Final Notebook

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0.1 Phase 2 Final Project Submission

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Business Problem

The mortgage department at Bentley & Co. Bank of Seattle is looking for an additional method of appraising the value of homes. They currently hire an appraisal management company, and will continue to do so. However, as independent appraisals can be costly and take time, Bentley & Co. Bank is looking for a tool that can estimate the value of a house cheaply and quickly.

This will be useful for obtaining a ballpark estimate of the value of a home before an appraisal can be performed. In addition, it will be useful for estimating the price impact of any renovations performed on a house Bentley & Co. Bank has an interest in without any additional appraisals.

This tool must meet two criteria to be of use to Bentley & Co. Bank:

The tool must be capable of accurately predicting the price of a house provided information about the house.

The tool must provide insight into what factors impact the price of a house the most.

Goals

Bentley Bank & Co. can use the models created in this notebook to: * Generate a range of prices that the price of a given house can be expected to fall within. * Predict the price impact of any physical changes to a home.

Imports & Important Functions

import varnings import pandas as pd import numpy as np import seaborn as sns import math import matplotlib.pyplot as plt import statsmodels.api as sm import scipy.stats as stats

```
from datetime import datetime as dt
from sklearn.preprocessing import StandardScaler
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_squared_error, mean_absolute_error
from sklearn.linear_model import LinearRegression

# Set important global options
%matplotlib inline
plt.style.use('seaborn')
warnings.filterwarnings("ignore")
pd.options.display.float_format = '{:.3f}'.format
```

I made the following function to answer my business problem. It uses the best model to get a range of prices for any given house.

```
[36]: # This can not be run until the model sm best is created in memory
     def predict_interval(house,confidence=0.001):
         # Calculates predicted value and confidence interval of specified alpha
         prediction = np.exp(sm_best.get_prediction(house).predicted_mean[0])
         conf_interval = np.exp(sm_best.get_prediction(house).
      # Formats everything nicely
         pred_statement = f'This house has a predicted value of ${math.
      →trunc(prediction)}.'
         interval_statement = (f'A safe value for this house would fall between '
             f'${math.trunc(conf_interval[0])} and ${math.trunc(conf_interval[1])}.')
         print(pred_statement)
         print(interval statement)
         return(prediction)
     # This can not be run until the model sm best is created in memory
     #predict_interval(X_test_best.iloc[42]);
```

I prefer SKLearn to statsmodels so I created a helper function to extract all of the relevant information from an SKLearn regression.

```
[37]: # The following function returns the results of a sklearn model

def model_summary(model,train_X,test_X,train_y,test_y):
    #Evaluates the model on training data
    train_r2 = model.score(train_X,train_y)
    train_mae = mean_absolute_error(train_y,model.predict(train_X))
    train_mse = mean_squared_error(train_y,model.predict(train_X))
    train_rmse = mean_squared_error(train_y,model.

→predict(train_X),squared=False)

#Evaluates the model on test data
```

```
test_r2 = model.score(test_X,test_y)
  test mae = mean_absolute_error(test_y,model.predict(test_X))
  test_mse = mean_squared_error(test_y,model.predict(test_X))
  test_rmse = mean_squared_error(test_y,model.predict(test_X),squared=False)
  # Prepare the results to be added to a dataframe
  labels = ['Train R2','Train Mean Abs Err','Train Mean Sq Err','Train Root⊔
→Mean Sq Err',
           'Test R2','Test Mean Abs Err','Test Mean Sq Err','Test Root Mean Sq∟
←Err']
  results = [train_r2, train_mae, train_mse, train_rmse,
          test r2, test mae, test mse, test rmse]
  #Return the results as pandas dataframes
  dfr = pd.DataFrame(results,index=labels,columns=['Values'])
  coefficients = pd.DataFrame(model.coef_,index=train_X.
return dfr, coefficients
```

Data Understanding

The data provided in 'kc_house_data.csv' contains information on 21 thousand homes sold in the King County, WA area between 2014 and 2015.

The data provided in 'zips.csv' contains a list of zipcodes and the corresponding city for each zipcode in King County, WA.

I began by loading each dataset into dataframes, dropping most of the columns suggested by the project description, and merging the two datasets together by the zipcode column.

```
<class 'pandas.core.frame.DataFrame'>
Int64Index: 21597 entries, 0 to 21596
Data columns (total 13 columns):
# Column Non-Null Count Dtype
```

```
21597 non-null
                                          float64
      0
          price
      1
          bedrooms
                         21597 non-null
                                          int64
      2
          bathrooms
                         21597 non-null
                                          float64
      3
          sqft living
                         21597 non-null int64
      4
          sqft lot
                         21597 non-null int64
          floors
      5
                         21597 non-null float64
      6
          waterfront
                         19221 non-null
                                          object
      7
          view
                         21534 non-null object
                         21597 non-null
      8
          condition
                                          object
      9
                         21597 non-null
          grade
                                          object
                         21597 non-null
                                          int64
      10
          yr_built
          yr_renovated
                         17755 non-null
                                          float64
      11
          city
                         21597 non-null
      12
                                          object
     dtypes: float64(4), int64(4), object(5)
     memory usage: 2.3+ MB
[39]: # Quick statistics on the data
      homes.describe()
[39]:
                  price bedrooms
                                    bathrooms
                                                sqft_living
                                                                sqft_lot
                                                                             floors
              21597.000 21597.000
                                    21597.000
                                                  21597.000
                                                               21597.000 21597.000
      count
      mean
             540296.574
                             3.373
                                         2.116
                                                   2080.322
                                                               15099.409
                                                                              1.494
      std
                             0.926
             367368.140
                                         0.769
                                                    918.106
                                                               41412.637
                                                                              0.540
              78000.000
                             1.000
                                         0.500
                                                    370.000
                                                                 520.000
                                                                              1.000
      min
      25%
             322000.000
                             3.000
                                         1.750
                                                   1430.000
                                                                5040.000
                                                                              1.000
      50%
             450000.000
                             3.000
                                         2.250
                                                   1910.000
                                                                7618.000
                                                                              1.500
      75%
             645000.000
                             4.000
                                         2.500
                                                                              2.000
                                                   2550.000
                                                               10685.000
      max
            7700000.000
                            33.000
                                         8.000
                                                  13540.000 1651359.000
                                                                              3.500
             yr_built
                        yr_renovated
      count 21597.000
                           17755.000
      mean
             1971.000
                              83.637
      std
               29.375
                             399.946
      min
             1900.000
                               0.000
      25%
             1951.000
                               0.000
      50%
             1975.000
                               0.000
      75%
             1997.000
                               0.000
      max
             2015.000
                            2015.000
[40]: # Quick overview of the data
      homes.head()
[40]:
                     bedrooms
                               bathrooms
                                           sqft_living
                                                         sqft_lot
                                                                   floors waterfront
             price
      0 221900.000
                            3
                                    1.000
                                                             5650
                                                                    1.000
                                                  1180
                                                                                  NaN
                            3
      1 538000.000
                                   2.250
                                                  2570
                                                             7242
                                                                    2.000
                                                                                   NO
                            2
      2 180000.000
                                   1.000
                                                   770
                                                            10000
                                                                    1.000
                                                                                   NO
      3 604000.000
                            4
                                   3.000
                                                  1960
                                                             5000
                                                                    1.000
                                                                                   NO
```

4	510000	.000	3	2.000	16	8080	1.000	NO
	view	condition		grade	<pre>yr_built</pre>	$yr_renovated$	city	
0	NONE	Average	7	Average	1955	0.000	Seattle	
1	NONE	Average	7	Average	1951	1991.000	Seattle	
2	NONE	Average	6 Low	Average	1933	nan	Kenmore	
3	NONE	Very Good	7	Average	1965	0.000	Seattle	
4	NONE	Average		8 Good	1987	0.000	Sammamish	

Data Cleanup & Pre-processing

Not too much looks weird here, but the homes.describe() shows that at least one home has 33 bedrooms. Let's investigate this further.

[41]:	homes	[homes.bedroo	oms > 8]						
		_							
[41]:		price	bedrooms	s bathrooms	1	sqft_living	sqft_lot	floors \	
	4092	599999.000	Ç	4.500		3830	6988	2.500	
	4231	700000.000	Ç	3.000		3680	4400	2.000	
	6073	1280000.000	(4.500		3650	5000	2.000	
	8537	450000.000	(7.500		4050	6504	2.000	
	8748	520000.000	1:	3.000		3000	4960	2.000	
	13301	1150000.000	10	5.250		4590	10920	1.000	
	15147	650000.000	10	2.000		3610	11914	2.000	
	15856	640000.000	33	3 1.750		1620	6000	1.000	
	16830	1400000.000	(4.000		4620	5508	2.500	
	18428	934000.000	(3.000		2820	4480	2.000	
	19239	660000.000	10	3.000		2920	3745	2.000	
		_				_		_	
		waterfront	view	condition		grade	yr_built	yr_renovated	\
	4092	NO	NONE	Average		7 Average	1938	0.000	
	4231	NO	NONE	Average		7 Average	1908	0.000	
	6073	NO	NONE	Average		8 Good	1915	2010.000	
	8537	NO	NONE	Average		7 Average	1996	0.000	
	8748	NO	NONE	Average		7 Average	1918	1999.000	
	13301	NO	AVERAGE	Average		9 Better	2008	0.000	
	15147	NO	NONE	Good		7 Average	1958	0.000	
	15856	NO	NONE	Very Good		7 Average	1947	0.000	
	16830	NO	NONE	0	11	Excellent	1915	0.000	
	18428	NO	NONE	Average		7 Average	1918	0.000	
	19239	NO	NONE	Good		7 Average	1913	0.000	
		city							
	4092	Seattle							
	4231	Seattle							
	6073	Seattle							
	8537	Seattle							
	8748	Seattle							

```
13301 Bellevue
15147 Bellevue
15856 Seattle
16830 Seattle
18428 Seattle
19239 Seattle
```

The 33 bedroom house only has 1600 sq. ft. of living space. I will assume this is a data entry issue and impute the median value of 3 bedrooms on this home.

```
[42]: homes.loc[homes.bedrooms > 20,'bedrooms'] = 3
```

Waterfronts seems to have some missing values. I will impute the mode "NO" for the missing values, and then map the values No to 0 and Yes to 1 so this feature can be used in my model.

```
[43]: waterfront_rule = {'NO':0,'YES':1}
waterfronts = homes.waterfront.fillna('NO').map(waterfront_rule)
homes.waterfront = waterfronts
```

Views also seems to have some missing values. I will impute the mode "NONE" for the missing values. In order to get this column to work with my model, I will take the values from worst to best and map them to the numbers 0 through 4.

```
[44]: view_rule = {'NONE':0,'FAIR':1,'AVERAGE':2,'GOOD':3,'EXCELLENT':4}
views = homes.view.fillna('NONE').map(view_rule)
homes.view = views
```

Condition is very similar to view, but without any missing values to impute. In order to get this column to work with my model, I will take the values from worst to best and map them to the numbers 0 through 4.

```
[45]: condition_rule = {'Poor':0, 'Fair':1, 'Average':2, 'Good':3, 'Very Good':4} conditions = homes.condition.map(condition_rule) homes.condition = conditions
```

Grade already has a numerical rating in the column, so I will extract that number for use in my model.

```
[46]: # Numerical rating is the part of grade before the space grades = homes.grade.apply(lambda x: int(x.split()[0])) homes.grade = grades
```

I decided to engineer a feature called since_reno which is the number of years since the last renovation. If the home had an NA value for year renovated, I assumed the home had not been renovated and used the year built as the renovation date. I used a helper function since_reno to calculate this feature.

```
[47]: homes.yr_renovated.fillna(0,inplace=True)

def since_reno(home):
```

```
# Use the year built if the house has not been renovated
if home.yr_renovated < home.yr_built:
    return dt.today().year - home.yr_built
else:
    return dt.today().year - home.yr_renovated

homes['since_reno'] = homes.apply(lambda x:since_reno(x),axis=1)
homes.drop('yr_renovated',inplace=True,axis=1)</pre>
```

I decided to drop the year built in favor of the home's age. This probably won't affect the model but is easier to read.

```
[48]: homes['age'] = dt.today().year - homes['yr_built'] homes.drop('yr_built',inplace=True,axis=1)
```

City is a categorical feature, so I had to one-hot-encode it so it would work with my model. I did not merge cities back into my main dataset yet so the visualizations will be easier to see.

```
[49]: cities = pd.get_dummies(homes.city,prefix='city',sparse=False,drop_first=True)
# Grouped cities is created for plotting purposes later
grouped_cities = homes.copy().groupby('city')
homes.drop('city',inplace=True,axis=1)
cities.head()
```

```
[49]:
         city_Bellevue
                         city_Black_Diamond
                                               city_Bothell city_Carnation
                      0
                                            0
                                                          0
                                                                            0
      0
      1
                      0
                                            0
                                                          0
                                                                            0
                      0
      2
                                            0
                                                          0
                                                                            0
      3
                      0
                                            0
                                                          0
                                                                            0
                                            0
         city_Duvall city_Enumclaw city_Fall_City
                                                        city Federal Way
      0
                    0
                                    0
      1
                    0
                                    0
                                                     0
                                                                         0
                                    0
                                                                         0
      2
                    0
                                                     0
      3
                    0
                                    0
                                                     0
                                                                         0
      4
                    0
                                                     0
                                                                         0
                                           city_Medina city_Mercer_Island \
         city_Issaquah
                         city_Kenmore
      0
                      0
                                     0
                                                                            0
                                                                            0
      1
                      0
                                     0
                                                      0
      2
                      0
                                                      0
                                                                            0
      3
                      0
                                     0
                                                      0
                                                                            0
         city_North_Bend city_Redmond city_Renton city_Sammamish city_Seattle \
      0
                        0
                                       0
                                                     0
                                                                      0
```

2	0	0	0	0	0
4	0	0	0	1	0
	city_Snoqualmie	city_Vashon	city_Woodinville		
0	0	0	0		
1	0	0	0		
2	0	0	0		
3	0	0	0		
4	0	0	0		

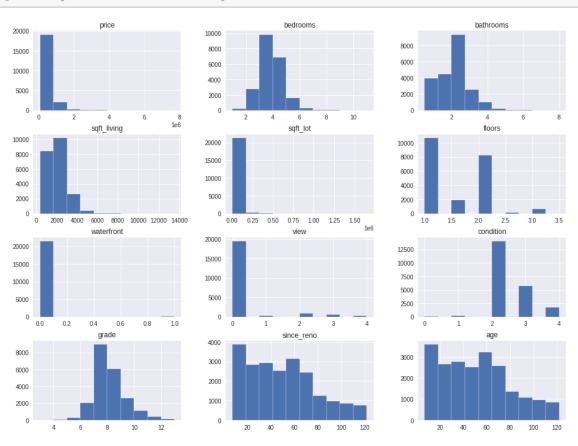
[5 rows x 23 columns]

Exploratory Data Analysis

Distrobutions

This plot shows how each numeric variable in the homes dataframe is distributed. Age and Since_reno seem to be very similar. Price and both sqft columns seem to be good candidates for log transformations.

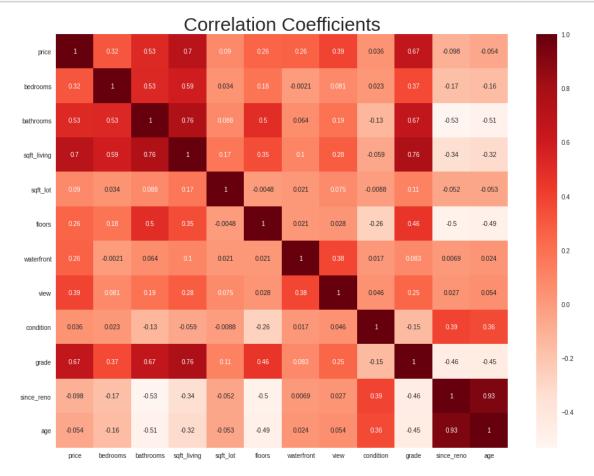
[50]: pd.plotting.hist_frame(homes,figsize=(16,12));



Correlations

Just a standard correlation coefficient matrix.

```
[51]: fig,ax = plt.subplots(figsize = (16,12))
ax.set_title('Correlation Coefficients',fontsize=30);
sns.heatmap(homes.corr(),annot=True,ax=ax,cmap='Reds');
ax.set_yticklabels(homes.columns,rotation=0);
```

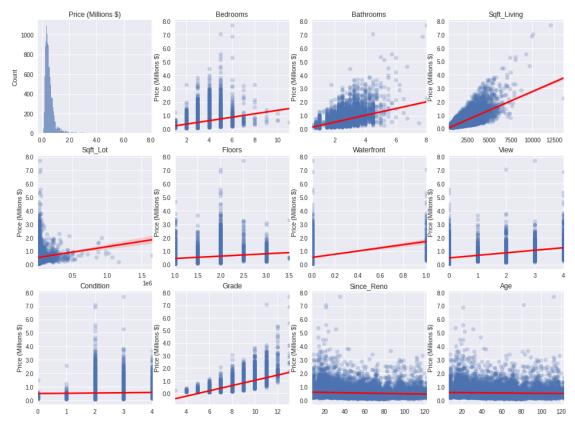


Regression Plots

This takes a year and a half to run. This helps to visualize which variables have linear relationships with price.

```
[52]: fig,ax = plt.subplots(3,4,figsize=(16,12))
for idx,row in enumerate(ax):
    for idx2,col in enumerate(row):
        y_val = homes.columns.values[(4*idx) + idx2]

# Make a histogram for the price column
    if y_val == 'price':
```



Median Price by Location

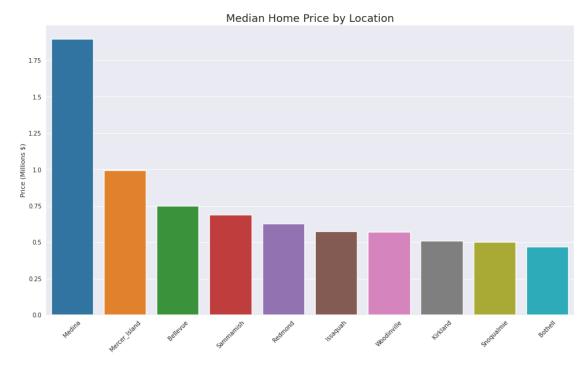
Location has a huge impact on the price of a home, but has been left out of the plots so far.

```
[53]: # Reshaping the data and taking only the first 10 cities for visibility grouped_cities = pd.DataFrame(grouped_cities['price'].agg(np.median).

--sort_values(ascending=False)[:10]).T

fig,ax = plt.subplots(figsize = (16,9))
```

```
sns.set_theme(context='talk');
sns.barplot(data = grouped_cities.palette='tab10')
ax.set_xticklabels(grouped_cities.columns.values[:10], rotation = 45);
ax.set_yticklabels(ax.get_yticks()/1000000);
ax.set_title('Median Home Price by Location');
ax.set_ylabel('Price (Millions $)');
ax.set_xlabel('');
```



Models

I start here by adding the encoded location data back to the main dataframe. This was kept separate earlier to keep the plots clean.

```
[54]: # Plotting is done so we can bring the encoded cities data back homes = pd.concat([homes,cities],axis=1)
```

Basic Model

This is a very basic linear regression model that only used sqft_living to predict the price.

```
[55]: X_basic = homes[['sqft_living']]
    y_basic = homes.price

#Scaling the data so the coefficients are comparable
    scaler_basic = StandardScaler()
    X_scaled_basic = scaler_basic.fit_transform(X=X_basic,y=y_basic)
```

[55]: Values Train R2 0.488 Train Mean Abs Err 175043.731 Train Mean Sq Err 70579154795.151 Train Root Mean Sq Err 265667.376 Test R2 0.509 Test Mean Abs Err 171258.475 Test Mean Sq Err 62125867519.457 Test Root Mean Sq Err 249250.612

```
[56]: # Print coefficients
basic_summary[1].sort_values(by='Values',ascending=False)
```

[56]: Values sqft_living 259302.560 const 0.000

An R2 of around 0.5 for both train and test is not great and the RMSE is around \$250,000. This means the model is off by a quarter of a million dollars on average. Not good!

Slightly Better Model

This is a better linear regression model that uses all of the available predictors to predict the housing price.

```
[57]: X_mid = homes.drop('price',axis=1)
y_mid = homes.price

scaler_mid = StandardScaler()
X_scaled_mid = scaler_mid.fit_transform(X=X_mid,y=y_mid)
X_scaled_mid = pd.DataFrame(X_scaled_mid,columns=X_mid.columns)
```

```
X_scaled_mid = sm.add_constant(X_scaled_mid)
      # Perform a train test split with the default size
      # Random seed e = 2.71828
      X_train_mid, X_test_mid, y_train_mid, y_test_mid\
           = train_test_split(X_scaled_mid,y_mid,random_state=271828)
      # Create and fit linear regression and get summary
      mid_regression = LinearRegression().fit(X_train_mid,y_train_mid)
      mid_summary = model_summary(mid_regression,
                                    X_train_mid, X_test_mid, y_train_mid, y_test_mid)
      # Print summary statistics
      mid summary[0]
[57]:
                                       Values
     Train R2
                                       0.728
      Train Mean Abs Err
                                  120343.656
      Train Mean Sq Err
                             37499863867.808
      Train Root Mean Sq Err
                                  193648.816
      Test R2
                                       0.762
      Test Mean Abs Err
                                  116574.837
      Test Mean Sq Err
                             30129105775.133
      Test Root Mean Sq Err
                                  173577.377
[58]: # Print coefficients
      mid_summary[1].sort_values(by='Values',ascending=False)
[58]:
                             Values
      sqft_living
                         161404.841
      grade
                         113241.238
      city_Seattle
                          95183.422
                          87532.790
      age
      city_Bellevue
                          85803.122
      city_Medina
                          58767.617
      city_Kirkland
                          53127.830
      city_Mercer_Island 50847.110
      waterfront
                          49556.441
      city_Redmond
                          42439.396
      view
                          33166.125
     bathrooms
                          27850.444
      city_Issaquah
                          27576.336
      city_Sammamish
                          27002.028
      city_Woodinville
                          17728.645
      city_Renton
                          17404.948
      floors
                          16619.022
      condition
                          15046.525
      city_Kenmore
                          13027.638
```

```
city_Snoqualmie
                    11390.561
city Bothell
                    10575.870
city_Fall_City
                     9652.928
city_North_Bend
                     9453.148
city_Duvall
                     8351.466
city_Carnation
                     7983.642
city_Maple_Valley
                     6111.203
city_Black_Diamond
                     5347.325
city Kent
                     2827.747
sqft lot
                     2045.366
const
                       -0.000
city_Enumclaw
                     -125.125
city_Vashon
                     -223.728
city_Federal_Way
                    -5959.077
since_reno
                   -17860.985
bedrooms
                   -37013.718
```

An R2 value of between 0.728 and 0.762 is pretty alright for this model. We even got the RMSE down to between \$193,000 and \$173,000. This is about \$60,000 better than the previous model. We can still do better though.

Best I Could Do

This is the best linear regression model I could make that uses some of the available predictors to predict the housing price. It differs from the previous models in that I transform some of the data before I use it to make a prediction.

```
[59]: # These two features did not provide significant value in the previous model
homes.drop('sqft_lot',inplace=True,axis=1)
homes.drop('since_reno',inplace=True,axis=1)

# These predictors appear to be log normally distributed
homes.price = homes.price.apply(np.log)
homes.sqft_living = homes.sqft_living.apply(np.log)
```

```
[60]: X_best = homes.drop('price',axis=1)
y_best = homes.price

# Scaling the data this time
#scaler_best = StandardScaler()
#X_scaled_best = scaler_best.fit_transform(X=X_best,y=y_best)
#X_scaled_best = pd.DataFrame(X_scaled_best,columns=X_best.columns)

X_best = sm.add_constant(X_best)

# Perform a train test split with the default size
# Random seed e = 2.71828
X_train_best, X_test_best, y_train_best, y_test_best\
= train_test_split(X_best,y_best,random_state=271828)
```

[60]: Values Train R2 0.779 Train Mean Abs Err 0.187 Train Mean Sq Err 0.062 Train Root Mean Sq Err 0.248 Test R2 0.783 Test Mean Abs Err 0.183 Test Mean Sq Err 0.059 Test Root Mean Sq Err 0.244

[61]: # Print coefficients
best_summary[1].sort_values(by='Values',ascending=False)

[61]: Values city_Medina 1.178 city_Mercer_Island 0.777 city_Bellevue 0.685 city_Kirkland 0.594 city_Redmond 0.582 city_Sammamish 0.499 city_Issaquah 0.481 city_Fall_City 0.465 city_Seattle 0.464 city_Woodinville 0.444 sqft_living 0.423 city_Bothell 0.410 city Snoqualmie 0.406 city_Kenmore 0.383 city_Vashon 0.339 city_Carnation 0.338 waterfront 0.330 city_Duvall 0.328 city_North_Bend 0.328 city_Black_Diamond 0.272 city_Renton 0.230 city_Maple_Valley 0.171 0.171 grade floors 0.081

```
bathrooms
                      0.064
view
                      0.054
condition
                      0.053
city_Enumclaw
                      0.048
city_Kent
                      0.038
                      0.004
age
const
                      0.000
bedrooms
                     -0.036
city_Federal_Way
                     -0.045
```

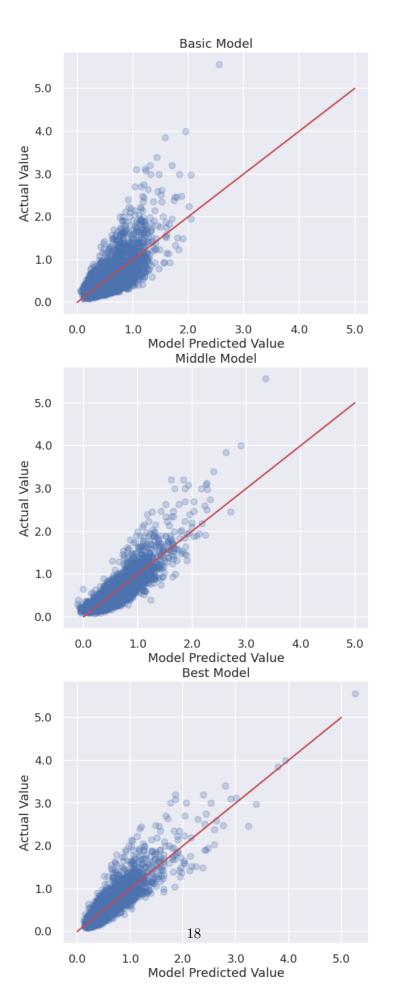
This model got an R2 value between 0.779 and 0.783 which is pretty good. The rest of the factors are not super easy to interpret though because this model is predicting the natural log of the price of the house instead of the price directly. You can inverse the log to get good price predictions from this model, but it is less useful in analyzing the effects of each variable than the lase model.

Comparing Model Predictions

The following graphs show the predictive power of each model. The ideal model would just show the line y=x where the predictions from the model are exactly the same as the actual home prices.

```
[62]: y_x = np.linspace(0, 5e6, 100)
      # Generating predictions for each model
      basic_pred = basic_regression.predict(X_test_basic)
      mid_pred = mid_regression.predict(X_test_mid)
      # This model predicts the log so we need to exponentiate
      best_pred = np.exp(best_regression.predict(X_test_best))
      fig,(ax1,ax2,ax3) = plt.subplots(3,figsize = (8,24))
      # Plot for the basic model
      ax1.scatter(basic_pred,y_test_basic,alpha=0.25)
      ax1.plot(y_x,y_x,color='r')
      ax1.set_title('Basic Model')
      # Plot for the middle model
      ax2.scatter(mid_pred,y_test_mid,alpha=0.25)
      ax2.plot(y_x,y_x,color='r')
      ax2.set_title('Middle Model')
      # Plot for the third model
      # This model predicts the log so we need to exponentiate
      ax3.scatter(best_pred,np.exp(y_test_best),alpha=0.25)
      ax3.plot(y_x,y_x,color='r')
      ax3.set_title('Best Model')
      for ax in [ax1,ax2,ax3]:
          ax.set_xlabel('Model Predicted Value');
```

```
ax.set_ylabel('Actual Value')
ax.set_yticklabels(ax.get_yticks()/1000000);
ax.set_xticklabels(ax.get_xticks()/1000000);
```



Using Statsmodels

Statsmodels shows mostly the same information as the SKLearn models. It was mostly used for the confidence interval function at the top of this notebook and statistical information on my coefficients.

```
[63]: # Generate the regressions using the same data as from SKLearn sm_basic = sm.OLS(y_train_basic, X_train_basic).fit() sm_mid = sm.OLS(y_train_mid, X_train_mid).fit() sm_best = sm.OLS(y_train_best, X_train_best).fit()
```

Basic Model

```
[64]: sm_basic.summary()
```

Covariance Type:

[64]: <class 'statsmodels.iolib.summary.Summary'>

OLS Regression Results

Dep. Variable:	price	R-squared:	0.488
Model:	OLS	Adj. R-squared:	0.488
Method:	Least Squares	F-statistic:	1.541e+04
Date:	Tue, 22 Feb 2022	Prob (F-statistic):	0.00
Time:	20:16:53	Log-Likelihood:	-2.2528e+05
No. Observations:	16197	AIC:	4.506e+05
Df Residuals:	16195	BIC:	4.506e+05
Df Model:	1		

=======================================		=========			
coef	std err	t	P> t	[0.025	0.975]

nonrobust

const	5.406e+05	2087.606	258.967	0.000	5.37e+05	5.45e+05
sqft_living	2.593e+05	2088.744	124.143	0.000	2.55e+05	2.63e+05
========	========		========			
Omnibus:		11598.3	01 Durbin	-Watson:		2.008
Prob(Omnibus):	0.0	00 Jarque	-Bera (JB):		486196.505
Skew:		2.9	65 Prob(J	B):		0.00

Kurtosis: 29.178 Cond. No. 1.00

Notes:

11 11 11

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Slightly Better Model

[65]: sm_mid.summary()

[65]: <class 'statsmodels.iolib.summary.Summary'>

OLS Regression Results

OLS Regression Results						
Dep. Variable: Model: Method: Date: Time: No. Observations: Df Residuals: Df Model: Covariance Type:	Least S Tue, 22 Fe 20 non	OLS Squares eb 2022 0:16:53 16197 16162 34 arobust	R-squared: Adj. R-squar F-statistic: Prob (F-stat Log-Likeliho AIC: BIC:	0.728 0.727 1271. 0.00 -2.2016e+05 4.404e+05 4.407e+05		
0.975]	coef	std err		P> t	[0.025	
 const 5.43e+05	5.404e+05	1523.539	354.689	0.000	5.37e+05	
bedrooms -3.31e+04	-3.701e+04	2008.667	-18.427	0.000	-4.1e+04	
bathrooms 3.33e+04	2.785e+04	2771.829	10.048	0.000	2.24e+04	
sqft_living 1.68e+05	1.614e+05	3192.868	50.552	0.000	1.55e+05	
sqft_lot 5228.179	2045.3660	1623.792	2 1.260	0.208	-1137.447	
floors	1.662e+04	1986.635	8.365	0.000	1.27e+04	
2.05e+04 waterfront 5.28e+04	4.956e+04	1657.552	29.897	0.000	4.63e+04	
view 3.66e+04	3.317e+04	1770.952	18.728	0.000	2.97e+04	
condition 1.84e+04	1.505e+04	1711.802	8.790	0.000	1.17e+04	
grade 1.19e+05	1.132e+05	2716.668	41.684	0.000	1.08e+05	
since_reno	-1.786e+04	4196.327	-4.256	0.000	-2.61e+04	
-9635.720 age 9.57e+04	8.753e+04	4176.321	20.959	0.000	7.93e+04	
9.57e+04 city_Bellevue 9.05e+04	8.58e+04	2398.625	35.772	0.000	8.11e+04	

city_Black_Diamond 8455.386	5347.3252	1585.655	3.372	0.001	2239.265	
city_Bothell 1.38e+04	1.058e+04	1637.897	6.457	0.000	7365.411	
city_Carnation 1.12e+04	7983.6422	1640.045	4.868	0.000	4768.973	
city_Duvall 1.16e+04	8351.4665	1659.447	5.033	0.000	5098.766	
city_Enumclaw 3262.904	-125.1253	1728.488	-0.072	0.942	-3513.154	
city_Fall_City 1.29e+04	9652.9279	1648.583	5.855	0.000	6421.523	
city_Federal_Way	-5959.0769	2022.277	-2.947	0.003	-9922.963	
city_Issaquah 3.16e+04	2.758e+04	2043.705	13.493	0.000	2.36e+04	
city_Kenmore 1.65e+04	1.303e+04	1791.541	7.272	0.000	9516.020	
city_Kent 7233.521	2827.7468	2247.717	1.258	0.208	-1578.027	
city_Kirkland 5.74e+04	5.313e+04	2165.408	24.535	0.000	4.89e+04	
city_Maple_Valley 9896.991	6111.2027	1931.416	3.164	0.002	2325.414	
city_Medina 6.19e+04	5.877e+04	1583.538	37.112	0.000	5.57e+04	
city_Mercer_Island 5.43e+04	5.085e+04	1744.843	29.141	0.000	4.74e+04	
city_North_Bend 1.28e+04	9453.1477	1699.063	5.564	0.000	6122.796	
city_Redmond 4.67e+04	4.244e+04	2165.701	19.596	0.000	3.82e+04	
city_Renton 2.22e+04	1.74e+04	2431.316	7.159	0.000	1.26e+04	
city_Sammamish 3.11e+04	2.7e+04	2099.489	12.861	0.000	2.29e+04	
city_Seattle 1.03e+05	9.518e+04	3980.495	23.912	0.000	8.74e+04	
city_Snoqualmie 1.49e+04	1.139e+04	1775.716	6.415	0.000	7909.960	
city_Vashon 2936.050	-223.7276	1612.040	-0.139	0.890	-3383.505	
city_Woodinville 2.14e+04	1.773e+04	1894.929	9.356	0.000	1.4e+04	
Omnibus:	 14:		urbin-Watson:		2.013	
Prob(Omnibus):		0.000 J	arque-Bera (J	D);	1794755.841	L

Skew:	3.732	Prob(JB):	0.00
Kurtosis:	54.026	Cond. No.	9.16

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified. 11 11 11

Best Model

[66]: sm_best.summary()

[66]

=======================================		Regressio			.=======
Dep. Variable:			 -squared:		0.77
Model:		OLS A	dj. R-squared	:	0.77
Method:	Least S	1	'-statistic:		1777
Date:	Tue, 22 Fe		rob (F-statis		0.0
Time:	20		.og-Likelihood	:	-411.3
No. Observations:			IC:		888.
Df Residuals:			BIC:		1142
Df Model:		32			
Covariance Type:		robust			
======		=======		=======	=======
	coef	std err	t	P> t	[0.025
0.975]	0001	DUG CII	· ·	17 0	[0.020
const	7.6879	0.057	135.386	0.000	7.577
7.799					
bedrooms	-0.0358	0.003	-12.111	0.000	-0.042
-0.030					
bathrooms	0.0637	0.005	14.067	0.000	0.055
0.073					
sqft_living	0.4230	0.010	43.799	0.000	0.404
0.442	0.0004	0 005	17 150	0.000	0.074
floors	0.0806	0.005	17.150	0.000	0.071
0.090	0.3300	0.000	10 750	0.000	0.070
waterfront 0.381	0.3302	0.026	12.753	0.000	0.279
view	0.0536	0.003	18.141	0.000	0.048
0.059	0.0556	0.003	10.141	0.000	0.040
condition	0.0529	0.003	15.939	0.000	0.046
0.059	0.0029	0.003	10.303	0.000	0.040

grade 0.176	0.1706	0.003	58.986	0.000	0.165
age 0.004	0.0036	0.000	36.188	0.000	0.003
city_Bellevue	0.6855	0.012	55.113	0.000	0.661
city_Black_Diamond	0.2720	0.030	9.103	0.000	0.213
0.331 city_Bothell	0.4096	0.022	18.464	0.000	0.366
0.453 city_Carnation	0.3381	0.028	12.292	0.000	0.284
0.392 city_Duvall	0.3282	0.023	14.421	0.000	0.284
0.373 city_Enumclaw	0.0481	0.021	2.254	0.024	0.006
0.090 city_Fall_City	0.4650	0.035	13.454	0.000	0.397
0.533 city_Federal_Way	-0.0453	0.014	-3.263	0.001	-0.073
-0.018 city_Issaquah	0.4814	0.014	33.283	0.000	0.453
0.510 city_Kenmore	0.3835	0.020	19.000	0.000	0.344
0.423 city_Kent	0.0378	0.013	3.004	0.003	0.013
0.062 city_Kirkland	0.5937	0.013	44.513	0.000	0.568
0.620 city_Maple_Valley	0.1708	0.015	11.237	0.000	0.141
0.201 city_Medina	1.1781	0.042	27.907	0.000	1.095
1.261 city_Mercer_Island	0.7767	0.020	39.461	0.000	0.738
0.815 city_North_Bend	0.3278	0.022	15.155	0.000	0.285
0.370 city_Redmond	0.5822	0.013	43.598	0.000	0.556
0.608 city_Renton	0.2298	0.012	19.313	0.000	0.207
0.253 city_Sammamish	0.4987	0.014	35.041	0.000	0.471
0.527 city_Seattle	0.4642	0.010	44.935	0.000	0.444
0.484 city_Snoqualmie	0.4057	0.019	21.145	0.000	0.368
0.443 city_Vashon	0.3392	0.028	12.159	0.000	0.285
• =					

0.394 city_Woodinville 0.477	0.4441	0.017	26.746	0.000	0.412
Omnibus:			Durbin-Watson:		2.012
<pre>Prob(Omnibus): Skew:</pre>			<pre>Jarque-Bera (J Prob(JB):</pre>	В):	1272.602 4.55e-277
Kurtosis:		4.335	Cond. No.		1.80e+03

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 1.8e+03. This might indicate that there are strong multicollinearity or other numerical problems.

Model Validation

There are three assumptions made when using a linear regression model.

Linearity: Is there a linear relationship between the target and the predictors?

We looked at this during the exploratory data analysis.

Normality: Are the residuals of the model normally distributed?

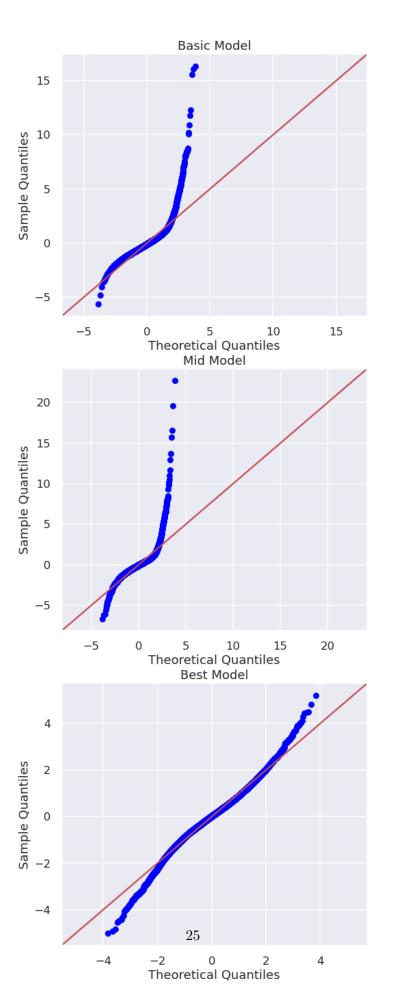
We will look at this below.

Homoscedasticity: Does the variance of the residuals change based on the value of the target?

We looked at this in the comparing model predictions section. It does appear that the residuals variance increases as price increases. I am not sure if this is statistically significant because I was unable to get the code for the Goldfeld-Quandt test working.

Normality

The basic and medium models perform poorly in terms of normality of the residuals. The best model's residuals are pretty normally distributed however, only really deviating at the tails.



Results

We were successful in creating a model that Bentley & Co. Bank can use to predict the price of a home given information about its features.

A linear regression model was appropriate for predicting home price using the provided dataset.

78 Percent of the variance in home price can be explained by the selected home features in the best model.

The following features proved to be the most important when predicting the price of a home:

Location

Grade

Living Area Square-Footage

I recommend that Bentley & Co. Bank use the best model for quick-and-dirty estimates of home price before a professional appraisal can be performed.

I recommend that Bentley & Co. Bank use the best model to estimate the price impact of renovations on homes it has an interest in when an additional appraisal is not appropriate.

An example price prediction is shown below.

```
[68]: # Predict a random house from the test set's price
predict_interval(X_test_best.iloc[42],confidence=0.001);
```

This house has a predicted value of \$663648.

A safe value for this house would fall between \$640175 and \$687982.