《人工智能与智能驾驶基础》期末大作业

路径规划与轨迹跟踪
说明文档及源代码

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软件：MATLAB 2021b

时间：2021 年 12 月 28 日

目录

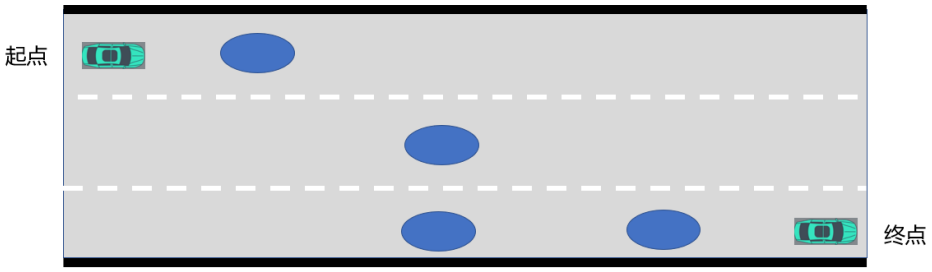
第一部分：说明文档

一． 题目要求

1．根据要求建立道路环境和静态障碍物信息；

2．利用任意一种路径规划方法进行规划；

3．利用车辆质点模型和PID控制器完成轨迹跟踪，到达终点；（注1：可以选其他车辆模型和其他控制器完成设计任务）（注2：除了完成轨迹的跟踪，还需要完成设定车速的跟踪【设定车速自定】）



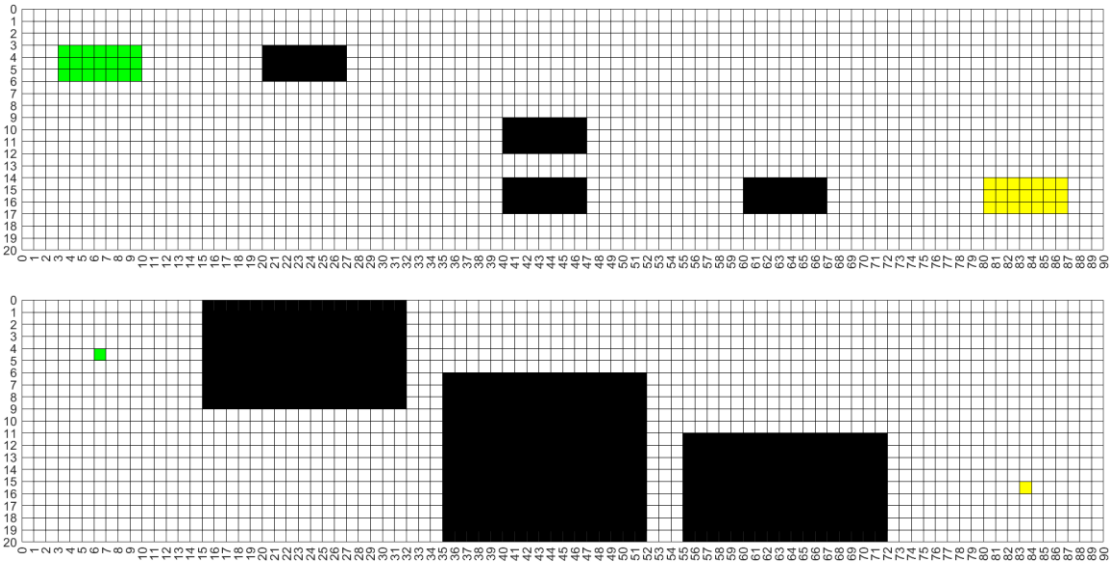
二． 路径规划部份

1. 环境建模

栅格地图下，我国机动车道宽度标准 3.5-3.75 米，车长一般为 3.8-4.3 米，车宽 1.8-2 米，取车宽为 1.8 米，车长 4.2 米，车道宽为 3.6 米，栅格地图一格代表 0.6 米，因此小车占据栅格地图的面积为 3*7 格，车道宽为 6 格，三车道总宽为 18 格，

最小半径 4 格，对障碍物进行膨胀：

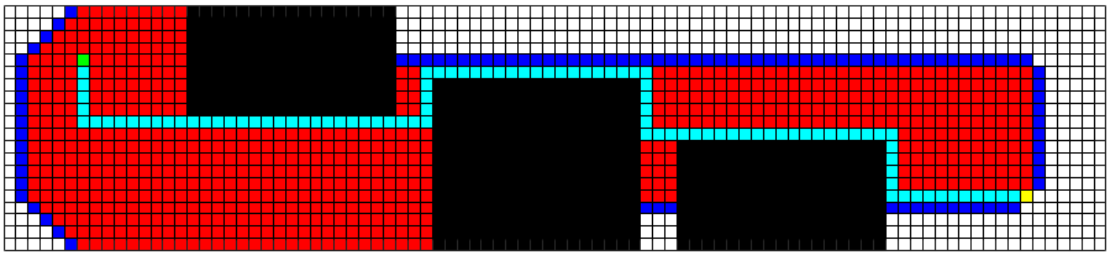
$$\sqrt{3^2 \times 7^2}$$



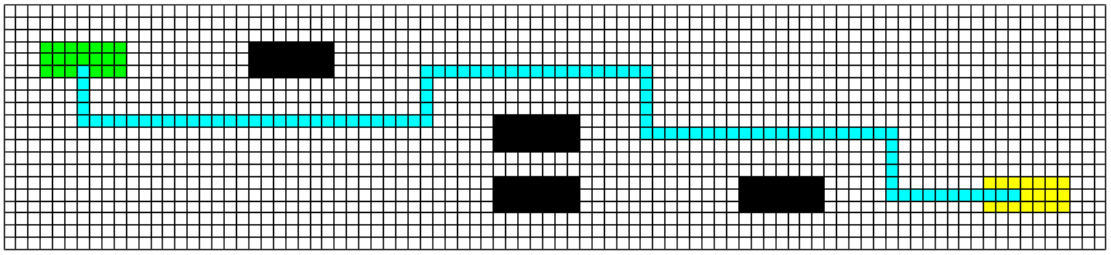
2. 路径规划

分别采用 A*和 Dijkstra 算法进行路径规划，结果如下：

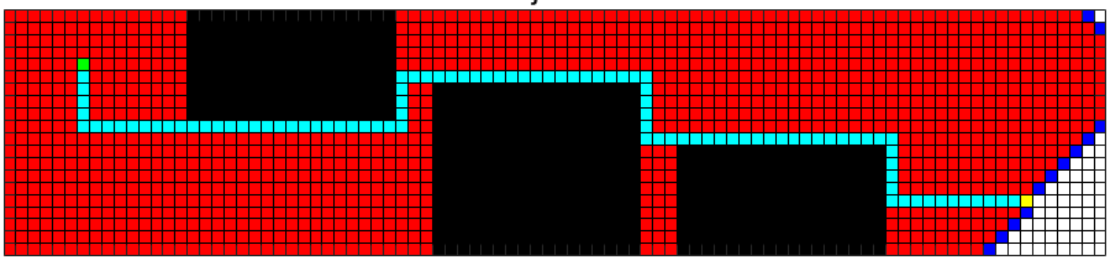
A*



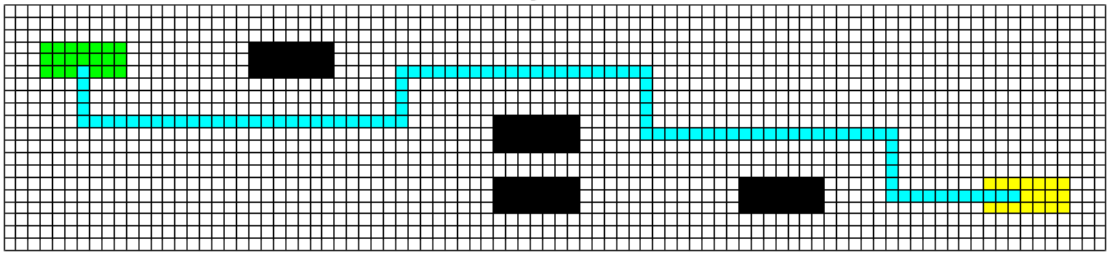
A*



Dijkstra



Dijkstra



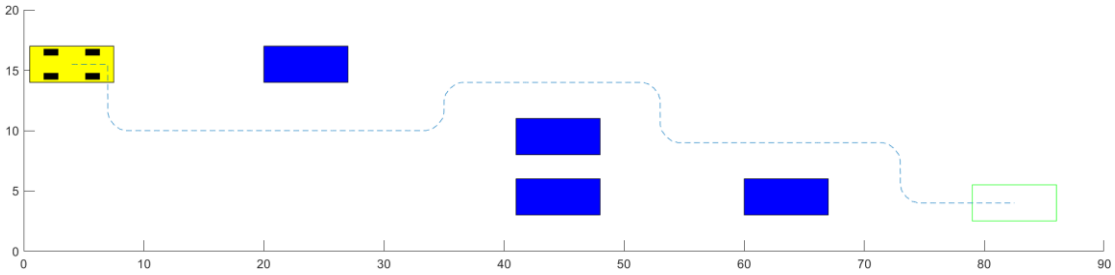
从迭代次数上可以看出，A*的效率比 Dijkstra 高：

```
A* plan succeeded! iteration times: 944 path length: 96
Dijkstra plan succeeded! iteration times: 1449 path length: 96
```

三． 轨迹跟踪

1. 建立场景

为方便动画展示，将栅格地图中的信息移植到像素坐标系下。对每段路径分别设定目标车速。



2. 运动学模型：以后轮为原点的单车模型（Bicycle Model）

模型有如下假设：

1）不考虑车辆在平坦路面上行驶，忽略垂直方向(Z 轴方向)的运动；

2) 假设车辆左右侧轮胎在任意时刻都拥有相同的转向角度和转速，即忽略阿克曼转向性质，这样车辆的左右两个轮胎的运动可以合并为一个轮胎来描述；

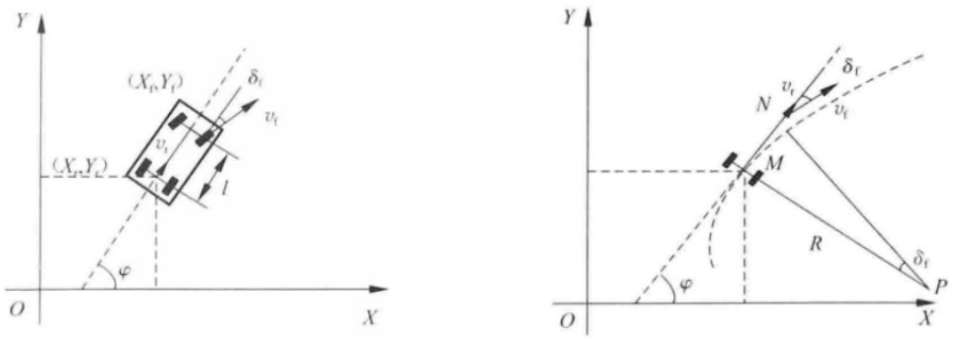
3）假设车辆行驶速度变化缓慢，忽略前后轴载荷的转移；

4）假设车身和悬架系统都是刚性系统；

5）假设轮胎为刚性，忽略轮胎侧偏特性；

6）不考虑载荷的左右转移；

模型示意图：



在模型中，(X_r, Y_r)为车辆后轴的轴心坐标，(X_f, Y_f)为车辆前轴的轴心坐标，v_r为后轴中心的速度，v_f为前轴中心的速度，l为轴距，在车辆转向过程中R为车辆转向半径，P为转向的瞬时转动中心，M为后轴中心。

在后轴轴心(X_r, Y_r)处，速度为：

$$v_r = \dot{X}_r cos\varphi + \dot{Y}_r sin\varphi$$

前后轴的运动学约束为：

$$\begin{cases} \dot{X}_f \sin(\varphi + \delta_f) - \dot{Y}_f \cos(\varphi + \delta_f) = 0 \\ \dot{X}_r sin\varphi - \dot{Y}_r cos\varphi = 0 \end{cases}$$

前两式联立可得:

$$\begin{cases}\dot{X}_r = v_r cos\varphi \\ \dot{Y}_r = v_r sin\varphi\end{cases}$$

根据前后轮的几何关系有:

$$\begin{cases}X_f = X_r + lcos\varphi \\ Y_f = Y_r + lsin\varphi\end{cases}$$

将前三组式子联立，可得:

$$\begin{cases}\omega = \dfrac{v_r}{l}tan\delta_f \\ R = \dfrac{v_r}{\omega} \\ \delta_f = \arctan\left(\dfrac{l}{R}\right)\end{cases}$$

由此可得车辆运动学模型:

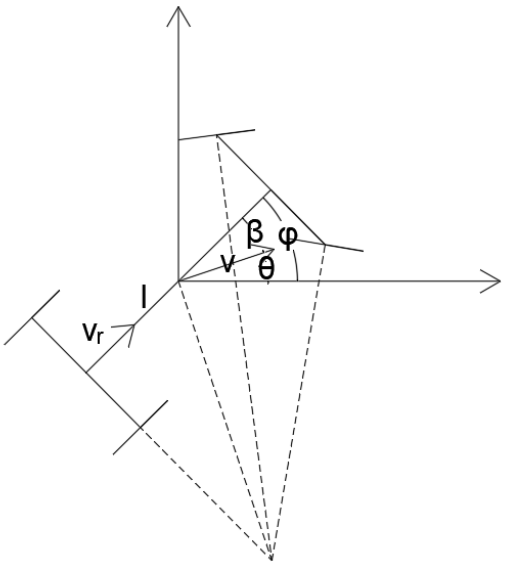
$$\begin{bmatrix}\dot{X}_r \\ \dot{Y}_r \\ \dot{\varphi}\end{bmatrix} = \begin{bmatrix}cos\varphi \\ sin\varphi \\ \dfrac{tan\delta_f}{l}\end{bmatrix} v_r$$

在无人驾驶车的路径跟踪控制过程中，常以(v_r, ω)作为控制量，则车辆的运动学模型为:

$$\begin{bmatrix}\dot{X}_r \\ \dot{Y}_r \\ \dot{\varphi}\end{bmatrix} = \begin{bmatrix}cos\varphi \\ sin\varphi \\ 0\end{bmatrix} v_r + \begin{bmatrix}0 \\ 0 \\ 1\end{bmatrix} \omega$$

3. 控制方法：PID 控制法

由于车辆不能进行平移，对轨迹的跟踪包括三点：姿态（车辆横摆角）跟踪，车速跟踪（大小、方向），位置跟踪。首先考虑车辆姿态，绘图如下



v：车辆质心速度
v_r：车辆后轮速度
l：轴距
β：质心侧偏角
θ：航向角
φ：横摆角

对后轴与质心有运动学约束:

$$vcos\beta = v_r$$

$$vsin\beta = \frac{\omega l}{2}$$

可得：

$$\omega = \frac{2v\sin\beta}{l}$$

航向角：

$$\theta = \text{atan}\left(\frac{v_y}{v_x}\right)$$

β、θ、φ之间存在约束：

$$\beta = \theta - \varphi$$

车辆横摆角：

$$\varphi = \int_0^t \omega\, dt$$

可知φ不再发生改变当且仅当$\omega = 0$，此时有$\beta = \theta - \varphi = 0$即$\theta = \varphi$，此时航向角与横摆角相同，车辆沿直线行驶。角度的变化仅取决于v_x与v_y两个参量，故速度函数与横摆角函数一一对应，不需要对其特别追踪。

其次考虑车速与位置追踪。设车辆当前坐标为$(x \quad y \quad v_x \quad v_y)^T$，将参考点设置于预定轨迹前视距离处一点，设其坐标及目标速度为$(x_t \quad y_t \quad v_{tx} \quad v_{ty})^T$，即可知当前位置与待跟踪位置之误差：

$$er = (er_x \quad er_y)^T = (x_t - x \quad y_t - y)^T$$

将速度误差方向设置为误差方向即可完成对位置的跟踪，即：

$$dv_{des} = \frac{1}{|er|} er$$

车速方面将参考点预设车速作为目标车速，

$$dv = dv_{des} * |v_{tx} \quad v_{ty}| = \frac{|v_{tx} \quad v_{ty}|}{|er|} er$$

可以计算得到当前速度与目标速度在 x 与 y 方向上的误差：

$$er_v = \frac{|v_{tx} \quad v_{ty}|}{|er|} er - (v_x \quad v_y)^T$$

通过 PID 即可同时完成了对姿态、速度与位置的跟踪。

即：

$$\delta v = k_p er_v(k) + k_i \sum_{i=0}^{k} er_v(i) + k_d(er_v(k) - er_v(k-1))$$

考虑到对车辆的控制一般是通过控制转向盘与加速踏板完成，下面推导由转向盘与加速踏板和加速度（误差）之间的关系

设前轮转角为δ，δ可以通过转向盘控制。由刚体运动学约束：

$$v_f \sin\delta = 2v\sin\theta$$
$$v_f \cos\delta = v\cos\theta$$

得：

$$\tan\delta = 2\tan\theta$$

设前轮转动角速度为ω_f后轮加速度为 a

$$d\varphi = +\omega_f dt$$

$$er_v = \frac{dv}{dt} = \frac{d\left(v\begin{bmatrix}\cos\theta \\ \sin\theta\end{bmatrix}\right)}{dt} = a\begin{bmatrix}\cos\theta \\ \sin\theta\end{bmatrix} + v\frac{d\theta}{dt}\begin{bmatrix}-\sin\theta \\ \cos\theta\end{bmatrix}$$

$$sec\delta^2 \frac{d\delta}{dt} = 2sec\theta^2 \frac{d\theta}{dt}$$

得:

$$er_v = a\begin{bmatrix} cos\theta \\ sin\theta \end{bmatrix} + v\omega_f \frac{sec\delta^2}{2sec\theta^2}\begin{bmatrix} -sin\theta \\ cos\theta \end{bmatrix}$$

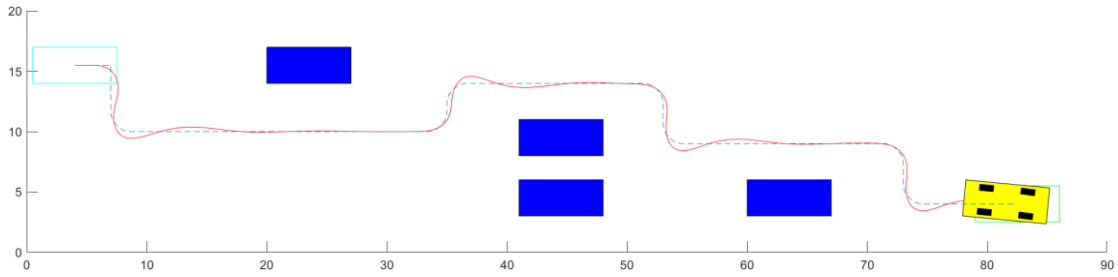
故可以通过er_v推得δ、θ

$$a = \frac{er_x cos\theta + er_y sin\theta}{sin2\theta}$$

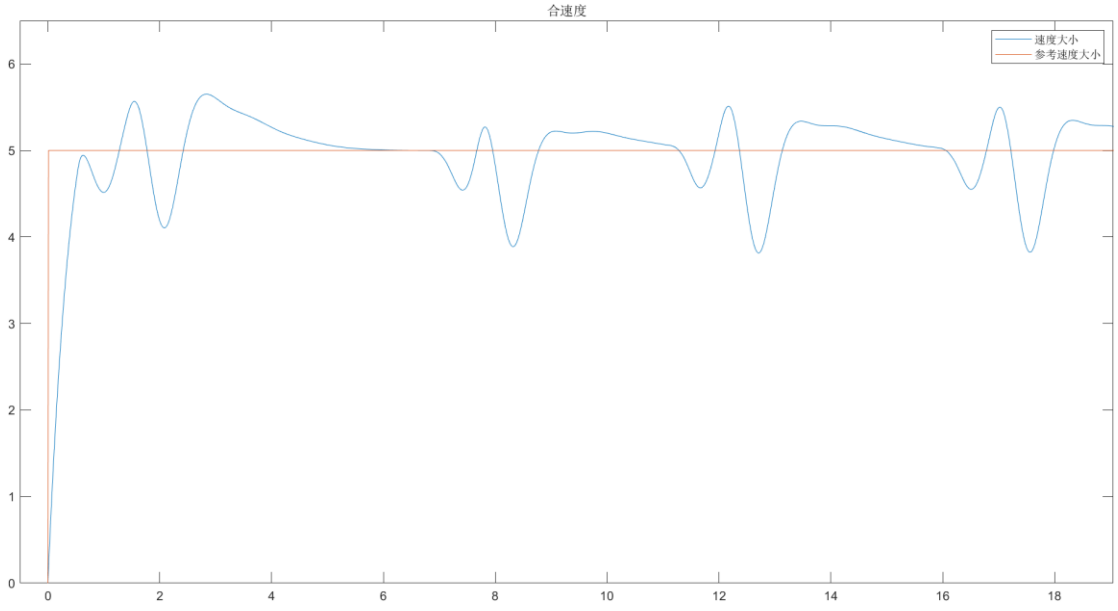
$$\delta = atan\frac{2(er_x cos\theta - er_y sin\theta)}{vcos\theta^2}$$

四． 最终结果

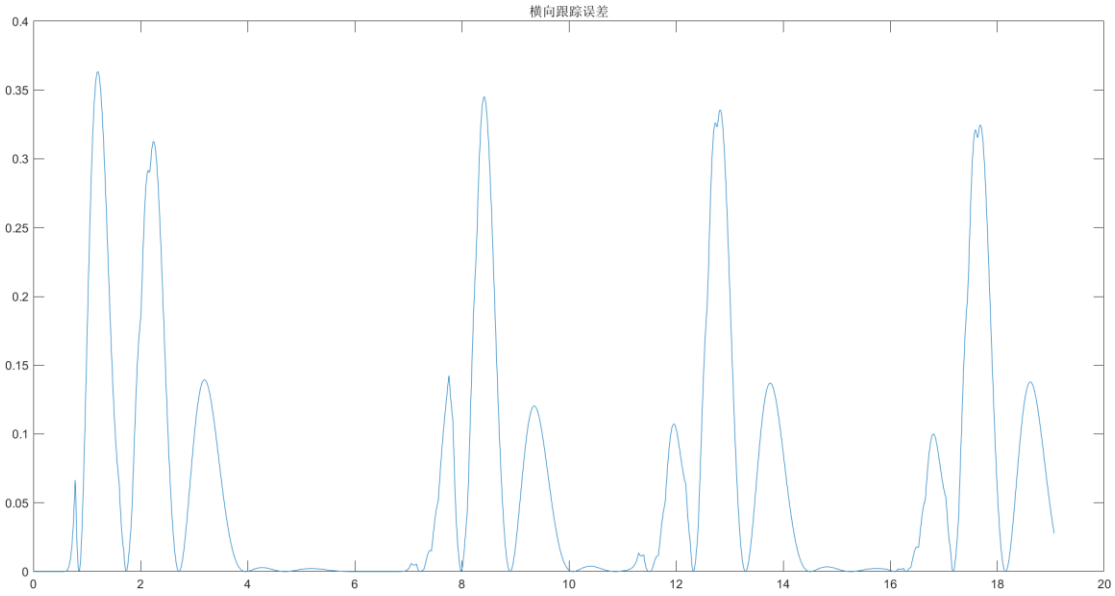
1. P(5M/S)



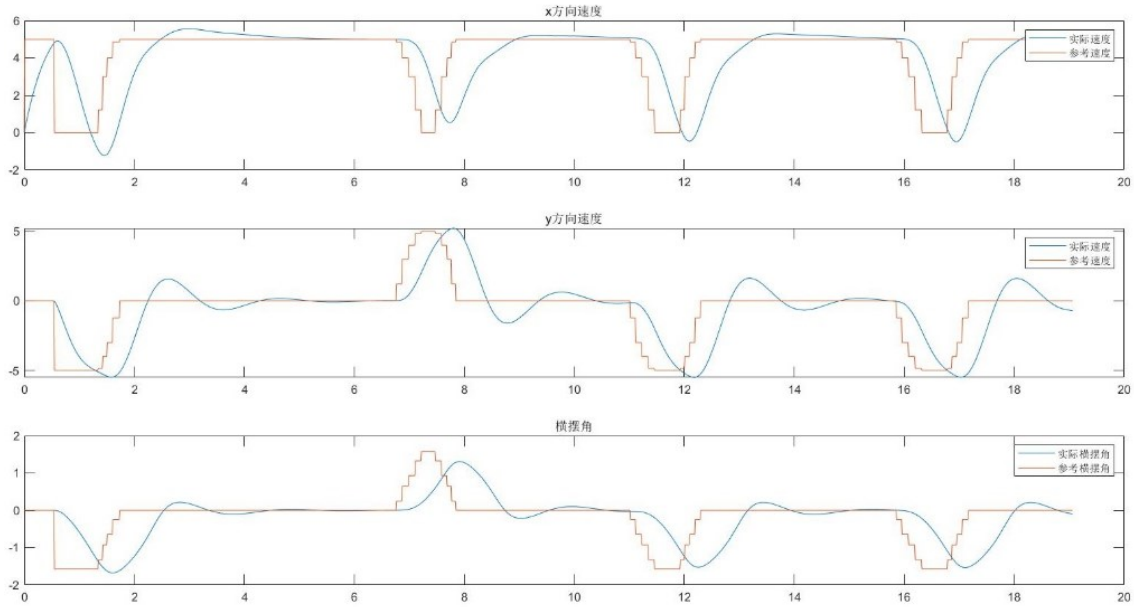
路径跟踪结果



速度跟踪结果

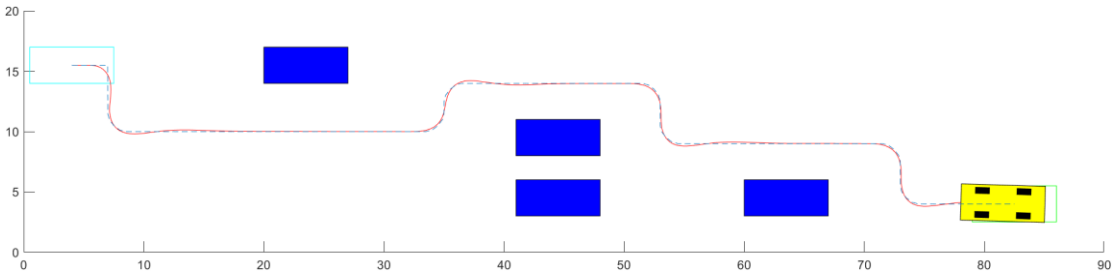


横向跟踪误差

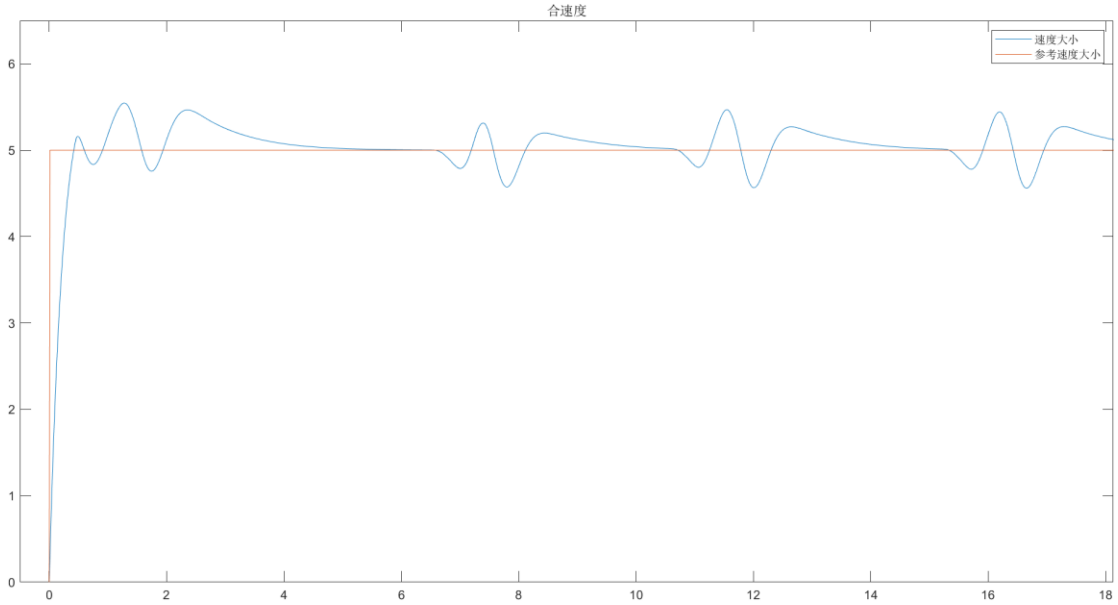


速度分量跟踪误差

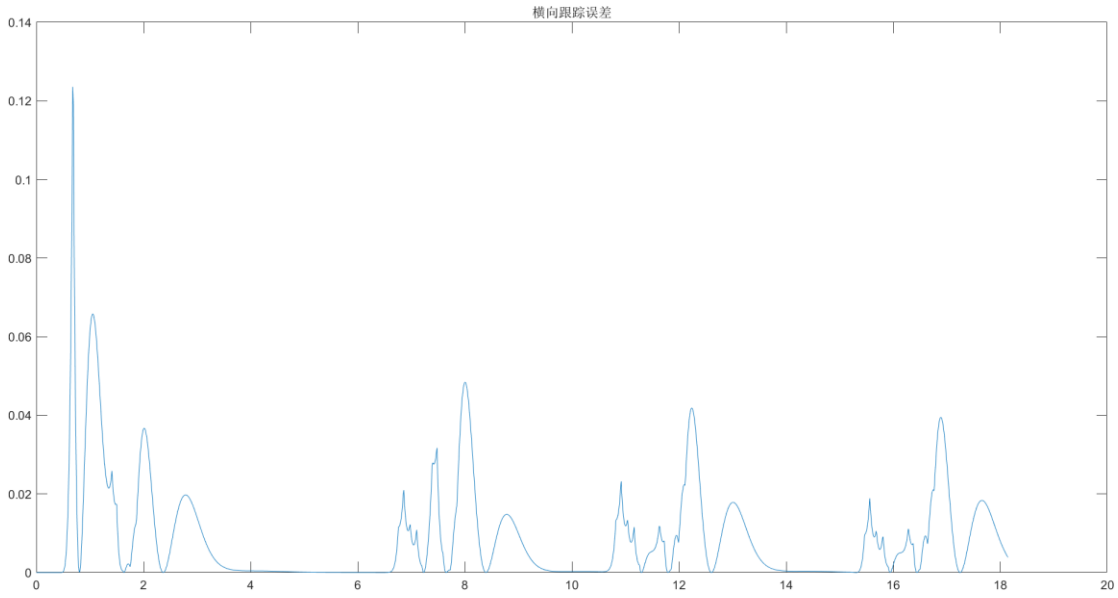
2. PI(5M/S)



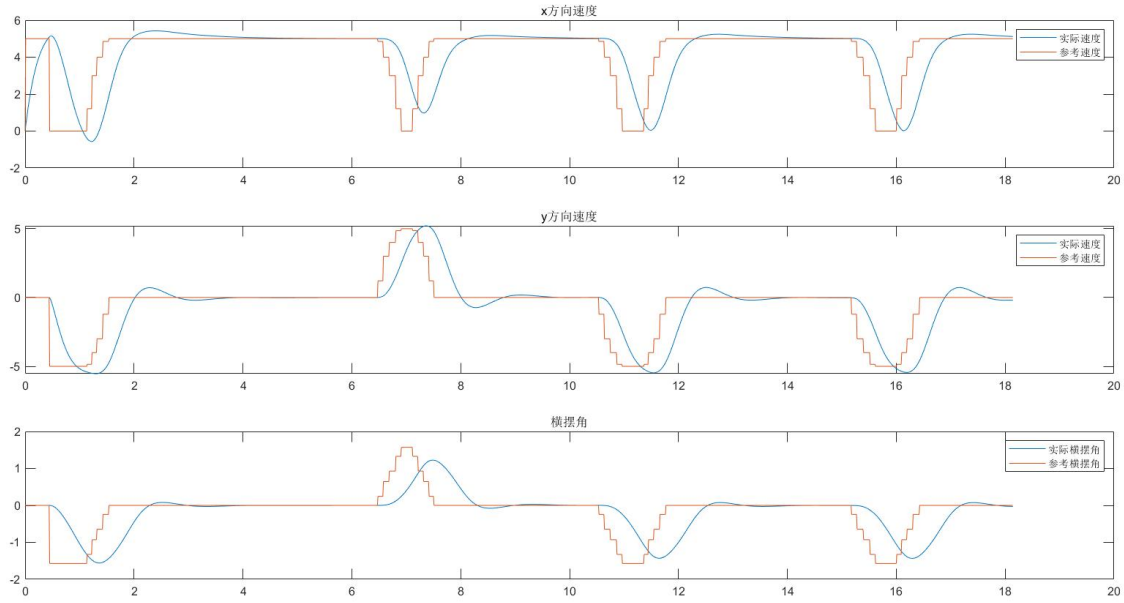
路径跟踪结果



速度跟踪结果

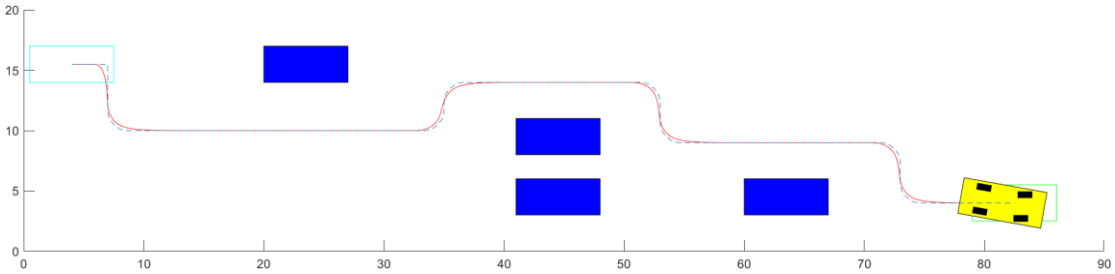


横向跟踪误差

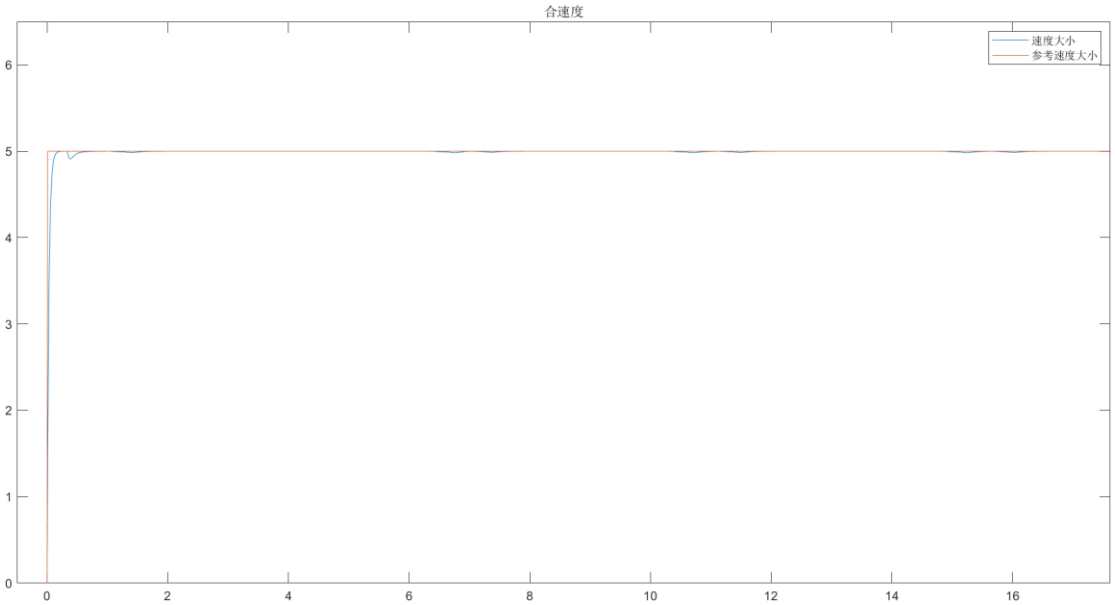


速度分量跟踪误差

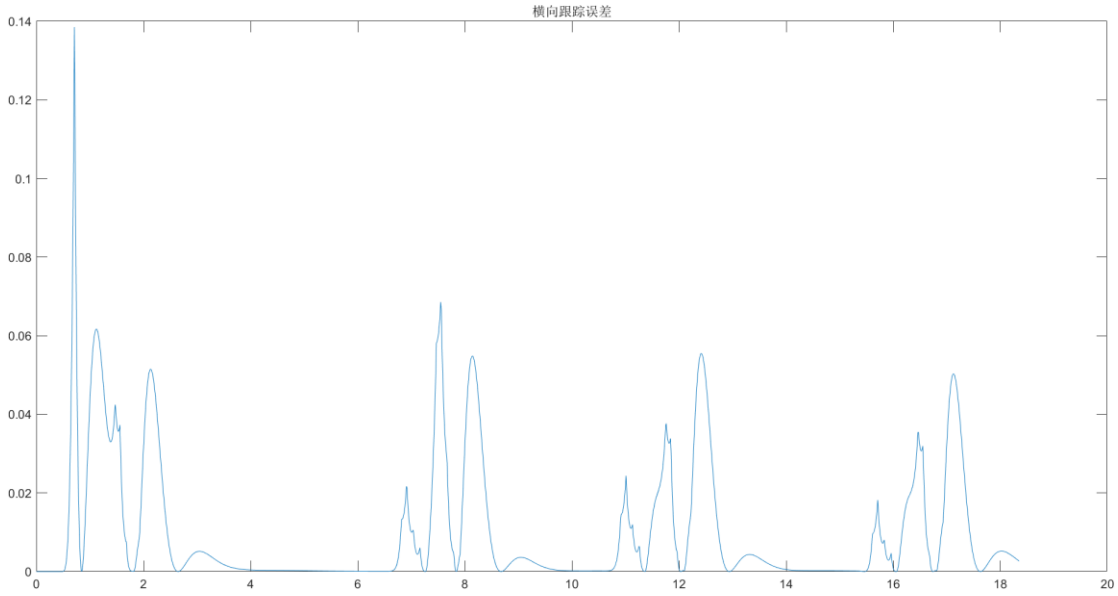
3. PID(5M/S)



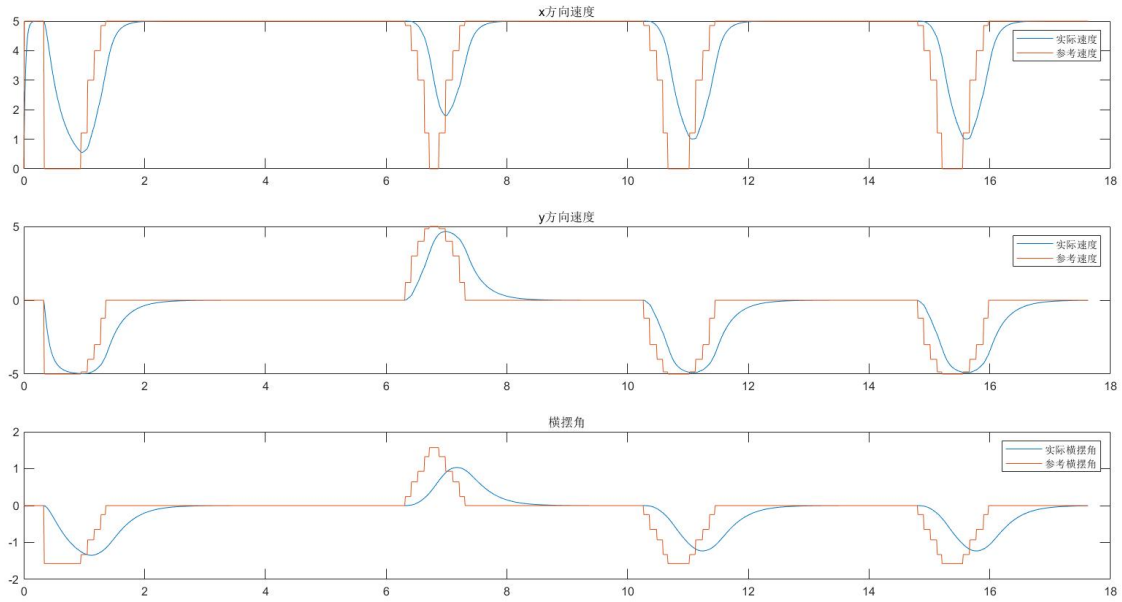
路径跟踪结果



速度跟踪结果

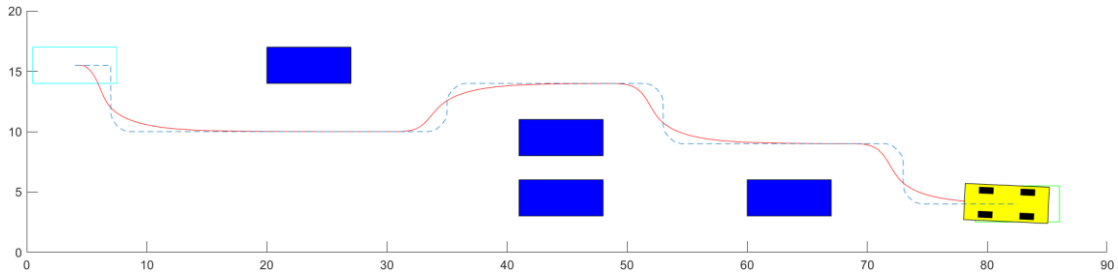


横向跟踪误差

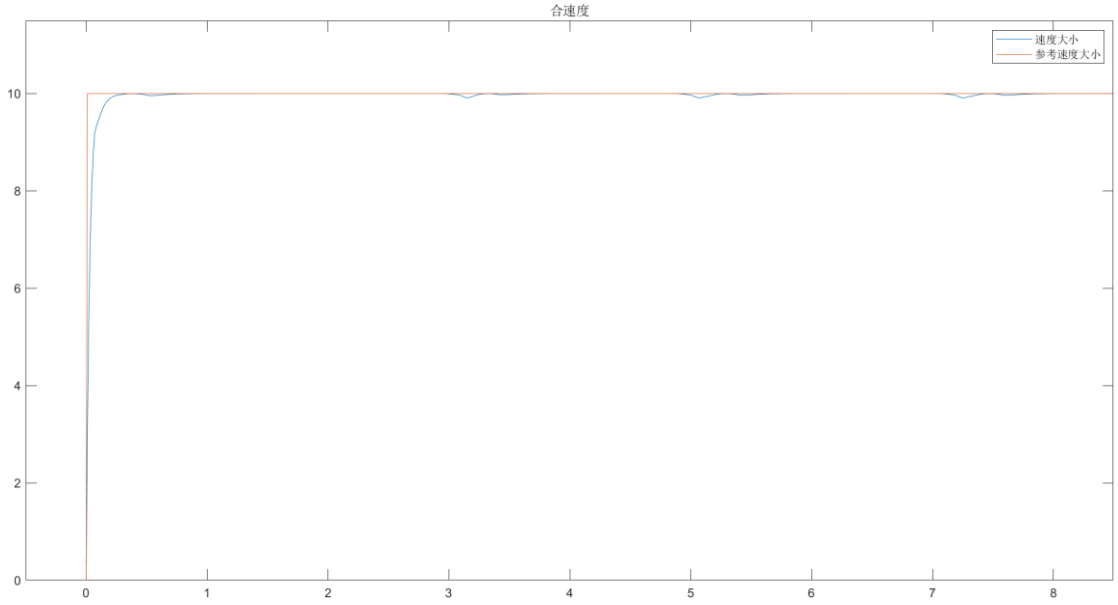


速度分量跟踪误差

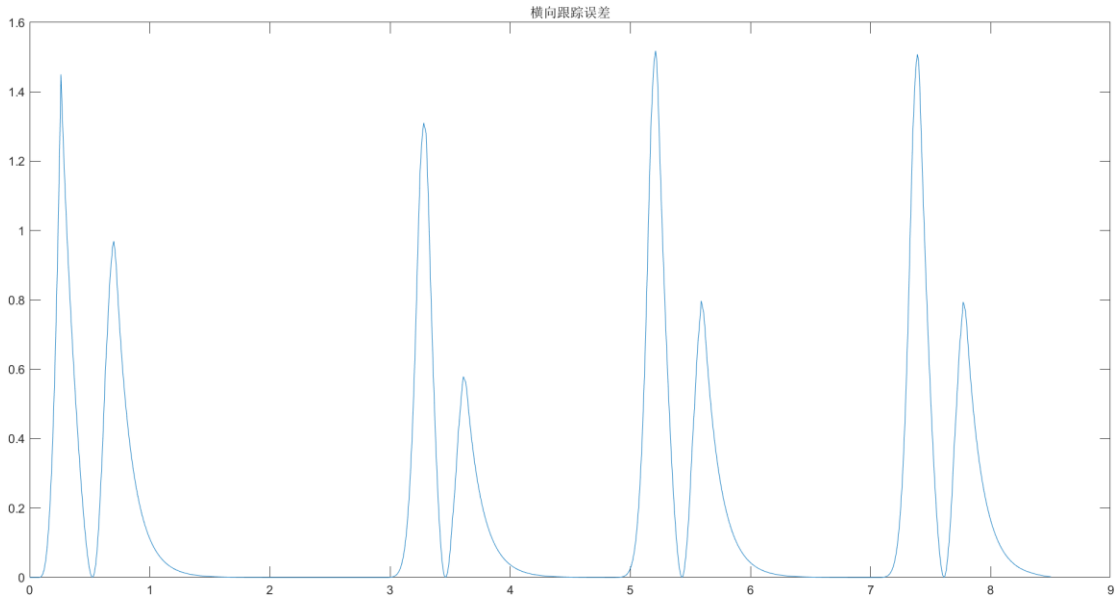
4. PID(10M/S)



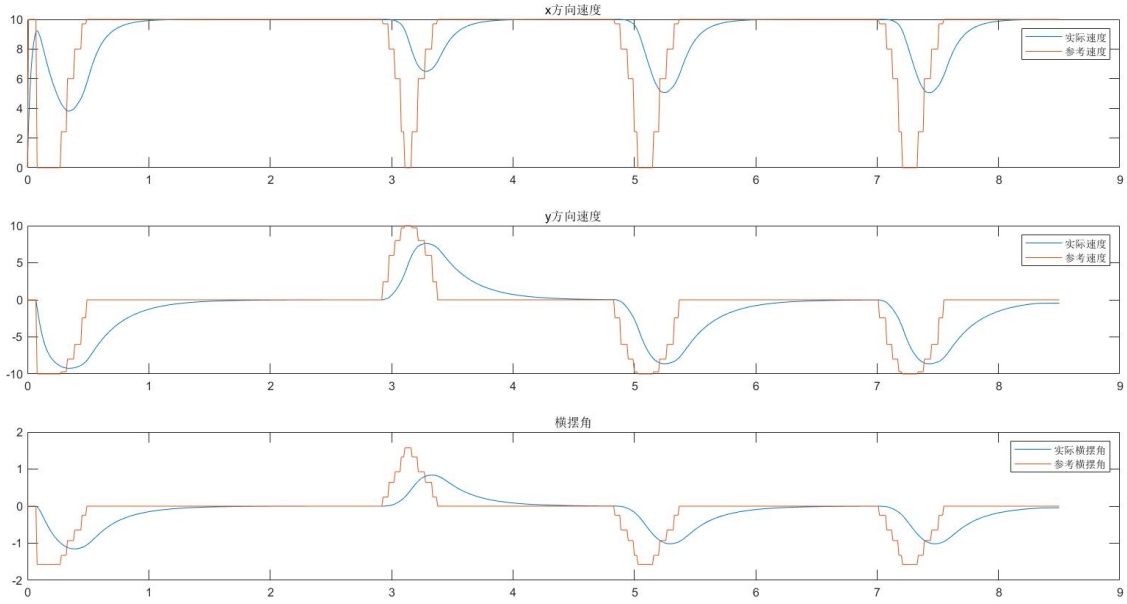
路径跟踪结果



速度跟踪结果

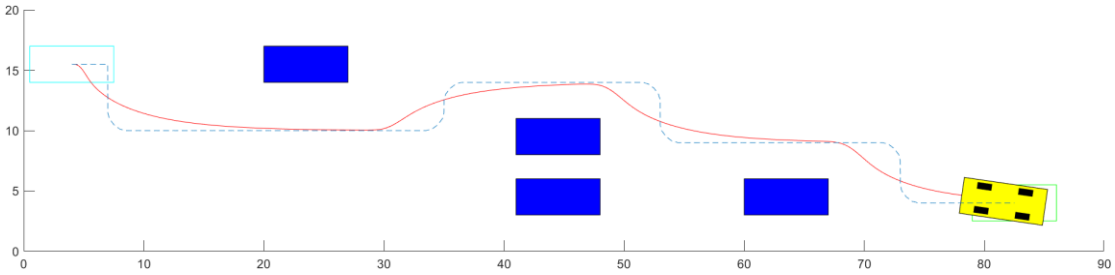


横向跟踪误差

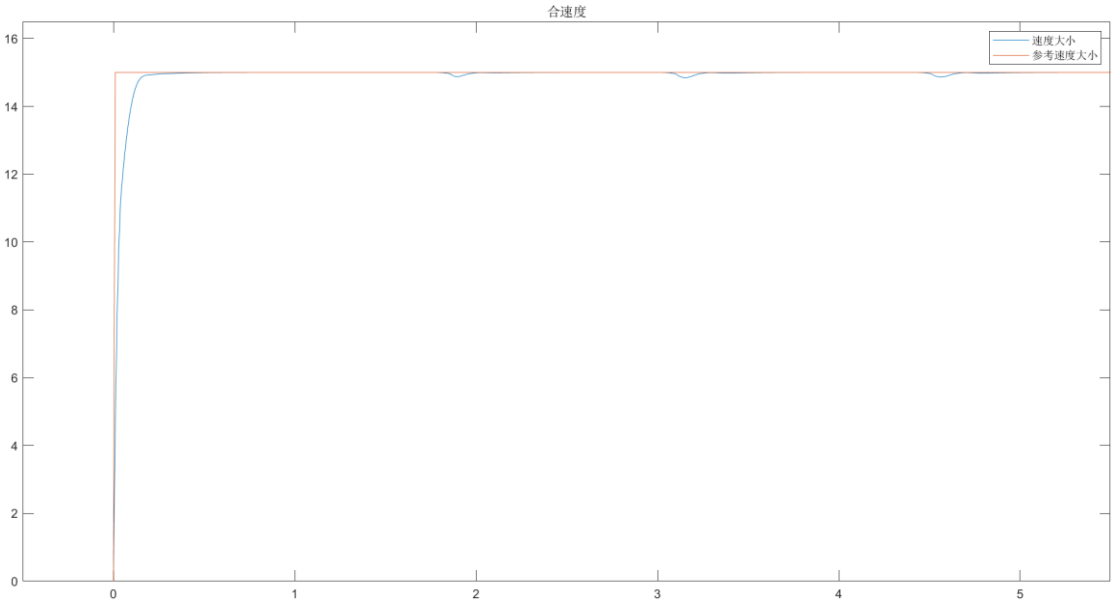


速度分量跟踪误差

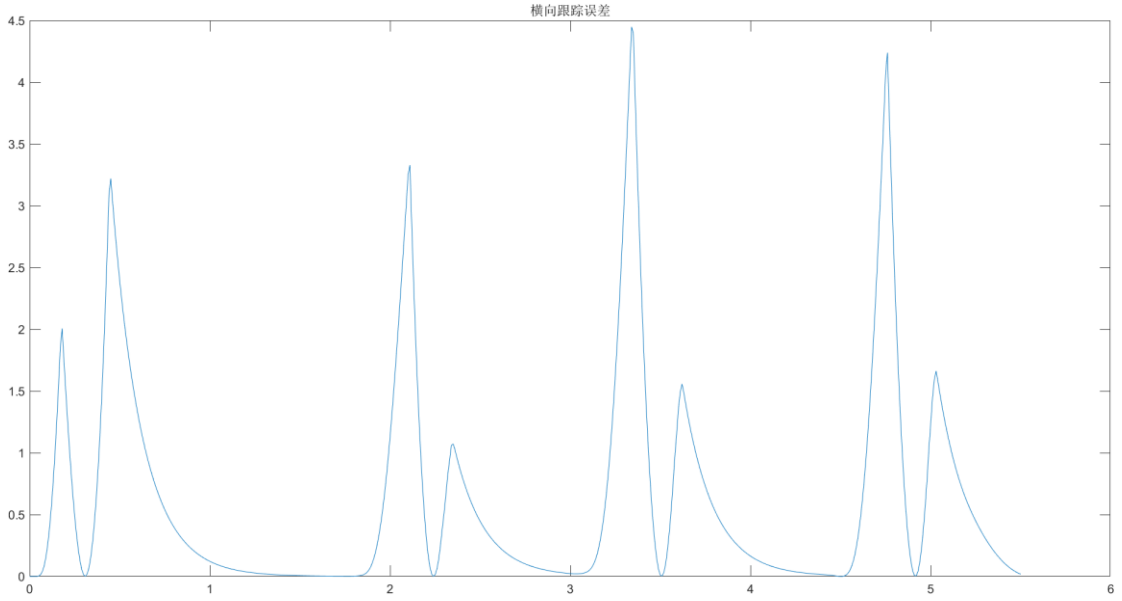
5. PID(15M/S)



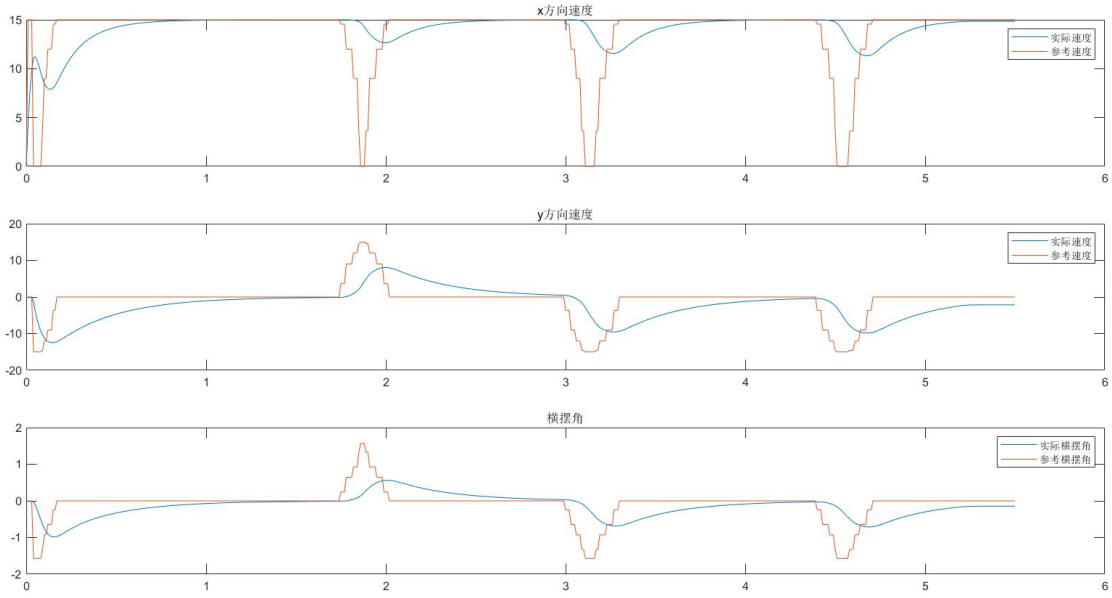
路径跟踪结果



速度跟踪结果



横向跟踪误差



速度分量跟踪误差

第二部分：源代码

1. 路径规划部分

[1]. A*

```
function [path, iteration_times,map] = Astar(Map, origin, destination)
% record the iteration times
iteration_times = 0;

%set the scale factor of Heuristic function
Heuristic_scale = 1;

% identifier setting
Obstacle = 2;
Origin = 3;
Destination = 4;
Finished = 5;
Unfinished = 6;
Path = 7;

% color setting
white = [1,1,1];
black = [0,0,0];
green = [0,1,0];
yellow = [1,1,0];
red = [1,0,0];
blue = [0,0,1];
cyan = [0,1,1];
color_list = [white; black; green; yellow; red; blue; cyan];
colormap(color_list);


% listes initialize
MapSize = size(Map);

% create map
logical_map = logical(Map);
map = zeros(MapSize(1),MapSize(2));
map(logical_map) = 2;
map(~logical_map) = 1;

% create node_g_list
node_g_list = Inf(MapSize(1), MapSize(2));
node_g_list(origin(1), origin(2)) = 0;  % set the node_cost of the origin node zero

% create node_f_list
node_f_list = Inf(MapSize(1), MapSize(2));
node_f_list(origin(1), origin(2)) = Heuristic(origin, destination, Heuristic_scale);
```

```
% create parent_list
parent_list = zeros(MapSize(1), MapSize(2));

destination_index = sub2ind(MapSize, destination(1), destination(2));
origin_index = sub2ind(MapSize, origin(1), origin(2));

Open_list = [origin_index];

plan_succeeded = false;
```

```
while true
    iteration_times = iteration_times+1;
    map(origin(1), origin(2)) = Origin;
    map(destination(1), destination(2)) = Destination;

    % uncomment this part to show the animation, but it will spend more time during algorithm running.
    image(0.5,0.5,map);
    grid on;
    title('A*');
    set(gca,'xtick',0:1:MapSize(2),'xticklabel',[],'ytick',0:1:MapSize(1),'yticklabel',[]);
    set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
    axis image;
    drawnow limitrate;

    [min_node_cost, current_node_index] = min(node_f_list(:));
    if(min_node_cost == inf || current_node_index == destination_index)
        plan_succeeded = true;
        break;
    end
    node_f_list(current_node_index) = inf;
    map(current_node_index) = Finished;
    [x,y] = ind2sub(MapSize, current_node_index);
    for k = 0:3 % four direction
        if(k == 0)
            adjacent_node = [x-1,y];
        elseif (k == 1)
            adjacent_node = [x+1,y];
        elseif (k == 2)
            adjacent_node = [x,y-1];
        elseif(k == 3)
            adjacent_node = [x,y+1];
        end
```

```
       if((adjacent_node(1) > 0 && adjacent_node(1) <= MapSize(1)) ...
               && (adjacent_node(2) > 0 && adjacent_node(2) <= MapSize(2)))
           % make sure the adjacent_node don't exceeds the map
           if(map(adjacent_node(1),adjacent_node(2)) ~= Obstacle ...
                   && map(adjacent_node(1),adjacent_node(2)) ~= Finished)
               if(node_g_list(adjacent_node(1),adjacent_node(2)) > min_node_cost + 1 )
                   node_g_list(adjacent_node(1),adjacent_node(2)) = node_g_list(current_node_index) + 1;
                   node_f_list(adjacent_node(1),adjacent_node(2)) = node_g_list(adjacent_node(1), ...
                       adjacent_node(2)) + Heuristic(adjacent_node, destination, Heuristic_scale);
                   %uncomment this line to change Astar to Greedy algorithm
                   %node_f_list(adjacent_node(1),adjacent_node(2)) = Heuristic(adjacent_node, destination, Heuristic_scale);

                   if(map(adjacent_node(1),adjacent_node(2)) == Origin)
                       parent_list(adjacent_node(1),adjacent_node(2)) = 0;
                       % Set the parent 0 if adjacent_node is the origin.
                   else
                       parent_list(adjacent_node(1),adjacent_node(2)) = current_node_index;
                       %Set the parent current_node_index
                   end
                   if(map(adjacent_node(1),adjacent_node(2)) ~= Unfinished)
                       map(adjacent_node(1),adjacent_node(2)) = Unfinished;
                       % Mark the adjacent_node as unfinished
                   end
               end
           end
       end
   end
end
```

```
if(plan_succeeded)
    path = [];
    node = destination_index;
    while(parent_list(node) ~= 0)
        path = [parent_list(node), path];
        node = parent_list(node);
    end

    for k = 2:size(path,2)
        map(path(k)) = 7;
        image(0.5,0.5,map);
        grid on;
        title('A*');
        set(gca,'xtick',0:1:MapSize(2),'xticklabel',[],'ytick',0:1:MapSize(1),'yticklabel',[]);
        set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
        axis image;
        drawnow limitrate;
    end
else
    path = [];
end
end
```

[2]. Dijkstra

```
function [path, iteration_times,map] = Dijkstra(Map, origin, destination)
iteration_times = 0;
%% identifier setting
Obstacle = 2;
Origin = 3;
Destination = 4;
Finished = 5;
Unfinished = 6;
Path = 7;

% color setting
white = [1,1,1];
black = [0,0,0];
green = [0,1,0];
yellow = [1,1,0];
red = [1,0,0];
blue = [0,0,1];
cyan = [0,1,1];
color_list = [white; black; green; yellow; red; blue; cyan];
colormap(color_list);

% listes initialize
MapSize = size(Map);

% create map
logical_map = logical(Map);
map = zeros(MapSize(1),MapSize(2));
map(logical_map) = 2;
map(~logical_map) = 1;
```

```
% create node_cost_list
node_cost_list = Inf(MapSize(1), MapSize(2));
node_cost_list(origin(1), origin(2)) = 0;   % set the node_cost of the origin node zero

% create parent_list
parent_list = zeros(MapSize(1), MapSize(2));

destination_index = sub2ind(MapSize, destination(1), destination(2));
origin_index = sub2ind(MapSize, origin(1), origin(2));

plan_succeeded = false;

while true
    iteration_times = iteration_times+1;
    map(origin(1), origin(2)) = Origin;
    map(destination(1), destination(2)) = Destination;

    % uncomment this part to show the animation
    image(0.5,0.5,map);
    grid on;
    title('Dijkstra');
    set(gca,'xtick',0:1:MapSize(2),'xticklabel',[],'ytick',0:1:MapSize(1),'yticklabel',[]);
    set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
    axis image;
    drawnow;

    [min_node_cost, current_node_index] = min(node_cost_list(:));
    if(min_node_cost == inf || current_node_index == destination_index)
        plan_succeeded = true;
        break;
    end
    node_cost_list(current_node_index) = inf;
    map(current_node_index) = Finished;
    [x,y] = ind2sub(MapSize, current_node_index);
    for k = 0:3 % four direction
        if(k == 0)
            adjacent_node = [x-1,y];
        elseif (k == 1)
            adjacent_node = [x+1,y];
        elseif (k == 2)
            adjacent_node = [x,y-1];
        elseif(k == 3)
            adjacent_node = [x,y+1];
        end
```

```
if(plan_succeeded)
    path = [];
    node = destination_index;
    while(parent_list(node) ~= 0)
        path = [parent_list(node), path];
        node = parent_list(node);
    end

    for k = 2:size(path,2)
        map(path(k)) = 7;
        image(0.5,0.5,map);
        grid on;
        title('Dijkstra');
        set(gca,'xtick',0:1:MapSize(2),'xticklabel',[],'ytick',0:1:MapSize(1),'yticklabel',[]);
        set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
        axis image;
        drawnow;
    end
else
    path = [];
end
end
```

```
        if((adjacent_node(1) > 0 && adjacent_node(1) <= MapSize(1)) && ...
                (adjacent_node(2) > 0 && adjacent_node(2) <= MapSize(2)))
            % make sure the adjacent_node don't exceeds the map
            if(map(adjacent_node(1),adjacent_node(2)) ~= Obstacle && ...
                    map(adjacent_node(1),adjacent_node(2)) ~= Finished)
                if(node_cost_list(adjacent_node(1),adjacent_node(2)) > ...
                        min_node_cost + 1)
                    node_cost_list(adjacent_node(1),adjacent_node(2)) = min_node_cost + 1;
                    if(map(adjacent_node(1),adjacent_node(2)) == Origin)
                        parent_list(adjacent_node(1),adjacent_node(2)) = 0;
                        % Set the parent 0 if adjacent_node is the origin.
                    else
                        parent_list(adjacent_node(1),adjacent_node(2)) = current_node_index;
                        %Set the parent current_node_index
                    end
                    map(adjacent_node(1),adjacent_node(2)) = Unfinished;
                    % Mark the adjacent_node as unfinished
                end
            end
        end
    end
end
```

[3]. 建立栅格地图

```
clc
clear

%% 1.建立原始栅格地图
%% 构建颜色MAP图
% identifier setting
Obstacle = 2;
Origin = 3;
Destination = 4;
Finished = 5;
Unfinished = 6;
Path = 7;
```

```
% color setting
white = [1,1,1];
black = [0,0,0];
green = [0,1,0];
yellow = [1,1,0];
red = [1,0,0];
blue = [0,0,1];
cyan = [0,1,1];
color_list = [white; black; green; yellow; red; blue; cyan];
colormap(color_list);

%% 构建栅格地图场景
% 栅格界面大小:行数和列数
rows = 20;
cols = 90;

% 定义栅格地图全域，并初始化空白区域
field = ones(rows, cols);

% 障碍物区域
% obstacle1(4,24)
for i=1:3
    for j=1:7
        field(3+i,20+j)=2;
    end
end
% obstacle2(10,44)
for i=1:3
    for j=1:7
        field(9+i,40+j)=2;
    end
end
```

```
% obstacle3(15,44)
for i=1:3
    for j=1:7
        field(14+i,40+j)=2;
    end
end
% obstacle4(15,64)
for i=1:3
    for j=1:7
        field(14+i,60+j)=2;
    end
end

% 起始点和目标点
% start(4,7)
for i=1:3
    for j=1:7
        field(3+i,3+j)=3;
    end
end
```

```
% goal(15,84)
for i=1:3
    for j=1:7
        field(14+i,80+j)=4;
    end
end
```

```
%% 画栅格图
figure(1);
image(0.5,0.5,field);
grid on;
axis equal;
axis([0,cols,0,rows])
set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
%设置栅格线条的样式（颜色、透明度等）
set(gca,'xtick',0:1:cols,'ytick',0:1:rows)

save('field.mat',"field")
```

```
%% 2.建立抽象栅格地图
%% 对障碍物进行膨胀处理
dilateR=4;
field1 = ones(rows, cols);
% 障碍物区域膨胀
% obstacle1
for i=-dilateR:dilateR
    for j=-2*dilateR:2*dilateR
        field1(5+i,24+j)=2;
    end
end
```

```
% obstacle2
for i=-dilateR:dilateR
    for j=-2*dilateR:2*dilateR
        field1(11+i,44+j)=2;
    end
end
% obstacle3
for i=-dilateR:dilateR
    for j=-2*dilateR:2*dilateR
        field1(16+i,44+j)=2;
    end
end
% obstacle3
for i=-dilateR:dilateR
    for j=-2*dilateR:2*dilateR
        field1(16+i,64+j)=2;
    end
end
% start
field1(5,7)=3;
% goal
field1(16,84)=4;
```

```
%% 画栅格图
figure(2);
colormap(color_list);
image(0.5,0.5,field1);
grid on;
axis equal;
axis([0,cols,0,rows])
set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
set(gca,'xtick',0:1:cols,'ytick',0:1:rows)

save('field1.mat',"field1")
```

[4]. 执行路径规划

```
clc
clear
close
load('field1.mat');    % import the existed map
field1=field1-1;
start_node = [5, 7];    % coordinate of the start node
dest_node  = [16, 84]; % coordinate of the destination node

% identifier setting
Obstacle = 2;
Origin = 3;
Destination = 4;
Finished = 5;
Unfinished = 6;
Path = 7;
% color setting
white = [1,1,1];
black = [0,0,0];
green = [0,1,0];
yellow = [1,1,0];
red = [1,0,0];
blue = [0,0,1];
cyan = [0,1,1];
color_list = [white; black; green; yellow; red; blue; cyan];
rows = 20;
cols = 90;
```

```
h = figure();
warning('off','MATLAB:HandleGraphics:ObsoletedProperty:JavaFrame');
jFrame = get(h,'JavaFrame');
pause(0.1);
set(jFrame,'Maximized',1);
pause(0.1);
warning('on','MATLAB:HandleGraphics:ObsoletedProperty:JavaFrame');

subplot(2,2,1);
[path, iteration_times,map1] = Astar(field1, start_node, dest_node);
```

```
if(size(path,2) ~= 0)
    disp(['A* plan succeeded! ','iteration times: ',num2str( ...
        iteration_times), ' path length: ', num2str(size(path,2))]);
else
    disp('A* plan failed!');
end

load("field.mat");
[m,n]=find(map1==7);
path1=[m,n];
save('path1.mat',"path1")
for i=1:length(path1)
    field(path1(i,1),path1(i,2))=7;
end

pause(0.25);
```

```
subplot(2,2,3);
colormap(color_list);
image(0.5,0.5,field);
grid on;
axis equal;
axis([0,cols,0,rows])
title('A*');
set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
%设置栅格线条的样式（颜色、透明度等）
set(gca,'xtick',0:1:cols,'xticklabel',[],'ytick',0:1:rows,'yticklabel',[])
save('fieldAstar.mat',"field")

pause(0.5);

subplot(2,2,2);
[path, iteration_times,map2] = Dijkstra(field1, start_node, dest_node);

if(size(path,2) ~= 0)
    disp(['Dijkstra plan succeeded! ','iteration times: ',num2str( ...
        iteration_times), ' path length: ', num2str(size(path,2))]);
else
    disp('Dijkstra plan failed!');
end

load("field.mat");
[m,n]=find(map2==7);
path2=[m,n];
for i=1:length(path2)
    field(path2(i,1),path2(i,2))=7;
end

pause(0.25);
```

```
subplot(2,2,4);
colormap(color_list);
image(0.5,0.5,field);
grid on;
axis equal;
axis([0,cols,0,rows])
title('Dijkstra');
set(gca,'gridline','-','gridcolor','k','linewidth',0.1,'GridAlpha',1);
%设置栅格线条的样式（颜色、透明度等）
set(gca,'xtick',0:1:cols,'xticklabel',[],'ytick',0:1:rows,'yticklabel',[])
save('fieldDijkstra.mat',"field")
```

2. 轨迹跟踪部分

```
clear all;

%% 窗口
h = figure();
warning('off','MATLAB:HandleGraphics:ObsoletedProperty:JavaFrame');
jFrame = get(h,'JavaFrame');
pause(0.1);
set(jFrame,'Maximized',1);
pause(0.1);
warning('on','MATLAB:HandleGraphics:ObsoletedProperty:JavaFrame');
%% 静态场景
axis equal;
axis([0 90 0 20])
point.start=[0.5 14];
point.end=[79 2.5];
obstacle.obs1.y=20.-[6 3 3 6];
obstacle.obs1.x=[20 20 27 27];
obstacle.obs2.y=20.-[12 9 9 12];
obstacle.obs2.x=[41 41 48 48];
obstacle.obs3.y=20.-[17 14 14 17];
obstacle.obs3.x=[41 41 48 48];
obstacle.obs4.y=20.-[17 14 14 17];
obstacle.obs4.x=[60 60 67 67];
patch(obstacle.obs1.x,obstacle.obs1.y,'b')
patch(obstacle.obs2.x,obstacle.obs2.y,'b')
patch(obstacle.obs3.x,obstacle.obs3.y,'b')
patch(obstacle.obs4.x,obstacle.obs4.y,'b')
rectangle('Position',[point.start 7 3],'EdgeColor','c')
rectangle('Position',[point.end 7 3],'EdgeColor','g')
h_car= animatedline('color','r');
```

```
%% 数据定义
%PID参数
Kp = 30;
Ti =inf;
Td = 0;

verxs = [0];%误差序列 0便于微分/积分操作
verys = [0];
l = 5;%轴距
l_2=l/2;%半轴距
s=2;
aerfa=pi/6;
T = 0.01;%积分间隔
%x轴逆时针方向旋转规定为正
vx = 0;%x方向速度
vy = 0;%y方向速度
vxs=[vx];
vys=[vy];
v = sqrt(vx^2+vy^2);%当前速度
r = 1+2*v*T;%视界 随v改变而变化
theta = atan2(vy,vx);%航向角（速度方向与地面坐标系夹角）
phit = 0;%参考点姿态
xt = 0;%参考点位置
yt = 0;%参考点位置
vxt = 0;%参考点x方向速度大小
vyt = 0;%参考点y方向速度大小
```

```
%% 小车尺寸
Pos=[4,15.5,0];    %pos为车位姿信息（X,Y,θ），初始值为（0,12,1.5pi）
A.R_w = 3/2;   %robot width/2
A.R_l = 7/2;   % robot length/2
A.a1 = [-A.R_l -A.R_w]';
A.b1 = [A.R_l -A.R_w]';
A.b2 = [A.R_l A.R_w]';
A.c = [-A.R_l A.R_w]';
A.P = [A.a1 A.b1 A.b2 A.c]; %四个角点的位置
A.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*A.P;
%rotated car：旋转矩阵*四个角点的位置
A.Prot_trasl = A.Rot + [ ones(1,4)*Pos(1); ones(1,4)*Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
A.P_robot=patch(A.P(1,:),A.P(2,:),'y');
%Patch：绘制一个填充多边形区域
A.P_robot.XData=A.Prot_trasl(1,:)';
A.P_robot.YData=A.Prot_trasl(2,:)';
```

```
%% 车轮
% 后轮
B.wheel1.Pos=[Pos(1)-s*cos(aerfa+Pos(3)),Pos(2)-s*sin(aerfa+Pos(3))];
B.wheel1.R_w = 1/4;   %robot width/2
B.wheel1.R_l = 7/12;   % robot length/2
B.wheel1.a1 = [-B.wheel1.R_l -B.wheel1.R_w]';
B.wheel1.b1 = [B.wheel1.R_l -B.wheel1.R_w]';
B.wheel1.b2 = [B.wheel1.R_l B.wheel1.R_w]';
B.wheel1.c = [-B.wheel1.R_l B.wheel1.R_w]';
B.wheel1.P = [B.wheel1.a1 B.wheel1.b1 B.wheel1.b2 B.wheel1.c]; %四个角点的位置
B.wheel1.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*B.wheel1.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel1.Prot_trasl = B.wheel1.Rot + [ ones(1,4)*B.wheel1.Pos(1); ones(1,4)*B.wheel1.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel1.P_robot=patch(B.wheel1.P(1,:),B.wheel1.P(2,:),'k');
%Patch: 绘制一个填充多边形区域
B.wheel1.P_robot.XData=B.wheel1.Prot_trasl(1,:)';
B.wheel1.P_robot.YData=B.wheel1.Prot_trasl(2,:)';

B.wheel2.Pos=[Pos(1)-s*cos(aerfa-Pos(3)),Pos(2)+s*sin(aerfa-Pos(3))];
B.wheel2.R_w = 1/4;   %robot width/2
B.wheel2.R_l = 7/12;   % robot length/2
B.wheel2.a1 = [-B.wheel2.R_l -B.wheel2.R_w]';
B.wheel2.b1 = [B.wheel2.R_l -B.wheel2.R_w]';
B.wheel2.b2 = [B.wheel2.R_l B.wheel2.R_w]';
B.wheel2.c = [-B.wheel2.R_l B.wheel2.R_w]';
B.wheel2.P = [B.wheel2.a1 B.wheel2.b1 B.wheel2.b2 B.wheel2.c]; %四个角点的位置
B.wheel2.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*B.wheel2.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel2.Prot_trasl = B.wheel2.Rot + [ ones(1,4)*B.wheel2.Pos(1); ones(1,4)*B.wheel2.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel2.P_robot=patch(B.wheel2.P(1,:),B.wheel2.P(2,:),'k');
%Patch: 绘制一个填充多边形区域
B.wheel2.P_robot.XData=B.wheel2.Prot_trasl(1,:)';
B.wheel2.P_robot.YData=B.wheel2.Prot_trasl(2,:)';
```

```
% 前轮
B.wheel3.Pos=[Pos(1)+s*cos(aerfa+Pos(3)),Pos(2)+s*sin(aerfa+Pos(3))];
B.wheel3.R_w = 1/4;   %robot width/2
B.wheel3.R_l = 7/12;   % robot length/2
B.wheel3.a1 = [-B.wheel3.R_l -B.wheel3.R_w]';
B.wheel3.b1 = [B.wheel3.R_l -B.wheel3.R_w]';
B.wheel3.b2 = [B.wheel3.R_l B.wheel3.R_w]';
B.wheel3.c = [-B.wheel3.R_l B.wheel3.R_w]';
B.wheel3.P = [B.wheel3.a1 B.wheel3.b1 B.wheel3.b2 B.wheel3.c]; %四个角点的位置
B.wheel3.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*B.wheel3.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel3.Prot_trasl = B.wheel3.Rot + [ ones(1,4)*B.wheel3.Pos(1); ones(1,4)*B.wheel3.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel3.P_robot=patch(B.wheel3.P(1,:),B.wheel3.P(2,:),'k');
%Patch: 绘制一个填充多边形区域
B.wheel3.P_robot.XData=B.wheel3.Prot_trasl(1,:)';
B.wheel3.P_robot.YData=B.wheel3.Prot_trasl(2,:)';
```

```
B.wheel4.Pos=[Pos(1)+s*cos(aerfa-Pos(3)),Pos(2)-s*sin(aerfa-Pos(3))];
B.wheel4.R_w = 1/4;   %robot width/2
B.wheel4.R_l = 7/12;   % robot length/2
B.wheel4.a1 = [-B.wheel4.R_l -B.wheel4.R_w]';
B.wheel4.b1 = [B.wheel4.R_l -B.wheel4.R_w]';
B.wheel4.b2 = [B.wheel4.R_l B.wheel4.R_w]';
B.wheel4.c = [-B.wheel4.R_l B.wheel4.R_w]';
B.wheel4.P = [B.wheel4.a1 B.wheel4.b1 B.wheel4.b2 B.wheel4.c]; %四个角点的位置
B.wheel4.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*B.wheel4.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel4.Prot_trasl = B.wheel4.Rot + [ ones(1,4)*B.wheel4.Pos(1); ones(1,4)*B.wheel4.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel4.P_robot=patch(B.wheel4.P(1,:),B.wheel4.P(2,:),'k');
%Patch: 绘制一个填充多边形区域
B.wheel4.P_robot.XData=B.wheel4.Prot_trasl(1,:)';
B.wheel4.P_robot.YData=B.wheel4.Prot_trasl(2,:)';
```

```
%% 载入路径
load('path_node');
vt=15;
paths=getpath(path_node,ones(length(path_node)-1)*vt);
hold on;
plot(paths(1,:),paths(2,:),'--');
```

```
%% 寻路
flag = 1;
%初始化车辆参数
vx = 0;
vy = 0;
CTE_list=[];
phis=[];
% scatter(Pos(1),Pos(2))
% hold on
%车辆速度
k=1;
while flag
r = 1+2*v*T;%视界 随v改变而变化
pt = find((paths(1,:)-Pos(1)).^2+(paths(2,:)-Pos(2)).^2-r^2<=0,1,'last');
xt = paths(1,pt);
yt = paths(2,pt);
erx = xt - Pos(1);
ery = yt - Pos(2);
d = sqrt(erx^2+ery^2);
vxt = paths(3,pt);
vyt = paths(4,pt);
vt = sqrt(vxt^2+vyt^2);%目标速度大小
vvxt = erx/d*vt;%车辆需要追踪的x方向速度
vvyt = ery/d*vt;%车辆需要追踪的y方向速度
verx = vvxt-vx;%x方向速度误差
very = vvyt-vy;%y方向速度误差
dverx = verx - verxs(end);%微分操作
dvery = very - verys(end);%微分操作
```

```
verxs(end+1) = verx;
verys(end+1) = very;
sverx = sum(verxs);%积分操作
svery = sum(verys);%积分操作
dvx = Kp*(verx + Td*dverx + sverx/Ti);
dvy = Kp*(very + Td*dvery + svery/Ti);
vx = vx + T*dvx;
vy = vy + T*dvy;
vxs(end+1) = vx;
vys(end+1) = vy;
v = vx^2+vy^2;
Pos(1) = Pos(1)+vx*T;
Pos(2) = Pos(2)+vy*T;
theta = atan2(vy,vx);
b = theta - Pos(3);%质心侧偏角（车辆速度与车头指向夹角）(车头指向逆时针方向为正)
w = v*sin(b)/l;%车辆角速度
Pos(3) = Pos(3)+w*T;
phis(end+1) = Pos(3);
addpoints(h_car,Pos(1),Pos(2));
[CTE,CTE_point] = min((paths(1,:)-Pos(1)).^2+(paths(2,:)-Pos(2)).^2);
CTE_list(end+1) = CTE;
A.Rot = [cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*A.P; %车辆旋转
A.Prot_trasl = A.Rot + [ones(1,4)*Pos(1); ones(1,4)*Pos(2)]; %车辆移动
A.P_robot.XData=A.Prot_trasl(1,:)';
A.P_robot.YData=A.Prot_trasl(2,:)'; %更新车辆位姿

B.wheel1.Pos=[Pos(1)-s*cos(aerfa+Pos(3)),Pos(2)-s*sin(aerfa+Pos(3))];
B.wheel1.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*B.wheel1.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel1.Prot_trasl = B.wheel1.Rot + [ ones(1,4)*B.wheel1.Pos(1); ones(1,4)*B.wheel1.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel1.P_robot.XData=B.wheel1.Prot_trasl(1,:)';
B.wheel1.P_robot.YData=B.wheel1.Prot_trasl(2,:)';

B.wheel2.Pos=[Pos(1)-s*cos(aerfa-Pos(3)),Pos(2)+s*sin(aerfa-Pos(3))];
B.wheel2.Rot = [ cos(Pos(3)) -sin(Pos(3)); sin(Pos(3)) cos(Pos(3))]*B.wheel2.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel2.Prot_trasl = B.wheel2.Rot + [ ones(1,4)*B.wheel2.Pos(1); ones(1,4)*B.wheel2.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel2.P_robot.XData=B.wheel2.Prot_trasl(1,:)';
B.wheel2.P_robot.YData=B.wheel2.Prot_trasl(2,:)';

B.wheel3.Pos=[Pos(1)+s*cos(aerfa+Pos(3)),Pos(2)+s*sin(aerfa+Pos(3))];
B.wheel3.Rot = [ cos(theta) -sin(theta); sin(theta) cos(theta)]*B.wheel3.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel3.Prot_trasl = B.wheel3.Rot + [ ones(1,4)*B.wheel3.Pos(1); ones(1,4)*B.wheel3.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel3.P_robot.XData=B.wheel3.Prot_trasl(1,:)';
B.wheel3.P_robot.YData=B.wheel3.Prot_trasl(2,:)';

B.wheel4.Pos=[Pos(1)+s*cos(aerfa-Pos(3)),Pos(2)-s*sin(aerfa-Pos(3))];
B.wheel4.Rot = [ cos(theta) -sin(theta); sin(theta) cos(theta)]*B.wheel4.P;
%rotated car: 旋转矩阵*四个角点的位置
B.wheel4.Prot_trasl = B.wheel4.Rot + [ ones(1,4)*B.wheel4.Pos(1); ones(1,4)*B.wheel4.Pos(2)];
%汽车位置的变化（结果仍是四个角点的位置）
B.wheel4.P_robot.XData=B.wheel4.Prot_trasl(1,:)';
B.wheel4.P_robot.YData=B.wheel4.Prot_trasl(2,:)';
pause(0.008);
```

```
% scatter(Pos(1),Pos(2))
% hold on
% pause(0.001)
% frame=getframe(gcf);
% im = frame2im(frame);
% [imind,cm] = rgb2ind(im,256);
% if k==1
%     imwrite(imind,cm,'p.gif','gif', 'LoopCount',inf,'DelayTime',0.000001);
% end
% if rem(k,2)==0
%     imwrite(imind,cm,'p.gif','gif','WriteMode','append','DelayTime',0.000001);
% end
% k=k+1;
if sqrt((Pos(1)-paths(1,end))^2+(Pos(2)-paths(2,end))^2)<1
    flag = 0;
end
end
```

```
%% 画图
figure()
subplot(3,1,1);
plot(vxs)
hold on
plot(refvx)
legend('实际速度','参考速度')
title('x方向速度')

subplot(3,1,2);
plot(vxy)
hold on
plot(refvy)
legend('实际速度','参考速度')
title('y方向速度')

subplot(3,1,3);
plot(phis)
hold on
plot(refphi)
legend('实际横摆角','参考横摆角')
title('横摆角')

figure()
plot(sqrt(vys.*vys+vxs.*vxs))
hold on
plot(sqrt(refvy.^2+refvx.^2))
legend('速度大小','参考速度大小')
title('合速度')
axis([-0.5,max(time)+0.5,0,vset+0.5])

figure()
plot(CTE_list);
title('横向跟踪误差')
```