## **Introduction to Crystal Plasticity Finite Element Method (CPFEM)**

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The present document is an introduction manual on how to use the crystal plasticity finite element method (CPFEM) for materials deformation simulation. CPFEM is based on a crystal plasticity constitutive model incorporated in the UMAT user subroutine of the commercial finite element software ABAQUS 6.9. The single crystal or polycrystal of face-centered cubic (FCC), body-centered cubic (BCC) and hexagonal closed (HCP) structures will respond to an applied stress by dislocation slip which is simulated using CPFEM. Orientations of grains will rotate during deformation. At the same time, the threshold stress of each slip systems will increase because of the self-hardening and latent hardening of the deformation modes. As such, the mechanical response (stress-strain curve) and the orientation of the crystals (texture) will be captured by the CPFEM. By comparing predicted results with experiments, one can get useful information about deformation mode activation, stress-strain data and crystal re-orientations, aspects that lead to a fundamentally understanding of the nature of metal deformation at the grain scale.

This particular document includes six parts as follows:

- a) Introduction
- b) Setup
- c) Input files
- d) Running CPFEM
- e) Output files
- f) References

#### Introduction

Crystal Plasticity model coded in the subroutine UMAT describes the deformation of single crystals and polycrystals assuming crystallographic slip as the main deformation mode. For a given initial texture and material parameters of the model, the code computes the stress-strain response and orientation evolution of single crystals or aggregate of crystals.

#### Setup

To use CPFEM, one need first install the finite element software ABAQUS in your computer. At present, we have a license to run ABAQUS 6.9 at CAVS.

The steps of running CPFEM in ABAQUS as follows:

#### Step 1:

Open ABAQUS in the current folder.

swsetup abaqus---> abaqus cae--->file---> open database (select oneelement.cae) as

# Figure 1.

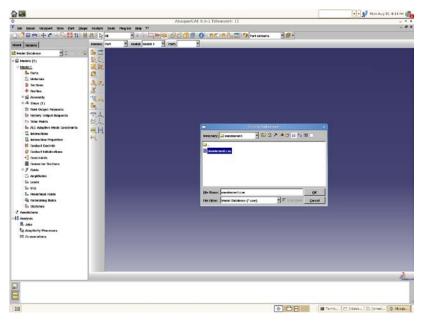


Figure 1. Open the oneelement.cae

# **Step 2**: Create a job, click the *job* menu and select *create* menu as Figure 2:

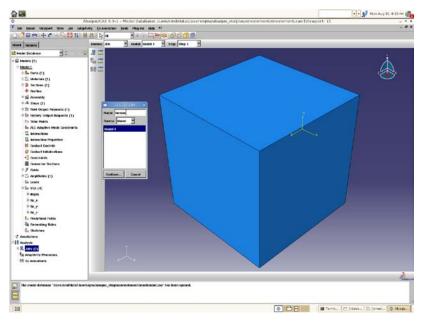


Figure 2. Create a job and give a name (e.g. tension)

# Step 3:

Coutinue-- $\rightarrow$ General-- $\rightarrow$ Select the crystal plasticity model *umat\_xtal.f* as the *subroutine* file as Figure 3.

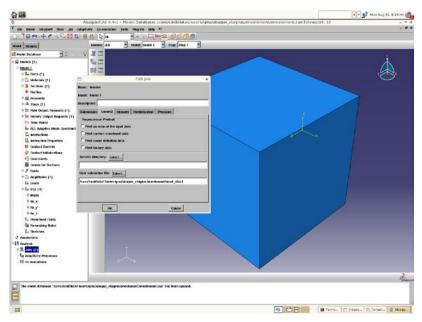


Figure 3. Select the CPFEM model umat\_xtal.f

# Step 4:

Right click job menu-- $\rightarrow$ Manager-- $\rightarrow$  select the job--- $\rightarrow$  submit the job and run the job in ABAQUS as Figure 4 below.

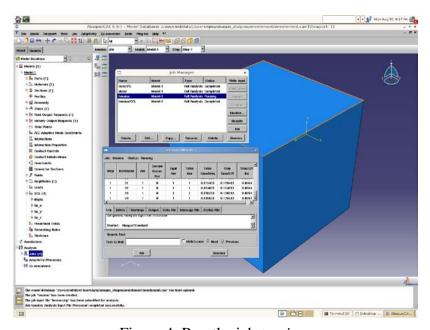


Figure 4. Run the job tension.

# Step 5:

Job is done as shown in Figure 5.

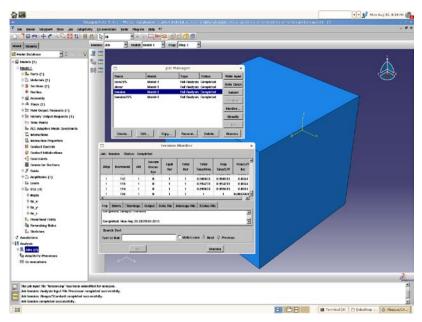


Figure 5. Job is done.

# Step 6:

Check the result as Figure 6.

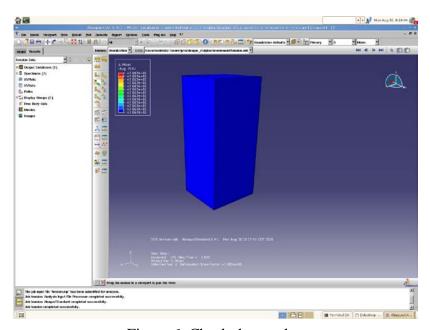


Figure 6. Check the results.

As for **compression** and **simple shear**, one just needs to change the boundary conditions as follows:

## For compression:

BC---→displa---→change the U3 from "0.75" to "-0.75".

## For simple shear:

BC---→fixZ as U1=U2=U3=0---→displa check U2=0.75 uncheck U1 and

```
U2---→create a job----→submit job----→run job.
```

#### **Input files**

There are five input files and they must be located in the same folder which you will run the CPFEM. These five files are:

```
umat_xtal.f
texture.txti
fcc.sx
test.xtali
params_xtal.inc
numbers.inc
```

#### • umat\_xtal.f

The umat\_xtal.f file is the central file of CPFEM. It integrates the constitutive equations of crystal plasticity. One must change the variable path in the code to your present working directory::

```
& /'/cavs/cmd/data1/users/***/'/
The folder "***" is your working directory.
```

The first several lines in the umat\_xtal.f subroutine look like as follows:

```
С
2
С
  UMAT subroutine for crystal plasticity - SNL & MSU
С
2
С
     subroutine umat ( stress, statev, ddsdde, sse,
                                                spd,
    &
                     scd,
                            rpl,
                                   ddsddt,
                                          drplde, drpldt,
    &
                     strain, dstrain, time,
                                        dtime,
                                               temp,
    &
                    dtemp,
                            predef, dpred,
                                           cmname, ndi,
    &
                    nshr,
                            ntens,
                                   nstaty, props,
                                                 nprops,
                            drot,
                                   pnewdt, celent, dfgrd0,
    &
                     coords,
                     dfgrd1,
    &
                           noel,
                                          layer,
                                                 kspt,
                                   npt,
    &
                    kstep,
                            kinc)
```

```
include 'ABA_PARAM.INC' character*8 cmname
```

. . . . . .

#### • texture.txti

texture.txti contains the initial texture information used in the simulation. It can include many initial orientations as Euler angles using Kocks convention. The texture.txti contains the following lines:

500		
0 0		
101.98	145.03	249.44
131.73	86.26	229.29
13.58	153.68	314.40
88.98	124.12	115.16
132.81	105.72	180.69
238.51	61.10	158.50
346.98	88.58	325.61
82.38	144.74	207.65
329.83	45.23	169.92
208.78	79.17	347.94
144.95	30.76	261.40
31.83	159.33	264.14
228.51	95.52	192.43
158.86	79.44	359.90
253.69	118.83	330.44
48.85	160.26	259.66
55.97	134.44	65.93
71.21	139.18	354.20
327.43	125.04	162.16
146.09	99.43	133.64
202.51	74.62	274.15
51.67	97.14	63.49

555

The number 500 means that there are 500 orientations in this texture file. The last line number 555 is the seed number it should be larger than the total orientation number (500 in this case). The three columns of data are the corresponding three Euler angles in Kocks convention.

#### • fcc.sx

fcc.sx is another key input file. It includes all the deformation modes and the corresponding hardening parameters. When you change these parameters you will get different output results. The parameters of these deformation modes can be obtained in the published literature or by calibration using experimental data. It includes the following:

```
2
                                           / elastID (1: iso, 2: ani) /
108.2e3 61.3e3 28.5e3
                                           / c11(c1), c12(c2), c44(c3) /
10.0e-6 10.0e-6 10.0e-6
                             0.0e0
                                      0.0e0
                                               0.0e0
                                                            /Thermal expansion Coeffs/
1.0
           dummy for Cubic Crystals (for hcp: c/a ratio)
2
            nmodesx
                         (total # of modes listed in file)
1
            nmodes
                         (# of modes to be used in the calculation)
1
                        (label of the modes to be used)
            mode(i)
28
                  = nvtx (number of vertices of scys)
vert fcc.028.00
                = filename for file with vertices of scys
*<111>{110} SLIP
 1 12 1
                                       modex,nsmx,isensex
0.05 1.0
                                        / xm, gam0 /
 5.e-4
                                        /bdrag/
 20. 40 3.7
            30.80 0.0-4 5.0e10
                                      / h0, tausi, taus0, xms, gamss0 /
3.7
                                      / initial slip system hardness (kappa0) /
 0.000
         0
                  0.000
                           0.000
                                            twshx,isectw,thres1,thres2
       1.0
              1.0
                                            hlat(nmodes)
   1. 1. 1.
                     0. 1.-1.
   1.
      1.
          1.
                     1. 0.-1.
   1.
      1.
         1.
                     1. -1. 0.
                     0. 1.-1.
  -1.
      1.
         1.
  -1.
      1.
          1.
                     1. 0. 1.
  -1. 1. 1.
                     1. 1. 0.
  -1. -1. 1.
                       1. 1.
                    0.
  -1. -1.
                    1. 0. 1.
  -1. -1. 1.
                    1. -1. 0.
   1. -1. 1.
                    0. 1. 1.
   1. -1. 1.
                     1. 0.-1.
                     1. 1. 0.
   1. -1. 1.
*<111>{112} TWIN
2 12 0
                                       modex,nsmx,isensex
 0.05 1.0
                                         / xm, gam0 /
5.e-4
                                        /bdrag/
 20.40
        3.7
             30.80
                    0.0-4 5.0e10
                                       / h0, tausi, taus0, xms, gamss0 /
 3.7
                                      / initial slip system hardness (kappa0) /
 0.707
         0
                  0.100
                           0.500
                                            twshx,isectw,thres1,thres2
              1.0
       1.0
                                            hlat(nmodes)
       1. 1.
   1.
                    -2. 1. 1.
       1. 1.
                     1. -2. 1.
   1.
      1.
         1.
                     1. 1.-2.
  -1.
      1.
         1.
                     2. 1. 1.
      1.
                    -1. -2. 1.
  -1.
         1.
```

```
-1. 1. 1. -1. 1. -2.

-1. -1. 1. 2. -1. 1.

-1. -1. 1. -1. 2. 1.

-1. -1. 1. -1. -2.

1. -1. 1. 1. 2. 1.

1. -1. 1. 1. 1. 2. 1.

1. -1. 1. 1. -1. -2.
```

#### • test.xtali

This input file controls which structure you will use and how many orientations you will use in your simulation. The file structure looks like as follows:

```
500
                                               / crystalID (1:FCC, 2:BCC, 3:HCP), numgrn/
1
fcc.sx
                                            / single crystal input file
1
                                         / ODF code (fODFCode) /
20
                                              / multiples of inc to output texture (fODFOutInc) /
texture
                                            / filename for I/O texture /
200 1.0d-5
                                             / maxIterState, tolerState /
200 1.0d-10
                                              / maxIterNewt, tolerNewt (absolute tolerance) /
 20
                                              / maxIterN (global Newton) /
 1.0d-8 1.0d-10 100.d0
                                             / tolerN, zeroTolerN, divTolerN /
                                            / alwaysLS (global line search) /
 .true.
                                            / searchIters (if 0 -> LS is off) /
 0.1d0
          2.5d0
                                              / maxStepSize, orthoToler /
 10
                                              / maxIncrCuts (allowable time step cuts) /
                                              / quickSolveTol (# iters in a "quick" solution) /
  6
  3
                                              / quickSeriesTol (# "quick" solns before time step
increase) /
  0.01d0
                                              / DEQP_ref /
   1000.0
                                              / number of load stages, total time /
 1
                                              / stage i
  0.01
                                       / dtimeStage(i), incrStage(i) /
          150
 1255.0
            1255.0
                                              / thetaStage_n(i), thetaStage(i) /
 0.5d-0
          0.0
                   0.0
                                             / velGradStage(i) - PSC /
 0.0
           0.5d-0 0.0
 0.0
                  -1.0d-0
           0.0
```

The number 500 is the total number of grains. If one change it to 1 that means just one grain will be deformed. Note that there are 12 {111}<011> slip systems in a FCC structure.

#### • params\_xtal.inc

The params\_xtal.inc input file defines some control parameters. Usually, users can not change this input file. But, users should change the parameter like below when you simulate 2D or 3D problems.

parameter (NTENS=6, NDI=3, NSHR=3) // this parameter for 3D structure c parameter (NTENS=4, NDI=3, NSHR=1) // this parameter for 2D structure

#### • numbers.inc

This file lists a number of numerical constants used in the UMAT. This file does not need to be changed.

## **Running CPFEM**

To run CPFEM in your computer, make sure all the input files have been loaded in your present working folder. You also need to change the working path in the input file: umat\_xtal.f. First, you should install ABAQUS and open the ABAQUS CAE and create your 2D or 3D structure model. At present, you can directly open the example CAE file *oneelement.cae* to practice as shown in **SETUP** part of this manual. Note that the boundary conditions also need to be changed if you want to change the deformation condition, e.g., uniaxial compression, shear, plane strain compression.

## **Output files**

Output files of CPFEM include the texture.txto, test.xtal.trss, test.xtal.strs, test.xtal.strs, test.xtal.efss and test.agg.efss. The texture.txto contains the deformed texture at various strain levels. One can use this file to plot any pole figures and calculate orientation distribution functions (ODFs) using the texture software MTEX (a MATLAB tool box, it is a powerful texture calculation tool and can download free through website: <a href="http://code.google.com/p/mtex/">http://code.google.com/p/mtex/</a>). The output file test.agg.effss includes the effective stress-strain data. One can also use the ABAQUS CAE to output any stress- strain data.

The texture.txto file looks like as follows:

\*----\*
Initial Assigned Orientations -----\*

ang1	ang2	ang3	igrn	intpt	ielem //	ang1 ang2 ang	3 are the three Euler angle
101.98	145.03	249.44	1	1	1 // i	n degree. Igrn r	neans the grain ID, intpt
131.73	86.26	229.29	2	1	1 // m	eans the integra	ation point in one element.
13.58	153.68	314.40	3	1	1// ie	elem means the	element ID.
88.98	124.12	115.16	4	1	1		
132.81	105.72	180.69	5	1	1		
238.51	61.10	158.50	6	1	1		
346.98	88.58	325.61	7	1	1		
82.38	144.74	207.65	8	1	1		
329.83	45.23	169.92	9	1	1		
208.78	79.17	347.94	10	1	1		
144.95	30.76	261.40	11	1	1		
31.83	159.33	264.14	12	1	1		
228.51	95.52	192.43	13	1	1		
158.86	79.44	359.90	14	1	1		
253.69	118.83	330.44	15	1	1		
48.85	160.26	259.66	16	1	1		
55.97	134.44	65.93	17	1	1		
71.21	139.18	354.20	18	1	1		
327.43	125.04	162.16	19	1	1		
146.09	99.43	133.64	20	1	1		
202.51	74.62	274.15	21	1	1		
51.67	97.14	63.49	22	1	1		
26.77	85.13	4.27	23	1	1		
131.69	72.44	156.67	24	1	1		
78.50	137.25	212.56	25	1	1		
			400	4	1		
66.60	166.72	222.04	498	1	1		
83.61	117.93	341.25	499	1	1		
165.49	99.96	280.51	500	1	1	E 1 1 .	
	Ü	les at incr				_	time increments 40 steps.
ang1 107.41	ang2	•	igrn 1	intpt 1	ielem 1	kappa(1) 10.63	d_eff 0.67E+00
131.71		-113.38					
			2	1	1	11.07	0.67E+00
12.89		-45.11	3	1	1	9.87	0.67E+00
86.95	124.16	120.29	4	1	1	10.67	0.67E+00
132.74	104.13		5	1	1	9.13	0.67E+00
-122.81	59.81	152.79	6 7	1	1	10.28	0.67E+00
-13.04	88.00	-33.76	7	1	1	10.97	0.67E+00
76.07	141.80		8	1	1	10.37	0.67E+00
-32.65	45.71	166.46	9	1	1	10.97	0.67E+00
-151.38	80.23	-10.99	10	1	1	9.01	0.67E+00

142.43							
	30.21	-100.54	11	1	1	10.23	0.67E+00
32.01	161.13	-95.34	12	1	1	9.14	0.67E+00
-131.60	94.62 -	169.37	13	1	1	8.93	0.67E+00
158.84	81.21	-0.41	14	1	1	8.80	0.67E+00
-104.88	120.04	-33.01	15	1	1	10.77	0.67E+00
49.33	162.00	-99.89	16	1	1	9.18	0.67E+00
60.01	132.27	60.40	17	1	1	10.57	0.67E+00
72.79	139.19	-7.52	18	1	1	11.27	0.67E+00
-30.56	125.08	156.85	19	1	1	10.55	0.67E+00
146.11	102.39	133.37	20	1	1	11.08	0.67E+00
-157.84	76.31	-85.81	21	1	1	8.94	0.67E+00
53.15	99.78	64.33	22	1	1	9.72	0.67E+00
26.75	85.72	3.81	23	1	1	8.94	0.67E+00
130.40	69.51	154.34	24	1	1	9.97	0.67E+00
74.85	134.43	-143.15	25	1	1	10.76	0.67E+00
13.19	85.09	10.88	26	1	1	9.03	0.67E+00
118.70	144.81	129.49	27	1	1	10.21	0.67E+00
* E	uler Ang	les at incr	180	*//gra	in orientati	ons at time inc	rement 180 steps.
ang1	ang2	ang3	igrn	intpt	ielem	kappa(1)	d_eff
121.95					iciciii	11 ( )	<u>u_</u>
121.75	133.62	-130.26	1	1	1	23.54	0.44E+00
130.82		-130.26 -129.40	1 2	1			_
					1	23.54	0.44E+00
130.82	75.37	-129.40	2	1	1	23.54 24.01	0.44E+00 0.44E+00
130.82 12.08	75.37 138.01 124.35	-129.40 -44.72	2 3	1 1	1 1 1	23.54 24.01 22.80	0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19	75.37 138.01 124.35	-129.40 -44.72 129.85	2 3 4	1 1 1	1 1 1 1	23.54 24.01 22.80 24.06	0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18	75.37 138.01 124.35 98.64	-129.40 -44.72 129.85 -178.02 141.02	2 3 4 5	1 1 1	1 1 1 1	23.54 24.01 22.80 24.06 20.45	0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03	75.37 138.01 124.35 98.64 56.45	-129.40 -44.72 129.85 -178.02 141.02 -31.52	2 3 4 5 6	1 1 1 1	1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03	75.37 138.01 124.35 98.64 56.45 84.29	-129.40 -44.72 129.85 -178.02 141.02 -31.52	2 3 4 5 6 7	1 1 1 1 1	1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03	75.37 138.01 124.35 98.64 56.45 84.29	-129.40 -44.72 129.85 -178.02 141.02 -31.52	2 3 4 5 6 7	1 1 1 1 1	1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03	75.37 138.01 124.35 98.64 56.45 84.29	-129.40 -44.72 129.85 -178.02 141.02 -31.52	2 3 4 5 6 7	1 1 1 1 1	1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03	75.37 138.01 124.35 98.64 56.45 84.29	-129.40 -44.72 129.85 -178.02 141.02 -31.52 -137.48 47.89	2 3 4 5 6 7	1 1 1 1 1	1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03 67.51	75.37 138.01 124.35 98.64 56.45 84.29 131.49	-129.40 -44.72 129.85 -178.02 141.02 -31.52 -137.48	2 3 4 5 6 7 8	1 1 1 1 1 1	1 1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83 23.67	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03 67.51	75.37 138.01 124.35 98.64 56.45 84.29 131.49	-129.40 -44.72 129.85 -178.02 141.02 -31.52 -137.48 	2 3 4 5 6 7 8 	1 1 1 1 1 1	1 1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83 23.67	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03 67.51 -118.68 -61.62 64.36 89.08	75.37 138.01 124.35 98.64 56.45 84.29 131.49 128.22 109.73 173.91 122.13	-129.40 -44.72 129.85 -178.02 141.02 -31.52 -137.48 	2 3 4 5 6 7 8  496 497 498 499	1 1 1 1 1 1	1 1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83 23.67 24.14 22.29 20.17 23.53	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00
130.82 12.08 82.19 132.88 -128.18 -14.03 67.51 -118.68 -61.62 64.36	75.37 138.01 124.35 98.64 56.45 84.29 131.49 128.22 109.73 173.91	-129.40 -44.72 129.85 -178.02 141.02 -31.52 -137.48 47.89 61.42 -135.95	2 3 4 5 6 7 8  496 497 498	1 1 1 1 1 1 1	1 1 1 1 1 1 1 1	23.54 24.01 22.80 24.06 20.45 23.78 23.83 23.67 24.14 22.29 20.17	0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00 0.44E+00

As such, the first three columns of data are the texture information. You can use the first three columns of Euler angles and MTEX to plot pole figure.

As for stress-strain data, one can obtain these results as follows:

## Step 1:

File---→Open---→\*.odb---→Tools--→XY Data---→Manager...-→Create...-→ODB field output --→Continue...on the figure select select Unique Nodal, select strain LE33 as Figure 7.

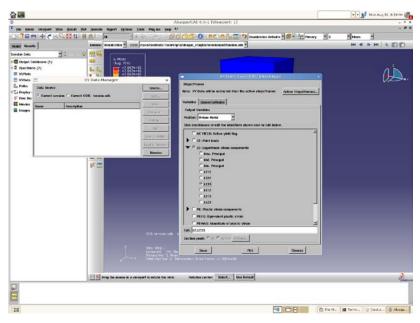


Figure 7. Select strain LE33 as the output data.

## **Step 2:**

Select one node at the force surface as shown by the red dot in Figure 8, press Done--- $\rightarrow$ save--- $\rightarrow$ Ok.

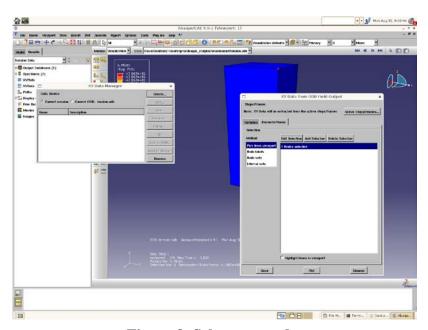


Figure 8. Select one node.

## **Step 3:**

Remove the LE33 in the edit field, and then select S33 stress as the stress output data

everything as above, as shown in Figure 9.

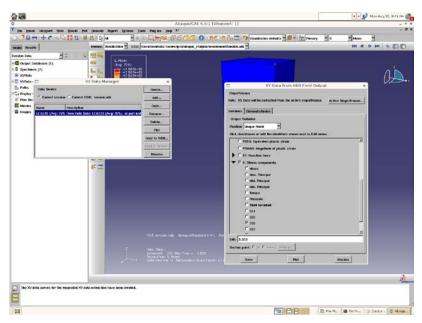


Figure 9. Select stress S33 as the output data.

## **Step 4:**

Click Create... menu again and click Operate on XY Data as shown in Figure 10. In the XY Data manager window we have both STRAIN and STRESS data.

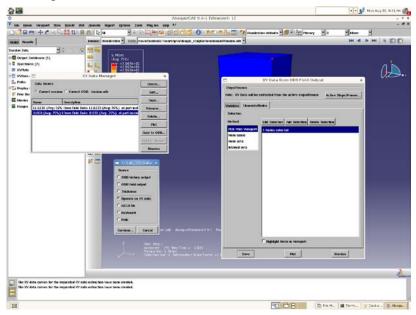


Figure 10. Operate on stress-strain data.

## **Step 5:**

Select combin() and add the strain and stress data to the combin () as shown in Figure 11.

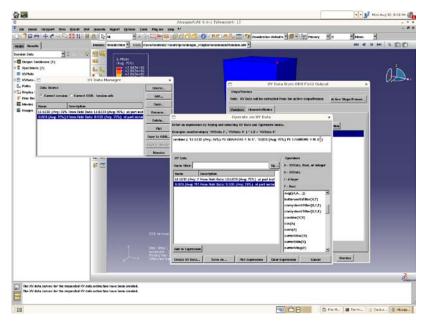


Figure 11. combine stress and strain data.

## Step 6:

Plot stress-strain curve as shown in Figure 12.

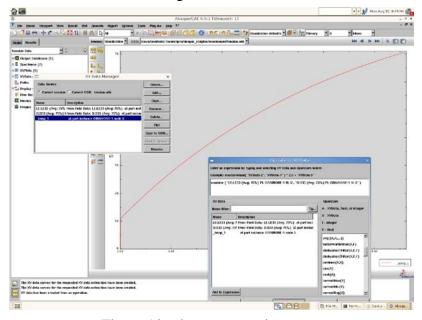


Figure 12. plot stress-strain curve.

# **Step 7:**

Save stress-strain data as shown in Figure 13 and Figure 14. Save as--- $\rightarrow$ Report--- $\rightarrow$ Select saved data--- $\rightarrow$ Setup---- $\rightarrow$ select--- $\rightarrow$ give name---- $\rightarrow$ Ok---- $\rightarrow$ Ok.

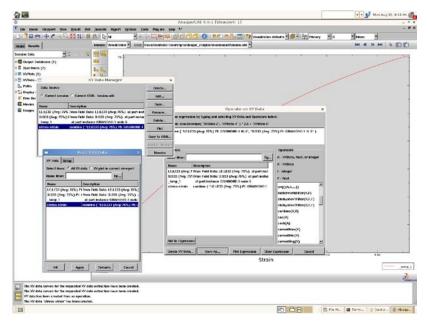


Figure 13. Save stress-strain data.

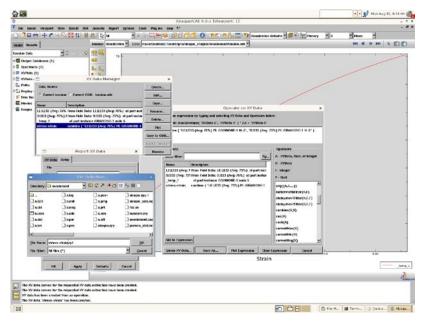


Figure 14. save the stress-strain data in the current folder.

The stress-strain data looks like as follows:

## X stress-strain

0.	//strain	0.	//stress
74.9972	2E-06	5.34312	
149.989I	E-06	8.8698	
262.466H	E-06	10.3045	
431.157I	E-06	10.7584	
684.141I	E-06	10.9172	

11.0235
11.1435
11.3073
11.5459
11.8998
12.4258
13.1561
13.8763
14.5868
15.288
15.9802
16.6636
17.3381
18.0042
18.6618
19.3112
19.9524
20.5857
21.2111
21.8287
22.4386
23.0411
23.6363
24.2243
24.2243
25.3793
25.9462
26.5064
27.0602
27.6074
28.148
28.6821
29.21
29.7318
30.2475
30.7572
31.2608
31.7585
32.2505
32.7367
33.2174
33.6926
34.1622
34.6266

154.026E-03	35.0858
157.492E-03	35.5403
160.946E-03	35.9899
164.387E-03	36.4347
167.817E-03	36.8747
171.236E-03	37.3101
174.642E-03	37.741
178.038E-03	38.1674
181.421E-03	38.5895
184.793E-03	39.0072
188.154E-03	39.4203
191.504E-03	39.8291
194.842E-03	40.2333
198.17E-03	40.6333
201.486E-03	41.0293
204.792E-03	41.4212
208.086E-03	41.8091
211.37E-03	42.193
214.643E-03	42.5729
217.905E-03	42.9491
221.157E-03	43.3214
224.398E-03	43.6897
227.629E-03	44.0543
230.849E-03	44.4152
234.059E-03	44.7727
237.259E-03	45.1267
240.448E-03	45.4771
243.627E-03	45.824
246.797E-03	46.1676
249.956E-03	46.5076
253.105E-03	46.8439
256.245E-03	47.1768
259.374E-03	47.5062
262.494E-03	47.8325
265.604E-03	48.1558
268.705E-03	48.4763
271.796E-03	48.794
274.877E-03	49.1088
277.949E-03	49.4206
281.012E-03	49.7294
284.065E-03	50.0352
287.109E-03	50.3381
290.143E-03	50.6383
293.169E-03	50.9358

296.185E-03	51.2306
299.192E-03	51.5228
302.19E-03	51.8125
305.18E-03	52.0993
308.16E-03	52.3832
311.132E-03	52.6642
314.094E-03	52.9426
317.048E-03	53.2183
319.993E-03	53.4912
322.93E-03	53.7616
325.858E-03	54.0294
328.777E-03	54.2946
331.688E-03	54.5572
334.591E-03	54.8173
337.485E-03	55.075
340.37E-03	55.3302
343.248E-03	55.5829
346.117E-03	55.8333
348.978E-03	56.0816
351.831E-03	56.3276
354.676E-03	56.5716
357.512E-03	56.8135
360.341E-03	57.0532
363.161E-03	57.2908
365.974E-03	57.5262
368.779E-03	57.7595
371.576E-03	57.9908
374.365E-03	58.2199
377.146E-03	58.447
379.92E-03	58.6719
382.686E-03	58.8946
385.444E-03	59.115
388.195E-03	59.3333
390.938E-03	59.5496
393.674E-03	59.7642
396.402E-03	59.9771
399.123E-03	60.1884
401.837E-03	60.3982
404.543E-03	60.6065
407.242E-03	60.8132
409.933E-03	61.0181
412.618E-03	61.221
415.295E-03	61.4219
417.965E-03	61.6209

420.628E-03	61.8183
423.284E-03	62.0142
425.932E-03	62.2082
428.574E-03	62.4005
431.209E-03	62.5913
433.837E-03	62.7806
436.458E-03	62.9684
439.072E-03	63.1547
441.68E-03	63.3396
444.28E-03	63.5232
446.874E-03	63.7057
449.461E-03	63.8868
452.042E-03	64.0665
454.615E-03	64.2444
457.183E-03	64.4205
459.743E-03	64.595
462.297E-03	64.768
464.845E-03	64.9395
467.386E-03	65.1094
469.921E-03	65.2779
472.449E-03	65.445
474.971E-03	65.6108
477.486E-03	65.7752
479.996E-03	65.9383
482.499E-03	66.1003
484.995E-03	66.2611
487.486E-03	66.4207
489.97E-03	66.5789
492.448E-03	66.736
494.92E-03	66.8917
497.386E-03	67.0461
499.846E-03	67.199
502.3E-03	67.3504
504.748E-03	67.5003
507.19E-03	67.6489
509.626E-03	67.7962
512.056E-03	67.9423
514.48E-03	68.0874
516.898E-03	68.2314
519.31E-03	68.3745
521.717E-03	68.5164
524.118E-03	68.6573
526.513E-03	68.797
528.902E-03	68.9358

531.286E-03	69.0735
533.664E-03	69.2103
536.036E-03	69.3461
538.403E-03	69.4811
540.764E-03	69.6152
543.119E-03	69.7483
545.469E-03	69.8803
547.814E-03	70.011
550.153E-03	70.1404
552.487E-03	70.2689
554.815E-03	70.3964
557.138E-03	70.523
559.455E-03	70.6488
559.612E-03	70.6544

As such, you can plot stress-strain curve using these data above.

## References

One can read the following publications to learn the theory of CPFEM and applications.

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- [7] D. Peirce, R.J. Asaro, A. Needleman, Analysis of nonuniform and localized deformation in FCC single crystals, Acta Metallurgica, 30(1982), 1087-1119.
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