

EC443 PS 15 Question 4

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Question 4: LM Test for Autocorrelation

LM Test for autocorrelation (Breusch-Godfrey)

H_0 : No autocorrelation in error term u

H_1 : u is $AR(p)$ process

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- ▶ Perform naive OLS regression

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- ▶ Test statistic: $U = TR^2$ of this regression. Reject H_0 iff $U > \chi_1^2(0.95)$.
- ▶ For $p = 1$ this is asymptotically equivalent to Durbin h -test.