# Electronics of Radio

Notes on David Rutledge's book

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## Basic concepts

- Potential difference  $(V, \phi)$ :  $\phi = \int_a^r E \cdot ds$ , energy per charge, 1V = 1 J/s
- Kirkoff 1:  $\sum_{loop} V_i = 0$  (Conservation of energy)
- Kirkoff node:  $\sum_{node} I_i = 0$  (Conservation of charge)
- $V(t) = V_p \cos(\omega t)$ ,  $\omega = 2\pi f$ ,  $I(t) = I_p \cos(\omega t)$ ,  $\omega = 2\pi f$
- Instantaneous power:  $P(t) = V(t)I(t) = V_pI_p \cos^2(\omega t)$
- Average power:  $P_a = \int_0^{1/f} V(t) I(t) dt = V(t) I(t) = \int_0^{2\pi/\omega} V_p I_p \cos^2(\omega t) dt = \frac{V_p I_p}{2}$
- Band names:

Name	Frequency
VLF	3-30kHz
LW	20-300kHz
MW	300kHz-3MHz
HF	3MHz-30MHz
VHF	30-300MHz

Name	Frequency
UHF	300MHz-1GHz
uW	1-30GHz
milliW	30-300GHz
submilliF	>300GHz

# Signals

- Gain (G) expressed in decibels:  $G = 10 \log_{10}({^{P_{out}}/_{P_{in}}})$
- Mixer:

• 
$$V(t) = \cos(\omega_1 t) \cos(\omega_2 t) = \frac{1}{2} [\cos(\omega_+ t) + \cos(\omega_- t)], \omega_+ = \omega_1 + \omega_2, \omega_- = \omega_1 - \omega_2$$

Modulation

Name	Equation
AM	$V(t) = a(t)\cos(\omega_c t)$
FM	$V(t) = V_c \cos((\omega_c + a(t))t)$
FSK	$V(t) = V_c \cos(\omega_1 t)$ , if 1 $V(t) = V_c \cos(\omega_0 t)$ , if 0
PSK	$V(t) = +V_p \cos(\omega t), \text{ if } 1$ $V(t) = -V_p \cos(\omega t), \text{ if } 0$

## Resistors, capacitors, inductors











#### Resistors

- Analytic model: IR = V
- Energy dissipated:  $E = \int_{t_i}^{t_f} IV \, dt = \int_{t_i}^{t_f} I^2 R dt$
- Capacitors
  - Analytic model: CV = q,  $C\frac{dV}{dt} = i$
  - Capacitor Energy stored:  $E = \int_{t_i}^{t_f} CV \frac{dV}{dt} dt = \frac{1}{2} CV^2$
- Inductors
  - Analytic model:  $V = L \frac{di}{dt}$
  - Inductor Energy stored:  $E = \int_{t_i}^{t_f} IV \, dt = \int_{t_i}^{t_f} LI \frac{dI}{dt} \, dt = \frac{1}{2} LI^2$



# Diodes, transformers

#### Diodes

- Devices that allow current to flow only in one direction
- Silicon diodes, for example have, essentially infinite resistance if  $V_{ac}$ <0, that is if the cathode is at a higher potential than the anode and very low resistance if  $V_{ac}$ > .7V.
- The cathode is usually labelled with a band
- Transformers
  - AC only:  $\frac{N_2}{N_1} = \frac{V_2}{V_1}$

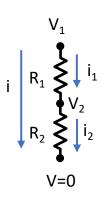


Credit: Make Electronics



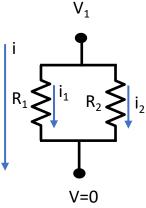


# Simple circuit analysis with Kirchhoff



- $R_{eq}$  is the equivalent resistance, replacing the top left circuit with a single resistance.
- Top ier. S...

  By Kirchhoff's node rule,  $i_1 = i_2 = \iota$ , so  $\frac{V_2}{R_1} = \frac{V_2}{R_2} = \frac{V_1}{R_2} \text{ thus } \frac{R_1}{R_{eq}} V_1 = V_1 V_2 \text{ and}$   $\frac{R_2}{R_{eq}} V_1 = V_2. \text{ Adding, we get } \frac{R_1}{R_{eq}} V_1 + \frac{R_2}{R_{eq}} V_1 = \frac{d(V_1 V_2)}{dt} = \frac{d(V_1 V_2)}{dt$



- Again let  $R_{eq}$  is the equivalent resistance, replacing the bottom left circuit with a single resistance.
- By Kirchhoff's node rule,  $i_1 + i_2 = i$ , so

$$\bullet \ \frac{V_1}{R_1} + \frac{V_1}{R_2} = \frac{V_1}{R_{eq}}.$$

• Solving, we get.  $\frac{R_1R_2}{R_1+R_2}=R_{eq}$ 

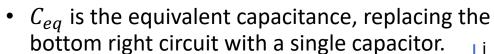
- $C_{eq}$  is the equivalent capacitance, replacing the top right circuit with a single capacitor.

• 
$$C_1 \frac{d(V_1 - V_2)}{dt} = C_2 \frac{d(V_2)}{dt} = C_{eq} \frac{dV_1}{dt}$$

• 
$$\frac{C_{eq}}{C_1} \frac{d(V_1)}{dt} = \frac{d(V_1 - V_2)}{dt}$$
 and 
$$\frac{C_{eq}}{C_2} \frac{d(V_1)}{dt} = \frac{d(V_2)}{dt}$$



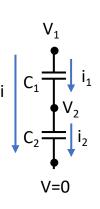
• 
$$\frac{C_{eq}}{C_1} + \frac{C_{eq}}{C_2} = 1$$
 and solving, we get.  $\frac{C_1C_2}{C_1 + C_2} = C_{eq}$ 

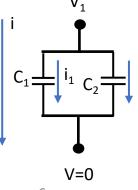




• 
$$C_{eq} \frac{dV_1}{dt} = C_1 \frac{dV_1}{dt} + C_2 \frac{dV_1}{dt}$$
, so

• 
$$C_{eq} = C_1 + C_2$$





# Simple circuit analysis with Kirchhoff



- Let  $L_{eq}$  be the equivalent inductance, replacing the top left circuit with a single inductor.
- By Kirchhoff's node rule,  $i_1 = i_2 = i$ , so

• 
$$L_{eq} \frac{di}{dt} = V_1$$
,  $L_1 \frac{di_1}{dt} = V_1 - V_2$ ,  $L_1 \frac{di_2}{dt} = V_2$ 

• 
$$V_1 = L_{eq} \frac{di}{dt} = L_1 \frac{di}{dt} + L_2 \frac{di}{dt}$$
 and

• 
$$L_{eq} = L_1 + L_2$$



• Let  $L_{eq}$  be the equivalent inductance, replacing the bottom left circuit with a  $\frac{di}{dt} = V_1 \quad di_1 \quad V_1 \quad di_2 \quad V_1$ 

$$\frac{V_1}{L_{eq}}, \frac{di_1}{dt} = \frac{V_1}{L_1}, \frac{di_2}{dt} = \frac{V_1}{L_2},$$

- single inductor.
- By Kirchhoff's node rule,  $i_1 + i_2 = i$ , so

• 
$$\frac{V_1}{L_{eq}} = \frac{V_1}{L_1} + \frac{V_1}{L_2}$$
 and

$$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$$

• The circuit on the right, is useful and is called a *voltage divider*.

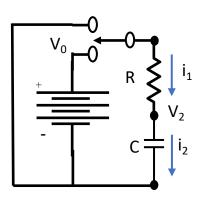
• 
$$i = i_1 = i_2$$
 so  $\frac{V_1 - V_2}{R_1} = \frac{V_2}{R_2}$ ,  $V_1 - V_2 = \frac{R_1}{R_2} V_2$ 

• Thus, 
$$V_1 = (1 + \frac{R_1}{R_2})V_2$$
 and so

• 
$$V_2 = \frac{R_2}{R_1 + R_2} V_1$$



# Simple circuit analysis with Kirchhoff



RC behavior: charging

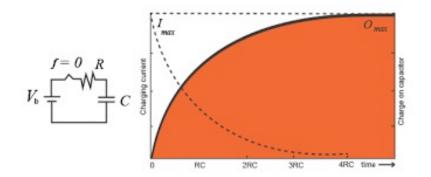
• 
$$V_0 - V_2 = i_1 R = V_R, i_1 = \frac{V_R}{R}$$

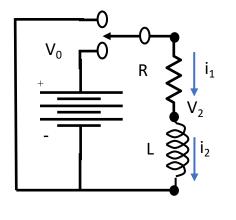
• 
$$i_2 = C \frac{dV_2}{dt}$$
,  $V_C = V_2$ 

• 
$$i_1 = i_2$$
,  $V_C = V_0 - V_R$ 

• 
$$i_1 = i_2$$
,  $V_C = V_0 - V_R$   
•  $\frac{V_R}{R} = C \frac{dV_C}{dt}$ ,  $RC \frac{dV_C}{dt} = V_0 - V_C$ , or  $RC \frac{dV_C}{dt} + V_C = V_0$ 







RL behavior: charging

• 
$$V_0 - V_2 = i_1 R = V_R$$

• 
$$V_L = V_2 = L \frac{di_2}{dt}$$

• 
$$V_L = V_2 = L \frac{di_2}{dt}$$
  
•  $i_1 = i_2, V_R = V_0 - V_L$ , so  $L \frac{d}{dt} \frac{V_0 - V_L}{R} = V_L$ 

$$\bullet \ \frac{L}{R} \frac{d V_L}{dt} + V_L = 0$$

• Solution is  $V_L = V_0 e^{-\frac{Rt}{L}}$ 



#### Phasors

- V(t) = RI(t)
- $V(t) = L\dot{I}(t)$
- $I(t) = C\dot{V}(t)$
- Suppose  $V(t) = Acos(\omega t + \theta)$  and  $I(t) = Bcos(\omega t + \phi)$ . If  $\phi > \theta$ , we say the current leads the voltage.
- $V(t) = Re(e^{j(\omega t + \theta)})$ , and  $I(t) = Re(e^{j(\omega t + \phi)})$
- Now define  $V = Ae^{j\theta}$  and  $I = Be^{j\phi}$ , so |V| = A, |I| = B,  $\angle V = \theta$ , and  $\angle I = \phi$ . V and I are called phasors and do not include time. Note that  $V(t) = Re(Ve^{j\omega t})$  and  $I(t) = Re(Ie^{j\omega t})$ .
- Note that  $I = CVj\omega$ , for a capacitor and  $V = LIj\omega$ , for an inductor

# Circuit analysis with Kirchhoff and impedance

- Impedance unifies the "simple" ohms law with capacitance and inductance.
- Z=R, for resistors,  $Z=j\omega L$ , for inductors and  $Z=\frac{1}{j\omega C}$ , for capacitors.
- In general, Z = R + jX and all the ohm like laws hold for resistors, capacitors and inductors .
  - $Z_{eq} = Z_1 + Z_2$  for two components with impedance  $Z_1, Z_2$  connected in series
  - $Z_{eq} = \frac{Z_1 2}{Z_1 + Z_2}$  for two components with impedance  $Z_1, Z_2$  connected in parallel
- For example, for a resistor and capacitor in series has impedance  $Z = R + \frac{1}{j\omega C}$

# Phasors, impedance and power

- For the circuit on the right,  $Z = R + \frac{1}{i\omega C}$  is the impedance for the resistor and capacitor in series.
- The phasor  $I=\frac{V_0}{Z}$  and the phasor  $V=\frac{I}{j\omega C}=\frac{V_0}{1+j\omega RC}$  Further,  $|I|=\frac{V_0}{|Z|}$ ,  $\angle I=\angle\frac{V_0}{|Z|}$  and  $|V|=\frac{|I|}{|j\omega C|}=|\frac{V_0}{1+j\omega RC}|$



- The average power is  $P_a = Re(P) = Re(\frac{V\overline{I}}{2})$ . We define the reactive power as  $P_r = Im(P)$ .
- $P_r = \omega(E_L E_C)$ , where  $E_L$  and  $E_C$  are respectively, the energy stored in the inductor and capacitor respectively.



# Q and phasors

- Consider the series resonance on the right.  $Z_{LCR} = R + j \left(\omega L \frac{1}{\omega C}\right)$
- The phasor,  $I = \frac{V_0}{Z_{LCR}}$ , and the phasor  $V_R = \frac{V_0}{Z_{LCR}} Z_R$ , where  $Z_R = R$ .
- So  $V_R = \frac{RC\omega V_0}{RC\omega + i(LC\omega^2 1)}$ .
- $|V_R|$  is maximum when  $\omega^2 LC = 1$ . Put  $\omega_0 = \frac{1}{\sqrt{LC}}$ . When  $\omega = \omega_0$ ,  $|V_R| = V_R = V_0$ .
- $|V_R| = \frac{V_0}{\sqrt{2}}$ , when X = R. Note that the power through R when X = R is half the power through R when X=0 or  $\omega=\omega_0$ .



- We define  $Q = \frac{X}{R} = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 CR}$ .
- Solving for  $\omega_u$  and  $\omega_l$ , we get  $\frac{L\omega_u}{\omega_0} \frac{\omega_0}{c\omega_u} = R$  and  $\frac{L\omega_l}{\omega_0} \frac{\omega_0}{c\omega_l} = -R$ , or, in terms of Q,  $\frac{\omega_u}{\omega_0} \frac{\omega_0}{\omega_u} = \frac{1}{Q}$  and  $\frac{\omega_l}{\omega_0} \frac{\omega_0}{\omega_l} = -\frac{1}{Q}$ . In fact,  $\omega_0 = \sqrt{\omega_u \omega_l}$ , and so  $\frac{\omega_u}{\omega_0} \frac{\omega_l}{\omega_0} = \frac{1}{Q}$ .
- Thus  $Q = \frac{\omega_0}{\omega_0 \omega_I} = \frac{\omega_0}{\Delta \omega}$
- From the definition of  $P_a$ , earlier,  $Q = \omega_0 \frac{E}{P_a}$ , where E is the total energy stored in L and C, which is in turn the peak  $E_L$  and peak  $E_C$  at resonance.



# Phasors, impedance and power

- For the circuit on the right,  $Z = R + \frac{1}{i\omega C}$  is the impedance for the resistor and capacitor in series.
- The phasor  $I=\frac{V_0}{Z}$  and the phasor  $V=\frac{I}{j\omega C}=\frac{V_0}{1+j\omega RC}$  Further,  $|I|=\frac{V_0}{|Z|}$ ,  $\angle I=\angle\frac{V_0}{|Z|}$  and  $|V|=\frac{|I|}{|j\omega C|}=|\frac{V_0}{1+j\omega RC}|$

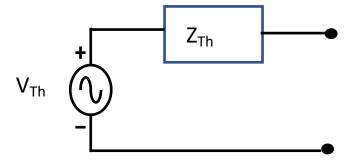


- The average power is  $P_a = Re(P) = Re(\frac{V\overline{I}}{2})$ . We define the reactive power as  $P_r = Im(P)$ .
- $P_r = \omega(E_L E_C)$ , where  $E_L$  and  $E_C$  are respectively, the energy stored in the inductor and capacitor respectively.



#### Thevenin and Norton

 Thevenin: Any combination of linear sources and passive elements terminating in two terminals is equivalent to a pure voltage source in series with an impedance



 Norton: Any combination of linear sources and passive elements terminating in two terminals is equivalent to a pure current source in parallel with an conductance



Similar theorems for two terminal input and output devices (with transfer function)

#### Thevenin and Norton

- We can use lookback resistance to calculate the Thevenin equivalent resistance and ideal source.
- To find the lookback resistance, short the source and apply the usual laws.
  - Here  $R_s = R_1 || R_2$
- To find the new ideal source, notice  $R_1$  and  $R_2$  form a voltage divider.
  - The new source voltage is  $\frac{V_0 R_2}{R_1 + R_2}$

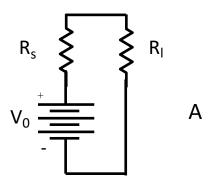


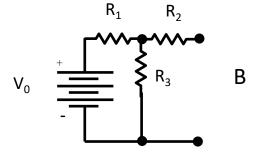
Is equivalent to

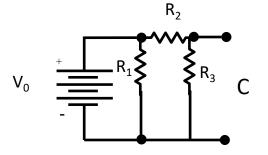


#### Exercise 1: Resistors

- 1. Consider (A). Find the formula for power in the load. Find the  $R_l$  that maximizes the power to the load.
- 2. For (B) and (C), find the Thevenin and Norton parameters





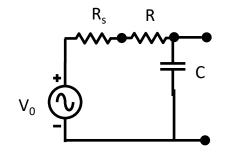


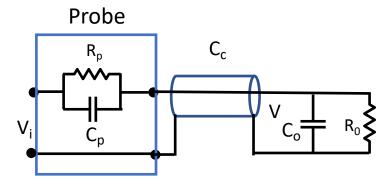
## Exercise 2: Sources

Not important

## Exercise 3: Capacitors

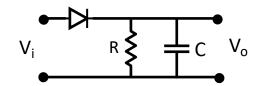
- In the circuit on the right,  $V_0$  is a 2 volt pp ideal square wave source of frequency 20Hz,  $R_S=50\Omega$ ,  $R=300k\Omega$  and C=10~nF.
- What is the voltage, V, at the output? The scope has an input resistance of  $1M\Omega$ .
- Let  $t_2$ , the time to discharge to OV. Calculate  $\tau$  and  $t_2$ .
- Capacitance on the scope prevents the delay from being 0. Measure the new  $t_2$  with these changes.
- Given C<sub>0</sub> and C<sub>p</sub> and R<sub>p</sub>
- Now calculate the new  $t_2$ .





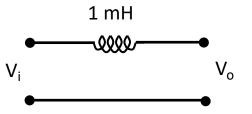
## Exercise 4: Diode detectors

Χ



## Exercise 5: Inductors

Χ

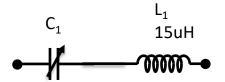


## Exercise 6: Diodes and snubbers

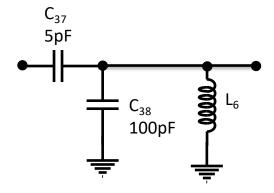
Χ

## Exercise 7: Parallel to Series conversion

#### Exercise 8: Series resonance



#### Exercise 9: Parallel resonance



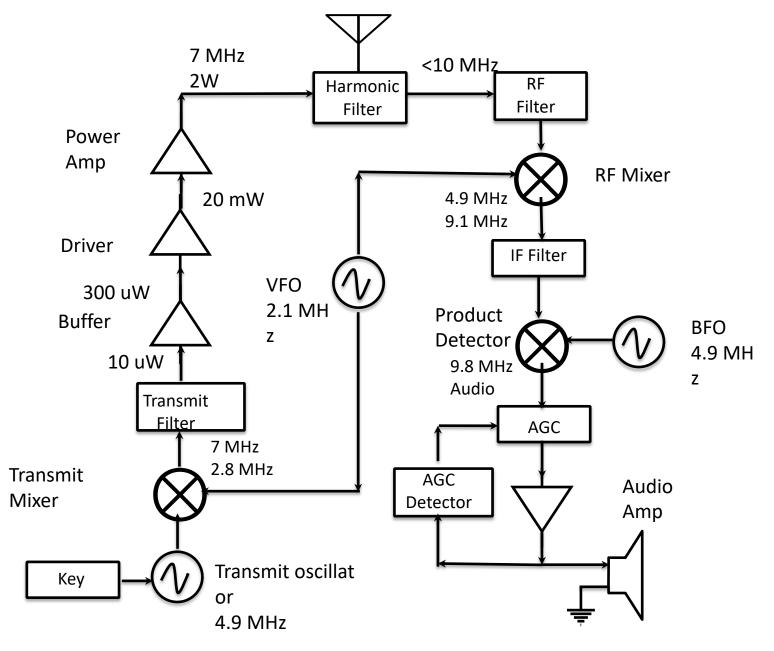
## Direct conversion and superhet receivers

- Image frequency
  - $\omega_{rf} = \omega_{LO} \omega_a$
  - $\omega_i = \omega_{LO} + \omega_a$
- Superheterodyne designs
  - $\omega_{rf} = \omega_{IF} + \omega_{VFO}$
  - $\omega_{vi} = \omega_{IF} \omega_{VFO}$
  - $\omega_{IF} = \omega_{BFO} \omega_a$
  - $\omega_{bi} = \omega_{BFO} + \omega_a$
  - $\omega_{usb} = \omega_{VFO} + \omega_{BFO} + \omega_a$
  - $\omega_{lsb} = \omega_{VFO} + \omega_{BFO} \omega_a$

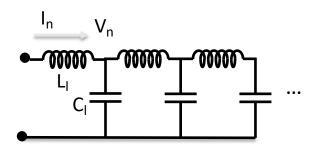


**Direct conversion** 

#### Norcal 40A



#### **Transmission Lines**



**Power** 

$$\tau = \frac{V}{V_{+}} = 1 + \rho = \frac{2Z}{Z + Z_{0}}, V = 2V_{+}$$

Lookback resistance is  $R_s = Z_0$ 

$$P_{+} = \frac{{V_{+}}^2}{2Z_0} = \frac{{V_0}^2}{8Z_0}$$
, This is the total available power

• 
$$V_{n+1} - V_n = -L_l \frac{\partial I_{n+1}}{\partial t}$$
,  $L = \frac{L_l}{l}$ 

• 
$$I_{n+1} - I_n = -C_l \frac{\partial V_n}{\partial t}$$
,  $C = \frac{C_l}{l}$ 

• 
$$\frac{\partial^2 V}{\partial z^2} = LC \frac{\partial^2 V}{\partial t^2}$$
 and  $\frac{\partial^2 I}{\partial z^2} = LC \frac{\partial^2 I}{\partial t^2}$ 

- Solution is V(z-vt),  $v=\frac{1}{\sqrt{LC}}$ , for forward wave
- V' = vLI',  $\frac{V}{I} = \sqrt{\frac{L}{C'}}$ ,  $Z_0 = \sqrt{\frac{L}{C}}$
- Another solution is V(z+vt),  $v=\frac{1}{\sqrt{LC}}$ , for r everse wave

• 
$$Z_0 = \frac{V_+}{I_+}, -Z_0 = \frac{V_-}{I_-}, V = V_+ + V_-$$

• 
$$P_{+}(t) = \frac{V_{+}^{2}}{Z_{0}}, P_{-}(t) = -\frac{V_{-}^{2}}{Z_{0}}$$

• 
$$\rho = \frac{V_{-}}{V_{+}}, \ Z = \frac{V}{I} = \frac{V_{+} + V_{-}}{I_{+} + I_{-}} = \frac{V_{+}}{I_{+}} \frac{1 + \frac{V_{-}}{V_{+}}}{1 + \frac{I_{-}}{I_{+}}} = Z_{0} \frac{1 + \rho}{1 - \rho}$$

$$\bullet \quad \rho = \frac{Z - Z_0}{Z + Z_0}$$

• 
$$\rho_i = \frac{i_-}{i_+} = -\rho$$

## Transmission Lines - continued

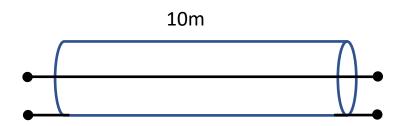
v

### Exercise 10: Coax



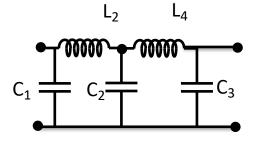
### Exercise 11: Waves

#### Exercise 12: Resonance

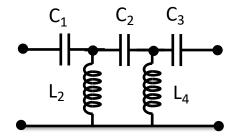


## **Filters**

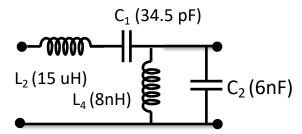
Low pass

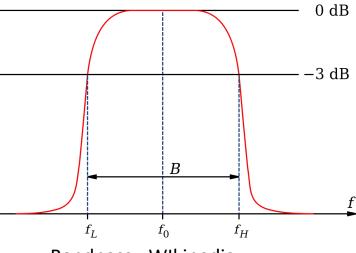


High pass

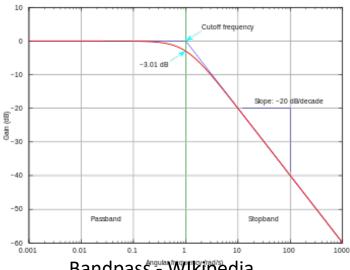


#### 7 MHz bandpass



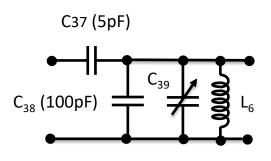


Bandpass - WIkipedia



Bandpass - Wikipedia

## Norcal transmit bandpass filter



• 
$$C_{39} = 50pF$$
,

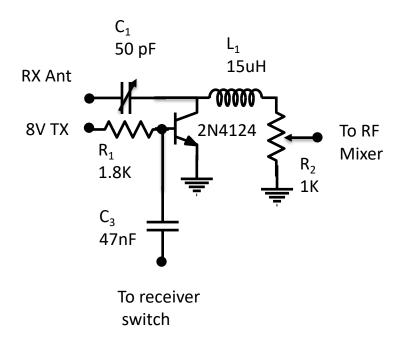
- $L_6$  is 36 turns #28 on T37-2 which has  $A_l = 4 \frac{nH}{turn^2}$
- $L_6 = A_l \cdot 36^2 = 3.1 \mu H$

• 
$$Z_2 = -\frac{j}{(C_{38} + C_{39})\omega_o}$$
,  $Z_3 = jL_6\omega_o$ ,  $Z_1 = \frac{j}{C_{37}\omega_o}$ 

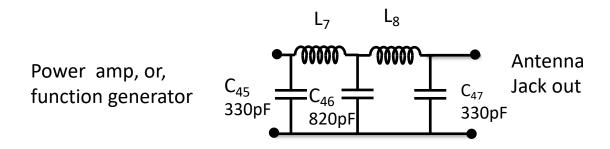
$$Z_{2,3-eq} = \frac{jL_6\omega_0}{L_6(C_{38}+C_{39})\omega_0^2-1}$$

- Resonance is when  $Z_{2,3-eq} \rightarrow \infty$ ,  $\omega_o^2 = \frac{1}{(C_{38}+C_{30})L_6} \approx \frac{10^{18}}{465}$ , when almost all the voltage drop is across  $Z_{2,3-eq}$   $\omega_o = \frac{10^9}{\sqrt{465}} \approx 50.8 \times 10^6$ ,  $f_0 = \frac{\omega_o}{2\pi} \approx 7.1 \ MHz$
- Q of filter is:  $Q_s = \frac{X_s}{R_s}$ .  $R_s$  comes from the other components and must be measured
- Note that  $Z_{2,3-eq}$  is small for the other modulation product

## Norcal RF Filter

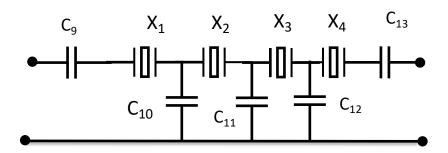


#### Exercise 13: Norcal Harmonic Filter

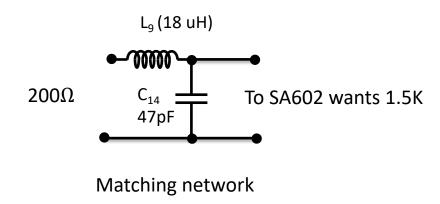


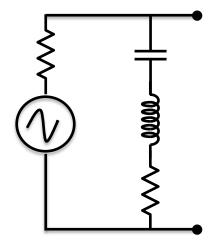
- L<sub>7</sub>, L<sub>8</sub> use T37-2 core, 18 turns, 1.3uH
- Compare loss at 7MHz and 14MHz

#### Exercise 14: Norcal IF Cohn Filter



- X<sub>1</sub> through X<sub>4</sub> are 4.91 MHz
- C<sub>10</sub>, C<sub>11</sub>, C<sub>12</sub> are 270 pF
- Set function generator to  $50 \text{mV}_{pp}$  from function generator
- Calculate R and X for filter





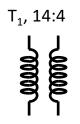
Equivalent circuit for crystal and generator

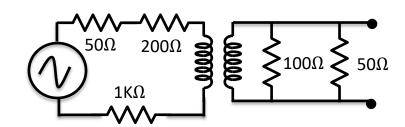
# **Transformers**

• x

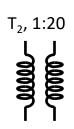
# Norcal matching transformers

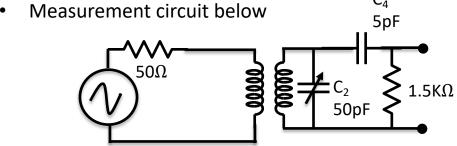
- T<sub>1</sub> is driver matcher uses FT 37-43
- Measurement circuit below



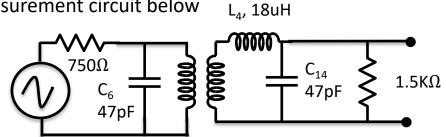


T<sub>2</sub> is RF matcher uses FT 37-61



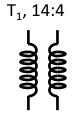


- T<sub>3</sub>, 23:6
- -0000
- T<sub>3</sub> is IF matcher uses FT 37-61
- Measurement circuit below

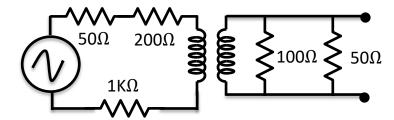


#### Exercise 15: Norcal Driver Transformers

• x

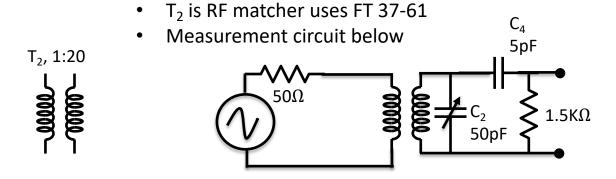


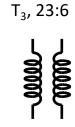
- $T_1$  is driver matcher uses FT 37-43
- Measurement circuit below



#### Exercise 16: Norcal Tuned Transformers

• x





- T<sub>3</sub> is IF matcher uses FT 37-61
- Measurement circuit below

ement circuit below  $C_{4}$ , 18uH  $C_{14}$   $C_{6}$  47pF  $C_{14}$  47pF  $C_{15}$   $C_{14}$   $C_{14}$   $C_{15}$   $C_{15}$ 

#### Acoustics

• 
$$\frac{\partial^2 P}{\partial t^2} = \frac{\gamma P}{\rho} \frac{\partial^2 P}{\partial x^2}$$
,  $v = \sqrt{\frac{\gamma P}{\rho}} = 332 \frac{m}{s}$   
•  $SWR = \frac{\lambda^2}{2\pi A}$ , A is the area of the tube

Sound	L <sub>p</sub>	Power density
rustling leaves	10dB	1pW/m²
broadcast studio	20dB	1pW/m²
classroom	50dB	10nW/m <sup>2</sup>
heavy truck	90dB	1nW/m²
Shout at 1m	100dB	10mW/m <sup>2</sup>
jackhammer	110db	100mW/m <sup>2</sup>
jet takeoff at 50m	120dB	1W/m <sup>2</sup>

# Exercise 17: Tuned Speaker

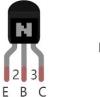
• x

# Exercise 18: Acoustic Standing Wave

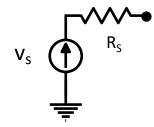
• x

# **Bipolar Transistors**

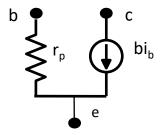
- NPN, PNP
- Model
- $i_C = \alpha i_E$
- $i_C = \beta i_B$
- $\beta = \alpha/(1-\alpha)$
- $\beta \sim 100$







Bipolar source model

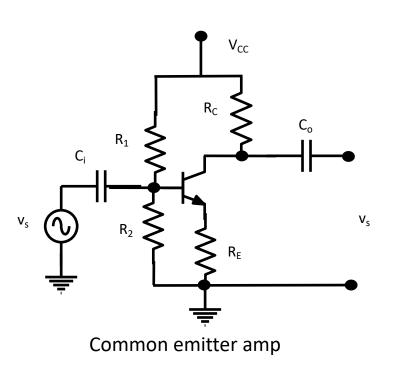


Bipolar equivalent circuit

# **Bipolar Switches**

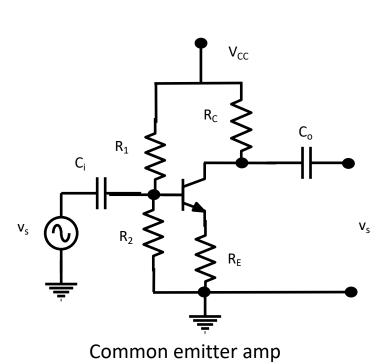
- NPN, PNP
- Model
- $i_C = \alpha i_E$
- $i_C = \beta i_B$
- $\beta = \alpha/(1-\alpha)$
- $\beta \sim 100$

#### BJT common emitter amplifier



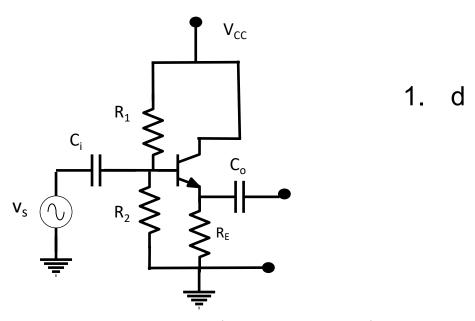
- Here's how to design a common emitter amplifier. We use a 2n3904 transistor with  $\beta$ =150. This circuit will work! Build it.
  - 1. Pick the supply voltage  $V_{cc}$ =12V.
  - 2. Choose a gain (amplification factor), A = 5.
  - 3. Choose the "Q point" of the conducting transistor (4mA).
  - 4.  $V_{cc} = (i_c \cdot R_C) + V_{ce} + i_e R_E \sim i_e \cdot (R_C + R_E) + V_{ce}$  with  $i_c = 4mA$ . We get  $(R_C + R_E) = (V_{cc} V_{ce})/(4mA) = 1.75 \text{ k}\Omega$ .
  - 5. Since A = 5 and A=R<sub>C</sub>/R<sub>E</sub>, R<sub>C</sub>= 5 R<sub>E</sub> so R<sub>E</sub>  $\sim$  270  $\Omega$  (this is a standard resistor value) and R<sub>C</sub>= 1.5k $\Omega$ .

### BJT common emitter amplifier continued



- 6.  $i_b = 4mA/\beta = 27 \mu A$ .
- 7. Since  $V_{be}$  must be greater than .7V throughout the input signal range, we want the voltage across  $R_2$  to satisfy  $V_{be}$  +  $i_cR_E$  = 1.8V.
- 8. We insert a voltage divider consisting of  $R_1$  and  $R_{2}$ , so that  $R_1$ = (12-1.8)/270  $\mu$ A  $\sim$  39 k $\Omega$ .
- 9.  $C_o$  and  $C_i$  are picked to offer small resistance to the frequency range we're interested in and  $C_o = C_i = 5 \mu F$ .
- I haven't explained why we want  $R_E$  but it provides thermal stability for the transistor over the range we care about. The fact that  $A=R_C/R_E$  can be calculated using Kirchhoff's laws.

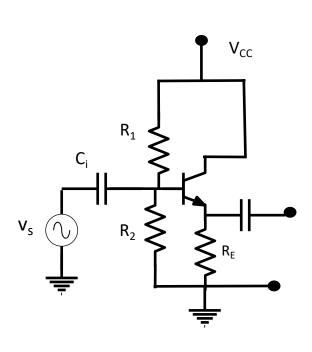
# BJT common collector amplifier



Common collector amp (Emitter Follower)

Common collector amp

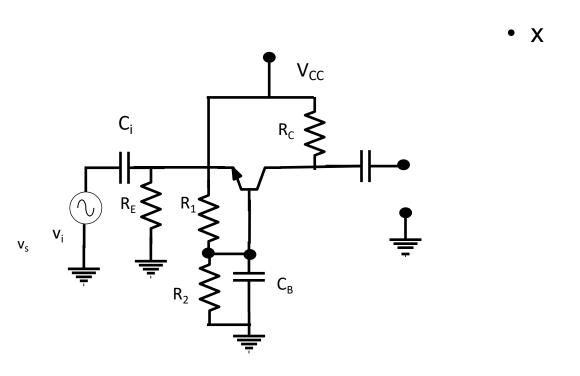
# BJT common collector amplifier continued



6. x

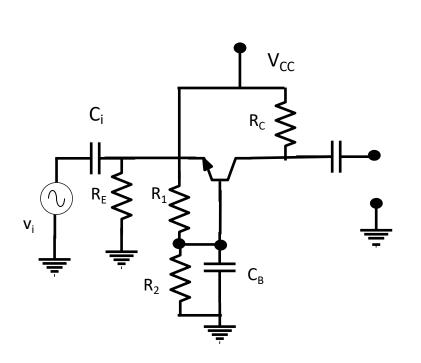
Common collector amp (Emitter Follower)

# BJT common base amplifier



Common base amp

# BJT common base amplifier continued

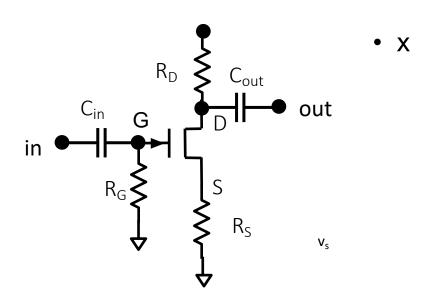


6. x

Common base amp

# **JFETs**

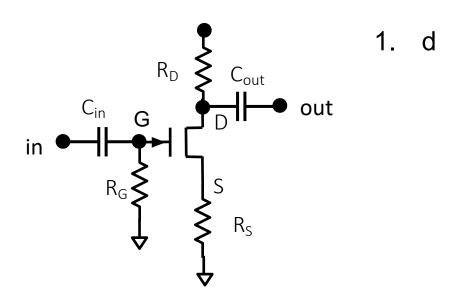
# JFET Common Emitter Amplifier



# JFET common emitter amplifier continued

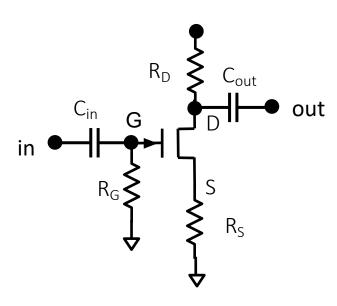
6. x

# JFET common source amplifier

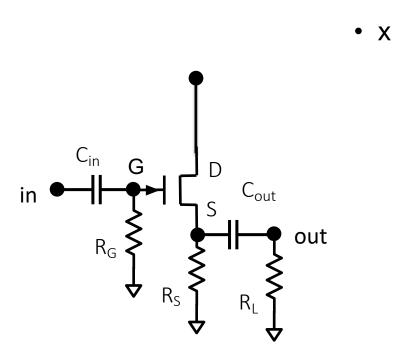


# JFET Common Source Amplifier continued

6. x

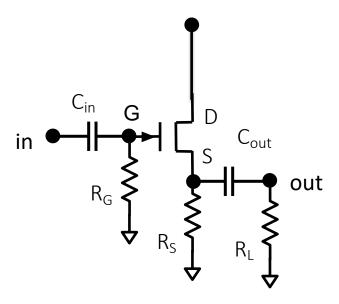


# JFET common drain amplifier

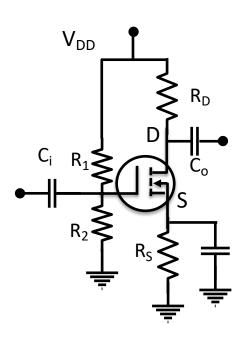


# JFET common drain amplifier continued

6. x



### CMOS common emitter amplifier



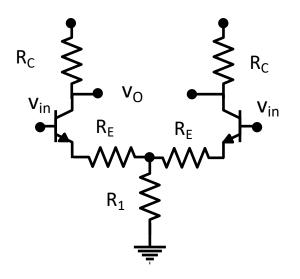
- Pick power
- $\bullet \quad V_{DD} = i_D R_D + V_{DS} + i_D R_S$
- $V_{GS} = V_G i_S R_S$   $V_G = V_{DD} \frac{R_1}{R_1 + R_2}$   $i_D = k(V_G V_{TH})^2$

- Bias around  $\frac{V_{DD}}{3}$  Pick gain,  $A = \frac{R_D}{R_S + \frac{1}{a_m}}$

# Differential Amplifier

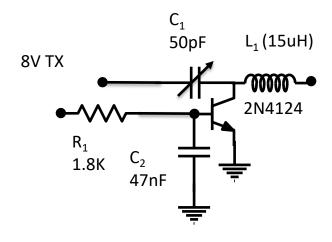
- Two port model
- $\bullet \quad \begin{pmatrix} i_1 \\ i_2 \end{pmatrix} = \begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}$

#### Differential amplifier



- Pick power  $\pm 12$
- Choose collecter current ( 2mA) by picking  $R_1$
- Pick gain,  $A = \frac{R_C}{2R_E}$

#### Exercise 19: Norcal receiver switch



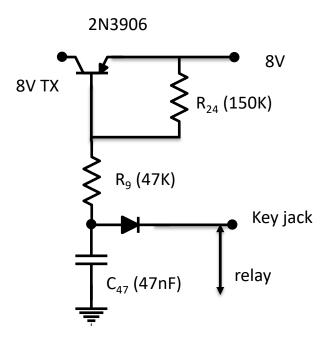
• Receiver mixer or an oscilloscope with  $50\Omega$ 

When transistor conducts the receiver filter shorts

Harmonic filter

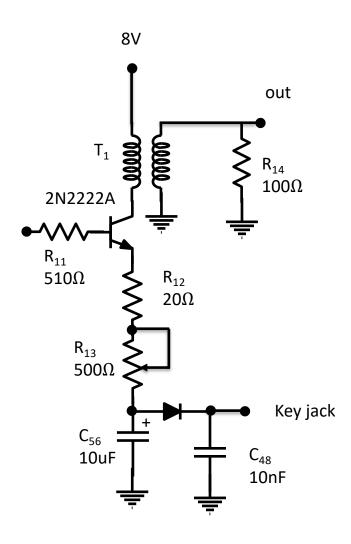
If using function generator use a 1.8K resistor

#### Exercise 20: NorCal transmitter switch



When key is down, transistor conducts

#### Exercise 21: Norcal Driver

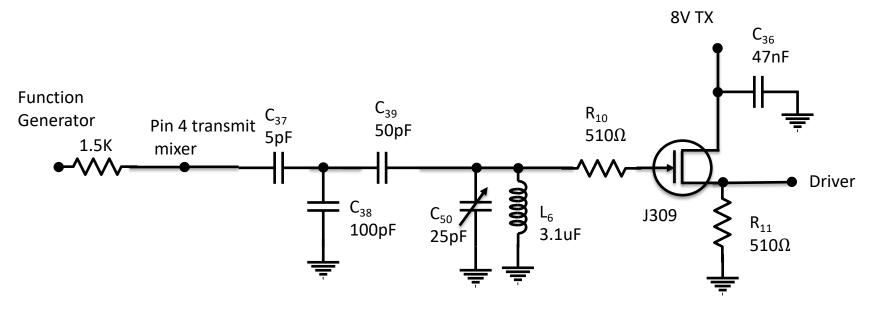


• Use  $50\Omega$  scope probe

# Exercise 22: Emitter degeneration

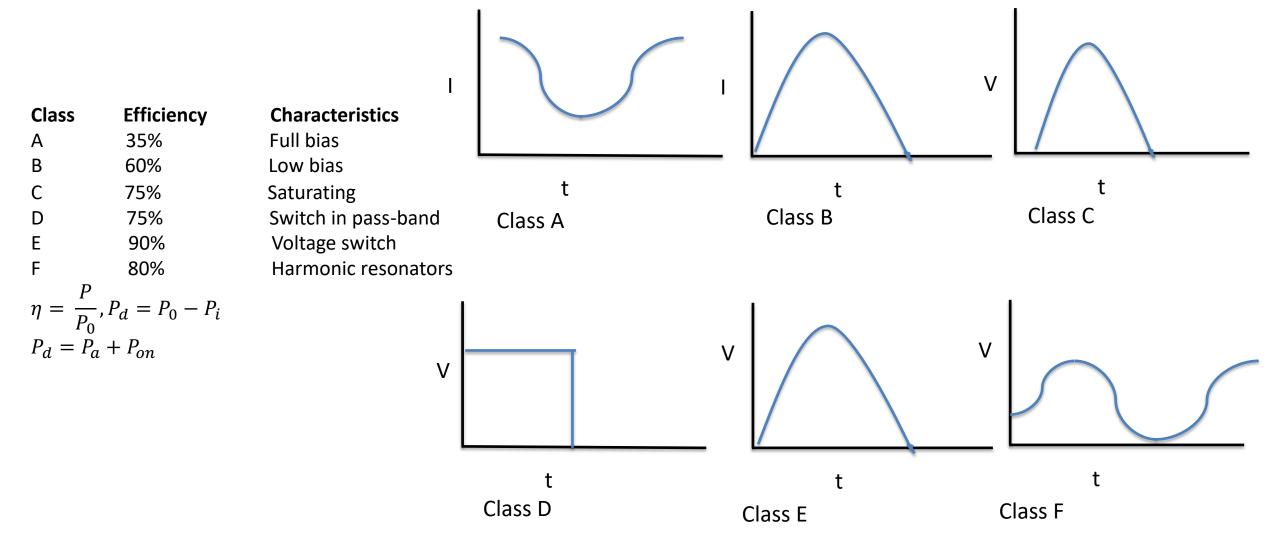
• Use  $50\Omega$  scope probe

# Exercise 23: Norcal Buffer amplifier



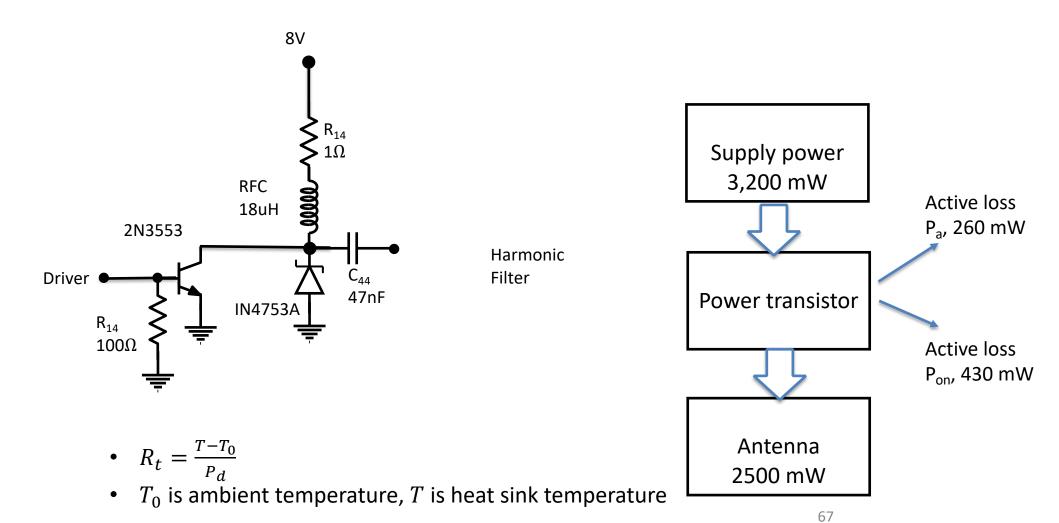
$$G_V = \frac{V}{V_i}$$

# Amplifier classes



### Exercise 24: Norcal Power Amp

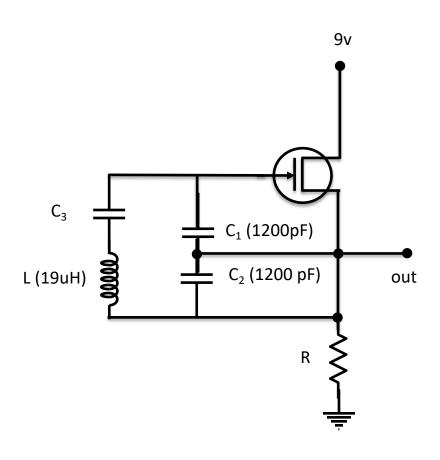
Norcal-40 Power amp is class C



# Exercise 25: Power modelling

• Use  $50\Omega$  scope probe

# Clapp oscillator



• 
$$i_d = g_m v_{gs}$$

• Resonance: 
$$-\frac{1}{j\omega_0 c_2} = j\omega_0 L + \frac{1}{j\omega_0 c_3} + \frac{1}{j\omega_0 c_1}$$

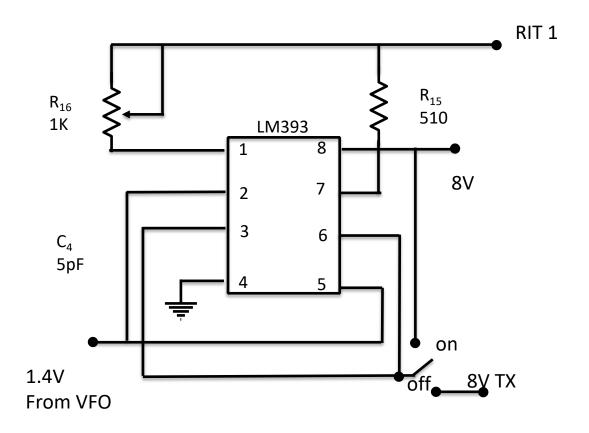
• 
$$\omega_0 = \frac{1}{\sqrt{LC}}, C = C_1 ||C_2||C_3$$

• At resonance, 
$$v_{gs} = Ri_d \frac{c_1}{c_2}$$
,  $L = \frac{c_1}{Rc_2}$ 

• Oscillation continues if 
$$g_m > \frac{C_1}{RC_2}$$

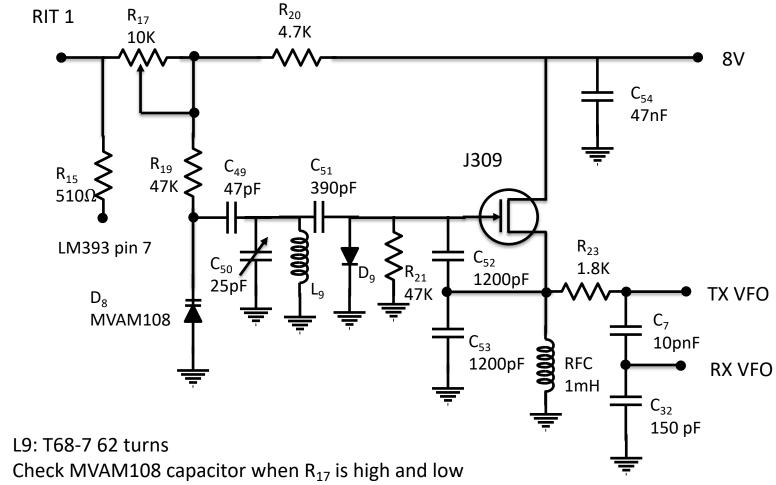
• 
$$v_{gs} = 2v_s$$

## Norcal Receiver Incremental Tuning (RIT)



- LM393 is a comparator
- For function generator connect through 1.5K

#### Exercise 26: Norcal VFO



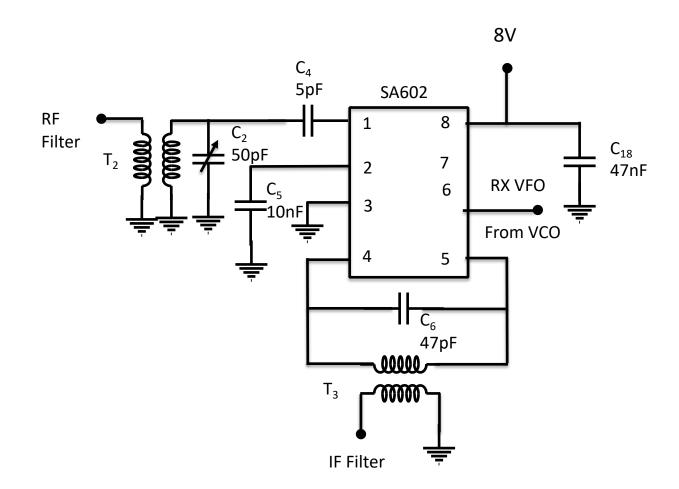
- Start resistor (R<sub>21</sub>) pulls gat to ground at start
- When gain limiting diode (D9) conducts, it pulls gate negative
- Oscillator keeps growing as long as g<sub>m</sub>>1/R

# Exercise 27: Gain limiting

• *x* 

## Mixers

#### Exercise 28: Norcal RF Mixer

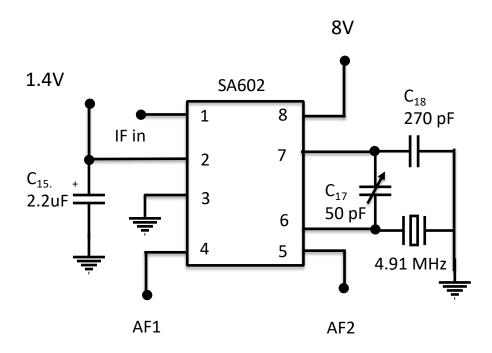


50mVpp if

generator

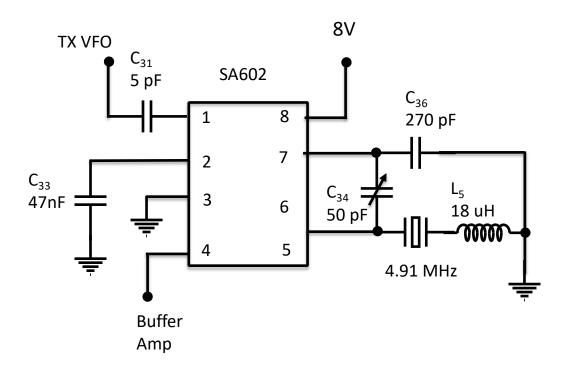
using function

#### Exercise 29: Norcal Product Detector

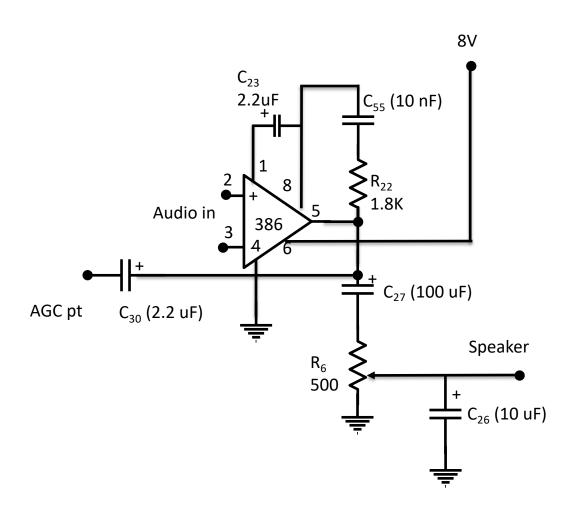


• 620 Hz output through AF1 and AF2

#### Exercise 30: Norcal transmit mixer and oscillator

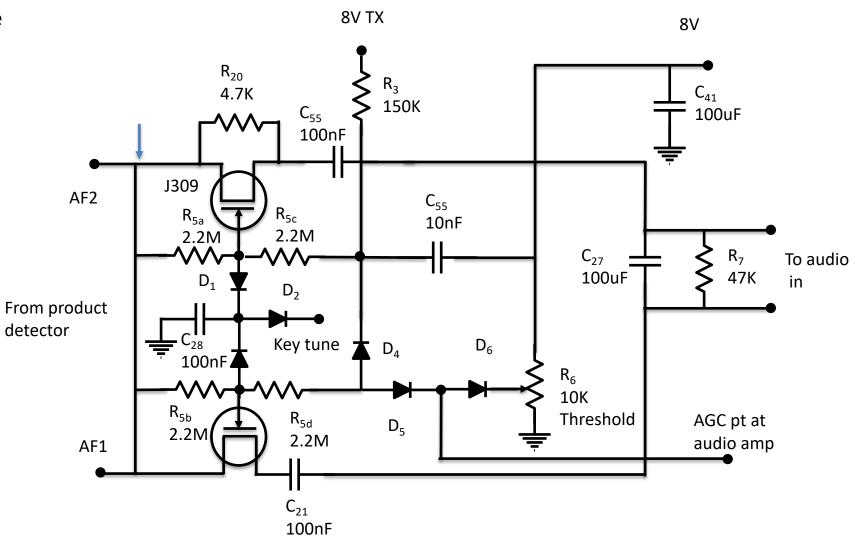


# Exercise 31: Norcal Audio Amp



#### Exercise 32: Norcal AGC

Connect to function generator through 300K, here

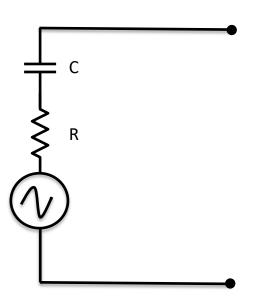


# Exercise 33: Alignment

## Antennas and propagation

- From Maxwell, for a plane wave (E in x direction, H in y direction), wave is of form  $\exp(j\omega t j\beta z)$
- $\nabla \times E = -j\mu_0 \omega H$
- $\nabla \times B = j\epsilon_0 \omega E$
- $\beta \hat{z} \times E = \mu_0 \omega H$ ,  $\beta E_x \hat{y} = \mu_0 \omega H$
- Substituting and taking the restricted cross products, we get:  $\beta E_x = \omega \mu_0 \frac{\omega \epsilon_0}{\beta}$ , so  $\beta = \omega \sqrt{\mu_0 \epsilon_0}$
- Power density:  $S = Re\left(\frac{E_x \overline{H_y}}{2}\right) = \frac{(|E_x|)^2}{2\eta_0}$
- $\bullet \quad \eta_0 = \frac{E_x}{H_y} = \sqrt{\frac{\mu_0}{\epsilon_0}} = 377\Omega$
- Impedance:  $P_t = \frac{R|I|^2}{2}$ , R is real part of Z,  $R = R_r + R_l$ ,  $\eta = \frac{R_r}{R}$
- Power density for isotropic antenna:  $S_i = \frac{P_t}{4\pi r^2}$
- Define  $G(\theta, \phi) = \frac{S(\theta, \phi)}{S_r}$ .  $S(\theta, \phi)$  is just the Poynting vector
- For isotropic reference,  $G = \frac{4\pi r^2 S}{P_t}$

Receiving antenna Thevenin



#### Antennas and propagation

- Receiving antenna:
- $V_0 = hE$ , h is effective antenna length ( $h = \frac{l}{2}$  for short antenna)
- For dipole:  $V_0 = \frac{l}{2} E \sin(\theta)$
- $A(\theta, \phi) = \frac{P_r}{S(\theta, \phi)}$ . This is the definition of the effective area, A.
- By reciprocity,  $A(\theta, \phi) = \frac{\lambda^2}{4\pi} G(\theta, \phi)$
- $P_r = \frac{|V_0|^2}{8R_a} = \frac{|hE|^2}{8R_a}$ , so
- $P_r = \frac{h^2 S \eta_0}{4R}$   $A = \frac{h^2 \eta_0}{4R}$

## Antennas and propagation

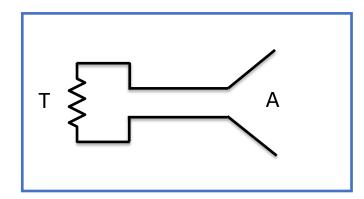
- Antenna theorem:  $\oint A \ d\Omega = \lambda^2$
- For cavity on right, T is constant at thermodynamic equilibrium and the same power is transmitted and emitted, the Johnson noise is kT. The energy received is

$$E=rac{4\pi kT}{c\lambda^2}$$
. Set  $B=rac{kT}{\lambda^2}$ .  $kT=\oint BA\ d\Omega=\oint Arac{kT}{\lambda^2}\ d\Omega$ , which gives the antenna theorem

- For transmitting/receiving antenna pairs:  $G_1A_2=\frac{|V|^2\pi r^2}{|I|^2R_1R_2}=G_2A_1$ . So  $\frac{G_1}{A_1}=\frac{G_2}{A_2}=\frac{4\pi}{\lambda^2}$
- Friis formulas

• 
$$S = \frac{P_t G}{4\pi r^2}$$
,  $P_r = SA = \frac{P_t GA}{4\pi r^2}$ 

#### Insulated cavity



## Reciprocity and dipole

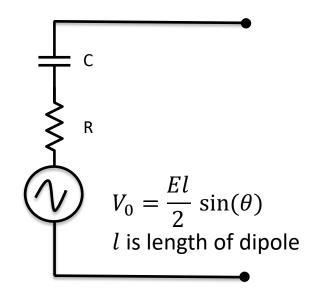
Dipole Thevenin equivalent circuit

• For dipole (Length: 
$$l = \frac{\lambda}{2}$$
)

• 
$$\lambda^2 = \int A \ d\Omega = \int \frac{h^2 \eta_0}{4R_r} \ d\Omega$$
, so

• 
$$R_r = \frac{l^2 \eta_0}{16\lambda^2} \int \sin^2(\theta) d\Omega = \eta_0 \frac{\pi}{6} \left(\frac{l}{\lambda}\right)^2$$

• 
$$R_r=\frac{l^2\eta_0}{16\lambda^2}\int sin^2(\theta)d\Omega=\eta_0\frac{\pi}{6}(\frac{l}{\lambda})^2$$
  
•  $A=\frac{3\lambda^2}{8\pi}sin^2(\theta)$  and  $G=1.5sin^2(\theta)$ . Note we used  $h=\frac{l}{2}\sin(\theta)$ 



• For Norcal, G = 1,  $A = 150m^2$ , for r = 2000 m,  $P_r = 6pW$ 

#### Noise

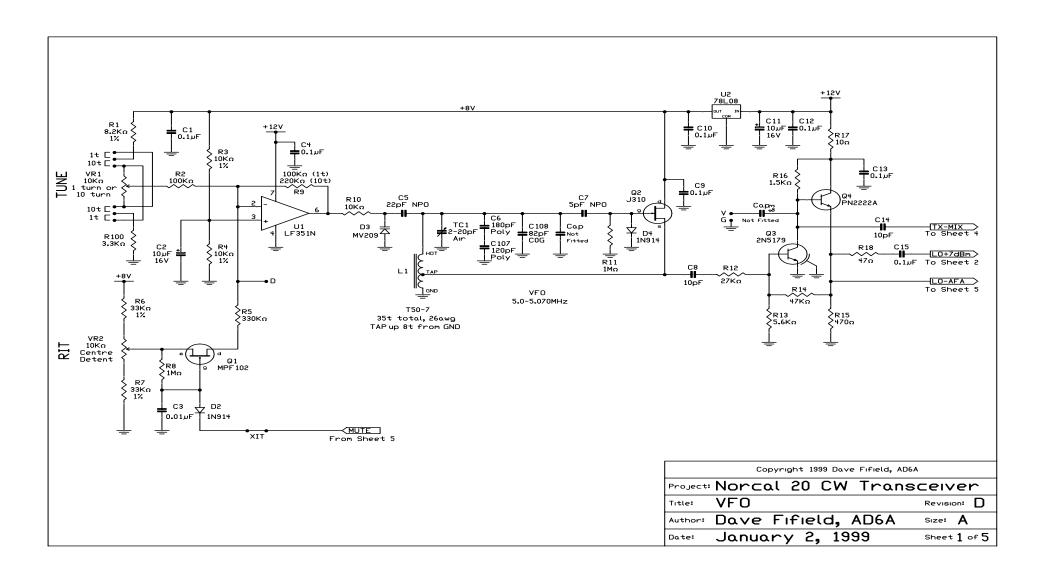
• 
$$V_{n(rms)} = \sqrt{\frac{1}{\tau} \int_0^{\tau} V(t)^2} dt$$

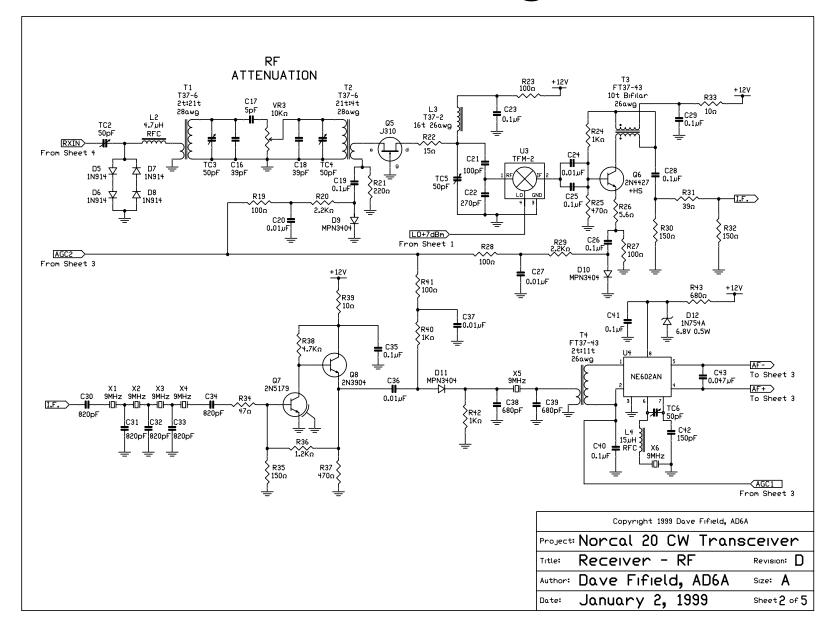
- $V_{n(rms)} = \sqrt{\frac{1}{\tau} \int_0^{\tau} V(t)^2} dt$   $P_n = \frac{V_{n(rms)}^2}{R}$ , R is load resistance
- $SNR = \frac{P}{P_n}$
- $MDS = \frac{P_n}{G}$
- Nyquist
- $V_C = \frac{1}{j\omega C} \frac{V_n}{R + j\omega L + \frac{1}{j\omega C}}$
- $\overline{|V_C|^2} = \frac{\overline{|V_n|^2}}{|1-\omega^2 LC + j\omega RC|^2}$
- Expected energy at resonance is  $kT = \frac{c}{2} \int_0^\infty |V_c|^2 df$
- $\bullet \int_0^\infty \frac{1}{|1 \omega^2 LC + i\omega RC|^2} df = \frac{1}{4RC}$
- So,  $|V_c|^2 = 8kTR$

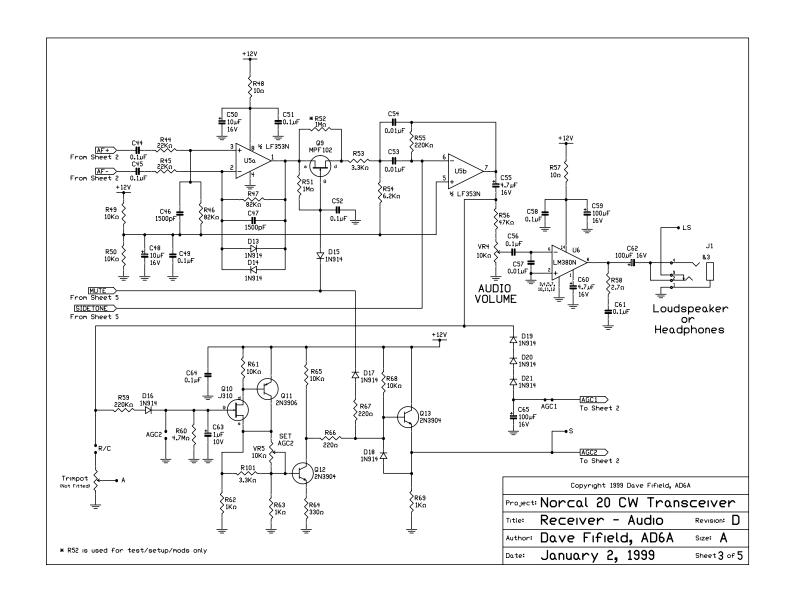
#### Exercise 35: Intermodulation

#### Exercise 37: Antennas

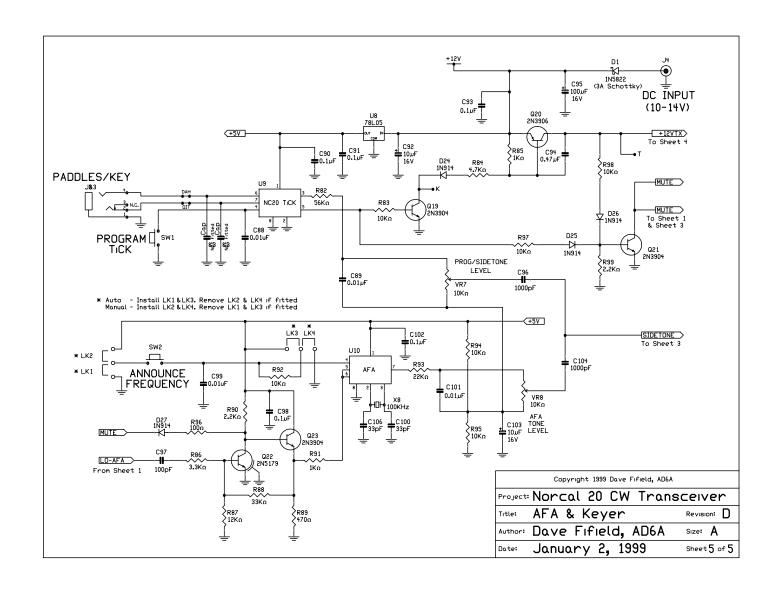
# Exercise 38: Propagation







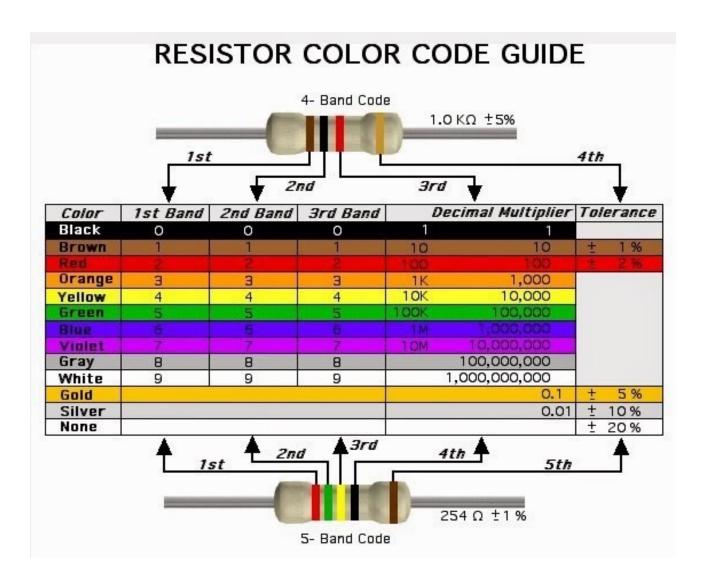




#### Morse

Symbol	Code	Symbol	Code	Symbol	Code
a	•_	m		У	
b		n	_•	Z	
С		0		0	
d		р	··	1	•
e	•	q	·_	2	
f		r		3	
g		S	•••	4	
h	••••	t	_	5	••••
i	••	u		6	
j	•	V		7	
k		W	•	8	
Ī		Х		9	

#### Color codes



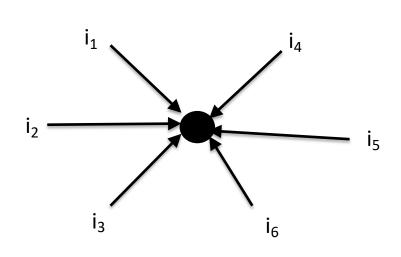
Resistors: ohms

Capacitors: picoFards

Inductors: milliHenries

# Kirchhoff

• There are two Kirkoff's laws, one describes voltages the other describes currents.



$$i_1 + i_2 + i_3 + i_4 + i_5 + i_6 = 0$$

