Abschlussarbeit

zur Erlangung des akademischen Grades

Bachelor of Science (B.Sc.) Psychologie

Assessing Publication Bias in Meta-Analyses: A Simulation-Based Estimation Approach Focusing on the Joint Distribution of Effect Size and Sample Size

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vorgelegt von

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- Cooper et al (1019): Only through the formal modes, however, can scientists achieve their true goal, which is recognition for claims of new knowledge in a cumulative enterprise.
- Science perceived as a cumulative enterprise -> overarching goal of robust knowledge about phenoma (Kitcher, 1993), maybe don´t include
- Research often study the same phenomena -> idea of meta-analysis: generalizing and synthesising findings from individual studies contributes the the cumulative advancement of knowledge
- Schmidt (1997): very important look into -> meta-analysis as a driver to foster cumulative science
- Premise hinges on important assumption: available/published scientific literature is representative for all conduceted research (Rothstein et al., 2005; Song et al., 2010)
- Contrary to this, scientists have pointed out for over half a century that results of published studies differ systematically from unpublished studies (Bakan, 1966; Bozarth & Roberts, 1972; Smart, 1964; Sterling, 1959)
- Introduction of publication bias -> publication of a study often hinges of the strength or direction of its findings (Dickersin, 1990; Dickersin & Min, 1993)
- Especially in currently still present publishing culrture that prioritizes novelty and positive results (Nosek et al., 2012) –> many statistically non-significant studies end up in the "file-drawer" and never get published (Rosenthal, 1979)

- Ramifications of publication bias are severe, culminating in
  - meta-analytical effect sizes (Franco et al., 2014; Stanley et al., 2021)
  - heightened false-positive rate/risk (Ioannidis, 2005; Kicinski, 2014; Munafò & Flint, 2010)
  - increasing the risk of erroneous conclusions that may jeopardize the validity of research (Begg, 1994)
  - publication bias especially a major concern in the context of meta-analyses which are widely aknowledged as paramount method for objectively appraising and synthesizing evidence across diverse fields (Rothstein et al., 2005)
- These ramifications become especially relevant in the light of recent large-scale

replication projects providing evidence for non-replicability of many psychological findings (Camerer et al., 2018; Ebersole et al., 2016, 2020; Klein et al., 2014, 2018; Open Science Collaboration, 2015)

- This underscores why publication bias identified as a major threat to replicable science (Munafò et al., 2017) and thus a considered as a significant contributor to the replication crisis (Renkewitz & Keiner, 2019).
- Given the myriad of issues associated with publication bias and its widespread impact, there has been considerable attention directed towards investigating methodologies to detect publication bias. (it is not unsurprising that … significant attention for methods to detect publication bias and correct…)

- In general overwhelming amount of statistical procedures developed over the passed decades
- Many methods rely on the relationship betweem effect size and sample size small study effects explain the idea of small study effects shortly
- Effect size and sample size (or other measures of sampling bias such as SE) used for publication bias assessment
- Idea of small study-effects N-ES als Beispiel PET-PEESE, Egger´s Regression, Begg´s Rank correlation, etc. N-ES correlation exemplarisch hervorheben (und deren Probleme)
- Only indirect assessment of publication bias methods in small-study effects
- Publication bias selection methods Möglicherweise nochmal ein Abstecher zu Publication Selection Models (für Einführung des Publicationsbiasparameters?)
  (Carter et al., 2019; Renkewitz & Keiner, 2019; Van Aert et al., 2019)

Thema Flexibilität: - SPEEC Methode unterscheidet sich drastisch durch Simulationsbasierte Schätzmethodik große Flexibilität - Important point framework within which specific assumptions can be changed regarding marginal distributions e.g. - Explicit statement of assumption of the publication bias model in the generative publication bias model

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- Overwhelming amount of methods but, problems:

  - Heterogeneity
  - Disagreement between methods
- Often the assumption of homogeneity of effect sizes for publication bias detection methods

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Research questions:

- How does publication bias influence the joint probability distribution of effect size and sample size?
- How can the magnitude of publication bias in meta-analyses be estimated and effect sizes under publication bias be corrected from the joint distribution of sample size and effect size?

The Present Study

The present study introduces SPEEC (**S**imulation-based **P**ublication bias **E**stimation and **E**ffect size **C**orrection), a novel simulation-based framework to assess the extent of publication bias in meta-analyses and estimate corrected effect sizes in the presence of publication bias based on the joint distribution of effect size and sample size. The thesis sets out with two primary objectives. Firstly, it aims to introduce the reader to the SPEEC method and provide a comphrensive description of its assumptions and its procedure. Secondly, it aims to assess the SPEEC method in a proof of concept using empirical meta-analytical data sourced from Linden and Hönekopp (2021) to preliminary assess the initial feasability of the introduced approach. For this purpose, four theoretically justifiable hypotheses involving predictions about the estimated parameters of the SPEEC method that should apply to the empirical data are derived in the section Hypotheses. The thesis is structured as follows: In this section, a brief primer on the central ideas of the SPEEC method is provided, followed by a detailed derivation of the hypotheses. Next, a detailed introduction to the SPEEC method itself is offered. This is followed by the empirical analyses of the hypotheses and a discussion and evaluation of the results of the empirical analyses.

Brief Introduction to SPEEC

The central idea of SPEEC is to explicitely model the generative process of publication bias in a simulation framework and iteratively compare how the simulated

distribution of effect size and sample size diverges from the actual empirical meta-analytical data. The publication bias model of the simulation framwork integrates both assumption of the marginal distribution of effect size and sample size as well as how publication bias influences the joint distribution of both. Regarding the former, the sample sizes modeled by Negative-Binomial distribution and effect sizes by Gaussian distribution, where the mean parameter is corrected meta-analytical estimate under publication bias. For the latter, the extent of publication bias is modeled by a publication bias parameter ω_{PBS} that captures the probability of a statistically non-significant simulated study being selected (i.e., published) relative to a significant study being selected. From this generative publication bias model, theoretical studies are simulated (effect size and sample size). Next compare the estimated kernel density distributions of simulated data from generative model to empirical meta-analytical data to quantify the statistical divergence between the the data of the model and the empirical data. This framework can be regarded as an optimization problem, with the goal of parameter values for the distributional parameters and publication bias parameter of the generative model such that the statistical divergence from the empirical data is minimized. Iterative algorithmic optimization can be used (differential evolution) of distributional parameters and publication bias parameter to minimize the loss function to estimate parameters.

Confirmatory Hypotheses

To assess the SPEEC method, a set of four theoretical predictions are derived, that constitute the hypotheses of this study. These hypotheses serve as benchmarks for assessing the viability of the proposed method and are therefore expected to hold true if the approach works in principle. If the predictions fail to be corroborated by the empirical meta-analytical data, this would raise concerns about the viability of the SPEEC method and necessitate a further review of its implementation.

Firstly, we conducted a direct comparison between the correlation of effect size and sample size, serving as an indicator of publication bias, and the publication bias parameter ω_{PBS} estimated within the SPEEC method. It can be expected that the estimated publication bias parameter $\hat{\omega}_{\text{PBS}}$ is positively associated with the Fisher z-transformed Spearman correlation coefficients of the association between unsigned effect size and sample size in each meta-analysis. In other words, when the proposed method

estimates high publication bias (i.e., low probabilities for $\hat{\omega}_{\text{PBS}}$) it is expected that the correlation coefficients for each meta-analysis to be more negative and conversely. In statistical terms, this implies that the regression coefficient $\beta_{z_{r_s}}$ is expected to be greater than zero.

$$\begin{aligned} \mathcal{H}_0^{\text{i}} &: \beta_{z_{r_s}} \leq 0 \\ \mathcal{H}_1^{\text{i}} &: \beta_{z_{r_s}} > 0 \end{aligned} \tag{1}$$

In cases where substantial publication bias is present within the scientific literature of a particular research phenomenon, and the true effect size is precisely zero ($\delta = 0$), the distribution of effect size and sample size exhibits increased symmetric sparsity around zero in areas where individual studies would not be statistically significant for a given effect size and sample size (Light & Pillemer, 1984). This is explained by the fact that only studies with either large positive or large negative effects will be statistically significant and consequently have a higher likelihood of being published in the presence of publication bias. Because of this symmetry for a true effect size of zero, the average effect size $\hat{\delta}$ should not be biased since negative and positive effects should, in theory, mutually cancel each other out. Consequently, the difference Δ_{μ_d} between the average effect size $\hat{\delta}$ and the estimated mean parameter μ_d of the effect size distribution from the SPEEC approach should remain invariant independent of the magnitude of publication bias. However, when the true effect size exceeds zero ($\delta > 0$), publication bias leads to an overestimation of the true effect (i.e. $\hat{\delta} > \delta$), and conversely, overestimation in the opposite direction (i.e., $\hat{\delta} < \delta$) when $\delta < 0$. If the estimated mean parameter $\hat{\mu}_d$ of the Gaussian effect size distribution obtained from the *SPEEC* approach is a more accurate estimate of the true effect size δ in the presence of publication bias compared to the mean effect size $\hat{\delta}$, it follows from the prior reasoning that a curvilinear, inverted U-shaped pattern can be expected between the difference δ_{μ_d} of these two parameters and the publication bias parameter ω_{PBS}. In other words, when the mean difference Δ_{μ_d} is approaching zero, publication bias severity is expected to decrease (indicated by larger values for ω_{PBS}). Conversely, when the difference Δ_{μ_d} diverges from zero in both negative and positive directions, publication bias severity is expected to increase (i.e. lower values for ω_{PBS}). In statistical terms, for the second hypothesis of this study $\mathcal{H}^{\text{i}}$, the quadratic regression term $\beta_{\Delta_{\mu_d}}$ is expected to be smaller than zero.

$$\begin{aligned} \mathcal{H}_0^{\text{i}} : &\quad \beta_{\Delta_{\mu_d}} \geq 0 \\ \mathcal{H}_1^{\text{i}} : &\quad \beta_{\Delta_{\mu_d}} < 0 \end{aligned} \tag{2}$$

Registered reports are an alternative two-stage publishing model, where study protocols are submitted, peer-reviewed and in-princple accepted prior to data collection (Chambers & Tzavella, 2022; Nosek & Lakens, 2014). In-princple accepted studies are then published regardless of the outcome of the study, because the decision to publish was made before the results of the studies are known, which eliminates publication bias (Chambers & Tzavella, 2022; Simons et al., 2014). Consequently, the effect sizes within these multisite replication projects and registered replication reports that are publishied within this framework cannot be biased by publication bias. Following this reasoning, in the third hypothesis of the present study $\mathcal{H}^{\text{iii}}$, it can expected that the average effect size of a registered replication report $\hat{\delta}$ to be equivalent to the mean parameter of the Gaussian effect size distribution μ_d that is estimated using the SPEEC approach within specified equivalence bounds $\Delta_{EQ} = \{\Delta_L,\ \Delta_U\}$. The equivalence bounds are defined by the smallest effect size of interest for this study (Lakens et al., 2018) and are set to $\Delta_{EQ} = \{-0.18, 0.18\}$ (see section Smallest Effect Size of Interest for the rationale of this decision).

$$\begin{gathered} \Delta_{\mu_d} = \hat{\delta} - \hat{\mu}_d \\ \mathcal{H}_{01}^{\text{iii}} : \Delta_{\mu_d} \leq \Delta_L \quad \cap \quad \mathcal{H}_{02}^{\text{iii}} : \Delta_{\mu_d} \geq \Delta_U \\ \mathcal{H}_1^{\text{iii}} : \Delta_L > \Delta_{\mu_d} > \Delta_U \end{gathered} \tag{3}$$

In theory, one could posit that the publication bias parameter ω_{PBS} in registered replication reports should precicely equal one, as individual replication studies are almost always predetermined in the registration of the study and included in the final report independent of their statistical outcomes. However, due to the inherent upper limits of one for the publication bias parameter ω_{PBS}, testing this point prediction would not be sensible within a null hypothesis testing framework. Instead, a relative comparison between traditional meta-analyses and registered replication reports allows for making testable predictions. More specifically, it can be expected that the publication bias parameter ω_{PBS} is greater for multisite replication studies in comparison to traditional meta-analysis. This indicates that relative to individual statistically non-

significant primary studies within traditional meta-analyses, statistically non-significant individual replication studies should have a greater likelihood of being of being included in the the final registered replication report (and thus being published). In statistical terms, when the regressor is a binary indicator of the type of research synthesis with the reference level being the publication biased absent multisite replication studies (MR) and the outcome is the estimated publication bias parameter ω_{PBS}, the regression coefficient β_{MR} can be expected to be greater than zero.

$$\begin{aligned} \mathcal{H}_0^{\text{iv}}: &\quad \beta_{MR} \leq 0 \\ \mathcal{H}_1^{\text{iv}}: &\quad \beta_{MR} > 0 \end{aligned} \tag{4}$$

Method

The SPEEC Method

This section offers a comprehensive description and explanation of the SPEEC framework to assess the extent of publication bias and estimate effect sizes in the presence of publication bias in meta-analyses. The flowchart in Figure 1 provides an overview of the sequentials steps of the SPEEC method. Currently, SPEEC is being developed as an open-source R package and is accessible on GitHub at https://github.com/jlschnatz/speec (alpha version).

Figure 1

Overview of the SPEEC Approach

Note. Test.

Simulation Framework

The initial step in the SPEEC method entails defining the marginal distributions of effect size and sample size for the generative publication bias model. This requires additional assumptions regarding the type of study design from which the simulated effect sizes and sample sizes originate. For the purpose of this study, Cohen´s d is

adopted as a widely used effect sizes measure for mean differences(Lakens, 2013) as the effect size of interest. Consequently, it is assumed that the simulated effect sizes originate from a between-subjects two-sample t-test study design. However, it is worth noting that the SPEEC framework is adaptable to different study designs where alternative effect size measures are typically employed (e.g., correlational effect sizes or effect sizes derived from proportional data). Depending on the effect size, this would require adapting the marginal distribution of the effect size and how statistical significance is determined based on a different test statistic, which is required for the application of publication bias (see Application of Publication Bias).

The marginal distribution for the total sample size n of a study should be inherently modeled as a discrete distribution. Count data of this nature are commonly modeled using either a Poisson or Negative-Binomial distribution. In various psychological domains, sample size distributions often exhibit considerable variance and skewness (see for example Cafri et al., 2010; Marszalek et al., 2011; Sassenberg & Ditrich, 2019; Shen et al., 2011; Szucs & Ioannidis, 2017). Considering this, the Negative-Binomial distribution was chosen as it can model overdispersed better effectively by introducing a second parameter (Ismail & Jemain, 2007; Lloyd-Smith, 2007). The mean-dispersion parametrization of the Negative-Binomial distribution is used where probability of sucess p and the target number of sucesses r are reparametrized to mean $\mu = \frac{r \cdot (1-p)}{p}$ and dispersion $\phi = r$ to model the study-specific total sample sizes n_i.

$$n_1, n_2, \dots, n_k \quad \text{where} \quad N \overset{\text{i.i.d.}}{\sim} \mathcal{NB}(\phi_n, \mu_n) \quad \text{for } i = 1, \dots, k \tag{5}$$

Concerning the marginal distribution of effect size d, it is reasonable to assume a Gaussian distribution with mean μ_d and variance σ_d^2. To account for the increasing precision in estimating the true effect size mean μ_d as the sample size increases (i.e., the sampling error), we compute the variance of the mean differences $\bar{x}_{i1} - \bar{x}_{i2}$, from which the effect sizes are assumed to originate in this type of study design. Subsequently, a normalization factor γ_i can be derived by scaling each individual variance $\sigma^2_{\bar{x}_{i1} - \bar{x}_{i2}}$ with the overall mean of those variances such that that $\bar{\gamma} = 1$.

$$\sigma^2_{\bar{x}_{i1}-\bar{x}_{i2}} = \sigma^2_d / n_i$$
$$\gamma_i = \frac{\sigma^2_{\bar{x}_{i1}-\bar{x}_{i2}}}{\sum_{i=1}^{k} \sigma^2_{\bar{x}_{i1}-\bar{x}_{i2}} / k} \tag{6}$$

With this normalization factor, the total variance of the individual variances of the individual variances is $\mathbb{E}(\gamma_i \cdot \sigma^2_d) = \sigma^2_d$. The study-specific effect sizes d_i are subsequently modeled as

$$d_1,\, d_2,\, \dots,\, d_k \quad \text{where} \quad D \sim \mathcal{N}(\mu_d, \gamma_i \cdot \sigma^2_d) \quad \text{for} \quad i = 1, \dots, k. \tag{7}$$

Using this definition for the marginal distribution of effect size, the SPEEC method assumes a fixed effects meta-analytical model, where the only source of variation in effect size is explained by measurement error. However, it is worth noting that the publication bias simulation model of the SPEEC method could be further extended to account for effect size heterogeneity. This could involve including an additional heterogeneity parameter τ^2 in the simulation framework to account for additional variability bayond sampling error.

Conditional on the marginal distributions, k individual studies are sampled from the joint distribution of effect size and sample size. The selection of k is user-defined, however, the larger the number of samples k, the lower the uncertainty of the joint distribution of effect size and sample size. In general, there is a trade-off between the increased computational cost and the reduced uncertainty of the joint distribution for increasing values of k. We opted for $k = 10^4$ samples for each simulation iteration for the analyses of the hypotheses.

Application of Publication Bias

«!- Nochmal drüber schauen nach Einleitung –>

Following the simulation step of sampling k studies from the joint distribution of effect size and sample size, the subsequent stage involves the application of publication bias to the samples studies. As previously discussed, publication bias is operationalized in terms of the likelihood of a study being published conditional on the statistical significance of its results. Statistical significance in traditional null hypothesis significance testing (NHST) contexts is commonly determined using p-values, employing a dichoto-

mous decision rule with conventional type I erro-rates set as cut-off values (Andrade, 2019; McShane et al., 2019). Translated to this simulation setting, two-tailed p-values for each individual study i can be calculated from the corresponding effect size d_i and sample size n_i. To implement this, it is assumed that the individual studies i originate from a balanced sample size design. That is, when the total sample size n_i is even, the between-subject group sample sizes n_{1i} and n_{2i} are defined as $n_i/2$. Otherwise, when the total sample size n_i is odd, the group sample sizes are determined as the ceilinged $\lceil n_i/2 \rceil$ and floored $\lfloor n_i/2 \rfloor$ values, respectively. Subsequently, the p-value p_i of each simulated study can be derived from its corresponding t-value

$$t_i = \left| \frac{d_i}{\sqrt{1/n_{1i} + 1/n_{2i}}} \right|. \tag{8}$$

$$p_i = 2 \cdot P(t_i \mid df_i) \tag{9}$$

where $P(t_i, df_i)$ is the cumulative t-distribution with degrees of freedom $df_i = n_i - 2$. Given each p-value p_i, publication bias is introduced by assigning each study i a weight

$$\omega_{\text{PBS}_i}(p_i) = \begin{cases} \omega_{\text{PBS}} & \text{for} \quad p_i \geq \alpha \\ 1 & \text{otherwise} \end{cases} \tag{10}$$

with the constraint $\omega_{\text{PBS}} \in \mathbb{R} : 0 \leq \omega_{\text{PBS}} \leq 1$. This weight denotes the probability of a study i being selected conditional on the p-value and the type I error rate α. This definition of the publication bias weight is directly analogue to the step weighting function used in publication bias selection models (see Hedges, 1992; Iyengar & Greenhouse, 1988). If a study i is statistically nonsignificant (i.e., $p_i \geq \alpha$), the publication bias parameter ω_{PBS} is assigned, else the probability of a study being selected is equal to one, indicating no publication bias. Thus, the publication bias parameter ω_{PBS} denotes the probability of the selection of a non-significant study relative to a statistiacally significant study. For instance, a publication bias parameter of $\omega_{\text{PBS}} = 0.5$ would indicate that simulated studies that are non-significant are half as likely to be selected (i.e., published) in comparison to studies that are statistically significant. Importantly, the type I error rate needs to be fixed across all simulated studies and is set to the common significance threshold of $\alpha = 0.05$ for the analyses of the hypotheses. Following

the computation of publication bias weight ω_{PBS_i} for each study i, the probability of a study being selected can be expressed as $\mathbb{P}(S_i = 1) = \omega_{\text{PBS}_i}$. Here, S_i is a binary indicator function, signifying whether an individual study i is selected during the publication bias selection process. Following the computation of the of the publication bias weight ω_{PBS_i} for each study i, the publication bias selection process can be defined in terms of an indicator function.

$$1_\alpha(\omega_{\text{PBS}_i}) = \begin{cases} 0 & \text{if} \quad \omega_{\text{PBS}_i} \geq \alpha \quad \text{study not selected} \\ 1 & \text{if} \quad \omega_{\text{PBS}_i} < \alpha \quad \text{study selected} \end{cases} \tag{11}$$

Using this indictor function, the resulting subsets for the selected (d_i', n_i') and non-selected samples (d_i'', n_i'') from the initial k simulated studies can be defined as

$$\begin{aligned} \{d_i', n_i'\} &= \{d_i, n_i \mid 1_\alpha(\omega_{\text{PBS}_i}) = 1\} \quad \text{for} \quad i = 1, \dots, k' \quad \text{and} \\ \{d_i'', n_i''\} &= \{d_i, n_i \mid 1_\alpha(\omega_{\text{PBS}_i}) = 0\} \quad \text{for} \quad i = 1, \dots, k''. \end{aligned} \tag{12}$$

One challenge in simulating a fixed number of k studies lies in the fact that, ceteris paribus, as the degree of publication bias increases (i.e. for lower values for ω_{PBS}), increasingly fewer studies k' remain after the selection process compared to the original number of simulations k. This would lead to a loss of precision in the parameter estimation for decreasing values of ω_{PBS}. To adress this, the aforementioned steps (from Equation 5 - Equation 12) are repeated a second time with an adjusted number of simulations $k_{\text{adj}} = \lceil k^2/k' \rceil$, thereby ensuring that the number of selected studies k'_{adj} is approximately equal over the entire range of ω_{PBS}.

Formulation as an Optimization Problem

After the simulation of k_{adj} from the publication bias model conditional of the marginal distributional parameters (μ_d, σ_d^2, ϕ_n, μ_n) and the publication bias parameter ω_{PBS} to determine the subset (d_i', n_i') for $i = 1, \dots, i = k'_{\text{adj}}$, the following step involves quantifying how closely the simulated data from the publication bias model aligns with the empirical meta-analytical data. More specifically, this step involves measuring the statistical dissimilarity of the bivariate kernel density estimates between the empirical meta-analytical data and the simulated data of the publication bias model. While various measures of statistical dissimilarity between probability distributions exist (for

an overview, see Cha (2007)), the Kullback-Leibler divergence (KL-divergence, Kullback & Leibler, 1951) was chosen as a dissimlarity measure for SPEEC. This choice was motivated by the KL-divergence's superior performance in capturing dissimilarity between estimated kernel densities compared to alternative measures (total variation distance and earthmover distance) tested for the SPEEC method, particularly across boundary conditions. In addition, the KL divergence has an intuitive interpretation in this context. It can be interpreted as the expected value of the log-likelihood ratio favoring the ture model over a candidate model (Etz, 2018). Here, the estimated joint density of effect size and sample size from the meta-analytical data $\hat{f}_e$ is regarded as the true data generating distribution, and the estimated kernel density from the simulated data $\hat{f}_t$ generated by the publication bias model serves as the approximate candidate distribution.

To implement this step, the *KernSmooth* R package (Wand et al., 2023) was used to estimate the joint kernel density distribution for both empirical data and simulated using a bivariate standard Gaussian kernel that is evaluated on a linearly-binned square grid (Wand, 1994; Wand & Jones, 1994). The grid size was chosen to be $n_{\text{grid}} = 2^7 + 1$ equidistant grid points in each dimension but is user-definable in the *speec* R package. The bandwidth of the kernel function was determined using the reliable plug-in method proposed by Sheather and Jones (1991), but the *speec* R package also offers other common bandwidth selection methods. To ensure the comparability of the estimated kernel densities between the empirical and simulated data, the bounds of the the square grid, $\mathrm{b_n} \times \mathrm{b_d}$, must be identical and are determined from the empirical meta-analytical data.

For defining these bounds, the maximum likelihood values for the parameters of the marginal distribution of effect size $(\hat{\mu}_d, \hat{\sigma}_d^2)$ and sample size $(\hat{\phi}_n, \hat{\mu}_n)$ are estimated. Using these estimates, the quantiles spanning the inner 99 percentile of the cumulative distribution are obtained from the quantile functions $Q_d(p \mid \hat{\mu}_d,\ \hat{\sigma}_d^2)$ and $Q_d(p \mid \hat{\phi}_n,\ \hat{\mu}_n)$, for the percentiles $p_1 = 0.5$ and $p_2 = 99.5$. Subsequently the bounds for the effect size $\mathrm{b_d}$ and sample size $\mathrm{b_n}$ are defined as the minimum and maximum values of these quantiles and the range of the empirical data, respectively.

$$
\begin{aligned}
\mathrm{b_d} &= \{Q_d(p_1 \mid \hat{\mu}_d,\ \hat{\sigma}_d^2) \wedge \min(d),\ Q_d(p_2 \mid \hat{\mu}_d,\ \hat{\sigma}_d^2) \vee \max(d)\} \\
\mathrm{b_n} &= \left\{Q_n(p_1 \mid \hat{\phi}_n,\ \hat{\mu}_n) \wedge \min(n),\ Q_n(p_2 \mid \hat{\phi}_n,\ \hat{\mu}_n) \vee \max(n)\right\}
\end{aligned}
\tag{13}
$$

This ensures that the an adequate range is covered for the kernel density estimation. Finally, the Kullback-Leibler-Divergence is computed from the binned kernel density estimates of the empirical $\hat{f}_e$ and simulated theoretical $\hat{f}_t$ data.

$$D_{\mathrm{KL}}(\hat{f}_e \parallel \hat{f}_t) = \sum_{u=1}^{n_{\mathrm{grid}}} \sum_{v=1}^{n_{\mathrm{grid}}} \hat{f}_e(u,v) \ln \left(\frac{\hat{f}_e(u,v)}{\hat{f}_t(u,v)} \right) \tag{14}$$

Parameter Optimization with Differential Evolution

Summarizing the previous sections, the simulation framework within the publication bias model of SPEEC requires the distributional parameters for the marginal distributions of effect size and sample size and the publication bias parameter as input and returns a single scalar value representing the Kullback-Leibler divergence between the estimated joint kernel density of the simulated theoretical data and the empirical meta-analytical data. This framework can be considered as an optimization problem of finding parameter values for such that

$$\begin{gathered} \min_{\mu_d,\ \sigma_d^2,\ \mu_n,\ \phi_n,\ \omega_{PBS}} \Big\{ D_{\mathrm{KL}}(\hat{f}_e \parallel \hat{f}_t) \Big\}, \\ \text{subject to: } \mu_d,\ \sigma_d^2,\ \mu_n,\ \phi_n,\ \omega_{PBS} \in \mathbb{R}, \quad \text{where} \quad 0 \leq \omega_{PBS} \leq 1, \\ -4 \leq \mu_d \leq 4, \quad 0 \leq \sigma_d^2 \leq 6, \quad 10 \leq \mu_n \leq 15000, \quad 0.01 \leq \phi_n \leq 1000. \end{gathered} \tag{15}$$

For this purpose, we use the differential evolution (DE, Storn & Price, 1997), which is a simple algorithm for global optimization (Feoktistov, 2006). DE is an evolutionary metaheuristic based on principles such as as mutation, cross over and selection, and requires only few control parameters that are generally straightforward to select to achieve favorable outcomes in comparison to other optimization algorithms (Storn & Price, 1997). Importantly, all parameters of the DE algorithm including the control parameters, the stopping criterion and boundary constraints of the differential evolution algorithm were defined globally for the parameter estimation of all meta-analyses.

To apply DE for optimization within the SPEEC approach, the R package *RcppDE* (Edelbuettel, 2022) was utilized, which implements the classical DE algorithm DE/rand/1 (Storn & Price, 1997). The control parameters for DE were chosen based on the recommendations of Storn and Price (1997) with additional adjustments informed

by preliminary testing of simulated data from the simulation framework of SPEEC, setting the population size NP to 150, the mutation constant F to 0.9 and the crossover constant CR to 0.1. In the application of the DE algorithm, we adopted a direct termination criteria approach (Ghoreishi et al., 2017; Jain et al., 2001), with the termination condition being the maximum number of generations. Since there are no universally applicable default values for the maximum number of generations, as it is contingent upon the optimization problem at hand (Jain et al., 2001), the choice for $t_{\max}$ was also informed by preliminary testing of the simulation framework of SPEEC. These tests suggested that $t_{\max} = 1000$ is a reasonable decision. In determining the boundaries for the parameter search space (see Equation 15), a balance was made between avoiding boundaries that are too wide, which could lead to inefficient exploration of the search space, and ensuring that the boundaries are not too narrow to ensure sufficient coverage of the potential parameters. More specifically, the minima and maxima for all distributional parameters were determined using Maximum Likelihood (see Table XXX), and the boundaries were set slightly above those values to ensure good coverage.

Secondary Data Description

To examine the confirmatory hypotheses of this study aiming to provide a preliminary assessment of the viability of the SPEEC method, we use secondary data sourced from previous research by Linden and Hönekopp (2021). The dataset can be accessed both from its original source (see https://osf.io/yr3xd/) and through the OSF and GitHub repositories associated with this project (see section Appendix B: Research Transparency Statement). Furthermore, detailed metadata of the dataset and a transparency statement regarding prior knowledge of the data are provided in the preregistration of this study. The dataset is comprehensive and includes both "traditional" meta-analyses and registered replication reports for which publication bias is absent. The dataset encompasses a total of 207 research syntheses covering various psychological phenomena. Within the dataset, there are 150 meta-analyses, each subset consisting of 50 meta-analyses from different subfields of psychology (social psychology, organizational psychology, and cognitive psychology). Additionally, the dataset includes 57 registered replication reports, which are particularly relevant for investigating hypotheses $\mathcal{H}^{\text{iii}}$ and $\mathcal{H}^{\text{iv}}$. For each research synthesis, information on the total sample size n_i and effect size d_i of each primary study was compiled. The meta-analyses were se-

lected using random sampling, with predefined inclusion criteria and specified journals from which the data were selected. One important inclusion criterion by Linden and Hönekopp (2021) was that effects must be reported as standardized mean differences (Cohen´s d or Hedges´ g) or as correlations (Pearson´s r or Fisher´s z). In cases where a different effect size measure than Cohen's d was used, effect sizes were transformed accordingly (Linden & Hönekopp, 2021).

Statistical Analysis

The confiromatory statistical analyses were preregistered and were performed using the R programming language (version 4.4.0 Puppy Cup, R Core Team, 2023). Any supplementary analyses not preregistered are explicitly labeled as such. All data and analysis scripts are made available for this thesis (see section Appendix B: Research Transparency Statement)

Regarding the hypotheses, in which the publication bias parameter ω_{PBS} was the dependent variable ($\mathcal{H}^{\text{i}}$, $\mathcal{H}^{\text{ii}}$, $\mathcal{H}^{\text{iv}}$), beta regression as implemented in the *betareg* package (Zeileis et al., 2021) was used to analyse the data. This choice was motivated by the restriction of the parameter space for the publication bias to the standard unit interval, whereby non-normality, skewness and heteroscedasticity can anticipated (Cribari-Neto & Zeileis, 2010; Smithson & Verkuilen, 2006). Beta regression is recognized for its adaptability in handling such deviations. Because the optimization approach permits $\hat{\omega}_{\text{PBS}}$ values within the range $0 \leq \hat{\omega}_{\text{PBS}} \leq 1$ in principle, and the beta-regression model assumes that $0 < \hat{\omega}_{\text{PBS}} < 1$, a common transformation proposed by Smithson and Verkuilen (2006) was employed. This transfoormation, denoted as $\omega'_{\text{PBS}} = \frac{\omega_{\text{PBS}} \cdot (n-1)+0.5}{n}$, subtly adjusts the bounds to sligthly narrow the range between zero and one. We used a logit link for the mean parameter μ and a identity link for the dispersion paramater that was fixed such that the beta regression model can be described as

$$\begin{aligned} \omega_{\text{PBS}'_i} &\sim \mathcal{B}(\mu_i, \phi) \\ \log\left(\frac{\mu_i}{1-\mu_i}\right) &= x_i^\top \beta. \end{aligned} \tag{16}$$

The independent variables for these three hypotheses were as follows: regarding $\mathcal{H}^{\text{i}}$, the independent variable was the Fisher z-transformed correlation coefficient

of the correlation between effect size and sample size, where the transformation is defined as $z_r = \tanh^{-1}(r)$. The independent variable for $\mathcal{H}^{\text{ii}}$, was the difference $\Delta_{\widehat{\mu}_d}$ between the average effect size estimate of each meta-analysis and the mean parameter of the Gaussian effect size distribution estimated with SPEEC. Lastly, the independent variable for $\mathcal{H}^{\text{iv}}$, was a binary indicator specifying the research synthesis type (traditional meta-analysis or registered replication report), with registered replication reports set as the reference level for regression. The coefficients from the beta-regressions for these hypotheses were estimated using Maximum Likelihood estimation with the BFGS optimizer.

Hypothesis $\mathcal{H}^{\text{iii}}$ was aimed at comparing the estimated means of the Gaussian effect size distribution to the average effect sizes. This comparison aimed to assess whether the presence of effects in mean differences $\Delta_{\widehat{\mu}_d}$ deemed large enough to be considered meaningful, according to specified equivalence bounds Δ_{EQ}, can be rejected (Lakens et al., 2020). For this, we conducted an equivalence test using the Two One-Sided Tests procedure (Schuirmann, 1987) as implemented in the *TOSTER* R package (Lakens & Caldwell, 2023). We employed Welch´s two-sample *t*-tests for dependent samples with corrected degrees of freedom as the Welch's *t*-test generally offers better control of type I error rates when the samples are heteroscedastic, while maintaining robustness compared to Student's *t*-test when test assumptions are satisfied (Delacre et al., 2017). Furthermore, the choice of a dependent samples test was necessitated by the dependence between the pairs of samples originating from the same underlying data. The equivalence bounds Δ_{EQ} against which the data was tested were defined by the smallest effect size of interest.

Smallest Effect Size of Interest

For all four hypotheses, the smallest effect size of interest (SESOI) are established based on effect sizes that can be reliably detected, considering the constraints imposed by the sample size resources available for this secondary data analysis (Lakens, 2014; Lakens et al., 2018). More specifically, three simulation-based ($\mathcal{H}^{\text{i}}$, $\mathcal{H}^{\text{ii}}$, $\mathcal{H}^{\text{iv}}$) and one analytical ($\mathcal{H}^{\text{iii}}$)sensitivity power analysis were conducted to determine which effect sizes we have at least 80 percent power ($1 - \beta = 0.8$) to detect, taking into account the predetermined sample size and fixed type I error rate $\alpha = .05$ (details see Appendix A: Power Analyses determining the SESOIs). We specified the SESOI for $\mathcal{H}^{\text{iii}}$ in raw units

and all other SESOIs in odds ratios. The SESOI for the equivalence hypothesis defines the equivalence bounds for the TOST procedure ($\Delta_{EQ} = (-0.17, 0.17)$). Table XXX summarises all four SESOIs of the hypotheses.

Table 1

Smallest Effect Sizes of Interest of the Hypotheses

Hypothesis	SESOI	Unit
$\mathcal{H}_1$	1.28	*OR*
$\mathcal{H}_2$	0.59	*OR*
$\mathcal{H}_3$	0.17	raw unit
$\mathcal{H}_4$	1.28	*OR*

Note. Except for $\mathcal{H}_3$ all SESOIs are defined in terms of odds ratios (OR). The SESOI of $\mathcal{H}_3$ is defined in raw units.

Results

Evaluation the Assumptions for the SESOIs

As an initial step, the assumptions made to determine the Smallest Effect Sizes of Interest (SESOI) for the four hypotheses were assessed. In the simulations-based sensitivity power analyses aimed to determine the SESOIs (see the Appendix for detailed explanations), three dispersion parameter conditions $\phi : \{10, 20, 30\}$ for the distribution of the publication bias parameter ω_{PBS} were simulated. Employing an intercept-only beta regression model with the complete dataset, the estimated dispersion parameter was $\hat{\phi} = 1.56$, 95% CI [1.27, 1.84], $SE = 0.15$, $z = 10.72$, $p < .001$. This finding contradicts our initial assumptions regarding the dispersion parameter's magnitude, rendering the interpretation of SESOIs for our hypotheses untenable. Consequently, it is appropriate to refrain from interpreting SESOIs that were determined from the simulation-based sensitivty power analyses in the subsequent analyses.

Figure 2

Visual Summary of the Results from the Four Hypotheses

Note. **A**. Estimated publication bias parameter vs. Fisher z-transformed correlation coefficients. Fitted line: regression coefficients with 95

Confirmatory Results of the Predictions from the Hypotheses

Regarding hypothesis $\mathcal{H}_1$, panel A of Figure 2 depicts the relationship between estimated publication bias parameter $\widehat{\omega}_{\text{PBS}}$ and the Fisher z-transformed Spearman correlation coefficients z_{r_s} of the effect size sample size correlation in each meta-analysis. The observed slope was sign was positive in the direction of the hypothesis and statistically signifcant $OR = 2.22$, 95% CI [1.38, Inf], $SE = 0.29$, $z = 2.74$, $p = .003$. We reject null hypothesis $\mathcal{H}_0$, that the beta coefficient is $z_{r_s} \leq 0$. Lower values for z_{r_s} were significantly associated with lower publication bias parameter values $\widehat{\omega}_{\text{PBS}}$. Additionally, to enhance the interpretability of the regression slope, we refitted the model with standardized values of z_{r_s} and computed the average marginal effects using the *marginaleffects* package (Arel-Bundock, 2024). On average, for every standard deviation increase in the Fisher z-transformed correlation coefficient, $SD(z_{r_s}) = 0.31$, the model only predicted an increase of 4.35% in the publication bias parameter $\widehat{\omega}_{\text{PBS}}$. In line with this, the general explanative power of the model as determined by the pseudo R^2 (Ferrari & Cribari-Neto, 2004) was low, $R^2 = 0.051$. Thus, only 5.07% of the variance in ω_{PBS} could be explained by the variance of z_{r_s}.

Concerning $\mathcal{H}_2$, panel B of Figure 2 depicts the relationship between estimated publication bias parameter as a function of the difference between the average effect size $\widehat{\delta}$ and the estimated mean parameter of the Gaussian effect size distribution $\widehat{\mu}_d$. The corresponding estimated quadratic slope was negative as indicated by the predicted concave inverse u-shaped line and statistically significant at an α-level of 5\%, $OR =$ 0.04, 95% CI [0.00, 0.73], $SE = 1.84$, $z =$ -1.81, $p = .035$. We again calculated the average marginal effect for improved interpretability. On average, for every standard deviation increase in $\Delta_{\widehat{\mu}_d,\widehat{\delta}}$ ($SD(\Delta_{\widehat{\mu}_d,\widehat{\delta}}) = 0.13$), the model only predicted an increase of -0.09% in the publication bias parameter $\widehat{\omega}_{\text{PBS}}$. The overall explained variation of ω_{PBS} by $\Delta_{\widehat{\mu}_d,\widehat{\delta}}$ was low, $R^2_{\text{pseudo}} = 0.026$.

In relation to hypothesis $\mathcal{H}_3$, panel C of Figure 2 illustrates the mean difference $\Delta_{\widehat{\mu}_d,\widehat{\delta}}$ between the estimated mean parameter of the Gaussian effect size distribution $\widehat{\mu}_d$ and the average effect size $\widehat{\delta}$, along with its corresponding confidence interval. Additionally, the null t-distributions of the Two One-Sided Tests (TOST) against the equivalence bounds $\Delta_{EQ} = (-0.17, 0.17)$ are illustrated. We only report the results of the t-test with the lower t-value in the main results as both tests must be significant to reject

the null hypothesis (Lakens, 2017). Both one-sided paired t-tests were statistically significant, $t(56) = 17.3$, $SE = 0.01$, $p < .001$. This is also indicated by 90% confidence interval lying within the equivalence range in panel C of Figure 2. We additionally conducted an exploratory null hypothesis significance test to test the point hypothesis that the true mean difference of $\Delta_{\widehat{\mu}_d,\hat{\delta}}$ is exactly zero. The mean difference significantly deviated from zero M = -0.02, 90% CI [-0.03, -0.01], $t(56)$ = -2.36, SE = 0.01, p = 0.022. This indicates that, despite the significant null hypothesis significance test, the difference was too small to be considered meaningful according to the equivalence range $\Delta_{EQ} = (-0.17, 0.17)$ of the equivalence test.

Finally, regarding hypothesis $\mathcal{H}_4$, panel D of Figure 2 illustrates the comparison between the estimated publication bias parameters for typical meta-analysis in comparison to multisite replication studies / registered reports. Already descriptively, contrary to our expectation that the estimated puhblication bias parameters for multisite replication studies (MR) would be greater (i.e., lower publication bias) than for regular meta-analysis (MA), the mean of the estimated publication bias values ω_{PBS} of the regular meta-analysis subset is greater than the mean of the multisite replication subset ($M_{\text{MA}} = 0.82$; $M_{\text{MR}} = 0.79$). In line with this, slope of the beta regression was non-significant, OR = 0.81, 95% CI [0.61, Inf], SE = 0.18, z = -1.17, p p = .879, as also indicated by the overlappping confidence interval of the predicted marginal means in panel D. Once more, we computed the average marginal effect to examine how the estimated publication bias parameter $\hat{\omega}_{\text{PBS}}$ changes with the discrete shift from the reference level (multisite replication studies / registered reports) to typical meta-analysis, as predicted by the regression model, reveiling a change of -3.93% in the opposing direction of the hypothesis.

Diagnostic Evaluation of Parameter Estimation in SPEEC

As this study relies on empirical data to preliminarily assess the proposed SPEEC approach, the true values for the distributional parameters and the publication bias parameter are unknown. However, as discussed previously, publication bias is inherently absent by design in multisite replication studies and registered reports. Thus, the four distributional parameters (μ_d, σ_d^2, μ_n, ϕ_n) within the SPEEC approach cannot be biased due to publication bias (especially the mean and variance of the effect size distribution). Leveraging this fact, we can use a subset of the data encompassing

the multisite replication studies and registered reports for a diagnostic evaluation of the parameter estimation within the SPEEC approach. More specifically, we can derive Maximum Likelihood estimates for the distributional parameters to compare them with the corresponding values estimated by the SPEEC approach, anticipating approximate equivalence between the two approaches. This part was of the analysis was not preregistered and conceived after the confirmatory analyses were conducted. Based on this comparative approach between ML and SPEEC, we formulated five diagnostic questions to assess parameter estimation:

1. To what degree do the estimated distributional parameters differ between SPEEC and MLE?
2. How are the discrepancies in one parameter associated with those in the other distributional parameters across SPEEC and MLE? Specifically, does a consistency exist in the discrepancies between these parameters?
3. Does the discrepancy between SPEEC and MLE estimates of the distributional parameters correlate with the sample size of the multisite replication studies?
4. Is the discrepancy between SPEEC and MLE in the distributional parameters associated with sample size of multisite replication studies k?
5. Is the discrepancy between SPEEC and MLE in the distributional parameters associated with the publication bias parameter ω_{PBS}?

The Maximum Likelihood estimates for the distributional parameters were obtained using the Nelder-Mead optimization algorithm (Nelder & Mead, 1965). Additionally, the mean and median discrepancy between SPEEC and MLE were calculated to descriptively to assess the average difference between the two estimation methods.

Figure 3

Scatter Plot comparing the estimated Distributional Parameters via SPEEC and Maximum Likelihood

Note. **A1**. Comparison of estimated mean parameter μ_d from Gaussian effect size distribution. **A2**. Comparison of estimated variance parameter σ_d^2 of Gaussian effect size distribution. Axes and colorbar are log (base 10) transformed. **B1**. Comparison of mean parameter μ_n of Negative-Binomial sample size distribution **B2**. Comparison of dispersion parameter ϕ_n of Negative-Binomial sample size distribution. Axes and colorbar are log (base 10) transformed.

Regarding question one, Figure 3 provides a visual summary of the analysis comparing the distributional parameters estimated by the SPEEC method against those estimated by Maximum Likelihood Estimation (MLE). The diagonal line signifies perfect alignment between MLE and SPEEC estimates. Values below the diagonal indicate higher values for MLE compared to SPEEC, while values above the diagonal indicate the opposite.

Panel A of figure XX reiterates the findings of the analysis of $\mathcal{H}_3$, suggesting a small discrepancy between the two methods in estimating the mean of the Gaussian effect size distribution, $M(\Delta_{\mu_d})$ = -0.03, $Mdn(\Delta_{\mu_d})$ = -0.02. This discrepancy can be deemed practically negligible according to the equivalence test of $\mathcal{H}_3$. However, the other panels indicate contrasting outcomes.Panel B reveils a systematic discepancy in the estimation of the variance parameter of the Gaussien effect size distribution between SPEEC and MLE, $M(\Delta_{\sigma_d^2})$ = 0.59, $Mdn(\Delta_{\sigma_d^2})$ = 0.11. Descriptively, this suggests that on average, the variance was estimated to be greater in the SPEEC approach compared to MLE. Furthermore, this discrepancy increases in exponential trend and displays substantial heteroscedasticity with rising variance estimates from the MLE approach. Similarly, Panel C also illustrates a systematic overestimation of the mean

parameter of the Negative-Binomial sample size distribution by SPEEC in comparison to MLE ($M(\Delta_{\mu_n}) = 46.96$, $Mdn(\Delta_{\mu_n}) = 3.52$), which again increases in an exponential trend with higher mean parameter estimates from MLE. Lastly, Panel D shows that the SPEEC approach generally understimates dispersion parameter of the sample size distribution in comparison to the ML estimate ($M(\Delta_{\phi_n})$ = -2.02, $Mdn(\Delta_{\phi_n})$ = -0.19) and also furthermore indicates a systematic relationship in the discrepancy between the two approaches.

Table 2

Pairwise Pearson Correlations between the Absolute Difference of the Distributional Parameters from SPEEC and ML, Publication Bias Parameter and Meta-Analysis Size

Variable	ω_{PBS}	$\lvert\Delta_{\mu_d}\rvert$	$\lvert\Delta_{\sigma_d^2}\rvert$	$\lvert\Delta_{\phi_n}\rvert$	$\lvert\Delta_{\mu_n}\rvert$
ω_{PBS}					
$\lvert\Delta_{\mu_d}\rvert$	-0.44*** [-0.61, -0.23]				
$\lvert\Delta_{\sigma_d^2}\rvert$	-0.37** [-0.56, -0.14]	0.67*** [0.54, 0.76]			
$\lvert\Delta_{\phi_n}\rvert$	0.08 [-0.18, 0.33]	-0.06 [-0.31, 0.2]	-0.05 [-0.3, 0.21]		
$\lvert\Delta_{\mu_n}\rvert$	0.03 [-0.23, 0.29]	0.15 [-0.11, 0.39]	0.04 [-0.22, 0.3]	-0.05 [-0.3, 0.21]	
k	-0.14 [-0.38, 0.12]	0.04 [-0.22, 0.29]	0.15 [-0.11, 0.39]	-0.17 [-0.41, 0.09]	0 [-0.26, 0.26]

Note. Computed p-values are corrected for multiple comparison using the correction by Benjamini & Hochberg (1995). $|\Delta|$ is the absolute difference for each distributional parameter between SPEEC and MLE.

* Significance *** $p < .001$; ** $p < .01$; * $p < .05$

To address the remaining diagnostic questions, we conducted a pairwise correlational analysis between the absolute differences of the parameter estimates derived from the two estimation methods, alongside the publication bias parameter $\hat{\omega}_{\text{PBS}}$ and the total number of primary replication studies k within each multisite replication project or registered report. We used the Pearson correlation coefficient and corrected the obtained p-values for multiple comparisons to control the false discovery rate (Benjamini & Hochberg, 1995).

Regarding the parameters of the Gaussian effect size distribution, a strong positive correlation was observed between the absolute difference in the mean parameter estimates and the variance parameter estimates obtained from ML and SPEEC. This indicates that as the absolute discrepancy between SPEEC and ML increased for the mean parameter μ_d, the absolute discrepancy also increased for the variance parameter σ_d^2 of the effect size distribution. Furthermore, strong negative correlations were found

between the publication bias parameter ω_{PBS} and the discrepancy between ML and SPEEC estimates of the mean and variance parameters of the effect size distribution. More specifically, as the absolute discrepancy between both estimation methods increased for both the mean ($|\Delta_{\mu_d}|$) and variance ($|\Delta_{\sigma_d^2}|$), the publication bias parameter ω_{PBS} decreased, signifying more severe predicted publication bias. Notably, the total number of of primary replications k was not significantly associated to the divergence of ML and SPEEC of any distributional parameter or the publication bias parameter ω_{PBS}.

Discussion

- Analysis four theoretical predictions that should hold true, if the approach works in principle -> or phrased oppositely, if we don´t find evidence for the hypotheses -> there are problems

  Confirmatory findings::

- Out of the four hypotheses, we found evidence for three predictions (speaking statistically) -> H1, H2, H3
- No evidence that publication bias parameter is greater (less severe publication bias) in registered replication reports in comparison to traditional meta-analyses -> concerning result -> motivated the additional exploratory diagnostic analyses to assess potential problems of the parameter optimization

  Exploratory findings::

  Q1:

- There are differences between the the ML and SPEEC estimates -> for variance of effect size distribution, and mean and dispersion parameter of sample size distribution
- These differences are not unsystematic across the entire range of the distributional parameters estimated via ML but rather show systematic trends (e.g.,)
- Proof of concept study -> not an comprehensive assessement of SPEEC appraoch
- Possibility of including:
  - Heterogeneity parameter τ^2 -> this could be very valuable
  - Different effect size and thus different marginal distributions (thats the flexible aspect of SPEEC) -> odds ratio (log odds ratio), R2 variance
  - Sample size planning parameter -> publiction bias not the only thing affecting n-es distribution

“‘

- We did not find working approach for parameter optimization of the study -> this should/could be the focus of future studies
- Framework has several areas which could be responsible for optimization problems
  - The choice of grid size
- Need for larger simulations study
  - Systematically vary: heterogeneity, true effect size, publication bias severity,

meta-analysis study size k

  - But also the control parameters of the SPEEC approach could be varied to see if systematic misestimation lies within here
  - For example: grid size choice for KDE has direct influece on the the loss function (KL-divergence) for the optimization -> fine grid size for low sample size studies could be problematic (because of too much uncertainty), while very coarse grid size could be also problematic (because then differences between regarding publication bias parameter cannot be captured anymore)
- Flexibility of SPEEC approach (extending SPEEC):
  - Possibility to include heterogeneity parameter (deviations from the true effect size not only due to sampling error but)
  - Possibility to include other influences on the sample size distribution -> sample size planning
  - Possibility to use other marginal distribution for sample size distribution (depending on the data)

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Appendix

Appendix A: Power Analyses determining the SESOIs

The simulated-based sensitivity power analysis targeted a statistical power of $1-\beta = 0.8$ with a fixed significance level of $\alpha = .05$. The simulated samples sizes were specified according to the hypotheses as follows:

- $\mathcal{H}_1$: $n = 150$ (only traditional meta-analyses)
- $\mathcal{H}_2$ and $\mathcal{H}_4$: $n = 207$ (both traditional meta-analyses and multisite replication studies)
- $\mathcal{H}_3$: $n = 57$ (only multisite replication studies)

The distributional assumptions for the four sensitivity power analyses were specified as follows:

$$\mathcal{H}_1: \quad z_{r_S} \sim \mathcal{N}(\mu = -0.1, \sigma = 0.5)$$

$$\mathcal{H}_2 \text{ and } \mathcal{H}_3: \quad \Delta_{\mu_d} \sim \mathcal{N}\Big(\mu = 0, \sigma_{diff} = \sqrt{0.3^2 + 0.3^2}\Big)$$

For hypothesis four, the proportions of the categorical predictor of the research synthesis type (traditional meta-analysis MA, multisite replication MR) were chosen according the the actual proportions of the data ($n_{MA} = 150, n_{MR} = 57$). For all simulations-based sensitivity power analyses ($\mathcal{H}_1, \mathcal{H}_2, \mathcal{H}_4$), the number of simulations was set to $n_{iter} = 5000$. More over, the the beta-regressions on ω_{PBS} in $\mathcal{H}_1$, $\mathcal{H}_2$, and $\mathcal{H}_4$ involved simulations for different dispersion parameter conditions $\phi = \{10, 20, 30\}$, as lower dispersion parameters result in reduced test power. We set the SESOI for the parameters of interest more conservatively, ensuring a minimum power of 80% for the lowest dispersion parameter $\phi = 10$.

Figure 4

Power Curves of the Sensitivity Power Analyses determining the SESOIs

Note. OR: Odds ratio. Ribbons around the lines represent the 95

Appendix B: Research Transparency Statement

The present thesis project was aimed to to be as transparent and reproducible as possible. The preregistration of the study, all data, code, and supplementary files needed to reproduce the results of this study are openly available on the zugehörigen OSF repository of this thesis (https://osf.io/87m9k/?view_only=030c8d1c46474270b5886c4dfc491a78) and on GitHub.To enhance the reproducability of this project, all analyses, figures, the thesis manuscript itself are generated within a containerized software environment using *Docker* (Merkel, 2014). The workflow for the analyses was explicitely management using *Snakemake* (Mölder et al., 2021) and the R packages dependencies and version management used for the statistical analyses were managemed using *renv* (Ushey & Wickham, 2024). The thesis manuscript itself is dynamically generated and reproducible using the *Quarto* publishing system.

- The project is fully st containerized using *Docker* (Merkel, 2014)

- Software and operating system virtualization, fully containerized project using Docker R package dependencies and version management using *renv* (Ushey & Wickham, 2024).
- Data analysis workflow management tool *Snakemake* (Mölder et al., 2021)
- thesis is written using the *Quarto* (Allaire et al., 2024) open-source scientific and technical publishing system

CITE: All analyses, figures, and the final manuscript were generated using a makefile, bash scripts, and R and Rmarkdown. All relevant metadata, as well as analysis and manuscript code, are available on GitHub: https://github.com/ZimmermanLab/SF-metrosideros-endophytes/ and archived at Zenodo (https://doi.org/10.5281/zenodo.8075450). The complete computational environment for the analyses is documented in a Dockerfile based on rocker containers (Boettiger, 2014) and a renv.lock (Ushey, 2021) file in that same repository.

Appendix C: Deviations of Preregistration

Appendix D: Test

Table 3

Estimated Parameters for the Distribution of Effect Size and Sample Size from each Meta-Analysis via ML

Parameter	Minimum	Maximum
Effect Size		
$\hat{\mu}_d$	-1.911	2.599
$\hat{\sigma}_d^2$	0.003	4.349
Sample Size		
$\hat{\phi}_n$	0.042	176.620
$\hat{\mu}_n$	17.365	1438.443

Note. Maximum Likelihood Estimation using the Nelder-Mead optimizer.

Appendix E: Regression Tables of Confirmatory Analyses

Table 4

Beta Regression Results for $\mathcal{H}_1$

Term	Estimate	CI (95%)	SE	z	p
Mean model component: μ					
Intercept	4.05^a	[3.16, 5.19]	0.13	11.07	$< .001$
z_{r_s}	2.22^a	$[1.38, Inf]^c$	0.29	2.74	.003
Precision model component: ϕ					
Intercept	5.84^b	[3.95, 8.63]	0.20	8.85	$< .001$

Note. LL = 132.03, MAE = 0.21, AIC = -258.06, BIC = -249.03, R^2 = 0.051

[a] OR

[b] Identity

[c] One-sided Confidence interval in direction of the hypothesis

Table 5

Beta Regression Results for $\mathcal{H}_2$

Term	Estimate	CI (95%)	SE	z	p
Mean model component: μ					
Intercept	3.30^a	[2.71, 4.03]	0.10	11.79	$< .001$
$\Delta^2_{\mu_d}$	0.04^a	$[0.00, 0.73]^c$	1.84	-1.81	.035
Precision model component: ϕ					
Intercept	4.85^b	[3.63, 6.47]	0.15	10.70	$< .001$

Note. LL = 164.25, MAE = 0.23, AIC = -322.51, BIC = -312.51, R^2 = 0.026

[a] OR

[b] Identity

[c] One-sided Confidence interval in direction of the hypothesis

Table 6

Two One-Sided Tests Result for $\mathcal{H}_3$

Type	t	SE	df	p
NHST	-2.36	0.009	56	.022
TOST $\Delta < \Delta_L$	17.30	0.009	56	$< .001$
TOST $\Delta > \Delta_L$	-22.02	0.009	56	$< .001$

Note. NHST: Null Hypothesis Significance Test, TOST: Two One-Sided Test

Table 7

Beta Regression Results for $\mathcal{H}_4$

Term	Estimate	CI (95%)	SE	z	p
Mean model component: μ					
Intercept	3.30^a	[2.67, 4.08]	0.11	11.07	$< .001$
Research Synthesis Type					
Meta-Analyses					
RRR	0.81^a	$[0.61, Inf]^c$	0.18	-1.17	.879
Precision model component: ϕ					
Intercept	4.79^b	[3.59, 6.38]	0.15	10.71	$< .001$

Note. MR: Multisite Replication; LL = 163.31, MAE = 0.23, AIC = -320.62, BIC = -310.62, R^2 = 0.011

[a] OR

[b] Identity

[c] One-sided Confidence interval in direction of the hypothesis

Eidesstattliche Erklärung

Hiermit versichere ich, dass ich diese Abschlussarbeit selbständig verfasst und keine anderen als die angegebenen Quellen und Hilfsmittel benutzt habe. Alle Stellen der Arbeit, die wortwörtlich oder sinngemäß aus anderen Quellen übernommen wurden, wurden als solche kenntlich gemacht. Die Arbeit hat in gleicher oder ähnlicher Form noch keiner Prüfungsbehörde vorgelegen und ist nicht veröffentlicht. Sie wurde nicht,

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Jan Luca Schnatz

Darmstadt, den r format(Sys.time(), ‘%d. %B %Y’)