# Electronics of Radio, Part 1

Notes on David Rutledge's book

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### Basic concepts

- Potential difference  $(V, \phi)$ :  $\phi = \int_a^r E \cdot ds$ , energy per charge, 1V = 1 J/C
- Kirhhoff loop:  $\sum_{loop} V_l = 0$  (Conservation of energy)
- Kirhhoff node:  $\sum_{node} I_i = 0$  (Conservation of charge)
- $V(t) = V_p \cos(\omega t)$ ,  $\omega = 2\pi f$ ,  $I(t) = I_p \cos(\omega t)$ ,  $\omega = 2\pi f$
- Instantaneous power:  $P(t) = V(t)I(t) = V_pI_p \cos^2(\omega t)$
- Average power:  $P_a = \int_0^{1/f} V(t)I(t)dt = \int_0^{2\pi/\omega} V_p I_p \cos^2(\omega t)dt = \frac{V_p I_p}{2}$
- Band names:

Name	Frequency
VLF	3-30kHz
LW	20-300kHz
MW	300kHz-3MHz
HF	3MHz-30MHz
VHF	30-300MHz

Name	Frequency
UHF	300MHz-1GHz
uW	1-30GHz
milliW	30-300GHz
submilliF	>300GHz

### Resistors, capacitors, inductors













#### Resistors

- Analytic model: IR = V
- Energy dissipated:  $E = \int_{t_i}^{t_f} IV \, dt = \int_{t_i}^{t_f} I^2 R dt$
- Capacitors
  - Analytic model: CV = q,  $C\frac{dV}{dt} = i$
  - Capacitor Energy stored:  $E = \int_{t_i}^{t_f} CV \frac{dV}{dt} dt = \frac{1}{2} CV^2$
- Inductors
  - Analytic model:  $V = L \frac{di}{dt}$
  - Inductor Energy stored:  $E = \int_{t_i}^{t_f} IV \, dt = \int_{t_i}^{t_f} LI \frac{dI}{dt} \, dt = \frac{1}{2} LI^2$
  - Open air:  $L(H)=\mu_0Kn^2\frac{A}{l}$ , distances in meters,  $\mu_0=4\pi\times 10^{-7}$ , K=1



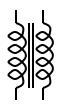
## Diodes, transformers

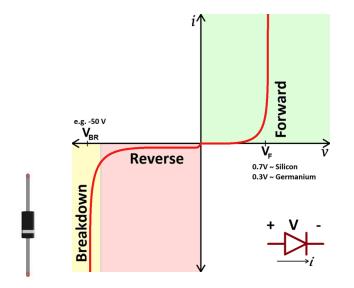
#### Diodes

- Devices that allow current to flow only in one direction
- Silicon diodes, for example have, essentially infinite resistance if  $V_{ac}$ <0, that is if the cathode is at a higher potential than the anode and very low resistance if  $V_{ac}$ > .7V.
- The cathode is usually labelled with a band
- Schottky diode: A metal-semiconductor contact that has a lower forward voltage drop than a PN diode.
- Zener diode: Provides a stable reference voltage.
- Tunnel diode: Has negative resistance due to tunneling, a quantum mechanical effect.
- PN junction diode: A diode made of two layers of semiconductor material.
- PIN diode: For high frequency (low capacitance)

#### • Transformers

• AC only:  $\frac{N_2}{N_1} = \frac{V_2}{V_1}$ 

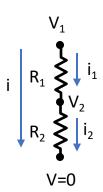




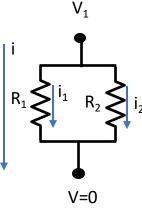
Credit: Make Electronics



## Simple circuit analysis with Kirchhoff



- $R_{eq}$  is the equivalent resistance, replacing the top left circuit with a single resistance.
- By Kirchhoff's node rule,  $i_1=i_2=\iota$ , so  $V_1 = V_2 = V_1 = V_2 = V_2 = V_1 = V_2 = V_2$



- Again let  $R_{eq}$  is the equivalent resistance, replacing the bottom left circuit with a single resistance.
- $i_{1}$  By Kirchhoff's node rule,  $i_{1} + i_{2} = i$ , so

• 
$$\frac{V_1}{R_1} + \frac{V_1}{R_2} = \frac{V_1}{R_{eq}}$$
.

• Solving, we get.  $\frac{R_1R_2}{R_1+R_2}=R_{eq}$ 

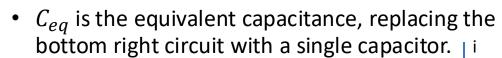
- $C_{eq}$  is the equivalent capacitance, replacing the top right circuit with a single capacitor.

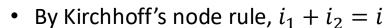
• 
$$C_1 \frac{d(V_1 - V_2)}{dt} = C_2 \frac{d(V_2)}{dt} = C_{eq} \frac{dV_1}{dt}$$

• 
$$\frac{C_{eq}}{C_1} \frac{d(V_1)}{dt} = \frac{d(V_1 - V_2)}{dt} \text{ and } \frac{C_{eq}}{C_2} \frac{d(V_1)}{dt} = \frac{d(V_2)}{dt}$$



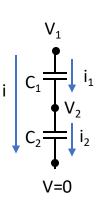
• 
$$\frac{C_{eq}}{C_1} + \frac{C_{eq}}{C_2} = 1$$
 and solving, we get.  $\frac{C_1C_2}{C_1 + C_2} = C_{eq}$ 





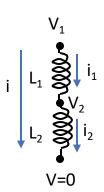
• 
$$C_{eq} \frac{dV_1}{dt} = C_1 \frac{dV_1}{dt} + C_2 \frac{dV_1}{dt}$$
, so

• 
$$C_{eq} = C_1 + C_2$$



V=0

## Simple circuit analysis with Kirchhoff

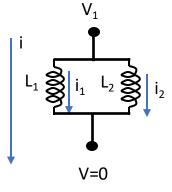


- Let  $L_{eq}$  be the equivalent inductance, replacing the top left circuit with a single inductor.
- By Kirchhoff's node rule,  $i_1 = i_2 = i$ , so

• 
$$L_{eq} \frac{di}{dt} = V_1$$
,  $L_1 \frac{di_1}{dt} = V_1 - V_2$ ,  $L_1 \frac{di_2}{dt} = V_2$ 

• 
$$V_1 = L_{eq} \frac{di}{dt} = L_1 \frac{di}{dt} + L_2 \frac{di}{dt}$$
 and

• 
$$L_{eq} = L_1 + L_2$$



• Let  $L_{eq}$  be the equivalent inductance, replacing the bottom left circuit with a single inductor.

• 
$$\frac{di}{dt} = \frac{V_1}{L_{eq}}, \frac{di_1}{dt} = \frac{V_1}{L_1}, \frac{di_2}{dt} = \frac{V_1}{L_2},$$

• By Kirchhoff's node rule,  $i_1 + i_2 = i$ , so

• 
$$\frac{V_1}{L_{eq}} = \frac{V_1}{L_1} + \frac{V_1}{L_2}$$
 and

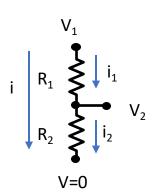
$$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$$

• The circuit on the right, is useful and is called a *voltage divider*.

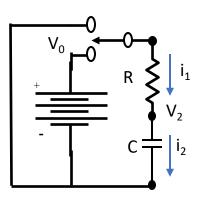
• 
$$i = i_1 = i_2$$
 so  $\frac{V_1 - V_2}{R_1} = \frac{V_2}{R_2}$ ,  $V_1 - V_2 = \frac{R_1}{R_2} V_2$ 

• Thus, 
$$V_1 = (1 + \frac{R_1}{R_2})V_2$$
 and so

• 
$$V_2 = \frac{R_2}{R_1 + R_2} V_1$$



## RC/RL circuit analysis with Kirchhoff



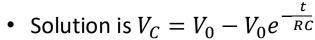
RC behavior: charging

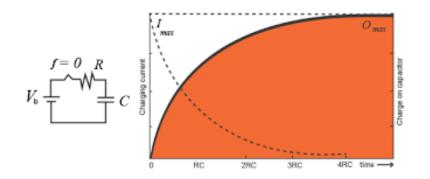
• 
$$V_0 - V_2 = i_1 R = V_R, i_1 = \frac{V_R}{R}$$

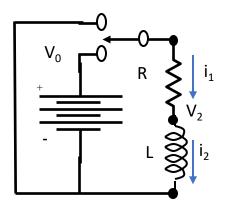
• 
$$i_2 = C \frac{dV_2}{dt}, V_C = V_2$$

• 
$$i_1 = i_2$$
,  $V_C = V_0 - V_R$ 

• 
$$i_1 = i_2$$
,  $V_C = V_0 - V_R$   
•  $\frac{V_R}{R} = C \frac{dV_C}{dt}$ ,  $RC \frac{dV_C}{dt} = V_0 - V_C$ , or  $RC \frac{dV_C}{dt} + V_C = V_0$ 







RL behavior: charging

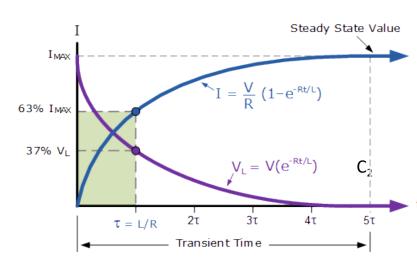
• 
$$V_0 - V_2 = i_1 R = V_R$$

• 
$$V_L = V_2 = L \frac{di_2}{dt}$$

• 
$$V_0 - V_2 = l_1 R = V_R$$
  
•  $V_L = V_2 = L \frac{di_2}{dt}$   
•  $i_1 = i_2$ ,  $V_R = V_0 - V_L$ , so  $L \frac{d}{dt} \frac{V_0 - V_L}{R} = V_L$ 

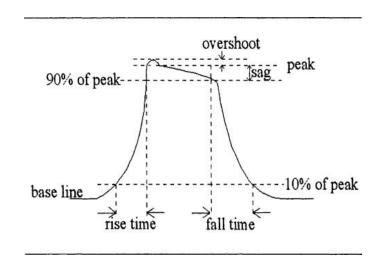
$$\bullet \ \frac{L}{R} \frac{d V_L}{dt} + V_L = 0$$

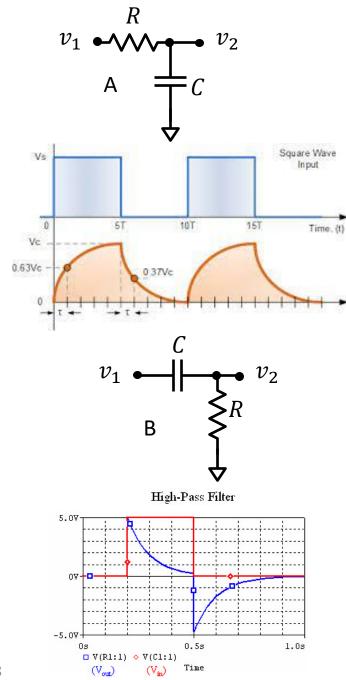
• Solution is  $V_L = V_0 e^{-\frac{Rt}{L}}$ 



## Voltage responses

- Response to square wave with width T
  - A:  $\tau = RC$ ,  $\tau = T$
  - B:  $\tau = RC$ ,  $\tau = .1T$
- Overshoot below





#### Phasors

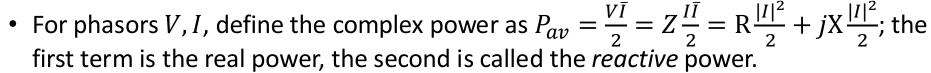
- V(t) = RI(t)
- $V(t) = L\dot{I}(t)$
- $I(t) = C\dot{V}(t)$
- Suppose  $V(t) = Acos(\omega t + \theta)$  and  $I(t) = Bcos(\omega t + \phi)$ . If  $\phi > \theta$ , we say the current leads the voltage.
- $V(t) = Re(Ae^{j(\omega t + \theta)})$ , and  $I(t) = Re(Be^{j(\omega t + \phi)})$
- Now define  $\hat{V} = V = Ae^{j\theta}$  and  $\hat{I} = Be^{j\phi}$ , so |V| = A, |I| = B,  $\angle V = \theta$ , and  $\angle I = \phi$ .  $\hat{V}$  and  $\hat{I}$  are called phasors and do not include time. Note that  $V(t) = Re(\hat{V}e^{j\omega t})$  and  $I(t) = Re(\hat{I}e^{j\omega t})$ .
- Note that  $I = CVj\omega$ , for a capacitor and  $V = LIj\omega$ , for an inductor
- $\hat{V} = Z\hat{I}, Z = R + jX$
- $\hat{I} = Y\hat{V}, Y = G + jB$

## Circuit analysis and impedance

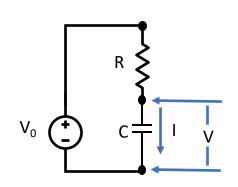
- Impedance unifies the "simple" ohms law with capacitance and inductance.
- Z=R, for resistors,  $Z=j\omega L$ , for inductors and  $Z=\frac{1}{j\omega C}$ , for capacitors.
- In general, Z = R + jX and all the ohm like laws hold for resistors, capacitors and inductors.
  - $Z_{eq}=Z_1+Z_2$  for two components with impedance  $Z_1,Z_2$  connected in series
  - $Z_{eq} = \frac{Z_1 Z_2}{Z_1 + Z_2}$  for two components with impedance  $Z_1, Z_2$  connected in parallel
- For example, for a resistor and capacitor in series has impedance  $Z = R + \frac{1}{j\omega C}$

## Phasors, impedance and power

- For the circuit on the right,  $Z=R+\frac{1}{j\omega C}$  is the impedance for the resistor and capacitor in series.
- The phasor  $I = \frac{V_0}{Z}$  and the phasor  $V = \frac{I}{j\omega C} = \frac{V_0}{1+j\omega RC}$
- Further,  $|I|=\frac{V_0}{|Z|}$ ,  $\angle I=\angle\frac{V_0}{|Z|}$  and  $|V|=\frac{|I|}{|j\omega C|}=|\frac{V_0}{1+j\omega RC}|$

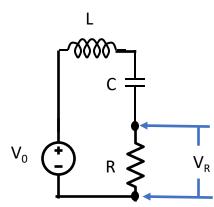


- The average power is  $P_a = Re(P) = Re(\frac{VI}{2})$ . We define the reactive power as  $P_r = Im(P)$ .
- $P_r = \omega(E_L E_C)$ , where  $E_L$  and  $E_C$  are respectively, the energy stored in the inductor and capacitor respectively.



## Q and phasors

- Consider the series resonance on the right.  $Z_{LCR} = R + j \left(\omega L \frac{1}{\omega C}\right)$
- The phasor,  $I=rac{V_0}{Z_{LCR}}$  , and the phasor  $V_R=rac{V_0}{Z_{LCR}}Z_R$  , where  $Z_R=R$  .
- So  $V_R = \frac{RC\omega V_0}{RC\omega + i(LC\omega^2 1)}$ .
- $|V_R|$  is maximum when  $\omega^2 LC = 1$ . Put  $\omega_0 = \frac{1}{\sqrt{LC}}$ . When  $\omega = \omega_0$ ,  $|V_R| = V_R = V_0$ .
- $|V_R| = \frac{V_0}{\sqrt{2}}$ , when X = R. Note that the power through R when X = R is half the power through R when X = 0 or  $\omega = \omega_0$ .
- Let the frequencies where  $R = \pm X$  be denoted  $\omega_u$  and  $\omega_l$ , where  $\omega_u > \omega_l$ .
- We define  $Q = \frac{X}{R} = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 CR}$ .
- Solving for  $\omega_u$  and  $\omega_l$ , we get  $\frac{L\omega_u}{\omega_0} \frac{\omega_0}{c\omega_u} = R$  and  $\frac{L\omega_l}{\omega_0} \frac{\omega_0}{c\omega_l} = -R$ , or, in terms of Q,  $\frac{\omega_u}{\omega_0} \frac{\omega_0}{\omega_u} = \frac{1}{Q}$  and  $\frac{\omega_l}{\omega_0} \frac{\omega_0}{\omega_l} = -\frac{1}{Q}$ . In fact,  $\omega_0 = \sqrt{\omega_u \omega_l}$ , and so  $\frac{\omega_u}{\omega_0} \frac{\omega_l}{\omega_0} = \frac{1}{Q}$ .
- Thus  $Q = \frac{\omega_0}{\omega_0 \omega_0} = \frac{\omega_0}{\Delta \omega}$
- From the definition of  $P_a$ , earlier,  $Q = \omega_0 \frac{E}{P_a}$ , where E is the total energy stored in L and C, which is in turn the peak  $E_L$  and peak  $E_C$  at resonance.



### Resonance and Q

#### Series Resonance

- At  $\omega_u$  and  $\omega_l$ ,  $X=\pm R$  [ $\omega_u$  is upper 3dB cutoff and  $\omega_l$  is lower 3dB cutoff]
- $\omega_u L \frac{1}{\omega_u C} = R$ ,  $\omega_l L \frac{1}{\omega_l C} = -R$
- Define  $Q = \frac{X}{R}$

• 
$$\frac{\omega_u}{\omega_0} - \frac{\omega_0}{\omega_u} = \frac{R}{\omega_0 L} = \frac{1}{Q}$$
 and  $\frac{\omega_l}{\omega_0} - \frac{\omega_0}{\omega_l} = -\frac{R}{\omega_0 L} = -\frac{1}{Q}$ 

• 
$$\frac{\omega_u}{\omega_0} - \frac{\omega_0}{\omega_u} = \frac{\omega_0}{\omega_l} - \frac{\omega_l}{\omega_0}$$
, so  $\omega_0^2 = \omega_u \omega_l$  and  $\frac{\omega_u - \omega_l}{\omega_0} = \frac{1}{Q}$ 

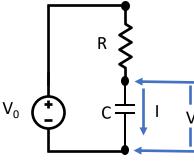
#### Parallel Resonance

• 
$$\frac{\omega_u}{\omega_0} - \frac{\omega_0}{\omega_u} = \frac{G}{\omega_0 C} = \frac{1}{Q_p}$$
 and  $\frac{\omega_l}{\omega_0} - \frac{\omega_0}{\omega_l} = -\frac{G}{\omega_0 C} = -\frac{1}{Q_p}$ 

## Phasors, impedance and power

- For the circuit on the right,  $Z=R+\frac{1}{j\omega C}$  is the impedance for the resistor and capacitor in series.
   The phasor  $I=\frac{V_0}{Z}$  and the phasor  $V=\frac{I}{j\omega C}=\frac{V_0}{1+j\omega RC}$  Further,  $|I|=\frac{V_0}{|Z|}$ ,  $\angle I=\angle\frac{V_0}{|Z|}$  and  $|V|=\frac{|I|}{|j\omega C|}=|\frac{V_0}{1+j\omega RC}|$

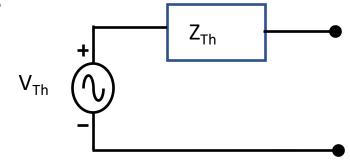
- Complex power:  $P = \frac{V\bar{I}}{2} = Z \frac{|I|^2}{2} = P_a + jP_r = R \frac{|I|^2}{2} + jX \frac{|I|^2}{2}$ 
  - $P_a$  is power delivered to resistor,  $P_r$  is power stored in inductor
  - For phasors V, I, define the complex power as  $P_{av} = \frac{V\overline{I}}{2} = Z\frac{I\overline{I}}{2} = R\frac{|I|^2}{2} + jX\frac{|I|^2}{2}$ ; the first term is the real power, the second is called the reactive power.
- $P_r = \omega(E_L E_C)$ , where  $E_L$  and  $E_C$  are respectively, the energy stored in the inductor and capacitor respectively.
- $P_r = \frac{\omega L|I|^2}{2} \frac{\omega C|V_c|^2}{2} = \omega (E_L E_C)$
- $Q = \omega \frac{L|I|^2}{R|I|^2} = \omega \frac{L}{R} = \omega \frac{E_L}{P_c}$



#### Thevenin and Norton

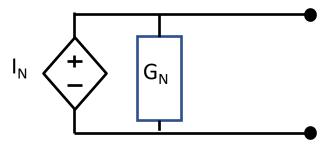
• Thevenin: Any combination of *linear* sources and passive elements terminating in two terminals is

equivalent to a pure voltage source in series with an impedance



• Norton: Any combination of *linear* sources and passive elements terminating in two terminals is

equivalent to a pure current source in parallel with a conductance

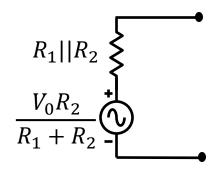


• Above,  $G_N = \frac{1}{Z_{Th}}$ 

• Similar theorems for *linear* two terminal input and output devices (with transfer function)

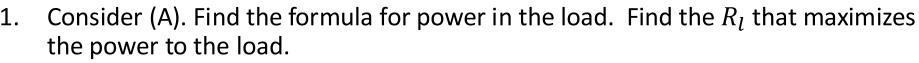
### Thevenin and Norton

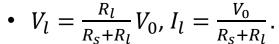
- $V_0 \bigoplus_{\mathsf{R}_2}^{\mathsf{R}_1}$ 
  - is equivalent to



- We can use lookback resistance to calculate the Thevenin equivalent resistance and ideal source.
- To find the lookback resistance, short the source and apply the usual laws.
  - Here  $R_S = R_1 || R_2$
- To find the new ideal source, notice  $R_1$  and  $R_2$  form a voltage divider.
  - The new source voltage is  $\frac{V_0 R_2}{R_1 + R_2}$
- In general, a Norton equivalent with parameters  $(i_N, Z_N)$  is the same as a Thevenin equivalent with parameters  $(V_{Th}, Z_{Th})$  with  $Z_{Th} = Z_N$  and  $V_{Th} = i_N Z_N$

#### Exercise 1: Resistors





• 
$$P_l = V_l I_l = \frac{R_l}{(R_S + R_l)^2} V_0^2$$
, which is maximum when  $R_l = R_S$ 

2. Find the Thevenin and Norton parameters for (B).

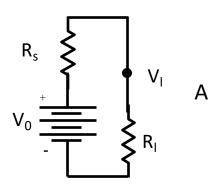
• 
$$V_{Th} = \frac{R_3}{R_1 + R_3} V_0$$

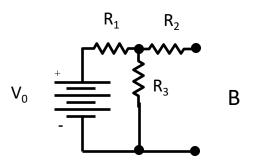
• 
$$R_{Th} = R_2 + R_1 || R_3$$

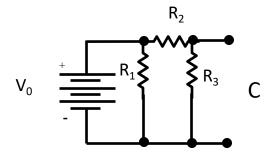
3. Find the Thevenin and Norton parameters for (C).

• 
$$V_{Th} = \frac{R_3}{R_2 + R_3} V_0$$

• 
$$R_{Th} = R_2 ||R_3|$$

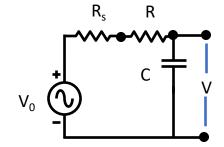




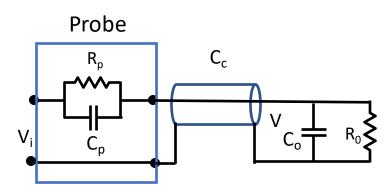


## Exercise 3: Capacitors

1. In the circuit on the right,  $V_0$  is a 2 volt pp ideal square wave source of frequency 20Hz,  $R_S=50\Omega$ ,  $R=300k\Omega$  and C=10~nF. Period is 50~millisec



- 2. What is the voltage, V, at the output? The scope has an input resistance of  $1M\Omega$ .
  - About a volt at peak
- 3. Let  $t_2$ , the time to discharge to 0V. Calculate  $\tau$  and  $t_2$ .
  - $\tau = 3 \times 10^5 \times 10^{-8} sec = 3 millisec$
  - $t_{12} \approx 1.5 ms$
- 4. Capacitance on the scope prevents the delay from being 0. Measure the new  $t_2$  with these changes.
- 5. Given  $C_0$  and  $C_p$  and  $R_{p.}$ 
  - $C_0 = 100pf/m$ ,  $C_o = 50pF$ ,  $C_p = 10pF$
- 6. Now calculate the new  $t_{12}$ .
  - $\tau = 6\mu$ -sec

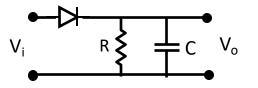


## Signals and modulation

- Gain:  $G = \frac{P_o}{P_i}$ , Loss:  $L = \frac{P_o}{P_{max}}$ , Rejection:  $R = \frac{P_{max}}{P_{pb}}$ . Gain (G) expressed in decibels:  $G = 10 \log_{10}(\frac{P_{out}}{P_{in}})$
- $P_S = \int \sigma E \cdot E + \epsilon \frac{E \cdot E}{2} + \frac{H \cdot H}{2\mu} dV + \int E \times H dA$
- Mixer:  $V(t) = \cos(\omega_1 t) \cos(\omega_2 t) = \frac{1}{2} [\cos(\omega_+ t) + \cos(\omega_- t)], \omega_+ = \omega_1 + \omega_2, \omega_- = \omega_1 \omega_2$
- Modulation

Name	Equation
AM	$V(t) = (1 + am(t))V_c \cos(\omega_c t)$
FM	$V(t) = V_c \cos([\omega_c + am(t)]t)$
Angle	$V(t) = V_c \cos(\omega_c t + \phi(t))$ , $\phi(t) = am(t)$ . [Like FM]
FSK	$V(t) = V_c \cos(\omega_1 t)$ , if 1 $V(t) = V_c \cos(\omega_0 t)$ , if 0
PSK	$V(t) = +V_p \cos(\omega t)$ , if 1 $V(t) = -V_p \cos(\omega t)$ , if 0

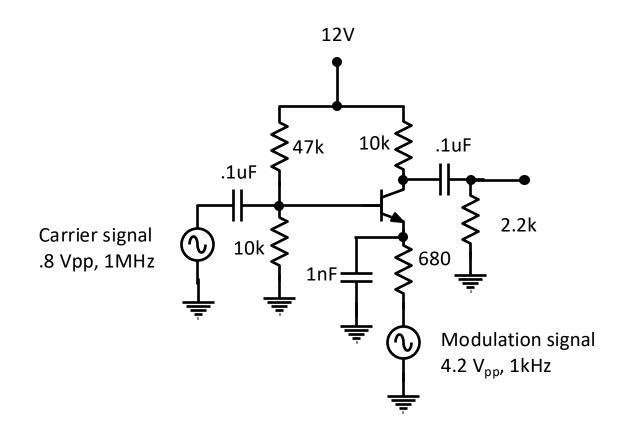
#### Exercise 4: Diode detectors



- For AM,  $V(t) = V_c \cos(\omega_c t) + a(t) \cos(\omega_c t)$ , Define the modulation depth  $m = \frac{a_p}{V_c}$
- In circuit on the right,  $R = 10k\Omega$ , C = 10 nF
- Set function generator for  $f_c = 1MHz$ ,  $V_{c,pp} = 5V$ ,  $f_m = 1kHz$ , m = .7
  - 1. Calculate  $\tau$  for the RC circuit.  $\tau = 10^4 \times 10^{-8} \text{ sec} = .1 \text{ms}$ .
    - $T_m$  is period of modulating signal.  $T_m = 10^{-3} sec = 1 ms$ . So  $\tau \ll T_m$
    - $T_c$  is period of modulating signal.  $T_c=10^{-6}sec=1\mu s.~ au\gg T_c$
    - As you change  $f_m$  does the frequency of  $V_o$  track it? (It better)
  - 2. Compare the max voltage of the AM signal to the max of  $V_0$ .
    - $V_0, p \approx .8V, V_{i,p} \approx 1.4V$
  - 3. What happens when we make m=1.0

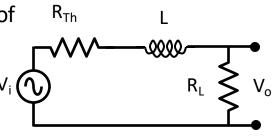
## AM Modulator for previous exercise

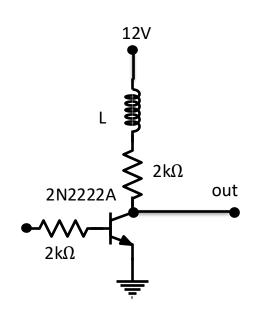
• I didn't have a signal generator that produced an AM signal, so I used the modulator on the right with the indicated inputs to produce the AM needed for the detector in the previous exercise.



#### Exercise 5: Inductors

- Set function generator for square wave with 5V  $V_{pp}$ , a Thevenin equivalent source resistance of  $R_{Th}=50\Omega$  and frequency 1kHz. Connect a load,  $R_L=100\Omega$  load, L=1mH
  - 1. Observe square wave with rounded corners, measure the time,  $t_2$  to decay to 0
    - About 20*μsec*
  - 2. In the top circuit, calculate inductor current and the expected delay,  $t_2$ 
    - $Z_{eq} = 150 + jL\omega$ ,  $\omega = 2\pi \times 10^3$ ,  $V_i = Re(V_{i,p}e^{j\omega t})$
    - As phasors,  $iZ_{eq} = V_i$ ,  $|i|\sqrt{150^2 + (\omega L)^2} = V_{i,p}$ ,  $|i| = \frac{V_{i,p}}{\sqrt{150^2 + (2\pi)^2}}$ ,  $\theta = \angle i = \arctan(-\frac{2\pi}{150})$ ,  $\theta \approx -2.4 \ rad = -15^\circ$
    - $V_o = Re\left(\frac{100V_{i,p}}{\sqrt{150^2 + (2\pi)^2}}e^{j(\omega t + \theta)}\right), |V_o| = 1.6V,$
    - $\tau_{RL} = \frac{10^{-3}}{100} sec \approx 10 \ \mu sec$
  - 3. In the second circuit, use 2 scope channels: one at input, one at output.
    - $1\mu \sec rise \ time$ . Ringing at 10MHz.  $\frac{1}{\sqrt{LC}} = 62.8 \times 10^6$ .  $C = \frac{10^3}{(62.8 \times 10^6)^2} \approx .25 pF$
  - Note: I made the pull-up 100K.



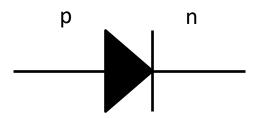


## Diodes and bipolar small signal models

#### • Diode model:

• 
$$i_d = i_s(\exp\left(\frac{eV}{kT}\right) - 1), \frac{e}{kT} = 40V^{-1}$$

- *T* is the junction temperature
- $\frac{di_d}{dV} = i_d \frac{e}{kT}$
- $r_d = \frac{e}{kTi_d}$
- When  $i_d$  is a few nano-Amps,  $r_d \approx 5\Omega$
- When  $i_d$  is a few  $\mu A$ ,  $r_d \approx 10^4 \Omega$



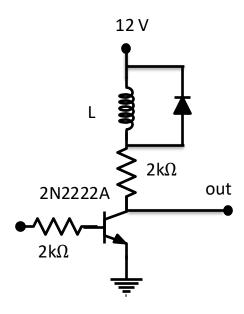
- Transition from p to n in  $1 \mu m$
- Doping provides
  - n side has excess free electrons
  - p side has excess holes

#### Exercise 6: Diodes and snubbers

- Add indicated snubber diode.
- 1. Swing up is nearly immediate with snubber

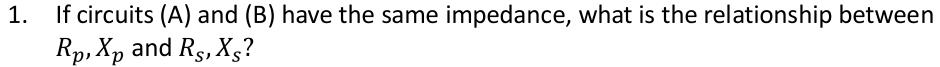
2. Ringing at 10MHz. 
$$\frac{1}{\sqrt{LC}} = 62.8 \times 10^6$$
.  $C = \frac{10^3}{(62.8 \times 10^6)^2} \approx .25 pF$ 

- 3. What is its effect on ringing?
  - Ringing is uniform at 5 MHz
- 4. Diode should be on when transistor is off.
- Note: I made the pull-up 100K.



#### Exercise 7: Parallel to Series conversion

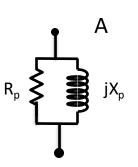
- For series:  $Z_S = R_S + j\omega L$ ,  $Q_S = \frac{X_S}{R_S}$
- For parallel:  $\frac{1}{Z_p} = \frac{1}{R_p} + \frac{1}{j\omega L}$ , so  $Z_p = \frac{j\omega L R_p}{R_p + j\omega L}$  and  $Q_p = \frac{R_p}{X_p}$
- If  $Q_p = Q_S$ ,  $X_p X_s = R_p R_S$

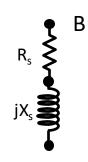


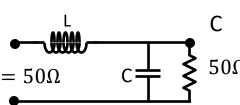
• 
$$\frac{1}{Z_p} = \frac{1}{R_p} + \frac{1}{jX_s}, Z_p = \frac{jR_pX_p}{R_p + jX_p} = \frac{X_p^2R_p + jR_p^2X_p}{R_p^2 + X_p^2}, Z_s = R_s + jX_s$$

• 
$$R_S = \frac{X_p^2 R_p}{R_p^2 + X_p^2}$$
,  $X_S = \frac{R_p^2 X_p}{R_p^2 + X_p^2}$ ,  $R_S = X_p \frac{X_p R_p}{R_p^2 + X_p^2}$ ,  $X_S = R_p \frac{X_p R_p}{R_p^2 + X_p^2}$ , set  $\rho = \frac{X_p R_p}{R_p^2 + X_p^2}$ 

- for later reference
- This shows the Q's must be equal as stated above.
- 2. Find a formula for  $X_s$ , for large  $Q=Q_p=Q_s$  and small  $Q=Q_p=Q_s$
- 3. Use circuit (C) to transfer a  $50\Omega$  load (circuit C) to a  $5\Omega$  load. What is  $X_C$  at 7 MHz?  $Z_i = 50\Omega$  What are C and L in that model?
  - Use the parallel to series conversion to make a series equivalent circuit consisting of C and the  $50\Omega$  with  $R_S=5\Omega$

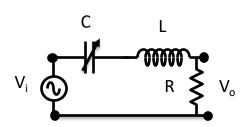






#### Exercise 8: Series resonance

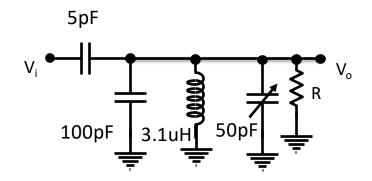
- For the circuit on the right, C= 8-50pf,  $L=15\mu H$  forming a bandpass filter.  $R=100\Omega$
- If C=34pf, the resonant frequency is  $\omega=\frac{1}{\sqrt{35\times10^{-12}\times15\times10^{-6}}}=\frac{10^9}{\sqrt{525}}\approx 44.2$ , so the resonant frequency is  $\frac{44.2}{2\pi}\approx 7.07MHz$



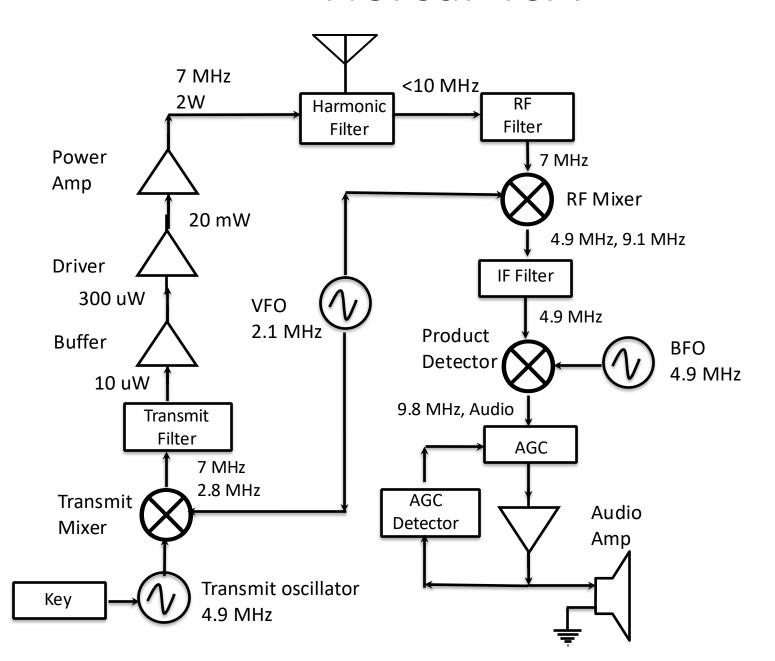
- 1. Tune the resonant frequency to 7MHz and find  $f_u$ ,  $f_l$  and  $\Delta f$  and thus Q.
  - $f_u = 7.67MHz$ ,  $f_l = 6.47MHz$ ,  $Q = \frac{f}{\Delta f} = \frac{7}{1.2} = 5.8$
- 2. Compute what these values should be
  - $Z_{eq} = R + j(\omega L \frac{1}{\omega C})$
  - As phasors,  $i = |i|e^{j\theta}$ ,  $|i| = \frac{V_{i,0}}{\sqrt{R^2 + (\omega L \frac{1}{\omega C})^2}}$ ,  $\theta = -arctan(\frac{\omega L \frac{1}{\omega C}}{R})$
  - $V_0=iR$ , Power through R at  $\omega$  is  $P(\omega)=|i^2|R=\frac{V_{i,0}{}^2R}{R^2+(\omega L-\frac{1}{\omega C})^2}$ . At resonance,  $P(\omega_r)=\frac{V_{i,0}{}^2}{R}$ . To find half power,  $\det\frac{1}{2}=(\frac{V_{i,0}{}^2R}{R^2+(\omega L-\frac{1}{\omega C})^2})/(\frac{V_{i,0}{}^2}{R}), \text{ or } R=\omega L-\frac{1}{\omega C}.$
  - Solving gives  $f_u = 7.67MHz$ ,  $f_l = 6.53MHz$ , Q = 6.1
  - General formulas:  $\omega_u = \frac{R}{2L} + \sqrt{(\frac{R}{2L})^2 + \frac{1}{LC}}$ ,  $\omega_l = -\frac{R}{2L} + \sqrt{(\frac{R}{2L})^2 + \frac{1}{LC}}$

#### Exercise 9: Parallel resonance

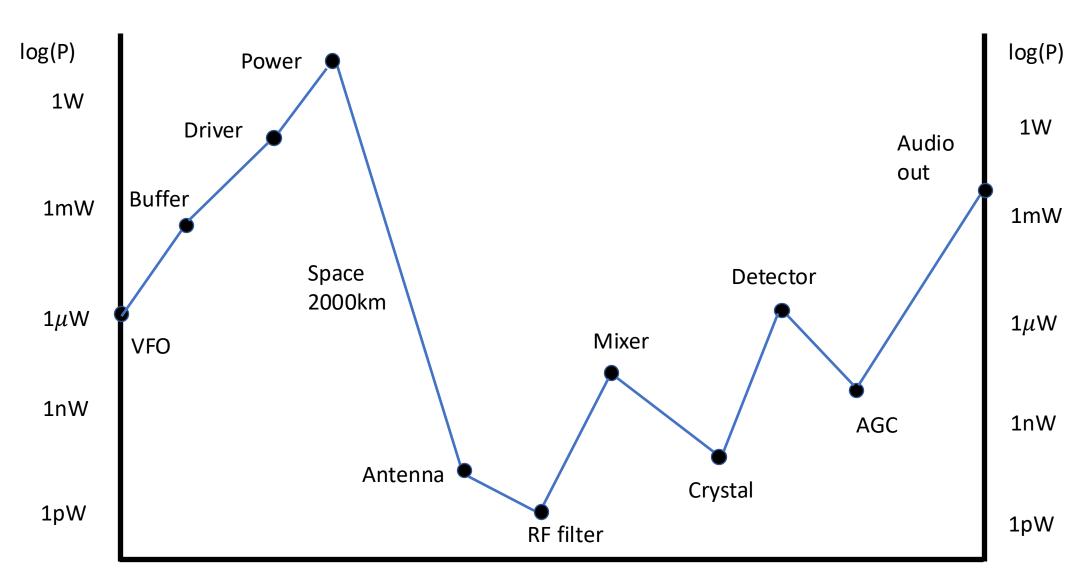
- $L=A_l\,N^2$ ,  $A_l=4\frac{nH}{turn^2}$  for T37-2 core so for 28 turns,  $L=3.1\mu H$
- 1. Find the resonant frequency, the frequencies corresponding to a 3db falloff, the bandwidth and the Q of this circuit. This circuit is in the transmit oscillator.
  - At tuned resonance (7MHz), effective capacitance is about 167 pF
  - $Q_p = \omega_0 RC$
  - For  $R = 1500\Omega$ , network:  $Q = 1500 \times 44 \times 10^6 \times 1.67 \times 10^{-10} = 11$
  - $BW = \frac{f_r}{Q} = \frac{7MHZ}{11} = .636MHz$ .  $f_u = f_r + \frac{BW}{2} = 7.318MHz$ ,  $f_l = f_r \frac{BW}{2} = 6.682MHz$ . This is 3dB cutoff.
- General formulas:  $BW = \frac{f_r}{Q}$ ,  $f_u = f_r + \frac{BW}{2}$ ,  $f_l = f_r \frac{BW}{2}$



### Norcal 40A



## NorCal power levels

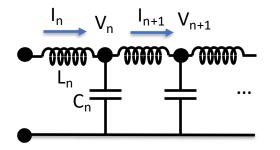


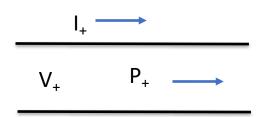
#### Transmission Lines

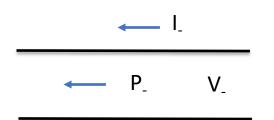
• 
$$V_{n+1} - V_n = -L_l \frac{\partial I_{n+1}}{\partial t}$$
,  $L = \frac{L_l}{l}$ , so  $\frac{\partial V}{\partial z} = -L \frac{\partial I}{\partial t}$ 

• 
$$I_{n+1} - I_n = -C_l \frac{\partial V_n}{\partial t}$$
,  $C = \frac{C_l}{l}$ , so  $\frac{\partial I}{\partial z} = -C \frac{\partial V}{\partial t}$ 

- Thus,  $\frac{\partial^2 V}{\partial z^2} = LC \frac{\partial^2 V}{\partial t^2}$  and  $\frac{\partial^2 I}{\partial z^2} = LC \frac{\partial^2 I}{\partial t^2}$ , whose solution is is  $V(z \pm vt)$
- $v = \frac{1}{\sqrt{LC}}$  for the forward wave .
- $\frac{\partial V}{\partial z} = -L \frac{\partial I}{\partial t}$  and  $\frac{\partial I}{\partial z} = -C \frac{\partial V}{\partial t}$  implies
- V' = vLI' and  $\frac{V}{I} = \sqrt{\frac{L}{C'}}$ , so  $Z_0 = \sqrt{\frac{L}{C'}}$ , where  $Z_0$  is the forward impedance
- $Z_0 = \frac{V_+}{I_+}, -Z_0 = \frac{V_-}{I_-}, V = V_+ + V_-, -Z_0$  is the backwards looking impedance
- $P_+(t) = \frac{V_+^2}{Z_0}$ ,  $P_-(t) = -\frac{V_-^2}{Z_0}$  (the negative sign implies energy flows to the left)







#### Transmission Lines - continued

- $V(z-vt)=Acos(\omega t-\beta z)$ ,  $v=\frac{\omega}{\beta}$ . The phasor is  $\hat{V}=Ae^{-j\beta z}$  although we drop the cap below.
- Now the forward and backward voltage phasors are  $V_+ = Ae^{-j\beta z}$ ,  $V_- = Ae^{j\beta z}$
- The complex power is  $P_{av} = \frac{V\bar{I}}{2}$ ,  $P_{+} = \frac{V_{+}\bar{I}_{+}}{2} = \frac{|V_{+}|^{2}}{2Z_{0}}$ ,  $P_{-} = \frac{V_{-}\bar{I}_{-}}{2} = -\frac{|V_{-}|^{2}}{2Z_{0}}$ , with  $\frac{V}{I} = Z_{0}$
- Suppose over a transmission line, Z is the distributed impedance/m, Y is the distributed admittance/m and suppose the forward wave is  $Ae^{j(\omega t-jk)}$ , with phasor is  $V=Ae^{-jkz}$ . Let  $Z=\frac{V}{I}$  then  $\frac{dV}{dz}=-ZI$ ,  $\frac{dI}{dt}=-YV$ .
- Put  $jk = \alpha + \beta j$  (to account for attenuation), then  $jk = \sqrt{ZY}$  and the forward phasor becomes  $e^{(-\alpha z j\beta z)}$ .  $\alpha_{dB/m}$  is a transmission loss.  $\alpha_{dB/m} = 8.686\alpha_{nepers/m}$ .
- By differentiating, we get jkV=ZI, -jkI=YV. Solutions are  $jk=\sqrt{ZY}$ ,  $Z_0=\frac{V}{I}=\sqrt{\frac{Z}{Y}}$ , all complex
- So, if  $Z=R+j\omega L$ ,  $Y=j\omega C+G$  for the transmission line, then  $jk=\sqrt{(j\omega L+R)(j\omega C+G)}$  and  $Z_o=\sqrt{\frac{(j\omega L+R)}{(j\omega C+G)}}$  (positive real root)

## Transmission Lines - dispersion

- $\alpha$  and v can vary with frequency; this is dispersion.
- Heaviside: Adjust parameters so  $\frac{R}{L} = \frac{G}{C}$ , then  $\alpha$  doesn't depend on v and we get:

• 
$$jk = j\omega\sqrt{LC}(1 + \frac{R}{j\omega L})$$
 and  $v = \frac{\omega}{\beta} = \frac{1}{\sqrt{LC}}$ ,  $\alpha = \sqrt{RG}$ 

- We also get  $Z_0 = \sqrt{\frac{L}{c}}$  as with a lossless line.
- If  $\omega L \gg R$

• 
$$G = 0$$
 and  $Z_0 = \sqrt{\frac{(j\omega L + R)}{j\omega C}} \approx \sqrt{\frac{L}{C}}$ 

• If  $R \gg \omega L$ 

• 
$$jk = \sqrt{\frac{(j\omega L + R)}{j\omega C}} \approx \sqrt{j\omega RC}$$
, and  $\alpha = \sqrt{\frac{\omega RC}{2}}$ ,  $\alpha = \sqrt{\frac{2\omega}{RC}}$ 

- For first transatlantic cable,  $L=460\frac{nH}{m}$ ,  $C=75\frac{pF}{m}$ , f=12Hz,  $R=7\frac{m\Omega}{m}$ , l=3600 km,  $\alpha=\sqrt{\frac{\omega RC}{2}}=4.4\times 10^{-3}$   $\frac{nepers}{m}$ ,  $\alpha l=140dB$ 
  - $\alpha l \approx 140 dB$  and highly dispersive

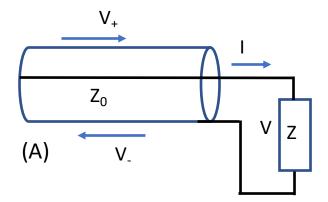
### Transmission Lines-reflections

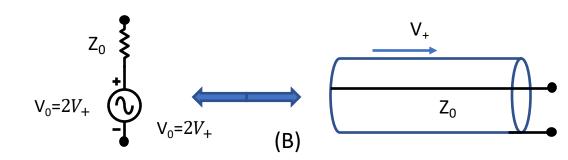
- Now we look at the end of the transmission line and define  $ho=rac{V_-}{V_+}$ , and  $ho_i=rac{i_-}{i_+}=ho$
- $V = V_+ + V_- = (1 + \rho)V_+$
- $\tau = \frac{V}{V_{+}} = 1 + \rho = \frac{2Z}{Z + Z_{0}}, V = 2V_{+}$
- Consider the circuit in the upper right (A):  $V = V_+ + V_-$ ,  $I = I_+ + I_-$ ,  $Z = \frac{V}{I}$

• 
$$Z = \frac{V}{I} = \frac{V_+ + V_-}{I_+ + I_-}$$

• 
$$\frac{Z}{Z_0} = \frac{1+\rho}{1-\rho}, \, \rho = \frac{Z-Z_0}{Z+Z_0}, \, \rho_{open-circuit} = 1.$$

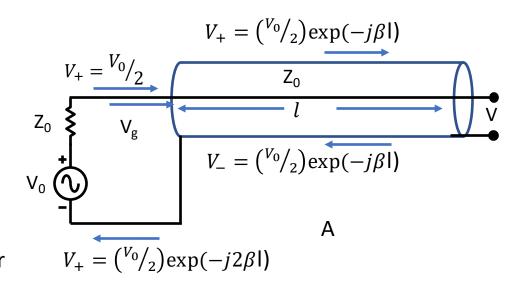
- For (B):
- Lookback resistance is  $R_S=Z_0$ , short circuit for (B) is  $i_S=\frac{v_0}{Z_0}$
- Thevenin equivalent for open circuit is (B)
- $P_+ = \frac{{V_+}^2}{2Z_0} = \frac{{V_0}^2}{8R_s}$ . This is the total available power.

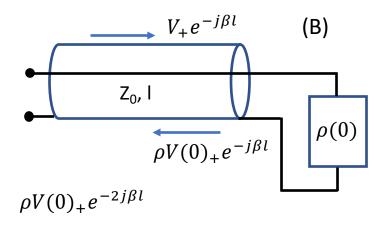




### Transmission Lines – resonance and Q

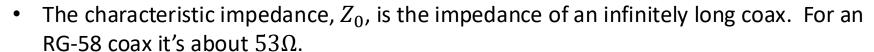
- For (A) on right,  $V_+ = \frac{V_0}{2}$ ,  $V = V_+ + V_- = V_0 e^{-j\beta l}$ ,  $V_- = \frac{V_0}{2} e^{-2j\beta l}$ 
  - $V_g = V_0 e^{-j\beta l} \cos(\beta l) = \frac{V_0}{2} (1 + e^{-2j\beta l}), V_g(\frac{\lambda}{4}) = 0$
  - $I_g = \frac{V_+}{Z_0} \frac{V_-}{Z_0} = jI_S e^{-j\beta l} \sin(\beta l).$
  - $X = \frac{V_g}{jI_g} = \frac{Z_0}{\tan(\beta l)}$
- $Q = \omega \frac{E}{P_a}$ ,  $E = \frac{lP_+}{v}$ ,  $P_a = P_+ P_+ e^{-2\alpha l} \rho(0) \approx 2\alpha l P_+$ ,  $Q = \frac{\beta}{2\alpha}$
- In (B) to the right, the coefficient of reflection is  $\rho(0)$  and the generator absorbs the reverse wave.  $V=V_++V_-=V_0e^{-j\beta l}$ .
  - $V_f = \rho(0)V_+e^{-j\beta l}, V_r = \rho(0)V_+e^{-2j\beta l}$
  - $\rho(l) = \frac{V_-}{V_+} = \rho(0)e^{-2j\beta l}$  is the reflection coefficient at generator.
  - $\rho\left(\frac{\lambda}{2}\right) = \rho(0), \, \rho\left(\frac{\lambda}{4}\right) = -\rho(0)$
  - $\frac{Z(^{\lambda}/_{4})}{Z_{0}} = \frac{Z_{0}}{Z(0)}, z = \frac{Z}{Z_{0}}, y = \frac{1}{z}, z\left(\frac{\lambda}{4}\right) = -\frac{1}{z(0)}$
  - Normalized:  $Z(^{\lambda}/_4) = \frac{1}{z(0)}$
  - $Z_0 = \sqrt{Z(\lambda/4)Z(0)}, Z_0 = \sqrt{R_S R_L}$

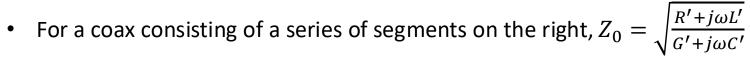




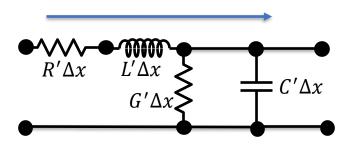
## Modelling Coaxial Cables

- A small segment of coax (of length  $\Delta x$ ) can be modelled by the circuit to the right.
  - R' and L' are characteristic of the two parallel conductors.
  - *G'* and *C'* are characteristic of the dielectric between the two conductors and the distance between them.



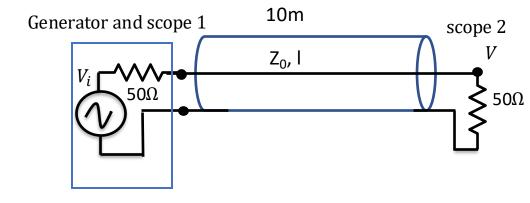


- In the last few slides, we have simplified the model considerably.
- Notice that at high frequency,  $Z_0 \approx \sqrt{\frac{L'}{C'}}$
- In an earlier slide (with a simpler circuit model), we showed that the propagation speed of a signal of high frequency is  $v=\frac{1}{\sqrt{C'L'}}$
- Since  $Z_0\sqrt{C'}=\sqrt{L'}$ ,  $Z_0C'=\sqrt{C'L'}$ .
- An RG-58 cable, has  $C'=82^{-pf}/m$  and thus,  $v=\frac{1}{53\times82\times10^{-12}} m/s\approx .75c$

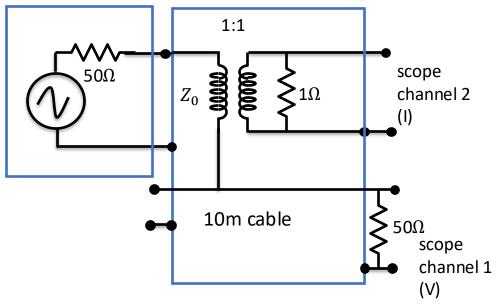


#### Exercise 10: Coax

- We'll measure the velocity of waves in RG58U by connecting one channel of the scope to the input and one to the output.
- 1. Measure the velocity, v, in 10m coax at 7MHz. Try different frequencies. Use 50ns,  $5V_{pp}$  using square waves at 20kHz. Ans: about  $\frac{2}{3}c$
- 2. Do the same with an antenna.
- 3. Calculate  $Z_0$  with  $50\Omega$  termination for the circuit on the right.
- 4. Remove the  $50\Omega$  and measure the V and use it and  $Z_0$  to calculate L, and C for the coax
  - Measured speed is  $v=2\times 10^8$  m/s.  $Z_0=50\Omega$  . For high impedance,  $Z_0=\sqrt{\frac{L}{c}}$  and  $v=\frac{1}{\sqrt{LC}}$ . So,  ${Z_0}^2C=L$  and  $v^2=\frac{1}{LC'}$  so  ${Z_0}^2C^2v^2$ =1.  $C=\frac{1}{Z_0v}=10^{-10}F$ .  $2500\times 10^{-10}F=L=250$ nH, which is what we use in the next problem.

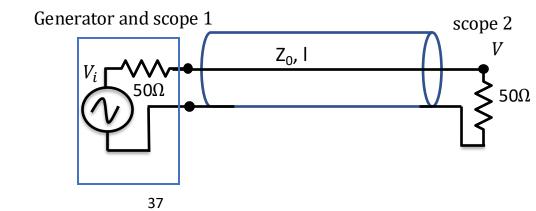


#### Function generator



#### Exercise 11: Waves

- Suppose we want to send voice over 100km of coax,  $Z_L = 50\Omega$ , l = 100km.
- 1. Measure the SWR which is the ratio of the maximum to minimum output
  - $V = V_+ + V_-$ ,  $\rho = \frac{Z Z_0}{Z + Z_0}$ ,  $Z = 50\Omega$ , we get  $Z_0$  from the previous exercise.
  - $|V_{max}| = |V_f| + |V_r| = (1+\rho)|V_f|, |V_{min}| = (1-\rho)|V_f| = |V_f|. SWR = \frac{V_{max}}{V_{min}} = \frac{1+\rho}{1-\rho},$
- 2. If  $L = 250 \frac{nH}{m}$ , C = 100 pf/m and the distributed resistance at voice is  $50 m\Omega/m$ , calculate total dB loss at 500, 1000 and 2000Hz using the high frequency approximation.
  - $Z(f) = j\omega L + R = 50 \times 10^{-3} + j \cdot 2\pi f \cdot 250 \times 10^{-9}$
  - $Y(f) = j\omega C + \frac{1}{R} = \frac{1}{50 \times 10^{-3}} + j \ 2\pi f \cdot 10^{-10}$
  - $Z_0(f) = \sqrt{\frac{Z(f)}{Y(f)}}$
  - $Z_0(500) = 400\Omega$ ,  $Z_0(1000) = 282\Omega$ ,  $Z_0(500) = 200\Omega$ ,
  - High resistance approximation:  $\alpha(f) = \sqrt{\frac{\omega RC}{2}}$ ,
  - $\alpha(500) = 8.8 \times 10^{-5}$ ,  $\alpha(1000) = 12.6 \times 10^{-5}$
  - $\alpha(2000) = 17.6 \times 10^{-5} \times 10^{5}$
  - For 100km, loss is  $\alpha \times 10^5$



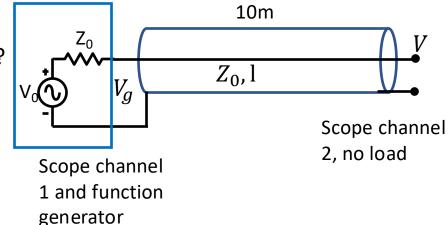
#### Exercise 11: Waves

- 3. Add a 100mH inductor every 1km. Now what's the loss?
  - $Z(f) = j\omega L + R = 50 \times 10^{-3} + j \cdot 2\pi f \cdot 10^{-4}, Z_0(f) = \sqrt{\frac{Z(f)}{Y(f)}}$
  - $Z_0(f) = \sqrt{\frac{Z(f)}{Y(f)}}$
  - $Z_0(500) = 318\Omega$ ,  $Z_0(1000) = 317\Omega$ ,  $Z_0(2000) = 316\Omega$
  - High reactance approximation:  $\alpha(f) = \frac{R}{2Z_0}$  ,  $Z_0 = \sqrt{\frac{L}{C}} = 1000\Omega$
  - $\alpha(f) = \frac{R}{2Z_0(f)}$ ,  $\alpha(500) = \alpha(1000) = \alpha(2000) = \frac{1}{5 \times 10^{-2}} = 5.5 \times 10^{-5} \text{ nepers/m}$
  - For 100km, loss is  $\alpha \times 10^5$ =5.5 or 5.5  $\times$  8.868  $\approx$  49dB

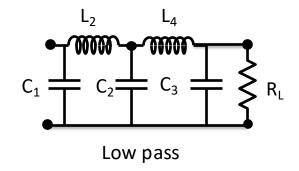
#### Exercise 12: Resonance

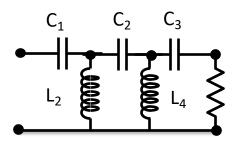
RG58U has a capacitance of about  $100rac{pF}{m}$ . Let lpha be the attenuation constant and eta be the phase

- 1. Derive an expression for  $|\frac{V_g}{V}|$  and assuming  $\alpha$  is small by finding the first resonance where  $V_g$  is minimum.
  - $V_g = V_0 e^{-j\beta l} \cos(\beta l)$ ,  $V = V_0 \exp(-j\beta l)$ .  $\left|\frac{V_g}{V}\right| = \cos(\beta l)$ . So, at  $l = \frac{\lambda}{2}$ ,  $\left|V_g\right| = |V|$
- 2. Find  $\alpha$  and the wave velocity by finding the resonant frequency (without the load,  $1V_{pp}$ ) and noting the time delay with a scope on the input and output. Use  $|\frac{V_g}{V}|$  to calculate  $\alpha$ .
  - |V| will be maximum at resonant frequency with unterminated line.
  - $|V_g(l)|$  is minimum when  $l = \frac{\lambda_r}{4}$  and  $\beta l = \frac{\pi}{4}$ . This gives  $\beta$ .
  - At  $l = \frac{\lambda}{2}$ ,  $\left| \frac{V_g}{V} \right| = e^{-\alpha(\lambda/2)}$
- 3. Use this to calculate the velocity, v. How large is the frequency shift caused?
  - $v = \frac{\omega_r}{\beta}$ . [v should be about  $2 \times 10^8 \ m/s$ ]
- 4. Find, as usual,  $f_u$ ,  $f_l$ , and Q.
  - $Q = \frac{\beta}{2\alpha}$
  - $Q = \frac{f_r}{BW}$ , so  $BW = \frac{f_r}{Q}$ .  $f_u = f_r + \frac{BW}{2}$ , and  $f_l = f_r \frac{BW}{2}$

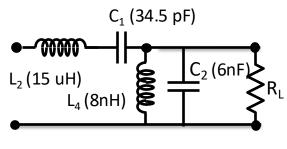


#### Filters





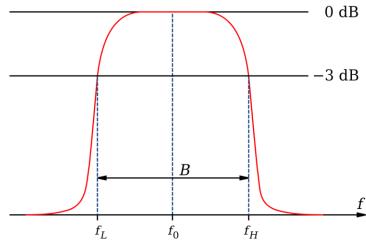
High pass



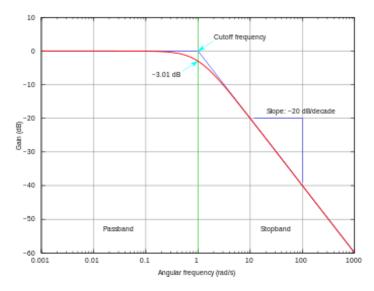
7 MHz bandpass

- Circuits on the left are called ladder filters.
- Low pass (Butterworth equivalent): Tabled values for inductors and capacitors based on frequency and dB drop-off.
- Can convert low pass into bandpass.
- For low pass to high pass
- Butterworth:  $L = \frac{P_i}{P} = 1 + (\frac{f}{f_c})^{2n}$ ,  $f_c$  is 3dB cutoff
- Chebyshev:  $L = 1 + \alpha C_n^2 (\frac{f}{f_c})^{2n}$ ,  $f_c$  is 3dB cutoff
- Normalized reactance's:  $a_i = \sin(\frac{(2i-1)\pi}{2n})$
- Ripple loss:  $1 + \alpha = 10^{L_r/_{10}}$
- $\beta = \sinh(\frac{\tanh^{-1}(1/\sqrt{1+\alpha})}{n}), c_i = \frac{a_i a_{i-1}}{c_{i-1}(\beta^2 + \sin^2((i-1)\pi/n))}$
- Example: cutoff at 10MHz, 4<sup>th</sup> order, 50ohm output, 3dB cutoff, L(20MHz)=6n=24dB,  $a_1=0.765$ ,  $X_1=x_1Z_0=38\Omega$ ,  $L_1=\frac{X_1}{\omega_c}=610nH$ ,  $b_2=a_2=1.848$ ,  $B_2=\frac{b_2}{Z_0}$ ,  $C_2=\frac{B_2}{\omega_c}$





Bandpass - WIkipedia



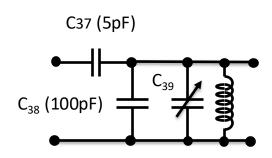
Lowpass - Wlkipedia

# Norcal transmit bandpass filter

- $C_{39} = 50pF$ ,
- $L_6$  is 36 turns #28 on T37-2 which has  $A_l = 4 \frac{nH}{turn^2}$ ,  $L_6 = A_l \cdot 36^2 = 3.1 \mu H$

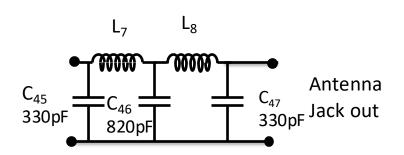
• 
$$Z_2 = -\frac{j}{(C_{38} + C_{39})\omega_o}$$
,  $Z_3 = jL_6\omega_o$ ,  $Z_1 = \frac{j}{C_{37}\omega_o}$ 

- $Z_{2,3-eq} = \frac{jL_6\omega_0}{L_6(C_{38}+C_{39})\omega_0^2-1}$  L<sub>6</sub>
- Resonance is when  $Z_{2,3-eq} \rightarrow \infty$ ,  $\omega_o^2 = \frac{1}{(C_{38}+C_{30})L_6} \approx \frac{10^{18}}{465}$ , when almost all the voltage drop is across  $Z_{2,3-eq}$   $\omega_o = \frac{10^9}{\sqrt{465}} \approx 50.8 \times 10^6$ ,  $f_0 = \frac{\omega_o}{2\pi} \approx 7.1$  MHz
- Q of filter is:  $Q_S = \frac{X_S}{R_S}$ .  $R_S$  comes from the other components and must be measured
- Note that  $Z_{2,3-eq}$  is small for the other modulation product



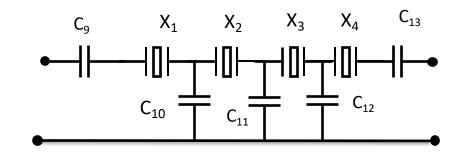
#### Exercise 13: Norcal Harmonic Filter

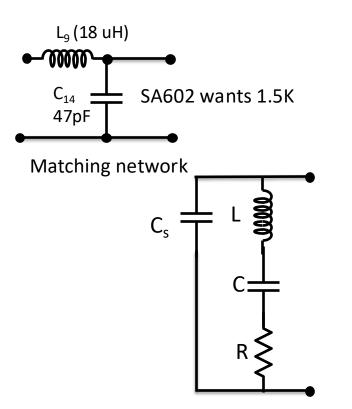
- L<sub>7</sub>, L<sub>8</sub> use T37-2 core, 18 turns, 1.3uH. Use  $50\Omega$  termination and set function generator at  $10V_{pp}$ .
- Compute and compare loss at 7MHz and 14MHz.
- 2. From  $A_l = 5nH/turn^2$ , calculate  $L_7$  and  $L_8$ .
- 3. What is the spur strength at 7, 14 and 28MHz? Measure and calculate.
- Need Puff (a simulator) to get losses. However, answer is there is a 6dB drop-off at every frequency doubling



#### Exercise 14: Norcal IF Cohn Filter

- X<sub>1</sub> through X<sub>4</sub> are 4.91 MHz
- C<sub>10</sub>, C<sub>11</sub>, C<sub>12</sub> are 270 pF
- Set function generator to  $50 \text{mV}_{pp}$  from function generator
- Calculate R and X for filter
- 1. Measure the resonant frequency of one of the crystals
  - Duh
- 2. Calculate the parameters of the crystal. Omitting  $\mathcal{C}_{\scriptscriptstyle S}$ 
  - $f_r=\frac{1}{2\pi\sqrt{LC}}$  and  $Q=\frac{1}{R}\sqrt{\frac{L}{C}}$ . We can measure  $f_r$  and find Q using the 3dB bandwidth. R is the resistance at resonance.
  - $Q \approx 80$
  - $25\Omega < R < 100\Omega$
  - If R = 50, C = 8.1pF,  $L = 130\mu H$



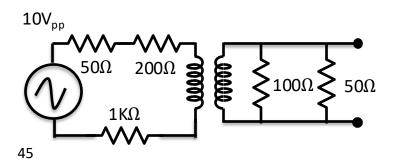


#### Transformers

- For solenoid,  $\oint B \cdot ds = \mu_0 nI$  inside
- $LI = \Phi_B$ . Since there are n turns in the solenoid, over the solenoid,  $LI = \mu_0 n^2 I$ , so  $L = \mu_0 n^2$ .
- This is the source of  $L = A_l n^2$
- $V_S = \frac{N_S}{N_p} V_p$   $Z_p = (\frac{N_p}{N_S})^2 Z_S$

# Exercise 15: Norcal Driver Transformers (1)

- T<sub>1</sub> uses FT 37–43.  $L(\mu H) = \frac{A_L t^2}{1000}$ ,  $A_L = 350$ .  $f_r = 7 \times 10^6 MHz$ ,  $n_p = 14$ ,  $n_S = 4$ ,  $\omega_r = 2\pi \times 7 \times 10^6 MHz = 4.4 \times 10^7$
- 1. Measure the output  $V_{out}$ .
- 2. Calculate  $V_{out}$ 
  - $L_p = 68.6 \mu H$ ,  $L_s = 5.6 \mu H$
  - $Z_{eq,in}(\omega) = 1250 + j(\omega L_p), Z_{eq,in}(\omega_r) = 1250 + 3016j, |Z_{eq,in}(\omega_r)| = 3264$
  - $Z_{eq,out}(\omega) = 33 + j\omega L_s, Z_{eq,out}(\omega_r) = 33 + j246, |Z_{eq,out}(\omega_r)| = 248$
  - $V_{t,in} = \frac{3016}{3264} V_{in}$
  - $V_{out} = V_{t,out} = \frac{n_s}{n_p} V_{t,in} = .29 V_{t,in} = .29 \times \frac{3016}{3264} \times 5 = 1.3 V$
  - $i_p(\omega) = \frac{V_{in}}{|Z_{eq,in}|} e^{j\theta_p(\omega)}$ ,  $\theta_p(\omega) = \arctan\left(\frac{\omega L_p}{1250}\right)$ ;  $i_s(\omega) = \frac{V_{out}}{|Z_{eq,out}|} e^{j\theta_s(\omega)}$ ,  $\theta_s(\omega) = \arctan\left(\frac{\omega L_s}{33}\right)$ .
  - $P_{in,a} = Re\left(\frac{V_{in}\overline{I_{in}}}{2}\right) = Re\left(\frac{V_{in}^2}{2|Z_{ea,in}(\omega)|}e^{j\theta_p(\omega)}\right)$
  - $P_{out,a} = Re\left(\frac{V_{out}\overline{I_{out}}}{2}\right) = Re\left(\frac{V_{out}^2}{2|Z_{eq,out}(\omega)|}e^{j\theta_s(\omega)}\right)$



T<sub>1</sub>, 14:4

### Exercise 15: Norcal Driver Transformers (2)

- $\cos(\theta_s(\omega_r)) = .13, \cos(\theta_p(\omega_r)) = .38,$
- $\frac{P_{out,a}(\omega_r)}{P_{in,a}(\omega_r)} = \left(\frac{V_{out}}{V_{in}}\right)^2 \frac{|Z_{eq,in}(\omega_r)|}{|Z_{eq,out}(\omega_r)|} \frac{\cos(\theta_s(\omega_r))}{\cos(\theta_p(\omega_r))} = \left(\frac{1.3}{5}\right)^2 \times \frac{3264}{248} \times \frac{.13}{.38} = .3$
- 3. Measure the 3dB cutoff,  $f_c$ .
- $\frac{P_{out,a}(\omega)}{P_{in,a}(\omega)} = \left(\frac{V_{out}}{V_{in}}\right)^2 \frac{|Z_{eq,in}(\omega)|}{|Z_{eq,out}(\omega)|} \frac{\cos(\theta_s(\omega))}{\cos(\theta_p(\omega))} = .15$

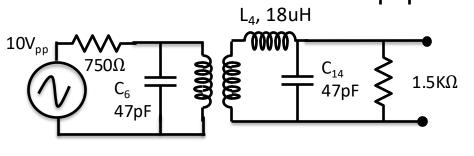
#### Exercise 16: Norcal Tuned Transformers

 $\begin{array}{c|c} & & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ &$ 

 $T_2$ , 1:20

T<sub>3</sub>, 23:6

- $T_2$ ,  $T_3$  are IF matchers using FT 37–61.  $A_L = 55 \, nH/turn^2$ .
- 1. Measure 3dB bandwidth
- 2. Find  $P/P_+$
- T<sub>2</sub>
  - $P_a = Re\left(\frac{V\bar{I}}{2}\right)$ ,  $V = V_+ + V_-$ ,  $\rho = \frac{V_+}{V_-} = \frac{Z Z_0}{Z + Z_0}$ , Z is look forward,  $Z_0$  is look back resistance.  $P_+ = \frac{V_+^2}{2Z_0}$ .  $L_{in} = 55nH$ ,  $L_{out} = 22\mu H$ ,  $\omega = 4.4 \times 10^7$
  - Z = 50 + 2.4j,  $Z_0 = 203 4030j$ ,  $\rho = 1$ , so  $V_+ = V_-$ ,  $V = 2V_+$
  - $\bullet \qquad \frac{P}{P_+} = \frac{1}{4}$
- Similar calculation for T<sub>3</sub>.



#### Acoustics

- $P = P_0 + P_{\rho}, \rho = \rho_0 + \rho_{\rho}$
- Gas moves and changes density: Displacement of undisturbed air is x. At time t, it's at  $x + \chi(x, t)$ , so  $\rho_0 \Delta x = \rho(x + \Delta x + \chi(x + \Delta x, t) - x - \chi(x, t))$ , or  $\rho_0 \Delta x = \rho(\frac{\partial \chi(x,t)}{\partial x} \Delta x + \Delta x)$ . So,  $\rho_e = -\rho_0 \frac{\partial \chi}{\partial x}$
- 2. Change in density causes change in pressure:  $P = f(\rho)$ ,  $P_0 + P_e = f(\rho_0 + \rho_0)$  $(\rho_e) = f(\rho_0) + \rho_e f'(\rho_0), f'(\rho_0) = \kappa = (\frac{dP}{d\rho})_0, \text{ or } P_e = \kappa \rho_e$
- Pressure differences cause motion:  $P(x,t) P(x + \Delta x, t) = -\frac{\partial P_e}{\partial x} \Delta x$ , Newton's law gives  $\rho_0 \frac{\partial^2 \chi}{\partial t^2} = -\frac{\partial P_e}{\partial x} = -\kappa \frac{\partial \rho_e}{\partial x}$ Substituting (1) into (3) gives  $\frac{\partial^2 \chi}{\partial t^2} = \kappa \frac{\partial^2 \chi}{\partial x^2}$ , put  $\kappa = \frac{1}{C_s^2}$
- Solution is  $\chi(x,t) = f(x-vt)$  [Different f than above].
- To find,  $\kappa = (\frac{dP}{d\rho})_0$ , note that the flow is adiabatic so  $PV^{\gamma} = C'$  and  $\rho$  varies inversely as V, so  $P = \rho^{\gamma}C$ , and finally, using PV = Nkt,  $\kappa = (\frac{dP}{do})_0 = \frac{\gamma kT}{r}$
- $L_p = 20 \log(\frac{P}{P_0}), P_0 = 20 \,\mu Pa$

Sound	L <sub>p</sub>	Power density
rustling leaves	10dB	1pW/m²
broadcast studio	20dB	1pW/m²
classroom	50dB	10nW/m²
heavy truck	90dB	1nW/m²
Shout at 1m	100dB	10mW/m²
jackhammer	110db	100mW/m <sup>2</sup>
jet takeoff at 50m	120dB	1W/m²

### Bipolar Transistors - I

#### NPN Model

- $V_f \approx .7V$ ,  $V_S \approx .2V$
- Conducts when  $V_{be} > V_f$
- $i_c = \beta i_b$
- $i_c = \alpha i_e$
- $\beta = \frac{\alpha}{1-\alpha} [= h_{fe}$ , small signal]
- $\beta \approx 100, \beta_r \approx 10$
- $r_e i_e = 25 mV$ ,  $r_b = (1 + \beta) r_e$ ,  $r_e \approx 33 \Omega$

active

saturated

saturated

cutoff

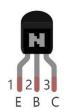
 $< V_f$   $< V_f$ 

rev

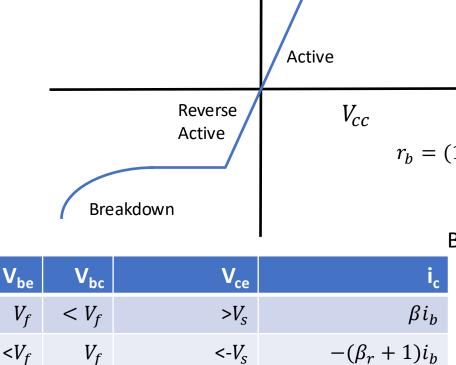
- $i_b = \frac{v_{be}}{(1+\beta)r_e}$
- $g_m v_{be} = g_m r_b i_b$

#### Switch

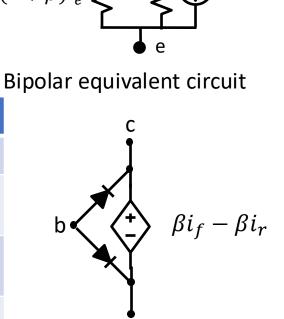
- $G_S = \frac{i_b}{15mV}$
- $R_S = 2\Omega$







 $V_s > V_{ce}$ 



Bipolar source model

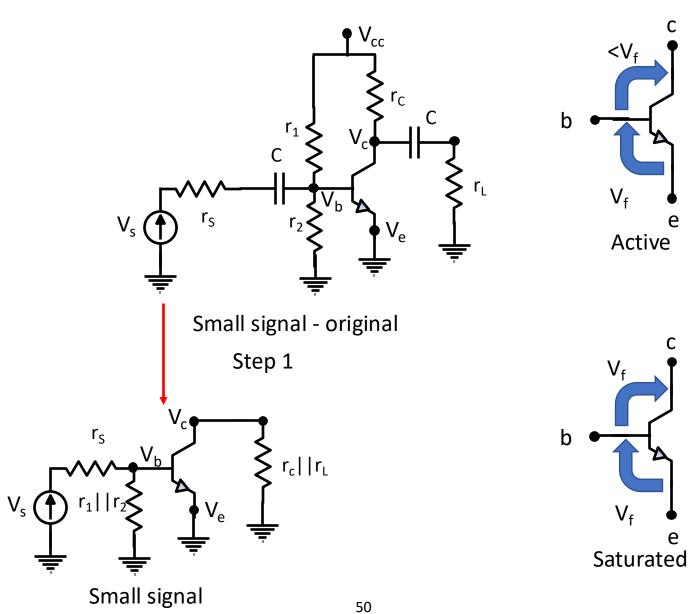
 $>-(\beta_r+1)i_b$ 

Saturation

Breakdown

### Bipolar Transistors - II

- NPN Mode
  - $V_f = .7V$
  - $\beta = g_m r_{\pi}$
  - $g_b = \frac{i_b}{V_t}$ ,  $V_t \approx 25 mV$ ,  $g_m = \frac{i_c}{V_t}$
- DC
  - $\frac{V_{cc}-2V_f}{R_C} < i_c, \beta i_b = i_c$
  - $V_c = V_{cc} i_c R_C$
  - $\bullet \quad \frac{V_{cc} V_b}{R_B} = i_b$
- Small signal
  - 1. Convert to AC only and simplify
  - 2. Thevenize circuit
  - 3. Replace transistor with model



# Bipolar Transistors - III

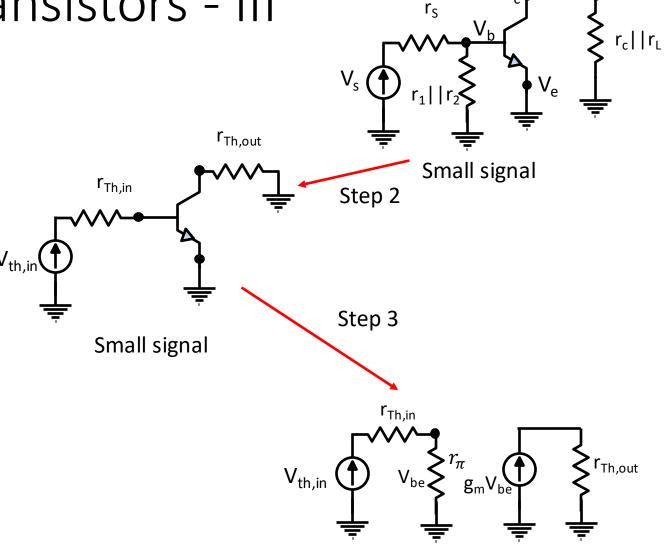
- Small signal
  - 1. Convert to AC only and simplify
  - 2. Thevienize

• 
$$V_{th,in} = V_S \frac{r_1||r_2|}{r_1||r_2+r_S|}$$

- $r_{th,in} = r_s ||r_1||r_2|$
- $r_{th,out} = r_C || r_L$
- 3. Replace transistor with model

$$\bullet \quad \frac{V_{out}}{V_{be}} = -g_m \, r_0 ||r_c||r_L$$

- $r_0$  is the transistor model resistance between b and c
- $A_{gail} = \frac{V_{out}}{V_S}$



# Bipolar transistors - IV

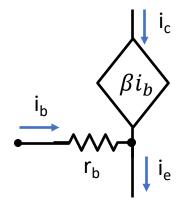
- At saturation,  $v_{bc} < V_f$ , so there is conduction from the collector to the base.
- $i_b=i_{bs}\exp(\frac{V_b}{V_t})$ ,  $V_t$  is the thermal voltage,  $V_t=25mV$ ,  $i_{bs}$  is the base saturation current.
- $i_c = i_{cs} \exp\left(\frac{V_c}{V_t}\right)$ . Note  $i_{cs} = \beta i_{bs}$ . Both increase rapidly with temperature
- Base resistance

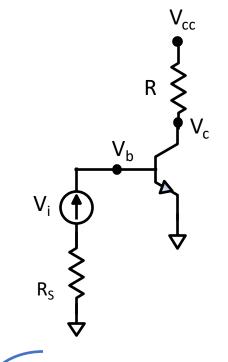
$$\bullet \quad g_b = \frac{i_b}{V_t} = \frac{di_b}{dV_b}$$

• 
$$r_b = \frac{25mV}{i_b}$$

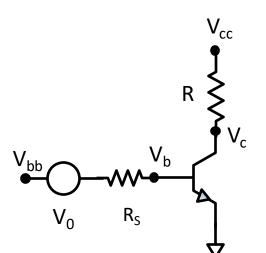
• 
$$g_m = \frac{i_c}{V_t} = \frac{di_c}{dV_h}$$

• 
$$i_b = r_b V_b$$



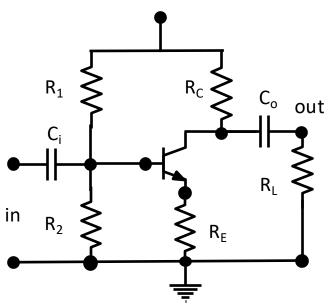




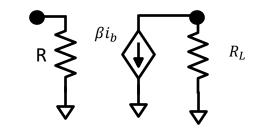


# More on bipolar transistor model

- $v_{R_2} = v_{be} + (i_c + i_b)R_E$
- $\bullet \quad i_{R_2} = \frac{v_{R_2}}{R_2}$
- $i_{R_1} = i_{R_2} + i_b$
- $v_{cc} = R_1 i_b + (R_1 + R_2) i_2$
- For  $R_B = R_1 || R_2$ ,  $v_{cc}R_B v_{be}R_1 = R_1R_2i_b + (i_c + i_b)R_1R_E$ ,  $i_c = \beta i_b$
- $i_C = \frac{v_{cc} \frac{R_B}{R_1} v_{be}}{R_E + \frac{(R_C + R_E)}{\beta}}$
- If  $R_E \gg \frac{(R_C + R_E)}{\beta}$ ,  $\frac{\partial i_c}{\partial v_{be}} = -\frac{1}{R_E}$ , be acts like diode so  $i_c = i_s \beta \exp(\frac{V_{be}}{V_T})$ . Want  $V_E \approx 2v$



Small signal equivalent



$$R = R_1 ||R_2||r_{\pi}$$

$$r_e = \frac{V_T}{i_c}, \quad r_{\pi} = r_e(\beta + 1)$$

# More on bipolar transistor model

• 
$$v_{be} = v_b - v_e$$
,  $v_{ce} = v_c - v_e$ ,  $v_{bb} = \frac{R_2}{R_1 + R_2} v_{cc}$ ,  $v_f \approx .6$  (for Si)

• 
$$v_b = v_e + v_f$$
,  $i_b = \frac{v_{bb} - v_b}{R_b}$ 

• 
$$i_c = \beta i_b + i_{ceo}, \frac{\partial i_b}{\partial v_{be}} = \frac{1}{r_d}$$

• 
$$\frac{\partial i_c}{\partial v_{be}} = g_S = -\frac{1}{R_B}$$
, and  $\frac{\partial i_c}{\partial \beta}$  measure stability

• 
$$i_b = \frac{v_{bb} - v_b}{R_b}$$

• 
$$i_c = \frac{\beta(v_{bb} - v_{be})}{R_b + (1+\beta)R_e} + \frac{(R_b - R_e)}{R_b + (1+\beta)R_e} i_{ceo}$$
,  $i_{ceo}$  is leakage current

• So, if 
$$\beta R_e \gg R_b + R_e$$
,  $i_c = \frac{v_{bb} - v_{be}}{R_e} = \frac{v_{cc} - v_c}{R_c}$ 

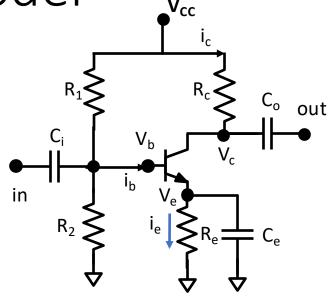
• 
$$Z_{in} = R_1 ||R_2|| (\beta + 1) R_e, Z_{out} = R_c$$

• 
$$v_{bb} - v_{be} = \frac{R_e}{R_c} (v_{cc} - v_c)$$

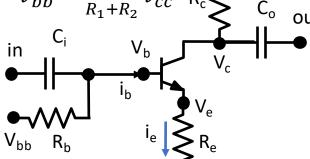
• Typical for Si: 
$$v_{be}=v_f\approx .6V$$
,  $\beta\approx 200$ ,  $v_{cc}=9V$ ,  $v_{bb}=3V$ ,  $R_b=10^4\Omega$ ,  $R_c=10^3\Omega$ ,  $R_e=270\Omega$ 

• 
$$3 - .6 = \frac{270}{1000}(9 - v_c)$$
, so  $v_c = .2V$ 

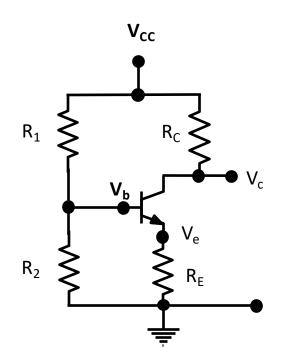
• For voltage divider:  $R_1 = 2 \times 10^4 \Omega$ ,  $R_2 = 10^4 \Omega$ ,



# Equivalent • $R_b = R_1 || R_2$ • $v_{bb} = \frac{R_1 R_2}{R_1 R_2} v_{cc}$ • $v_{cc} = \frac{R_1 R_2}{R_1 R_2} v_{cc}$



#### Transistor experiment



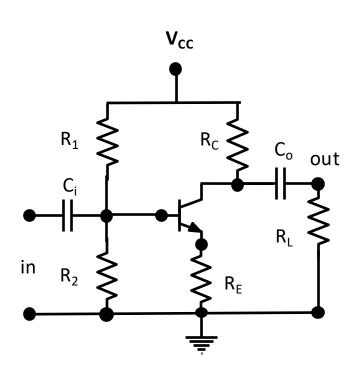
#### **Experiment A**

- $V_{cc}=9V$ ,  $R_1=22.8k\Omega$ ,  $R_2=7.2k\Omega$ ,  $R_c=1k\Omega$ ,  $R_E=220k\Omega$ . 2n3904 transistor,  $\beta=150$ .
- With no transistor,  $R_2$  adjusted so  $V_b = 2.36V$ .  $V_b = 2.24V$ ,  $V_e = 1.54V$ ,  $V_c = 1.89V$ .  $i_c = 7mA$ ,  $i_b = 46\mu A$ .

#### • Experiment B

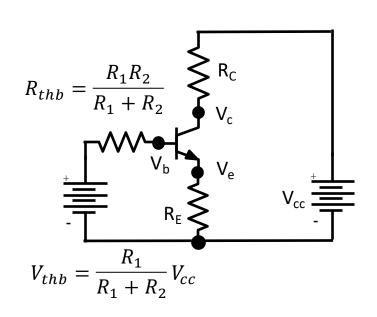
- Again,  $V_{cc}=9V$ ,  $R_1=20k\Omega$ ,  $R_2=10k\Omega$ ,  $R_c=1k\Omega$ ,  $R_E=220\Omega$ . 2n3904 transistor,  $\beta=150$ . With no transistor,  $R_2$  adjusted so  $V_b=5.8V$ . Put transistor in and  $V_b=2.4V$ .
- With transistor,  $V_b = 2.4V$ ,  $V_e = 1.7V$ ,  $V_c = 1.74V$ .  $i_c = 7mA$ ,  $i_b = 46\mu A$ .
- Analyze these with our transistor model.
- Now use the Thevenin equivalents to analyze them.

# Turn the transistor experiment into a CE amplifier



- Add C<sub>i</sub> and C<sub>o</sub>. Component values are:
  - $C_i = C_o = 1 \mu F$
  - $R_1 = 20k\Omega, R_2 = 10k\Omega$
  - $R_C = 1k\Omega$ ,  $R_E = 220\Omega$
  - $V_{cc} = 9V$
- 1. Use a function generator to generate a  $V_{pp}=800mV$ , 10kHz.
- 2. The input impedance is  $Z_{in} = R_1 ||R_2|| (\beta + 1) R_E$ , and the output impedance is  $Z_{out} = R_C$ . Add a load  $R_L$  whose value is  $Z_{out}$ .
- 3. Now connect a scope to the output and measure the gain. Calculate what it should be an compare them. How do the input and output waveforms compare?

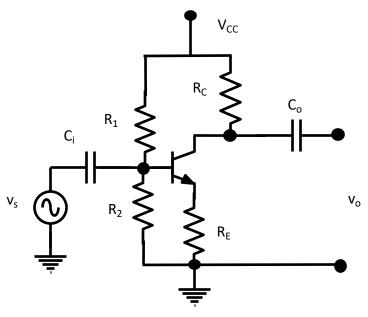
# Transistor experiment - Thevenin equivalent DC



- In Experiment A
  - $R_1 = 22.8k\Omega$ ,  $R_2 = 7.2k\Omega$ ,  $V_{thb} = 2.16V$ ,  $R_{th} = 5.5k\Omega$ .
  - If  $r_e \approx 33\Omega$ ,  $r_b \approx 5k\Omega$ ,  $i_b = \frac{2.16 1.54}{11500} = 53\mu A$ , which is close.
- In Experiment B
  - $R_1 = 22k\Omega$ ,  $R_2 = 8k\Omega$ ,  $V_{thb} = 2.4V$ ,  $R_{th} = 5.9k\Omega$ .
  - If  $r_e \approx 33\Omega$ ,  $r_b \approx 5k\Omega$ ,  $i_b = \frac{2.4-1.7}{10900} = 64\mu A$ , which is also close, but a little high.
- Turn this into a CE amplifier by adding 1uF input and output capacitors.
   Measure and calculate the voltages and gains.

### BJT common emitter amplifier

• Here's how to design a common emitter amplifier. We use a 2n3904 transistor with  $\beta$ =150. This circuit will work! Build it.

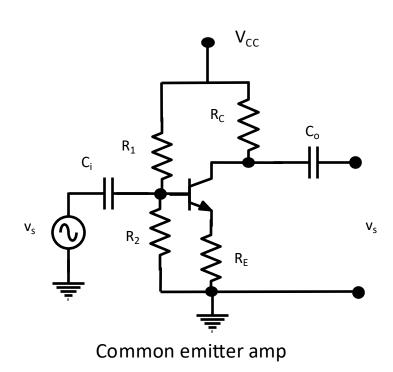


Common emitter amp

Credit: Ward, Hands on Radio.

- 1. Pick the supply voltage  $V_{cc}$ =12V.
- 2. Choose a gain (amplification factor), A = 5.
- 3. Choose the "Q point" of the conducting transistor (4mA) and  $V_{ce,q} = 5v$ .
- 4.  $V_{cc} = (i_c \cdot R_C) + V_{ce} + i_e R_E \sim i_e \cdot (R_C + R_E) + V_{ce}$  with  $i_c = 4mA$ . We get  $(R_C + R_E) = (V_{cc} V_{ce})/(4mA) = 1.75 \text{ k} \Omega$ .
- 5. Since A = 5 and A=R<sub>C</sub>/R<sub>E</sub>, R<sub>C</sub>= 5 R<sub>E</sub> so R<sub>E</sub>  $\sim$  270  $\Omega$  (this is a standard resistor value) and R<sub>C</sub>= 1.5k $\Omega$ .
- $Z_{in} = \beta R_E$
- $Z_{out} \approx R_C$
- $\frac{V_o}{V_i} = \frac{\beta R_c}{r_\pi + (\beta + 1)R_E}$

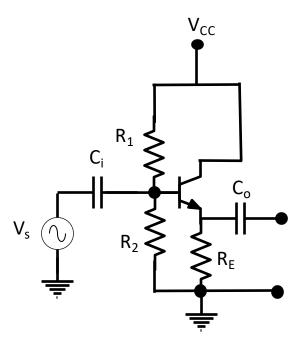
### BJT common emitter amplifier continued



Credit: Ward, Hands on Radio.

- 6.  $i_b = 4\text{mA}/\beta = 27 \,\mu\text{A}$ .
- 7. Since  $V_{be}$  must be greater than .7V throughout the input signal range, we want the voltage across  $R_2$  to satisfy  $V_{be} + i_c R_E = 1.8V$ .
- 8. Rule of thumb is current through R<sub>1</sub> and R<sub>2</sub> is  $10i_b$ . We insert a voltage divider consisting of R<sub>1</sub> and R<sub>2</sub>, so that R<sub>1</sub>= (12-1.8)/270  $\mu$ A  $\sim$  39 k $\Omega$ .  $R_2=6.7k\Omega$
- 9.  $C_o$  and  $C_i$  are picked to offer small resistance to the frequency range we're interested in and  $C_o = C_i = 5 \mu F$ .
- I haven't explained why we want  $R_E$  but it provides thermal stability for the transistor over the range we care about. The fact that  $A=R_C/R_E$  can be calculated using Kirchhoff's laws.

# BJT common collector amplifier



1. 
$$\beta = 150, A_V = 1, V_{CC} = 12v$$

2. Q-pt: 
$$i_{ce} = 5mA$$
,  $V_{ce,q} = 6v$  (rule of thumb),  $v_{be} = .7V$ .

3. 
$$i_{R_1 \to R_2} = 10i_b$$
 (ROT),  $V_{ce} = v_{be} + i_{ce,q}R_E$ ,  $R_E = 1.2k\Omega$ ,  $i_b = \frac{V_{ce,q}}{\beta} = 33\mu A$ 

4. 
$$V_{R_2} = V_{be} + i_C R_E = 6.7V$$
,  $V_{R_1} = 5.3V$ 

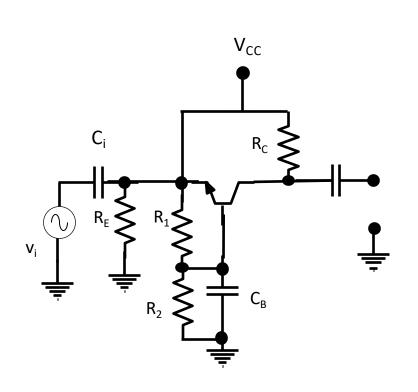
5. 
$$R_2 = \frac{6.7}{330\mu A} = 20k\Omega, R_1 = \frac{5.3}{330\mu A} = 16k\Omega$$

6. 
$$Z_{in} = R_1 ||R_2|| (\beta + 1) R_E, Z_{out} = R_E ||Z_E, Z_E|| = \frac{R_1 ||R_2|}{(\beta + 1)} + r_e'$$

7. 
$$R_{in} = 50\Omega$$
,  $Z_{out} = 5\Omega$ 

Common collector amp (Emitter Follower)

### BJT common base amplifier



• 
$$A_I = \frac{i_C}{i_E} = \frac{\beta}{\beta + 1}$$
,  $A_V = \frac{R_C || R_L}{r_e}$ ,  $Z_{out} \approx R_C$ 

1. 
$$V_{CC} = 12, V_{be} = .7V, R_E = 50\Omega, R_L = 1k\Omega, i_{ce,q} = 5mA, V_{ce,q} = 6V$$

2. 
$$i_b = \frac{i_{ce,q}}{\beta} = 33\mu A$$
,  $i_{R_1 \to R_2} = 10$   $i_b = 330\mu A$  (ROT)

3. 
$$V_{R_2} = V_{be} + i_C R_E = 6.7V, V_{R_1} = 5.3V$$

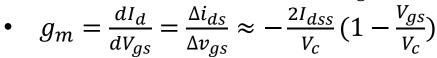
4. 
$$R_1 = \frac{5.3}{330\mu A} = 16k\Omega$$
,  $R_C = \frac{V_{cc} - i_{c,Q} R_E - V_{ce,Q}}{i_{c,Q}} = 1.35k\Omega$ 

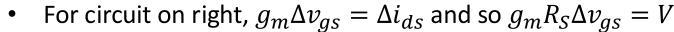
5. 
$$A_V = \frac{R_C || R_L}{^{26} / i_e} = 115$$

Common base amp

#### **JFETs**

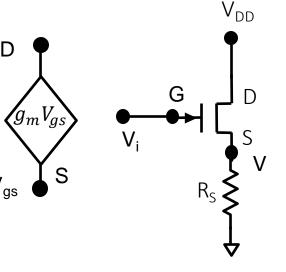
- JFET circuit model (active region):
  - $I_d=I_{dss}\,(1-\frac{V_{gs}}{V_c})^2$ , provided  $0< v_{gs}< V_c$  and  $V_{ds}>V_{gs}-V_c$ .  $i_{dss}$  is drain to source current when gate is at 0.  $v_{gs}\leq 0$

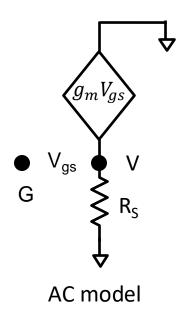




- $V_c$  is cutoff voltage. When  $v_{gs} < V_C$  there's no channel conduction. Some people call this  $V_T$  or  $V_P$ . JFET input impedance is high  $(10^{10}\Omega)$ .
- For J309,  $V_c \approx -2.6V$ ,  $i_{dss} \approx 23mA$ ,  $g_m \approx 12$ .
- DC:  $V_b = -i_b R_S$ , AC:  $V = R_S g_m V_{gS}$ ,  $v_{gS} = V_g V_g$
- $\bullet \quad V = R_S g_m v_{gs}$
- $v_{gs} = V_i V_{\bullet}V = \frac{RV_i}{R + \frac{1}{g_m}}$
- $G_v = \frac{V}{V_i} = \frac{Rg_m}{1 + Rg_m} \approx 1$
- $Z_0 = \frac{1}{g_m}$

Region	Characteristic	
ohmic	$i_d$ linear in $v_{ds}$ , $v_{gs} < 0$	
active	$v_{gs}$ controls $i_d$ linearly, $v_{gs}$ <0	
breakdown	v <sub>ds</sub> is so high channel breaks	
Pinch-off	V <sub>gs</sub> <<0 and i <sub>d</sub> =0 independent of	
	$v_{ds}$	



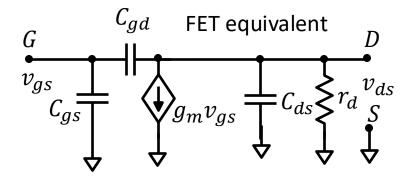


#### **FETs**

• 
$$\Delta i_d = \frac{\partial i_d}{\partial v_{GS}} \Delta v_{GS} + \frac{\partial i_d}{\partial v_{DS}} \Delta v_{DS}$$

$$rac{\partial i_d}{\partial v_{GS}}=g_m$$
,  $rac{\partial i_d}{\partial v_{DS}}=g_d$ ,  $r_d=rac{1}{g_d}$ 

- $\begin{array}{l} \bullet \quad \Delta i_d = \frac{\partial i_d}{\partial v_{GS}} \Delta v_{GS} + \frac{\partial i_d}{\partial v_{DS}} \Delta v_{DS} \\ \bullet \quad \frac{\partial i_d}{\partial v_{GS}} = g_m, \\ \frac{\partial i_d}{\partial v_{DS}} = g_d, \\ r_d = \frac{1}{g_d} \\ \bullet \quad i_d = g_m v_{gS} + \frac{v_{dS}}{r_d} \approx g_m v_{gS}, \\ \text{since } r_d \text{ is large} \end{array}$
- $Z_{in} = 10^9 \Omega$
- $Z_{out} = R_D ||r_d|| \frac{1}{i\omega(C_G s + C_D s)}$



#### More on FETs

#### For common source

• 
$$R_o = [r_d + R_S(1 + g_m r_d)] ||R_D$$
, if  $r_d \gg R_S$ ,  $R_D$ ,  $R_o \approx R_D$ 

• 
$$R_i = R_G = R_1 || R_2$$

• 
$$v_i = v_{gs} + i_d R_S = v_{gs} (1 + g_m R_S)$$

• 
$$v_o = -i_d(R_D||R_L) = -g_m v_{gs}(R_D||R_L)$$

• 
$$A_{v} = -\frac{R_{D}||R_{L}|}{R_{S}+^{1}/g_{m}}, A_{i} = -\frac{R_{G}}{R_{S}+^{1}/g_{m}} \frac{R_{D}}{R_{D}+R_{L}}$$

• 
$$R_G = 10^6 \Omega$$
,  $R_S = 10^4 \Omega$ ,  $R_D = 25 k\Omega$ ,  $g_m = 2000 \mu S$ ,  $g_d = 20 \mu S = \frac{1}{r_d}$ 

#### For common drain

• 
$$R_i = R_G = R_1 || R_2$$

• 
$$i_o = \frac{v_{gs}}{R_S} + g_m v_{gs}$$
,  $R_o = \frac{i_o}{v_{gs}} = \frac{1}{R_S} + g_m$ 

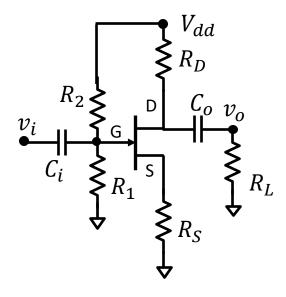
• 
$$v_0 = g_m v_{gs}(R_S||R_L), v_i = v_{gs} + g_m v_{gs}(R_S||R_L)$$

• 
$$A_v = -\frac{g_m(R_S||R_L)}{[1+g_m(R_S||R_L)]}, A_i = -\frac{R_G}{R_S+R_L} \frac{R_S}{[(R_S||R_L)+1/g_m]}$$

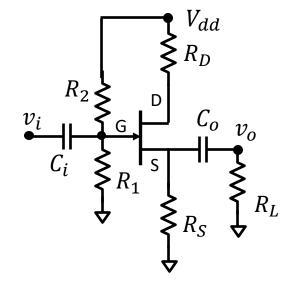
• 
$$R_o = \frac{1}{\frac{1}{r_d} + \frac{1}{R_S} + g_m} \approx 196\Omega$$
,

• 
$$R_G = 10^6 \Omega$$
,  $R_D = 100k$ ,  $R_S = 10^4 \Omega$ ,  $R_L \approx 10^6 \Omega$ 

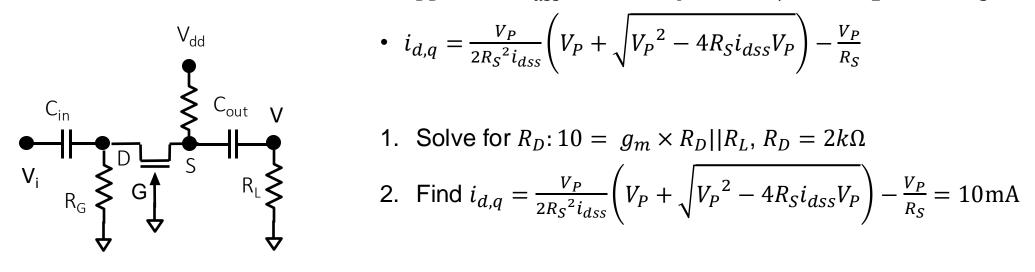
#### FET common source



#### FET common drain



### JFET common gate amplifier



• 
$$A_V = g_m(R_D||R_L), Z_{out} \approx r_0(g_m R_S + 1)||R_D, Z_{in} = R_S||\frac{1}{g_m}|$$

• 
$$V_{DD} = 12V$$
,  $i_{dss} = 60mA$ ,  $V_P = -6$ ,  $A_V = 10$ ,  $R_L = 1k\Omega$ ,  $R_S = 50\Omega$ 

• 
$$i_{d,q} = \frac{V_P}{2R_S^2 i_{dss}} \left( V_P + \sqrt{{V_P}^2 - 4R_S i_{dss} V_P} \right) - \frac{V_P}{R_S}$$

1. Solve for 
$$R_D$$
:  $10 = g_m \times R_D || R_L$ ,  $R_D = 2k\Omega$ 

2. Find 
$$i_{d,q} = \frac{V_P}{2R_S^2 i_{dss}} \left( V_P + \sqrt{V_P^2 - 4R_S i_{dss} V_P} \right) - \frac{V_P}{R_S} = 10 \text{ m/s}$$

#### Mosfet

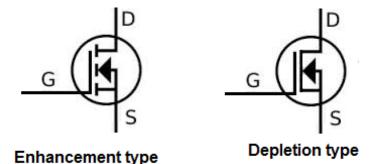
• 
$$r_{out} = \frac{1}{\lambda i_d} = \frac{\partial i_{ds}}{\partial V_{ds}}$$
,  $g_m = \frac{\partial i_d}{\partial V_{gs}}$ 

- Weak Inversion ( $V_{gs} < V_{th}$ )
  - $i_d = i_0 \exp(\frac{V_g V_{th}}{nV_t})$ ,  $n = 1 + \frac{C_{th}}{C_{ox}}$
- Linear ( $V_{gs} > V_{th}$ ,  $V_{ds} < V_{gs} V_{th}$ )

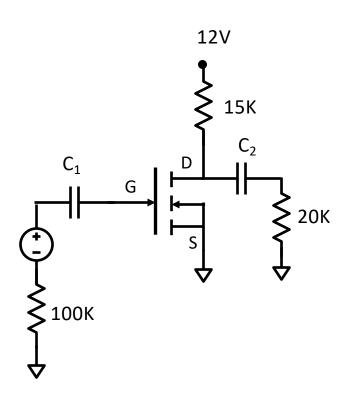
• 
$$i_d = \mu_n C_{ox} \frac{W}{L} [(V_{gs} - V_{th})V_{ds} - \frac{V_{ds}^2}{1}] (1 + \lambda V_{ds})$$

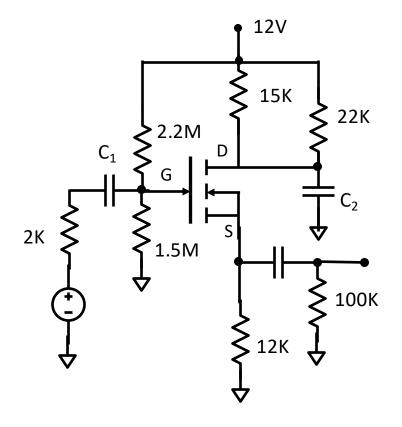
- Saturation ( $V_{gs} > V_{th}, V_{ds} \ge V_{gs} V_{th}$ )
  - $i_d = \mu_n C_{ox} \frac{W}{2L} (V_{gs} V_{th})^2 [1 + \lambda (V_{ds} V_{dsat})]$

#### N channel MOSFET

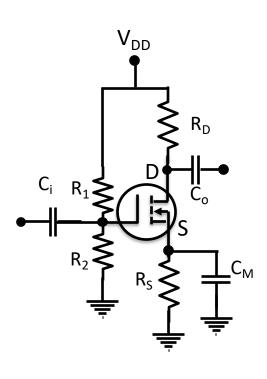


# Mosfet amps



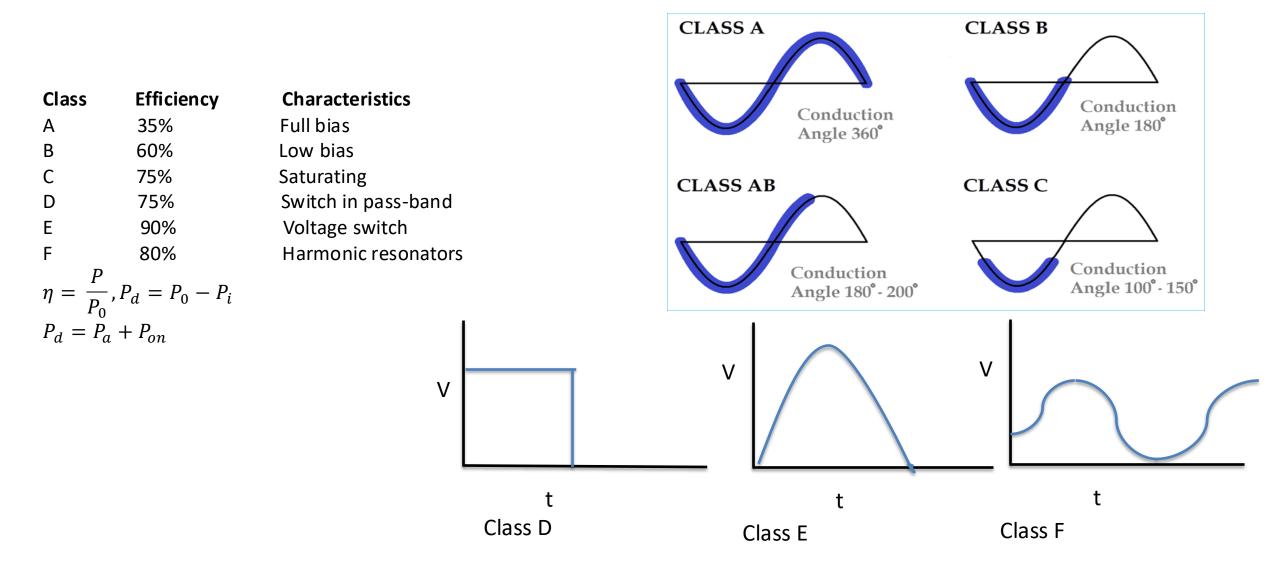


# CMOS common emitter amplifier



- Pick power
- $V_{DD} = i_D R_D + V_{DS} + i_D R_S$
- $V_{GS} = V_G i_S R_S$
- $V_G = V_{DD} \frac{R_1}{R_1 + R_2}$
- $i_D = k(V_G V_{TH})^2$
- Bias around  $\frac{V_{DD}}{3}$
- Pick gain,  $A = \frac{R_D}{R_S + \frac{1}{g_m}}$
- For 2N7000,  $g_m \approx 200$

# Amplifier classes

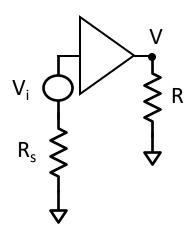


### Efficiency of class A amplifiers

- Here,  $P_o$  is the power from the supply,  $P_d$  is the dissipated power, P is the output power. R is the collector resistor.
- $\eta = \frac{P}{P_0}$ ,  $P_0$  is DC power
- $P_0 = V_{cc}I_0$ , where  $I_0 = \langle i_c \rangle$ , so  $I_0 = \frac{V_{cc}}{2R}$  (R is the collector resistance). Thus,  $P_0 = \frac{V_{cc}^2}{2R}$ .
- AC load power is  $P = \frac{V_{pp}I_{pp}}{8} = \frac{V_{cc}^2}{8R}$ . So maximum efficiency  $\eta = \frac{P}{P_0} = 25\%$ .
- DC load power is  $\frac{V_{cc}^2}{4R}$  and so is transistor power.
- Half the power in a class A is lost to load resistance. If we replace resistance with transformer,  $P_0 = \frac{{V_{cc}}^2}{R'}$ , where R' is the effective load resistance and  $P = \frac{{V_{pp}I_{pp}}}{8} = \frac{{V_{cc}}^2}{2R'}$ , giving 50% efficiency. Transformer turns ratio controls peak-to-peak current. Maximum current is  $I_m = \frac{2V_{cc}}{R'} = \frac{2V_{cc}}{n^2R}$ , where n is the turns ratio.

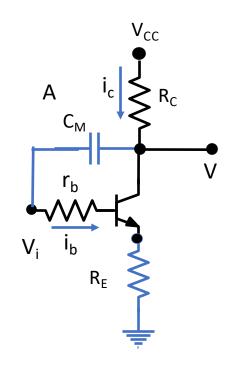
# Amplifier gain

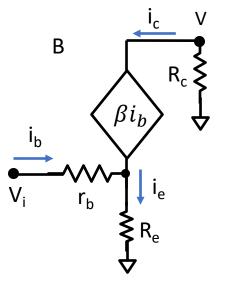
- Let  $P_+$  be the maximum input power (when load is matched) and  $V_+$  is the voltage at maximum power.  $V_+ = \frac{V_0}{2}$
- $G = 10\log(\frac{P}{P_+})$
- $P = \frac{V_{pp}^2}{8R}$
- $P_+ = \frac{V_{+,pp}^2}{8R_s}$
- $G_S = 10\log(\frac{V}{V_+})$



# Emitter degeneration

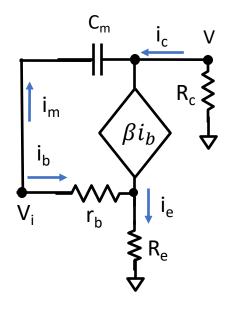
- To the usual transistor circuit (A), on the right, we add  $R_E$ . (B) is an equivalent circuit.
- $V_{bb} \approx V_f + i_c R_E$ . Let V be the output AC and  $V_i$  be the input AC.
- The gain is  $G_v = \frac{V}{V_i}$ .
- $V_i = i_b r_b + i_E R_E \approx i_C R_E$ ,  $Z_i = \frac{V_i}{i_b}$ ,
- $V = -i_c R_C$ .
- So  $G_v = -\frac{R_C}{R_E}$  (Doesn't depend on  $\beta$ ).
- $V_i \approx \beta i_b R_E$   $Z_i = \frac{V_i}{i_b}$ , so  $Z_i = \beta R_E$ .

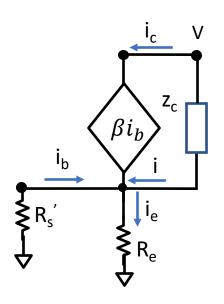




# Emitter degeneration

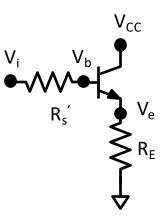
- $C_M$  is called a Miller capacitor and it arises from a capacitance,  $C_C$ , between the collector and emitter.  $i_m = j\omega C_C(V_i V) = j\omega C_M(1 + |G_v|)V_i$ .  $i_m$  is the maximum current between base and emitter in the equivalent circuit on the right.
- With the Miller capacitor,  $Z_i = \beta R_E ||(1 + |G_v|)C_M$
- $r_c \approx \frac{V_{early}}{i_c}$ ,  $r_c$  is the collector resistanc.e
- $R_S' = R_S + r_b$ ,  $r_b$  is the base resistance.  $R_S'$  is the combined source resistance.
- $z_C$  is called the collector impedance and  $z_C = r_C || C_C$ ,  $C_C$  is specified in data sheet (8pF).
- $Z_o = \frac{V}{i_C}$ ,  $i = i_C \beta i_b$ ,
- $i_b = -\frac{i_C R_S}{R_S' + R_E}$ ,
- $i = i_c (1 + \frac{\beta R_E}{R_S' + R_E})$
- $V = iz_C + i_C (R_S'||R_E)$
- $Z_o = \frac{V}{i_C} = z_C \left( 1 + \frac{\beta R_E}{R_S' + R_E} \right) + R_S' ||R_E|$
- $|z_c| \gg R_E$ , so  $Z_o = z_C \left( 1 + \frac{\beta R_E}{R_S' + R_E} \right)$





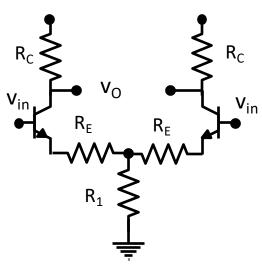
### More on emitter follower

- $Z_0 = \frac{v_e}{i_e}$   $v_b = -R_S'i_b$ ,  $R_S' = R_S + r_b$   $i_e \approx \beta i_b$   $Z_0 \approx \frac{R_S'}{\beta}$



# Differential Amplifier

- Two port model

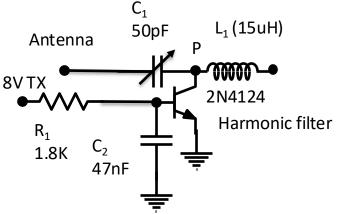


Differential amplifier

- Pick power 12
- Choose collector current (2mA) by picking  $R_1$
- Pick gain,  $A = \frac{R_C}{2R_E}$
- $G_d = -\frac{R_c}{R_e}$
- $Z_d = 2R_c$

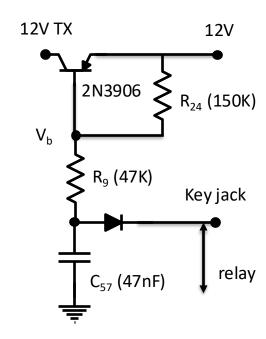
### Exercise 19: Norcal receiver switch

- 1. Consider the rising part of the base voltage waveform. Calculate slope.
- 2. Do the same for the falling part for voltage below .6V. Calculate  $t_2$ .
- 3. Measure the switch attenuation
  - When the transistor is saturated, the drop across ce is 1.4V. At full power,  $P = \frac{V_m^2}{8R}$  and  $V_m = 33.9V$ .  $\frac{P_{new}}{P_{original}} = \frac{1}{33.9^2}$ , so  $loss = 10 \log \left(\frac{1}{33.9^2}\right) = -31 dB$ .
- 4. Measure the voltage with the switch on. Measure output voltage and calculate on-off rejection ratio  $R=20 \log(V_{off}/V_{on})$



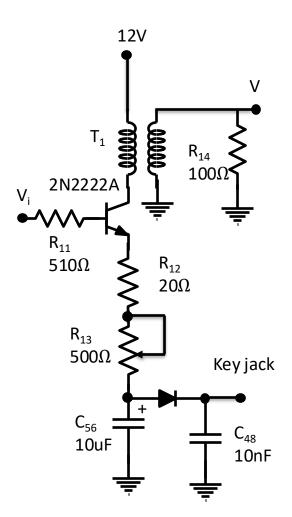
### Exercise 20: NorCal transmitter switch

- For transmitter switch, saturation resistance is  $\approx 2\Omega$ ,  $G_S = \frac{i_b}{15mV}$ .
- i is current into the load. In Norcal, i=7mA. For 2n3906, to ensure saturation,  $i_b=\frac{2i}{100}=140\mu A$ .
- 1. Calculate voltage on  $C_{57}$ . Measure time for capacitor to charge half-way. Calculate what the time should be.
  - $\tau = 197 \times 10^4 \times 47 \times 10^{-9} = 9.2 \times 10^{-2} sec = 92 msec$ .
- 2. Calculate the approximate current  $i_c$  when  $Q_4$  is on. Assume base voltage on  $Q_1$  is 700 mV. Neglect saturation voltage on  $Q_4$ . Calculate base current  $i_b$  required to produce this collector current assuming  $\beta=100$ .
- 3. Calculate  $i_b$  at key down assuming a 700 mV drop-in base-emitter of  $Q_4$  and at  $600 \, \text{mV}$  at  $D_{11}$ 
  - $V_b = \frac{R_9}{R_9 + R_{24}}$  (12)  $\approx 3V$ ,  $i_b = i_{bs} \exp(\frac{V_b}{V_t})$ ,
- 4. Sketch collector voltage at  $Q_4$  showing where transistor is saturated. What is the delay in going active?
- 5. Use the delay to measure  $\beta$ .



#### Exercise 21: Norcal Driver

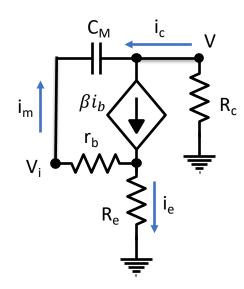
- 1. Measure the output voltage and calculate the power, P.
- 2. Calculate the power from the power supply.
- 3. Measure the voltage gain  $G_v = \frac{V}{V_i}$  with R13 at minimum and maximum gain.
- $\omega = 4.4 \times 10^7$ ,  $L_{p,T1} = 68.6 \mu H$ . This is a class A amplifier.
- $R' = n^2 R, n = \frac{14}{4}, R' = 1225\Omega$
- $Z_{eq}(R) = (20 + R) + j\omega L_{p,T1}$ ,  $0 \le R \le 500$ .  $R = R_{13}$
- $Z_{eq}(0) = 20 + 2992j$ ,
- $i_c = \frac{V_{cc} V_{ce}}{20 + R'}$ ,  $i_c = \beta i_b$ ,  $V_e = 20 i_c$
- From text,  $P = \frac{(V_{cc} V_e)^2}{2R'}$
- $P_o(R) = \frac{V_{cc}^2}{(20+R+R')}$
- Gain is between 2.5 and 60



## Exercise 22: Emitter degeneration

- In Driver amplifier, add probe to  $R_{11}$ , this allows us to measure the AC voltage,  $V_i$
- 1. Measure  $G_v = \frac{V}{V_i}$  with  $R_{13}$  turned fully counterclockwise and then fully clockwise.
  - $R' = 1225\Omega$
  - When  $R_{13}$  is fully counter-clockwise  $R_{E,effective} = 520\Omega$ ,  $G_v = \frac{1225}{520} = 2.36$
  - When  $R_{13}$  is fully clockwise  $R_{E,effective} = 20\Omega$ ,  $G_v = \frac{1225}{20} = 61$
  - Calculate the expected voltage gain for each setting of R<sub>13</sub>
- 2. Measure  $V_i$  at the maximal gain setting
- 3. The open circuit voltage is  $V_0=2V$ , calculate  $V_i$  in terms of  $\mathcal{C}_M$

• 
$$Z_i = \beta R_E ||(G_v + 1)C_M, V_i = Z_i i_b, V = -1225 i_c \text{ so } \frac{V}{V_i} = -\frac{1225}{Z_i} \cdot \frac{i_c}{i_b} = -\beta \frac{1225}{Z_i}$$



## Exercise 23: Norcal Buffer amplifier

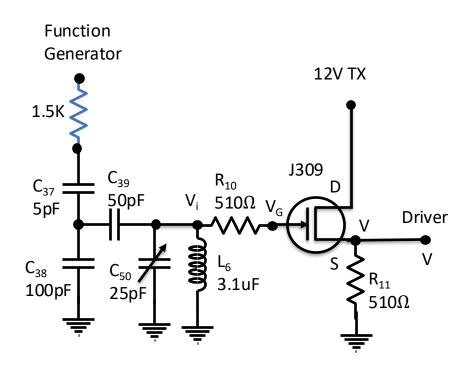
- 1.  $R_{11}$  determines the bias. Measure the DC voltage at source of the JFET (V).
- 2. Calculate the drain bias current. Calculate the source and drain voltages you should expect  $(R=R_{11})$

• 
$$V_{gs} = V_i - V$$
,  $i_d = i_{dss}(1 - \frac{V_{gs}}{V_C})^2$ ,  $V = g_m V_{gs} R$ 

- $g_m \approx 12$ ,  $i_{dss} = 23mA$ ,  $V_C = -2.6V$
- $V_{gs} = \frac{V_i}{1 + g_m R'}$ , substitute into  $i_d = i_{dss} (1 \frac{V_{gs}}{V_c})^2$  to get  $i_d$ .  $i_S = \frac{V}{R}$
- 3. Calculate and measure the voltage gain of the buffer.

• 
$$G_V = \frac{V}{V_i} = \frac{1}{1 + \frac{1}{g_m R}}$$
, or about 1 since  $g_m \approx 12$ 

- 4. Find the transconductance using the measured voltage gain.
- 5. Calculate the available power P $_{+}$  from the function generator through a  $1.5k\Omega$ load. Calculate gain in dB.

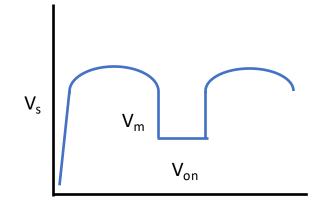


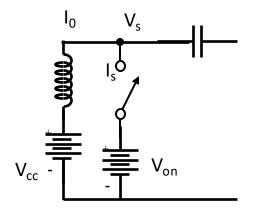
# Class Camplifiers and Norcal 40 Power amp

- Here  $P_o$  is the power from the supply,  $P_d$  is the dissipated power, P is the output power. The Norcal Power amplifier is a class C amplifier. For switch model, switch represents the transistor, when the transistor is on, the switch is open.
- $V_S = V_{on} + V_m \cos(\omega t)$ , (switch off),  $V_{on}$  (switch on)

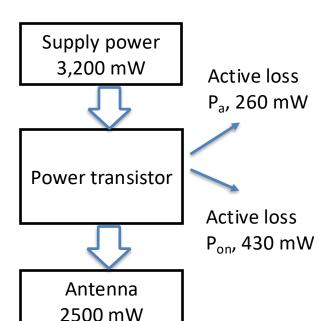
• 
$$V_{cc} = V_{on} + \frac{V_m}{\pi}, V_m = \pi (V_{cc} - V_{on})$$

- $P_0 = V_{cc}I_0$ ,  $P_d = V_{on}I_0$
- $P = P_o P_d = \frac{(V_{cc} V_{on})}{\pi}$
- $\bullet \quad \eta = \frac{P}{P_0} = \frac{(V_{cc} V_{on})}{V_{cc}}$
- $P = \frac{V_m^2}{8R}$ , R is input filter impedance
- $P_d = P_0 P = 3.2W 2.5W = 700mW$
- Cap energy:  $E = \frac{CV^2}{8R} = 37nJ$
- $P_a = Ef = 260mW$
- $i_c = i_0 i_c = 215mA$
- $P_{on} = V_{on}i_{on} = 430mW$
- $P_d = P_a + P_{on} = 690mW$



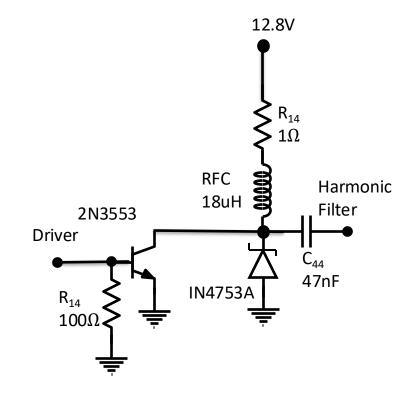


Switch model for class C amp



### Exercise 24: Norcal Power Amp

- 1. Measure the peak-to-peak voltage across 50ohm load required for output of 2W. Calculate it and compare. Calculate the gain in dB
  - $V_{cc} = 12.8V$ , R  $\approx 50\Omega$ ,  $I_0 = 250mA$
  - $P_{on} = V_{on}I_{on} = 430$ mW,  $P_a = Ef = 260$ mA,  $P_d = P_a + P_{on} = 690$ mW
  - $P_o = V_{cc}I_0 = 3.2W$ .
  - $P = \frac{(\pi(V_{cc} V_{on}))^2}{8R} = 2.6W$
- 2. Find pp output voltages or 5, 10, 15, 20, 25 and 30V. Calculate power supply current subtracting 2mA for regulator
- 3. Calculate the output power, efficiency and and dissipation power.
  - $P_d = P_0 P = 3.2W 2.5W$
  - $\eta = \frac{P}{P_0} = \frac{2.5}{3.2} = .78$



# Thermal modelling

- T is heat sink temperature,  $T_0$  is ambient temperature,  $P_d$  is power dissipated.
- $R_t = \frac{T T_0}{P_d}$ ,  $R_t$  is the thermal resistance
- $C_t \dot{T} = P_d$ ,  $C_t$  is the thermal capacitance
- $R_j = \frac{T_j T}{P_d}$ ,  $T_j$  is the junction temperature

• 
$$f(t) + \tau f(t) = f_{\infty}, f(t) = f_0 e^{-\frac{t}{\tau}}$$

• 
$$P_d = \frac{T(t) - T_0}{R_t} + C_t T(t), \tau = C_t R_t, T_\infty = P_d R_t + T_0$$

• 
$$T(t) + \tau T(t) = T_{\infty}, \tau = C_t R_t$$
.

• 
$$T_{\infty} = P_d R_t + T_0$$

• 
$$T(t) = T_{\infty} - P_d R_t e^{-\frac{t}{\tau}}$$

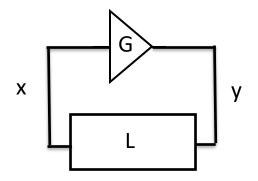
• 
$$T_j(t) = T(t) + R_j P_d$$

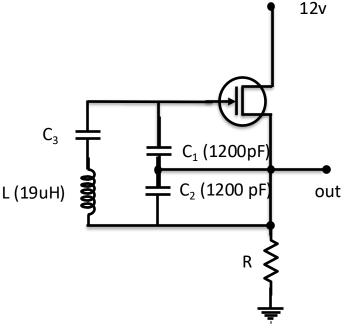
### Exercise 25: Thermal modelling

- For Motorola 2N3553,  $T_i = 25 \, ^{C}/_{W}$
- 1. Measure ambient temperature
- 2. Turn function generator until output is  $30V_{pp}$
- 3. After 20 minutes, measure  $T_{\infty}$ . Use this to calculate  $R_t$  and  $T_i$
- 4. Plot heat sink temperature vs time. Measure  $t_2$  and calculate  $\mathcal{C}_t$
- Need measurements

# Clapp oscillator

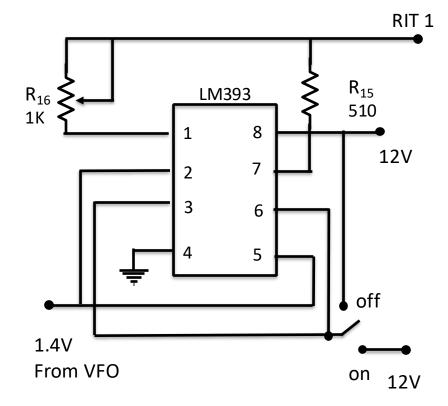
- Oscillation condition
  - Gx = y, Ly=x
  - |G| = |L| and  $\angle G = \angle L$
- Clapp (circuit on right)
  - $i_d = g_m v_{gs}$
  - Resonance:  $-\frac{1}{j\omega_0 C_2} = j\omega_0 L + \frac{1}{j\omega_0 C_3} + \frac{1}{j\omega_0 C_1}$
  - $\omega_0 = \frac{1}{\sqrt{LC}}, C = C_1 ||C_2||C_3$
  - At resonance,  $v_{gs} = Ri_d \frac{c_1}{c_2}$ ,  $L = \frac{c_1}{Rc_2}$
  - Oscillation continues if  $g_m > \frac{C_1}{RC_2}$
  - $v_{gs} = 2v_s$





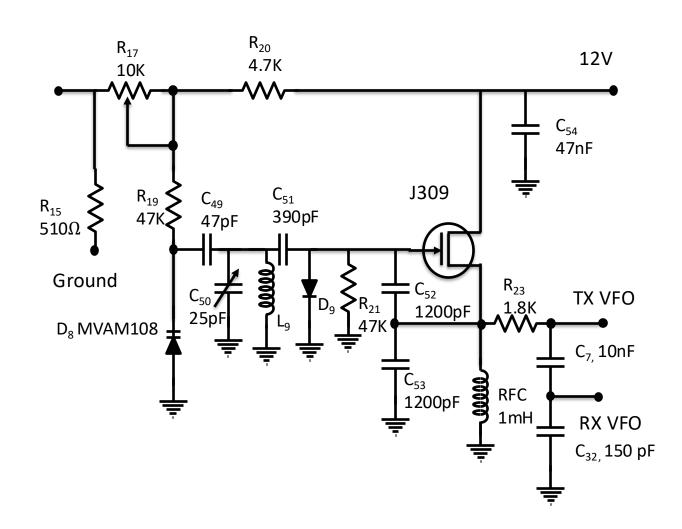
## Norcal Receiver Incremental Tuning (RIT)

- LM393 is a comparator
- RIT allows transmit and receive frequency to be offset.
- If transmitter is on, TX will be 8V and the left comparator will be off, the right one on and  $R_{15}$  will be grounded.
- For receiving, TX is <1.4V, disconnecting  $R_{15}$  and shorting  $R_{16}$  to ground.



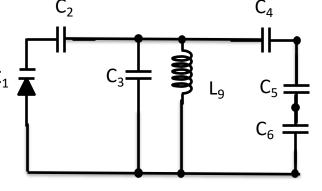
### Exercise 26: Norcal VFO

- Check MVAM108 capacitor when R<sub>17</sub> is high and low
- Start resistor (R<sub>21</sub>) pulls gate to ground at start
- When gain limiting diode (D<sub>9</sub>) conducts, it pulls gate negative
- Oscillator keeps growing as long as g<sub>m</sub>>1/R
- 1. Measure p-p voltage, V. What should you expect?
- 2. Measure DC voltage across wiper in R<sub>17</sub>
- 3. Calculate expected V for large signal oscillation
- 4. How does the frequency change as  $R_{17}$  changes?
- 5. Calculate the oscillation frequency and the loss ratio  $|V/V_1|$
- 6. How would this change if you took when L<sub>9</sub> is turned off?



#### **VFO Problem**

- The figure on the right is an equivalent circuit for the oscillator for the purpose of calculating resonant frequency. The varactor,  $C_1$  varies from 30 to 600 pF depending on the voltage.
- $C_2 = 47pF$ ,  $C_3 = 7pF$ ,  $C_4 = 390pF$ ,  $C_5 = C_6 = 1200pF$ ,  $L_9 = 19.2\mu H$
- The equivalent capacitance for  $C_4 C_5 C_6$  is  $C_{R,eq} = 236pF$ .
- When  $C_1=187pF$ , the equivalent capacitance for  $C_1-C_2-C_3$  is  $C_{L,eq}=46$ . 2pF and  $C_{osc}=282pF$ . At the resonant frequency,  $\omega L_9=\frac{1}{\omega C_{osc}}$ .  $\omega^2=\frac{1}{L_9C_{osc}}$ .  $f_r=2.16MHz$
- When  $C_1=54pF$ , the equivalent capacitance for  $C_1-C_2-C_3$  is  $C_{L,eq}=32pF$ .  $C_{osc}=268pF$  At the resonant frequency,  $\omega L_9=\frac{1}{\omega C_{osc}}$ .  $\omega^2=\frac{1}{L_9C_{osc}}$ .  $f_r=2$ . 22MHz.
- These values are what we want for the tunable VFO.



## Gain Limiting in Norcal 40

- The gain here is limited by the diode.  $C_1 = C_2$ .  $V_g = 2V_s$
- $V_g = V_f V$ ,  $V_f$  is the forward voltage of the diode.

• 
$$V_m = V_g + \frac{V}{2}$$
, or  $V_m = V_g - \frac{V}{2}$ 

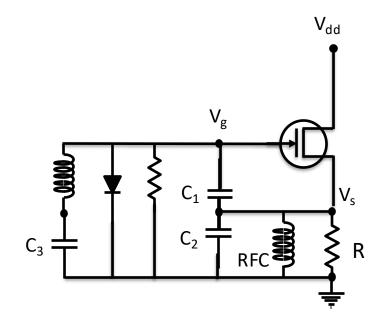
• 
$$G_m = \frac{I}{V} = \frac{1}{R}$$

• 
$$I_d = I_{dss} (1 - \frac{V_{gs}}{V_c})^2$$

• 
$$I_o = \frac{I_m}{4}$$
,  $I \approx I_m$ 

• 
$$G_m = \frac{I_m}{V}$$

• Oscillation condition is  $G_m = \frac{1}{R}$ 



### Exercise 27: Gain limiting

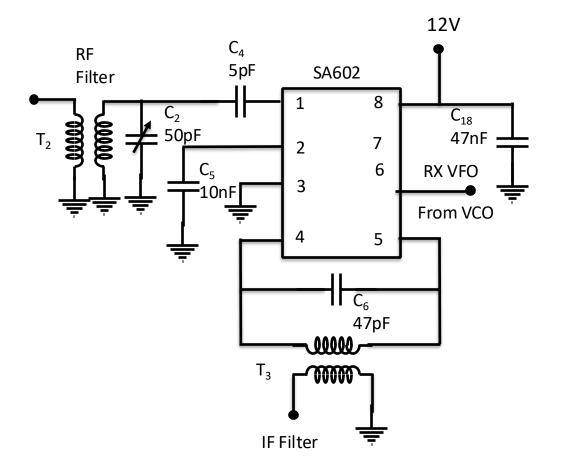
- 1. Measure the voltage, V, on  $R_{23}$
- 2. In deriving the oscillation condition, we neglected the inductor resistance and drain source resistance,  $r_d$ . How does this affect the conditions? L<sub>9</sub> has a Q of 250 and  $r_d = 5k\Omega$ , now what is the predicted V?
- 3. Calculate the loss ratio  $\left|\frac{V}{V_i}\right|$ .
- 4. Measure the temperature dependence of the VFO.
- 5. How much does the temperature have to change to cause a 100Hz shift?
- 6. What is the oscillation change if we remove one turn of the inductor?
- 7. What is the RIT tuning range?

# Gain limiting

Need measurements

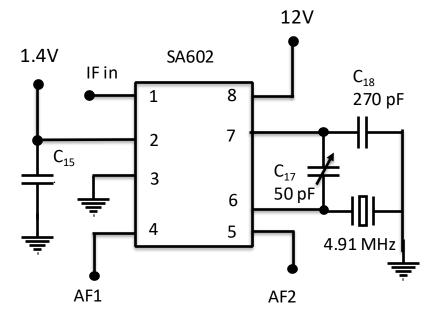
#### Exercise 28: Norcal RF Mixer

- 1. Measure conversion gain of the Mixer.
- 2. How much attenuation is provided by pot?
- 3. By how many dB is the image response suppressed. Look at the spur  $f_{\downarrow 5}$
- Need measurements



# Exercise 29: Norcal Product Detector (1)

- 1. Adjust C17 for minimum oscillation frequency and record it.
- 2. Calculate the minimum oscillation frequency you'd expect.
- 3. Measure the temperature coefficient for the BFO.
- 4. Measure the gain through the receiver from the antenna through the product detector.
- 5. Find the f5 spur calculate the expected f3.
- 6. By how much is the if spur suppressed?
- Need measurements



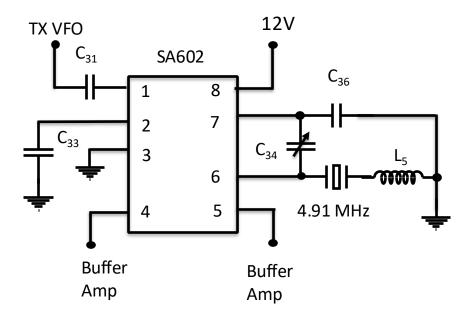
• 620 Hz output through AF1 and AF2

# Norcal Product Detector (2)

Χ.

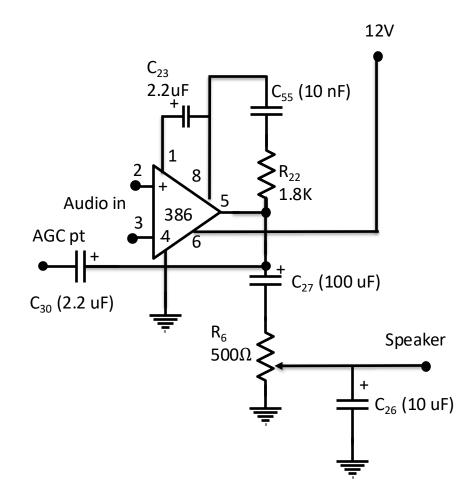
### Exercise 30: Norcal transmit mixer and oscillator

- 1. How much would you expect the inductor to lower the oscillation frequency
- 2. Use the TX VFO and the voltage attenuation to calculate the input power from the transmit mixer. Calculate the gain through the entire chain
- 3. Measure the rise and fall time of keying response
- 4. There is a spurious  $f_{mn}=mf_{vfo}+nf_{to}$ .
- Need measurements



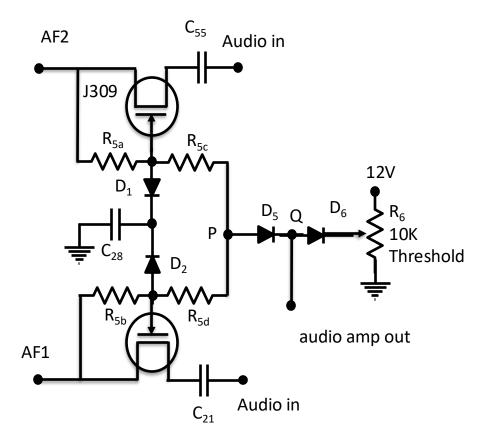
### Exercise 31: Norcal Audio Amp

- 1. Calculate input V<sub>i</sub> assuming very high input impedance
- 2. Measure the voltage gain  $G_v$  at high frequency and 3dB roll-off
- Input impedance is high.
- The 386 acts like a non-inverting op amp. The internal feedback resistor is  $R_f=15k\Omega$ .  $G=2\frac{R_f}{R_e}$ . With pins 1, 8 open,  $R_e=1.5k\Omega$ , so  $G=2\frac{15}{1.5}=20$ . pins 1 and 8 go across  $1.35k\Omega$  of  $R_e$ . So, shorting them (using the non-inverting gain circuit) results in a gain of  $G=2\frac{15}{.15}=200$ .

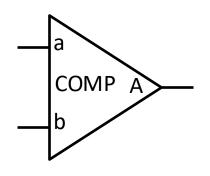


#### Exercise 32: Norcal AGC

- Connect function generator through 300K resistor to AF2 (620Hz sine, R<sub>6</sub> fully counterclockwise) and oscilloscope to audio output.
   Adjust input so output is 1V rms. Connect multimeter to P.
- 1. Plot audio output v dc control
- 2. What is the maximum control voltage we can measure? Infer cutoff voltage  $V_c$
- 3. What is the minimum control voltage?
- Need measurements

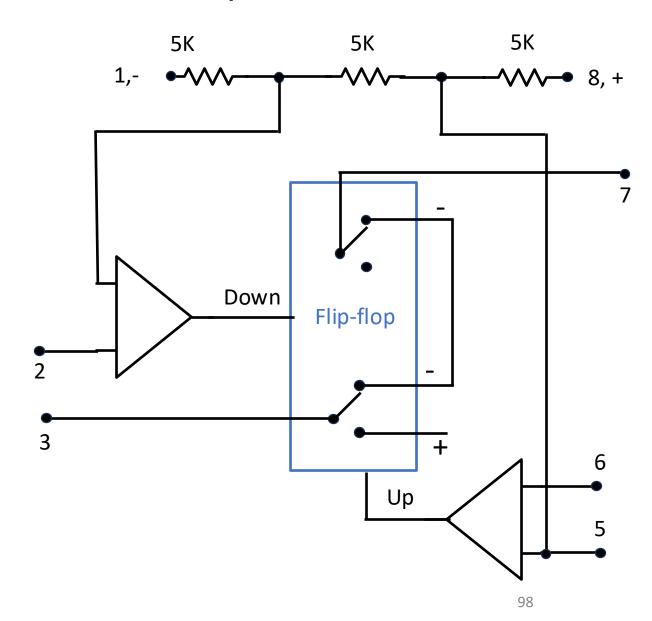


# 555 Equivalent



For comparator,

- A=1, if  $a \ge b$
- A=0, if a < b



# 555 Astable

