

The Cost of Capital and Misallocation in the United States

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Misallocation and the cost of capital

Research question: How does dispersion in the cost of capital affect misallocation?

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Traditional approach:

1. Strong assumptions about production functions (Homogeneous Cobb-Douglas)
2. Measure heterogeneity in marginal products from cross-sectional input and production data
3. Estimate capital misallocation

Our approach:

- Optimizing firms equate cost of capital to expected marginal product of capital
- Combine credit registry data + model to carefully measure cost of capital, and infer MPK
- Use dispersion in cost of capital to quantify welfare losses stemming from credit market frictions

This paper

Methodological contribution:

- Adapt a standard **dynamic corporate finance model** for measurement with **micro loan-level data**
- Derive a **sufficient statistic** for capital misallocation arising due to credit market frictions

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Empirical results for the US:

- Average cost of capital tracks 5-year treasury rates, with a spread
- Measures of cost of capital correlate with traditional measures of $ARPK_i$ at the firm level
- Credit markets efficient in normal times: losses from misallocation $\approx 0.9\%$ of GDP
- Losses from misallocation increased to 1.8% of GDP in 2020-2021

Related literature

- **Measuring misallocation:**

- Seminal work: Restuccia and Rogerson (2008), Hsieh and Klenow (2009)
- Challenge: Standard methods rely on strong assumptions (Haltiwanger et al., 2018).
- Recent advances: (Quasi-)Experimental methods to recover marginal products directly (Carrillo et al., 2023; Hughes and Majerovitz, 2025).
- **Contribution:** use **heterogeneity in funding costs** to measure **dispersion in MRPK**

- **Heterogeneity in the cost of capital:**

- Developing countries: Banerjee and Duflo (2005); Cavalcanti, Kaboski, Martins, and Santos (2024)
- US: Gilchrist, Sim, and Zakrajsek (2013); Binsbergen and Opp (2019); Gormsen and Huber (2023, 2024); Faria-e-Castro, Jordan-Wood, and Kozlowski (2024)
- **Contribution:**
 - Estimate firm cost of capital using **credit registry data**, controlling for loan characteristics
 - Derive and estimate **sufficient statistic** for misallocation

Outline

1. Model

2. Welfare and misallocation

3. Measurement with credit registry data

4. Empirical results

5. Cross-country comparison

Model Summary

- Discrete time, infinite horizon
- Continuum of firms, each matched with a lender
- No aggregate risk (for now - work in progress!)

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Data: We will measure heterogeneous ρ_i at the security level in credit-registry data (details later).

Key question: How do heterogeneity in ρ_i and financial frictions distort the allocation of capital?

Model

Firm value function:

$$V_i(k_i, b_i, z_i) = \max_{k'_i, b'_i} \pi_i(k_i, b_i, z_i, k'_i, b'_i) + \beta \mathbb{E} \left[\overbrace{\max \{V_i(k'_i, b'_i, z'_i), 0\}}^{\text{Limited liability}} \mid z_i \right]$$

Firm profits:

$$\pi_i(k_i, b_i, z_i, k'_i, b'_i) = f(k_i, z_i) + (1 - \delta)k_i - k'_i - \theta b_i + Q_i(k'_i, b'_i, z_i)[b'_i - (1 - \theta_i)b_i]$$

Price of debt:

$$Q_i(k'_i, b'_i, z_i) = \frac{\mathbb{E} \left\{ \overbrace{\mathcal{P}_i(k'_i, b'_i, z'_i)}^{\text{repayment prob.}} [\theta_i + (1 - \theta_i) Q_i(k''_i, b''_i, z'_i)] + (1 - \mathcal{P}_i(k'_i, b'_i, z'_i)) \overbrace{\frac{\phi_i k'_i}{b'_i}}^{\text{recovery}} \mid z_i \right\}}{1 + \rho_i}$$

lender discount rate

- **Cost of capital:**

$$\underbrace{\frac{\mathbb{E}[\mathcal{P}'_i(\theta_i + (1 - \theta_i)Q'_i) | z_i]}{Q_i}}_{1 + r_i^{\text{firm}}} \times \underbrace{\left[\frac{1 - \frac{\partial Q_i}{\partial k'_i} [b'_i - (1 - \theta_i)b_i]}{1 + \frac{\partial Q_i}{\partial b'_i} \frac{[b'_i - (1 - \theta_i)b_i]}{Q_i}} \right]}_{\mathcal{M}_i}$$

- $1 + r_i^{\text{firm}}$: implied interest rate perceived by the firm
- \mathcal{M}_i : price impact term capturing how (k'_i, b'_i) affect debt price Q_i

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- $1 + r_i^{\text{firm}}$: implied interest rate perceived by the firm
- \mathcal{M}_i : price impact term capturing how (k'_i, b'_i) affect debt price Q_i
- **Optimality:** firm equates cost of capital to expected MRPK

$$(1 + r_i^{\text{firm}}) \cdot \mathcal{M}_i = \underbrace{\mathbb{E}[\mathcal{P}'_i(f_k(k'_i, z'_i) + 1 - \delta) | z_i]}_{\text{expected MRPK}}$$

- **Measurement idea:** measure r_i^{firm} from loan data to infer dispersion in MRPK and misallocation.

Firm's cost of capital

Lemma 1 (Firm's cost of capital)

The firm's cost of capital is:

$$1 + r_i^{firm} = \frac{1 + \rho_i}{1 + \Lambda_i}$$

$$\Lambda_i := \frac{\mathbb{E}[(1 - \mathcal{P}'_i) \phi_i k'_i / b'_i | k'_i, b'_i, z_i]}{\mathbb{E}[\mathcal{P}'_i (\theta + (1 - \theta_i) Q'_i) | k'_i, b'_i, z_i]}$$

▷ *Proof*

- Limited liability + recovery creates wedge between ρ (lender discount rate) and r_i^{firm}
- Under default, firm liquidates and gets zero; liquidated capital is used to (partially) repay lender
- On the margin, firm investment raises lender's payoff in default but has no effect on firm's payoff
- In general, $r_i^{firm} < \rho_i$ if lender expects some recoveries in default

Outline

1. Model

2. Welfare and misallocation

3. Measurement with credit registry data

4. Empirical results

5. Cross-country comparison

Aggregate economy and welfare

- Aggregate resources available for consumption and new capital:

$$Y_{t+1} + (1 - \delta)K_{t+1} = \int_0^1 \mathbb{E}_t [\mathcal{P}_{i,t+1} (f(k_{i,t+1}, z_{i,t+1}) + (1 - \delta)k_{i,t+1}) + (1 - \mathcal{P}_{i,t+1}) \cdot \phi_i k_{i,t+1}] di$$

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- Let $\omega_{i,t}(S^t) \in \{0, 1\}$ denote whether a firm operates or not, as a function of history S^t
 - S^t is the history of productivity draws up to t
- Planner's problem:

$$\begin{aligned} U^* &= \max_{\{ \{k_{i,t}(S^{t-1}), \omega_{i,t}(S^t) \}_{i \in [0,1]} \}_{t=1}^{\infty}} \sum_{t=0}^{\infty} \beta^t \cdot u(C_t) \\ \text{s.t.} \quad K_t &= \int_0^1 k_{i,t}(S^{t-1}) di \\ C_t + K_{t+1} &= Y_t + (1 - \delta)K_t \\ \omega_{i,t+1}(S^{t+1}) &\leq \omega_{i,t}(S^t) \quad \forall S^t \subset S^{t+1}, \forall i \end{aligned}$$

Aggregate economy and welfare

Planner must decide:

- Which firms operate or exit
- Aggregate capital each period
- Allocation of capital across (operating) firms

Can separate planner's problem into outer (dynamic) and inner (static) problems:

$$U^* = \underbrace{\max_{\{K_t, \{\omega_{i,t}(S^t)\}_{i \in [0,1]}\}_{t=1}^\infty}}_{\substack{\text{Outer (dynamic)} \\ \text{Aggregate capital and exit}}} \sum_{t=0}^{\infty} \beta^t \cdot u \left(\underbrace{\max_{\{\{k_{i,t}(S^{t-1})\}_{i \in [0,1]}\}_{t=1}^\infty}}_{\substack{\text{Inner (static)} \\ \text{Reallocate capital}}} Y_t - l_t \right)$$

Aggregate economy and welfare: intensive-margin misallocation

- Inner problem: reallocate capital across firms, taking exit and aggregate capital as given
- Focus on misallocation at the intensive margin
 - As in most of the literature, e.g. Hsieh and Klenow (2009)
 - Necessary for measurement: hard to measure outcomes for counterfactual firms that don't exist
- Planner redistributes $\{k_{i,t+1}\}_{i \in [0,1]}$ taking exit decisions $\{\mathcal{P}_{i,t+1}^{DE}\}_{i \in [0,1]}$ and K_{t+1}^{DE} as given

$$\begin{aligned} & \max_{\{k_{i,t+1}^*\}_{i \in [0,1]}} \int_0^1 \mathbb{E}_t \left[\mathcal{P}_{i,t+1}^{DE} \left(f(k_{i,t+1}^*, z_{i,t+1}) + (1 - \delta)k_{i,t+1}^* \right) + (1 - \mathcal{P}_{i,t+1}^{DE}) \cdot \phi_i k_{i,t+1}^* \right] di \\ \text{s.t.} \quad & \int_0^1 k_{i,t+1}^* di = K_{t+1}^{DE} \end{aligned}$$

Social return on capital

Planner cares about payoffs to both lender and firm

- Total Surplus = $\mathbb{E}_t [\mathcal{P}_{i,t+1}^{DE} (f(k_{i,t+1}^*, z_{i,t+1}) + (1 - \delta)k_{i,t+1}^*) + (1 - \mathcal{P}_{i,t+1}^{DE}) \cdot \phi_i k_{i,t+1}^*]$

Define the **social marginal product of capital at firm i** , $r_{i,t}^{social}(k)$, as:

$$1 + r_{i,t}^{social}(k) := \mathbb{E} \left[\underbrace{\mathcal{P}_{i,t+1}^{DE} (f_k(k, z_{i,t+1}) + 1 - \delta)}_{(1+r_{i,t}^{firm}) \times \mathcal{M}_{i,t}} + \underbrace{(1 - \mathcal{P}_{i,t+1}^{DE}) \phi_i}_{\text{Recoveries}} \right]$$

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- In the empirically relevant case, $r_i^{firm} < r_i^{social} < \rho_i$
- Firm doesn't care about recoveries, planner cares the "right amount," lender cares too much

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Planner Optimality: Equalize $r_{i,t}^{social}(k_{i,t+1}^*)$ across firms

Inefficient Equilibrium: Dispersion in $r_{i,t}^{social} \rightarrow$ misallocation

Misallocation: sufficient statistic

Proposition 1 (Misallocation)

Misallocation can be measured with $\mathbb{E}[r_i^{social}]$ and $\text{Var}(r_i^{social})$ as

$$\log(Y^*/Y^{DE}) \approx \frac{1}{2} \cdot \mathcal{E} \cdot \log\left(1 + \frac{\text{Var}(r_i^{social})}{(\mathbb{E}[r_i^{social}] + \delta)^2}\right)$$

▷ *Proof*

- Extends Hughes and Majerovitz (2025) to a dynamic economy with default
 - Measures intensive-margin misallocation
 - Set $\mathcal{E} = \frac{1}{2}$ (elasticity of output w.r.t. $r^{social} + \delta$) and $\delta = 0.06$
- **Next:** Show how to measure r_i^{social} using credit registry data

▷ Calibration

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4. Empirical results
5. Cross-country comparison

- Quarterly loan-level panel on universe of loan facilities $> \$1\text{M}$
- Sample covers top 40 BHCs, 2014:Q4-2024:Q4
- 91% of C&I lending by top 25 banks; 55% of C&I undertaken by all commercial banks
- Detailed information on features of credit facilities
 - Origination date, size, maturity, interest rate/spread, probability of default, loss given default, fixed vs. floating, type of loan, etc.
- Focus on term loans at origination, issued to non-government, non-financial US companies

Pricing term loans

For a loan i originated at t , the **break-even** condition for a lender with discount rate $\rho_{i,t}$ is

$$1 = \sum_{s=1}^{T_{i,t}} \left[\frac{(P_{i,t})^s \cdot \mathbb{E}_t(r_{i,t,s}) + (P_{i,t})^{s-1} \cdot (1 - P_{i,t}) \cdot (1 - LGD_{i,t})}{(1 + \rho_{i,t})^s \cdot \mathbb{E}_t(\Pi_{t,s})} \right] + \frac{(P_{i,t})^{T_{i,t}}}{(1 + \rho_{i,t})^{T_{i,t}} \cdot \mathbb{E}_t(\Pi_{t,T_{i,t}})}$$

- “Bullet” loans: pay interest each period and principal at the end
- $T_{i,t}$: maturity
- $P_{i,t}$: repayment probability (constant over time)
- $LGD_{i,t}$: loss given default (constant over time)
- $\mathbb{E}_t[r_{i,t,s}]$: fixed rate or spread over benchmark (Gürkaynak, Sack, and Wright, 07) ▷ [forward rates](#)
- $\mathbb{E}_t(\Pi_{t,s})$: total expected inflation between t and s , from term structure of $\mathbb{E}_t\pi_s$ (Cleveland Fed)
- \Rightarrow **Solve for lender's discount rate:** $\rho_{i,t}$

Measuring firm and social cost of capital

Lemma 2 (Firm and social cost of capital)

We can write the firm cost of capital as:

$$1 + r_{i,t}^{firm} = (1 + \rho_{i,t}) - (1 - P_{i,t})(1 - LGD_{i,t})$$

and the social cost of capital as:

$$\begin{aligned} 1 + r_{i,t}^{social} &= (1 + r_{i,t}^{firm})\mathcal{M}_{i,t} + (1 - P_{i,t})(1 - LGD_{i,t})lev_{i,t} \\ &= \underbrace{(1 + \rho_{i,t})\mathcal{M}_{i,t}}_{\text{lender discount rate}} + \underbrace{(lev_{i,t} - \mathcal{M}_{i,t}) \cdot (1 - P_{i,t}) \cdot (1 - LGD_{i,t})}_{\text{wedge due to financial frictions}} \end{aligned}$$

▷ Proof

Where $lev_{i,t}$ is leverage: value of firm's debt over its capital

Sufficient statistic for misallocation

$$\log(Y_t^*/Y_t^{DE}) \approx \frac{1}{2} \cdot \mathcal{E} \cdot \log \left(1 + \frac{\text{Var}(r_{i,t}^{social})}{(\mathbb{E}[r_{i,t}^{social}] + \delta)^2} \right) \quad (1)$$

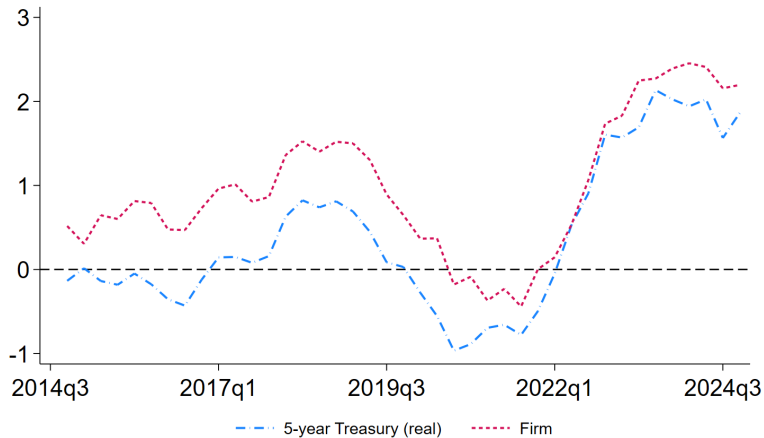
$$1 + r_{i,t}^{social} = (1 + \rho_{i,t}) \mathcal{M}_{i,t} + (lev_{i,t} - \mathcal{M}_{i,t}) \cdot (1 - P_{i,t}) \cdot (1 - LGD_{i,t}) \quad (2)$$

- Set $\mathcal{M}_{i,t} = 1$; reasonable approximation given our data ▷ estimate \mathcal{M}
- Can measure misallocation directly with credit registry data using (1) and (2)!
- Dispersion in $r_{i,t}^{social}$ comes from:
 1. Dispersion in lender's discount rate, $\rho_{i,t}$
 2. Dispersion in financial frictions wedge
 3. Covariance between $\rho_{i,t}$ and financial frictions wedge

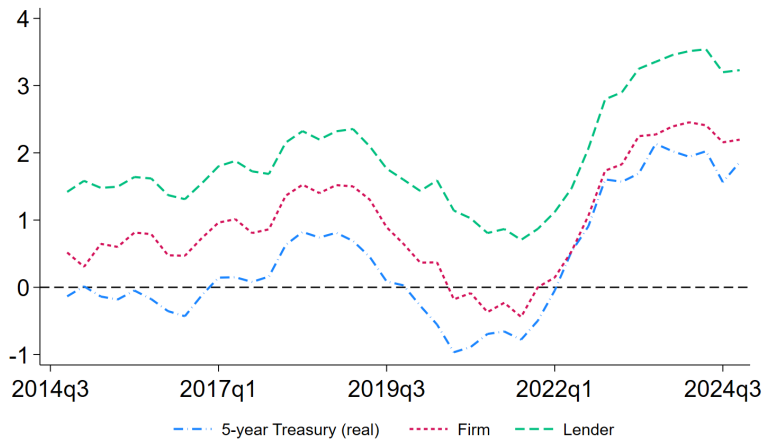
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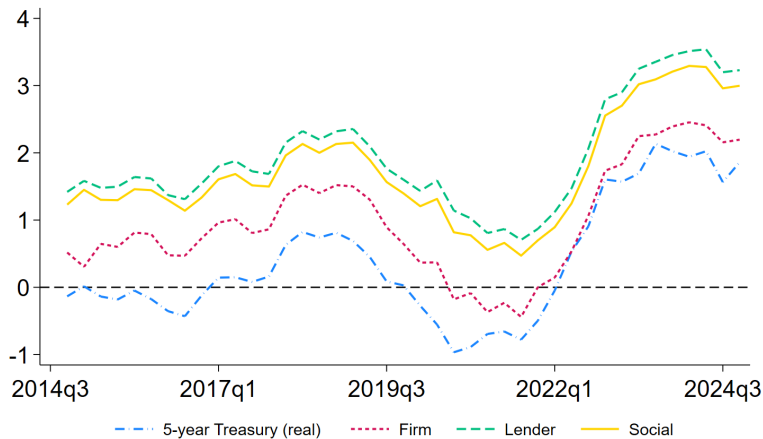
Time series for average discount rate, firm and social cost of capital



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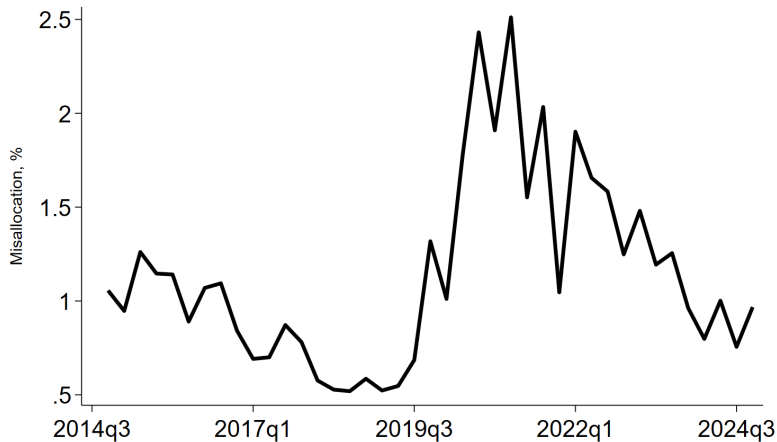
Estimates for lender discount rate, firm and social cost of capital

	Mean	SD	p10	p50	p90
ρ (%)	1.87	1.55	0.41	1.88	3.62
r^{firm} (%)	0.92	2.80	-0.86	1.26	3.03
r^{social} (%)	1.66	1.78	0.12	1.73	3.47

- Financial frictions/recovery: $\mathbb{E}[r_{i,t}^{firm}] < \mathbb{E}[r_{i,t}^{social}] < \mathbb{E}[\rho_{i,t}]$
- Standard deviation of $r^{social} = 1.78$, What is the implication for misallocation?

Misallocation in the US, 2014-2024

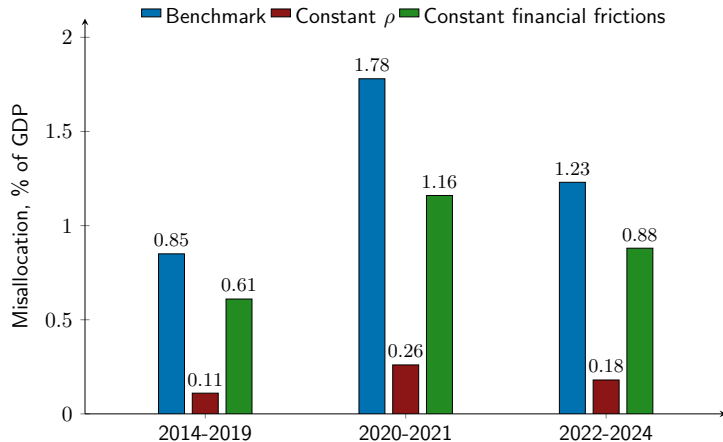
▷ weighted



- About 0.9% before 2020
- ↑ to 1.8% in 2020-2021
- ↓ to 1.2% in 2022-2024

Misallocation is driven by heterogeneity in ρ_i

▷ details



- Decomposition: set all ρ_i to quarterly mean (Constant ρ); same for financial frictions term
- Main driver: dispersion in lender discount rates
- Interaction between ρ_i and financial frictions ($0.85 > 0.11 + 0.61$)

Extensions & robustness

1. Estimate heterogeneous price-impact term \mathcal{M} . [▷ heterogeneous \$\mathcal{M}\$](#)
2. Variance decomposition: dispersion accounted by bank, firm, loan. [▷ variance decomposition](#)
3. Validate r^{social} using firm-level ARPK measures. [▷ details](#)
4. Compare to misallocation from traditional approach. [▷ details](#)

Work in progress:

1. Aggregate risk
2. Quantitative model

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Are credit markets more efficient in the United States?

Overall, US credit markets seem quite efficient

- Losses of $\approx 1\%$ from heterogeneous r^{social}

How efficient are credit markets around the world?

- Widely believed that developing-country credit markets are inefficient, with high dispersion in cost of capital (Banerjee and Duflo 2005)
- Essential for understanding if this is an important driver of development

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Ideal: Redo **exact same analysis** in credit registry data for other countries

For now: Infer what we can from other papers, making some strong assumptions

Cross-country comparison: Methodology and assumptions

- Search for papers that report default probability as well as mean and SD of interest rates

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- For a fixed real interest rate $r_{i,t}$, ρ has a closed-form:

$$1 + \rho_{i,t} = P_{i,t} (1 + r_{i,t}) + (1 - P_{i,t}) (1 - LGD_{i,t})$$

- We will use this formula, even though loans are not fixed real rate

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 1. Obtain mean real rate by subtracting average realized inflation from mean nominal rate
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- Most papers report nominal rates, need to handle inflation
 1. Obtain mean real rate by subtracting average realized inflation from mean nominal rate
 2. Inflation should not affect standard deviation of nominal rates (or spreads)
- Assume all loans have the same $P_{i,t}$, $LGD_{i,t}$, equal to the average
- Recovery rates from the World Bank's Doing Business Database
- Approximate $r_{i,t}^{social} \approx \rho_{i,t}$ and compute misallocation using our formula

Cross-country comparison

	Aleem 1990 Pakistan	Khwaja & Mian 2005 Pakistan	Cavalcanti et al. 2024 Brazil	Beraldi 2025 Mexico	This paper 2025 United States
Years of data	1980–1981	1996–2002	2006–2016	2003–2022	2014–2024
Mean real rate, %	66.8	8.00	83.0	12.4	1.4
SD real rate, %	38.1	2.9	93.3	5.2	1.2
Mean def. prob., %	2.7	16.9	4.0	8.9	1.5
Mean recovery rate, %	42.8	42.8	18.2	63.9	66.6
Implied misallocation, %	6.5	13.5	21.5	2.8	0.8

- **Developing countries:** higher mean and standard deviation of real interest rates
- **U.S.:** lower mean and standard deviation of interest rates, **higher recovery**
- **Brazil:** most extreme misallocation: 21.5%.

A plea for data

- We would like to do a follow-up project that measures the cost of capital around the world, using our methodology in each country
- Need credit data with:
 - Interest rate
 - Loan terms (e.g. fixed vs. variable rate, loan maturity)
 - Information on default probability and recovery rates
- We know this is possible in other countries (e.g. Mexico), but are looking for more data sets
- **If you know of a data set that we could use, please talk to me or send us an email!**

Conclusion

- Framework to measure misallocation from credit registry data.
 1. Standard dynamic corporate finance model as measurement device
 2. Sufficient statistic for capital misallocation
 3. Uses standard credit registry variables (r, P, LGD, T, \dots)
- Application to U.S. credit registry data
 1. Estimate lender discount rates, firm-level cost of capital and social cost of capital
 2. Misallocation around 1% in normal times
 3. Cross-country comparison with other countries

Credit markets in the US are close to efficient, developing countries appear more distorted.

Appendices

Firm FOCs:

$$[k'_i] : \quad -1 + \frac{\partial Q_i(k'_i, b'_i, z_i)}{\partial k'_i} [b'_i - (1 - \theta_i)b_i] + \beta \mathbb{E} \{ \mathcal{P}_i(k'_i, b'_i, z'_i) [f_k(k'_i, z'_i) + 1 - \delta] | z_i \} = 0$$

$$[b'_i] : \quad \frac{\partial Q_i(k'_i, b'_i, z_i)}{\partial b'_i} [b'_i - (1 - \theta_i)b_i] + Q_i(k'_i, b'_i, z_i) - \beta \mathbb{E} \{ \mathcal{P}_i(k'_i, b'_i, z'_i) [\theta_i + (1 - \theta_i)Q_i(k''_i, b''_i, z'_i)] | z_i \} \\ = 0$$

$$\begin{aligned}\frac{1}{Q_t} \mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})] &= \frac{(1 + \rho) \mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})]}{\mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})] + \mathbb{E}_t [(1 - \mathcal{P}_{t+1}) \phi k' / b']} \\ &= (1 + \rho) \left(1 + \frac{\mathbb{E}_t [(1 - \mathcal{P}_{t+1}) \phi k' / b']}{\mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})]} \right)^{-1} \\ &= (1 + \rho) (1 + \Lambda)^{-1}\end{aligned}$$

where

$$\Lambda \equiv \frac{\mathbb{E}_t [(1 - \mathcal{P}_{t+1}) \phi k' / b']}{\mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})]}$$

- Formally, planner's problem is now the same as solving $Y = \max_{\{k_i\}_i} \int_0^1 f_i(k_i) di$, where $f_i(k_i)$ is now expected output
- Apply Hughes and Majerovitz (2024), noting $\frac{dY}{dk} = r^{social} + \delta$

$$\log(Y^*/Y^{DE}) \approx \frac{1}{2} \cdot \mathcal{E} \cdot \log\left(1 + \frac{\text{Var}(r^{social})}{(\mathbb{E}[r^{social}] + \delta)^2}\right)$$

- \mathcal{E} is (negative) elasticity of output w.r.t. cost of capital ($r^{social} + \delta$)

- \mathcal{E}_i is the elasticity of expected output with respect to the cost of capital
- Assume that $f(k, z) = z \cdot k^\alpha$ and there is no default, then

$$\mathcal{E} = \frac{\alpha}{1 - \alpha}$$

- $\alpha = \frac{1}{3}$ implies $\mathcal{E} = \frac{1}{2}$

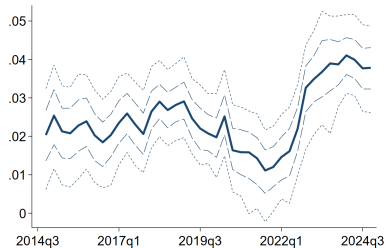
Summary statistics

[▷ back](#)

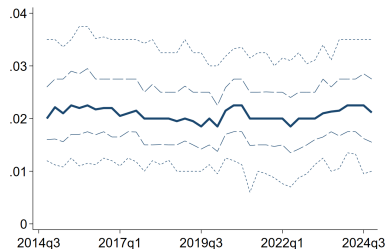
	Mean	St. Dev.	p10	p50	p90
Interest rate	4.18	1.69	2.21	3.94	6.60
Maturity (yrs)	6.83	4.65	3.00	5.00	10.25
Real interest rate	2.39	1.24	0.88	2.33	4.00
Prob. Default (%)	1.45	2.53	0.19	0.85	2.88
LGD (%)	34.41	13.17	16.00	35.60	50.00
Loan amount (M)	10.75	67.58	1.11	2.57	22.92
Sales (M)	1,269.93	6,051.48	2.16	58.50	1,560.10
Assets (M)	1,760.37	8,894.15	1.07	35.55	1,782.22
Leverage (%)	72.17	24.68	42.68	71.29	100.00
Return on assets (%)	27.60	58.51	4.56	15.76	47.81
N Loans	65,284				
N Firms	38,751				
N Fixed Rate	32,592				
N Variable Rate	32,692				

Time series for averages and quantiles: real interest rate, PD, LGD [▷ back](#)

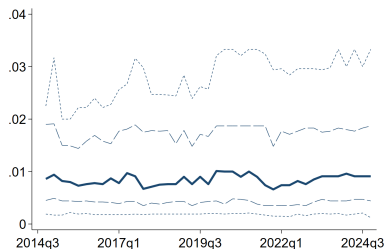
Real interest rate



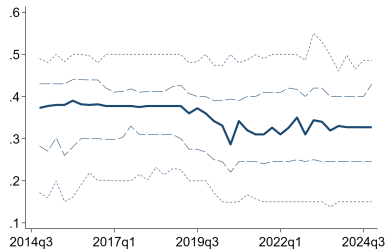
Interest rate spread (var.)



Probability of default



Loss given default



Data cleaning and sample construction

▷ back

We use FR Y-14Q Schedule H.1 data from 2014Q4 to 2024Q4.

Borrower Filters:

- Drop loans without a Tax ID
- Keep only Commercial & Industrial loans to nonfinancial U.S. addresses
- Drop borrowers with NAICS codes:
 - 52 (Finance and Insurance), 92 (Public Administration)
 - 5312 (Real Estate Agents), 551111 (Bank Holding Companies)

Data cleaning and sample construction, cont'd

▷ back

Loan Filters:

- Drop loans with:
 - Negative committed exposure
 - Utilized exposure exceeding committed exposure
 - Origination after or maturity before report date
- Keep only “vanilla” term loans (Facility type = 7)
- Drop loans with:
 - Mixed-interest rate structures
 - Maturity less than 1 year or longer than 10 years
 - Implausible interest rates or spreads (outside 1st - 99th percentile)
 - Missing or invalid PD/LGD values (outside $[0, 1]$)
 - PD = 1 (flagged as in default)

Forward interest rate expectations

▷ [back](#)

To estimate ρ_i for floating rate loans, need estimates of $\mathbb{E}_0[r_t] + s_i$

- Floating rate loans charge reference rate + spread
- Approximate LIBOR/SOFR using Treasury forward yield curve estimates (Gürkaynak, Sack, and Wright, 2007)
- Average spread between SOFR and Treasury rates 2018-2025 $\simeq 2$ basis points
- Assume expectations hypothesis: long rates reflect expected short rates
- Back out $\mathbb{E}_0[r_t] + s_i$ for each loan, using treasury forward rate plus loan's spread

$$Q_t = \frac{\mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1}) + (1 - \mathcal{P}_{t+1}) \phi k_{t+1} / b_{t+1}]}{1 + \rho}$$

Note that

$$\begin{aligned} Q_t &= Q_t^P + Q_t^D \\ Q_t^P &= \frac{\mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})]}{1 + \rho} \\ Q_t^D &= \frac{\mathbb{E}_t [(1 - \mathcal{P}_{t+1}) \phi k_{t+1} / b_{t+1}]}{1 + \rho} \end{aligned}$$

That is, we strip the bond into the payment in repay (Q_t^P) and the payment in default (Q_t^D). Then:

$$\Lambda = \frac{\mathbb{E}_t [(1 - \mathcal{P}_{t+1}) \phi k_{t+1} / b_{t+1}]}{\mathbb{E}_t [\mathcal{P}_{t+1} (\theta + (1 - \theta) Q_{t+1})]} = \frac{Q_t^D}{Q_t^P}$$

Firm cost of capital: measurement

▷ back

The firm defaults with probability $(1 - P)$ and the lender recovers $(1 - LGD)$. Hence

$$Q_t^{D,data} = \frac{(1 - P)(1 - LGD)}{1 + \rho}$$

For the payment portion notice that at issuance we have the following condition

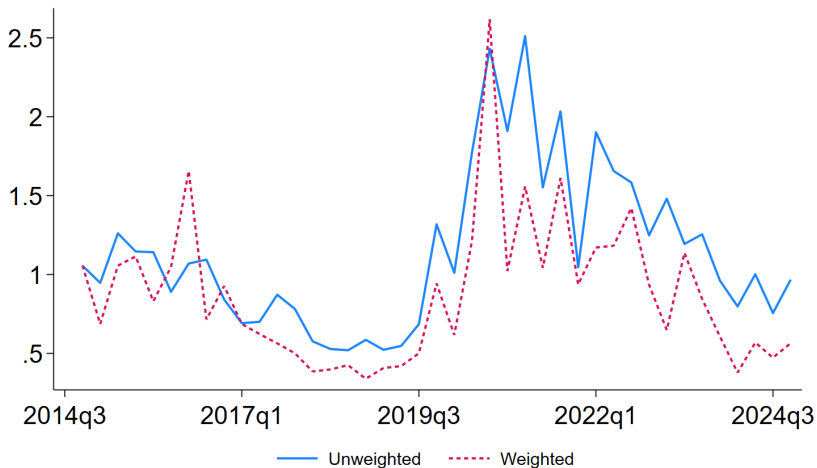
$$1 = \sum_{s=1}^T \left[\frac{P^s \mathbb{E}_t[r_{t+s}] + P^{s-1} (1 - P)(1 - LGD)}{(1 + \rho)^s} \right] + \frac{P^T}{(1 + \rho)^T}$$
$$1 = \frac{(1 - P)(1 - LGD)}{1 + \rho} + P \frac{\mathbb{E}_t[r_{t+1}]}{1 + \rho} + \left(\sum_{s=2}^T \left[\frac{P^s \mathbb{E}_t[r_{t+s}] + P^{s-1} (1 - P)(1 - LGD)}{(1 + \rho)^s} \right] + \frac{P^T}{(1 + \rho)^T} \right)$$

So, we can define $Q_t^{P,data}$ as $1 = Q_t^{P,data} + Q_t^{D,data}$ so $Q_t^{P,data} = 1 - Q_t^{D,data}$. Finally

$$\Lambda^{data} = \frac{Q_t^{D,data}}{Q_t^{P,data}} = \frac{(1 - P)(1 - LGD)}{1 + \rho - (1 - P)(1 - LGD)}$$

Misallocation, weighted by loan size

▷ back



Decomposing misallocation

▷ back

Counterfactual I: What if all lenders have the same $\bar{\rho}$?

$$1 + r_{social}^{cf,I} = \overline{(1 + \rho)\mathcal{M}} + (lev - \mathcal{M}) \cdot PD \cdot (1 - LGD)$$

Heterogeneity in r_{social}^{cf} → Misallocation due to financial frictions

Counterfactual II: what if we equalize financial frictions?

$$1 + r_{social}^{cf,II} = (1 + \rho)\mathcal{M} + \overline{(lev - \mathcal{M}) \cdot PD \cdot (1 - LGD)}$$

Heterogeneity in r_{social}^{cf} → Misallocation due to heterogeneous cost of capital

“Real yield”: decomposing ρ

▷ back

- The “real yield” is the implied $\rho_{i,t}^*$ when $P_{i,t} = 1$

$$1 = \sum_{s=1}^{T_{i,t}} \left[\frac{\mathbb{E}_t(r_{i,t,s})}{\left(1 + \rho_{i,t}^*\right)^s \cdot \mathbb{E}_t(\Pi_{t,s})} \right] + \frac{1}{\left(1 + \rho_{i,t}^*\right)^{T_{i,t}} \cdot \mathbb{E}_t(\Pi_{t,T_{i,t}})}$$

- Real yield independent of $P_{i,t}$, $LGD_{i,t}$
- Only affected by losses through the contractual rate r

$$\mathcal{M} = \frac{1 - \gamma \times \frac{Qb'}{k'} \times \frac{\partial \log Q}{\partial \log k'}}{1 + \gamma \times \frac{\partial \log Q}{\partial \log b'}}$$

Need Q , γ , and firm leverage Qb'/k' to compute \mathcal{M}

1. To compute Q , assume that loans are perpetuities that decay at a geometric rate θ , discounted at the loan's real interest rate r :

$$Q = \frac{\theta + (1 - \theta)Q}{1 + r} = \frac{\theta}{r + \theta}$$

r is directly observed in the data, and we can approximate $\theta = 1/T$

2. Guess a functional approximation $Q(z, k, b, \rho)$
3. Estimate $\log \hat{Q}(z, k, b, \rho)$ for every loan origination; compute partial derivatives
4. At steady state, $\gamma = \theta = 1/T$

Estimating \mathcal{M} : Q elasticities

▷ back

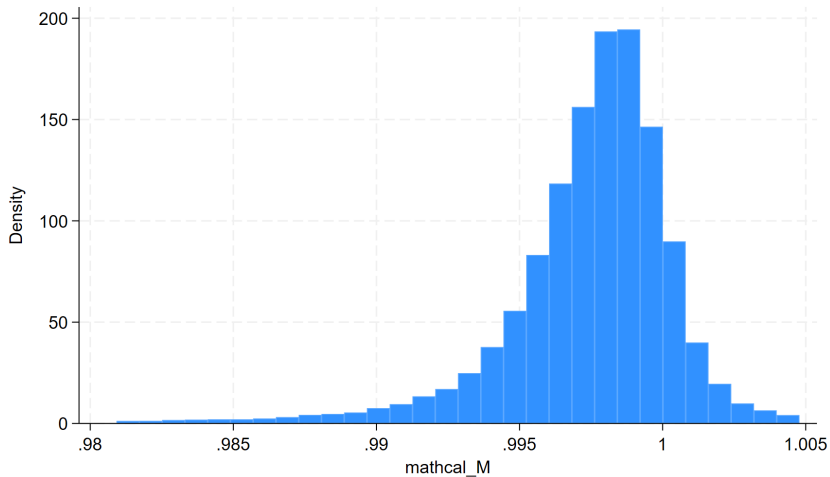
- We approximate (the log of) Q as a polynomial of firm capital, borrowing, productivity and ρ

$$\begin{aligned}\log Q_i = & \alpha + \beta_k \log k_i + \beta_b \log b_i + \beta_z \log z_i + \beta_\rho \rho_i \\ & + \beta_{k,k} (\log k_i)^2 + \beta_{k,b} \log k_i \times \log b_i + \beta_{k,z} \log k_i \times \log z_i + \beta_{k,\rho} \log k_i \times \rho_i \\ & + \beta_{b,b} (\log b_i)^2 + \beta_{b,z} \log b_i \times \log z_i + \beta_{b,\rho} \log b_i \times \rho_i \\ & + \beta_{z,z} (\log z_i)^2 + \beta_{z,\rho} \log z_i \times \rho_i + \beta_{\rho,\rho} (\rho_i)^2 + \epsilon_i\end{aligned}$$

- Capital: tangible assets
- Borrowing: total debt owed by the firm at loan origination
- Productivity: sales over tangible assets
- This allows us to compute $\frac{\partial \log Q}{\partial \log k'}$ and $\frac{\partial \log Q}{\partial \log b'}$

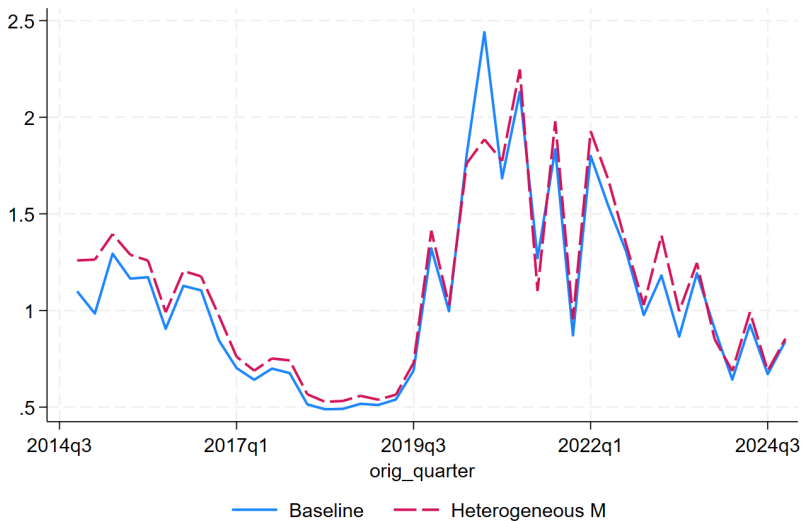
Estimating \mathcal{M} : results

[▷ back](#)



Misallocation with heterogeneous \mathcal{M}

▷ back



	Time	Bank	Firm	Loan
Contractual rate	69	2	15	15
Real rate	49	4	25	22
ρ	43	4	23	30
r^{firm}	17	4	31	49
r^{social}	35	4	25	36

Notes: 1,844 firms and 16,088 loans. Sample restricted to firms with at least five securities.

Within-period dispersion of r^{social} :

- Bank 6%
- Firm 38%
- Loan 55%

Large dispersion even within a quarter-bank-firm relationship.

Validation: r^{social} correlates with standard measures of ARPK

▷ back

	(1)	(2)	(3)	(4)	(5)
	$\log(ARPK), \text{Sales}$	$\log(ARPK), \text{EBITDA}$	$\log(ARPK), \text{Sales}$	$\log(ARPK), \text{EBITDA}$	$\log(ARPK), \text{VA}$
$\log(r^{social} + \delta)$	0.15*** (0.03)	0.24*** (0.04)	0.16** (0.07)	0.15* (0.08)	0.39*** (0.07)
Observations	59294	57334	4184	4072	3432
Adj. R2	0.27	0.22	0.68	0.52	0.61
NAICS4, Quarter FE	yes	yes	yes	yes	yes
Sample	Y-14	Y-14	Compustat	Compustat	Compustat

Robust standard errors in parentheses

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$

ARPK-based misallocation

▷ back

Focus on Compustat firms to make measures comparable

	$r^{social} + \delta$	$\frac{\text{Sales}}{\text{Capital}}$	$\frac{\text{EBITDA}}{\text{Capital}}$	$\frac{\text{Value Added}}{\text{Capital}}$
$Var(\log)$	0.01	0.19	0.24	0.21
Misallocation (%)	0.36	4.75	6.20	5.28

- Our measure looks only at misallocation coming from heterogeneity in the cost of capital
- ...but does not require detailed data on firm financials (i.e., value added)
- \implies directly applicable to most existing credit registries

	(1)	(2)	(3)	(4)	(5)
	log <i>ARPK</i> , Sales	log <i>ARPK</i> , EBITDA	log <i>ARPK</i> , Sales	log <i>ARPK</i> , EBITDA	log <i>ARPK</i> , VA
$\log(r^{social} + \delta)$	0.15*** (0.03)	0.24*** (0.04)	0.16** (0.07)	0.15* (0.08)	0.39*** (0.07)
Observations	59294	57334	4184	4072	3432
Adj. R2	0.27	0.22	0.68	0.52	0.61
NAICS4, Quarter FE	yes	yes	yes	yes	yes
Sample	Y-14	Y-14	Compustat	Compustat	Compustat
Var(log <i>ARPK</i>)	1.97	1.52	0.19	0.24	0.21
Misalloc., <i>ARPK</i> , %	63.63	46.08	4.75	6.20	5.28
Var(log($r^{social} + \delta$))	0.04	0.04	0.01	0.01	0.01
Misalloc., $r^{social} + \delta$, %	0.96	0.96	0.36	0.36	0.36

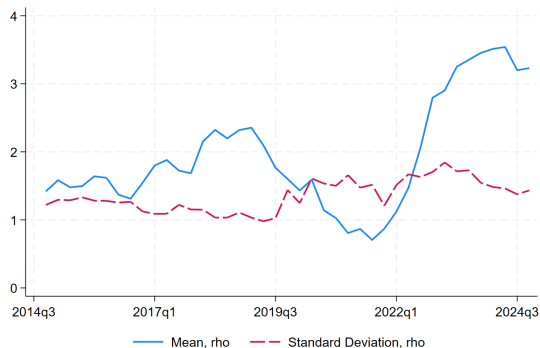
Standard errors in parentheses

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$

The 2020–2021 increase in misallocation

1. Driven by dispersion in lender discount rates ρ_i , not financial frictions.
2. Sharp rise in the coefficient of variation of ρ_i .
3. Variance of ρ_i increases due to increased dispersion of expected losses.

2. The CV of ρ_i increased during 2020-21



- Policy rates \downarrow in 2020-21 \Rightarrow mean $\rho_i \downarrow$
- $\sigma(\rho_i) \uparrow$ during this period - why?

\Rightarrow 2. Coefficient of variation of $\rho_i \uparrow$

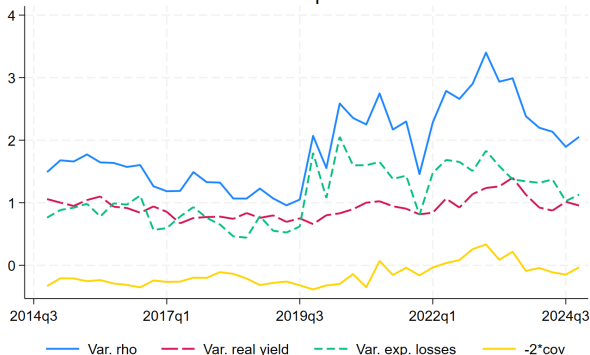
3. Variance of ρ related to variance of expected losses

- Compute “real yield” $\rho_{i,t}^*$: lender discount rate if no default

▷ real yield

- Decomposition: $\rho_i = \underbrace{\rho_i^*}_{\text{real yield}} - \underbrace{[\rho_i^* - \rho_i]}_{\text{exp. losses}}$

Variance decomposition of rho



Variance of ρ_i :

$$\mathbb{V}[\text{yield}] + \mathbb{V}[\text{exp. losses}] - 2C[\text{yield}, \text{exp. losses}]$$

- Increase in variance explained by exp. losses
- Covariance falls in absolute value
- \uparrow in dispersion of exp. losses without \uparrow in dispersion of contractual rates