



# Robust estimation of fundamental frequency positive-sequence component for grid-integration applications in energy systems

Hafiz Ahmed, Rosane Ushirobira, Denis Efimov

## ► To cite this version:

Hafiz Ahmed, Rosane Ushirobira, Denis Efimov. Robust estimation of fundamental frequency positive-sequence component for grid-integration applications in energy systems. The 5th International Conference on Renewable Energy and Environment Engineering, Aug 2022, Brest, France. hal-03766158

**HAL Id: hal-03766158**

**<https://inria.hal.science/hal-03766158>**

Submitted on 31 Aug 2022

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Robust estimation of fundamental frequency positive-sequence component for grid-integration applications in energy systems

Hafiz Ahmed<sup>a\*</sup>, Rosane Ushirobira<sup>b</sup>, Denis Efimov<sup>b</sup>

<sup>a</sup> Nuclear Futures Institute, Bangor University, Bangor LL57 1UT, UK

<sup>b</sup> Inria, Univ. Lille, CNR, UMR 9189 CRISTAL, F-59000 Lille, France

---

## Abstract

This article studies the problem of fundamental frequency positive-sequence component separation in unbalanced three-phase systems for grid-integration applications. We propose a simple-to-implement approach involving a modified delayed signal cancellation method and moving average filtering. A delay-based linear-regression framework is considered to make the sequence component separation frequency-adaptive, providing fast and accurate frequency estimation. Comparative experimental results demonstrate the suitability of the proposed method over conventional approaches.

© 2022 Hafiz Ahmed. Published by Elsevier Ltd.

Peer-review under responsibility of the scientific committee of the 5th International Conference on Renewable Energy and Environment Engineering (REEE 2022)

**Keywords:** Sequence estimation; unbalanced voltage; delayed signal cancellation

---

## 1. Introduction

Fast and accurate separation of sequence components is essential for controlling converters operating in an unbalanced grid [1]-[9]. It motivated the development of numerous grid-synchronizing sequence component separation methods. Most approaches are built around the traditional synchronous reference frame phase-locked loop (SRF-PLL) [10].

Delayed signal cancellation (DSC) [11] is a popular choice among the various sequence separation methods available in the literature. This method can be applied either as an in-loop or pre-loop filter in conjunction with SRF-PLL. A DSC with a quarter-cycle delay is suggested in [12] to reject the fundamental frequency negative-sequence component (FFNS). Several modifications are proposed in the literature to speed up the convergence of DSC-based PLL. A modified DSC is proposed in [13], where the required delay is significantly lower than a quarter-cycle. However, this approach requires a pre-loop filter to reduce the effect of noise and harmonics. Another solution is reported in [14], where an additional phase compensator is used in the PLL to speed up the convergence. However, this deteriorates the transient performance in the presence of large voltage sag and/or phase jump. Moreover, numerous parameters also need to be tuned.

---

\* Corresponding author. Tel.: + 441248 382330.; fax: +0-000-000-0000 .  
E-mail address: hafiz.ahmed@bangor.ac.uk

---

In [15], a combination of modified DSC and moving average filter (MAF) is used in conjunction with quasi type-1 PLL (QT1- PLL) [16], [17]. Thanks to the proportional loop-filter of QT1-PLL, this method can significantly decrease the convergence time, however, at the cost of sensitivity to harmonics and noise. A similar hybrid DSC and MAF approach and an open-loop frequency estimator are considered in [18]. However, it is very complicated to implement.

This article proposes applying a modified DSC method for fundamental frequency positive sequence (FFPS) separation. The FFPS component is converted into SRF through demodulation, where MAF enhances harmonic robustness. Finally, the proposed method is made frequency adaptive by considering unknown frequency estimation under a delay-based linear-regression framework [19], [20]. The contributions of this work are twofold. Firstly, the FFPS separation method uses lower delay, resulting in a fast estimation of the sequence components. Secondly, the frequency evaluation is decoupled from the sequence separation, resulting in a fast frequency estimation, unlike conventional methods, which depend on the sequence separation.

The rest of this article is organized as follows: The development of the proposed estimator is given in Section 2, experimental results are provided in Section 3, and finally, concluding remarks are given in Section 4.

## 2. Proposed Estimator Design

Unbalanced three-phase grid voltages with measurement offset in the stationary reference frame are given by:

$$y_{\alpha}(t) = Y_{\alpha 0} + Y^{+} \cos(\omega t + \varphi^{+}) + Y^{-} \cos(\omega t + \varphi^{-}), \quad (1a)$$

$$y_{\beta}(t) = Y_{\beta 0} + Y^{+} \sin(\omega t + \varphi^{+}) - Y^{-} \sin(\omega t + \varphi^{-}), \quad (1b)$$

where the superscript  $+$  and  $-$  denotes the positive and negative sequence,  $\phi^{\pm} = \omega t + \varphi^{\pm}$  is the total phase,  $Y^{\pm}$ ,  $\omega$ ,  $\varphi^{\pm}$ ,  $Y_{\alpha 0}$ , and  $Y_{\beta 0}$  represent the amplitude, angular frequency, phase angle, and DC offsets in phases  $\alpha$  and  $\beta$ , respectively. The extraction of the FFPS component, i.e.,  $y_{\alpha}^{+} = Y^{+} \cos(\omega t + \varphi^{+})$  and  $y_{\beta}^{+} = Y^{+} \sin(\omega t + \varphi^{+})$ , and the estimation of  $\phi^{+}$  are considered in this work. In the remainder of this article, the time-dependence of a signal is often not explicitly stated for convenience. Moreover, continuous- and discrete-time signals and notation of filtered signals are often mixed for brevity.

### 2.1. Separation of FFPS component

The first step in developing the proposed estimator is to separate the FFPS component from (1). For this purpose, the DSC method is a very suitable choice. In the case of unbiased voltage measurement, a traditional  $\alpha\beta$ -DSC operator can separate the FFPS with a delay of  $T/4$ , where  $T$  is the signal period. However, this makes the convergence slower. A modified DSC method is proposed in [13] to overcome this issue. However, as shown in [13, Table 1], the separation of sequences requires many arithmetic operations involving trigonometric quantities. Here, we propose a simplified version that significantly reduces the computational complexity. For this purpose, let us denote that  $y_{\alpha}^{\phi_d} = y_{\alpha}(\phi - \phi_d)$  and  $y_{\beta}^{\phi_d} = y_{\beta}(\phi - \phi_d)$  with  $\phi = \omega t$ ,  $\phi_d = 2\pi f N_d T_s$ , where  $f = \omega/2\pi$  is the frequency,  $N_d$  is the number of delayed samples, and  $T_s$  is the sampling time. Then, the FFPS can be extracted by a modified first-order DSC operation inspired from [15]:

$$\hat{y}_{\alpha}^{+} = \frac{1}{2} (y_{\alpha} + \cot(\phi_d) y_{\beta} - \csc(\phi_d) y_{\beta}^{\phi_d}), \quad (2a)$$

$$\hat{y}_{\beta}^{+} = \frac{1}{2} (y_{\beta} - \cot(\phi_d) y_{\alpha} + \csc(\phi_d) y_{\alpha}^{\phi_d}), \quad (2b)$$

where  $\hat{y}_{\alpha}^{+}$  and  $\hat{y}_{\beta}^{+}$  are the estimated FFPS components. In theory, (2) can extract the FFPS component for any value of  $N_d$ . However, a higher value provides better robustness against harmonic disturbances at the cost of a slow dynamic

response. So,  $N_d = 10$  for  $f = 50\text{Hz}$  ( $f_s = 1/T_s = 10\text{kHz}$ ) can be considered as a good compromise value. To provide additional robustness to grid frequency variation, a two first-order frequency-adaptive DSC operation (2) can be cascaded and this issue is considered in this work.

## 2.2. Phase angle estimation

The FFPS component separation process described in Sec. 2.1 is not very robust to noise and grid harmonics. According to IEEE 519-2014 standard, the total harmonic distortion of the terminal voltage of grid-connected converters should be below 5%, and individual harmonic components should be less than 3%. To respect these limits, moving average filters are considered in this work. To apply these filters, a separated FFPS component is converted to a synchronous reference frame through demodulation and is given by [21]:

$$\begin{bmatrix} \hat{Y}_d^+ \\ \hat{Y}_q^+ \end{bmatrix} = \begin{bmatrix} \cos(\hat{\omega}t) & \sin(\hat{\omega}t) \\ -\sin(\hat{\omega}t) & \cos(\hat{\omega}t) \end{bmatrix} \begin{bmatrix} \hat{y}_\alpha^+ \\ \hat{y}_\beta^+ \end{bmatrix}, \quad (3)$$

$$\begin{bmatrix} \hat{Y}_d^+ \\ \hat{Y}_q^+ \end{bmatrix} = \begin{bmatrix} \hat{Y}^+ \cos(\hat{\phi}^+) \\ \hat{Y}^+ \sin(\hat{\phi}^+) \end{bmatrix}. \quad (4)$$

where  $\hat{\omega}$  is the estimated frequency,  $\hat{Y}_d^+$  and  $\hat{Y}_q^+$  are the estimated FFPS voltages, and  $\hat{Y}^+$  is the estimated FFPS voltage amplitude. In the  $\alpha\beta$  to  $dq$  –frame conversion through (3), the estimated value of the grid frequency  $\hat{\omega}$  is used. Details of the used estimation approach are given in Sec. 2.3. From (4), the phase angle of the FFPS component can be estimated as:

$$\hat{\phi}^+ = \text{atan2}(\hat{Y}_q^+, \hat{Y}_d^+), \quad (5)$$

where  $\text{atan2}$  is the double quadrant arctangent function. To obtain (4), we assume that the grid voltage does not contain any harmonics. However, in practice, the grid voltage contains harmonics. The IEEE 519-2014 standard puts particular emphasis on odd-order harmonics. The presence of odd-order harmonics in the grid voltage will generate even-order AC ripple in the estimated DC quantities  $\hat{Y}_d^+$  and  $\hat{Y}_q^+$ . A MAF can eliminate these even-order harmonics in the  $dq$  –frame with a half-cycle window length. The transfer function of the discrete-time MAF is given by:

$$G_{MAF}(z) = \frac{1}{N_m} \frac{1 - z^{-N_m}}{1 - z^{-1}}, \quad (6)$$

where  $N_m = f_s/2f_n$  is the half-cycle window length with  $f_n$  the nominal frequency. The non-adaptive window length MAF (6) introduces a small-amplitude estimation ripple in the off-nominal grid frequency case. In this work, we consider a frequency-adaptive MAF where fractional delays are implemented through linear interpolation as suggested in [14].

## 2.3. Unknown frequency estimation

In implementing the demodulation (3), an estimate of the unknown grid frequency is required. SRF-based PLLs pass the estimated phase angle through a loop-filter to estimate the grid frequency variation. However, this makes the frequency estimation dependent on the FFPS component separation dynamics. A direct frequency estimation is

considered here to break this loop within a delay-based linear-regression framework. For this purpose, let us consider that for  $n = 1, 2, 3$  [19]:

$$y_{\alpha}^{n\tau}(t) = y_{\alpha}(t - n\tau) \text{ and } y_{\beta}^{n\tau}(t) = y_{\beta}(t - n\tau), \tau > 0. \quad (7)$$

Using the measured grid voltages (1) and delayed versions (7), the following relationships can be obtained [19]:

$$y_{\alpha} - y_{\alpha}^{\tau} + y_{\alpha}^{2\tau} - y_{\alpha}^{3\tau} - 2 \cos(\omega\tau)(y_{\alpha}^{\tau} - y_{\alpha}^{2\tau}) = 0. \quad (8a)$$

$$y_{\beta} - y_{\beta}^{\tau} + y_{\beta}^{2\tau} - y_{\beta}^{3\tau} - 2 \cos(\omega\tau)(y_{\beta}^{\tau} - y_{\beta}^{2\tau}) = 0. \quad (8b)$$

The above equation can be rewritten as the following linear regression model:

$$v_{\alpha} = x_{\alpha}\theta_{\alpha} \text{ and } v_{\beta} = x_{\beta}\theta_{\beta}, \quad (9)$$

where  $v_{\alpha} = y_{\alpha} - y_{\alpha}^{\tau} + y_{\alpha}^{2\tau} - y_{\alpha}^{3\tau}$ ,  $v_{\beta} = y_{\beta} - y_{\beta}^{\tau} + y_{\beta}^{2\tau} - y_{\beta}^{3\tau}$ ,  $x_{\alpha} = 2(y_{\alpha}^{\tau} - y_{\alpha}^{2\tau})$ ,  $x_{\beta} = 2(y_{\beta}^{\tau} - y_{\beta}^{2\tau})$ , and  $\theta_{\alpha} = \theta_{\beta} = \cos(\omega\tau)$ . From the unknown parameters  $\theta_{\alpha}$  and  $\theta_{\beta}$  in (9), the unknown grid frequency  $\omega$  can easily be estimated. The estimates  $\hat{\theta}_{\alpha}$  and  $\hat{\theta}_{\beta}$  can be derived by using the gradient method and is given by:

$$\dot{\hat{\theta}}_{\alpha} = \eta x_{\alpha}(v_{\alpha} - x_{\alpha}\hat{\theta}_{\alpha}), \quad (10a)$$

$$\dot{\hat{\theta}}_{\beta} = \eta x_{\beta}(v_{\beta} - x_{\beta}\hat{\theta}_{\beta}), \quad (10b)$$

where  $\eta > 0$  is the rate control gain. From the estimated unknown parameters, the unknown frequency is evaluated as [19]:

$$\hat{\omega} = \frac{1}{2\tau} \left( \arccos(\hat{\theta}_{\alpha}) + \arccos(\hat{\theta}_{\beta}) \right). \quad (11)$$

According to [22], the exponential convergence of the estimator (10), and consequently, the unknown frequency  $\omega$  can be established if the delay  $\tau$  in (7) is selected to be less than  $\pi/\omega$ . In this work, we consider  $\tau = T_n/4$  with  $T_n$  being the nominal period which satisfies  $\tau < \pi/\omega$ . This value can enhance the convergence speed and reduce the effect of noise and unmodeled disturbances (e.g., harmonics) on the estimated frequency. For real-time implementation, delayed signals in (7) are implemented through delay-shift operator with  $\tau = T_n/4T_s$ . By passing the unknown frequency (11) through an integrator, the unknown total phase of the FFPS component can be evaluated as:

$$\hat{\omega} = \hat{\omega}t + \hat{\varphi}^+. \quad (12)$$

The block diagram of the proposed method is given in Figure 1.

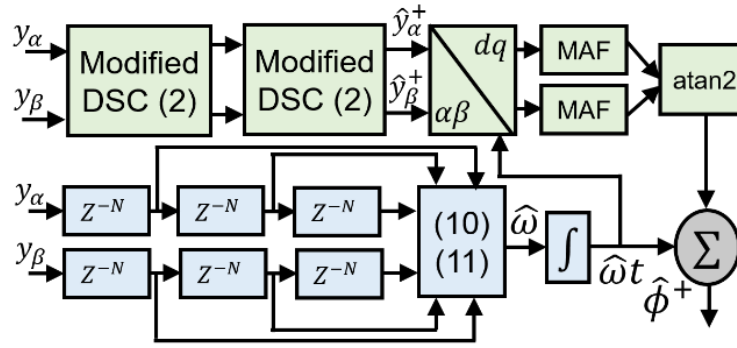


Fig. 1. Block diagram of the proposed method.

### 3. Results and discussions

The experimental setup, shown in Fig. 2, is used to validate the proposed method. Here, a PWM-controlled three-phase inverter is used to emulate the adverse grid voltage signal. Details of the experimental setup can be found in [16]. As comparative techniques, modified DSC-based QT1-PLL [15] and frequency-adaptive MAF-PLL [23] are selected. The proposed and comparative methods all use MAF with half-cycle window length. Parameters of QT1- and MAF-PLLs are selected the same as in [15] and [23]. All the techniques are implemented in Matlab/Simulink with  $T_s = 100\mu\text{sec}$ . for code generation and real-time implementation in dSPACE 1104 platform. The parameters of the proposed method are:  $N_d = 10$ ,  $N_m = f_s/2f$  (nominal), and  $\eta = 35$ . Zero initial conditions are used for implementing all the delay blocks. Results from dSPACE ControlDesk are exported to Matlab for further processing.

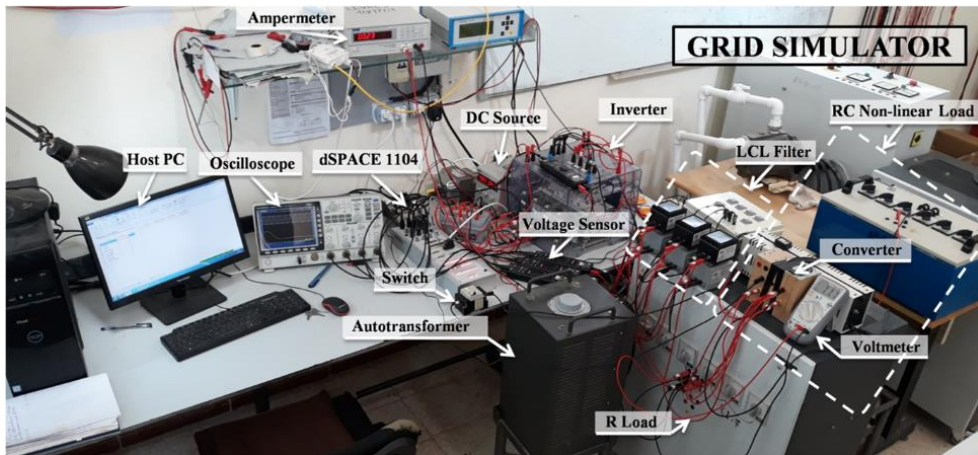
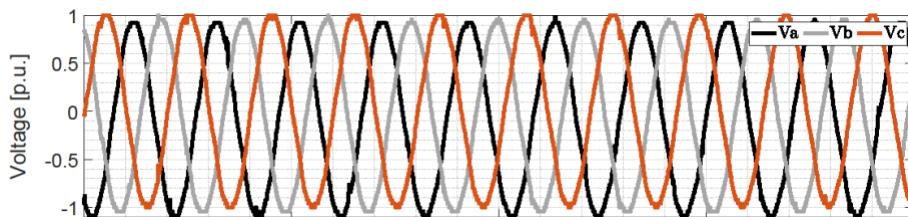


Fig. 2. Test setup [16].



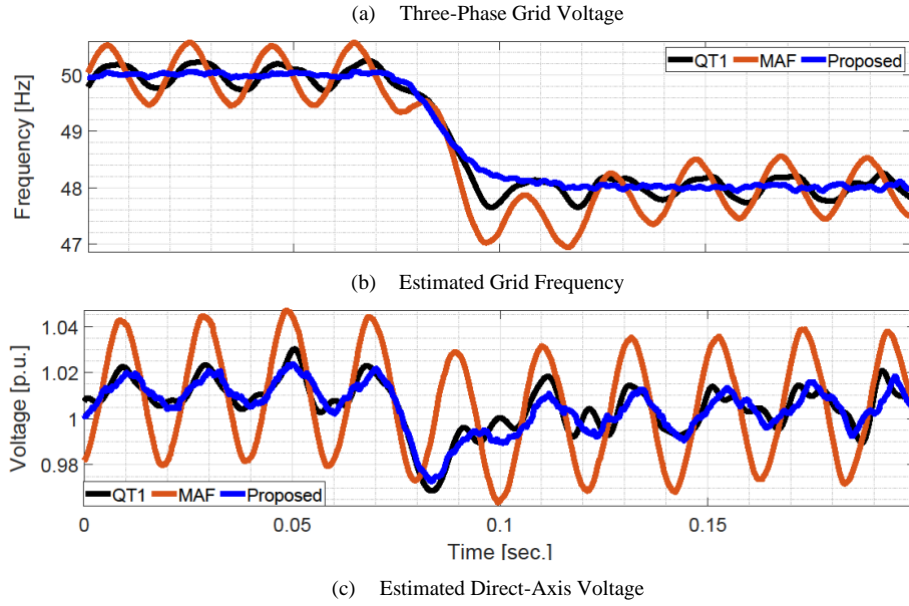
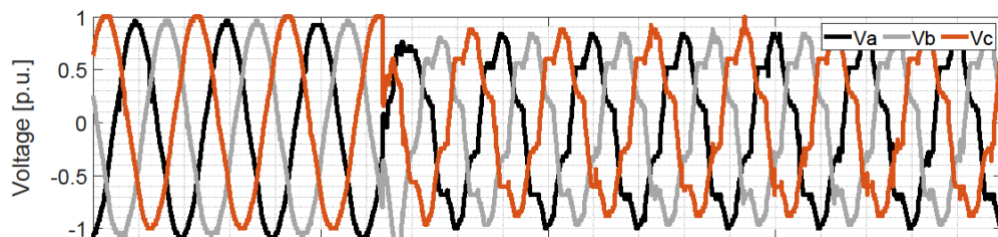


Fig. 3. Comparative experimental results for -2Hz frequency step change.

Two experimental tests are considered. In the first test, a step change of  $-2\text{Hz}$  in frequency is considered and the results are given in Fig. 3. Results in Fig. 3 (b) and (c) show that the proposed method has significantly lower peak to peak overshoot together with fast convergence speed. In the second test, diode-rectifier-based nonlinear load is connected to generate harmonically distorted and unbalanced grid voltage signals. Results in Fig. 4 (b) show that the proposed method has the lowest peak overshoot and the steady-state ripple compared to QT1- and MAF-PLLs. In terms of total harmonic distortion (THD), it can be concluded that the technique developed in this work can significantly lower the THD value, which makes it a suitable tool for control of grid-connected converters. A comparative time domain performance summary is given in Table I.

Table 1. Comparative steady-state performance summary.

Performance Indicators	MAF	QT1	Proposed
Test-I: -2Hz Frequency Step Change			
Frequency ripple (peak-to-peak) (Hz)	1.03	0.48	0.15
Voltage ripple (peak-to-peak) (p.u.)	0.06	0.03	0.02
Test-II: Unbalanced and Distorted Grid			
Frequency ripple (peak-to-peak) (Hz)	1.17	0.58	0.17
Voltage ripple (peak-to-peak) (p.u.)	0.065	0.032	0.023
THD (%) (Grid-15.79%)	0.82	1.22	0.75



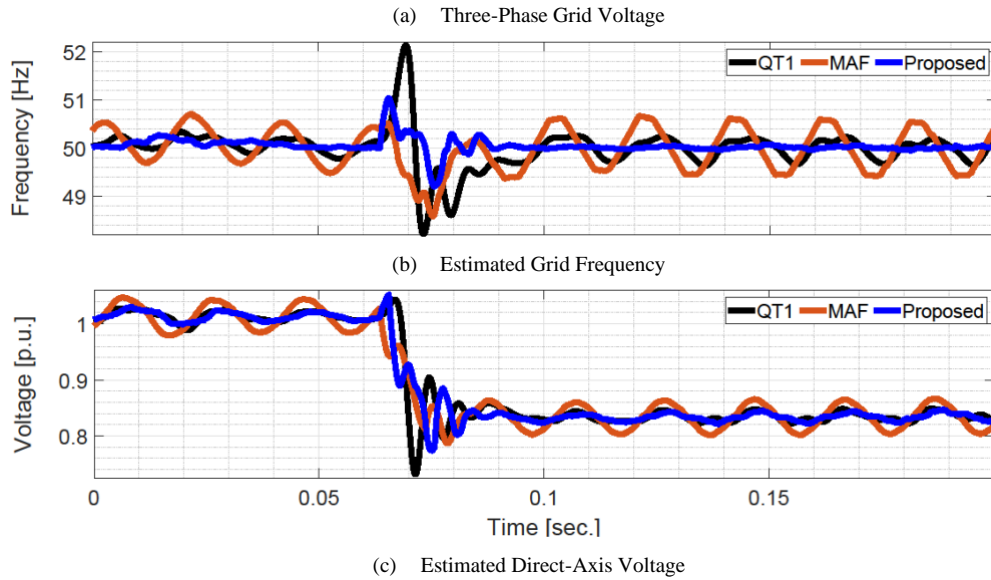


Fig. 4. Comparative experimental results for unbalanced and distorted grid.

#### 4. Conclusion and future works

In this article, an enhanced grid-synchronizing sequence component separation method was proposed, where a modified, delayed signal cancellation method was applied for the sequence separation. Moving average filters working in the synchronous reference frame were implemented to enhance harmonic robustness. Finally, our method was made frequency-adaptive by estimating the unknown grid frequency using gradient estimator under delay-based linear-regression framework. Comparative experimental results show that the FFPS voltage amplitude estimation ripple by the proposed method is at least 50% better than the next best comparative technique.

In this work, we have studied the grid-synchronization problem for grid-connected converters. Extraction of frequency, phase and FFPS components are important for monitoring the transmission power grid. Several issues in the transmission grid, such as decaying offset, transformer saturation, low- and sub-synchronous oscillations, and dynamic change in grid inertia, make the parameter extraction very challenging. These issues will be considered in future work.

#### Acknowledgements

The work of H. Ahmed is funded through the Sêr Cymru II 80761-BU-103 project by Welsh European Funding Office (WEFO) under the European Regional Development Fund (ERDF). The authors greatly acknowledge the contribution of Prof. Zoheir Tir from the University of El Oued, Algeria for his technical support in conducting the experiments.

#### References

- [1] Ishaq, S., Khan, I., Rahman, S., Hussain, T., Iqbal, A. and Elavarasan, R.M. (2022) "A review on recent developments in control and optimization of micro grids." *Energy Reports* 8 (2022): 4085-4103.
- [2] Gawhade, P. and Ojha, A. (2021) "Recent advances in synchronization techniques for grid-tied PV system: A review." *Energy Reports* 7 (2021): 6581-6599.
- [3] Ebrahim, M.A., Aziz, A.B., Nashed, M.N.F. and Osman, F.A. (2022) "Optimal design of controllers and harmonic compensators for three-level cascaded control in stationary reference frame for grid-supporting inverters-based AC microgrid." *Energy Reports* 8 (2022): 860-877.
- [4] Benyamina, F., Benrabah, A., Khoucha, F., Zia, M.F., Achour, Y. and Benbouzid, M. (2021) "Online current limiting-based control to improve fault ride-through capability of grid-feeding inverters." *Electric Power Systems Research* 201 (2021): 107524.



- [5] Benyamina, F., Benrabah, A., Khoucha, F., Zia, M.F., Achour, Y. and Benbouzid, M. (2021) “Online current limiting-based control to improve fault ride-through capability of grid-feeding inverters.” *Electric Power Systems Research* 201 (2021): 107524.
- [6] Celik, D. and Meral, M.E. (2019) “A flexible control strategy with overcurrent limitation in distributed generation systems.” *International Journal of Electrical Power & Energy Systems* 104 (2019): 456–471.
- [7] Celik, D. and Meral, M.E. (2020) “Minimisation of power oscillations with a novel optimal control strategy for distributed generation inverter under grid faulty and harmonic networks.” *IET Renewable Power Generation* 14.15 (2020): 3010–3022.
- [8] Celik, D. and Meral, M.E. (2020) “Voltage support control strategy of grid-connected inverter system under unbalanced grid faults to meet fault ride through requirements.” *IET Generation, Transmission & Distribution* 14.16 (2020): 3198–3210.
- [9] Hassaine, L. and Bengourina, M.R. (2020) “Control technique for single phase inverter photovoltaic system connected to the grid.” *Energy Reports* 7 (2020): 200–208.
- [10] Kaura, V. and Blasko, V. (1997) “Operation of a phase locked loop system under distorted utility conditions.” *IEEE Transactions on Industry Applications* 33.1 (1997): 58–63.
- [11] Sevilmis, F. and Karaca, S. (2022) “Implementation of enhanced non-adaptive cascaded DSC-PLLs for renewable energy systems.” *International Journal of Electrical Power & Energy Systems* 134 (2022): 107470.
- [12] Wang, Y.F. and Li, Y.W. (2010) “Grid synchronization PLL based on cascaded delayed signal cancellation.” *IEEE Transactions on Power Electronics*, 26.7 (2010): 1987–1997.
- [13] Cardenas, R., Rojas, F. and Clare, J. (2014) “Fast convergence delayed signal cancellation method for sequence component separation.” *IEEE Transactions on Power Delivery*, 3.4 (2014): 2055–2057.
- [14] Huang, Q. and Rajashekara, K. (2017) “An Improved Delayed Signal Cancellation PLL for Fast Grid Synchronization Under Distorted and Unbalanced Grid Condition.” *IEEE Transactions on Industry Applications* 53.5 (2017): 4985–4997.
- [15] Mellouli, M.S., Hamouda, M., Slama, J.B.H. and Al Haddad, K. (2021) “A third-order MAF based QT1-PLL that is robust against harmonically distorted grid voltage with frequency deviation.” *IEEE Transactions on Energy Conversions* 36.3 (2021): 1600–1613.
- [16] Ahmed, H., Tir, Z., Verma, A.K., Ben Elghali, S. and Benbouzid, M. (2021) “Quasi Type-1 PLL With Tunable Phase Detector for Unbalanced and Distorted Three-Phase Grid.” *IEEE Transactions on Energy Conversions* (2021), doi: <https://doi.org/10.1109/TEC.2021.3130492>
- [17] Sevilmis, F. and Karaca, S. (2022) “Performance enhancement of DSOGI-PLL with a simple approach in grid-connected applications.” *Energy Reports* 8 (2022): 9–18.
- [18] Verma, A.K., Jarial, R.K., Roncero-Sánchez, P., Ungarala, M.R. and Guerrero, J.M. (2021) “An improved hybrid prefiltered open-loop algorithm for three-phase grid synchronization.” *IEEE Transactions on Industrial Electronics* 68.3 (2021): 2480–2490.
- [19] Ahmed, H., Ushirobira, R. and Efimov, D. (2021) “A Simple Frequency Estimator for Power Systems.” *IEEE Transactions on Instrumentation and Measurement* 70 (2021): 9003902.
- [20] Ahmed, H., Ushirobira, R. and Efimov, D. (2022) “On Biased Harmonic Signal Estimation: Application to Electric Power Grid Monitoring.” *IEEE Transactions on Control Systems Technology* (2022), doi: <https://doi.org/10.1109/TCST.2022.3155322>
- [21] Ahmed, H., Biricik, S. and Benbouzid, M. (2021) “Enhanced frequency adaptive demodulation technique for grid-connected converters.” *IEEE Transactions on Industrial Electronics* 68.11 (2021): 11053–11062.
- [22] Ioannou, P.A. and Sun, J. (1996) “Robust adaptive control”. Upper Saddle River, NJ: PTR Prentice-Hall.
- [23] Mellouli, M.S., Hamouda M. and Slama, J.B.H. (2017) “A comparative study and evaluation of improved MAF-PLL algorithms.” *International Journal of Renewable Energy Research* 7.1 (2017): 88–95.