```
%%% List of the stations serving more than one line
 2
     multiple_lines(S):-
3
         stop(L1,_,S),
 4
         stop(L2,_,S),
5
         L1 = L2.
 6
7
     %%% Computing terminals
8
9
     first_stop(L,S):-
10
         line(L),
11
         stop(L, 1, S).
12
     not_last_stop(L,S):-
13
         line(L),
14
         stop(L,N,S),
15
         stop(L, N1,_),
16
         N1>N.
17
     last_stop(L,S):-
18
         line(L),
19
         stop(L, \_, S),
20
         \+not_last_stop(L,S).
21
     termini(L,S1,S2):-
22
         first_stop(L,S1),
23
         last_stop(L,S2).
24
25
26
     %%% List of all the stations of a line (stations are ordered)
27
     next_stop(L, S1, S2):-
28
         line(L),
29
         stop (L, N1, S1),
30
         N2 is N1+1,
31
         stop(L, N2, S2).
32
     list_stops_helper(L,ACC,RES):-
33
         ACC = [S _],
34
         first_stop(L,S),
35
         RES = ACC.
36
     list_stops_helper(L,ACC,RES):-
37
         ACC = [S]_{,}
38
         next_stop(L,P,S),
39
         list_stops_helper(L,[P ACC],RES).
40
     list_stops(L,List):-
41
         line(L),
42
         last_stop(L,S),
43
         list_stops_helper(L,[S],List).
44
45
46
     %%% Path from a station to another. Ths solutions fulfills both proerty (a) and
     proerty (b)
47
48
     %%% Set of the stations traversed
49
     stations_in_segment(segment(_,S,S),[S]).
50
     stations_in_segment(segment(L,S1,S2),Result):-
51
         next_stop(L,S1,T),
52
         stations_in_segment(segment(L,T,S2),Temp),
53
         Result = [S1 Temp].
54
     stations_traversed([],[]).
55
     stations_traversed([segment(L,S1,S2) | Tail],Result):-
         stations_traversed(Tail, Temp),
56
57
         stations_in_segment(segment(L,S1,S2),TempFirst),
58
         union (TempFirst, Temp, Result).
59
60
     %%% Cyclic segment
61
     segment_adds_cycle(segment(_,_,_),[]):-false.
62
     segment_adds_cycle(segment(L,S1,S2),Path):-
63
         stations_traversed(Path, StPath),
         next_stop(L,S1,T),
64
65
         stations_in_segment(segment(L,T,S2),StSeg),
66
         \+intersection(StPath, StSeg,[]).
67
68
     %%% Test whether the path uses a specific line
69
     uses_line(_,[]):-false.
     uses_line(L,[segment(L,_,_)|_]).
70
71
     uses_line(L,[_ Rest]):-uses_line(L,Rest).
```

```
72
 73
      %%% Finally the predicate for the path
 74
      path(S1,S2,List):-pathHelper(S1,S2,List,[]).
 75
      pathHelper(S1,S2,List,ATTEMPT):-
 76
          stop(X,N1,S1),
 77
          stop(X, N2, S2),
 78
          N1<N2,
 79
          \+uses_line(X,ATTEMPT),
          \+segment_adds_cycle(segment(X,S1,S2),ATTEMPT),
 80
 81
          List=[segment(X, S1, S2)].
 82
      pathHelper(S1,S2,List,ATTEMPT):-
 83
          stop(X, N1, S1),
 84
          stop(X, N_Med, S_Med),
 85
          N1 < N_Med
          \+uses_line(X,ATTEMPT),
 86
 87
          \+segment_adds_cycle(segment(X,S1,S_Med),ATTEMPT),
          pathHelper(S_Med, S2, L_Temp, [segment(X, S1, S_Med) | ATTEMPT]),
 88
 89
          List=[segment(X,S1,S_Med) | L_Temp].
 90
 91
 92
      %%% Path with minimum numer of changes
 93
      list_length([],0):-!.
 94
      list_length([_ R],N):-
 95
          list_length(R,N1),
 96
          N is N1+1.
 97
 98
      non_minimum_path(S1,S2,P):-
 99
          path (S1, S2, P),
100
          path (S1, S2, P2),
101
          list_length(P,N1),
102
          list_length(P2,N2),
103
          N2<N1.
104
      minimum_path(S1,S2,P):-
105
          path (S1, S2, P),
106
          \+non_minimum_path(S1,S2,P).
107
```