



For spherical triangle

- $\cos(\alpha) = \cos(A) \sin(\beta) \sin(\gamma) + \cos(\beta) \cos(\gamma)$
- $\frac{\sin(\alpha)}{\sin(A)} = \frac{\sin(\beta)}{\sin(B)} = \frac{\sin(\gamma)}{\sin(C)}$

- N is North Pole
- O is observer at latitude  $\lambda$
- $R_1$  is position of sun at sunrise  $OR_1=90$
- $R_2$  is position of sun at sunrise  $OR_2=90$
- $T_1$  is longitude of sun at sunrise
- $T_2$  is longitude of sun at sunset
- $\cos(NR_1) = \cos(90 + \epsilon) = -\cos(\alpha) \cos(\lambda) = -\sin(\epsilon)$
- So,  $\cos(\alpha) = \frac{\sin(\epsilon)}{\cos(\lambda)}$  (equation 1)
- $CT_1 = \beta$
- $\sin(\beta) = \frac{\sin(\alpha)}{\cos(\epsilon)}$  (equation 2)
- 1. Solve for  $\alpha$  in equation 1
- 2. Solve for  $CT_1 = \beta$  in equation 2
- 3. Length of day is  $\frac{2CT_1}{180} \cdot 12$  hours
- Note  $\epsilon(t) = 23.5 \cdot \cos(t)$ ,  $t$  is number of days since December 22 divided by 365.25 times  $2\pi$