = 0.000e+00

- 2.4.3 My calculated FAP for each method of splicing the data was 0 and I ran them all for 10000 Monte Carlo iterations so the FAP must be $\leq 10^{-4}$. This indicates a high probability ($\geq 99.99\%$) of this being a true planet detection
- 3 2) Investigating Gaussian absorption lines
- 3.1 2a) Generate Gaussian absorption line for normalized spectrum with: A = 0.5, $\sigma = 1$ angs. centered at 5000 angs. with pixels every 0.5 angs.

```
[3]: # Gaussian spectrium with SNR=100:1
SNR_100 = SpectralFeatures(5000.0,1.0,0.5,0.0,1.0,0.5,100)
x,y_100 = SNR_100.GaussianNoise()
```



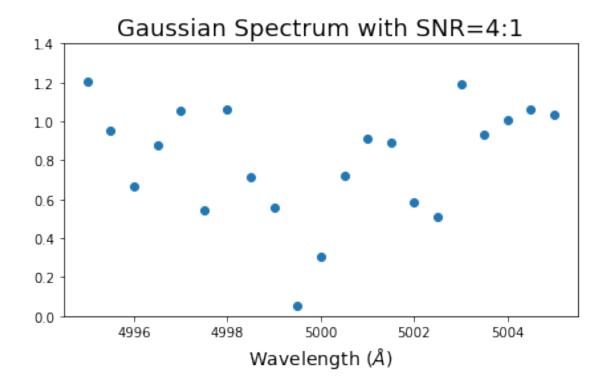
```
[4]: # Gaussian spectrium with SNR=20:1
SNR_20 = SpectralFeatures(5000.0,1.0,0.5,0.0,1.0,0.5,20)
x,y_20 = SNR_20.GaussianNoise()
```



```
[5]: # Gaussian spectrium with SNR=4:1

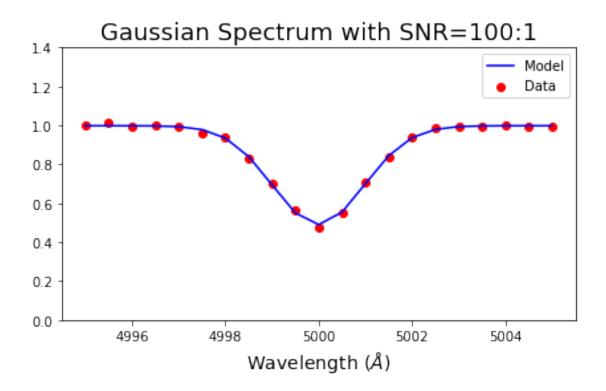
SNR_4 = SpectralFeatures(5000.0,1.0,0.5,0.0,1.0,0.5,4)

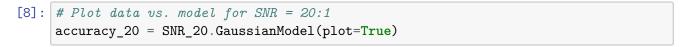
x,y_4 = SNR_4.GaussianNoise()
```

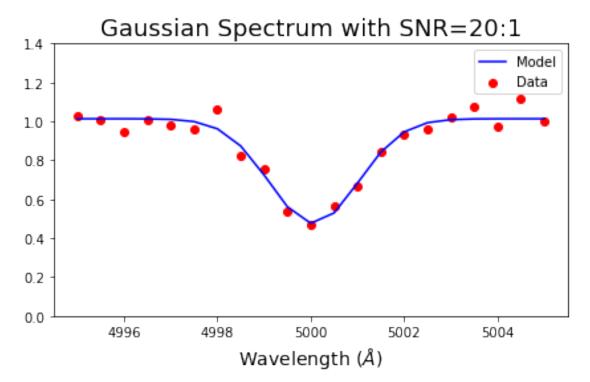


3.2 2a) Use curve_fit to fit Gaussian to noisy data from 2a. Plot accuracy of the center of the profile (mean) vs. SNR

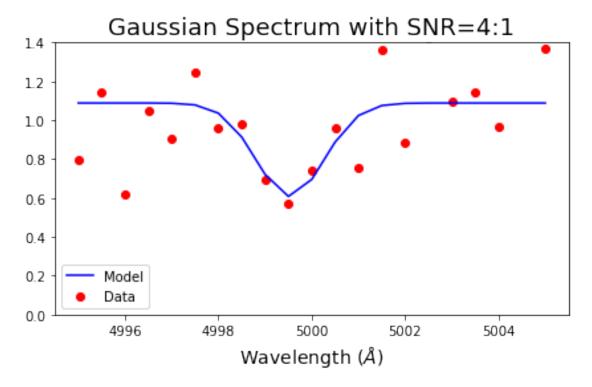
```
[6]: # Plot data vs. model for SNR = 100:1
accuracy_100 = SNR_100.GaussianModel(plot=True)
```





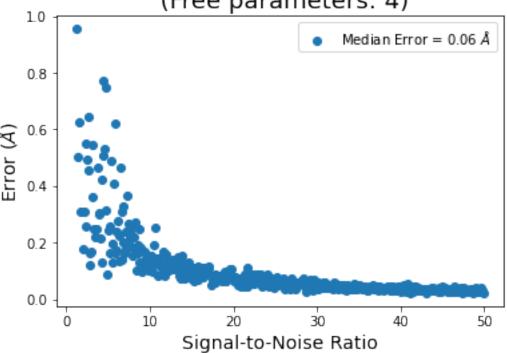


```
[10]: # Plot data vs. model for SNR = 4:1
accuracy_4 = SNR_4.GaussianModel(plot=True)
```



```
[48]: # Make list of SNRs and empty list of accuracies
SNRs = np.arange(1,50,.1)
Accuracy(4,SNRs)
```

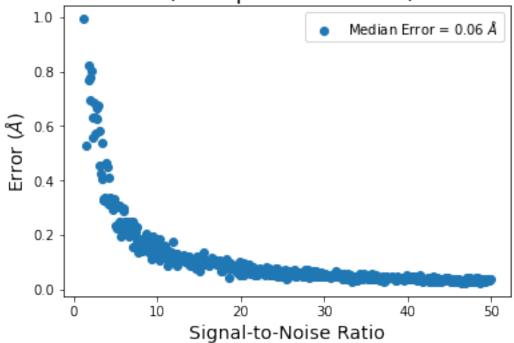
Accuracy of Model vs. SNR (Free parameters: 4)



3.3 2c) Repeat 2b for the mean being the only free parameter

[49]: Accuracy(1,SNRs)

Accuracy of Model vs. SNR (Free parameters: 1)

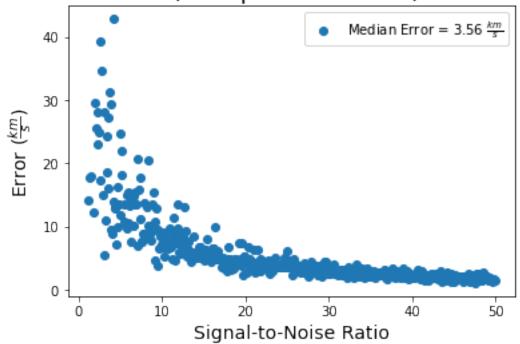


 $3.4\,$ 2d) Convert accuracy in angs to km/s for 2b and 2c (using non-relativistic Doppler Eqn.)

3.4.1
$$\lambda' = \lambda_0 \left(1 + \frac{v}{c_0} \right) -> v = c_0 \left(\frac{\lambda'}{\lambda_0} - 1 \right)$$

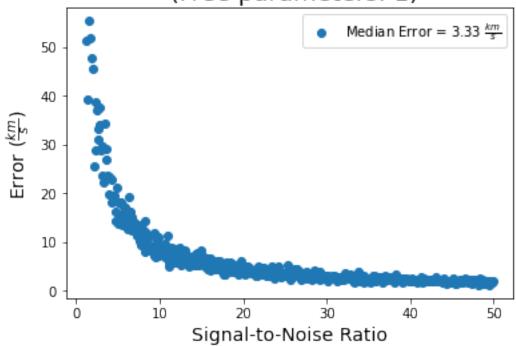
[51]: Accuracy(4,SNRs,'km/s')

Accuracy of Model vs. SNR (Free parameters: 4)

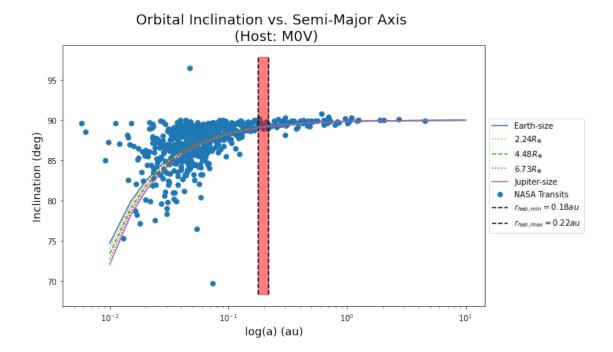


[52]: Accuracy(1,SNRs,'km/s')

Accuracy of Model vs. SNR (Free parameters: 1)



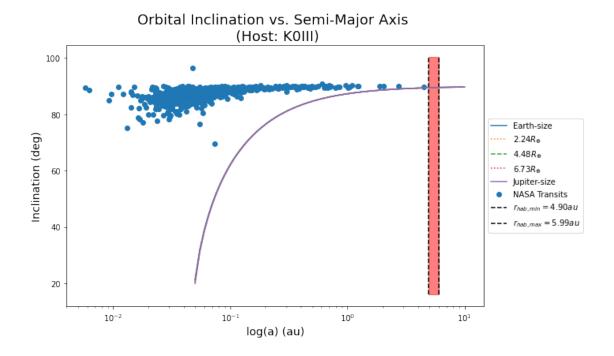
- 3.4.2 Models agree much better for data sets with higher SNR. Once SNR > 30, model doesn't fit significantly better if SNR keeps getting better (increasing). Models also agree better when you fit less free parameters (less deviation this way)
- 3.5 2e) What mass planet could you detect if you have $N=10^1, 10^2, 10^3$ absorption lines? Remember that accuracy improves as \sqrt{N} (so $\frac{accuracy}{\sqrt{N}}$)
- **3.5.1** For N=10: $\sqrt{10}\approx 3.16$ $-> acc. \approx 1.10\frac{km}{s}=1110\frac{m}{s}$ -> detect $M_p>10^{28.5}kg\approx 16.6M_{Jup}$
- **3.5.2** For $N=10^2$: $\sqrt{10^2}=10$ -> $acc. \approx 0.34 \frac{km}{s}=340 \frac{m}{s}$ -> \det $\det M_p > 10^{28} kg \approx 5.26 M_{Jup}$
- **3.5.3** For $N=10^3$: $\sqrt{10^3}\approx 31.6$ -> $acc.\approx 0.10\frac{km}{s}=100\frac{m}{s}$ -> detect $M_p>10^{27.5}kg\approx 1.66M_{Jup}$
- 4 3) Plot of orbital inclination vs. semi-major axis with lines corresponding to grazing transit for planets from Earth to Jupitersize. Also shading approx. habitable zone.
- 4.1 Grazing transit
- **4.1.1** i) Impact parameter (b): b = acos(i)
- **4.1.2** ii) Grazing condition: $b = acos(i) \le R_p + R_*$
- **4.2 3a)** MOV (dwarf) Host Star: $T_{eff} = 3870K$; $R_* = .559R_{\odot}$
- 4.3 3b) K0III (giant) Host Star: $T_{eff} = 4810K, R_* = 10R_{\odot}$ (couldn't find exact radius)
- $4.3.1 \quad Property \ source: \ http://www.pas.rochester.edu/{\sim}emamajek/EEM_dwarf_UBVIJHK_colored to the control of the contro$
- [4]: # Plot grazing transits and habitable zone for MOV star
 MOV = GrazingTransit('M')
 MOV.InclinationSemiMajor()



4.3.2 It is well within observational limits to observe an Earth to Jupiter size planet in the habitable zone of an M0V star with the transit method. Many transit detections published in the NASA Exoplanet Archive fall in this detection range.

```
[5]: # Plot grazing transits and habitable zone for MOV star
KOIII = GrazingTransit('K')
KOIII.InclinationSemiMajor()
```

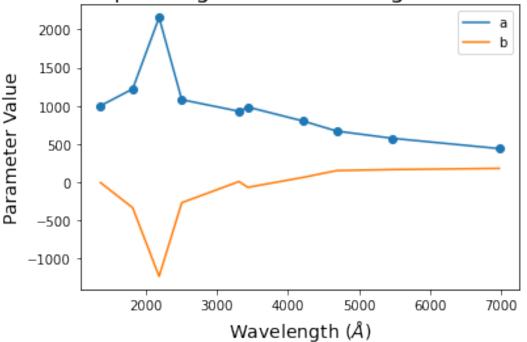
/d/users/jimmy/Documents/ASTR5490/HW3/GrazingTransit.py:56: RuntimeWarning:
invalid value encountered in arccos
 def InclinationSemiMajor(self):



- 4.3.3 It seems just beyond observational limits to observe an Earth to Jupiter size planet in the habitable zone of a K0III star with the transit method. There are a few transit detections published in the NASA Exoplanet Archive that lie near this detection range, but none lie within it. In both plots we see a bias in transit detections of high-inclination exoplanets likely because the exoplanet occults more of the star's light when the system is ege-on w.r.t Earth. We don't see a transit if the system is at a low inclination (i.e. face on) so it's not surprising that most transit detections have high inclinations.
- 5 4) Simulate a star as a solid face-on disk by breaking the stellar surface into a grid of 1000x1000 square pixels
- 5.1 4a) Assign each pixel a surface brightness with 1.0 at the center. Use quadratic limb darkening tables-Van Hamme (1993)-to assign a relative brightness to other pixels. Assume G2V star with $T_{eff}=5500K$ and $\lambda_{obs}=5000$ angs
- 5.1.1 Van Hamme (1993): https://ui.adsabs.harvard.edu/abs/1993AJ....106.2096V/abstract
- 5.1.2 Source for log(g) of dwarf (V) stars: http://www.astro.sunysb.edu/metchev/PHY521/lecture
- **5.2** Q.L.D.: $I(\mu) = I(0) [1 a(1 \mu) b(1 \mu)^2]$
- 5.3 Substituting for μ : $I(\mu) = I(0) \left[1 a \left(1 \sqrt{\frac{R_*^2 r^2}{R_*^2}} \right) b \left(1 \sqrt{\frac{R_*^2 r^2}{R_*^2}} \right)^2 \right]$ where a is the radius of the disc and r is the distance from the center of the disc (guidance from http://orca.phys.uvic.ca/~tatum/stellatm/atm6.pdf)
- 5.4 I'm sourcing a and b from Table 5 on the 10th page of Wade & Rucinski (1985): http://articles.adsabs.harvard.edu/pdf/1985A%26AS...60..471W

[57]: <matplotlib.legend.Legend at 0x7fc85429eeb8>

Extrapolating Limb Darkening Parameters



5.4.1 In range of 5000 angs., the relationship for both parameters seems pretty linear so I'll use a linear extrapolation to find a and b at 5000 angs

```
[58]: # List indexes of lambdas that lie above and below 5000 angs.
min_index = 7
max_index = 8

# Define sublists of points below and above point of interest
a_sub = [a_list[min_index],a_list[max_index]]
b_sub = [b_list[min_index],b_list[max_index]]
lambdas_sub = [lambdas[min_index],lambdas[max_index]]

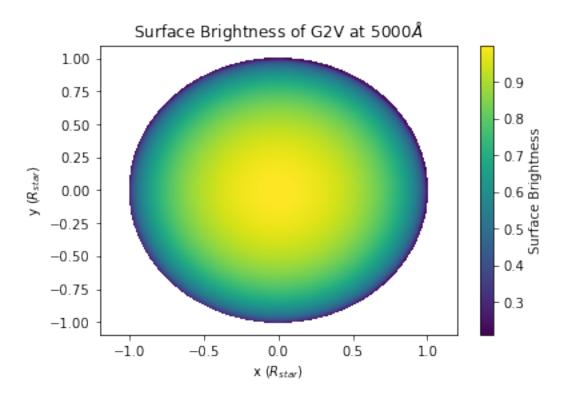
# Interpolate to find proper values at 5000 angs
a_new = np.interp(5000,lambdas_sub,a_sub)
b_new = np.interp(5000,lambdas_sub,b_sub)
print(a_new,b_new)
```

633.2652284263959 159.56091370558374

```
[59]: # Use LimbDarkening function to plot surface of G2V star
star = LimbDarkening(633.27/1000,159.56/1000)
x,y,intensities = star.Star(1000)
```

/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:36: RuntimeWarning: invalid value encountered in sqrt

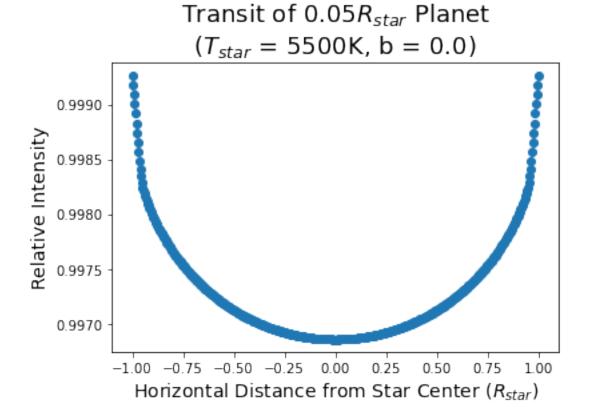
 $mu = np.sqrt(1-abs(r**2/R_star**2))$



5.5 4b) Plot light curve of transit of $.05R_{star}$ at impact parameter 0

```
[10]: star_b = LimbDarkening(5500,500)
[27]: star_b.Transit(0.05,0.0,False)
```

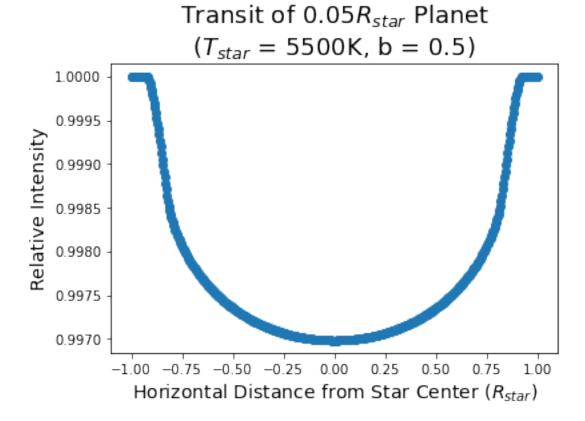
My program took 240.88 seconds to run



5.6 4c) Plot light curve of transit of $.05R_{star}$ at impact parameter 0.5

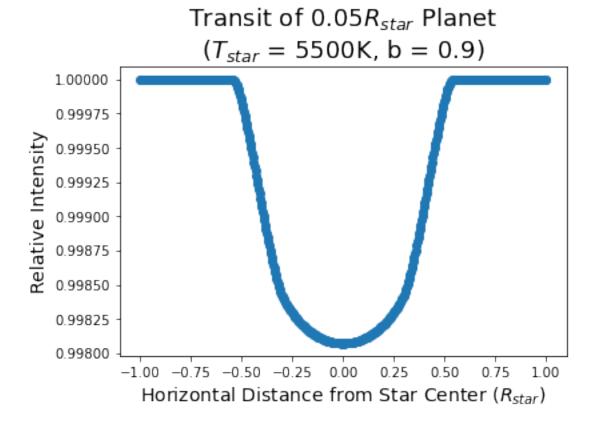
[11]: star_b.Transit(0.05,0.5,False)

My program took 3.75 minutes to run



5.7 4d) Plot light curve of transit of $.05R_{star}$ at impact parameter 0.9 (grazing transit)

My program took 3.84 minutes to run



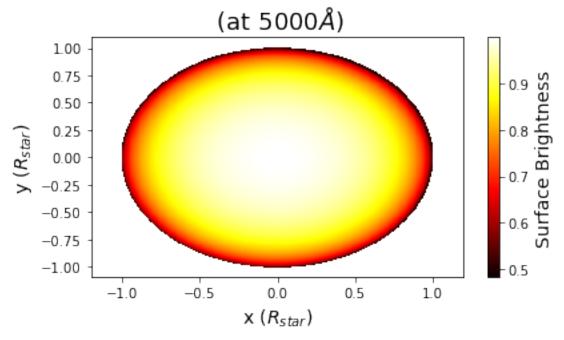
- 5.8 4e) Overplot on the plots for B/C/D the light curve for a T=10,000~K host star and a 3600 K host star and summarize the differences
- 5.8.1 For 10000K, got parameters from: First two rows at relevant temp. in Table 3 of Claret (2013) http://cdsarc.u-strasbg.fr/ftp/cats/J/A+A/552/A16/ori/Table3

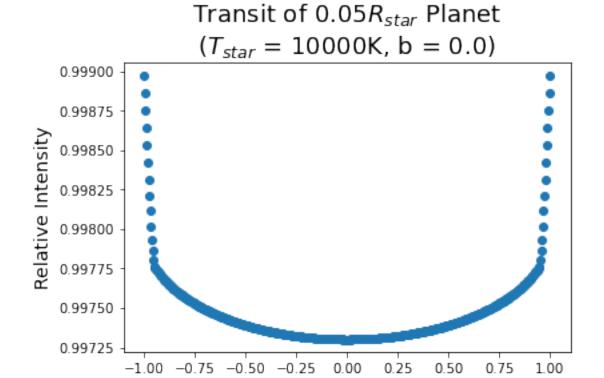
```
[13]: star_10000K = LimbDarkening(10000,500)

[30]: # impact parameter = 0
    star_10000K.Star(plot=True)
    star_10000K.Transit(0.05,0.0,False)
```

My program took 4.87 minutes to run

Surface Brightness of T=10000K Star





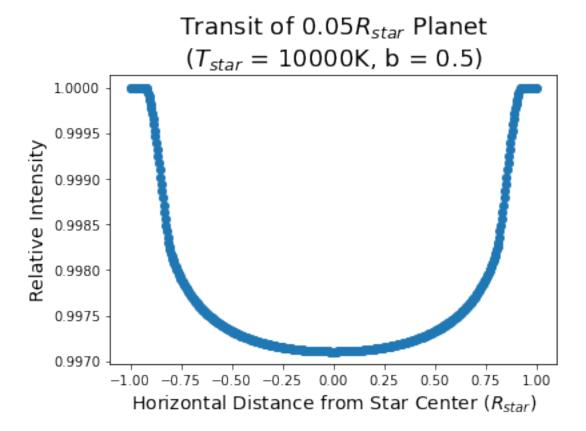
0.50

0.25

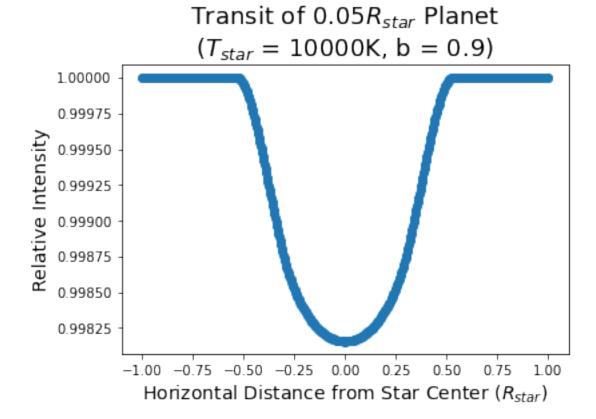
Horizontal Distance from Star Center (R_{star})

```
[31]: # impact parameter = 0.5
star_10000K.Transit(0.05,0.5,False)
```

My program took 4.15 minutes to run



My program took 4.15 minutes to run



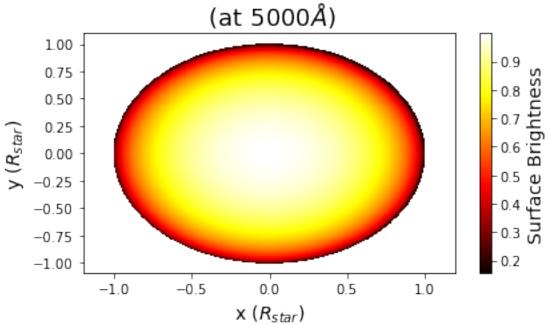
5.8.2 For \mathbf{got} parameters from: Column 10 filter) 3600K, https://cdsarc.unistra.fr/vizof **Table** $\mathbf{2}$ from Claret (1998)bin/ReadMe/J/A+A/335/647?format=html&tex=true

```
[14]: star_3600K = LimbDarkening(3600,500)

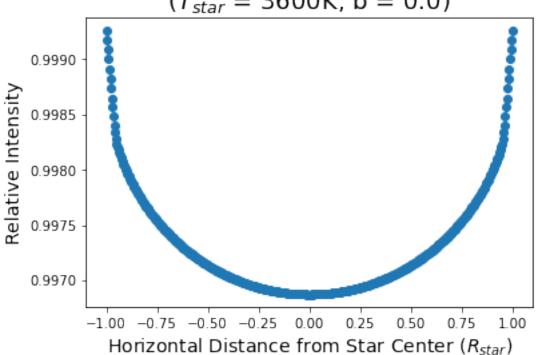
[35]: # impact parameter = 0
star_3600K.Star(plot=True)
star_3600K.Transit(0.05,0.0,False)
```

My program took 4.13 minutes to run

Surface Brightness of T=3600K Star

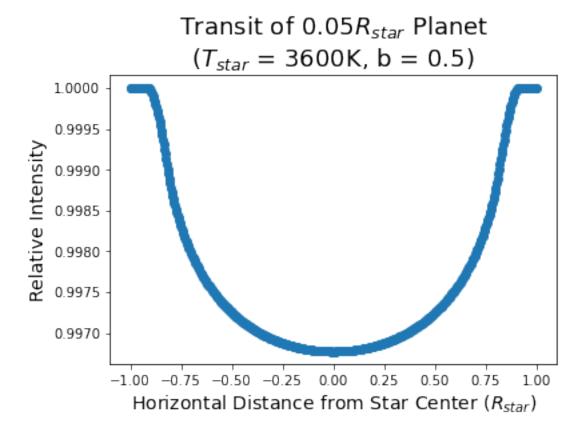


Transit of $0.05R_{star}$ Planet $(T_{star} = 3600K, b = 0.0)$

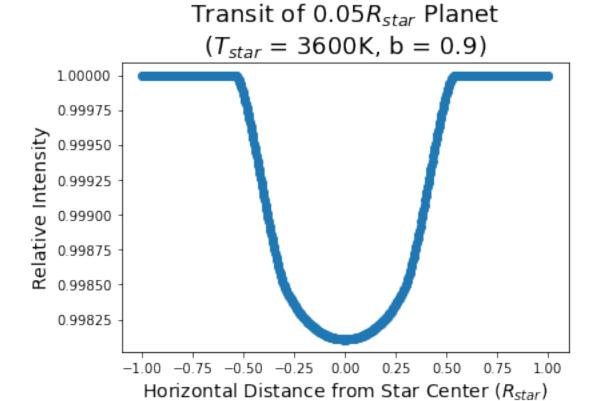


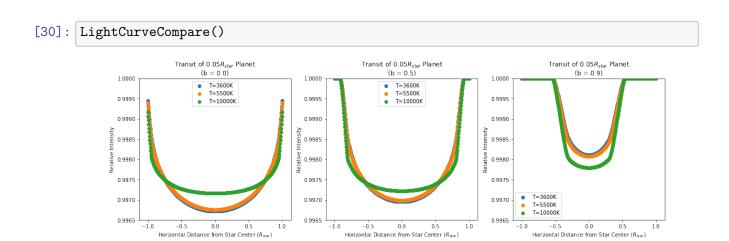
```
[36]: # impact parameter = 0.5
star_3600K.Transit(0.05,0.5,False)
```

My program took 4.20 minutes to run



My program took 3.74 minutes to run





- 5.9 4f) Comparing result from 4c (b=0.5) to results from Kreidberg 2015 who used 'batman'
- 5.9.1 Figure 2 of Kreidberg 2015 https://iopscience.iop.org/article/10.1086/683602/pdf
- 5.9.2 My plots are very similar qualititavely with the same wide U-shaped curve with flat edges at the beginning and end of the transit. Quantitatively, my model dooes not dip as low as Kreidberg (0.997 for mine, 0.990 for theirs). Overall, I'd say my model replicates theirs quite well. For b=0, my code stars when the planet is just on the edge which is why there's no horizontal lines at the top of the transit 'well' in this case.
- 6 5) Now let your star rotate with an equatorial velocity of $v_R = 10 \frac{km}{s}$. The projected radial velocity of each surface element is a function of stellar latitude ϕ and longitude θ

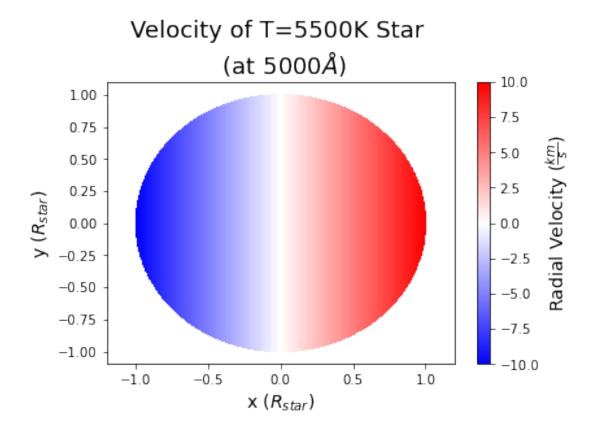
```
##
v_{rad} = v_R sin\theta cos\phi
```

Using your pixelated numerical star surface code, 6.1 5a) produce intensity-weighted velocity profile plot \mathbf{for} $ext{the}$ transit. also known the rotational velocity $\mathbf{a}\mathbf{s}$ profile (in the following, I use conventions define in Table 1 here https://en.wikipedia.org/wiki/Del in cylindrical and spherical coordinates)

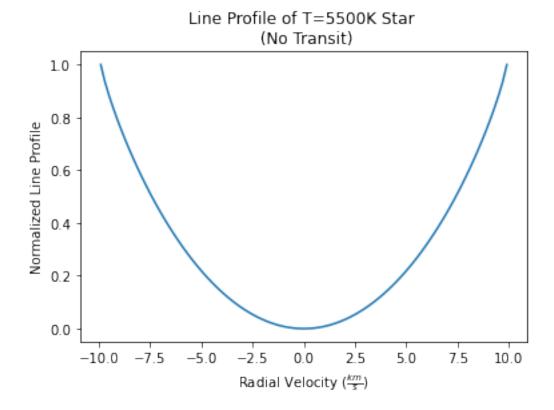
```
##
\theta = \arctan\left(\frac{\sqrt{x^2 + y^2}}{z}\right), \ \phi = \arctan\left(\frac{y}{x}\right)
##
v_{rad} = v_R \sin\left(\arctan\left(\frac{\sqrt{x^2 + y^2}}{\sqrt{R_{star}^2 - x^2 - y^2}}\right)\right) \cos\left(\arctan\left(\frac{y}{x}\right)\right)
```

```
[5]: # Tests of class and functions within the class
RotatingStar = LimbDarkening(5500,1000)
RotatingStar.RVProfile(plot='star')
```

```
/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:53: RuntimeWarning:
invalid value encountered in sqrt
  mu = np.sqrt(1-abs(r**2/R_star**2))
/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:213: RuntimeWarning:
invalid value encountered in sqrt
  theta = np.sqrt((x**2+y**2)/(1.0-x**2-y**2))
```



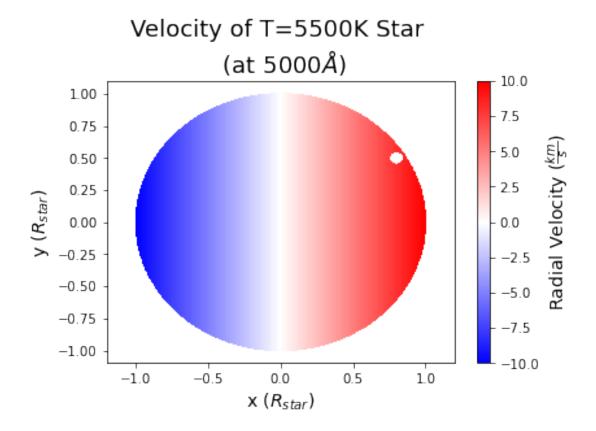
[6]: RotatingStar.RVProfile(plot='profile')



- 6.2 5b) Produce the same proifle for the star for when the planet is at four different positions across the disk of the star at an impact parameter of b=0.5
- 6.3 5c) Plot the difference between the 5a and 5b plots. Compare quantitatively to those in Figure 1 of Gaudia & Winn (2007, ApJ).
- 6.4 https://ui.adsabs.harvard.edu/abs/2007ApJ...655..550G/abstract

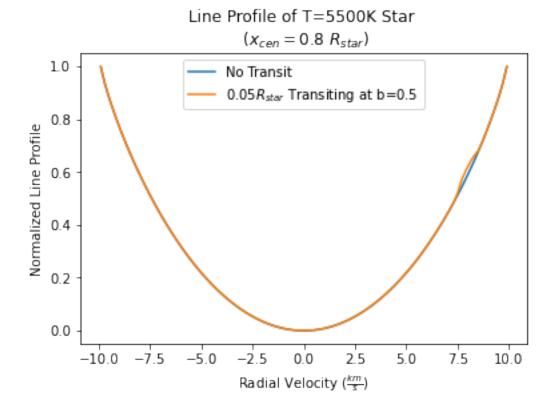
```
[10]: RotatingStar.RVProfileTransit(x_center=0.8,plot='star')

/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:53: RuntimeWarning:
   invalid value encountered in sqrt
      mu = np.sqrt(1-abs(r**2/R_star**2))
   /d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:213: RuntimeWarning:
   invalid value encountered in sqrt
      theta = np.sqrt((x**2+y**2)/(1.0-x**2-y**2))
```



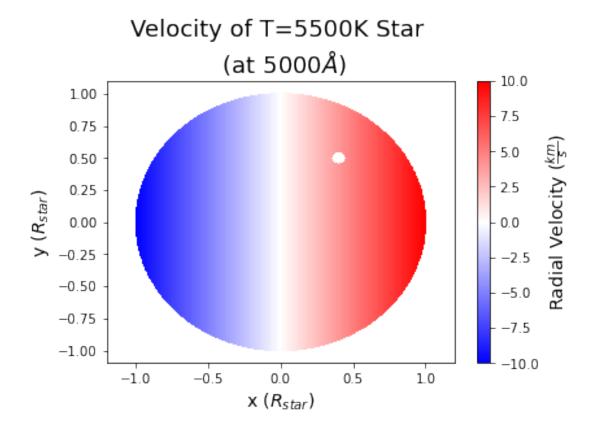
```
[14]: RotatingStar.RVProfileTransit(x_center=0.8,plot='profile')
```

```
/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:53: RuntimeWarning:
invalid value encountered in sqrt
  mu = np.sqrt(1-abs(r**2/R_star**2))
/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:213: RuntimeWarning:
invalid value encountered in sqrt
  theta = np.sqrt((x**2+y**2)/(1.0-x**2-y**2))
```

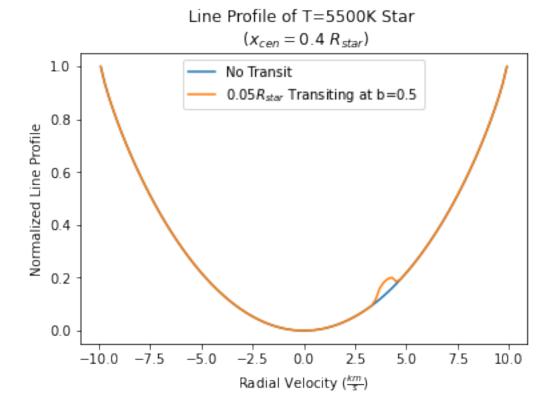


```
[15]: RotatingStar.RVProfileTransit(x_center=0.4,plot='star')

/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:53: RuntimeWarning:
invalid value encountered in sqrt
    mu = np.sqrt(1-abs(r**2/R_star**2))
/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:213: RuntimeWarning:
invalid value encountered in sqrt
    theta = np.sqrt((x**2+y**2)/(1.0-x**2-y**2))
```

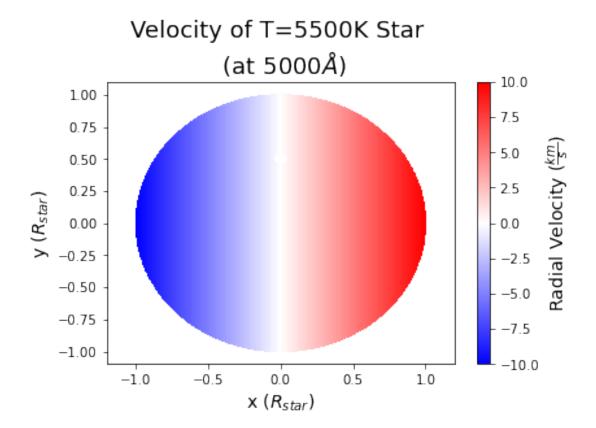


[16]: RotatingStar.RVProfileTransit(x_center=0.4,plot='profile')

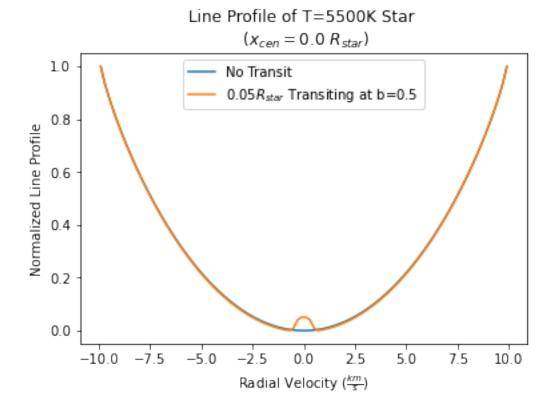


```
[17]: RotatingStar.RVProfileTransit(x_center=0.0,plot='star')

/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:53: RuntimeWarning:
   invalid value encountered in sqrt
      mu = np.sqrt(1-abs(r**2/R_star**2))
   /d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:213: RuntimeWarning:
   invalid value encountered in sqrt
      theta = np.sqrt((x**2+y**2)/(1.0-x**2-y**2))
```

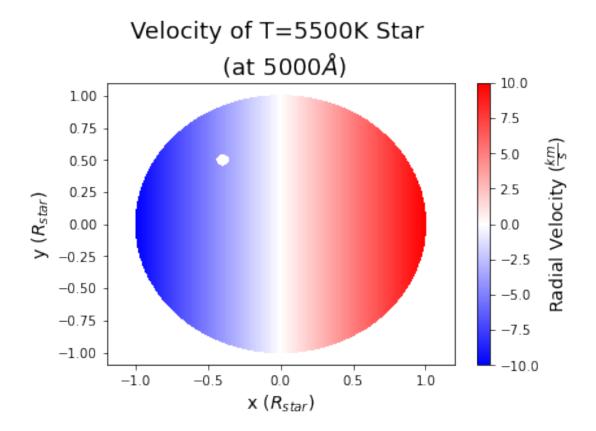


[18]: RotatingStar.RVProfileTransit(x_center=0.0,plot='profile')



```
[19]: RotatingStar.RVProfileTransit(x_center=-.4,plot='star')

/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:53: RuntimeWarning:
invalid value encountered in sqrt
    mu = np.sqrt(1-abs(r**2/R_star**2))
/d/users/jimmy/Documents/ASTR5490/HW3/LimbDarkening.py:213: RuntimeWarning:
invalid value encountered in sqrt
    theta = np.sqrt((x**2+y**2)/(1.0-x**2-y**2))
```



[20]: RotatingStar.RVProfileTransit(x_center=-.4,plot='profile')

Line Profile of T=5500K Star $(x_{cen} = -0.4 R_{star})$ 1.0 No Transit $0.05R_{star}$ Transiting at b=0.5 0.8 Normalized Line Profile 0.6 0.4 0.2 0.0 -7.5-5.0-2.50.0 2.5 5.0 7.5 10.0 -10.0Radial Velocity (km)

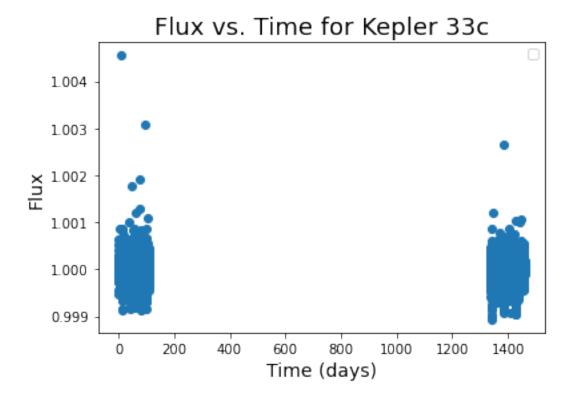
- 6.5 My plots are qualitatively very similar to those in Gaudi & Winn (2007, ApJ). My plots only include when the planet is just out-of-transit and fully in-transit so I don't have the zero-slope edges at the top-right and top-left of my plots like they do.
- period 6) Fold Kepler 33 data at of Use 'batman' light Planet C. curve tool (https://www.cfa.harvard.edu/~lkreidberg/batman/tutorial.html) light transit the fit curve \mathbf{to} data and \mathbf{a} replanet parameters from Lissauer \mathbf{et} al. (2012;https://ui.adsabs.harvard.edu/abs/2012ApJ...750..112L/abstract)
- 7.1 Raw Light Curve (chose subset of phase interval to zoom in on dip)

```
[4]: # Initialize my Periodicity class and plot the light curve
Kepler33c = Periodicity('Kepler33.dat','Kepler

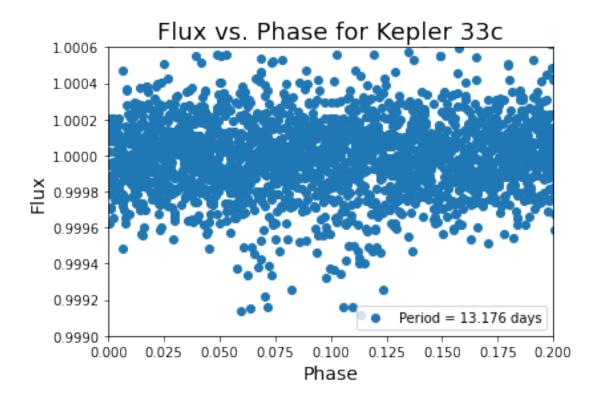
→33c',['col0','col1','col2'],5000,contiguous='Bookend',period=13.17562)

[5]: time,rel_flux,err = Kepler33c.LightCurve(plot=True,xaxis='Time')
```

No handles with labels found to put in legend.



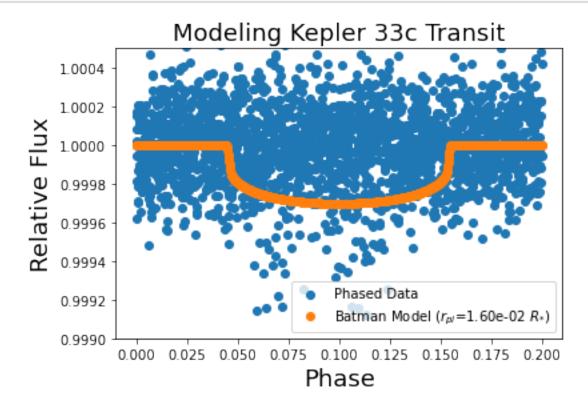
[6]: phase,rel_flux,err = Kepler33c.LightCurve(plot=True,xaxis='Phase')



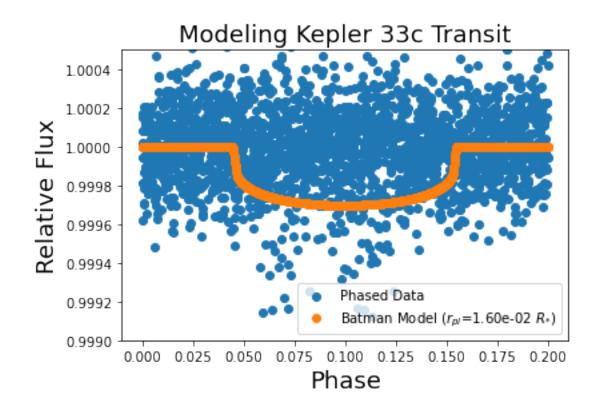
```
[37]: # Using actual parameters from paper
      batman_time_actual,batman_flux_actual,rad_pl_actual = BatmanModel(P=13.
       \rightarrow17562,rad_pl=0.01602,a=13.8,i=88.19,e=0.2,w=0.0,coeff=[0.4899, 0.
       \rightarrow1809],plot=False)
[38]: # Cut real data to zoom in on transit
      phase_cut = [(i,x) for (i,x) in enumerate(phase) if x <= 0.2]</pre>
      cuts = [x[0] for x in phase_cut]
      phase_cuts = [x[1] for x in phase_cut]
      rel_flux_cuts = []
      for index in cuts:
          flux = rel_flux[index]
          rel_flux_cuts.append(flux)
      def BatmanCompare(xdata,ydata,rad_pl):
          # Plot real phased data and Batman model
          fig,ax = plt.subplots()
          ax.scatter(phase_cuts,rel_flux_cuts,label='Phased Data')
          ax.scatter(xdata,ydata,label=r'Batman Model ($r_{pl}$=%.2e $R_{*}$)'%rad_pl)
          ax.get_yaxis().get_major_formatter().set_useOffset(False)
          ax.set_ylim(0.999,1.0005)
          ax.set_xlabel('Phase',fontsize=18)
          ax.set_ylabel('Relative Flux',fontsize=18)
```

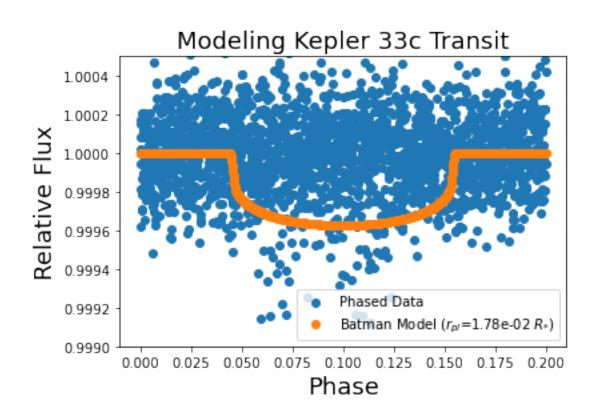
```
ax.set_title('Modeling Kepler 33c Transit',fontsize=18)
ax.legend()
```

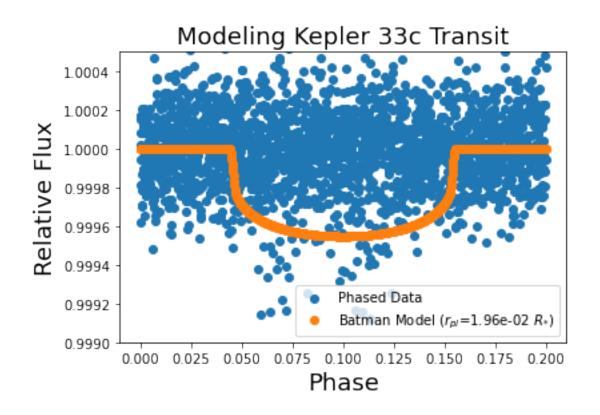
[39]: BatmanCompare(batman_time_actual,batman_flux_actual,rad_pl_actual)

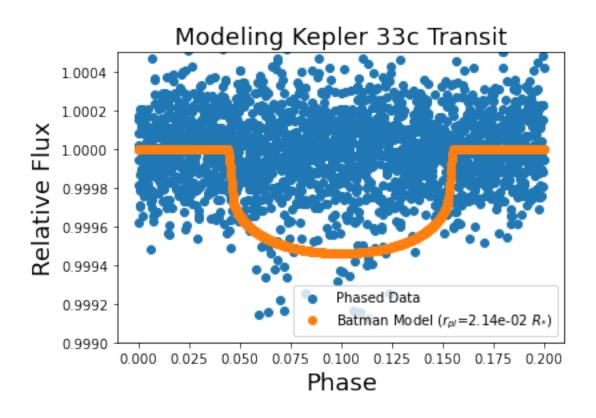


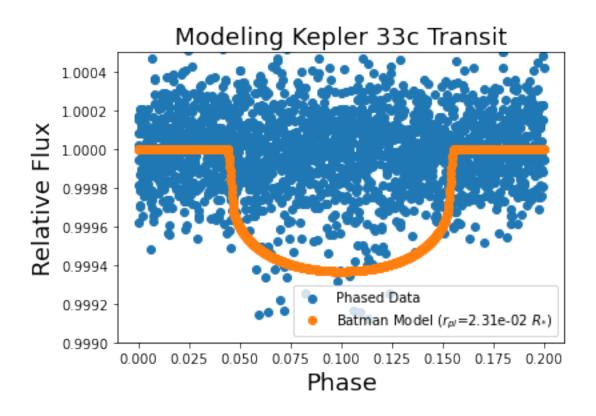
7.1.1 Actual radius from paper doesn't look like it quite fits. I'll try looping over radii to test better versions

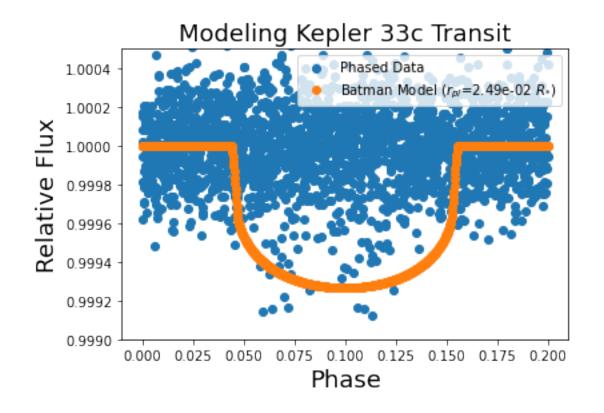


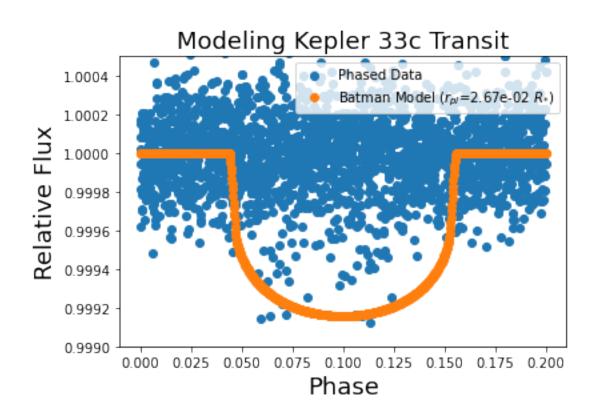


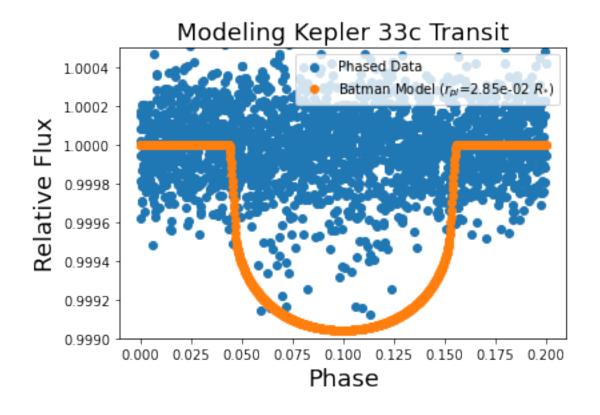


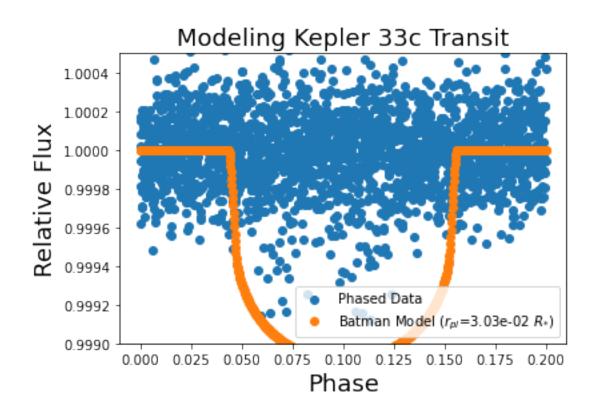


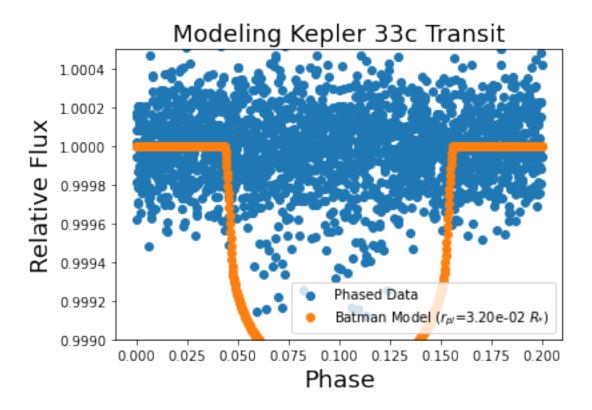


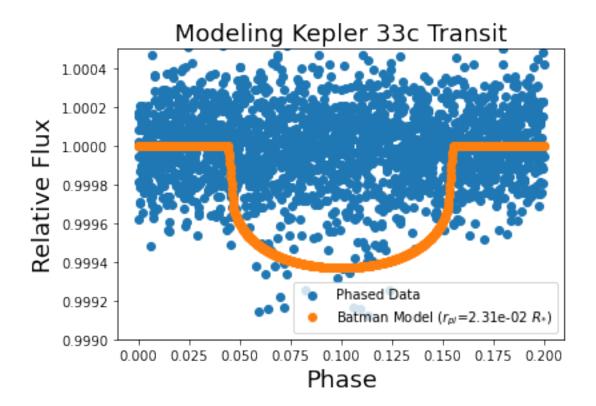












7.1.2 My best-fit used a radius of $0.0231R_*$ which is 1.44 times greater than the published value of $0.01602R_*$. Not bad at all!