

## For spherical triangle

$$\frac{\cos(\alpha) = \cos(A)\sin(\beta)\sin(\gamma) + \cos(\beta)\cos(\gamma)}{\sin(A)} = \frac{\sin(\beta)}{\sin(B)} = \frac{\sin(\gamma)}{\sin(C)}$$

- N is North Pole
- O is observer at latitude  $\lambda$
- R<sub>1</sub> is position of sun at sunrise OR<sub>1</sub>=90
- R<sub>2</sub> is position of sun at sunrise OR<sub>2</sub>=90
- T<sub>1</sub> is longitude of sun at sunrise
- T<sub>2</sub> is longitude of sun at sunset
- $NR_1 = \cos(90 + \epsilon) = -\cos(\alpha)\cos(\lambda) = -\sin(\epsilon)$
- So,  $\cos(\alpha) = \frac{\sin(\epsilon)}{\cos(\lambda)}$  (equation 1)
- $CT_1 = \beta$
- $\sin(\beta) = \frac{\sin(\alpha)}{\cos(\epsilon)}$  (equation 2)
- 1. Solve for  $\alpha$  in equation 1
- 2. Solve for  $CT_1 = \beta$  in equation 2
- 3. Length of day is  $\frac{2CT_1}{180} \cdot 12$  hours
- Note  $\epsilon(t) = 23.5 \cdot cos(t)$ , t is number of days since December 22 divided by 365.25 times  $2\pi$