#### Time Value of Money

- Would you prefer \$1,000 today or \$1,000 one year from now?
  - Today
  - Opportunity to invest
- Would you prefer \$1,000 today or \$1,200 one year from now?
  - Dependent upon interest rate or opportunity to invest
- Time value of money: value of money decreases over me

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### Net Present Value (NPV)

Converts future cash flow stream into today's dollars

- Cash flow by date
  - Investments: negav e numbers
  - Returns and savings: posiv e numbers
- Interest rate
- Net present value: what a given cash flow is worth to you today

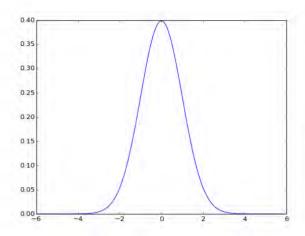
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#### **NPV Interpretation**

- Positive NPV: make more money than bank interest rate
  - Compare alternav es for highest NPV
- Negative NPV: lose money compared to bank interest rate

## Internal Rate of Return (IRR)

- Measures the effecv e rate of return for your cash flow stream
- Calculates exact interest rate you're earning
- For example:
  - Posiv e NPV: goal of 7% interest rate converts to 7.3% IRR
  - Negav e NPV: goal of 7% interest rate converts to 3% IRR
- Calculates exact interest rate you would achieve if NPV is set to zero



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# **Descriptive Statistics**

- Simple measures of data
- Examples:
  - Mean: arithmec a verage
  - Median: middle point in distribuon
  - Mode: most common value (highest frequency of occurrence)
  - Kurtosis: height of data peak relav e to normal distribuon
  - Skewness: left or right posion of da ta relav e to normal distribuon
  - Standard deviaon: measur e of spread
  - Range: highest value minus lowest value

#### **Correlations Overview**

- The measure of how two variables are related
- Examples:
  - Educaon and earning pot enal (posiv e correlaon)
  - Product price and product demand (negav e correlaon)
- Posiv e correlaon: v ariables moving in same direcon
- Negav e correlaon: v ariables moving in opposite direcons

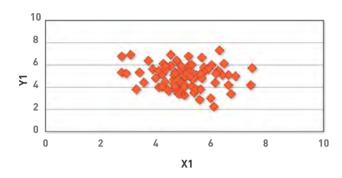
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## **Types of Correlations**

- Negav e
- Posiv e
- Zero

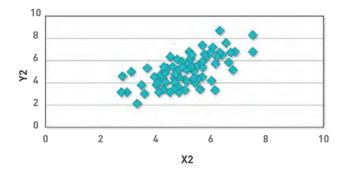
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# **Zero Correlation**

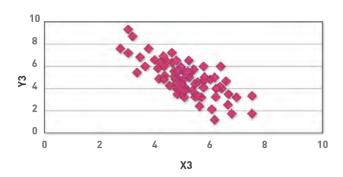


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# **Positive Correlation**



# **Negative Correlation**



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#### **Correlation Measurements**

- Measured on a scale from -1 to +1.
  - ∘ Perfectly negav e correlaon: -1
    - Perfectly posiv e correlaon: +1
- No relaonship be tween variables: 0
  Number reflects how strong the correlaon is.
- Correlaon does not mean c ausaon.
  - A much stronger relaonship is r equired to show causaon.

## <u>View All</u> <u>View Keyframes</u>

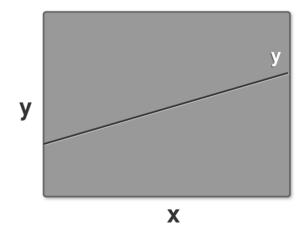
# Correlation: whether variables move together or in different directions

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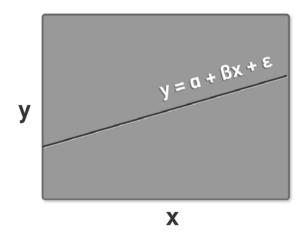
# Regression

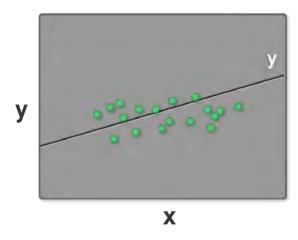
- Measure of change associated with one variable and its effect on another
- E.g., how much interest rates affect mortgage applicaons

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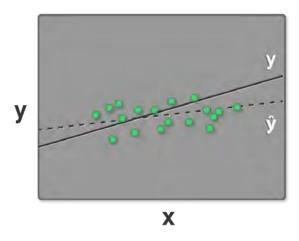


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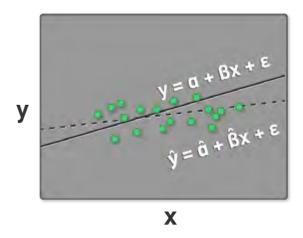




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## **Linear Regression Assumptions**

- 1. Relaonship be tween X and Y is linear.
- 2. If there is more than one X variable, they are not correlated.
- 3. The error terms (distance from data point to predicted line):
  - Have zero mean and constant variance (no heteroscedascity)
  - Are independent (no serial correlaon)
  - Are normally distributed

## **Regression Measurements**

- F-statistic: measures if we have confidence in the equaon
  - Should have **p-value** (likelihood of an error) of less than 0.05
- R-squared (R<sup>2</sup>): measures percent of variaon in Y v ariable explained by X variables
- Coefficient: measures relaonship be tween X and Y, or measures intercept
- T-statistic: measures if we have confidence in the coefficient of a variable
  - Should have p-value of less than 0.05 (95% confidence)

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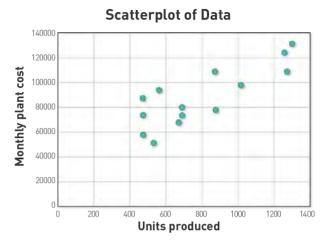
#### p-Values

- 90% confidence = 0.10 p-value
- 99% confidence = 0.01 p-value
- 95% confidence = 0.05 p-value

#### **Univariate Linear Regression**

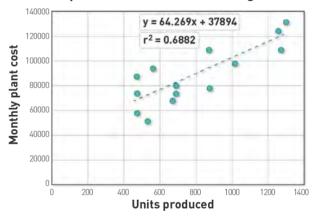
- This regression has only one X variable.
- Excel can quickly generate these results from the graphing package.
- Trend lines, equaons, and R <sup>2</sup> values can be added to sca erplots.
- This does not generate stas c al confidence levels.

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# Scatterplot of Data with Linear Regression



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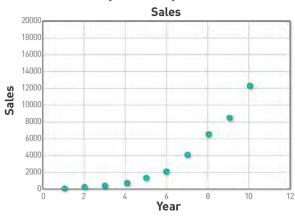
# **Fixed Costs and Variable Costs**

- Fixed costs: expenses paid by factory independent of business acvity
- Variable costs: costs that vary depending on factory's producon v olume

#### **Exponential Regression**

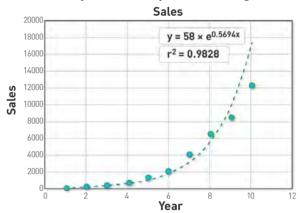
- Not all data is linear.
- Nonlinear pa erns can be made evident by generang a sc a erplot.
- Exponenal gr owth is a form on nonlinear behavior.
  - E.g., Annual sales data for an organizaon 5 of 9

# **Scatterplot of Exponential Data**



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# **Scatterplot with Exponential Regression**



#### Multivariate Regression

- Mulple X v ariables
- No sca erplots
- Form of a mulv ariate equaon:

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + ... + \varepsilon$$

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## Results of a Multivariate Regression

Regressio	n Statistics				
Mulple R	0.803398744				
$R^2$	0.645449542				
Adjusted R <sup>2</sup>	0.57453945				
Standard Error	1252.763898				
Observaons	19	_			
ANOVA					
	df	SS	MS	F	Significance F
Regression	3	42856229.89	14285409.96	9.102365067	0.001126532
Residual	15	23541260.74	1569417.383		
Total	18	66397490.63			
	Coefficients	Standard Error	t Stat	P-value	
Intercept	35102.90045	1837.226911	19.10645889	6.11198E-12	
A Made	2.065953296	1.664981779	1.240826369	0.23372682	
B Made	4.176355531	1.681252566	2.484073849	0.025287785	
C Made	4.790641037	1.789316107	2.677358695	0.017222643	
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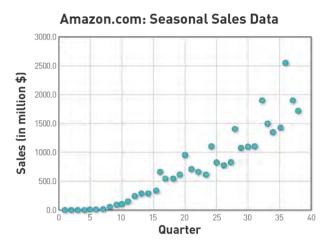
# General Conclusions

- We have a significant equaon.
- It explains 64–65% of change in producon costs.
- We have confidence in our intercept (fixed cost).
- We have confidence in variable costs for B and C.

#### Simple Time Series: Moving Average

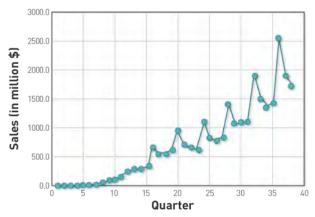
- Seasonality: when data experiences regular changes that occur every year
- Examples:
  - Holiday sales in the retail industry
  - Home sales during summer
  - Gasoline sales during summer vacaons
- Moving average: reduces effect of seasonality so true pa erns can be seen

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## Amazon.com: Seasonal Data With Connected Data



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# Amazon.com: Results of a Moving Average Model

