SDSS-IV MANGA: THE RADIAL PROFILE OF ENHANCED STAR FORMATION IN CLOSE GALAXY PAIRS

JOSHUA L. STEFFEN¹, HAI FU^{1,2}, J. M. COMERFORD³, Y. SOPHIA DAI⁴, SHUAI FENG^{5,6,7}, ARRAN C. GROSS¹, AND RUI XUE¹ Draft version December 8, 2020

ABSTRACT

We compare the radial profiles of the specific star formation rate (sSFR) in a sample of 175 star-forming galaxies in close pairs with those of mass-matched isolated galaxies in the SDSS-IV MaNGA survey. We find that the sSFR is centrally enhanced (within one effective radius) in interacting galaxies by ~ 0.25 dex and that there is a weak sSFR suppression in the outskirts of the galaxies of ~ 0.1 dex. We stack the differences profiles for galaxies in five stellar mass bins between $\log(M/M_{\odot}) = 9.0-11.5$ and find that the sSFR enhancement has no dependence on the stellar mass. The same result is obtained when the comparison galaxies are matched to each paired galaxy in both stellar mass and redshift. In addition, we find that that the sSFR enhancement is elevated in pairs with nearly equal masses and closer projected separations, in agreement with previous work based on single-fiber spectroscopy. We also find that the sSFR offsets in the outskirts of the paired galaxies are dependent on whether the galaxy is the more massive or less massive companion in the pair. The more massive companion experiences zero to a positive sSFR enhancement while the less massive companion experiences sSFR suppression in their outskirts.

Keywords: galaxies: star formation — galaxies: nuclei — galaxies: interactions — galaxies: mass evolution

1. INTRODUCTION

In the Λ CDM model, galaxy evolution is a hierarchical process. In this model, massive galaxies are the product of several past merger events of smaller galaxies. In fact, cosmological hydrodynamical simulations have shown that repeated merger events may be responsible for as much as $\sim 60\%$ of stellar mass in massive galaxies like M87 (e.g., Rodriguez-Gomez et al. 2016; Pillepich et al. 2018). As the galaxies undergo the merging process, the gas within the galaxies are subjected to gravitational torques which perturb the morphology of the galaxies.

The internal dynamics of these interacting galaxies were first modeled in the seminal work, Toomre & Toomre (1972). Since then, hydrodynamical simulations have expanded upon the N-body simulations of Toomre & Toomre (1972) by modeling gas-dynamics within the galaxies. These simulations show the process by which barred structures develop within the disks of the interacting galaxies due to the tidal torques between them (Barnes & Hernquist 1991). As the bars form, the gases within the galaxy's disk lose angular momentum and get funneled into the centers of the galaxies.

When the gas-inflows impact upon the gases in the nucleus of the galaxy, a burst of new star formation in triggered (Barnes & Hernquist 1996; Mihos & Hernquist 1996). These gas inflows will also bring metal-poor gases from the disk into the center of the galaxy which can dilute the central metallic-

- ¹ Department of Physics & Astronomy, University of Iowa, Iowa City, IA 52242 Institute for Astronomy, University of Hawaii, Honolulu, HI 96822
- ³ Department of Astrophysical and Planetary Sciences, University of Colorado, Boulder, CO 80309
- Chinese Academy of Sciences South America Center for Astronomy (CASSACA), 20A Datun Road, Beijing 100012, China
- Department of Physics, Hebei Normal University, 20 South Erhuan Road, Shijiazhuang, 050024, China
- ⁶ Kev Laboratory for Research in Galaxies and Cosmology, Shanghai Astronomical Observatory, Chinese Academy of Sciences, 80 Nandan Road, Shanghai 200030, China
- ⁷ University of the Chinese Academy of Sciences, No.19A Yuquan Road, Beijing 100049, China

ity (Rupke et al. 2010; Perez et al. 2011; Scudder et al. 2012). The gas-inflows may also be able to reach into the very center of the galaxy and trigger an episode of supermassive black hole (SMBH) accretion (Capelo et al. 2017).

Interaction induced star formation was first seen observationally in the bluer colors of peculiar galaxies in Larson & Tinsley (1978). Similar observations have has also been shown in more recent works using the single-fiber spectroscopic survey, SDSS (Sloan Digital Sky Survey) (Ellison et al. 2008; Li et al. 2008; Scudder et al. 2012; Patton et al. 2013; Bustamante et al. 2020). From these previous works it has been shown that the strength of the star formation enhancement in the centers of paired galaxies is dependent on the stellar mass of the pairs (Li et al. 2008), the projected separation between the pairs (Ellison et al. 2008; Li et al. 2008; Scudder et al. 2012), and the mass ratio between the pairs (Ellison et al. 2008).

The previously mentioned works using SDSS were restricted to studying the centers of the paired galaxies through 1-1.5"-radius optical fibers. With the recent large integral field spectroscopic (IFS) surveys, interacting galaxies can now be studied with unprecedented spatial detail. These surveys allow us to study the centers of merging galaxies more rigorously since apertures can be set to the physical scale of the galaxies instead of being bound by a fixed sky aperture. These IFS surveys will also allow us to see the extent of the centrally induced star formation and to see how the star formation in the disks of the galaxies are affected.

Indeed, Barrera-Ballesteros et al. (2015) used the CALIFA (Calar Alto Legacy Integral Field Area) survey to study a sample of 103 paired galaxies by varying the size of the aperture through which the EW(H α) is extracted. In this study, they found a moderate enhancement to the sSFR in the centers of paired galaxies and a moderate suppression to the sSFR in outskirts of the paired galaxies.

Pan et al. (2019) used the SDSS-IV MaNGA survey to study radial profiles of a sample of 205 paired galaxies. The enhancement to the sSFR was shown to be the strongest in the centers of the paired galaxies. This central enhancement linearly fell with increasing galactocentric radii; however, a moderate enhancement to the sSFR remains in the outskirts of the galaxies. Pan et al. (2019) further studied the paired galaxies as a function of merger stage, from well separated pairs to post-merger galaxies. Across the different merger stages, the sSFR enhancement was greatest in close pairs with tidal features and in post-merger galaxies. This was in agreement with previous hydrodynamical simulations which showed that a burst of star formation is triggered after the first pericenter and as the two galaxies begin to coalesce (Scudder et al. 2012).

The radial profile of sSFR in post-merger galaxies has also been studied with the MaNGA survey by Thorp et al. (2019). The post-merger galaxies were shown to have a strong enhancement to the sSFR in their centers as well as a moderate enhancement in their outskirts.

Where previous studies on the radial profile of the sSFR offsets in paired galaxies have focused on studying the profiles as a function of interaction stage, we will focus on the radial profile as a function of the stellar mass, projected separation, and mass ratio. As mentioned previously, these parameters have been covered by studies restricted to the nuclear region of the paired galaxies. With the MaNGA survey, we will be able to expand upon these previous studies in greater spatial detail. We will be able to analyze how these three parameters affect both the level of the sSFR offsets in the centers of the paired galaxies and the offsets in the outskirts of the galaxies. We will also be able to study whether any of the three parameters influence the gradient of the sSFR enhancement profiles or if the gradient is preserved between different configurations.

In our previous work using the MaNGA data included in the 14th Public Data Release (DR14; Abolfathi et al. 2018), we built a sample of close galaxy pairs where both components of the pair were contained within the field of view of a single integral field unit (Fu et al. 2018, hereafter Paper I). We found that approximately 5.7% of the MaNGA galaxies have a companion galaxy contained within the field-of-view of a single IFU. In this work, we update this sample and supplement it with a sample of companion galaxies identified outside the field-of-view of the MaNGA IFUs.

This paper is organized as follows; in § 2 we will discuss the properties of the MaNGA survey along with the construction of our pair and control samples, in § 3 we will discuss how we measure star formation rates and how we build radial profiles of star formation, in § 4 we study the radial profiles as a function of stellar mass, projected separation, and the mass ratio, in § 5 we compare our work against previous works, and in § 6 we summarize the findings of the work. Throughout we adopt the Λ CDM cosmology with $\Omega_{\rm m}=0.3,~\Omega_{\Lambda}=0.7,$ and h=0.7.

2. DATA AND SAMPLES

MaNGA is an IFS survey at the Apache Point Observatory (APO) which uses the SDSS (Sloan Digital Sky Survey) 2.5-meter telescope along with two dual-channel BOSS spectrographs (Drory et al. 2015). MaNGA captures spectra through 17 integral field units (IFUs) with variable numbers of fibers: 19, 37, 61, 91, and 127 fibers covering 12.5", 17.5", 22.5", 27.5", and 32.5" on the sky respectively (Law et al. 2015). MaNGA is an optical survey with a spectral coverage of 3600–10,300 Å with a resolution of R \sim 2000 and a PSF of 2.5" FWHM (Bundy et al. 2015).

The MaNGA survey targets galaxies from a subset of

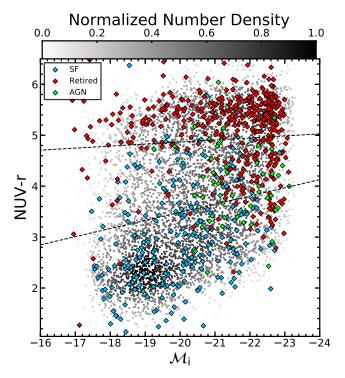


Figure 1. Color-magnitude diagram for MaNGA galaxies. The grey circles represent the whole MaNGA sample and the color scale reflects the local density around each data point in this color-magnitude plane, as indicated by the color bar on the top. The *blue* diamonds represent the star forming paired galaxies (by the BPT and EW(H α) cuts), the *red* diamonds represent the paired galaxies which are classified as retired (by the EW(H α) cut), and the *green* diamonds represent the paired galaxies containing an AGN (as identified by the BPT diagnostic). From top to bottom, the dashed lines divide the sample into red sequence, green valley, and blue cloud. The star-forming galaxy sample used in this paper are the galaxies below the lower dividing line.

41,154 galaxies in the NASA-Sloan Atlas (NSA v1_0_1; http://www.nsatlas.org) with a redshift range of 0.01 < z < 0.15 and a luminosity range of -17.7 $< \mathcal{M}_i <$ -24.0, where \mathcal{M}_i is the rest frame *i*-band magnitude within the survey's elliptical Petrosian apertures. MaNGA plans to cover 10,000 galaxies with a flat stellar mass distribution at two spatial coverages, 1.5 $R_{\rm eff}$ and 2.5 $R_{\rm eff}$ (where $R_{\rm eff}$ is the radius which contains 50% of the galaxy's total light). In this work we use the data from the 8th MaNGA Product Launch (MPL-8), which covers 6142 unique galaxies observed by July 3, 2018.

We classify galaxies in this survey as star forming galaxies by selecting galaxies in the blue cloud on the color-magnitude diagram (CMD). We show the CMD for the MaNGA survey and our pair sample in Figure 1 along with demarcation lines which separate the blue cloud, red sequence, and green valley. We established the demarcation lines by collapsing the CMD to a color histogram for each of the three regions. We then varied the slopes between the regions until we found the slopes which best fit the data. These demarcation lines are;

$$NUV - r = 3.1682 - 0.16(\mathcal{M}_i + 18) \tag{1}$$

$$NUV - r = 4.7866 - 0.04(\mathcal{M}_i + 18),$$
 (2)

Where NUV - r is the color from SDSS's k-corrected absolute magnitude and \mathcal{M}_i is the i-band magnitude from the NSA catalog. We further apply an EW(H α) \geq 3Å cut on galaxy spec-

tra extracted from a 1.0 $R_{\rm eff}$ aperture to ensure that all passive galaxies are removed from the sample (Cid Fernandes et al. 2011). Finally, we use the BPT diagnostic (Baldwin et al. 1981) to remove galaxies with possible AGN in their centers. Specifically, we use the emission line ratios, $\log([O\ III]/H\beta)$ and $\log([N\ II]/H\alpha)$, extracted from a 1.3 kpc aperture along with the maximum starburst line of Kewley et al. (2001) as the demarcation between the star-forming branch and the AGN branch.

On top of the star formation cuts, we require that all galaxies are in either the Primary or Secondary MaNGA subsamples (Wake et al. 2017), and that the stellar mass range of the galaxy sample is between $\log(M/M_{\odot}) = 9.0-11.5$. We use masses calculated from the elliptical Petrosian apertures in the NSA catalog for our total stellar masses.

We build two different pair samples in this work; the inside-IFU sample which contains paired galaxies where both galaxies are covered by a single MaNGA IFU and the outside-IFU sample where a MaNGA target galaxy is coupled with another galaxy found outside of its MaNGA IFU.

2.1. Inside-IFU Sample

To identify potential paired galaxies covered by individual IFUs, we start by overlaying SDSS photometric objects over each MaNGA fields of view. We manually inspect each MaNGA field, removing photometric objects which are over-deblended galaxy fragments and, very rarely, adding any objects missed in the SDSS photometric catalog. At this stage the object catalog includes foreground stars and foreground/background galaxies along with the potential paired galaxies.

To select paired galaxies out of our object catalog, we inspect the spectra of each object. We use our own IDL based spectral fitting code, SPFIT, to model the spectra from the MaNGA datacubes. SPFIT simultaneously fits emission lines and the stellar continuum with the Levenberg-Marquardt nonlinear least-squares minimization algorithm (Paper I). Emission lines are parameterized as a Gauss-Hermite series and the stellar continuum is the sum of simple stellar populations (SSPs) convolved with the line-of-sight velocity distribution (LOSVD).

The spectra of the identified objects is extracted through a 1" circular aperture and fitted assuming the MaNGA target's redshift and then manually sorted into the following categories: "good" galaxy spectra, broad-line AGN, foreground star, foreground/background galaxies, or poor S/N objects. The "good" galaxy spectra are the objects whose spectra are well modeled by SPFIT at the target galaxy's redshift, whether it is the target galaxy itself or a nearby companion galaxy. This means that the companion galaxy can be within approximately $\pm 3000~{\rm km~s^{-1}}$ of the MaNGA target. We found 6573 "good" objects, 57 broad-line AGN, 836 foreground stars, 319 foreground/background galaxies, and 1546 objects with poor S/N.

Among the 6142 MaNGA IFUs considered here, 404 have multiple galaxy objects within the IFU. We further restrict the sample by setting a relative velocity cut of $\Delta v < 500 \ \mathrm{km \ s^{-1}}$ to remove projected companions. Given the redshift range of the MaNGA sample and the size of MaNGA's IFUs, the maximum projected separation for a companion galaxy in the IFU is \sim 40 kpc. Again, the galaxy sample is also restricted to galaxies with a stellar mass range of $\log(M/M_{\odot}) = 9.0-11.5$ and galaxies in the Primary or Secondary MaNGA subsam-

ples. We also require that the galaxies are classified as star forming as described in § 2. These requirements reduce our sample down to 87 star forming MaNGA targets with inside-IFU companions. While the companions to the inside-IFU MaNGA targets contained are within the MaNGA IFUs, we only use the MaNGA targets when building radial profiles. We leave out the identified companions from the analysis because the MaNGA targets are covered by the NSA catalog with geometries and total stellar masses while the companions are not covered by the NSA catalog.

Several of the target galaxies in our sample have multiple companions. From the whole set of 404 IFUs, there are 327 pairs, 67 triplets, 7 quadruplets, and 1 quintuplet. In cases where a MaNGA target has multiple viable companions galaxies, we chose the closest companion when measuring the pair's mass ratio and projected separation.

2.2. *Outside-IFU Sample*

We supplement the inside-IFU sample with a set of pairs identified outside of the field of view of the MaNGA IFU. We select these outside-IFU pairs from the NSA catalog. We search for these external pairs by selecting objects with a projected separation from the MaNGA targets of $r_{\rm p} < 50$ kpc using the MaNGA target's redshift. We further use a relative velocity cut of $\Delta \nu < 500$ km s⁻¹ to remove projected galaxies from the selection.

From the NSA catalog's 641,409 galaxies, we find 492 galaxies which are paired to MaNGA targets. After restricting the sample to SFGs, we have another 133 MaNGA targets with paired galaxies outside of the IFU. MaNGA targets which have both an inside-IFU and an outside-IFU pair are left to the inside-IFU sample. This give us a total of 175 close pairs.

2.3. Control Sample

To show how the population of galaxy pairs differs from isolated galaxies, we will compare our pair sample to a sample of isolated galaxies in the MaNGA survey. We build this control sample from the MaNGA target galaxies which have no spectroscopic companions within $r_{\rm p} < 50$ kpc and $\Delta \nu < 500$ km s⁻¹ either inside or outside of the IFU. This gives us a control sample of 1888 star forming control galaxies.

It has been shown that the SFR in galaxies is dependent on both the stellar mass and the redshift of the galaxies (e.g., Noeske et al. 2007). We will compare our interacting galaxies with isolated galaxies of a similar stellar mass and redshift, to account for these other dependencies. To do this, we will use two different methods of pair - control comparison.

In the first method, we simply control for the stellar mass between the pairs and controls. We split both the pair and control samples into five evenly spaced stellar mass bins over the range, $\log(M/M_{\odot}) = 9.0{-}11.5$. The pairs are then compared to their respective controls within each stellar mass bins. While the redshift is not constrained in this method, we will show in § 4.1.1 that this method is sufficient to reveal the merger induced star formation.

In the second method, we select a "tailored" control sample for each paired galaxy from the full sample of isolated galaxies. We select a subsample of 20 control galaxies for each paired galaxy. We first select all of the control galaxies which are within a 0.1 dex stellar mass limit and within the same MaNGA subsample (e.g. Primary or Secondary) as the paired galaxy. Since the MaNGA sample has a tight distribution in stellar mass and redshift, the stellar mass and MaNGA

subsample restriction effectively sets a $\Delta z \lesssim \sim 0.025$ redshift tolerance. With these requirements, most paired galaxies will find between 20–100 control galaxies. Since we want each paired galaxy to be treated in a similar manner, we randomly down-select the total number of acquired control galaxies to 20. A given control galaxy may be selected for multiple pairs by the pipeline; most of the control galaxies are used at least once and the average number of times a given control is reused is between 4–6 times. In the cases where a paired galaxy does not initially acquire 20 control galaxies we iteratively expand the stellar mass limit by 0.1 dex until at least 20 control galaxies are found. Only 5 of the paired galaxies required an extra iteration to find 20 controls.

3. ANALYSIS METHODS

3.1. Specific Star Formation Rate

For each MaNGA $1'' \times 1''$ spaxel, we use our spectral fitting code, SPFIT, to get measurements of emission line fluxes, equivalent widths, velocities, and velocity dispersions of 19 emission lines and measurements of stellar masses, ages, [Fe/H], and the kinematics of the stellar populations.

We correct the emission lines for reddening using the extinction curve from Cardelli et al. (1989) with updated coefficients from O'Donnell (1994). The extinction is parameterized as $R_V \equiv A_V/E(B-V) = 3.1$, where we estimate the value of the *V*-band extinction, A_V , by comparing the $\text{H}\alpha/\text{H}\beta$ ratio to the expected value of 2.85 for Case-B recombination.

We measure the SFR from the extinction corrected H α luminosity, $L_{\rm H}\alpha$. We use the SFR formula, Equation 3, from Murphy et al. (2011) which uses a Kroupa IMF, Solar metallicity, a constant SFR at an age of 100 Myr, and Case-B recombination:

$$\frac{\text{SFR}}{M_{\odot} \,\text{yr}^{-1}} = \frac{L_{\text{H}\alpha}}{1.86 \times 10^{41} \,\text{erg s}^{-1}}.$$
 (3)

Since the stellar mass of a galaxy is not uniformly distributed within the galaxy, we normalize the SFR by the stellar mass in the same spaxel, giving us the specific star formation rate (sSFR):

$$sSFR = \frac{SFR}{M}.$$
 (4)

The local stellar masses used here is derived from SPFIT's best-fit stellar continuum. Utilizing sSFR, instead of SFR, allows us to compare regions of high mass surface density to regions of low mass surface density.

3.2. Radial Profiles

In order to spatially characterize the star formation in the paired galaxies we build radial profiles of sSFR. First, the geometry of the galaxies needs to be defined. Specifically we will need the position angle, the inclination angle, and the effective radius of each of the MaNGA targets. We use the *r*-band elliptical Petrosian apertures from the NSA catalog and the *r*-band Sérsic apertures from Simard et al. (2011) to define the geometries of the galaxies.

The NSA catalog has complete coverage over the MaNGA sample (since MaNGA selects its targets from this catalog); however, it tends to fail to properly fit paired galaxies with close on-sky separations. We found that the apertures from Simard et al. (2011) work better for these close paired galaxies; however, the catalog does not completely cover the MaNGA sample. We use the NSA catalog for the outside-IFU

pair sample because they are well separated on the sky. The Simard et al. (2011) catalog is used for the inside-IFU sample. If the paired galaxy is not covered by Simard et al. (2011), we use the ellipse from the NSA catalog.

We fit the geometry with apertures from both catalogs when available. When using the first method of pair-control comparison, where pairs and controls are grouped into stellar mass bins, we fit the control galaxies with the NSA apertures. When making the comparison with the second method, paired galaxies fitted with the NSA apertures are compared against controls fitted with the NSA apertures and paired galaxies fitted with the Simard et al. (2011) apertures are compared against controls fitted with the Simard et al. (2011) apertures. Further, when defining a galaxy's geometry with the Simard et al. (2011) apertures we also use the masses given in the catalog for the total stellar mass of the galaxy. Note that although we carefully treat the two catalogs separately whenever possible, we find excellent agreement in the geometry parameters of isolated galaxies in both catalogs.

We calculate the inclination angle, *i*, of the galaxies using the major-to-minor axis ratios from the elliptical apertures;

$$\cos^2(i) = \frac{(b/a)^2 - q^2}{1 - q^2},\tag{5}$$

Where b/a is the major-to-minor axis ratio and q is the intrinsic oblateness. We use the empirically determined oblateness of q = 0.13, from Giovanelli et al. (1994).

The inclination angle, along with the galaxy's position angle, is used to deproject the geometries of the galaxies. We use the 50% half light radius (*i.e.*, the effective radius, $R_{\rm eff}$) to scale the sizes of the galaxies. Doing this will allow us to compare galaxies of different sizes against each other.

Once the geometries of the galaxies are set, we can build azimuthally averaged radial profiles. The spaxels are binned into radius increments of $0.2~R_{\rm eff}$ from $0.0-2.6~R_{\rm eff}$. While the MaNGA sample is limited spatially to $1.5-2.5~R_{\rm eff}$ the spaxels along the semi-minor axis of a galaxy will be able to extend beyond that range because of the galaxy's inclination angle, $\sin(i)$.

Within each radius bin we take the median of the specific star formation rate. The profiles' errors are the standard error of the mean of the data within each radius bin. We build an azimuthally averaged radial profile for each MaNGA star forming galaxy and later stack and differentiate these profiles in the subsequent analysis.

4. RESULTS

4.1. Star Formation Enhancement

With the individual log(sSFR) profiles built for each MaNGA galaxy, we now use two different methods to compare the profiles of paired galaxies against the profiles of control galaxies. In the first method, in § 4.1.1, paired galaxies are compared to control galaxies within evenly spaced stellar mass-bins. In the second method, in § 4.1.2, paired galaxies are compared to a subset of 20 control galaxies which are matched in stellar mass and redshift.

4.1.1. Mass-Binned Difference Profiles

In the first method, paired and control galaxies are grouped into five evenly spaced stellar mass bins between $\log(M/M_{\odot})$ = 9.0–11.5. Within each stellar mass bin, we create a median profile of $\log(\text{sSFR})$ as a function of R_{eff} -scaled galactocentric

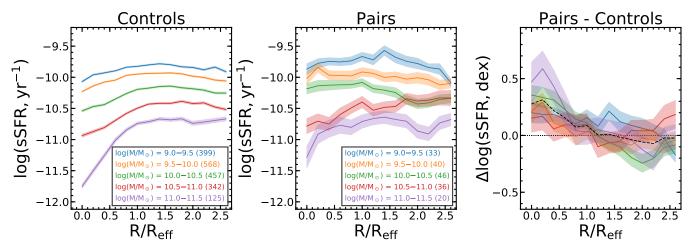


Figure 2. The log(sSFR) as a function of galactocentric radius for control galaxies (**Left**) and galaxy pairs (**Middle**). The difference between the profiles of the paired galaxies and the control galaxies are shown in the **Right** panel. The dashed black profile represents the mean of the difference profiles. The colors of the profiles represent the mass range of the selected galaxies which is given in the legend along with the number of galaxies in that mass bin in parantheses. The highlighted region around the profiles represent the standard error of the mean of the data at the given radius interval.

distance for both paired and control galaxies. The control profiles are constructed using all available control galaxies within each mass bin. The error associated with the "stacked" profile is the standard error of mean of the data at each radius bin. We show these stacked profiles for control galaxies in the left hand panel of Figure 2 and the stacked profiles for paired galaxies in the middle panel of Figure 2. Star formation in the control galaxies are quenched in their centers with respect to their disks and the difference between the sSFR in their centers and their disks increases with stellar mass, consistent with previously published results using the MaNGA survey (Belfiore et al. 2018). In contrast, the paired galaxies show flatter sSFR profiles where the level of the sSFR remains roughly consistent across their disks except for paired galaxies with stellar masses above $\log(M/M_{\odot}) = 10.5$, which still show some central quenching.

We then take the difference between the stacked profiles of the paired galaxies and the control galaxies, pair - control, in log space (this means that the difference profiles really represent a ratio between the pairs and controls in linear space). This gives us the difference profile, $\Delta \log(sSFR)$, which shows us where the sSFR is enhanced or suppressed (shown in the right hand panel of Figure 2). Across all stellar mass bins, the sSFR of paired galaxies are centrally enhanced by $\sim 0.3\pm 0.1$ dex, which gradually falls to zero around ~ 1.2 $R_{\rm eff}$. In the outskirts of the pairs beyond 1.2 $R_{\rm eff}$, the pairs feature lightly suppressed sSFR of 0.0-0.1 dex. All of the mass ranges except for the highest mass range, $\log(M/M_{\odot})$ = 11.0–11.5, trend closely to the median profile. For the most massive galaxies, $\log(M/M_{\odot}) = 11.0-11.5$, the enhancement to the sSFR within $0.5 R_{\rm eff}$ is significantly higher than the median profile (reaching 0.5-0.6 dex). As will be discussed in § 4.1.2, we believe this elevated enhancement in the highest mass bin is driven by more compact mergers instead of stellar

In summary, Figure 2 shows that the merger process is capable of rejuvenating star formation in the centers of these galaxies, resulting in almost flat sSFR radial profiles. In addition, the sSFR enhancement is mass independent – star formation proceeds at $\sim 2 \times (0.3 \text{ dex})$ greater rates in galaxies with close companions than in more isolated galaxies, across a wide mass range between $9.0 \leq \log(M/M_{\odot}) \leq 11.5$.

This method of stacking sSFR profiles by a single parameter (stellar mass) has the advantage of simplicity and large statistical samples. It has revealed the first order result of mass-independent, centrally enhanced star formation in close galaxy pairs. To proceed with exploring the dependency of Δ sSFR on merger parameters such as separation and mass ratio, we will utilize a more sophisticated method of selecting control samples for individual paired galaxies based on stellar mass and redshift in the following subsections.

4.1.2. Tailored-Controls Difference Profiles

In the second method, we match each paired galaxy to a set of 20 control galaxies of similar stellar masses and redshifts, as described in § 2.3. We then take the median of the azimuthally averaged profiles of the tailored control sample. Finally, we obtain the Δ logsSFR profile for each of the 175 paired galaxies by calculating the difference between its sSFR profile and the median profile of its control sample.

Before delving into merger parameters, we decided to stack the profiles by stellar mass to see how this method compares to the previous mass-binning method. We split the individual difference profiles into five evenly spaced stellar mass bins between $\log(M/M_{\odot}) = 9.0-11.5$ and stack the difference profiles within each mass bin. This gives us five difference profiles covering five different stellar mass ranges shown in the left hand panel of Figure 3. The errors of the stacked profiles are the standard error of the mean of the difference profiles within each bin.

To focus on the sSFR offsets in the centers of the galaxies, we also calculate the sSFR difference between each paired galaxy and its control sample in the central $0.5 R_{\rm eff}$. We depict the central $\Delta \log({\rm sSFR})$ as a function of stellar mass in the right hand panel of Figure 3.

The difference profiles are shown to be centrally enhanced by $\sim 0.25 \pm 0.1$ dex. Similar to what was seen in § 4.1.1, the level of the enhancement is independent of galaxy mass with the exception of the highest mass bin, $\log(M/M_{\odot}) = 11.0-11.5$, which is 0.15-0.25 dex higher than the sample average.

The central enhancement to the sSFR falls to zero around $1.2~R_{\rm eff}$ and the outskirts of the galaxies are lightly suppressed by $0.1~{\rm dex}$. The paired galaxies in the mass range,

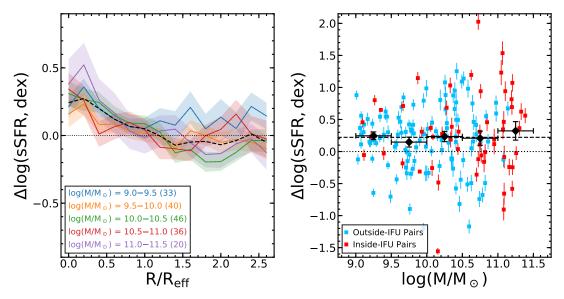


Figure 3. The Left panel shows the $\triangle \log(\text{sSFR})$ profiles where the difference profiles are constructed from the difference between the paired galaxy profiles and a set of 20 control galaxies. The profiles are split into five different stellar mass bins and the highlighted region about the profiles represent the standard error of mean of the profile. The black dashed line represents the mean profile between the four difference mass ranges. The number of paired galaxies in each mass range is given in the legend in parentheses. In the **Right** panel the nuclear $\triangle \log(\text{sSFR})$ are shown. The black squares are the mean values within a stellar mass bin (where the size of the bins are shown the the horizontal error bars). The vertical error bars on the black squares represent the standard deviation within the bin. The horizontal, dashed black line represents the median central enhancement of the pair sample. Galaxies in the outside-IFU (Blue) and inside-IFU (Red) samples are separately depicted.

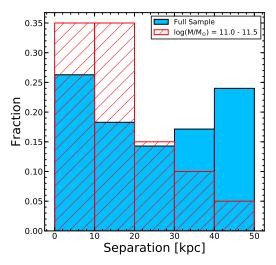


Figure 4. The projected separation distribution of the whole sample (blue) against the projected separation distribution for the highest mass galaxies, $\log(M/M_{\odot}) = 11.0-11.5$ (Red).

 $\log(M/M_{\odot}) = 9.0-9.5$, feature enhanced sSFR in their disks of 0.1–0.2 dex. As we will show in the next section, § 4.2, the offsets seen in the disks of paired galaxies are largely driven by whether the galaxy is the more massive or less massive companion in the pair.

To understand why these high mass galaxies behave differently from the rest of the sample, we compare the distribution of the projected separation for the whole sample and for galaxies in the highest mass bin in Figure 4. The whole sample has a v-shaped separation distribution. This is the result of the combination of the two different samples, the inside-IFU and outside-IFU samples. The outside-IFU sample should find more pairs at wide projected separations due to the larger volume to find companions in. The separation distribution of the inside-IFU sample is limited by MaNGA's IFU sizes and

the sample's redshift distribution; the maximum possible projected separation for a MaNGA target with z = 0.15 and a 127 spaxel IFU is about 40 kpc. The highest mass galaxies in the sample are at closer projected separations in comparison to the rest of the sample with 70% of the highest mass galaxies being within 20 kpc. As we will show in § 4.3, the central sSFR enhancement is strongest at small projected separation which means that higher sSFR in the centers of the massive galaxies may be driven by their close projected separations.

The results we obtain from the tailored-control method is largely consistent with the mass-binning method. Between the two methods we see that the $\Delta \log(\text{sSFR})$ profile is independent of the total stellar mass of the galaxies. In the next two sections, we will use the tailored-control method to study how the difference profiles behave as a function of the mass ratio (§ 4.2) and projected separation (§ 4.3).

4.2. Dependency on Mass Ratio

While the centrally enhanced star formation in close galaxy pairs seems mostly mass-independent, the mass ratio of the galaxy pair, like the projected separation, may be an important parameter that controls the level of enhancement (Ellison et al. 2008).

The mass ratio here is defined as,

$$\Delta \log(M) = \log(M_{\text{target}}) - \log(M_{\text{comp}}), \tag{6}$$

where $M_{\rm target}$ is the stellar mass of the MaNGA target galaxy and $M_{\rm comp}$ is the stellar mass of the companion galaxy. In the sample, the MaNGA target is not always the more massive component of the pair. We split the sample into two groups based on their mass ratios; primary companions in which the MaNGA target is the more massive galaxy and secondary companions in which the MaNGA target is the less massive galaxy.

For the outside-IFU pair sample we use the stellar masses enclosed by the *r*-band elliptical Petrosian apertures from the

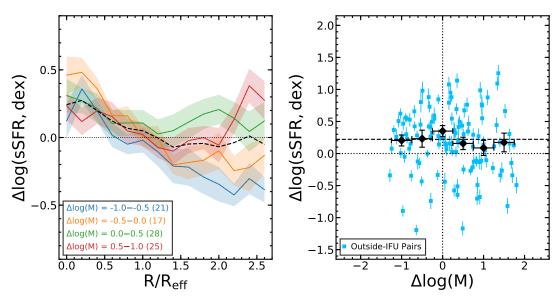


Figure 5. Same as Figure 3 except the difference profiles are split by the mass ratio of the pair. The inside-IFU sample is left out of this analysis because we do not yet have reliable measurements of their total stellar mass ratios.

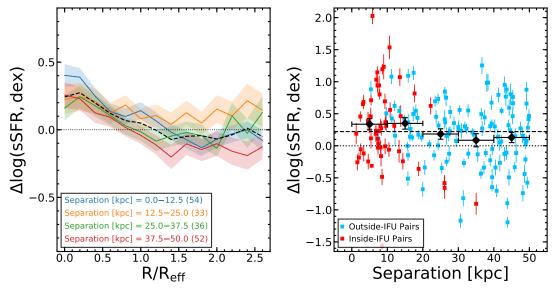


Figure 6. Same as Figure 3 except the difference profiles are split by projected separation.

NSA catalog. The inside-IFU pair sample is left out of this analysis, because most of the secondary companions in these pairs are missing in the NSA catalog and the Simard et al. (2011) catalog.

In the top left of Figure 5, we split the profiles by mass ratio in four bins; the primary and secondary companion of a major merger, $|\Delta \log(M)| < 0.5$, and the primary and secondary companion of a minor merger, $|\Delta \log(M)| > 0.5$. Regardless of the mass ratio, the centers of the paired galaxies are centrally enhanced, though major mergers have stronger enhancements in their centers by ~ 0.2 dex over minor mergers. Secondary companions also feature slightly higher levels of enhancement in their centers than primary companions at the same mass ratios by ~ 0.1 dex.

The sSFR offsets in the outskirts of the galaxy pairs show a dependence on the mass ratio. Primary companions show a zero to positive enhancement of 0.0–0.4 dex to the sSFR in their outskirts. Secondary companions feature a suppression

to the sSFR in their outskirts of about 0.1-0.4 dex.

In the top right of Figure 5 we see that the sSFR enhancement is strongest in galaxies close to a 1:1 mass ratio ($\Delta \log(M) = 0.0$). These galaxies feature a central enhancement of ~ 0.35 dex which is 0.1 dex higher than the average central enhancement of the whole sample. This enhancement falls with wider mass ratio; however, pairs with large differences in stellar mass still feature substantial levels of star formation enhancement, 0.15–0.20 dex at mass ratios of $|\Delta \log(M)| = 1.0$. We also see that secondary companions show a higher level of sSFR enhancement, by ~ 0.1 dex, with respect to primary companions.

From the mass ratio, we see two different effects. First, we see that the central enhancement to the sSFR is strongest for pairs with 1:1 mass ratios. Second, we see that secondary companions show steeper enhancement profiles with higher levels of sSFR enhancement in their centers and stronger levels of sSFR suppression in their disks with respect to primary

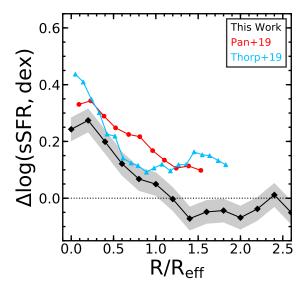


Figure 7. The mean radial profile of $\triangle \log(\text{sSFR})$ between pairs and controls of this work with the tailored control method (*Black*) compared against those of Pan et al. (2019) (*Red*), a pair sample, and Thorp et al. (2019) (*Blue*), a post-merger sample.

companions. It is interesting to note that the central enhancement to sSFR is dependent on both the mass ratio and the projected separation (which we will demonstrate in the next section) while the sSFR offsets in their outskirts primarily depends on whether the galaxy is the primary or secondary companion of the pair.

4.3. Dependency on Projected Separation

A number of previous studies have shown that the sSFR enhancement increases as projected separation decreases (e.g., Li et al. 2008; Ellison et al. 2008; Scudder et al. 2012; Patton et al. 2013), in agreement with simulations (Scudder et al. 2012).

Figure 6 shows the profile and the central level of sSFR enhancement as a function of the projected separation $(r_{\rm p})$ from our MaNGA data. The $\Delta \log({\rm sSFR})$ profiles show a clear gradient with the projected separation with close galaxy pairs showing higher levels of sSFR enhancement compared to pairs with wide separations. The profiles in the galaxy pairs in the separation range, $r_{\rm p}=0.0-12.5$, are generally $\sim 0.1-0.15$ dex above the median and the profiles of the galaxy pairs in the separation range, $r_{\rm p}=37.5-50.0$, are generally $\sim 0.05-0.1$ dex below the median.

This effect can be seen more clearly in the plot of the central $\Delta log(sSFR)$ enhancement as a function of projected separation. The level of the enhancement gradually increases with closer separation from 50 kpc to 10 kpc. While $\Delta log(sSFR)$ falls at higher separations, there is still a substantial level of enhancement between 40 and 50 kpc, $\sim\!0.1\text{--}0.2$ dex. Within 20 kpc, the $\Delta log(sSFR)$ enhancement jumps to 0.3–0.4 dex. Our data shows that the sSFR enhancement persists out to at least $r_{\rm p}=50$ kpc, which is the limit of our pair selection. In the next section, we will compare our results with those from previous studies.

5. COMPARISON WITH PREVIOUS WORK

5.1. Difference Radial Profiles

In Figure 7 we compare the $\Delta log(sSFR)$ profile as a function of galactocentric radius between our work and previous

works. The post-merger galaxies in Thorp et al. (2019) have sSFR enhancements between $\sim\!0.05\text{--}0.2$ dex higher than our sample of paired galaxies. The centers of the post-merger galaxies feature a greater level of sSFR enhancement in their centers compared to our galaxies pairs of $\Delta log(sSFR)=0.5$, roughly 0.25 dex higher than our paired galaxies. The post-merger galaxies also feature enhanced sSFR in their disk past $1.0~R_{\rm eff}$ of $\sim\!0.1\text{--}0.15$ dex. The heightened level of sSFR enhancement in the centers of post-merger galaxies in comparison to merging galaxies seems consistent with the idea that a second and greater burst of star formation occurs as the two merging galaxies coalesce into a single galaxy.

The galaxy pairs in Pan et al. (2019) have sSFR enhancements that are roughly ~ 0.1 –0.2 dex higher than our sample. Our paired galaxies show a slight sSFR suppression in their disks past 1.0 $R_{\rm eff}$ while the galaxy pairs in Pan et al. (2019) show an enhancement of ~ 0.15 dex to the sSFR in their disks. The reason for the discrepancies between our samples may be that Pan et al. (2019) includes a set of post-merger galaxies while our sample has no post-merger galaxies. These post-merger galaxies are predicted to have higher levels of star formation over other paired galaxies due to a second larger burst of star formation which is triggered as the merging galaxies coalesce and may be able to increase the sample's average sSFR enhancement.

5.2. Dependency on Merger Parameters

While in this work we find that $\Delta \log(sSFR)$ has essentially no dependence on the stellar mass of the galaxy, Li et al. (2008) found that lower mass galaxies experience greater levels of enhancement than higher mass galaxies. Galaxies in the mass range $\log(M/M_{\odot}) = 9.72$ were shown to experience an enhancement ~ 0.4 dex higher than galaxies in the mass range $\log(M/M_{\odot}) = 10.6$. The source of the difference is unclear; between our works we utilize different methods for determining the sSFR enhancement in galaxy pairs. Li et al. (2008) defines their enhancement function as the average sSFR of the paired galaxies at a given separation, weighted by the number of companions, subtracted by the average sSFR of the whole sample. While we do not find the same dependency between the sSFR enhancement and stellar mass, the sSFR enhancement as a function of projected separation between our studies is in good agreement (see Figure 8).

The dependency of the SFR enhancement on the mass ratio was studied in Ellison et al. (2008). They found that pairs with mass ratios of 2:1 have higher SFR enhancements of \sim 0.1 dex over pairs with wider 10:1 mass ratios. We find that pairs with mass ratios of $\Delta \log(M) = 0.25$ (1.8:1) are 0.2 dex over pairs with mass ratios of $\Delta \log(M) = 1.0$ (10:1). Ellison et al. (2008) also saw tentative evidence for SFR enhancement in the secondary companions of minor pairs. We not only confirm that secondary companions of minor pairs feature SFR enhancement, but also that the enhancement is higher than the primary component of pairs at the same mass ratios.

The observations are also consistent with simulations. Moreno et al. (2015) used GADGET-3, a smoothed particle hydrodynamics code, to study the spatial extent of the star formation enhancement. The merger simulations showed that the star formation enhancement was largely concentrated in the centers (R < 1 kpc) of the paired galaxies and that the offnuclear regions (1 < R < 10 kpc) showed a suppression to the star formation. Moreno et al. (2015) also found that lower mass secondary galaxies (in mergers with stellar mass ratios of 2.5:1) have higher levels of sSFR enhancement in their

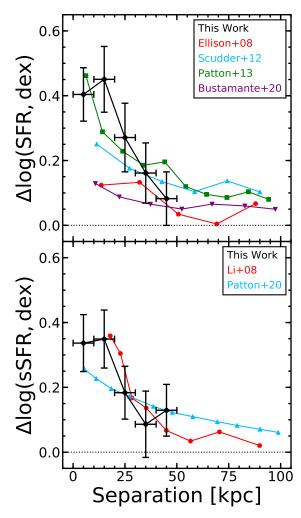


Figure 8. (Top) $\triangle \log(SFR)$ over projected separation from this study (Black), Ellison et al. (2008) (Red), Scudder et al. (2012) (Blue), Patton et al. (2013) (Green), and Bustamante et al. (2020) (Purple). (Bottom) $\triangle \log(SSFR)$ over projected separation from this study (Black), Li et al. (2008) (Red), and Patton et al. (2020) (Blue).

centers and have stronger levels of sSFR suppression in their disks. This is in good agreement with our work, we found that secondary companions show moderately higher levels of sSFR enhancement in their centers in comparison to primary companions at the same mass ratio. Further, the outskirts of the primary companions feature positive to zero enhancement to their sSFR while the secondary companions show a strong suppression to the sSFR in their outskirts.

Figure 8 compares the enhancement in both SFR and sSFR as a function of projected separation. For our data points, we use the mean $\Delta \log SFR$ and $\Delta \log sSFR$ measured within a deprojected radius of 0.5 $R_{\rm eff}$ (i.e., the black data points in the right side panel of Figure 6). The literature data is measured from single 1-1.5"-radius SDSS fibers (Ellison et al. 2008; Scudder et al. 2012; Patton et al. 2013; Bustamante et al. 2020). We find that our central SFR enhancements for closely separated pairs are higher than many of the previous studies, our sSFR enhancement is \sim 0.2 dex higher than Scudder et al. (2012) and \sim 0.3 dex higher than Ellison et al. (2008) and Bustamante et al. (2020). The central enhancement to the sSFR for closely separated pairs in our sample is \sim 0.1 dex higher than Patton et al. (2013). The sSFR enhancement function

from Li et al. (2008) follows closely to our own and remains \sim 0.05 dex above our sample out to 40 kpc.

The sSFR as a function of separation was studied with the cosmological hydrodynamical simulations of IllustrisTNG (Patton et al. 2020). In Figure 8 we show the $\Delta log(sSFR)$ enhancements across 2D separation (projected separation) from the TNG300-1 simulation. Patton et al. (2020) found a sSFR enhancement which is $1.8\times$ that of the isolated controls within a separation of 15 kpc and is statistically significant out to a 2D separation of $\sim\!250$ kpc. This enhancement is $\sim\!0.1$ dex lower than ours; however, our sSFR enhancement shown in Figure 8 was extracted from a $0.5~R_{\rm eff}$ aperture while Patton et al. (2020) extracted the sSFR from a 50% half-mass radius. This means that our extraction radius is effectively twice a small and is more restricted to the central burst of star formation.

Our sample only covers projected separations within 50 kpc, while previous surveys cover out to 100-200 kpc. While our sample covers a smaller separation range, the $\Delta log(SFR)$ of our sample at 50 kpc is roughly the same level as Scudder et al. (2012) and Patton et al. (2013) at the same projected separation. From this we see that our sSFR enhancement as a function of projected separation is consistent with with what has been found in previous works.

6. SUMMARY AND CONCLUSION

In this paper, we have demonstrated the power of a massive integral-field spectroscopic survey in comparison studies of galaxy properties. The nearby galaxy populations show consistent behaviors despite of their large diversity in star formation properties. Stacking was able to detect the signal buried in the noise by averaging, in the time domain, the likely stochastic star forming histories of galaxies (which drives the scatter in the sample). We focused on comparing the azimuthally averaged radial profiles of sSFR between galaxies in close pairs and a control sample of isolated galaxies. In agreement with previous studies, we found that, on average, star formation is elevated in close galaxy pairs. The properties of these purported merger-induced differences in sSFR can be summarized as follows:

- 1. Star formation is enhanced within the inner 1.0 $R_{\rm eff}$ and it peaks at a level of 0.25 ± 0.1 dex (i.e., $\sim 2 \times$ faster star formation). On the other hand, the outskirts of the paired galaxies ($R_{\rm eff} = 1.0$ –2.5) show a moderate amount of suppression in sSFR at a level of ~ 0.1 dex.
- 2. The sSFR difference profile is largely independent of the stellar mass.
- The level of central sSFR enhancement increases as the projected separation of the pair decreases.
- 4. The level of central sSFR enhancement depends on the mass ratio of the galaxy pair. Galaxies with small mass ratios, $|\Delta \log(M)| = 0.0$ –0.5, see an enhancement \sim 0.1 dex higher than the average. But the enhancement is still present in pairs with mass ratios as large as $|\Delta \log(M)| = 1.0$.
- 5. The merger-induced changes in sSFR also seem to differ between the more massive and the less massive member of a galaxy pair. At the same mass ratio, the less massive member in a galaxy pair shows a higher sSFR enhancement (by ~0.1 dex) in comparison to the

more massive member. And in the galactic outskirt $(R/R_{eff} = 1.0-2.5)$, the more massive member shows a general enhancement in sSFR, while the less massive member features a general suppression.

As of 2020 August 24, MaNGA has completed its observations of \sim 10,000 galaxies. This final sample gives us access to an unprecedentedly large sample of paired and control galaxies with 2" spatial sampling up to 2-3 $R_{\rm eff}$, which will undoubtedly improve the results presented here. In addition, the less massive members of the inside-IFU pairs can be included in such a comparison study once we build a better deblended photometric catalog using SDSS images.

We thank Cheng Li for our useful discussion on how the sSFR enhancement in galaxy pairs relates to their stellar mass and mass ratio. J.S. and H.F. acknowledge support from the National Science Foundation (NSF) grant AST-1614326. Funding for the Sloan Digital Sky Survey IV has been provided by the Alfred P. Sloan Foundation, the U.S. Department of Energy Office of Science, and the Participating Institutions. SDSS acknowledges support and resources from the Center for High-Performance Computing at the University of Utah. The SDSS web site is www.sdss.org.

SDSS is managed by the Astrophysical Research Consortium for the Participating Institutions of the SDSS Collaboration including the Brazilian Participation Group, the Carnegie Institution for Science, Carnegie Mellon University, the Chilean Participation Group, the French Participation Group, Harvard-Smithsonian Center for Astrophysics, Instituto de Astrofísica de Canarias, The Johns Hopkins University, Kavli Institute for the Physics and Mathematics of the Universe (IPMU) / University of Tokyo, the Korean Participation Group, Lawrence Berkeley National Laboratory, Leibniz Institut für Astrophysik Potsdam (AIP), Max-Planck-Institut für Astronomie (MPIA Heidelberg), Max-Planck-Institut für Astrophysik (MPA Garching), Max-Planck-Institut für Extraterrestrische Physik (MPE), National Astronomical Observatories of China, New Mexico State University, New York University, University of Notre Dame, Observatório Nacional / MCTI, The Ohio State University, Pennsylvania State University, Shanghai Astronomical Observatory, United Kingdom Participation Group, Universidad Nacional Autónoma de México, University of Arizona, University of Colorado Boulder, University of Oxford, University of Portsmouth, University of Utah, University of Virginia, University of Washington, University of Wisconsin, Vanderbilt University, and Yale University.

REFERENCES

Abolfathi, B., Aguado, D. S., Aguilar, G., et al. 2018, ApJS, 235, 42 Baldwin, J. A., Phillips, M. M., & Terlevich, R. 1981, PASP, 93, 5 Barnes, J. E., & Hernquist, L. 1996, ApJ, 471, 115 Barnes, J. E., & Hernquist, L. E. 1991, ApJL, 370, L65 Barrera-Ballesteros, J. K., Sánchez, S. F., García-Lorenzo, B., et al. 2015, A&A, 579, A45 Belfiore, F., Maiolino, R., Bundy, K., et al. 2018, MNRAS, 477, 3014

Belfiore, F., Maiolino, R., Bundy, K., et al. 2018, MNRAS, 477, 3014 Bundy, K., Bershady, M. A., Law, D. R., et al. 2015, ApJ, 798, 7 Bustamante, S., Ellison, S. L., Patton, D. R., & Sparre, M. 2020, MNRAS, 494, 3469

Capelo, P. R., Dotti, M., Volonteri, M., et al. 2017, MNRAS, 469, 4437
Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245
Cid Fernandes, R., Stasińska, G., Mateus, A., & Vale Asari, N. 2011, MNRAS, 413, 1687

Drory, N., MacDonald, N., Bershady, M. A., et al. 2015, AJ, 149, 77 Ellison, S. L., Patton, D. R., Simard, L., & McConnachie, A. W. 2008, AJ, 135, 1877

Fu, H., Steffen, J. L., Gross, A. C., et al. 2018, ApJ, 856, 93
Giovanelli, R., Haynes, M. P., Salzer, J. J., et al. 1994, AJ, 107, 2036
Kewley, L. J., Dopita, M. A., Sutherland, R. S., Heisler, C. A., & Trevena, J. 2001, ApJ, 556, 121

Larson, R. B., & Tinsley, B. M. 1978, ApJ, 219, 46 Law, D. R., Yan, R., Bershady, M. A., et al. 2015, AJ, 150, 19 Li, C., Kauffmann, G., Heckman, T. M., Jing, Y. P., & White, S. D. M. 2008,

MNRAS, 385, 1903 Mihos, J. C., & Hernquist, L. 1996, ApJ, 464, 641 Moreno, J., Torrey, P., Ellison, S. L., et al. 2015, MNRAS, 448, 1107 Murphy, E. J., Condon, J. J., Schinnerer, E., et al. 2011, ApJ, 737, 67 Noeske, K. G., Weiner, B. J., Faber, S. M., et al. 2007, ApJL, 660, L43 O'Donnell, J. E. 1994, ApJ, 422, 158

Pan, H.-A., Lin, L., Hsieh, B.-C., et al. 2019, ApJ, 881, 119 Patton, D. R., Torrey, P., Ellison, S. L., Mendel, J. T., & Scudder, J. M. 2013, MNRAS, 433, L59

Patton, D. R., Wilson, K. D., Metrow, C. J., et al. 2020, MNRAS, 494, 4969 Perez, J., Michel-Dansac, L., & Tissera, P. B. 2011, MNRAS, 417, 580 Pillepich, A., Nelson, D., Hernquist, L., et al. 2018, MNRAS, 475, 648 Rodriguez-Gomez, V., Pillepich, A., Sales, L. V., et al. 2016, MNRAS, 458, 2371

Rupke, D. S. N., Kewley, L. J., & Chien, L. H. 2010, ApJ, 723, 1255 Scudder, J. M., Ellison, S. L., Torrey, P., Patton, D. R., & Mendel, J. T. 2012, MNRAS, 426, 549

Simard, L., Mendel, J. T., Patton, D. R., Ellison, S. L., & McConnachie, A. W. 2011, ApJS, 196, 11

Thorp, M. D., Ellison, S. L., Simard, L., Sánchez, S. F., & Antonio, B. 2019, MNRAS, 482, L55

Toomre, A., & Toomre, J. 1972, ApJ, 178, 623

Wake, D. A., Bundy, K., Diamond-Stanic, A. M., et al. 2017, AJ, 154, 86