At each step:
$$\vec{E}_i = \vec{r} - \vec{r}_i'$$

$$\vec{r}_i = \vec{r} - \vec{r}_i'$$

$$\vec{E}(\vec{r}) = \int_{z'=-R}^{R} \int_{z'=0}^{\sqrt{R^2 - z_i'^2}} \int_{\theta'=0}^{2\pi} \left(k \, \frac{\rho(\vec{r}_i') \, (\varrho_i' \mathrm{d}\theta_i' \, \mathrm{d}\varrho_i' \, \mathrm{d}z_i')}{\left|\left|\vec{r}_i\right|\right|^2} \, \hat{r}_i \right)$$