Saas Fee School 2019 – Gaia tutorials

Jason Sanders

January 29, 2019

I provide a number of worked examples of using the Gaia data to illustrate some of the points made in the 'Fine structure of the stellar disc' lecture series. There are five tutorials that each demonstrate some basic data analysis technique using examples from Gaia. All of the tutorials use python.

The first section describes how to set up a virtual environment with the necessary packages. The examples obviously require data. We will show how to download Gaia data using the TAP protocol. For manipulating large datasets this becomes impractical. Therefore, we also will use locally stored data. These are available on USB sticks at the school (SF19_1, SF19_2) or can be downloaded from the provided sources.

Preliminaries

For these tutorials we will use Python 3.7 (available from https://www.python.org/downloads/). We first set up an environment using conda (if conda not installed, download miniconda from https://conda.io/miniconda.html)

```
conda create -n saas_fee_py python=3.7 anaconda
```

This sets up an environment distinct from your regular python installation. This is useful as we can edit and modify this environment independent of other projects. We use the environment using

```
source activate saas_fee_py
```

Then we want to install two further packages. First galpy. galpy requires gsl. The easiest way to do this is (installs a pre-compiled version)

```
conda install galpy -c conda-forge
```

Second healpy,

```
conda install healpy -c conda-forge
```

and then astroquery, emcee, corner and agama (last of which not required here).

```
pip install astroquery emcee corner agama
```

This should give you the tools you need to look at and analyse the Gaia data, as well as follow all of the examples given here. Now inside the folder with the notebooks, run

```
jupyter notebook
```

and you will see the available notebooks in the browser.

You can also run notebooks remotely. This is useful when working with large files and you only have a laptop available. First, run

```
jupyter notebook ---no-browser
```

on the computer that will run the notebooks. Note which port the notebook is using (likely 8888). Then on your computer set up an ssh tunnel to that computer like

```
ssh\ -N\ -f\ -L\ localhost: 8080: localhost: port\_on\_remote\_compute\ name\_of\_remote\_compute\ .
```

Now open the page localhost:8080 in the browser.

Tutorials

There are five tutorials.

- Tutorial 1: the vertical density profile simple accessing of Gaia data and reproducing thin-thick disc vertical density profile
- Tutorial 2: Coordinates and orbits using astropy and galpy to do coordinate transformation and integrate orbits. Illustrated with dwarf spheroidal galaxy orbits.
- Tutorial 3: Actions, angles and frequencies using galpy to find these coordinates, reproducing local substructure and the selection effects.
- Tutorial 4: Dissecting local chemo-kinematic structure cross-matching the Gaia data with spectroscopic catalogues to use chemical abundances. Splitting velocity structure based on metallicity.
- Tutorial 5: Generalized Oort constants fitting a model to data using emcee. Measure the generalized Oort constants from local proper motion and radial velocity data.

The notebooks are self-contained. They are repeated here in pdf form.

Tutorial1

January 29, 2019

1 Tutorial 1: The vertical density profile

```
In [1]: import numpy as np
        import matplotlib.pyplot as plt
        import seaborn as sns
        import warnings
        warnings.filterwarnings('ignore')
        %matplotlib inline
```

In this tutorial we will inspect the vertical density profile of the Milky Way. This will illustrate basic access of the Gaia data.

We use the TAP functionality in astroquery to collect Gaia DR2 data. This runs an ADQL query remotely and retrieves the data -- ADQL is like SQL with added functions to specifically querying astronomical datasets). You will get lots of warnings as astropy doesn't like the units used by Gaia -- I have switched these off with the warnings package. This query gets the top 100 stars with positive parallaxes and parallax/parallax_error>3. You can replace the ADQL query with your own ADQL query (see https://gea.esac.esa.int/archive-help/adql/examples/index.html for some examples of Gaia ADQL queries.

To get the names of the columns, we have to look here https://gea.esac.esa.int/archive/documentation/GDR2/Gaia_archive/chap_datamodel/

```
1635721458409799680 Gaia DR2 3665568907110130944 ...
1635721458409799680 Gaia DR2 3665359969836446592 ...
1635721458409799680 Gaia DR2 3665363298436254848 ...
1635721458409799680 Gaia DR2 3665310040841426688 ...
1635721458409799680 Gaia DR2 3665493384405764608 ...
1635721458409799680 Gaia DR2 3665430750897562752 ...
1635721458409799680 Gaia DR2 3665565990827782912 ...
1635721458409799680 Gaia DR2 3665558770987473408 ...
1635721458409799680 Gaia DR2 3665295609751790592 ...
1635721458409799680 Gaia DR2 6659606865605123328 ...
1635721458409799680 Gaia DR2 6659607140483404672 ...
1635721458409799680 Gaia DR2 6659669091091715840 ...
1635721458409799680 Gaia DR2 4051854146967173632 ...
1635721458409799680 Gaia DR2 454718259334117888 ...
1635721458409799680 Gaia DR2 454677027647939584 ...
1635721458409799680 Gaia DR2 6659596145366748288 ...
Length = 100 rows
```

We can access individual columns like this. Note the units.

In [3]: print(table['pmra'])

pmra mas / yr

- -4.723500811005363
- -1.2166110665275116
- -2.552363253029383
- 0.635310067557883
- 7.183843236279285
- -3.546599888307931
- 11.911708507626308
- -2.4256420035008754
- -0.17462586774462907
- -3.9148021973513023
 - . . .
- -4.938098907925836
- -6.335910962969821
- -3.6578054574670977
- -0.7909434760493024
- -3.8816262823174457
- -3.931825771742191
- -0.3983276159959158
- 13.828522532510284 -3.2895709286266417
- -5.0306145886236076

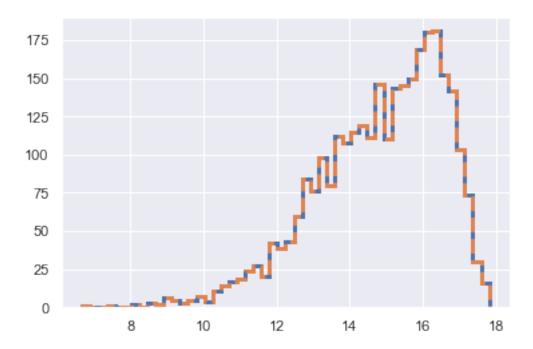
```
Length = 100 rows
```

We will now query some main sequence stars around the North Galactic Pole (Galactic latitude greater than 85 deg). The ADQL language implements various mathematical functions. Here we are using log10. We require good parallaxes (not negative and with small errors -- this might bias our sample in funny ways but for now it is good enough). We select a small range in colours $0.65 < (G_{BP} - G_{RP}) < 0.85$ and ensure they are main sequence by cutting on absolute magnitude. We don't worry about extinction as this effect is small when looking straight out of the disc.

Another way to do this is using the ADQL built-in geometric functions. POINT is a function describing a point on the sky and BOX, POLYGON, CIRCLE are all functions that describe a region on the sky. Typically they are used in conjunction with CONTAINS. This will return True (1) is POINT is CONTAINed in CIRCLE. In theory these should work with Galactic coordinates but I can't get this to work. We therefore require the coordinates of the NGP, using astropy. In theory, using ra, dec is faster as the Gaia archive has been indexed on these entries.

In [5]: from astropy.coordinates import SkyCoord, ICRS

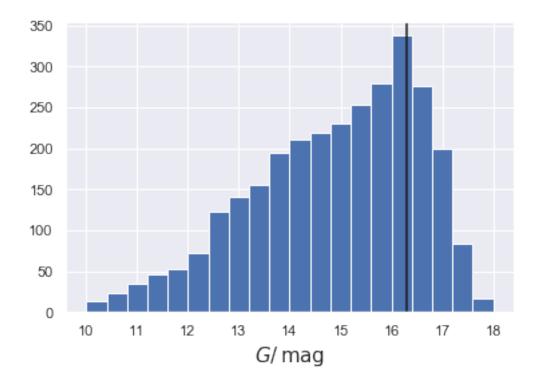
Query finished.



We have to worry about completeness. Gaia only observes down to a limiting magnitude. We can see in the magnitude distribution a truncation at around 16.3 mag. For our selected main sequence stars (with median magnitude 4.3) this corresponds to a limiting distance of 2.5 kpc.

```
In [8]: limiting_mag = 16.3 #
    plt.axvline(limiting_mag,color='k')
    plt.hist(table['phot_g_mean_mag'],range=[10.,18.],bins=20)
    plt.xlabel(r'$G/\,\mathrm{mag}$')

Mv = np.median(table['phot_g_mean_mag']-5.*np.log10(100./table['parallax']))
    limiting_distance = 10.**(0.2*(-Mv+limiting_mag)-2.)
    print('Limiting mag=',limiting_mag,'mag')
    print('Median absolute mag=',Mv,'mag')
    print('Limiting distance=',limiting_distance,'kpc')
Limiting mag= 16.3 mag
Median absolute mag= 4.2873335323882 mag
Limiting distance= 2.5265813933891805 kpc
```

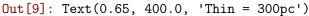


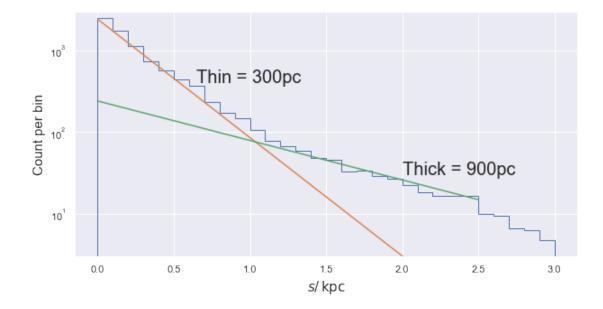
We have taken a sample in a cone. As such, there is a larger volume over which we observe distant stars than the volume over which we observe nearby stars. To compute the density with Galactic height we require a Jacobian factor. we denote distance s and parallax ω .

```
n(s) = s^2 \rho(s)
so \rho(s) = \omega^2 n(1/\omega).
```

We have overplotted the classical thin/thick disc scaleheight exponentials. Note how beyond s = 2.5 kpc incompleteness is an issue.

```
plt.ylabel(r'Count per bin')
plt.annotate('Thick = 900pc', xy=(2.,.3*scaling),fontsize=20)
plt.annotate('Thin = 300pc', xy=(.65,4.*scaling),fontsize=20)
```





We have confirmed the Gilmore-Reid result for the thin-thick vertical structure of the disc (not quite as we were looking at the North Galactic Pole). The original result used photometric distances so it is not trivial to reproduce this result. Other things to do would be

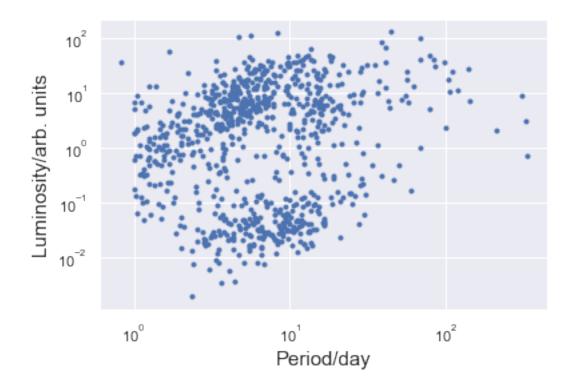
- 1. Look at different samples (other main sequence cuts, giants, etc. -- see Bovy 2017 TGAS paper),
- 2. Look away from North Pole (can we map the full density field in parallaxes? -- reproducing Juric et al. 2008 but over whole sky)
- 3. Look at perturbations relative to the smooth model (see Bennett and Bovy, 2018).

1.1 Joining with other tables

In addition to data in the Gaia DR2 source table, we might require additional data. Here we will grab results from the variability catalogue.

```
plt.plot(table3['period'],table3['lum'],'.')
plt.semilogy()
plt.semilogx()
plt.xlabel('Period/day')
plt.ylabel('Luminosity/arb. units');
```

Query finished.



1.2 Computing aggregate quantities

avg

We can also compute aggregate quantities. Here we compute the mean, standard deviation (implemented specifically for the Gaia TAP+ service) and count for stars within 0.1 deg of the NGP.

count_all

stddev

We can also compute averages binned by another column.

```
In [12]: from astroquery.gaia import Gaia
        job = Gaia.launch_job_async(
            """select aug(bp_rp) as mean_bprp, aug(pmra) as meanpmra, """
            """stddev(pmra) as std_pmra, count(*), round(bp_rp*5) as bin """
            """from qaiadr2.qaia_source """
            """where 1=CONTAINS(POINT('ICRS', ra, dec), CIRCLE('ICRS', 192.85947789, 27.12825241, 0.
            """group by bin order by bin"""
        table3 = job.get_results();
        print(table3)
Query finished.
    mean_bprp
              meanpmra std_pmra count_all bin
0.2925529479980469 0.9967250993514118
                                                             1 1.0
0.39504661560058596 -1.0437391618924852 1.3985565936889
                                                             5 2.0
0.6297840118408203 -9.720657922224543 13.901853618271293
                                                             5 3.0
                                                          11 4.0
0.8187069459394976 -5.403940264957905 9.735770728648967
                                                            7 5.0
1.0233988080705916 -4.155133222253669 8.532296573983963
                                                             3 6.0
1.2054602305094402 -17.024689929693437 3.9024275474255505
1.4590363502502441 -12.840884089086014 16.691582183256596
                                                            4 7.0
                                                             7 8.0
1.6041273389543806 -5.568259282869979 7.946967494249695
                                                            2 9.0
1.8112707138061523 4.0610378898025985 7.313314913581323
1.9614383697509765 -14.223314508195571 17.11847421314836
                                                             5 10.0
 2.191007614135742 4.63094220935661 4.932914063852677
                                                             2 11.0
2.4071226119995117 -11.468381741555222 7.447031720971797
                                                             2 12.0
 2.539379119873047 6.870534525327603 6.545338752799496
                                                             2 13.0
 2.749445915222168 5.748151886686594 5.572400805195707
                                                             2 14.0
```

1.3 Using Vizier

We can also use the TAP Vizier service. This is useful for cross-matching to other catalogues. Although, there are many cross-matches available in the Gaia arcive anyway.

10 --

-- -14.871813449918099

```
Port: 80
SSL Port: 443
Retrieving tables...
Parsing tables...
```

We have to find the name of the Gaia DR2 table in the Vizier database.

We now cross-match to LAMOST find Gaia stars within 1 arcsec (1/3600=0.00027777) of each LAMOST star.

Query finished.

designation			ra	ra_error	 ${\tt AssocData}$	FileName
			deg	mas		
${\tt Gaia}$	DR2	3452892198312193152	93.94713989337	0.2115	 fits	fits
Gaia	DR2	3452892198312193152	93.94713989337	0.2115	 fits	fits
Gaia	DR2	3452892335751157504	93.90288808031	0.0323	 fits	fits
Gaia	DR2	3452892438830368896	93.90882703471	0.0753	 fits	fits
Gaia	DR2	3452892507549841920	93.9066007639	0.0324	 fits	fits
Gaia	DR2	3452892679348521344	93.9447211398	0.056	 fits	fits
Gaia	DR2	3452892679348521344	93.9447211398	0.056	 fits	fits
Gaia	DR2	3452892778131053568	93.96622552691	0.039	 fits	fits
Gaia	DR2	3452892954226422784	93.93449688216	0.0272	 fits	fits
Gaia	DR2	3452893087375393536	93.95917993182	0.0243	 fits	fits

```
deg
                       deg
          float64
                     float64
 int32
-----
220504047 93.947134 93.94713989337
265104047 93.947134 93.94713989337
204804024 93.902888 93.90288808031
185904047 93.90881 93.90882703471
385304047 93.90658 93.9066007639
165104047 93.944752 93.9447211398
177304047 93.944756 93.9447211398
204804047 93.96622 93.96622552691
204904030 93.934479 93.93449688216
177304038 93.959324 93.95917993182
```

1.4 Gaia RVS selection function

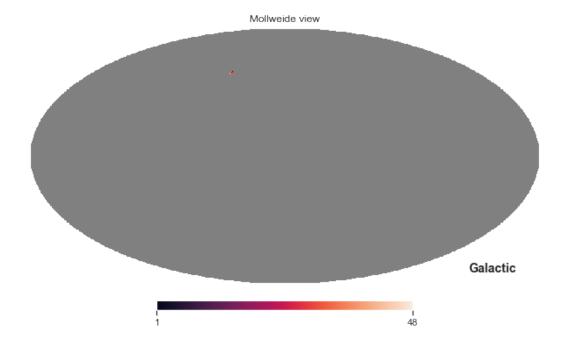
12.0 12.5

One other unique function provided in the Gaia archive is gaia_healpix_index which gives the healpix number of each Gaia source. Healpix are a method of dividing up the sphere into equal area pixels. This is useful as we can bin the catalogue by Healpix. In the following we count all sources in bins of G and healpix for a small region on the sky.

```
In [27]: from astroquery.gaia import Gaia
         job = Gaia.launch_job_async(
              """select qaia_healpix_index(8, source_id) AS hpx8, count(*), round(phot_g_mean_mag
              """from gaiadr2.gaia_source """
              """where 1=CONTAINS(POINT('ICRS', ra, dec), CIRCLE('ICRS', 50, 50, 1.)) """
              """ and phot_g_mean_mag>6. and phot_g_mean_mag<17. """
              """group by hpx8, G order by G"""
         )
         table3 = job.get_results();
         table3['gbin']=np.digitize(table3['g'],np.arange(6.,17.,0.5))
         print(np.unique(table3['g']))
Query finished.
g
7.0
 7.5
8.0
8.5
9.0
9.5
10.0
10.5
11.0
11.5
```

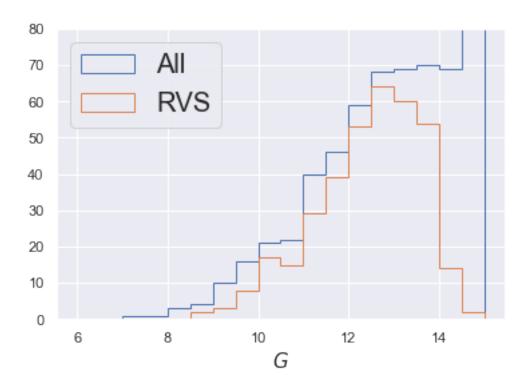
```
13.0
13.5
14.0
14.5
15.0
15.5
16.0
16.5
17.0
```

We plot with healpy.

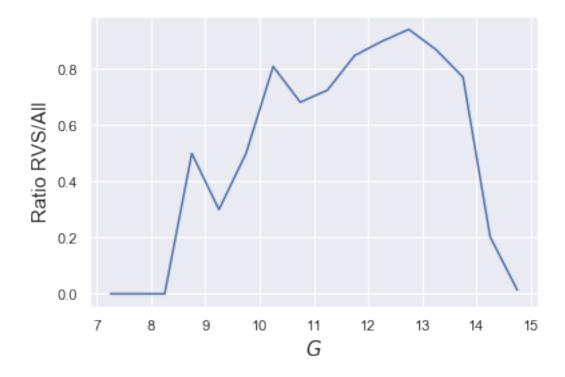


We perform the same calculation for those stars with radial velocities.

Plotting the ratio we see the approx. selection function of the RVS in this part of the sky. Approx. complete up to G=13 mag.



```
Out[41]: Text(0, 0.5, 'Ratio RVS/All')
```



2 Other methods

2.1 Reading downloaded VOT

Go to Gaia Archive (https://gea.esac.esa.int/archive/), query database, download vot (or other formats) and read in with astropy

2.2 Use TOPCAT

Download http://www.star.bris.ac.uk/~mbt/topcat/, query TAP services, etc.

Tutorial2

January 29, 2019

1 Tutorial 2: Coordinates and orbits

```
In [1]: import numpy as np
    import matplotlib.pyplot as plt
    import seaborn as sns
    from astropy.table import Table
    import urllib.request
    from astropy.coordinates import SkyCoord, Galactocentric
    import astropy.units as u

%matplotlib inline
```

In this tutorial we will look at the orbits of the Milky Way dwarf spheroidal galaxies. Many of these had their proper motions robustly measured for the first time (Helmi et al. 2018, Simon 2018, Fritz et al. 2018, Massari et al. 2018). This illustrates conversion from observed coordinates (equatorial coordinates, proper motions, distances and radial velocities) to more physical coordinates with respect to the Galaxy. We will also use galpy's orbit functionality.

I have combined the Gaia proper motion measurements (from Fritz et al. 2018) with the Mc-Connachie (2010) dwarf spheroidal galaxy catalogue (containing distances and radial velocities). It is available here: https://www.ast.cam.ac.uk/~jls/data/dwarf_spheroidal_data.fits . The table contains on-sky equatorial coordinates, distances (computed from distance moduli), radial velocities and proper motions. We have not provided uncertainties but in general these are significant.

satellite	ra	 pmra	pmdec
	deg	 mas / yr	mas / yr
Aqu II	338.4813	 -0.252	0.011
Boo I	210.025	 -0.553999999999999	-1.111
Boo II	209.5	 -2.68600000000000004	-0.53
Boo III	209.3	 nan	nan
CanVen I	202.01458333333333	 -0.159	-0.067
CanVen II	194.29166666666663	 -0.342	-0.473

```
Car I 100.40291666666668 ...
                                                0.485
                                                                     0.132
   Car II
                                                1.867 0.0819999999999999
                    114.1066 ...
  Car III
                    114.6298 ... 3.0460000000000000
                                                                     1.565
 ComBer I 186.7458333333333 ...
                                                0.471
                                                                    -1.716
                         . . . . . . .
                                                                       . . .
   Sgr I
                   283.83125 ...
                                               -2.736
                                                                    -1.357
   Sgr II
                   298.16875 ...
                                                  nan
                                                                       nan
   Tri II
                     33.3225 ...
                                                0.588 0.5539999999999999
   Tuc II 342.9795833333333 ...
                                                0.916
                                                                   -1.169
  Tuc III
                      359.15 ...
                                               -0.117 -1.700999999999998
   Tuc IV
                        0.73 ...
                                                  nan
                                                                      nan
 U Maj I
                      158.72 ... -0.682999999999999
                                                                     -0.72
                     132.875 ... 1.690999999999998
 U Maj II
                                                                    -1.903
 U Min I 227.28541666666663 ...
                                           -0.184 0.0819999999999999
                    162.3375 ...
                                               0.199
    Wil 1
                                                                    -1.342
Length = 43 \text{ rows}
```

1.0.1 Galactocentric coordinates

We use astropy coordinates to find the Galactocentric positions and velocities. First, we initialize a SkyCoord object. We can then transform to any frame (here Galactocentric). Note that the output coordinates come complete with a description of the assumed solar position and velocity.

1.0.2 Orbits

We now integrate orbits using galpy. We can either initialized the orbits using the SkyCoord objects.

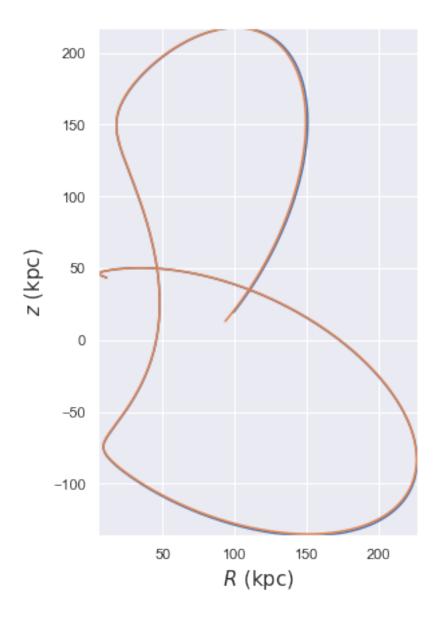
```
/Users/jls/anaconda/envs/saas_fee_py/lib/python3.7/site-packages/astropy/coordinates/baseframe.p 'favor of `representation_type`', AstropyDeprecationWarning)
```

Or we can explicitly compute the required galpy quantities (with units) and then initialize explicitly. These differ slightly in their assumed solar position and velocity.

We integrate both sets of orbits forwards for 10 Gyr in the MWPotential2014

We can inspect the individual orbits (e.g. Coma Berenices). Note the very small difference between the two orbits due to the two different conventions.

ComBer I



Now we plot all orbits in 3d.

```
In [9]: fig = plt.figure(figsize=[15.,15.])
    ax = fig.add_subplot(111, projection='3d')

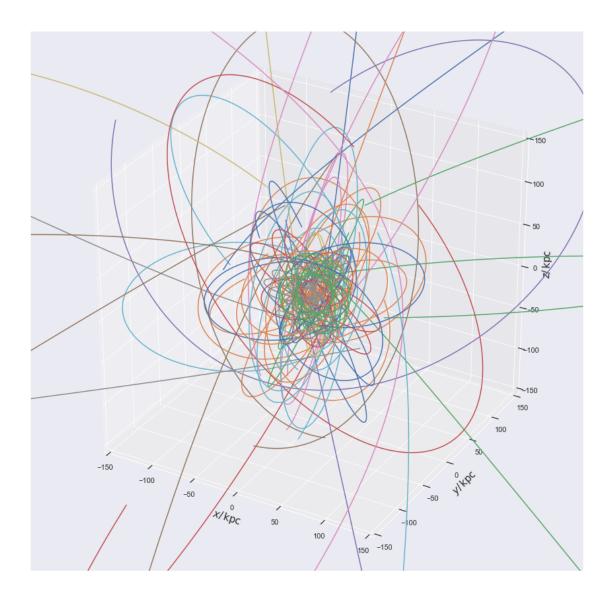
for ii in range(len(orbits)):
    orbits[ii].plot3d(overplot=True)

ax.set_xlim(-150.,150.)
ax.set_ylim(-150.,150.)
ax.set_zlim(-150.,150.)
ax.set_zlabel(r'$x/\,\mathrm{kpc}$')
```

```
ax.set_ylabel(r'$y/\,\mathrm{kpc}$')
ax.set_zlabel(r'$z/\,\mathrm{kpc}$');
```

/Users/jls/anaconda/envs/saas_fee_py/lib/python3.7/site-packages/numpy/core/_methods.py:32: Runt return umr_minimum(a, axis, None, out, keepdims, initial)

/Users/jls/anaconda/envs/saas_fee_py/lib/python3.7/site-packages/numpy/core/_methods.py:28: Runt return umr_maximum(a, axis, None, out, keepdims, initial)

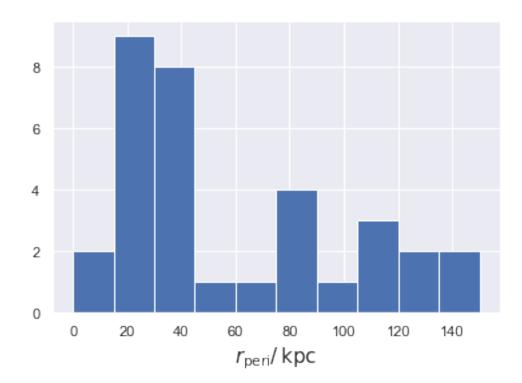


We can also inspect properties of the ensemble. Like the distribution of pericentric distances.

/Users/jls/anaconda/envs/saas_fee_py/lib/python3.7/site-packages/numpy/core/fromnumeric.py:83: R return ufunc.reduce(obj, axis, dtype, out, **passkwargs)

/Users/jls/anaconda/envs/saas_fee_py/lib/python3.7/site-packages/numpy/lib/histograms.py:754: Ru keep = (tmp_a >= first_edge)

/Users/jls/anaconda/envs/saas_fee_py/lib/python3.7/site-packages/numpy/lib/histograms.py:755: Ru keep &= (tmp_a <= last_edge)



We have inspected the orbits of the dwarf spheroidal galaxies in the Milky Way. The next things to do would be to look at:

- 1. Varying the potential
- 2. Calculating the uncertainties (Monte Carlo sampling)
- 3. Inspecting distributions of orbital quantities and their correlations (see Fritz et al. 2018, Helmi et al. 2018).

Tutorial3

January 29, 2019

1 Tutorial 3: Actions, angles and frequencies

```
In [1]: import numpy as np
    import matplotlib.pyplot as plt
    import seaborn as sns
    import pandas as pd
    from astropy.table import Table
    from astropy.coordinates import SkyCoord, Distance, Galactocentric
    import astropy.units as u
    from galpy.potential import MWPotential2014
    from galpy.actionAngle import actionAngleStaeckel
    from galpy.orbit import Orbit

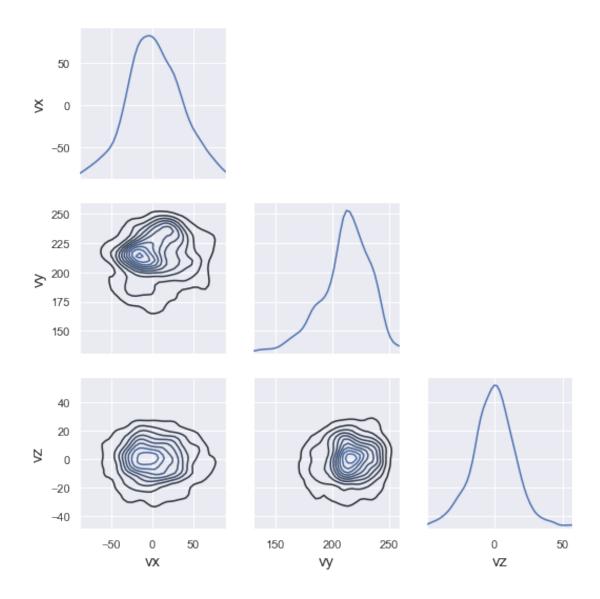
import warnings
    warnings.filterwarnings('ignore')
%matplotlib inline
```

In this tutorial we will demonstrate how to compute action, angle and frequency coordinates using the Gaia RVS sample. We begin by grabbing data via TAP. Here we limit ourselves to the first 1000 stars with radial velocities and proper motions and within 200 pc.

As in Tutorial 2, we construct SkyCoord objects. The difference here is we can construct a Distance object from parallaxes. In theory, the measured parallax could be negative (we have restricted ourselves to positive parallax), in which case we set allow_negative=True to propagate negative parallaxes through the calculation -- they get NaN distances.

```
In [3]: # allow_negative means the distance=nan if parallax<0</pre>
        s = SkyCoord(ra=table['ra'],dec=table['dec'],
                     distance=Distance(
                         parallax=table['parallax'].data.data*u.mas,
                         allow_negative=True),
                     pm_ra_cosdec=table['pmra'],pm_dec=table['pmdec'],
                     radial_velocity=table['radial_velocity'])
        galcen = s.transform_to(Galactocentric)
In [4]: def pair_plot(data):
            g = sns.PairGrid(data, diag_sharey=False)
            g.map_lower(sns.kdeplot)
            g.map_diag(sns.kdeplot)
            for i, j in zip(*np.triu_indices_from(g.axes, 1)):
                g.axes[i, j].set_visible(False)
            for i, j in zip(*np.tril_indices_from(g.axes, 1)):
                g.axes[i,i].set_ylim(*np.percentile(data.values[:,i],[1.,99.]))
                g.axes[i,i].set_xlim(*np.percentile(data.values[:,j],[1.,99.]))
            for i in range(np.shape(g.axes)[0]):
                g.axes[i,i].set_xlim(*np.percentile(data.values[:,i],[1.,99.]))
```

In velocity space we see the characteristic structures. In particular, in vx against vy we see the Hyades, Hercules and Sirius very clearly.

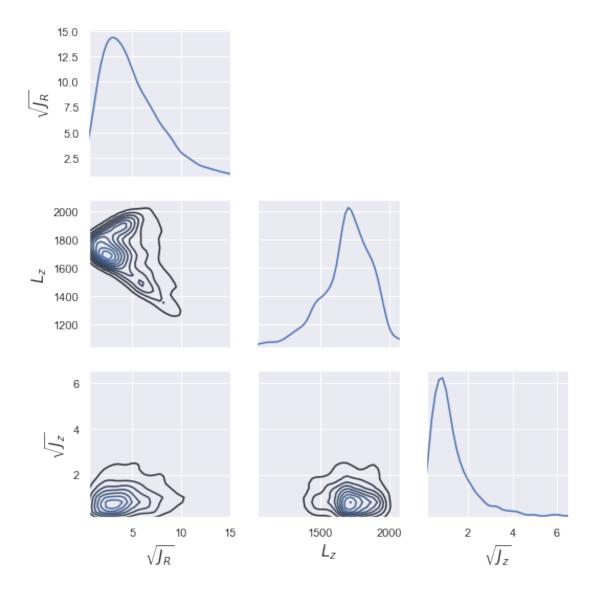


1.0.1 Action, angles and frequencies

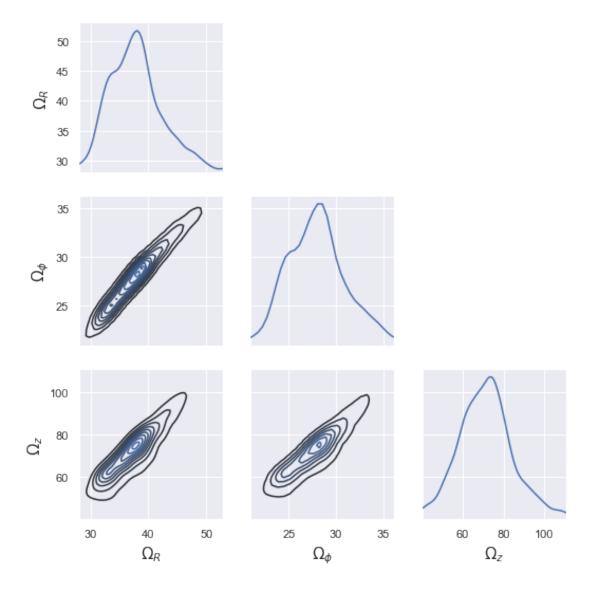
We now use the action-angle estimation routines in galpy. The standard method is the 'Staeckel fudge' which integrates the equations for the actions using those for a Staeckel potential. We use the MWPotential2014 from galpy. A choice of a parameter Δ is required for the method. We can use the SkyCoord object in the Orbit class so the coordinate transformations are handled internally. galpy outputs the actions and frequencies in its internal coordinates where distances in units of 8 kpc and velocities 220 km/s so we scale to physical.

```
In [7]: o = Orbit(s)
        jj = aAS.actionsFreqsAngles(o.R()*u.kpc,
                                    o.vR()*u.km/u.s,
                                    o.vT()*u.km/u.s,
                                    o.z()*u.kpc,
                                    o.vz()*u.km/u.s,
                                    o.phi()*u.rad)
        actions = np.array(jj[:3])*action_unit
        frequencies = np.array(jj[3:6])*freq_unit
        angles = np.array(jj[6:])*u.rad
        angles[1] = angles[1] - 2.*np.pi*u.rad*(angles[1] > np.pi*u.rad)
        # Convenient to work with sqrt(J_R) and sqrt(J_z)
        sqrt_actions = np.array([np.sqrt(actions[0]),actions[1],np.sqrt(actions[2])])
In [8]: actions[:,0], frequencies[:,0], angles[:,0]
Out[8]: (<Quantity [7.33880794e+00, 1.84714611e+03, 4.11417501e-02] km kpc / s>,
         <Quantity [34.4022353 , 25.72916766, 67.73227455] km / (kpc s)>,
         <Quantity [5.81893182, 0.04455854, 3.63249353] rad>)
```

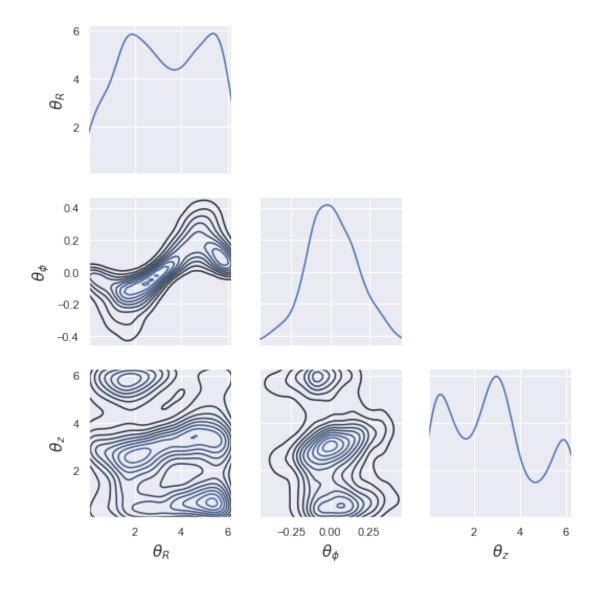
Inspecting the pair plots for these quantities we see the familiar features -- spurs due to the moving groups, edges due to the selection volume.



In [10]: pair_plot(pd.DataFrame(frequencies.T, ${\tt columns=[r'\$\backslash Omega_R\$',r'\$\backslash Omega_phi\$',r'\$\backslash Omega_z\$']))}$



In [11]: pair_plot(pd.DataFrame(angles.T, $columns = [r'$\theta_R^', r'$\theta_phi^', r'$\theta_z^']))$



We have seen how to compute action, angle and frequency coordinates. There are several things we can do next.

- 1. Propagate uncertainties through the calculation.
- 2. Attempt to find clumps in the action space.
- 3. Look at how these distributions change with Galactic location.

See Trick et al. (2018).

Tutorial4

January 29, 2019

1 Tutorial 4: Dissecting local chemo-kinematic structure

```
In [1]: import numpy as np
    import matplotlib.pyplot as plt
    import seaborn as sns
    import pandas as pd
    import glob
    from astropy.table import Table, hstack, vstack
    from astropy.coordinates import SkyCoord, Distance, Galactocentric
    import astropy.units as u
    import warnings
    warnings.filterwarnings('ignore')
//page 2. **Matplotlib**

// Matplotlib**
// Ma
```

In this tutorial we will complement the Gaia data with other spectroscopic data. This demonstrates the crucial function of cross-matching large catalogues.

Gaia does not provide any metallicity or abundance information. In order to understand the chemo-kinematic structure of the Galaxy we must complement with results from other spectroscopic surveys. Here we will use GALAH as it has observations of many nearby bright stars. This uses the pre-downloaded data tables (available on USB sticks, by downloading from

```
http://cdn.gea.esac.esa.int/Gaia/gdr2/gaia_source_with_rv/csv/and
https://www.ast.cam.ac.uk/~jls/data/galah_dr2.fits
or
https://datacentral.org.au/teamdata/GALAH/public/
```

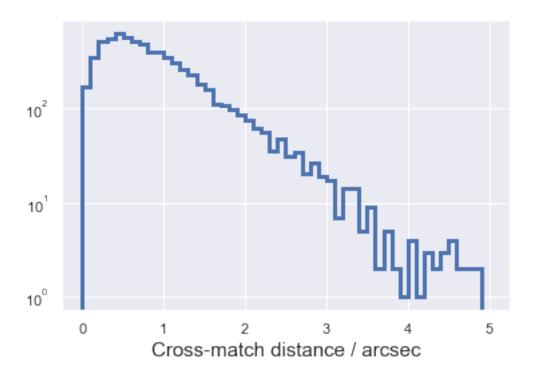
). Note that as GALAH provides radial velocities we could cross-match to the entire Gaia catalogue and only use Gaia proper motions and parallaxes.

```
gaia_rvs = vstack([read_gaia_rvs(f) for f in glob.glob('GaiaSource_*.csv')])
galah = Table.read('galah_dr2.fits')
```

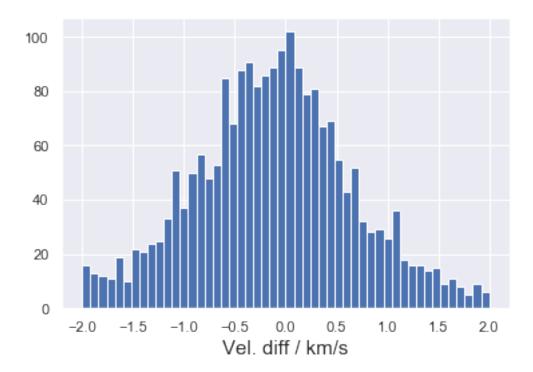
Here we find the entries in the Gaia RVS table that correspond to entries in the GALAH DR2 table. This will find the entry that is closest in $(\Delta \alpha \cos \delta, \Delta \delta)$.

We join the tables and then only keep entries where the cross-match distance was less than 3 arcsec.

Out[4]: Text(0.5, 0, 'Cross-match distance / arcsec')

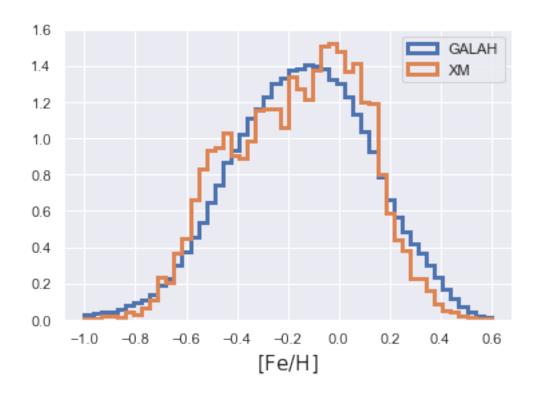


We can compare the radial velocities from Gaia and GALAH. Pretty good.



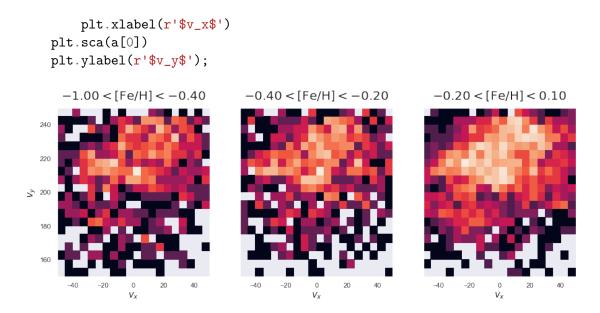
The cross-match metallicity distribution is similar to all of GALAH.

Out[6]: <matplotlib.legend.Legend at 0x1a1df6ff98>



1.1 Velocity distributions split by metallicity

```
In [7]: # allow_negative means the distance=nan if parallax<0
        s = SkyCoord(ra=gaia_xm['ra']*u.deg,dec=gaia_xm['dec']*u.deg,
                     distance=Distance(
                         parallax=gaia_xm['parallax'].data.data*u.mas,
                         allow_negative=True),
                     pm_ra_cosdec=gaia_xm['pmra']*u.mas/u.yr,
                     pm_dec=gaia_xm['pmdec']*u.mas/u.yr,
                     radial_velocity=gaia_xm['radial_velocity']*u.km/u.s)
        galcen = s.transform_to(Galactocentric)
In [8]: f,a=plt.subplots(1,3,figsize=[15.,5.],sharey=True)
        feh\_range = [-1., -0.4, -0.2, 0.1]
        from matplotlib.colors import LogNorm
        for f in range(len(feh_range)-1):
            plt.sca(a[f])
            fltr = (gaia_xm['fe_h']>feh_range[f])&(gaia_xm['fe_h']<feh_range[f+1])</pre>
            plt.hist2d(galcen.v_x.value[fltr],galcen.v_y.value[fltr], bins=20,
                      range=[[-50,50],[150.,250.]],norm=LogNorm(),normed=True)
            plt.annotate(r'$%0.2f<[\mathrm{Fe}/\mathrm{H}]<%0.2f$'\
                         %(feh_range[f],feh_range[f+1]),
                        xy=(0.5,1.05),xycoords='axes fraction',
                         ha='center',fontsize=20)
```



The Hercules is definitely more visible in the metal-rich bin.

We have demonstrated how to cross-match catalogues. This is necessary if we want to use Gaia with any chemical abundance information. We have used this to inspect the local velocity structure separated by metallicity.

Things to do next:

- 1. Subdivide based on other abundances
- 2. Inspect action, angle, frequency diagrams split by abundance
- 3. Investigate vertical distributions (Gaia spiral)

See Bland-Hawthorn et al. (2018)

Tutorial5

January 29, 2019

1 Tutorial 5: Generalized Oort constants

```
In [1]: import numpy as np
    import matplotlib.pyplot as plt
    import seaborn as sns
    import pandas as pd
    from astropy.table import Table, vstack
    import glob
    from astropy.coordinates import SkyCoord, Galactic
    import astropy.units as u
    from scipy.optimize import minimize
    import emcee
    import corner

import warnings
    warnings.filterwarnings('ignore')

%matplotlib inline
```

In this tutorial, we look at fitting models probabilistically to data. We demonstrate how to use emcee (https://emcee.readthedocs.io) -- an MCMC sampling package. We will use a simple example from the lectures of measuring the Generalized Oort constants (Lecture 4, Slides 25 onwards). In theory, this problem could be analysed using simple linear least-squares. However, that method has a tendency to underestimate uncertainties and for more complex models MCMC is necessary.

The Oort Constants are related to the averaged proper motions μ and radial velocities $v_{||}$ across the sky like

$$\bar{v}_{||}\omega = (K + C\cos 2\ell + A\sin 2\ell)\cos^{2}b \\
-\omega(u\cos \ell\cos b + v\sin \ell\cos b + w\sin b), \\
\bar{\mu}_{\ell} = (B + A\cos 2\ell - C\sin 2\ell)\cos^{2}b \\
-\omega(u\sin \ell + v\cos \ell), \\
\bar{\mu}_{b} = -(K + C\cos 2\ell + A\sin 2\ell)\sin b\cos b \\
+\omega(u\cos \ell\sin b + v\sin \ell\sin b - w\cos b).$$
(1)

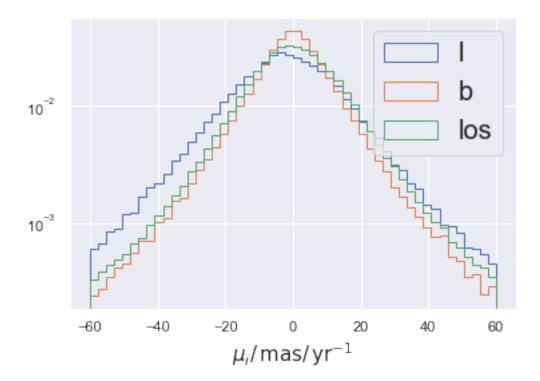
 ω is the parallax, (u, v, w) is the solar peculiar motion, (K, A, B, C) the Oort constants (Here we have ignored the constant 4.74 that relates proper motions to velocities $v = 4.74 \mu/\omega$.

We will use the Gaia RVS sample again, restricting ourselves to nearby main sequence stars.

We transform to Galactic coordinates -- in particular we require the proper motions in Galactic coordinates. We also complement the catalogue with a 'line-of-sight proper motion' i.e.

$$\mu_{\rm los} = \frac{v_{\rm los}\omega}{4.74}$$

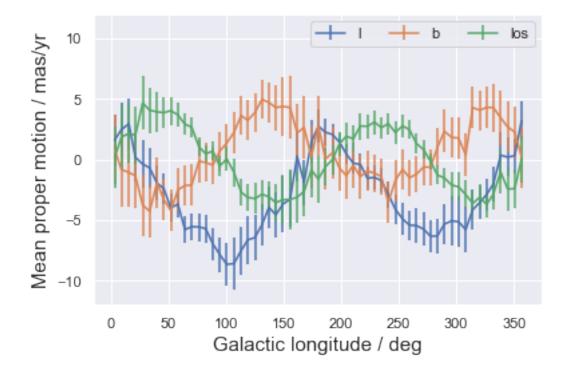
First, we correct the proper motions for the solar peculiar motion (we use Schoenrich et al. 2010) using the parallaxes.



We include a further geometric factor in b that relates the velocities and distances to in-plane velocities and distances. Dividing by this factor gives us the mean quantities related to e.g. $K + C \cos 2\ell + A \sin 2\ell$.

We bin the data in ℓ and compute the mean and standard error in each bin. This neglects uncertainties in the proper motions, which we could subtract off using a median error.

Out[6]: Text(0, 0.5, 'Mean proper motion / mas/yr')



We use a simple model where the likelihood is given by

$$\mathcal{L} = \prod_{i} \mathcal{N}(\bar{\mu}_i | K_1 + K_2 \cos 2\ell_i + K_3 \sin 2\ell_i, \sigma_{\mu,i})$$
 (2)

Here the product is over ℓ bins and the $\mathcal{N}(x,\mu,\sigma)$ is a Gaussian in x centred on μ with width σ . In each ℓ bin we have a measurement of the mean proper motion $\bar{\mu}_i$ with uncertainty $\sigma_{\mu,i}$. We know that the mean should follow one of the 'Oort functions' which in general look like $K_1 + K_2 \cos 2\ell + K_3 \sin 2\ell$ where K_i are different depending on which component we consider. Taking the logarithm we find

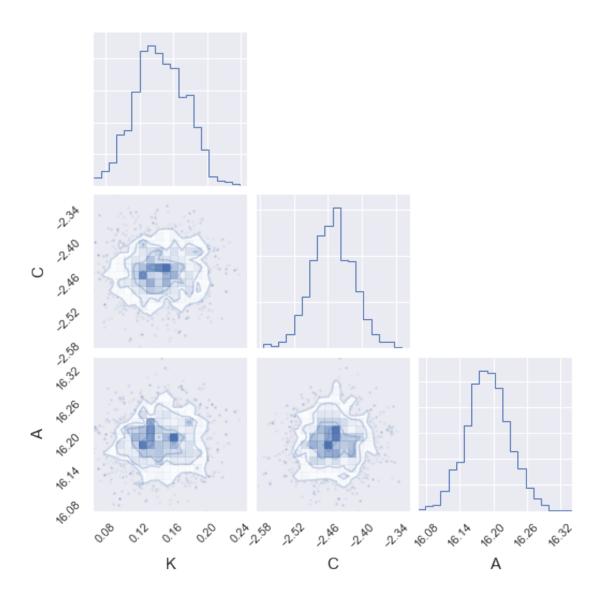
$$\log \mathcal{L} = -\sum_{i} \frac{(\bar{\mu}_{i} - (K_{1} + K_{2}\cos 2\ell_{i} + K_{3}\sin 2\ell_{i}))^{2}}{2\sigma_{\mu,i}^{2}}$$
(3)

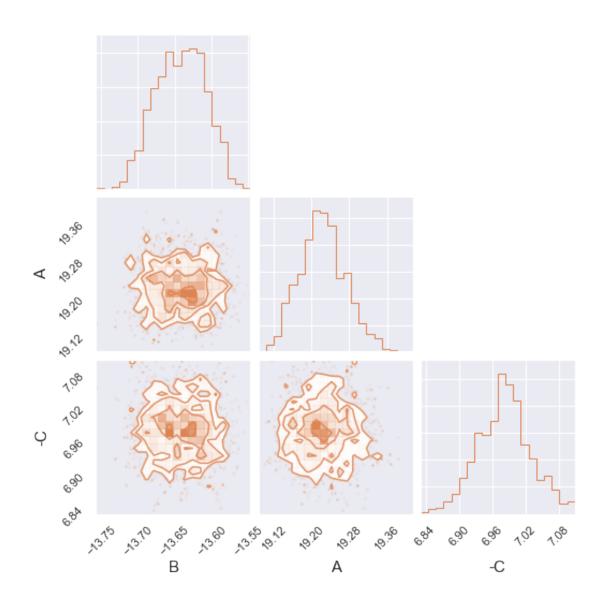
where we have ignored the constant normalization term. We define the log-likelihood function

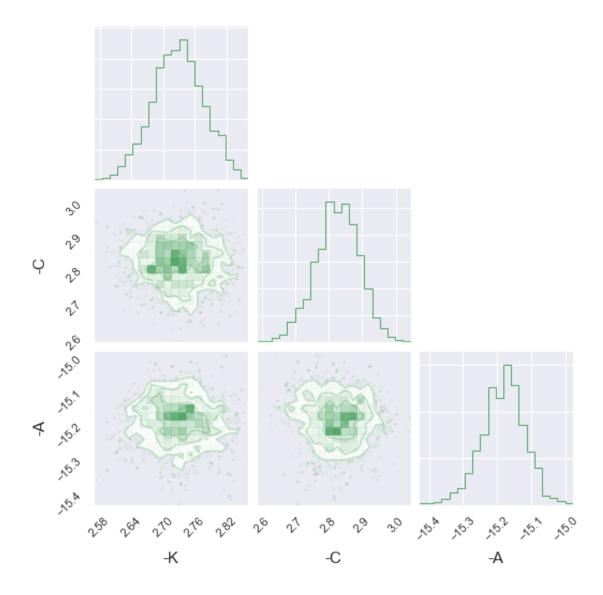
And set up a function to sample. We find an initial guess of the parameters using the minimize function in scipy.optimize.

```
In [8]: def run_sampler(column, nwalkers=50, nsamples=100):
            ''' Run model on column data -- use nwalkers, run nsamples where half are burn-in''
            ndim = 3
            # Set up data
            1 = np.deg2rad(Means['1'])
            data = Means[column+'_rf_g']
            invvar = 1. / Errors[column+'_rf_g']**2
            ## Initialize walkers using the maximum likelihood solution
            optimum = minimize(lambda x: -lnL(x,1,data,invvar),
                               np.array([-12.,15.,3.])/PM_Const.value).x
            print('Minimum found at',optimum*PM_Const.value)
            p0 = np.array([np.random.normal(loc=optimum,
                                            scale=.01*np.ones(ndim),
                                            size=ndim)
                           for i in range(nwalkers)])
            sampler = emcee.EnsembleSampler(nwalkers, ndim, lnL,
                                            args=[1,data,invvar],threads=4)
            sampler.run_mcmc(p0, nsamples)
            return sampler.flatchain[-int(nsamples*nwalkers/2):,:]
```

Run the samples and generate the standard corner plots. Here the constants are in units of proper motion (mas/yr).







We compare the models to the data. We have plotted many samples from the model, although you cannot tell. The formal uncertainty in the parameters is very small.

```
plt.sca(a[0])
plt.annotate(r'$\varpi>2\,\mathrm{mas}, \varpi/\sigma_\varpi>3$'+'\n'
             +r'$0.6<(G_{BP}-G_{RP})<0.7$',
             xy=(0.05,0.),xycoords='axes fraction', fontsize=20,
             ha='left', va='bottom')
for i,K in enumerate(['pmlos','pml','pmb']):
    a[i].errorbar(Means['l'], Means['%s_rf_g'%K], Errors['%s_rf_g'%K],
                  fmt='o',ms=5,color='grey');
plt.sca(a[0])
plot_models(samplesLOS)
plt.ylabel(r'$(v_{||,\max_{gc}})varpi/cos^2b)/\, \max_{mash, yr^{-1}}$')
plt.annotate(r'$(K+A)sin2\ell+C\cos2\ell)$',xy=(0.5,0.95),xycoords='axes fraction',
             fontsize=20,ha='center',va='top')
plt.annotate(r'$K=(\%0.2f\pm\%0.2f),$'\%(np.median(samplesLOS[:,0]*PM_Const.value),
                                       np.std(samplesLOS[:,0]*PM_Const.value))
            +r'$A=(\%0.2f\pm\%0.2f)$'\%(np.median(samplesLOS[:,2]*PM_Const.value),
                                     np.std(samplesLOS[:,2]*PM_Const.value))
             +'\n'+r'$C=(%0.2f\pm%0.2f)$'%(np.median(samplesLOS[:,1]*PM_Const.value),
                                            np.std(samplesLOS[:,1]*PM_Const.value)),
             xy=(0.5,1.02),xycoords='axes fraction',
             fontsize=20,ha='center',va='bottom')
plt.sca(a[1])
plot_models(samplesL)
plt.ylabel(r'$(\mu_{\ell,\mathrm{gc}}/\cos^2b)/\,\mathrm{mas},\yr^{-1}}$')
plt.annotate(r'$(B+A\cos2\ell-C\sin2\ell)$',xy=(0.5,0.95),xycoords='axes fraction',
             fontsize=20,ha='center',va='top')
plt.annotate(r'$B=(\%0.2f)pm\%0.2f), $'\(\(\(\)(np.median(samplesL[:,0]*PM_Const.value)\),
                                       np.std(samplesL[:,0]*PM_Const.value))
            +r'$A=(\%0.2f\pm\%0.2f)$'\%(np.median(samplesL[:,1]*PM_Const.value),
                                     np.std(samplesL[:,1]*PM_Const.value))
             +'\n'+r'$C=(%0.2f\pm%0.2f)$'\%(np.median(-samplesL[:,2]*PM_Const.value),
                                            np.std(samplesL[:,2]*PM_Const.value)),
             xy=(0.5,1.02),xycoords='axes fraction',
             fontsize=20,ha='center',va='bottom')
plt.sca(a[2])
plot_models(samplesB)
plt.ylabel(r'$(\mu_{b,\mathbb{gc}})/(\sin b,\cos b))/\, \athrm{mas}, yr^{-1}}$')
plt.annotate(r'$-(K+A\sin2\ell+C\cos2\ell)$',xy=(0.5,0.05),
             xycoords='axes fraction',fontsize=20,ha='center',va='bottom')
plt.annotate(r'$K=(%0.2f\pm%0.2f),$'%(np.median(-samplesB[:,0]*PM_Const.value),
                                       np.std(-samplesB[:,0]*PM_Const.value))
            +r'$C=(\%0.2f\pm\%0.2f)$'\%(np.median(-samplesB[:,1]*PM_Const.value),
                                     np.std(-samplesB[:,1]*PM_Const.value))
```

```
+'\n'+r'$A=(%0.2f\pm%0.2f)$'%(np.median(-samplesB[:,2]*PM_Const.value),
                                                                                    np.std(-samplesB[:,2]*PM_Const.value)),
                              xy=(0.5,1.02),xycoords='axes fraction',
                              fontsize=20,ha='center',va='bottom')
       for ii in range(3):
              plt.sca(a[ii])
              plt.xlabel(r'Galactic longitude / deg')
              plt.xlim(0.,360.)
              plt.ylim(-10.,10.)
    K = (0.14 \pm 0.03), A = (16.19 \pm 0.04)
                                             B = (-13.64 \pm 0.03), A = (19.22 \pm 0.05) K = (-2.73 \pm 0.05), C = (-2.83 \pm 0.07)
             C = (-2.45 \pm 0.04)
                                                         C = (-6.98 \pm 0.05)
                                                                                                     A = (15.18 \pm 0.06)
            (K + A\sin 2\ell + C\cos 2\ell)
                                                        (B + A\cos 2\ell - C\sin 2\ell)
    7.5
                                                                                       (\mu_{b,gc}/(\sin b \cos b))/\max yr^-
(v_{||, gc} \varpi / \cos^2 b) / \text{ mas yr}^{-1}
    5.0
                                               5.0
                                           (\mu_{\ell, gc}/\cos^2 b)/ mas yr
    2.5
    0.0
                                               0.0
                                               -2.5
                                               -5.0
        \varpi > 2 \text{ mas}, \varpi/\sigma_{\varpi} > 3
                                               -7.5
                                                                                                    -(K + A\sin 2\ell + C\cos 2\ell)
        0.6 < (G_{BP} - G_{RP}) < 0.7
               100 150 200 250
Galactic longitude / deg
```

Galactic longitude / deg

Galactic longitude / deg

Things to do next (e.g. Bovy 2017 with TGAS data):

- 1. Consider the (correlated) uncertainties in the observables.
- 2. Repeat calculation for different stellar populations.