Electronics of Radio

Notes on David Rutledge's book

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Basic concepts

- Potential difference (V, ϕ) : $\phi = \int_a^r E \cdot ds$, energy per charge, 1V = 1 J/s
- Kirkoff 1: $\sum_{loop} V_i = 0$ (Conservation of energy)
- Kirkoff node: $\sum_{node} I_i = 0$ (Conservation of charge)
- $V(t) = V_p \cos(\omega t)$, $\omega = 2\pi f$, $I(t) = I_p \cos(\omega t)$, $\omega = 2\pi f$
- Instantaneous power: $P(t) = V(t)I(t) = V_pI_p \cos^2(\omega t)$
- Average power: $P_a = \int_0^{1/f} V(t) I(t) dt = V(t) I(t) = \int_0^{2\pi/\omega} V_p I_p \cos^2(\omega t) dt = \frac{V_p I_p}{2}$
- Band names:

| Name | Frequency |
|------|-------------|
| VLF | 3-30kHz |
| LW | 20-300kHz |
| MW | 300kHz-3MHz |
| HF | 3MHz-30MHz |
| VHF | 30-300MHz |

| Name | Frequency |
|-----------|-------------|
| UHF | 300MHz-1GHz |
| uW | 1-30GHz |
| milliW | 30-300GHz |
| submilliF | >300GHz |

Signals

- Gain (G) expressed in decibels: $G = 10 \log_{10}({^{P_{out}}/_{P_{in}}})$
- Mixer:

•
$$V(t) = \cos(\omega_1 t) \cos(\omega_2 t) = \frac{1}{2} [\cos(\omega_+ t) + \cos(\omega_- t)], \omega_+ = \omega_1 + \omega_2, \omega_- = \omega_1 - \omega_2$$

Modulation

| Name | Equation |
|------|---|
| AM | $V(t) = a(t)\cos(\omega_c t)$ |
| FM | $V(t) = V_c \cos((\omega_c + a(t))t)$ |
| FSK | $V(t) = V_c \cos(\omega_1 t)$, if 1 $V(t) = V_c \cos(\omega_0 t)$, if 0 |
| PSK | $V(t) = +V_p \cos(\omega t), \text{ if } 1$ $V(t) = -V_p \cos(\omega t), \text{ if } 0$ |

Resistors, capacitors, inductors

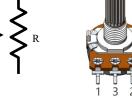
















Resistors

- Analytic model: IR = V
- Energy dissipated: $E = \int_{t_i}^{t_f} IV \, dt = \int_{t_i}^{t_f} I^2 R dt$
- Capacitors
 - Analytic model: CV = q, $C\frac{dV}{dt} = i$
 - Capacitor Energy stored: $E = \int_{t_i}^{t_f} CV \frac{dV}{dt} dt = \frac{1}{2} CV^2$
- Inductors
 - Analytic model: $V = L \frac{di}{dt}$
 - Inductor Energy stored: $E = \int_{t_i}^{t_f} IV \, dt = \int_{t_i}^{t_f} LI \frac{dI}{dt} \, dt = \frac{1}{2} LI^2$

Credit: Make Electronics

Diodes, transformers

Diodes

- Devices that allow current to flow only in one direction
- Silicon diodes, for example have, essentially infinite resistance if V_{ac} <0, that is if the cathode is at a higher potential than the anode and very low resistance if V_{ac} > .7V.
- The cathode is usually labelled with a band
- Transformers
 - AC only: $\frac{N_2}{N_1} = \frac{V_2}{V_1}$

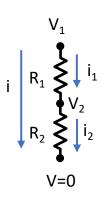


Credit: Make Electronics



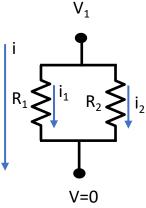


Simple circuit analysis with Kirchhoff



- R_{eq} is the equivalent resistance, replacing the top left circuit with a single resistance.
- Top ier. S...

 By Kirchhoff's node rule, $i_1 = i_2 = \iota$, so $\frac{V_2}{R_1} = \frac{V_2}{R_2} = \frac{V_1}{R_2} \text{ thus } \frac{R_1}{R_{eq}} V_1 = V_1 V_2 \text{ and}$ $\frac{R_2}{R_{eq}} V_1 = V_2. \text{ Adding, we get } \frac{R_1}{R_{eq}} V_1 + \frac{R_2}{R_{eq}} V_1 = \frac{d(V_1 V_2)}{dt} = \frac{d(V_1 V_2)}{dt$



- Again let R_{eq} is the equivalent resistance, replacing the bottom left circuit with a single resistance.
- By Kirchhoff's node rule, $i_1 + i_2 = i$, so

$$\bullet \ \frac{V_1}{R_1} + \frac{V_1}{R_2} = \frac{V_1}{R_{eq}}.$$

• Solving, we get. $\frac{R_1R_2}{R_1+R_2}=R_{eq}$

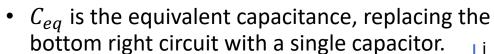
- C_{eq} is the equivalent capacitance, replacing the top right circuit with a single capacitor.

•
$$C_1 \frac{d(V_1 - V_2)}{dt} = C_2 \frac{d(V_2)}{dt} = C_{eq} \frac{dV_1}{dt}$$

•
$$\frac{C_{eq}}{C_1} \frac{d(V_1)}{dt} = \frac{d(V_1 - V_2)}{dt}$$
 and
$$\frac{C_{eq}}{C_2} \frac{d(V_1)}{dt} = \frac{d(V_2)}{dt}$$



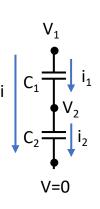
•
$$\frac{C_{eq}}{C_1} + \frac{C_{eq}}{C_2} = 1$$
 and solving, we get. $\frac{C_1C_2}{C_1 + C_2} = C_{eq}$

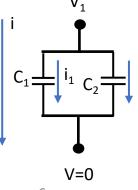




•
$$C_{eq} \frac{dV_1}{dt} = C_1 \frac{dV_1}{dt} + C_2 \frac{dV_1}{dt}$$
, so

•
$$C_{eq} = C_1 + C_2$$





Simple circuit analysis with Kirchhoff



- Let L_{eq} be the equivalent inductance, replacing the top left circuit with a single inductor.
- By Kirchhoff's node rule, $i_1 = i_2 = i$, so

•
$$L_{eq} \frac{di}{dt} = V_1$$
, $L_1 \frac{di_1}{dt} = V_1 - V_2$, $L_1 \frac{di_2}{dt} = V_2$

•
$$V_1 = L_{eq} \frac{di}{dt} = L_1 \frac{di}{dt} + L_2 \frac{di}{dt}$$
 and

•
$$L_{eq} = L_1 + L_2$$



• Let L_{eq} be the equivalent inductance, replacing the bottom left circuit with a $\frac{di}{dt} = V_1 \quad di_1 \quad V_1 \quad di_2 \quad V_1$

$$\frac{V_1}{L_{eq}}, \frac{di_1}{dt} = \frac{V_1}{L_1}, \frac{di_2}{dt} = \frac{V_1}{L_2},$$

- single inductor.
- By Kirchhoff's node rule, $i_1 + i_2 = i$, so

•
$$\frac{V_1}{L_{eq}} = \frac{V_1}{L_1} + \frac{V_1}{L_2}$$
 and

$$L_{eq} = \frac{L_1 L_2}{L_1 + L_2}$$

• The circuit on the right, is useful and is called a *voltage divider*.

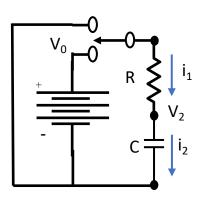
•
$$i = i_1 = i_2$$
 so $\frac{V_1 - V_2}{R_1} = \frac{V_2}{R_2}$, $V_1 - V_2 = \frac{R_1}{R_2} V_2$

• Thus,
$$V_1 = (1 + \frac{R_1}{R_2})V_2$$
 and so

•
$$V_2 = \frac{R_2}{R_1 + R_2} V_1$$



Simple circuit analysis with Kirchhoff



RC behavior: charging

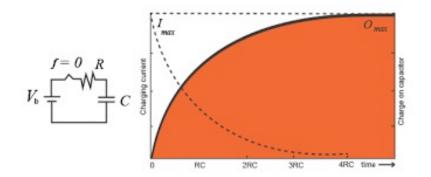
•
$$V_0 - V_2 = i_1 R = V_R, i_1 = \frac{V_R}{R}$$

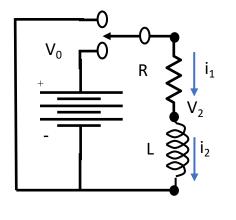
•
$$i_2 = C \frac{dV_2}{dt}$$
, $V_C = V_2$

•
$$i_1 = i_2$$
, $V_C = V_0 - V_R$

•
$$i_1 = i_2$$
, $V_C = V_0 - V_R$
• $\frac{V_R}{R} = C \frac{dV_C}{dt}$, $RC \frac{dV_C}{dt} = V_0 - V_C$, or $RC \frac{dV_C}{dt} + V_C = V_0$







RL behavior: charging

•
$$V_0 - V_2 = i_1 R = V_R$$

•
$$V_L = V_2 = L \frac{di_2}{dt}$$

•
$$V_L = V_2 = L \frac{di_2}{dt}$$

• $i_1 = i_2, V_R = V_0 - V_L$, so $L \frac{d}{dt} \frac{V_0 - V_L}{R} = V_L$

$$\bullet \ \frac{L}{R} \frac{d V_L}{dt} + V_L = 0$$

• Solution is $V_L = V_0 e^{-\frac{Rt}{L}}$



Phasors

- V(t) = RI(t)
- $V(t) = L\dot{I}(t)$
- $I(t) = C\dot{V}(t)$
- Suppose $V(t) = Acos(\omega t + \theta)$ and $I(t) = Bcos(\omega t + \phi)$. If $\phi > \theta$, we say the current leads the voltage.
- $V(t) = Re(e^{j(\omega t + \theta)})$, and $I(t) = Re(e^{j(\omega t + \phi)})$
- Now define $V = Ae^{j\theta}$ and $I = Be^{j\phi}$, so |V| = A, |I| = B, $\angle V = \theta$, and $\angle I = \phi$. V and I are called phasors and do not include time. Note that $V(t) = Re(Ve^{j\omega t})$ and $I(t) = Re(Ie^{j\omega t})$.
- Note that $I = CVj\omega$, for a capacitor and $V = LIj\omega$, for an inductor

Circuit analysis with Kirchhoff and impedance

- Impedance unifies the "simple" ohms law with capacitance and inductance.
- Z=R, for resistors, $Z=j\omega L$, for inductors and $Z=\frac{1}{j\omega C}$, for capacitors.
- In general, Z = R + jX and all the ohm like laws hold for resistors, capacitors and inductors .
 - $Z_{eq} = Z_1 + Z_2$ for two components with impedance Z_1, Z_2 connected in series
 - $Z_{eq} = \frac{Z_1 2}{Z_1 + Z_2}$ for two components with impedance Z_1, Z_2 connected in parallel
- For example, for a resistor and capacitor in series has impedance $Z = R + \frac{1}{j\omega C}$

Phasors, impedance and power

- For the circuit on the right, $Z = R + \frac{1}{i\omega C}$ is the impedance for the resistor and capacitor in series.
- The phasor $I=\frac{V_0}{Z}$ and the phasor $V=\frac{I}{j\omega C}=\frac{V_0}{1+j\omega RC}$ Further, $|I|=\frac{V_0}{|Z|}$, $\angle I=\angle\frac{V_0}{|Z|}$ and $|V|=\frac{|I|}{|j\omega C|}=|\frac{V_0}{1+j\omega RC}|$



- The average power is $P_a = Re(P) = Re(\frac{V\overline{I}}{2})$. We define the reactive power as $P_r = Im(P)$.
- $P_r = \omega(E_L E_C)$, where E_L and E_C are respectively, the energy stored in the inductor and capacitor respectively.



Q and phasors

- Consider the series resonance on the right. $Z_{LCR} = R + j \left(\omega L \frac{1}{\omega C}\right)$
- The phasor, $I = \frac{V_0}{Z_{LCR}}$, and the phasor $V_R = \frac{V_0}{Z_{LCR}} Z_R$, where $Z_R = R$.
- So $V_R = \frac{RC\omega V_0}{RC\omega + i(LC\omega^2 1)}$.
- $|V_R|$ is maximum when $\omega^2 LC = 1$. Put $\omega_0 = \frac{1}{\sqrt{LC}}$. When $\omega = \omega_0$, $|V_R| = V_R = V_0$.
- $|V_R| = \frac{V_0}{\sqrt{2}}$, when X = R. Note that the power through R when X = R is half the power through R when X=0 or $\omega=\omega_0$.



- We define $Q = \frac{X}{R} = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 CR}$.
- Solving for ω_u and ω_l , we get $\frac{L\omega_u}{\omega_0} \frac{\omega_0}{c\omega_u} = R$ and $\frac{L\omega_l}{\omega_0} \frac{\omega_0}{c\omega_l} = -R$, or, in terms of Q, $\frac{\omega_u}{\omega_0} \frac{\omega_0}{\omega_u} = \frac{1}{Q}$ and $\frac{\omega_l}{\omega_0} \frac{\omega_0}{\omega_l} = -\frac{1}{Q}$. In fact, $\omega_0 = \sqrt{\omega_u \omega_l}$, and so $\frac{\omega_u}{\omega_0} \frac{\omega_l}{\omega_0} = \frac{1}{Q}$.
- Thus $Q = \frac{\omega_0}{\omega_0 \omega_I} = \frac{\omega_0}{\Delta \omega}$
- From the definition of P_a , earlier, $Q = \omega_0 \frac{E}{P_a}$, where E is the total energy stored in L and C, which is in turn the peak E_L and peak E_C at resonance.



Phasors, impedance and power

- For the circuit on the right, $Z = R + \frac{1}{i\omega C}$ is the impedance for the resistor and capacitor in series.
- The phasor $I=\frac{V_0}{Z}$ and the phasor $V=\frac{I}{j\omega C}=\frac{V_0}{1+j\omega RC}$ Further, $|I|=\frac{V_0}{|Z|}$, $\angle I=\angle\frac{V_0}{|Z|}$ and $|V|=\frac{|I|}{|j\omega C|}=|\frac{V_0}{1+j\omega RC}|$

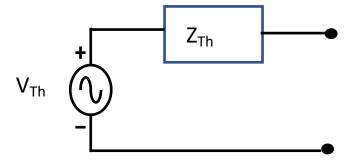


- The average power is $P_a = Re(P) = Re(\frac{V\overline{I}}{2})$. We define the reactive power as $P_r = Im(P)$.
- $P_r = \omega(E_L E_C)$, where E_L and E_C are respectively, the energy stored in the inductor and capacitor respectively.



Thevenin and Norton

 Thevenin: Any combination of linear sources and passive elements terminating in two terminals is equivalent to a pure voltage source in series with an impedance



 Norton: Any combination of linear sources and passive elements terminating in two terminals is equivalent to a pure current source in parallel with an conductance



Similar theorems for two terminal input and output devices (with transfer function)

Thevenin and Norton

- We can use lookback resistance to calculate the Thevenin equivalent resistance and ideal source.
- To find the lookback resistance, short the source and apply the usual laws.
 - Here $R_s = R_1 || R_2$
- To find the new ideal source, notice R_1 and R_2 form a voltage divider.
 - The new source voltage is $\frac{V_0 R_2}{R_1 + R_2}$



Is equivalent to



Exercise 1: Resistors



- L. Consider (A). Find the formula for power in the load. Find the R_l that maximizes the power to the load.
 - $V_l = \frac{R_l}{R_S + R_l} V_0$, $I_l = \frac{V_0}{R_S + R_l}$.
 - $P_l = V_l I_l = \frac{R_l}{(R_S + R_l)^2} V_0^2$, which is maximum when $R_l = R_S$
- 2. Find the Thevenin and Norton parameters fore (B).

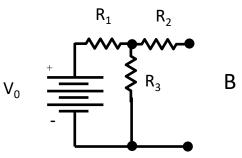
•
$$V_{Th} = \frac{R_3}{R_1 + R_3} V_0$$

•
$$R_{Th} = R_2 + R_1 || R_3$$

3. Find the Thevenin and Norton parameters fore (C).

•
$$V_{Th} = \frac{R_3}{R_2 + R_3} V_0$$

•
$$R_{Th} = R_2 ||R_3|$$



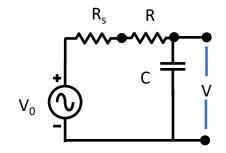


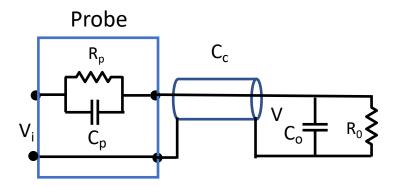
Exercise 2: Sources

Skip

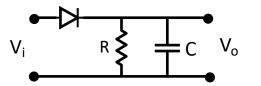
Exercise 3: Capacitors

- 1. In the circuit on the right, V_0 is a 2 volt pp ideal square wave source of frequency 20Hz, $R_S=50\Omega$, $R=300k\Omega$ and C=10~nF.
- 2. What is the voltage, V, at the output? The scope has an input resistance of $1M\Omega$.
- 3. Let t_2 , the time to discharge to 0V. Calculate τ and t_2 .
- 4. Capacitance on the scope prevents the delay from being 0. Measure the new t_2 with these changes.
- 5. Given C_0 and C_p and R_p
- 6. Now calculate the new t_2 .





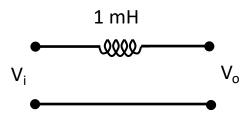
Exercise 4: Diode detectors



- For AM, $V(t) = V_c \cos(\omega_c t) + a(t) \cos(\omega_c t)$, Define the modulation depth $m = \frac{a_p}{V_c}$
- In circuit on the right, $R=3k\Omega$, C=10~nF
- Set function generator for $f_c=1$ MHz, $V_{c,pp}=5$ V, $f_m=1$ kHz, m=.7
 - 1. Calculate τ for the RC circuit. $\tau \ll a(t)$
 - 2. Compare the max voltage of the AM signal to the max of V_0 . $\tau \gg \frac{c}{f_c}$
 - 3. What happens when we make m=1.0

Exercise 5: Inductors

- Set function generator for 5V V_{pp} , 1kHz. Connect a 50Ω load
 - 1. Observe square wave with rounded corners, measure the time, t_2 to decay to 0
 - 2. Calculate pp inductor current and the expected delay, t_2

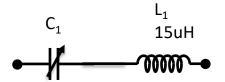


Exercise 6: Diodes and snubbers

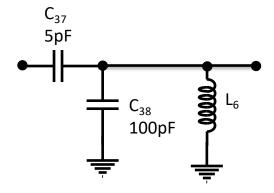
Χ

Exercise 7: Parallel to Series conversion

Exercise 8: Series resonance



Exercise 9: Parallel resonance



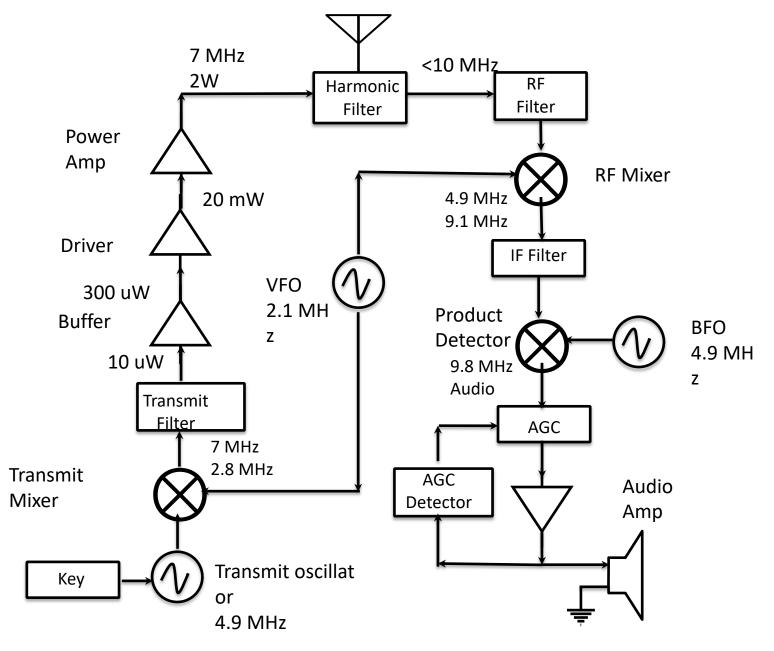
Direct conversion and superhet receivers

- Image frequency
 - $\omega_{rf} = \omega_{LO} \omega_a$
 - $\omega_i = \omega_{LO} + \omega_a$
- Superheterodyne designs
 - $\omega_{rf} = \omega_{IF} + \omega_{VFO}$
 - $\omega_{vi} = \omega_{IF} \omega_{VFO}$
 - $\omega_{IF} = \omega_{BFO} \omega_a$
 - $\omega_{bi} = \omega_{BFO} + \omega_a$
 - $\omega_{usb} = \omega_{VFO} + \omega_{BFO} + \omega_a$
 - $\omega_{lsb} = \omega_{VFO} + \omega_{BFO} \omega_a$

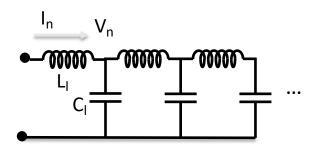


Direct conversion

Norcal 40A



Transmission Lines



Power

$$\tau = \frac{V}{V_{+}} = 1 + \rho = \frac{2Z}{Z + Z_{0}}, V = 2V_{+}$$

Lookback resistance is $R_s = Z_0$

$$P_{+} = \frac{{V_{+}}^2}{2Z_0} = \frac{{V_0}^2}{8Z_0}$$
, This is the total available power

•
$$V_{n+1} - V_n = -L_l \frac{\partial I_{n+1}}{\partial t}$$
, $L = \frac{L_l}{l}$

•
$$I_{n+1} - I_n = -C_l \frac{\partial V_n}{\partial t}$$
, $C = \frac{C_l}{l}$

•
$$\frac{\partial^2 V}{\partial z^2} = LC \frac{\partial^2 V}{\partial t^2}$$
 and $\frac{\partial^2 I}{\partial z^2} = LC \frac{\partial^2 I}{\partial t^2}$

- Solution is V(z-vt), $v=\frac{1}{\sqrt{LC}}$, for forward wave
- V' = vLI', $\frac{V}{I} = \sqrt{\frac{L}{C'}}$, $Z_0 = \sqrt{\frac{L}{C}}$
- Another solution is V(z+vt), $v=\frac{1}{\sqrt{LC}}$, for r everse wave

•
$$Z_0 = \frac{V_+}{I_+}, -Z_0 = \frac{V_-}{I_-}, V = V_+ + V_-$$

•
$$P_{+}(t) = \frac{V_{+}^{2}}{Z_{0}}, P_{-}(t) = -\frac{V_{-}^{2}}{Z_{0}}$$

•
$$\rho = \frac{V_{-}}{V_{+}}, \ Z = \frac{V}{I} = \frac{V_{+} + V_{-}}{I_{+} + I_{-}} = \frac{V_{+}}{I_{+}} \frac{1 + \frac{V_{-}}{V_{+}}}{1 + \frac{I_{-}}{I_{+}}} = Z_{0} \frac{1 + \rho}{1 - \rho}$$

$$\bullet \quad \rho = \frac{Z - Z_0}{Z + Z_0}$$

•
$$\rho_i = \frac{i_-}{i_+} = -\rho$$

Transmission Lines - continued

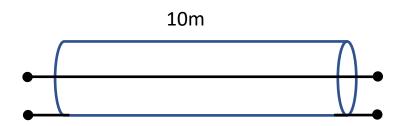
v

Exercise 10: Coax



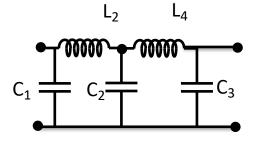
Exercise 11: Waves

Exercise 12: Resonance

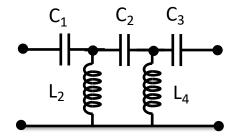


Filters

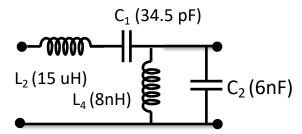
Low pass

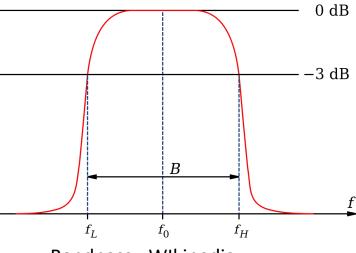


High pass

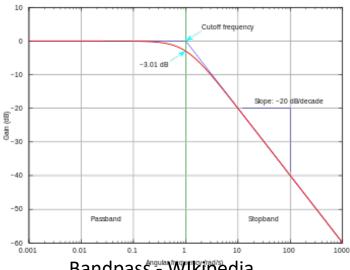


7 MHz bandpass



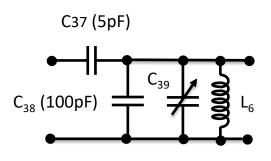


Bandpass - WIkipedia



Bandpass - Wikipedia

Norcal transmit bandpass filter



•
$$C_{39} = 50pF$$
,

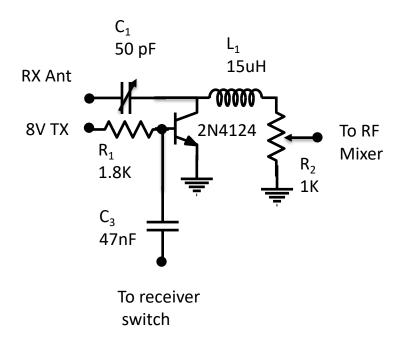
- L_6 is 36 turns #28 on T37-2 which has $A_l = 4 \frac{nH}{turn^2}$
- $L_6 = A_l \cdot 36^2 = 3.1 \mu H$

•
$$Z_2 = -\frac{j}{(C_{38} + C_{39})\omega_o}$$
, $Z_3 = jL_6\omega_o$, $Z_1 = \frac{j}{C_{37}\omega_o}$

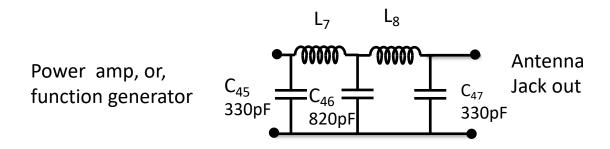
$$Z_{2,3-eq} = \frac{jL_6\omega_0}{L_6(C_{38}+C_{39})\omega_0^2-1}$$

- Resonance is when $Z_{2,3-eq} \rightarrow \infty$, $\omega_o^2 = \frac{1}{(C_{38}+C_{30})L_6} \approx \frac{10^{18}}{465}$, when almost all the voltage drop is across $Z_{2,3-eq}$ $\omega_o = \frac{10^9}{\sqrt{465}} \approx 50.8 \times 10^6$, $f_0 = \frac{\omega_o}{2\pi} \approx 7.1 \ MHz$
- Q of filter is: $Q_s = \frac{X_s}{R_s}$. R_s comes from the other components and must be measured
- Note that $Z_{2,3-eq}$ is small for the other modulation product

Norcal RF Filter

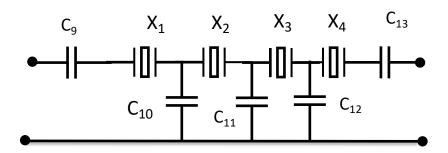


Exercise 13: Norcal Harmonic Filter

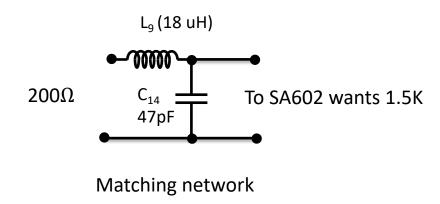


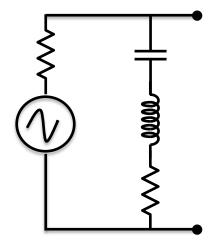
- L₇, L₈ use T37-2 core, 18 turns, 1.3uH
- Compare loss at 7MHz and 14MHz

Exercise 14: Norcal IF Cohn Filter



- X₁ through X₄ are 4.91 MHz
- C₁₀, C₁₁, C₁₂ are 270 pF
- Set function generator to $50mV_{pp}$ from function generator
- Calculate R and X for filter





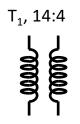
Equivalent circuit for crystal and generator

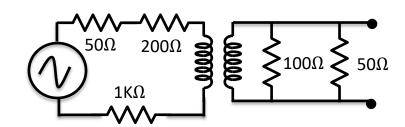
Transformers

• x

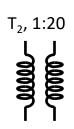
Norcal matching transformers

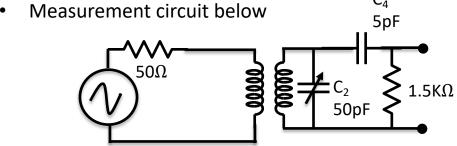
- T₁ is driver matcher uses FT 37-43
- Measurement circuit below



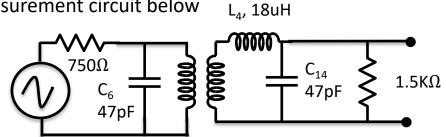


T₂ is RF matcher uses FT 37-61



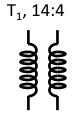


- T₃, 23:6
- -0000
- T₃ is IF matcher uses FT 37-61
- Measurement circuit below

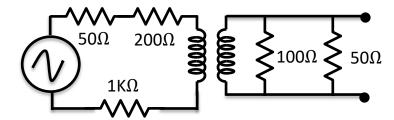


Exercise 15: Norcal Driver Transformers

• x

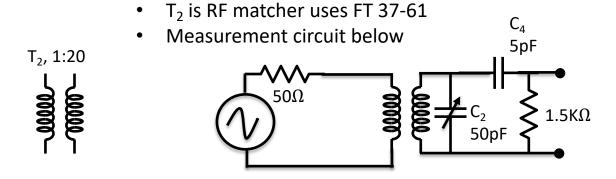


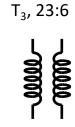
- T_1 is driver matcher uses FT 37-43
- Measurement circuit below



Exercise 16: Norcal Tuned Transformers

• x





- T₃ is IF matcher uses FT 37-61
- Measurement circuit below

ement circuit below C_{4} , 18uH C_{14} C_{6} 47pF C_{14} 47pF C_{15} C_{14} C_{14} C_{15} C_{15}

Acoustics

•
$$\frac{\partial^2 P}{\partial t^2} = \frac{\gamma P}{\rho} \frac{\partial^2 P}{\partial x^2}$$
, $v = \sqrt{\frac{\gamma P}{\rho}} = 332 \frac{m}{s}$
• $SWR = \frac{\lambda^2}{2\pi A}$, A is the area of the tube

| Sound | L _p | Power density |
|--------------------|----------------|----------------------|
| rustling leaves | 10dB | 1pW/m² |
| broadcast studio | 20dB | 1pW/m² |
| classroom | 50dB | 10nW/m ² |
| heavy truck | 90dB | 1nW/m² |
| Shout at 1m | 100dB | 10mW/m ² |
| jackhammer | 110db | 100mW/m ² |
| jet takeoff at 50m | 120dB | 1W/m ² |

Exercise 17: Tuned Speaker

• x

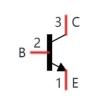
Exercise 18: Acoustic Standing Wave

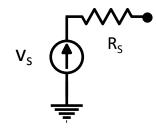
• x

Bipolar Transistors

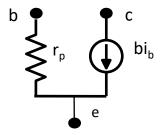
- NPN, PNP
- Model
- $i_C = \alpha i_E$
- $i_C = \beta i_B$
- $\beta = \alpha/(1-\alpha)$
- $\beta \sim 100$







Bipolar source model

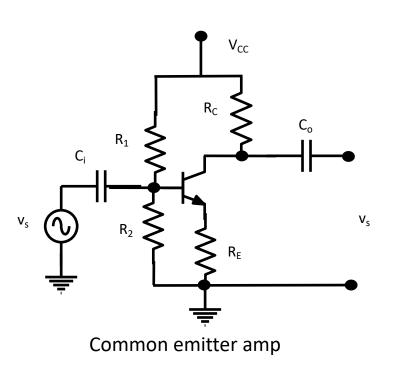


Bipolar equivalent circuit

Bipolar Switches

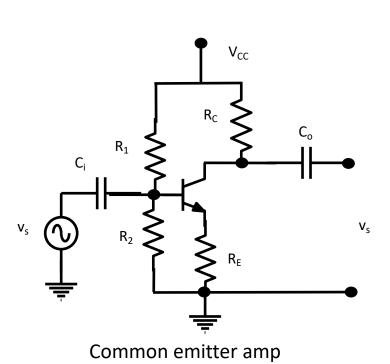
- NPN, PNP
- Model
- $i_C = \alpha i_E$
- $i_C = \beta i_B$
- $\beta = \alpha/(1-\alpha)$
- $\beta \sim 100$

BJT common emitter amplifier



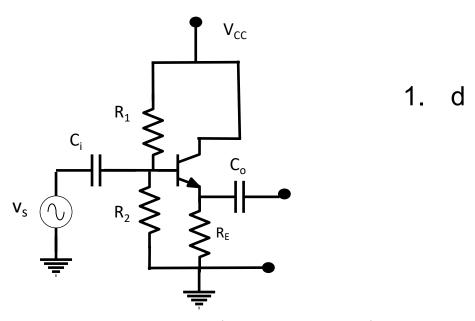
- Here's how to design a common emitter amplifier. We use a 2n3904 transistor with β =150. This circuit will work! Build it.
 - 1. Pick the supply voltage V_{cc} =12V.
 - 2. Choose a gain (amplification factor), A = 5.
 - 3. Choose the "Q point" of the conducting transistor (4mA).
 - 4. $V_{cc} = (i_c \cdot R_C) + V_{ce} + i_e R_E \sim i_e \cdot (R_C + R_E) + V_{ce}$ with $i_c = 4mA$. We get $(R_C + R_E) = (V_{cc} V_{ce})/(4mA) = 1.75 \text{ k}\Omega$.
 - 5. Since A = 5 and A=R_C/R_E, R_C= 5 R_E so R_E \sim 270 Ω (this is a standard resistor value) and R_C= 1.5k Ω .

BJT common emitter amplifier continued



- 6. $i_b = 4mA/\beta = 27 \mu A$.
- 7. Since V_{be} must be greater than .7V throughout the input signal range, we want the voltage across R_2 to satisfy V_{be} + $i_c R_F = 1.8V$.
- 8. We insert a voltage divider consisting of R_1 and R_{2} , so that R_1 = (12-1.8)/270 μ A \sim 39 k Ω .
- 9. C_o and C_i are picked to offer small resistance to the frequency range we're interested in and $C_o = C_i = 5 \mu F$.
- I haven't explained why we want R_E but it provides thermal stability for the transistor over the range we care about. The fact that $A=R_C/R_E$ can be calculated using Kirchhoff's laws.

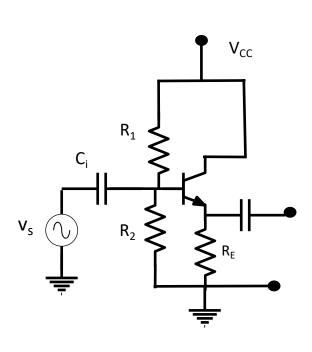
BJT common collector amplifier



Common collector amp (Emitter Follower)

Common collector amp

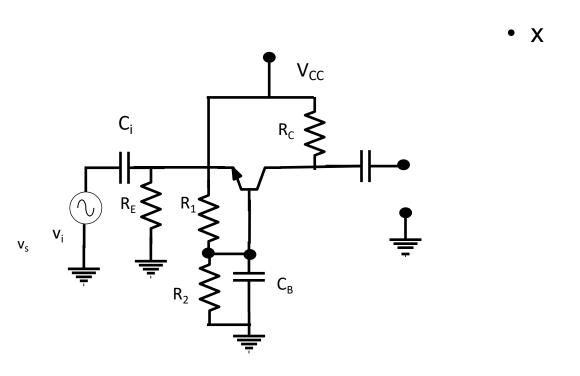
BJT common collector amplifier continued



6. x

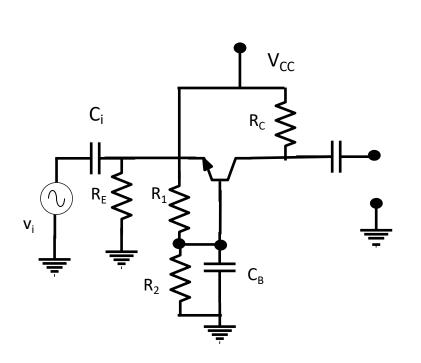
Common collector amp (Emitter Follower)

BJT common base amplifier



Common base amp

BJT common base amplifier continued

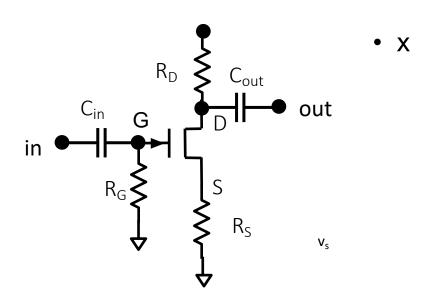


6. x

Common base amp

JFETs

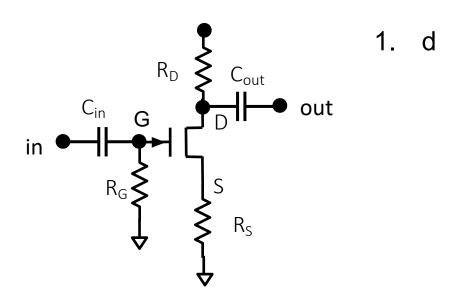
JFET Common Emitter Amplifier



JFET common emitter amplifier continued

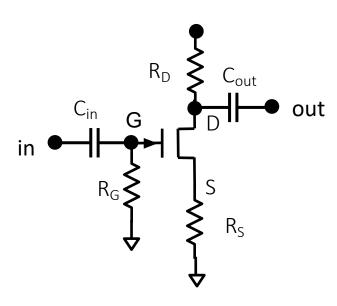
6. x

JFET common source amplifier

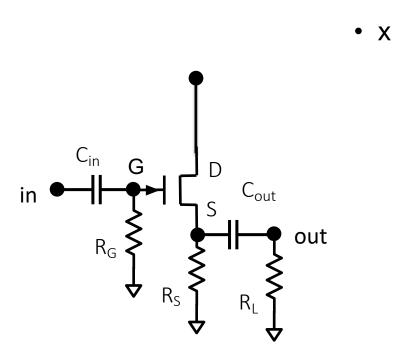


JFET Common Source Amplifier continued

6. x

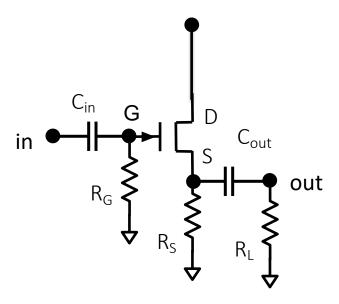


JFET common drain amplifier

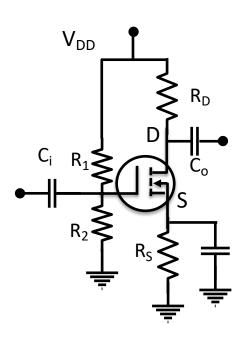


JFET common drain amplifier continued

6. x



CMOS common emitter amplifier



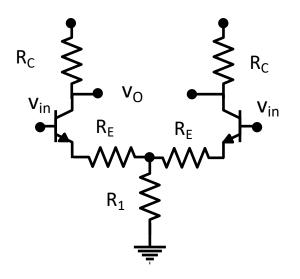
- Pick power
- $\bullet \quad V_{DD} = i_D R_D + V_{DS} + i_D R_S$
- $V_{GS} = V_G i_S R_S$ $V_G = V_{DD} \frac{R_1}{R_1 + R_2}$ $i_D = k(V_G V_{TH})^2$

- Bias around $\frac{V_{DD}}{3}$ Pick gain, $A = \frac{R_D}{R_S + \frac{1}{a_m}}$

Differential Amplifier

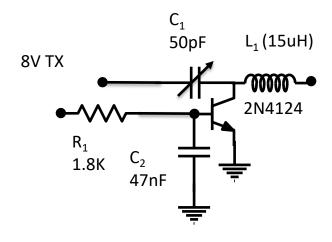
- Two port model
- $\bullet \quad \begin{pmatrix} i_1 \\ i_2 \end{pmatrix} = \begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}$

Differential amplifier



- Pick power ± 12
- Choose collecter current (2mA) by picking R_1
- Pick gain, $A = \frac{R_C}{2R_E}$

Exercise 19: Norcal receiver switch



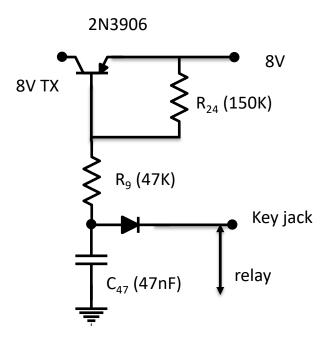
• Receiver mixer or an oscilloscope with 50Ω

When transistor conducts the receiver filter shorts

Harmonic filter

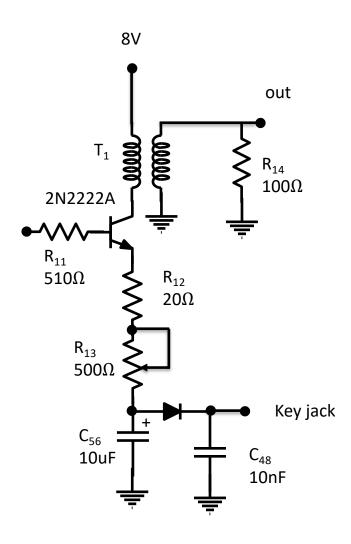
If using function generator use a 1.8K resistor

Exercise 20: NorCal transmitter switch



When key is down, transistor conducts

Exercise 21: Norcal Driver

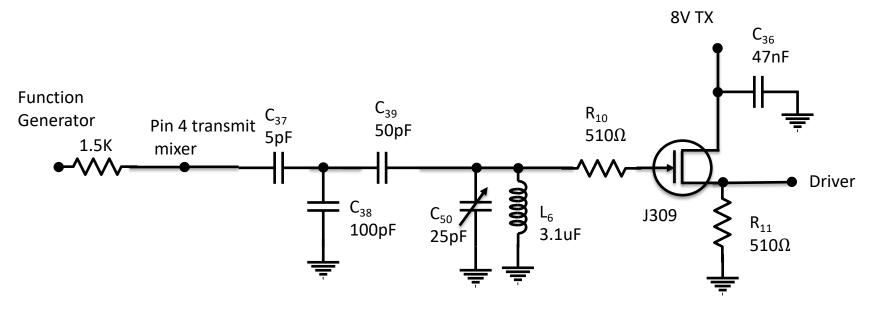


• Use 50Ω scope probe

Exercise 22: Emitter degeneration

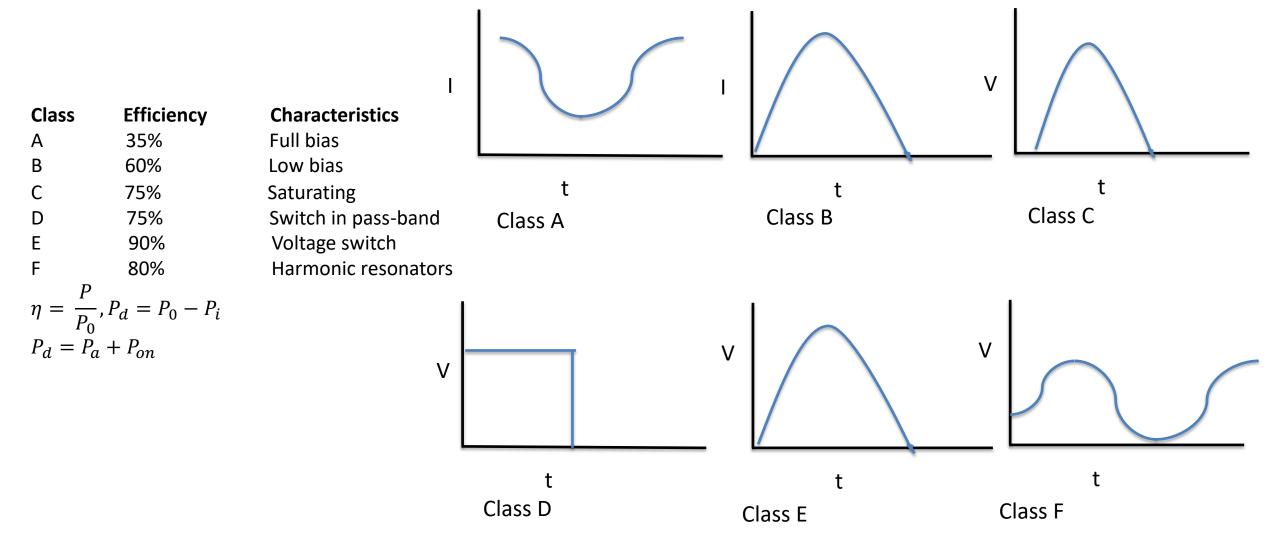
• Use 50Ω scope probe

Exercise 23: Norcal Buffer amplifier



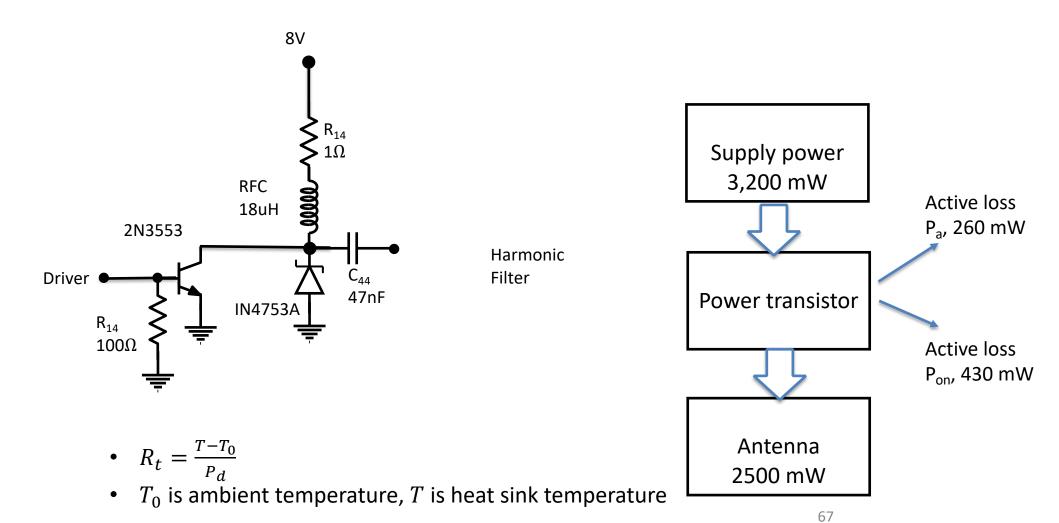
$$G_V = \frac{V}{V_i}$$

Amplifier classes



Exercise 24: Norcal Power Amp

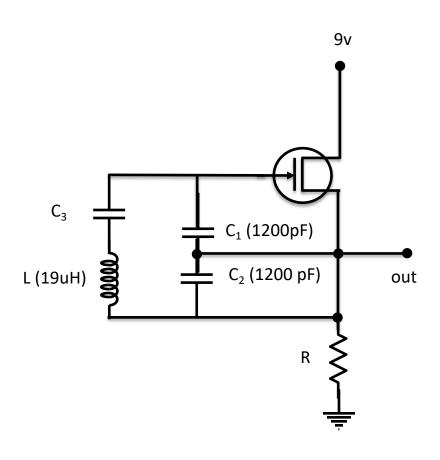
Norcal-40 Power amp is class C



Exercise 25: Power modelling

• Use 50Ω scope probe

Clapp oscillator



•
$$i_d = g_m v_{gs}$$

• Resonance:
$$-\frac{1}{j\omega_0 c_2} = j\omega_0 L + \frac{1}{j\omega_0 c_3} + \frac{1}{j\omega_0 c_1}$$

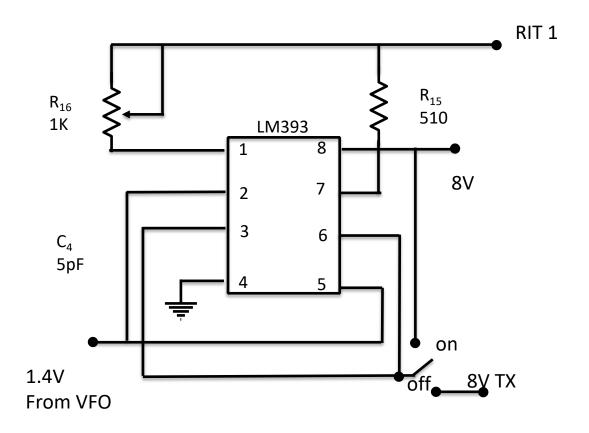
•
$$\omega_0 = \frac{1}{\sqrt{LC}}, C = C_1 ||C_2||C_3$$

• At resonance,
$$v_{gs} = Ri_d \frac{c_1}{c_2}$$
, $L = \frac{c_1}{Rc_2}$

• Oscillation continues if
$$g_m > \frac{C_1}{RC_2}$$

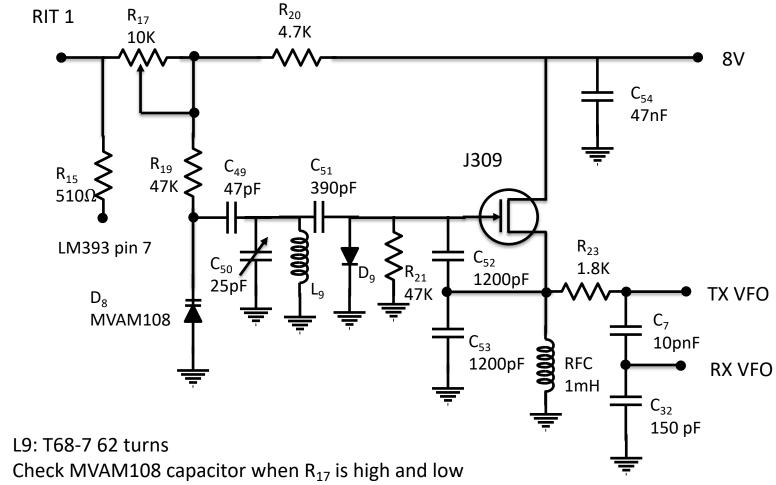
•
$$v_{gs} = 2v_s$$

Norcal Receiver Incremental Tuning (RIT)



- LM393 is a comparator
- For function generator connect through 1.5K

Exercise 26: Norcal VFO



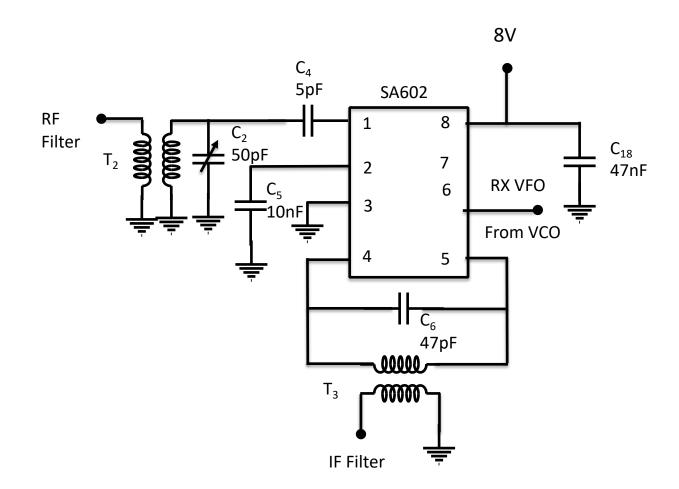
- Start resistor (R₂₁) pulls gat to ground at start
- When gain limiting diode (D9) conducts, it pulls gate negative
- Oscillator keeps growing as long as g_m>1/R

Exercise 27: Gain limiting

• *x*

Mixers

Exercise 28: Norcal RF Mixer

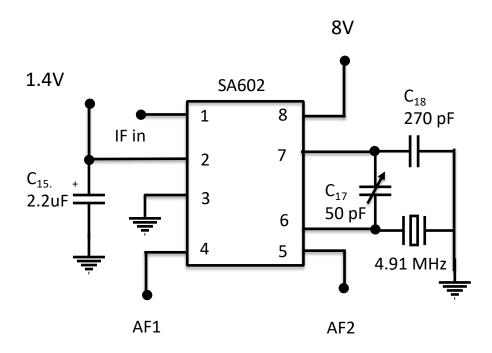


50mVpp if

generator

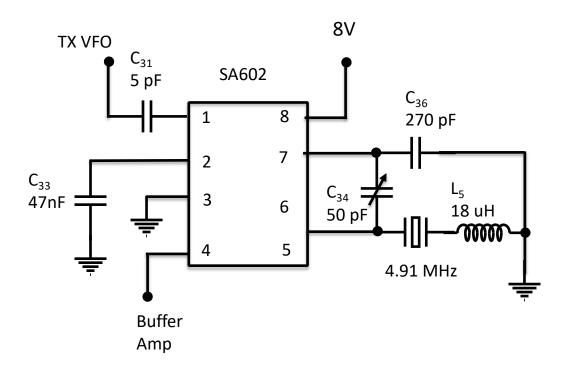
using function

Exercise 29: Norcal Product Detector

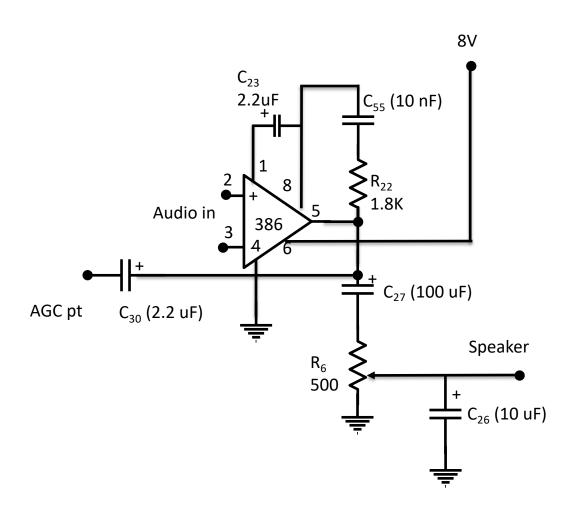


• 620 Hz output through AF1 and AF2

Exercise 30: Norcal transmit mixer and oscillator

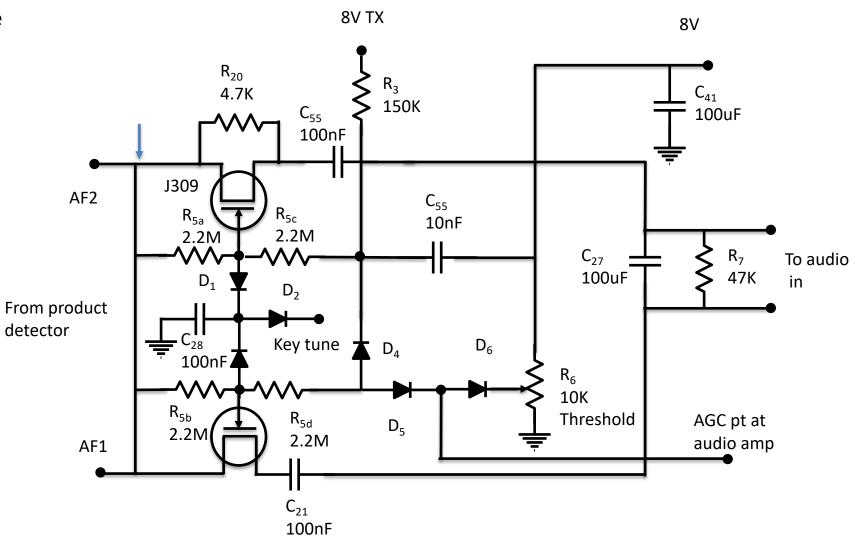


Exercise 31: Norcal Audio Amp



Exercise 32: Norcal AGC

Connect to function generator through 300K, here

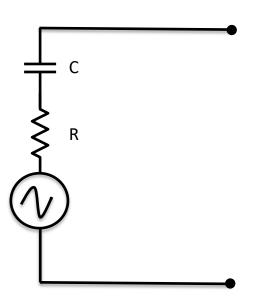


Exercise 33: Alignment

Antennas and propagation

- From Maxwell, for a plane wave (E in x direction, H in y direction), wave is of form $\exp(j\omega t j\beta z)$
- $\nabla \times E = -j\mu_0 \omega H$
- $\nabla \times B = j\epsilon_0 \omega E$
- $\beta \hat{z} \times E = \mu_0 \omega H$, $\beta E_x \hat{y} = \mu_0 \omega H$
- Substituting and taking the restricted cross products, we get: $\beta E_x = \omega \mu_0 \frac{\omega \epsilon_0}{\beta}$, so $\beta = \omega \sqrt{\mu_0 \epsilon_0}$
- Power density: $S = Re\left(\frac{E_x \overline{H_y}}{2}\right) = \frac{(|E_x|)^2}{2\eta_0}$
- $\bullet \quad \eta_0 = \frac{E_x}{H_y} = \sqrt{\frac{\mu_0}{\epsilon_0}} = 377\Omega$
- Impedance: $P_t = \frac{R|I|^2}{2}$, R is real part of Z, $R = R_r + R_l$, $\eta = \frac{R_r}{R}$
- Power density for isotropic antenna: $S_i = \frac{P_t}{4\pi r^2}$
- Define $G(\theta, \phi) = \frac{S(\theta, \phi)}{S_r}$. $S(\theta, \phi)$ is just the Poynting vector
- For isotropic reference, $G = \frac{4\pi r^2 S}{P_t}$

Receiving antenna Thevenin



Antennas and propagation

- Receiving antenna:
- $V_0 = hE$, h is effective antenna length ($h = \frac{l}{2}$ for short antenna)
- For dipole: $V_0 = \frac{l}{2} E \sin(\theta)$
- $A(\theta, \phi) = \frac{P_r}{S(\theta, \phi)}$. This is the definition of the effective area, A.
- By reciprocity, $A(\theta, \phi) = \frac{\lambda^2}{4\pi} G(\theta, \phi)$
- $P_r = \frac{|V_0|^2}{8R_a} = \frac{|hE|^2}{8R_a}$, so
- $P_r = \frac{h^2 S \eta_0}{4R}$ $A = \frac{h^2 \eta_0}{4R}$

Antennas and propagation

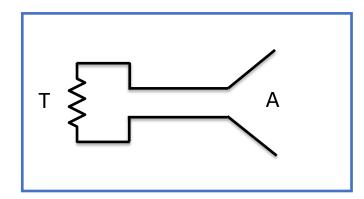
- Antenna theorem: $\oint A \ d\Omega = \lambda^2$
- For cavity on right, T is constant at thermodynamic equilibrium and the same power is transmitted and emitted, the Johnson noise is kT. The energy received is

$$E=rac{4\pi kT}{c\lambda^2}$$
. Set $B=rac{kT}{\lambda^2}$. $kT=\oint BA\ d\Omega=\oint Arac{kT}{\lambda^2}\ d\Omega$, which gives the antenna theorem

- For transmitting/receiving antenna pairs: $G_1A_2=\frac{|V|^2\pi r^2}{|I|^2R_1R_2}=G_2A_1$. So $\frac{G_1}{A_1}=\frac{G_2}{A_2}=\frac{4\pi}{\lambda^2}$
- Friis formulas

•
$$S = \frac{P_t G}{4\pi r^2}$$
, $P_r = SA = \frac{P_t GA}{4\pi r^2}$

Insulated cavity



Reciprocity and dipole

Dipole Thevenin equivalent circuit

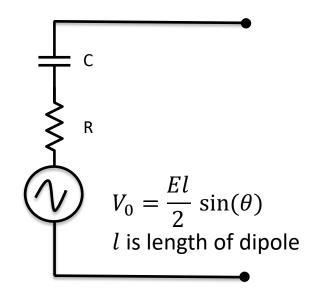
• For dipole (Length:
$$l = \frac{\lambda}{2}$$
)

•
$$\lambda^2 = \int A \ d\Omega = \int \frac{h^2 \eta_0}{4R_r} \ d\Omega$$
, so

•
$$R_r = \frac{l^2 \eta_0}{16\lambda^2} \int \sin^2(\theta) d\Omega = \eta_0 \frac{\pi}{6} \left(\frac{l}{\lambda}\right)^2$$

•
$$R_r=\frac{l^2\eta_0}{16\lambda^2}\int sin^2(\theta)d\Omega=\eta_0\frac{\pi}{6}(\frac{l}{\lambda})^2$$

• $A=\frac{3\lambda^2}{8\pi}sin^2(\theta)$ and $G=1.5sin^2(\theta)$. Note we used $h=\frac{l}{2}\sin(\theta)$



• For Norcal, G = 1, $A = 150m^2$, for r = 2000 m, $P_r = 6pW$

Noise

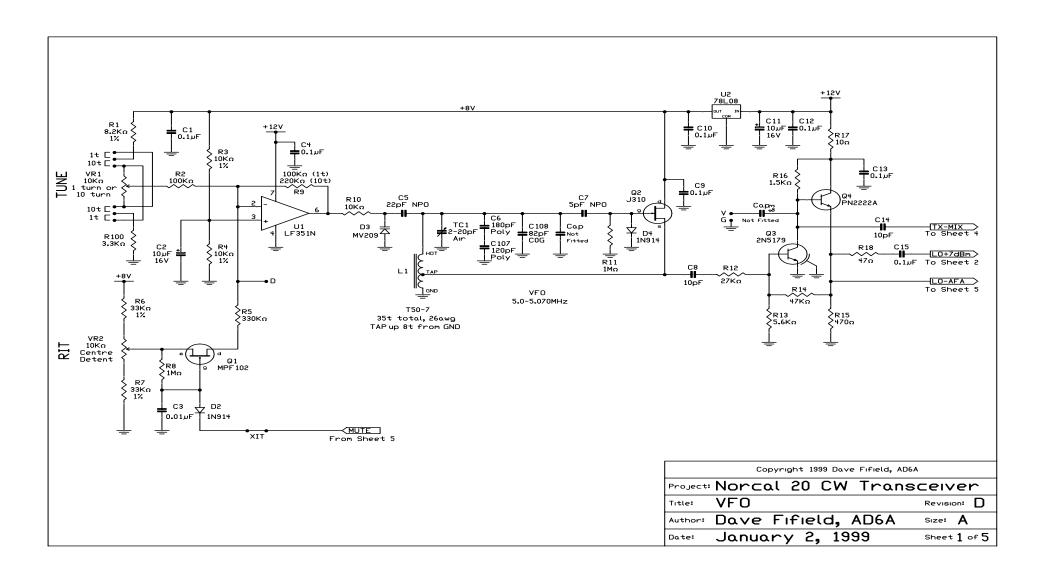
•
$$V_{n(rms)} = \sqrt{\frac{1}{\tau} \int_0^{\tau} V(t)^2} dt$$

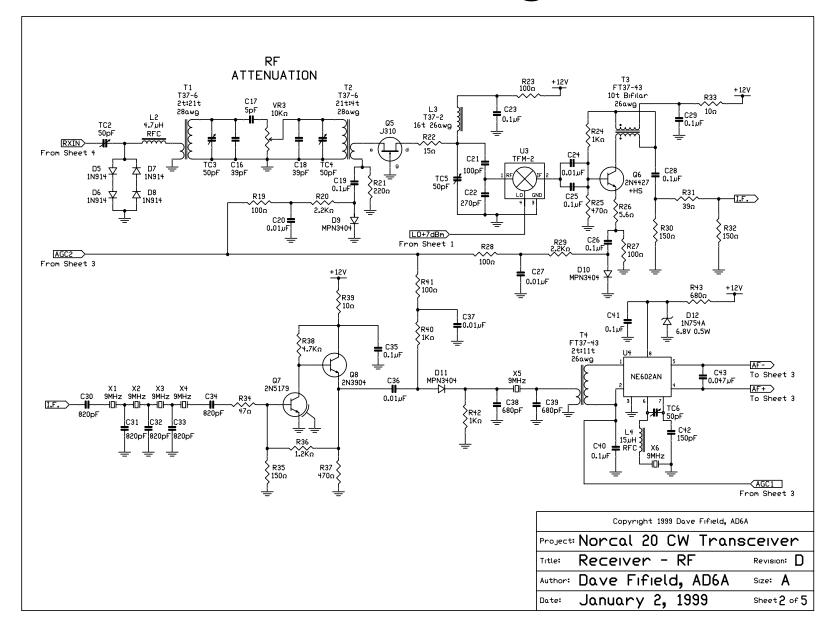
- $V_{n(rms)} = \sqrt{\frac{1}{\tau} \int_0^{\tau} V(t)^2} dt$ $P_n = \frac{V_{n(rms)}^2}{R}$, R is load resistance
- $SNR = \frac{P}{P_n}$
- $MDS = \frac{P_n}{G}$
- Nyquist
- $V_C = \frac{1}{j\omega C} \frac{V_n}{R + j\omega L + \frac{1}{j\omega C}}$
- $\overline{|V_C|^2} = \frac{\overline{|V_n|^2}}{|1-\omega^2 LC + j\omega RC|^2}$
- Expected energy at resonance is $kT = \frac{c}{2} \int_0^\infty |V_c|^2 df$
- $\bullet \int_0^\infty \frac{1}{|1 \omega^2 LC + i\omega RC|^2} df = \frac{1}{4RC}$
- So, $|V_c|^2 = 8kTR$

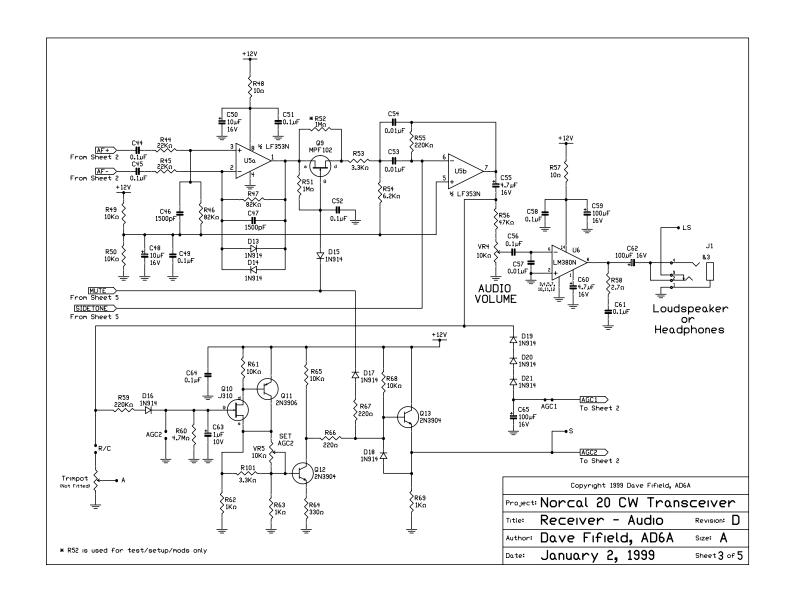
Exercise 35: Intermodulation

Exercise 37: Antennas

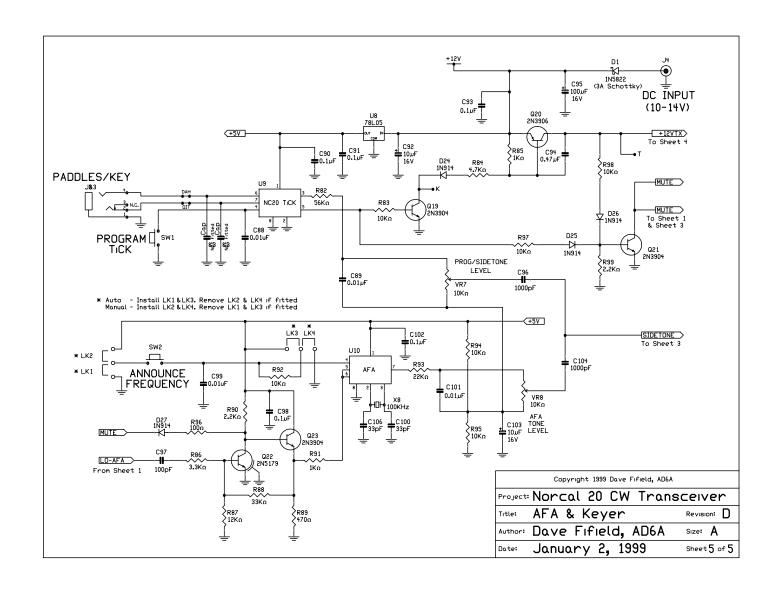
Exercise 38: Propagation







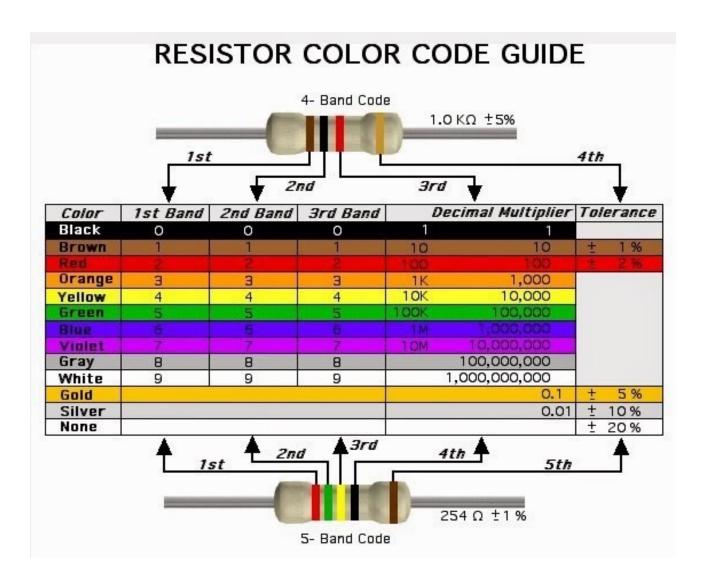




Morse

| Symbol | Code | Symbol | Code | Symbol | Code |
|--------|------|--------|------|--------|------|
| a | •_ | m | | У | |
| b | | n | _• | Z | |
| С | | 0 | | 0 | |
| d | | р | ·· | 1 | • |
| e | • | q | ·_ | 2 | |
| f | | r | | 3 | |
| g | | S | ••• | 4 | |
| h | •••• | t | _ | 5 | •••• |
| i | •• | u | | 6 | |
| j | • | V | | 7 | |
| k | | W | • | 8 | |
| Ī | | Х | | 9 | |

Color codes



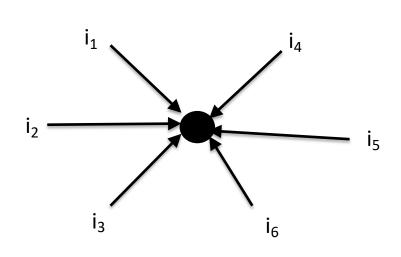
Resistors: ohms

Capacitors: picoFards

Inductors: milliHenries

Kirchhoff

• There are two Kirkoff's laws, one describes voltages the other describes currents.



$$i_1 + i_2 + i_3 + i_4 + i_5 + i_6 = 0$$

