

# Signal Curve Fitting

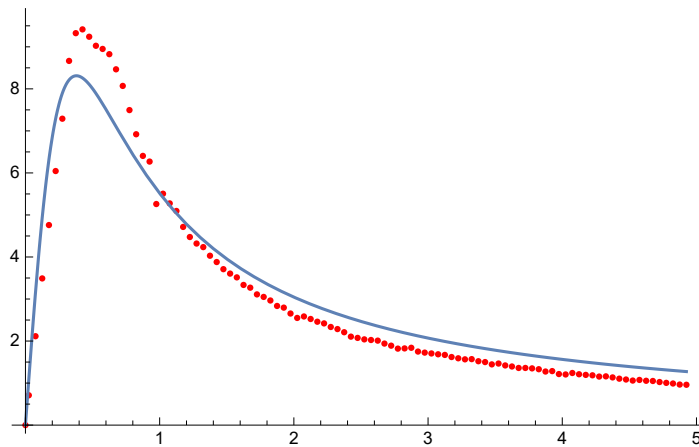
- What follows is a test of one signal function vs two signal functions.
  - For the most part,  $a_1$ ,  $b_1$  roughly =  $a_2$ ,  $b_2$  respectively, with several exceptions.
- 

NDTWM Amplitude scan 100nm - 1, 200nm - 2, and Glycerin -1

- Fit One Signal Function

```
Clear[v]
v = Import["\\\\files.brown.edu\\Home\\nlawandy\\Documents\\NDTWM
    Amplitude scan 100nm - 1, 200nm - 2, and Glycerin -1.csv"]
u = v[[4 ;; All, {2, 4}]]
FindFit[u, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

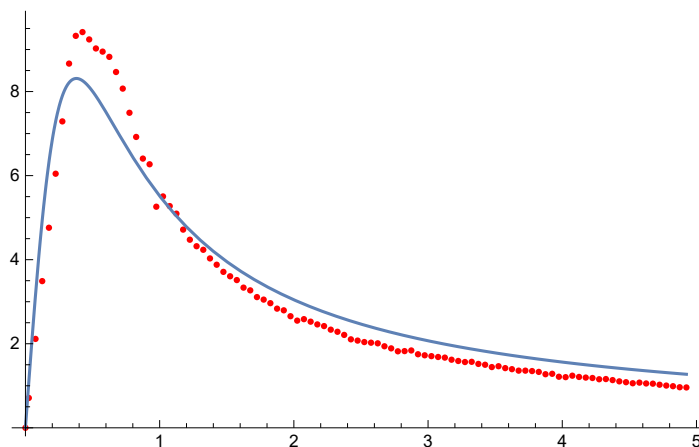
```
Show[ListPlot[u, PlotStyle -> Red],
Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 16.6225, b -> 0.379648}, {x, 0, 4.925}]]
```



## ■ Fitting Sum of Two Signal Functions

```
FindFit[u, ((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
{a -> 8.30401, b -> 0.379648, a2 -> 8.31853, b2 -> 0.379648}
```

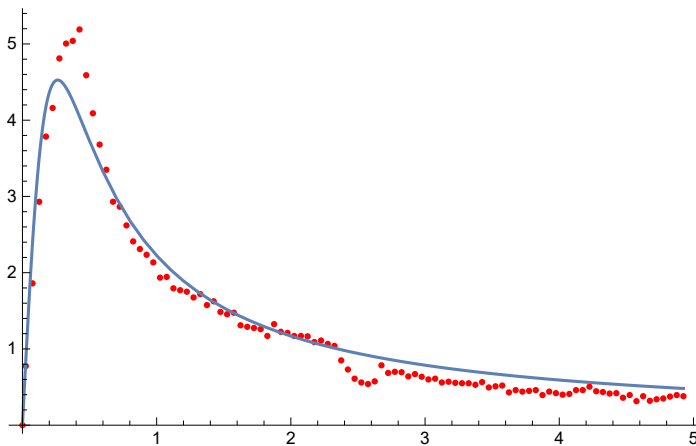
```
Show[ListPlot[u, PlotStyle -> Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.
{a -> 8.30401, b -> 0.379648, a2 -> 8.31853, b2 -> 0.379648}, {x, 0, 4.925}]]
```



NDTWAM Amplitude scan 100 nm,  
200 nm, and Glycerin (I)

## ■ Fit One Signal Function

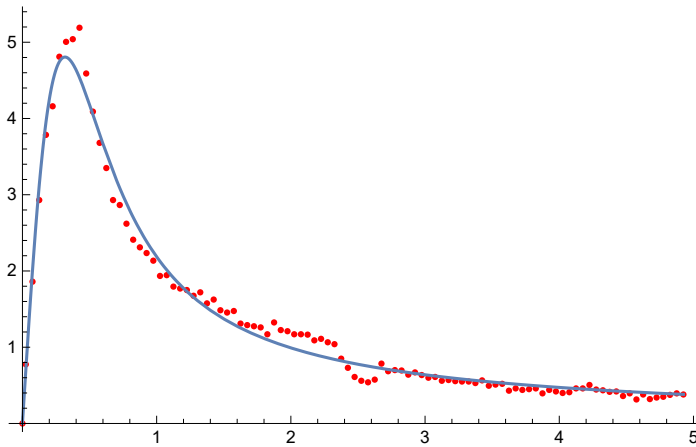
```
v1 = Import["\\\\files.brown.edu\\Home\\nlawandy\\Documents\\NDTWM
  Amplitude scan 100nm, 200nm, and Glycerin (1).csv"]
u1 = v1[[4 ;; All, {2, 4}]]
FindFit[u1, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
Show[ListPlot[u1, PlotStyle -> Red],
  Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 9.05221, b -> 0.262742}, {x, 0, 4.925}]]
```



## ■ Fitting Sum of Two Functions

```
FindFit[u1,
  ((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
{a -> 158.502, b -> 0.468763, a2 -> 149.899, b2 -> -0.48329}
```

```
Show[ListPlot[u1, PlotStyle → Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.  
{a → 158.502, b → 0.468763, a2 → 149.899, b2 → -0.48329}, {x, 0, 4.925}]]
```



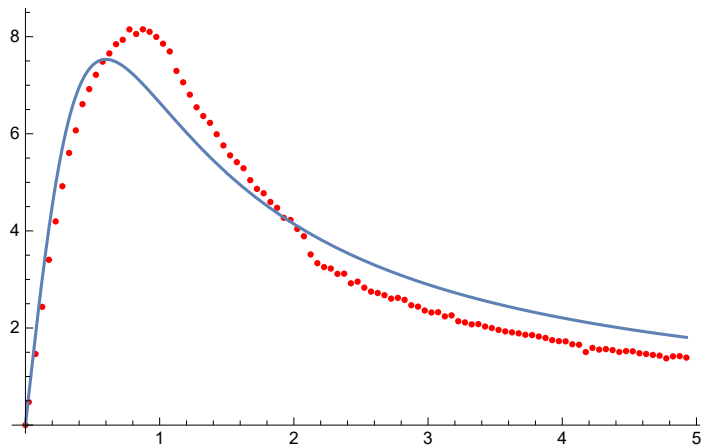
Higher power 33% 100nm, 10% + 33 % 200nm,  
1% +33% water

No 7 Power 37 Hz

## ■ Fit One Signal Function

```
v2 = Import["\\\\files.brown.edu\\\\Home\\\\nlawandy\\\\Documents\\\\No 7 Power 37Hz.csv"]  
u2 = v2[[4 ;; All, {2, 4}]]  
FindFit[u2, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

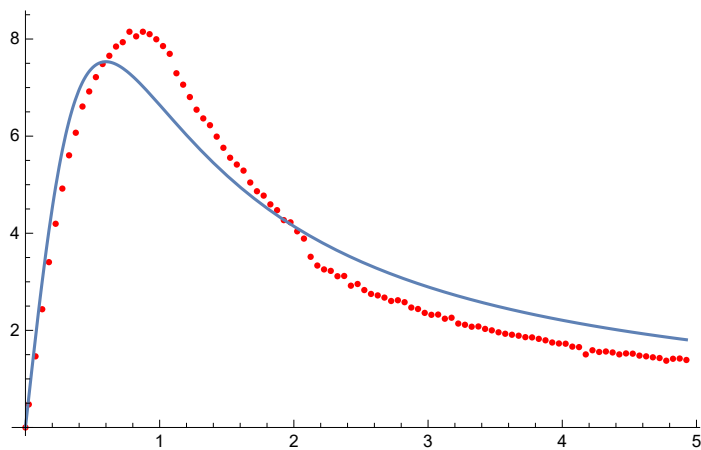
```
Show[ListPlot[u2, PlotStyle -> Red],
Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 15.0653, b -> 0.599399}, {x, 0, 4.925}]]
```



## ■ Fitting Sum of Two Functions

```
FindFit[u2,
((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
{a -> 7.60004, b -> 0.599399, a2 -> 7.46525, b2 -> 0.599399}
```

```
Show[ListPlot[u2, PlotStyle -> Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.
{a -> 7.60004, b -> 0.599399, a2 -> 7.46525, b2 -> 0.599399}, {x, 0, 4.925}]]
```

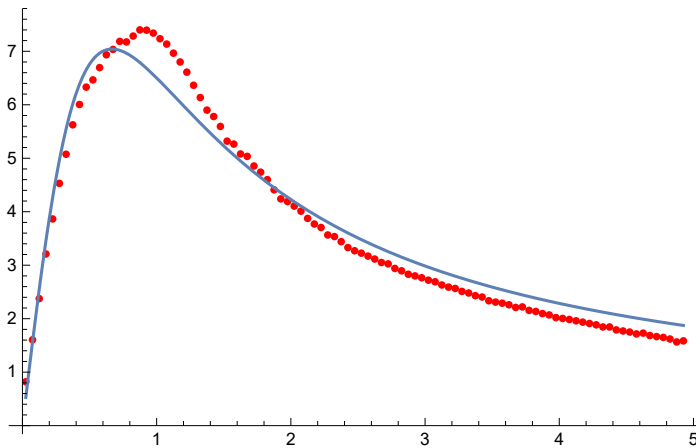


No 7 Power 74 Hz

## ■ Fit One Signal Function

```
v3 = Import["\\\\files.brown.edu\\Home\\nlawandy\\Documents\\No 7 Power 74Hzz.csv"]
u3 = v3[[4 ;; All, {2, 4}]]
FindFit[u3, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

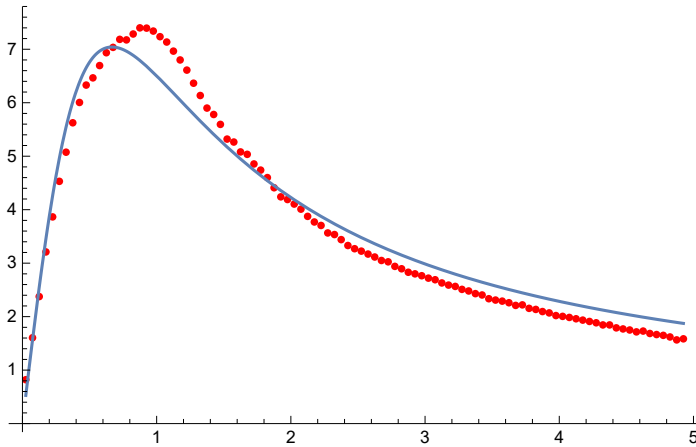
```
Show[ListPlot[u3, PlotStyle -> Red],
Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 14.0835, b -> 0.667205}, {x, 0.025, 4.925}]]
```



## ■ Fitting Sum of Two Functions

```
FindFit[u3,
((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
{a -> 5.82612, b -> 0.667205, a2 -> 8.25733, b2 -> 0.667205}
```

```
Show[ListPlot[u3, PlotStyle → Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.  
{a → 5.82612, b → 0.667205, a2 → 8.25733, b2 → 0.667205}, {x, 0.025, 4.925}]]
```

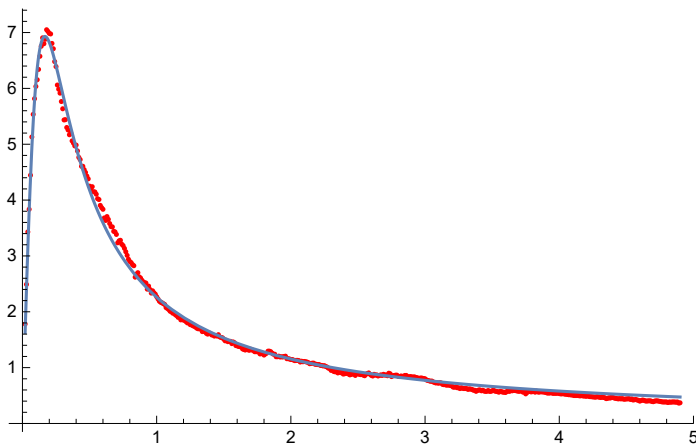


## No 7 Power 148 and 170 Hz

### ■ Fit One Signal Function

```
v4 =  
  Import["\\\\files.brown.edu\\\\Home\\\\nlawandy\\\\Documents\\\\No 7 power 148 and 170Hzz.csv"]  
u4 = v4[[4 ;; All, {2, 4}]]  
FindFit[u4, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

```
Show[ListPlot[u4, PlotStyle → Red],  
  Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a → 13.8598, b → 0.167663}, {x, 0.02, 4.9}]]
```

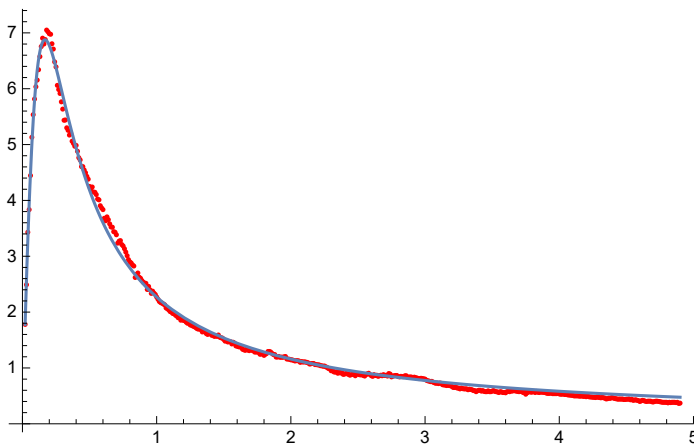


## ■ Fitting Sum of Two Functions

```
FindFit[u4,
  ((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
{a → 13.414, b → 0.17175, a2 → 0.658907, b2 → 0.0467836}
```

```
Show[ListPlot[u4, PlotStyle → Red], Plot[
  
$$\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)},
  {a → 13.414, b → 0.17175, a2 → 0.658907, b2 → 0.0467836}, {x, 0.02, 4.9}]]$$

```



## Polystyrene Nanospheres at Different Powers

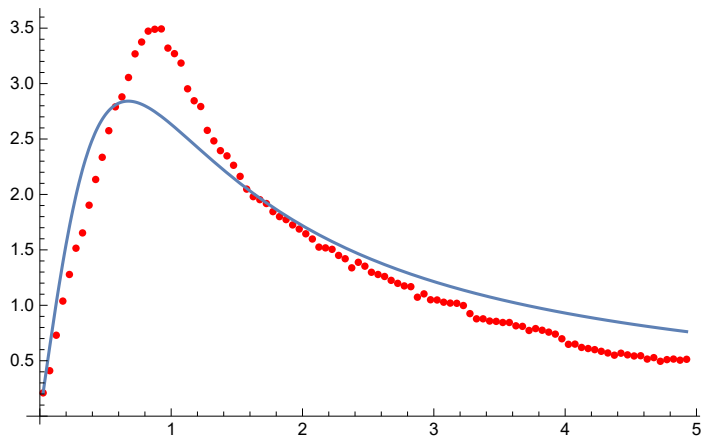
NDTWM Amplitude scan at different power, 200nm, 1proc

## ■ Fit One Signal Function

```
v5 = Import["NDTWM Amplitude scan at different power, 200nm , 1proc.csv"]
u5 = v5[[4 ;; All, {2, 10}]]
FindFit[u5, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```



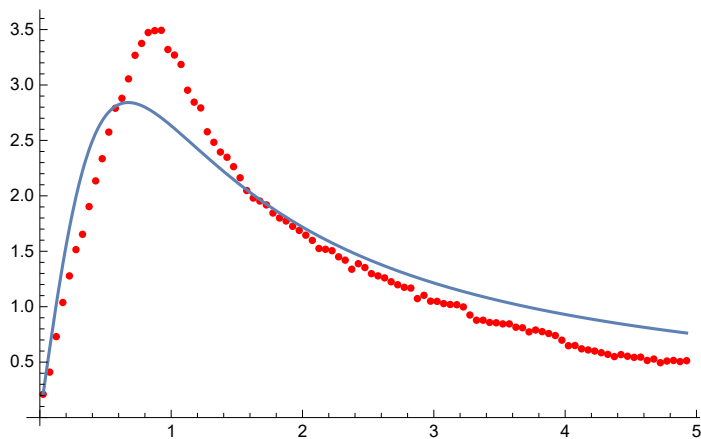
```
Show[ListPlot[u5, PlotStyle -> Red],
Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 5.68341, b -> 0.673088}, {x, 0.025, 4.925}]]
```



## ■ Fitting Sum of Two Functions

```
FindFit[u5,
((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
{a -> 2.73733, b -> 0.673088, a2 -> 2.94608, b2 -> 0.673088}
```

```
Show[ListPlot[u5, PlotStyle -> Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.
{a -> 2.73733, b -> 0.673088, a2 -> 2.94608, b2 -> 0.673088}, {x, 0.025, 4.925}]]
```

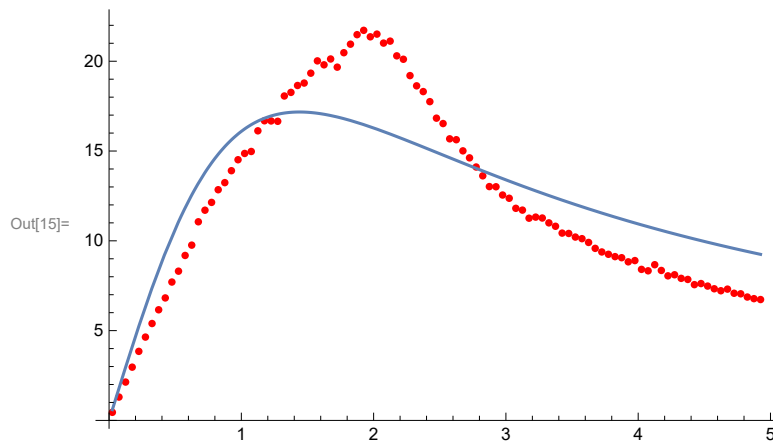


## NDTWAM Amplitude scan at different power, 100nm, 10proc

### ■ Fit One Signal Function

```
In[12]:= v6 = Import["\\\\files.brown.edu\\Home\\nlawandy\\Documents\\100nm, 10 proc.csv"]
u6 = v6[[3 ;; All, {3, 2}]]
FindFit[u6, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

```
In[15]:= Show[ListPlot[u6, PlotStyle -> Red],
Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 34.3466, b -> 1.43912}, {x, 0.025, 4.925}]]
```



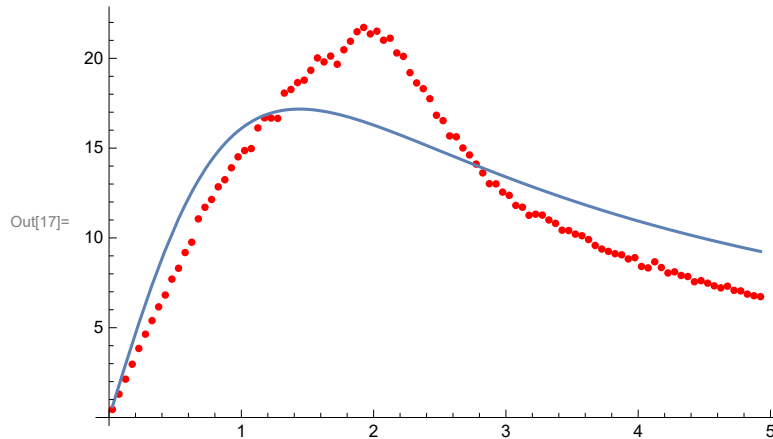
### ■ Fitting Sum of Two Functions

```
In[16]:= FindFit[u6,
((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
```

```
Out[16]:= {a -> 17.0056, b -> 1.43912, a2 -> 17.3411, b2 -> 1.43912}
```

```
In[17]:= Show[ListPlot[u6, PlotStyle → Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.  

{a → 17.0056, b → 1.43912, a2 → 17.3411, b2 → 1.43912}, {x, 0.025, 4.925}]]
```



## 100nm and 200nm Polystyrene NPs in 100um Cuvette

### Polystyrene 100nm, 10proc, 100um, Triangle

#### ■ Fit One Signal Function

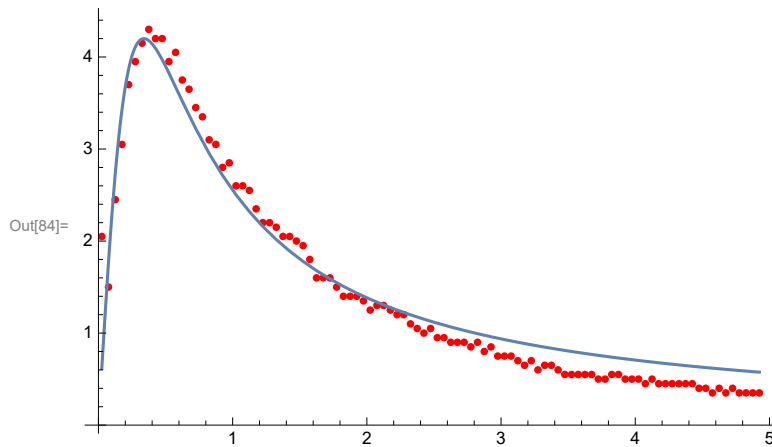
```
In[81]:= v7 = Import["\\\\files.brown.edu\\\\Home\\\\nlawandy\\\\Documents\\\\Polystyrene 100nm,  

10proc, 100um, Triangle.csv"]  

u7 = v7[[3 ;; All, {3, 1}]]  

FindFit[u7, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

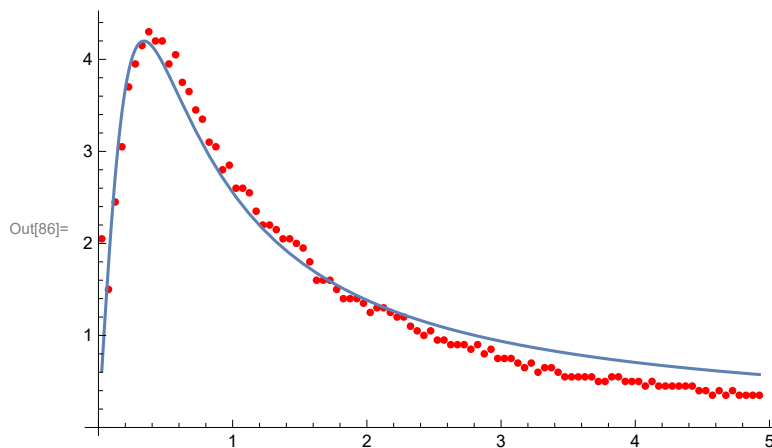
```
In[84]:= Show[ListPlot[u7, PlotStyle -> Red],
  Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 8.39805, b -> 0.338942}, {x, 0.025, 4.925}]]
```



## ■ Fitting Sum of Two Functions

```
In[85]:= FindFit[u7,
  ((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
Out[85]= {a -> 4.94181, b -> 0.338942, a2 -> 3.45623, b2 -> 0.338942}
```

```
In[86]:= Show[ListPlot[u7, PlotStyle -> Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.
  {a -> 4.94181, b -> 0.338942, a2 -> 3.45623, b2 -> 0.338942}, {x, 0.025, 4.925}]]
```

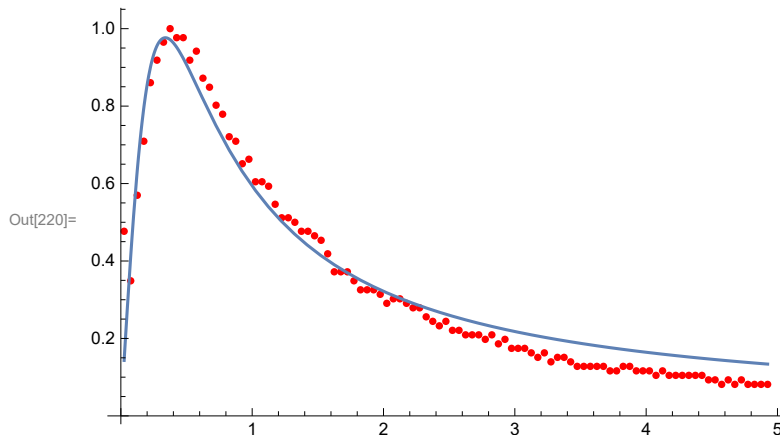


Polystyrene 100 nm, 10 proc, 100 um, Triangle Norm

## ■ Fit One Signal Function

```
v8 = Import["\\\\files.brown.edu\\Home\\nlawandy\\Documents\\Polystyrene
100nm, 10proc , 100um, Triangle Norm.csv"]
u8 = v8[[3 ;; All, {1, 3}]]
FindFit[u8, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

```
In[220]:= Show[ListPlot[u8, PlotStyle → Red],
Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a → 1.95303, b → 0.338942}, {x, 0.025, 4.925}]]
```

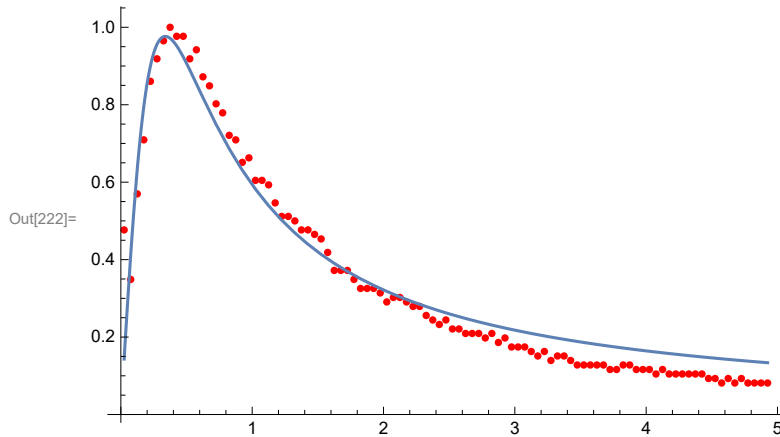


## ■ Fitting Sum of Two Functions

```
In[221]:= FindFit[u8,
((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
Out[221]= {a → 0.833705, b → 0.338942, a2 → 1.11933, b2 → 0.338942}
```

```
In[222]:= Show[ListPlot[u8, PlotStyle → Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.  

{a → 0.833705, b → 0.338942, a2 → 1.11933, b2 → 0.338942}, {x, 0.025, 4.925}]]
```



Polystyrene 200 nm, 1 proc, 100 um, Triangle

## ■ Fit One Signal Function

```
In[250]:= v9 = Import["\\\\files.brown.edu\\\\Home\\\\nlawandy\\\\Documents\\\\Polystyrene  

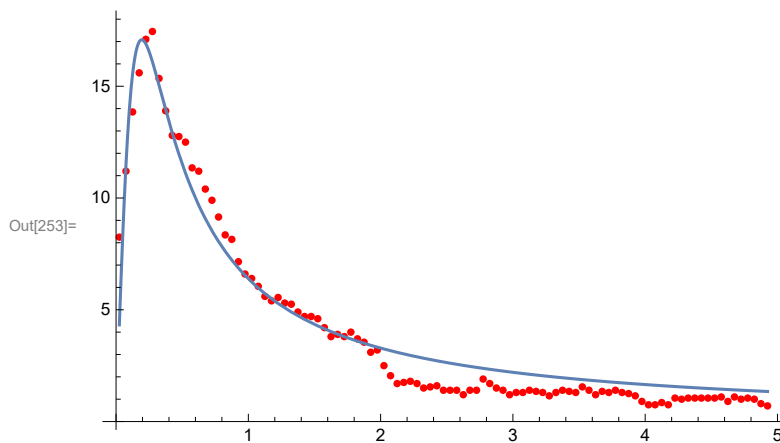
200nm, 1proc , 100um, Triangle!'.csv"]  

u9 = v9[[3 ;; 101, {1, 3}]]  

FindFit[u9, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]  

In[253]:= Show[ListPlot[u9, PlotStyle → Red],  

Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a → 34.1574, b → 0.194188}, {x, 0.025, 4.925}]]
```



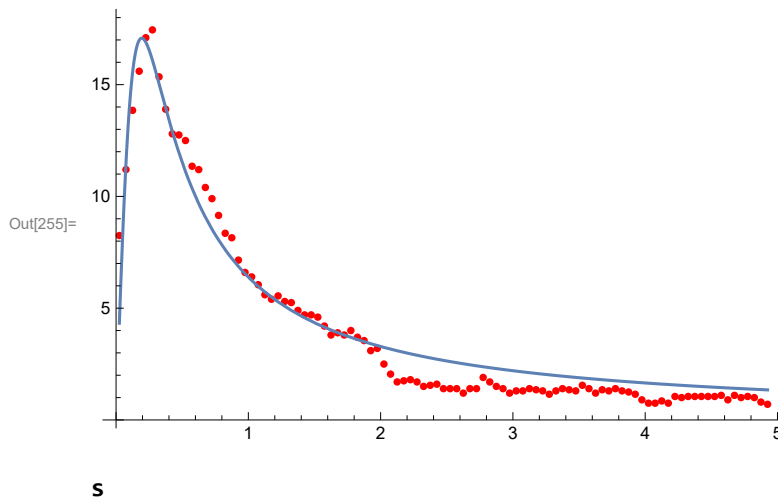
## ■ Fitting Sum of Two Functions

```
In[254]:= FindFit[u9,
  ((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
```

```
Out[254]:= {a → 16.9829, b → 0.194188, a2 → 17.1745, b2 → 0.194188}
```

```
In[255]:= Show[ListPlot[u9, PlotStyle → Red], Plot[
  
$$\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}, \{a \rightarrow 16.9829, b \rightarrow 0.194188, a2 \rightarrow 17.1745, b2 \rightarrow 0.194188\}, \{x, 0.025, 4.925\}] ]$$

```

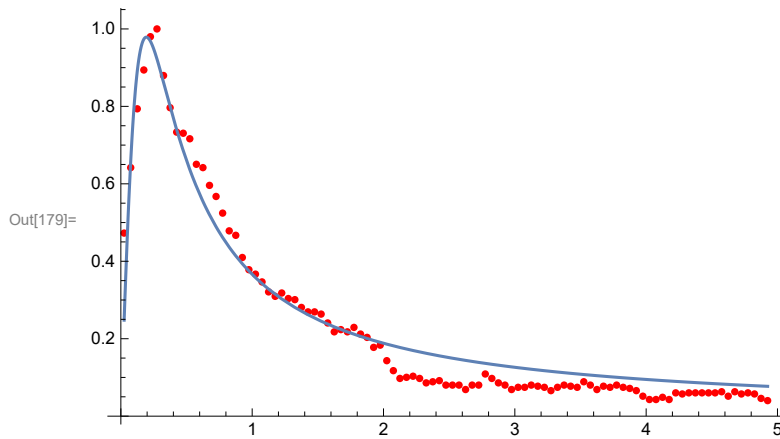


Polystyrene 200 nm, 1 proc, 100 um, Triangle Norm

## ■ Fit One Signal Function

```
In[176]:= v10 = Import["\\\\files.brown.edu\\Home\\nlawandy\\Documents\\Polystyrene
  200nm, 1proc , 100um, Triangle Norm.csv"]
u10 = v10[[3 ;; All, {1, 3}]]
FindFit[u10, (a * (x/b)) / (1 + (x/b)^2), {a, b}, x]
```

```
In[179]:= Show[ListPlot[u10, PlotStyle -> Red],
  Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)}$  /. {a -> 1.95745, b -> 0.194188}, {x, 0.025, 4.925}]]
```



## ■ Fitting Sum of Two Functions

```
In[180]:= FindFit[u10,
  ((a * (x/b)) / (1 + (x/b)^2) + (a2 * (x/b2)) / (1 + (x/b2)^2)), {a, b, a2, b2}, x]
Out[180]= {a -> 1.98621, b -> 0.221657, a2 -> 0.117465, b2 -> -2.68341}
```

```
In[181]:= Show[ListPlot[u10, PlotStyle -> Red], Plot[ $\frac{a x}{b \left(1 + \left(\frac{x}{b}\right)^2\right)} + \frac{a2 x}{b2 \left(1 + \left(\frac{x}{b2}\right)^2\right)}$  /.
  {a -> 1.98621, b -> 0.221657, a2 -> 0.117465, b2 -> -2.68341}, {x, 0.025, 4.925}]]
```

