# Electronics of Radio (Supplement)

Notes on David Rutledge's book

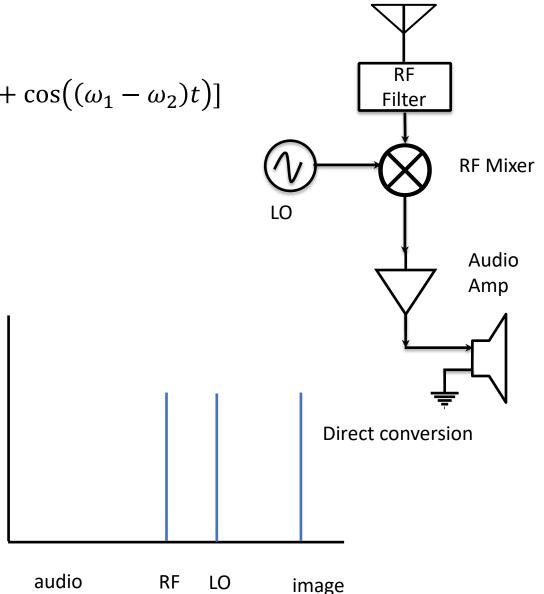
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### Modulation

- AM:  $V(t) = a(t)\cos(\omega_c t) + V_c\cos(\omega_c t)$
- FM:  $V(t) = V_c \cos([\omega_c + a(t)]t)$
- FSK:  $V(t) = V_c \cos(\omega_1 t)$ , if 1 [mark];  $V_c \cos(\omega_0 t)$ , if 0 [space]
- PSK:  $V(t) = V_p \cos(\omega_c t)$ , if 1;  $-V_p \cos(\omega_c t)$ , if 0 [space]
- Gain:  $G = \frac{P_o}{P_i}$ , Loss:  $L = \frac{P_o}{P_{max}}$ , Rejection:  $R = \frac{P_{max}}{P_{pb}}$ ,

#### Direct conversion receivers

- Mixer
  - $V(t) = \cos(\omega_1 t) \cos(\omega_2 t) = \frac{1}{2} [\cos((\omega_1 + \omega_2)t) + \cos((\omega_1 \omega_2)t)]$
- Image frequency
  - $\omega_{vi} = \omega_{LO} + \omega_a$
  - $\omega_{rf} = \omega_{LO} \omega_a$
- RF filter removes image
- Downside:
  - Not tunable



## Norcal 40A



### Mixers

- $V_{lo}(t)$  is a square wave with period  $\omega_{lo}$ . Expanding this in a Fourier series, we get:
- $V_{lo}(t) = \frac{4}{\pi}(\cos(\omega_{lo}t) \frac{\cos(3\omega_{lo}t)}{3} + \frac{\cos(5\omega_{lo}t)}{5}...), V_{rf}(t) = V_{rf}\cos(\omega_{rf}t)$
- $V_{lo}(t)V_{rf}(t) = \frac{2V_{rf}}{\pi}(\cos(\omega_{-}t) \frac{\cos(3\omega_{-}t)}{3} + \frac{\cos(5\omega_{-}t)}{5}...) + \frac{2V_{rf}}{\pi}(\cos(\omega_{+}t) \frac{\cos(3\omega_{+}t)}{3} + \frac{\cos(5\omega_{+}t)}{5}...)$
- $\omega_{+} = \omega_{lo} + \omega_{rf}$  and  $\omega_{-} = |\omega_{lo} \omega_{rf}|$
- We define  $\omega_{k+}=(k\omega_{lo}+\omega_{rf})$  and  $\omega_{k-}=|k\omega_{lo}-\omega_{rf}|$  and  $V_{k+}(t)=\frac{2V_{rf}}{k\pi}\cos(\omega_{k+}t)$  and  $V_{k-}(t)=\frac{2V_{rf}}{k\pi}\cos(\omega_{k-}t)$
- $\omega_i=\omega_{if}-\omega_{lo}$  and  $\omega_{if}=\omega_{if}+\omega_i$ ,  $\omega_i$  is a spurious signal.  $\omega_{k+}$  and  $\omega_{k-}$  are the spurs from the kth harmonic



### Phasors

- V(t) = RI(t)
- $V(t) = L\dot{I}(t)$
- $I(t) = C\dot{V}(t)$
- Suppose  $V(t) = Acos(\omega t + \theta)$  and  $I(t) = Bcos(\omega t + \phi)$ . If  $\phi > \theta$ , we say the current leads the voltage.
- $V(t) = Re(e^{j(\omega t + \theta)})$ , and  $I(t) = Re(e^{j(\omega t + \phi)})$
- Now define  $V = Ae^{j\theta}$  and  $I = Be^{j\phi}$ , so |V| = A, |I| = B,  $\angle V = \theta$ , and  $\angle I = \phi$ . V and I are called phasors and do not include time. Note that  $V(t) = Re(Ve^{j\omega t})$  and  $I(t) = Re(Ie^{j\omega t})$ .
- Note that  $I = CVj\omega$ , for a capacitor and  $V = LIj\omega$ , for an inductor
- $\hat{V} = Z\hat{I}, Z = R + jX$
- $\hat{I} = Y\hat{V}, Y = G + jB$

## Series resonance and Q

- At  $\omega_u$  and  $\omega_l$ ,  $X=\pm R$  [ $\omega_u$  is upper 3dB cutoff and  $\omega_l$  is lower 3dB cutoff]
- $\omega_u L \frac{1}{\omega_u C} = R$ ,  $\omega_l L \frac{1}{\omega_l C} = -R$
- Define  $Q = \frac{X}{R}$
- $\frac{\omega_u}{\omega_0} \frac{\omega_0}{\omega_u} = \frac{R}{\omega_0 L} = \frac{1}{Q}$  and  $\frac{\omega_l}{\omega_0} \frac{\omega_0}{\omega_l} = -\frac{R}{\omega_0 L} = -\frac{1}{Q}$
- $\frac{\omega_u}{\omega_0} \frac{\omega_0}{\omega_u} = \frac{\omega_0}{\omega_l} \frac{\omega_l}{\omega_0}$ , so  $\omega_0^2 = \omega_u \omega_l$  and  $\frac{\omega_u \omega_l}{\omega_0} = \frac{1}{Q}$

# Parallel resonance and Q

• 
$$\frac{\omega_u}{\omega_0} - \frac{\omega_0}{\omega_u} = \frac{G}{\omega_0 C} = \frac{1}{Q_p}$$
 and  $\frac{\omega_l}{\omega_0} - \frac{\omega_0}{\omega_l} = -\frac{G}{\omega_0 C} = -\frac{1}{Q_p}$ 

#### Power

- P(t) = I(t)V(t)
- Complex power:  $P = \frac{V\bar{I}}{2} = Z \frac{|I|^2}{2} = P_a + jP_r = R \frac{|I|^2}{2} + jX \frac{|I|^2}{2}$ 
  - $P_a$  is power delivered to resistor,  $P_r$  is power stored in inductor and capacitor

• 
$$P_r = \frac{\omega L|I|^2}{2} - \frac{\omega C|V_c|^2}{2} = \omega (E_L - E_C)$$

• 
$$Q = \omega \frac{L|I|^2}{R|I|^2} = \omega \frac{L}{R} = \omega \frac{E_L}{P_a}$$

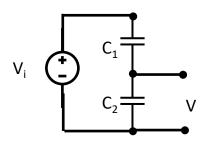
# General formulas for Q

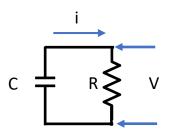
• x

## Exercises

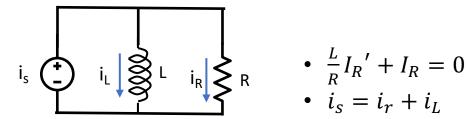
• Calculate wave form through bridge and after "smoothing capacitor"

### Misc-1





• 
$$I = \frac{V}{R} = -CV', \tau = RC,$$



$$\frac{L}{R}I_R' + I_R = 0$$

• 
$$i_s = i_r + i_L$$

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