

# CausalARC

## Abstract Reasoning with Causal World Models

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**Abstract.** This work introduces CausalARC: an experimental testbed for AI reasoning in low-data and out-of-distribution regimes, modeled after the Abstraction and Reasoning Corpus (ARC) [3]. Each reasoning task is sampled from a fully specified *causal world model*, formally expressed as a structural causal model (SCM). LLM performance on CausalARC varied heavily across tasks: (1) **abstract reasoning with test-time training**, (2) **counterfactual reasoning**, (3) **program synthesis**, (4) **causal discovery**.

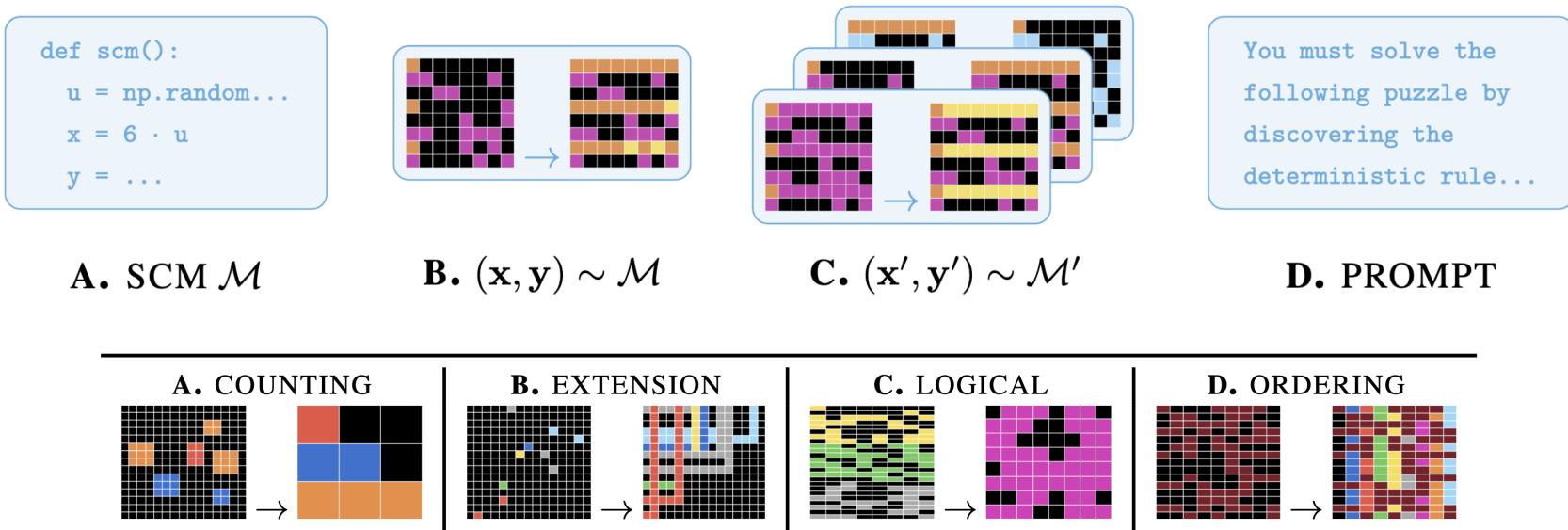


Figure 1: **The CausalARC testbed.** (A) First, SCM  $\mathcal{M}$  is manually transcribed in Python code. (B) Randomly sampled input-output pairs offer observational learning signals about the world model. (C) Sampling from submodels  $\mathcal{M}'$  of  $\mathcal{M}$  yields interventional samples  $(\mathbf{x}', \mathbf{y}')$ . Performing multiple interventions while holding the exogenous context constant yields a set of counterfactual pairs. (D) Automatically generated prompts with in-context demonstrations.

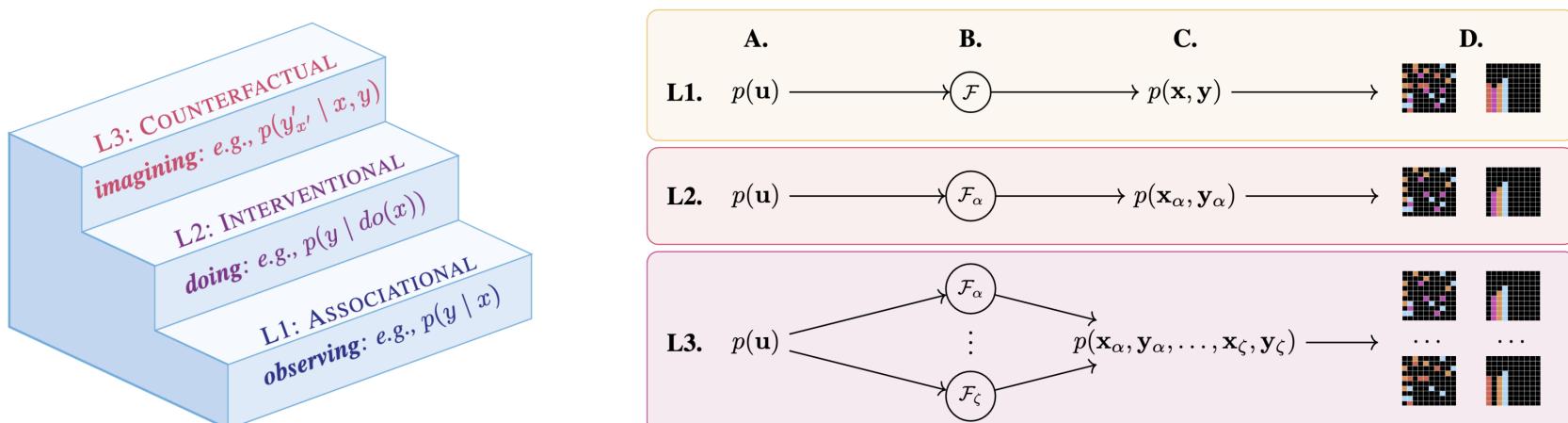


Figure 2: [Left] **The Pearl Causal Hierarchy (PCH)**: observing factual realities (L1), exerting actions to induce interventional realities (L2), and imagining alternate counterfactual realities (L3) [2]. [Right] **Jointly observed counterfactuals in CausalARC**. (A) The distribution over the exogenous context (i.e., the external state). (B) Transformations applied to the exogenous context (e.g., functions  $\mathcal{F}$  in the observational world; updated functions  $\mathcal{F}_\alpha$  under intervention  $\alpha$ ). (C) Induced distributions, following from the applied transformation. (D) CausalARC samples from each rung of the PCH. Adapted from [2].

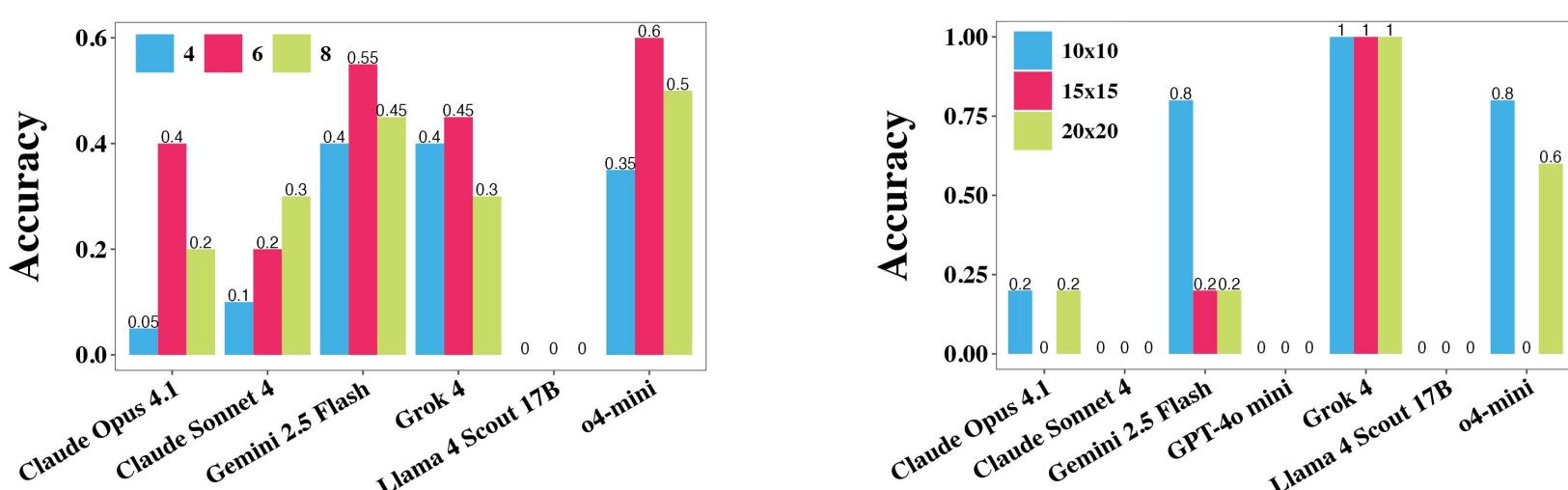


Figure 3: [Left] **Program synthesis** on four counting and extension tasks as total in-context demonstrations increased. [Right] **Causal discovery** with logical reasoning as array size increased. Scores were over five random L1 prompt samples.

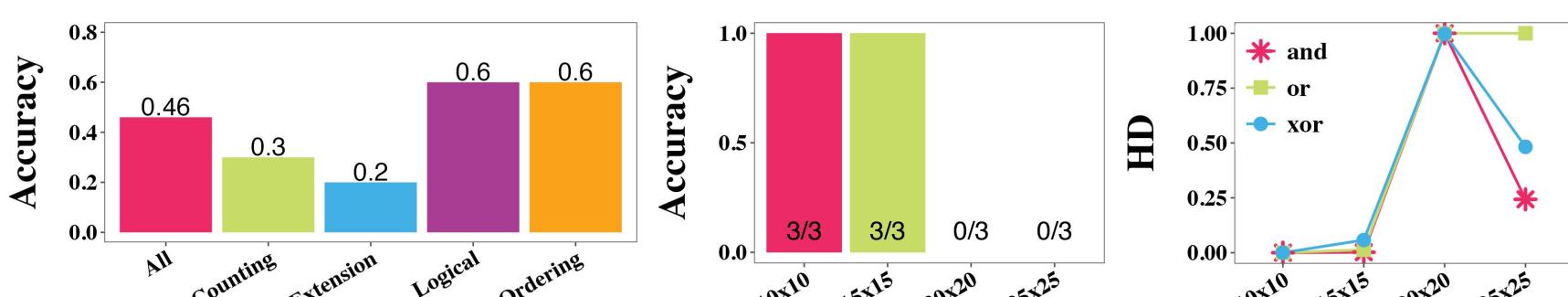


Figure 4: **Abstract reasoning with test-time training (TTT).** [Left] Accuracy by CausalARC theme for MARC with TTT (Llama 3 8B base) [1]. [Center, right] Performance on *and*, *or*, and *xor* tasks sampled from CausalARC task SCMdky5 as array size increases.