

# Trade and the End of Antiquity

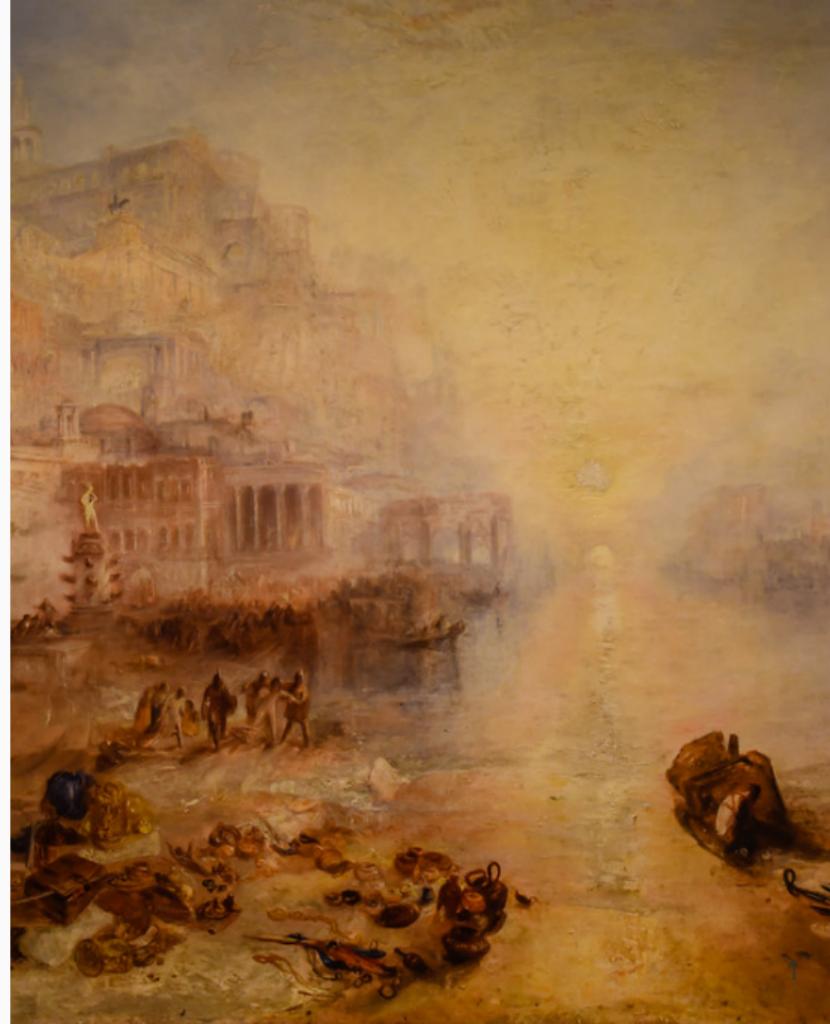
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# What caused the End of Antiquity?

- Antiquity: Roman and Greek civilizations centered around the Mediterranean
- Archaeological evidence points to a shift in economic activity away from the Mediterranean between 5th and 8th century AD (“end of antiquity”)
  - Rise of Northern Europe (Charlemagne).
  - “Golden Age” of Islam

→ *Question:* What caused the End of Antiquity?

- Discussed, among others, by Montesquieu (1734), Voltaire (1756), Gibbon (1789)
- Henri Pirenne (1937) blames the Arab conquests and the emerging Islamic-Christian border for the rupture in the Mediterranean unity

## Political changes in the Mediterranean: 600 AD



## Political changes in the Mediterranean: 600 AD



## Political changes in the Mediterranean: 600 AD



## Political changes in the Mediterranean: 600 AD



## Political changes in the Mediterranean: 632 AD



## Political changes in the Mediterranean: 634 AD

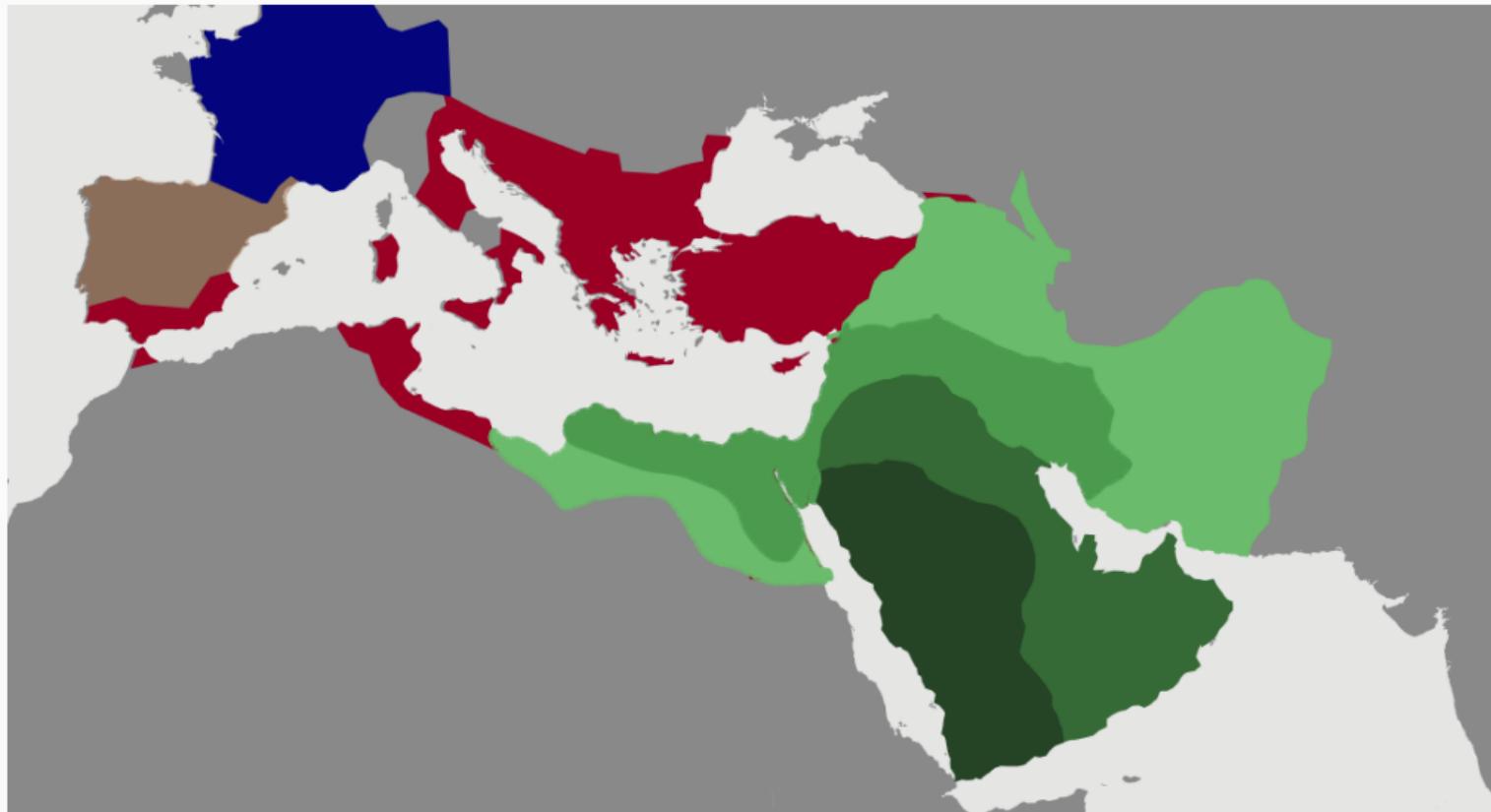


## Political changes in the Mediterranean: 644 AD

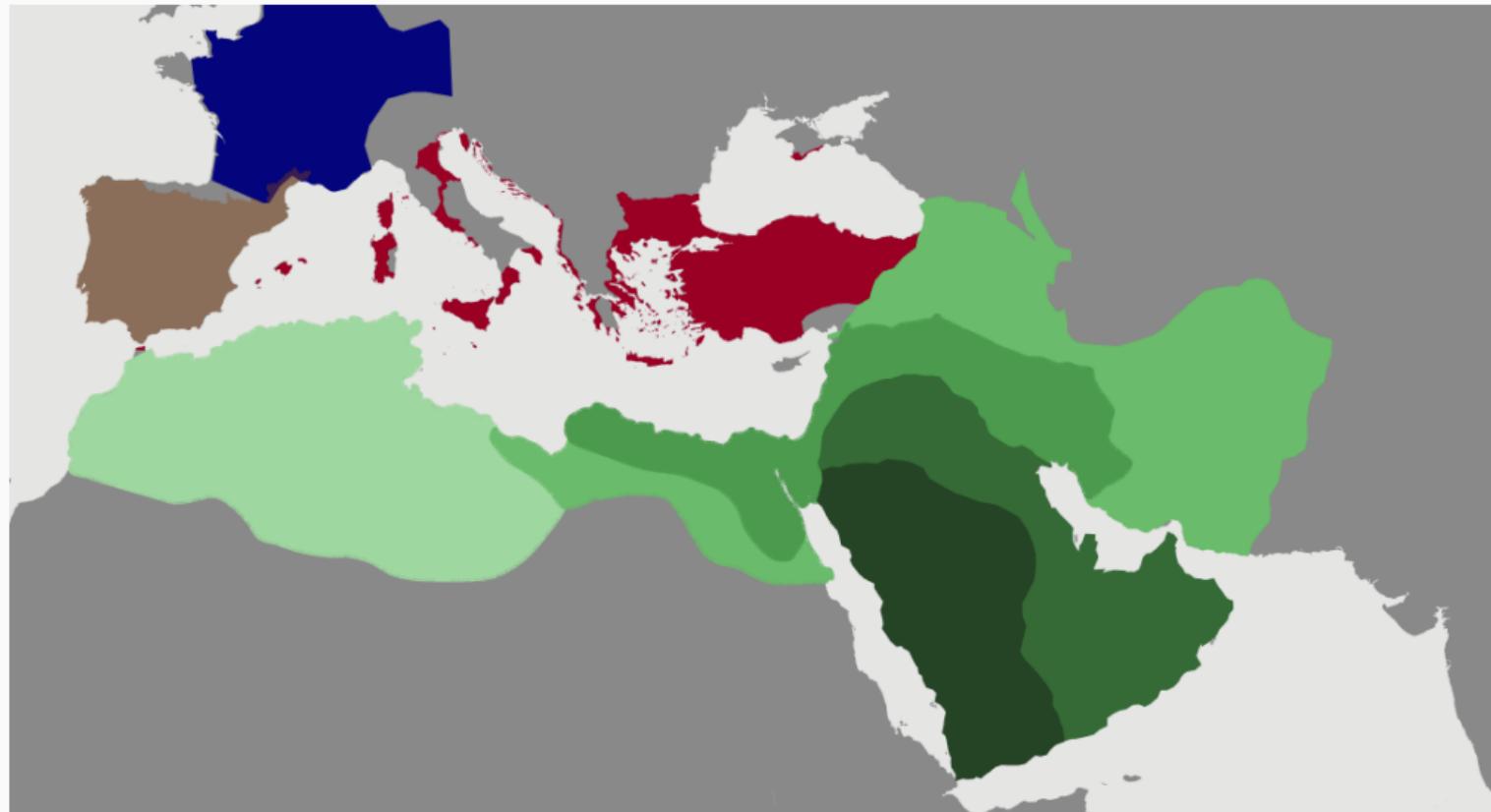


# Political changes in the Mediterranean:

661 AD

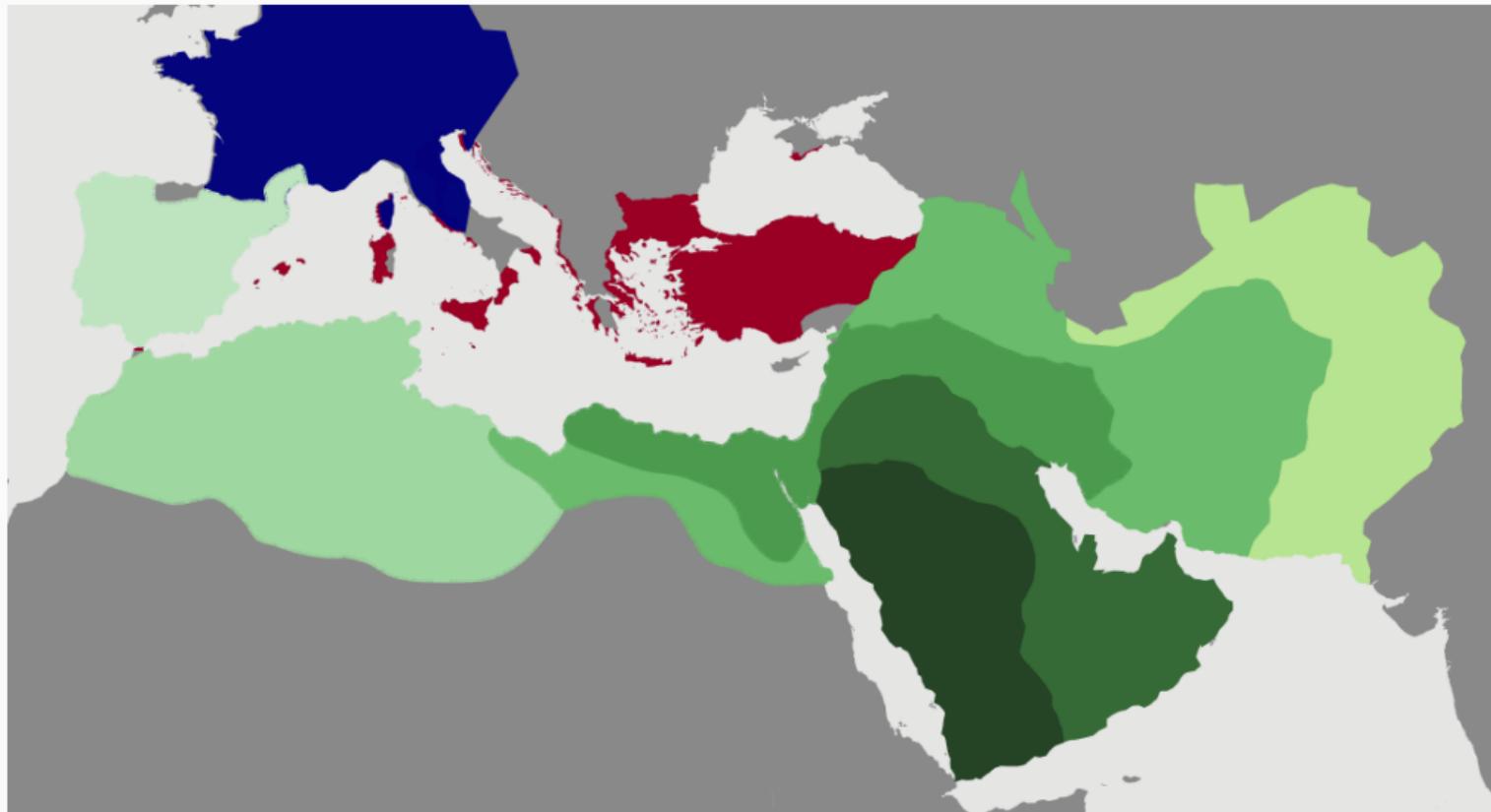


# Political changes in the Mediterranean: 661-700 AD



# Political changes in the Mediterranean:

750 AD



This paper: quantitatively investigate changing economic geography

Challenge: virtually no production/consumption/trade data

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⇒ Use data on the movement of coins to study the changing economic geography during Late Antiquity.

- Coins are the main medium of exchange during Late Antiquity, particularly for long-distance trade → informative about trade
- Coins are well studied & documented by historians and numismatists
- Coins have features that help solve econometric identification problems

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⇒ we interpret coin flows through the lens of a trade model and identify

- bilateral trade flows ( $i, j, t$ )
- technology ( $i, t$ )
- trade deficits ( $i, t$ )
- real consumption per capita ( $i, t$ )

in order to better understand what's going on during Late Antiquity

## Findings

- North-western Europe (and Islamic Spain) witness a large increase in relative real consumption in the 7th/8th century;
- Byzantine Heartlands see a large drop in relative real consumption
- Large collapse in trade in the Mediterranean, but (except for Byzantium) relatively small contribution to changes in per-capita consumption
- Most of changing relative real consumption driven by trade deficits (seigniorage) and technology.

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Econometric estimates broadly consistent with qualitative empirical evidence:

- Archaeological evidence on Carolingian commerce (Hodges and Whitehouse, 1983, McCormick, 2001, Wickham, 2006)
- Archaeological evidence on Byzantine monetary and economic collapse (“Byzantine dark ages”, Kazhdan, 1954; Pennas, 1996, Haldon, 1997)
- Urbanization patterns in Europe and Asia Minor (Brandes, 1989; Buringh, 2021)

# Outline

Data

Reduced form evidence

Model

Parameterization and Estimation

# Data: Coins around the Mediterranean, AD 325 to AD 950

Assemble a large dataset of coin finds from around the Mediterranean

## 1. FLAME (2023) project:

- “Framing the Late Antique and Early Medieval Economy.”
- Collaboration of >60 historians and numismatists.
- ~200,000 coins with complete records from ~4,600 hoards
- Pre AD 725.

## 2. Hand-coded records from numismatic / archaeological literature:

- 797 coin finds.
- 100,478 coins.
- post AD 725.

Data covers most of published literature on hoard records (and more)

## Coin hoard data: an example from al 'Ush (1972)

| No. | MINT    | DATE | DIAM. | WEIGHT | NUMB. |
|-----|---------|------|-------|--------|-------|
| 51  | الأندلس | 114  | 29.   | 2.93   | 4     |
| 52  | "       | 115  | 29.5  | 2.92   | 1     |
| 53  | "       | 116  | 26.5  | 2.92   | 3     |

Excerpt of an original publication on the Damascus silver hoard:

- record number (51)
- mint (al-Andalus) \*
- mint date (year 114 of the Hijri calendar) \*
- diameter (29mm)
- weight (2.93g)
- number of coins with these attributes (4) \*

The issuing dynasty (Umayyad) is given in the table headings and the denomination and material (silver *dirham*) is stated in the text. \* denotes required attributes

## Coin dataset

- Each coin provides the following information:
  1. Mint location (“birthplace”):  $m$
  2. Mint date (“birthdate”):  $\tau$
  3. Hoard location (“death place”):  $h$
  4. Terminus post quem,  $tpq$  (“death date”):  $T = \sup \tau$

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- 286,035 coins.
- Time:
  - Mint date > AD 325
  - $tpq$  < AD 950.
- Space:
  - Western Europe.
  - Southern Europe.
  - Northern Africa.
  - Middle East++.

## Spatial distribution: the (extended) Mediterranean

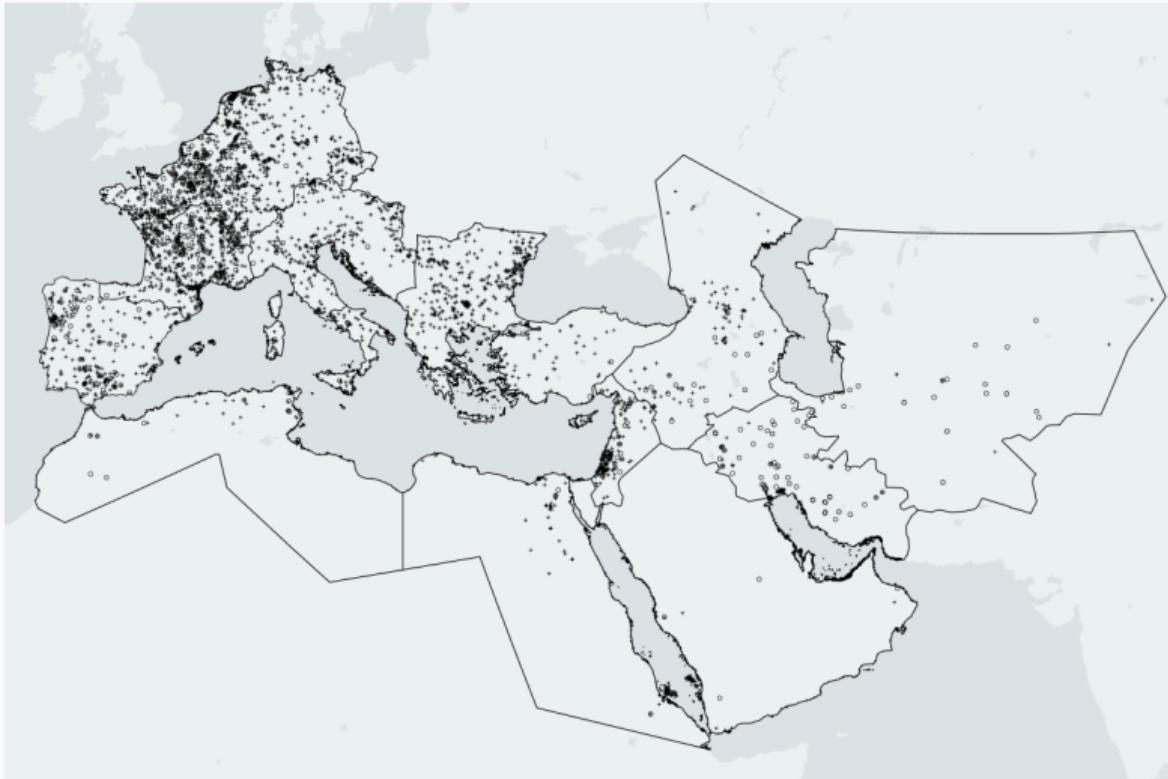


Figure 1: Region Definitions

## Distribution of coin “death dates” ( $tpq$ )

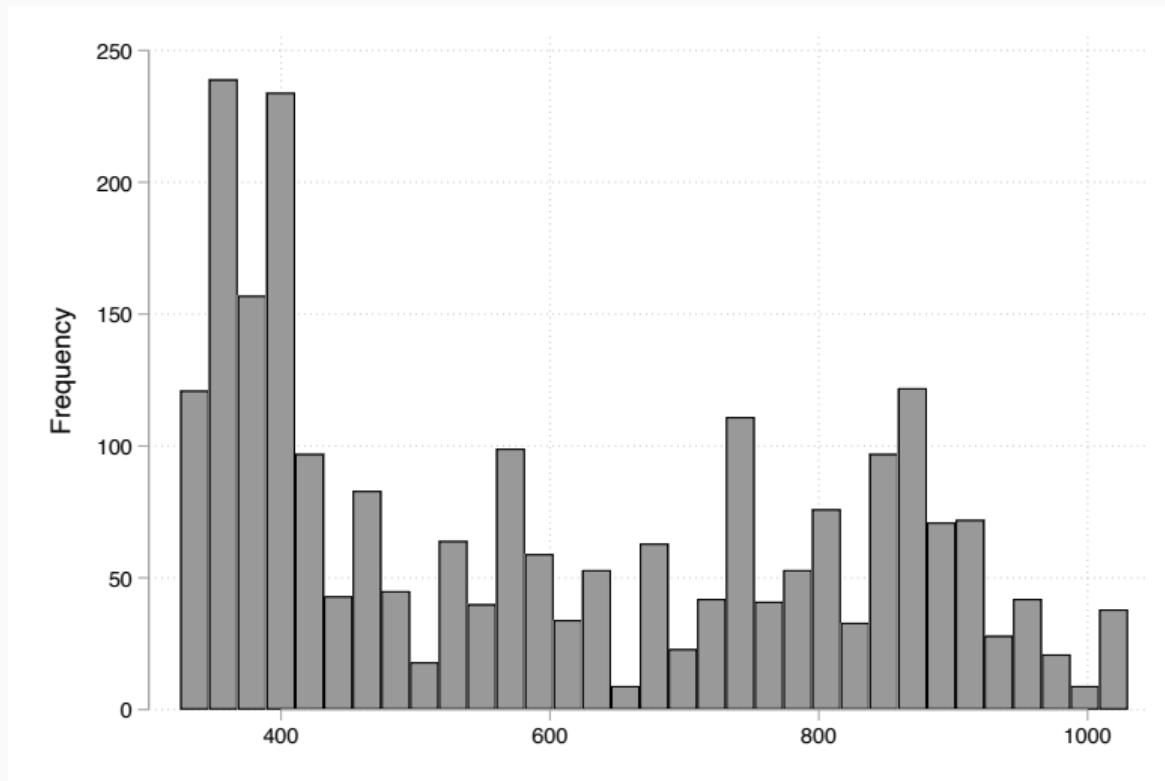


Figure 2: Terminus Post Quem ( $tpq$ ) of hoards

## Distribution of coin ages ( $tpq$ minus mint date)

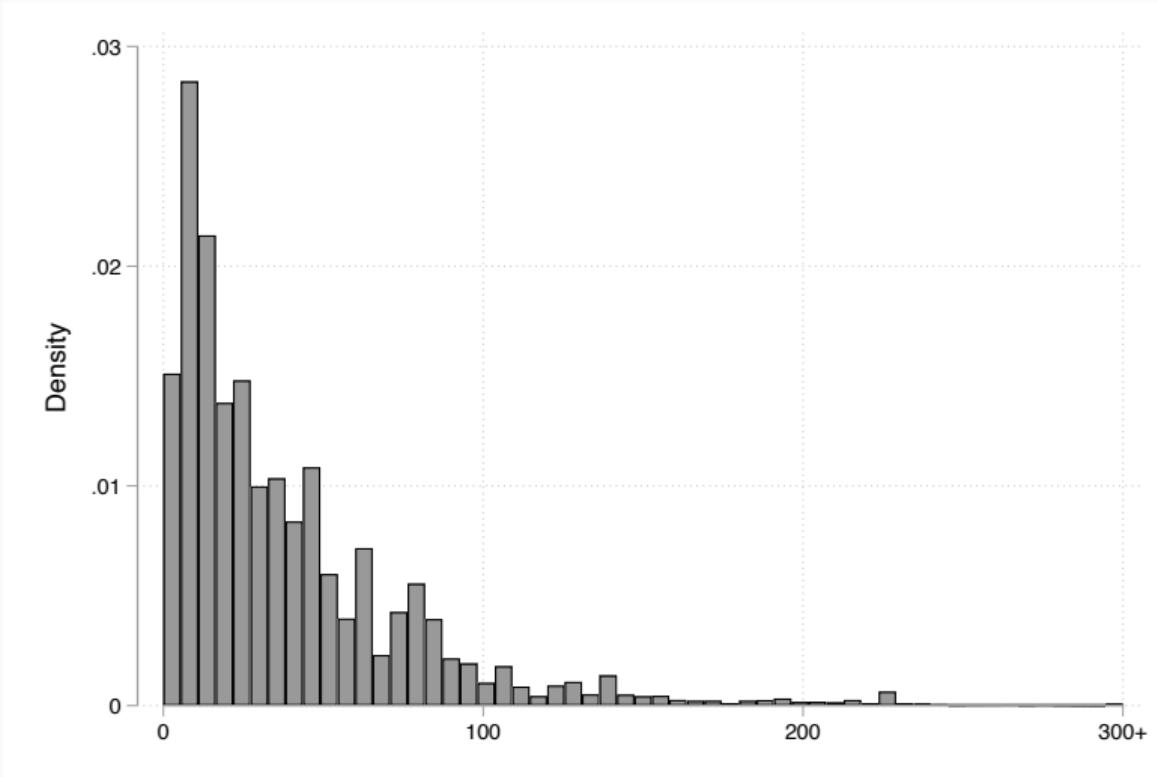


Figure 3: Coin age at time of deposit ( $tpq$ ), in years

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## Stylized facts

We document 3 main stylized facts:

1. Older coins travel further.
2. Distance *and* politics impede coin travels (gravity).
3. The geography of coin flows changes sharply around the Arab conquests.

# Fact #1: within a hoard, older coins have travel farther

Table 1: Within-hoard distance travelled and age of coin at deposit

| Dependent variable: Log Distance between Mint and Hoard |                     |                      |                     |                     |                     |
|---|---------------------|----------------------|---------------------|---------------------|---------------------|
|   | (1)                 | (2)                  | (3)                 | (4)                 | (5)                 |
| Log Age of Coin   | 0.146***<br>(0.044) | 0.0831***<br>(0.026) | 0.0749**<br>(0.031) | 0.160***<br>(0.043) | 0.0485**<br>(0.020) |
| Sample  |                     |                      |                     | No non-hoards       | No non-hoards       |
| Hoard FE  | Yes                 | Yes                  | Yes                 | Yes                 | Yes                 |
| Mint × 50-year-interval FE                              |                     | Yes                  |                     |                     |                     |
| Mint × 25-year-interval FE                              |                     |                      | Yes                 |                     | Yes                 |
| R <sup>2</sup>  | 0.762               | 0.863                | 0.869               | 0.775               | 0.898               |
| Observations  | 287243              | 287029               | 286873              | 250156              | 249830              |

Standard errors in parentheses, clustered at the hoard level.

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Age of coin =  $tpq - \text{mint date}$

⇒ coins diffuse across space over time.

## Fact #2: distance and political borders impede coin travels

Construct  $1^\circ \times 1^\circ$  cells for mint and hoard locations and calculate flows count<sub>mdh</sub>

Table 2: Gravity and Border Effects in Coin Flows

|                       | Dependent variable: # Coins <sub>mdh</sub> |                     |                     |                     |
|-----------------------|--|---------------------|---------------------|---------------------|
|                       | (1)  | (2)                 | (3)                 | (4)                 |
| Log Distance          | -1.137***<br>(0.12)                        | -1.002***<br>(0.13) | -0.727***<br>(0.10) | -0.694***<br>(0.10) |
| Political border      |  | -1.945***<br>(0.62) |                     | -1.541***<br>(0.41) |
| Hoard Cell FE         | Yes  | Yes                 | Yes                 | Yes                 |
| Mint × Empire Cell FE | Yes  | Yes                 | Yes                 | Yes                 |
| Sample                |  | Int. Marg. only     | Int. Marg. only     |                     |
| Estimator             | PPML                                       | PPML                | PPML                | PPML                |
| R <sup>2</sup>        |  |                     |                     |                     |
| Observations          | 217748                                     | 217748              | 6312                | 6312                |

Standard errors in parentheses, clustered at mint cell × empire and hoard cell level.

+ p < 0.10, \* p < 0.05, \*\* p < 0.01

Estimating eqn: count<sub>mdh</sub> = exp ( $\gamma_1 \log \text{distance}_{mh} + \gamma_2 \text{withinBorder}_{dh} + \alpha_{md} + \alpha_h + \varepsilon_{mhd}$ )

## Fact #2: distance has a weaker impact on older coin flows

$\text{logcount}_{mth\tau} =$

$$\sum_{\tau' \in T} \beta_{\tau'} \log \text{distance}_{mh} \times 1(t - \tau = \tau')$$

$$+ \alpha_{mt} + \alpha_{h\tau} + \varepsilon_{mth\tau}$$

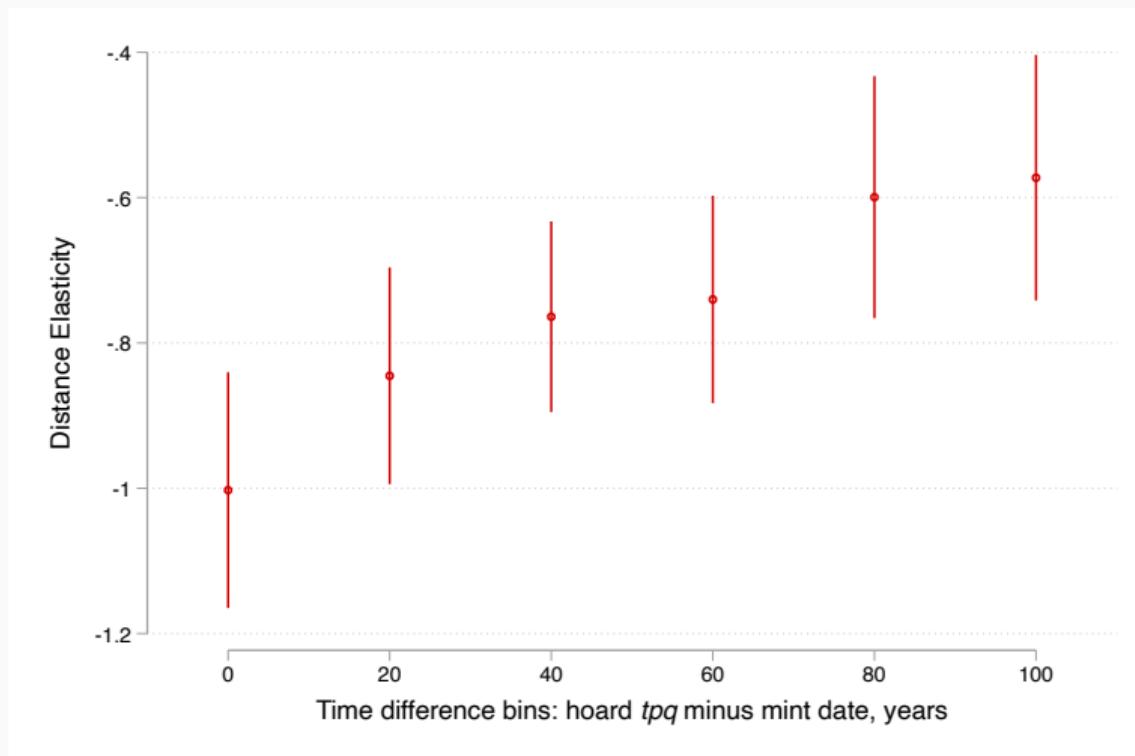


Figure 4: The distance elasticity declines as coins get older

## Fact #3: Coin flows before/after the Arab conquests

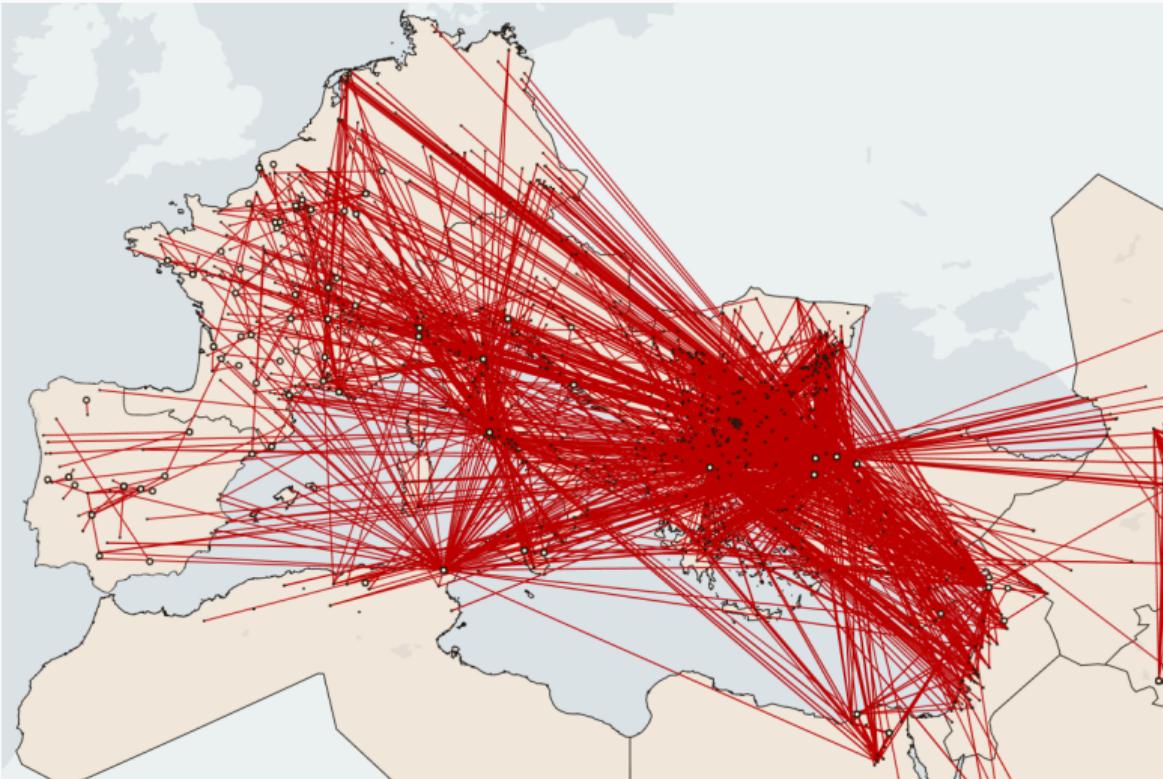


Figure 5: Before the Arab conquests: 450-630 AD

## Fact #3: Coin flows before/after the Arab conquests

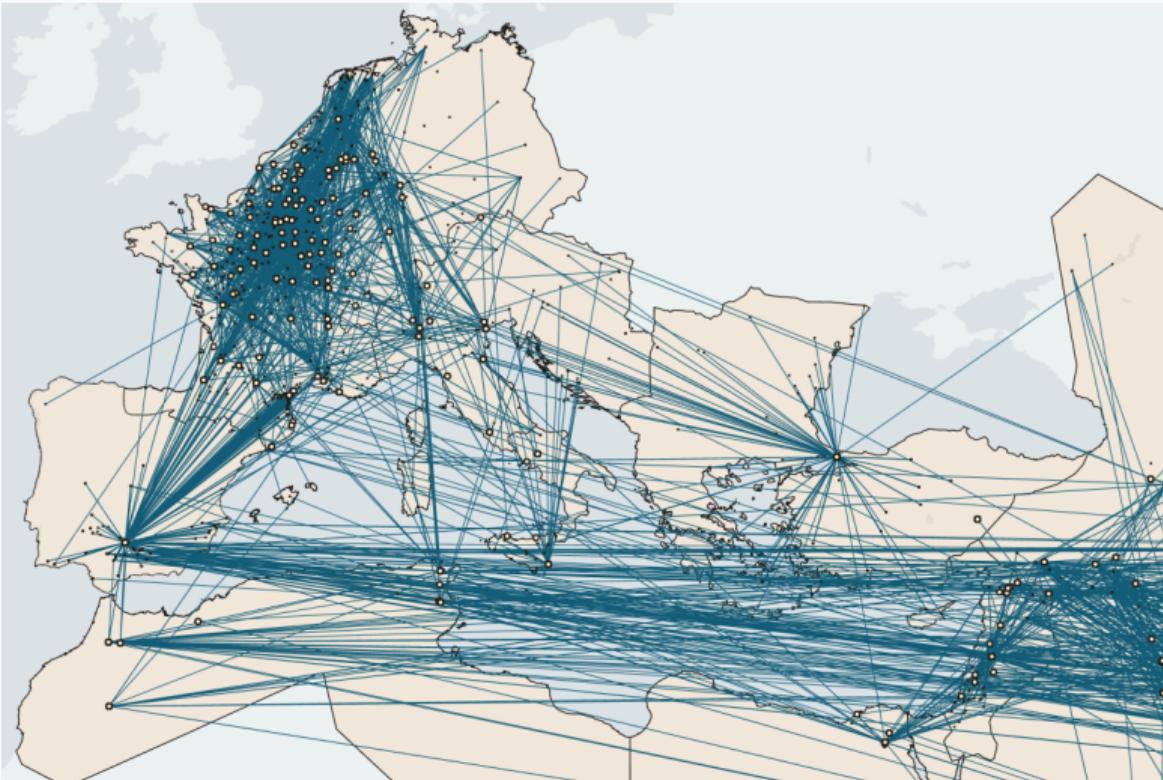


Figure 6: After the Arab conquests: 713-900 AD

► Cross-med: reg

► Cross-med: plot

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# Model

## Objective:

Quantify impact of trade barriers (and other changes) on market access / trade / welfare

## Approach:

Dynamic model of trade flows (gravity), where coins diffuse alongside trade and are thus informative about trade flows.

## Key Assumption:

Traders are blind to coin types (mint location and date).

- ⇒ Coins diffuse in proportion to trade flows
- ⇒ Recover trade flows from stocks of coin types in hords in different locations/time periods.

**Not** used/needed for identification: total *quantities* of coins found

## Setup

Location  $n$ , period  $t$ : homog. mass  $L_n(t)$  of workers. Four sub-periods  $t_{sub1}, t_{sub2}, t_{sub3}, t_{sub4}$

$t_{sub1}$  Start with  $S_n(t)$  coins saved from period  $t - 1$

$t_{sub2}$  A fraction  $\lambda_n(t)$  of those saved coins is lost

$M_n(t) \geq 0$  fresh new coins are minted

$t_{sub3}$   $X_n(t)$ , expenditure on consumption

Budget constraint:

$$X_n(t) \leq (1 - \lambda_n(t)) S_n(t) + M_n(t)$$

$t_{sub4}$   $L_n(t)$  workers produce and sell goods in exchange for coins

$w_n(t)$ , competitive wage,  $w_n(t)L_n(t)$ , aggregate labor income

$S_n(t+1)$  coins saved for  $t + 1$

$$\underbrace{(1 - \lambda_n(t)) \overbrace{S_n(t)}^{t_{sub1}} + M_n(t)}_{t_{sub2}} - \underbrace{X_n(t)}_{t_{sub3}} + \underbrace{w_n(t) L_n(t)}_{t_{sub4}} = \underbrace{S_n(t+1)}_{(t+1)_{sub1}}$$

## Intra-temporal allocations

- Fraction  $\pi_{ni}$  of expenditure  $X_n$  allocated to goods from  $i$ :

$$\pi_{ni}(t) = \frac{T_i(t)(w_i(t)d_{ni}(t))^{-\theta}}{\sum_k T_k(t)(w_k(t)d_{nk}(t))^{-\theta}}, \quad (1)$$

as in Eaton and Kortum (2002).

## Intertemporal preferences

- Intertemporal utility  $U_n$ , within period welfare  $W_n$ ,

$$U_n(t) = \mathbb{E} \left[ \sum_{\tau \geq t} \beta^{\tau-t} \ln \left( \frac{x_n(\tau)}{p_n(\tau)} \right) \right],$$

$$\text{with } p_n(t) = \gamma \left( \sum_k T_k(t) (w_k(t) d_{nk}(t))^{-\theta} \right)^{1/\theta}$$

## Dynamic optimization

- Optimal coin savings dynamics,

$$\max_{\{S_n(\tau)\}_{\tau \geq t}} \left[ \sum_{\tau \geq t} \beta^{\tau-t} \ln \left( \frac{X_n(\tau)}{p_n(\tau)} \right) \right]$$

$$X_n(\tau) = w_n(\tau)L_n(\tau) + M_n(\tau) + (1 - \lambda_n(\tau))S_n(\tau) - S_n(\tau+1),$$

$$S_n(\tau+1) \geq w_n(\tau)L_n(\tau), \forall \tau \geq t,$$

$$\lim_{\tau \rightarrow \infty} \beta^\tau S_n(\tau+1)/X_n(\tau) = 0$$

- Dynamic equilibrium wages clear markets,

$$w'_i L'_i = \sum_n \pi_{ni}(T, d; w) [w_n L_n + M_n + (1 - \lambda_n) S_n - S'_n]$$

Savings  $S_n(T, d, \delta, L, M; w)$  depend on parameters and wages, which depend on wages etc.

# Optimal consumption/saving

Under log utility:

- price level  $p_n(t)$  dynamics irrelevant (i.e. separates out)
- when unconstrained, consumption declines exponentially:

$$\frac{X_n(t+1)}{X_n(t)} = \beta(1 - \lambda_n(t)) < 1$$

- when constrained, consume as much as you can:

$$S'_n = w_n(t)L_n$$

Define *net saving*:

$$s_n(t) = \frac{(1 - \lambda_n(t))S_n(t) + M_n(t) - X_n(t)}{(1 - \lambda_n(t))S_n(t) + M_n(t)}$$

**Steady state: zero net savings,  $S_n(t+1) = S_n(t), \forall t$**

- No motive for extra savings,  $S_n = w_n L_n$ . Hence  $s_n(t) = 0$ .
- Wages and trade shares jointly determined,

$$w_i L_i = \sum_n \pi_{ni} ((1 - \lambda_n) w_n L_n + M_n)$$
$$\pi_{ni} = \frac{T_i (w_i d_{ni})^{-\theta}}{\sum_k T_k (w_k d_{nk})^{-\theta}}$$

- Constant aggregate stock of coins in circulation,

$$\sum_n M_n = \lambda_n \sum_n w_n L_n$$

- Note: trade deficits as in Dekle, Eaton and Kortum (2007), but endogenous:

$$D_n = X_n - Y_n = M_n - \lambda_n S_n$$

## Introducing and tracking coins of different vintages

Coin stocks  $S_n(\tau)$  consist of coins of different vintage:

$$S_n(\tau) = \sum_{m=1}^N \sum_{t < \tau} S_{mn}(t, \tau)$$

Coin stocks start their life when minted:  $S_{mm}(t, t) = M_m(t)$ .

Traders are ‘blind’ to coin types, draw coins with equal probability:

$$S_{mi}(t, \tau + 1) = \sum_{n=1}^N (1 - \lambda_n(\tau)) (1 - s_n(\tau)) S_{mn}(t, \tau) \pi_{ni}(\tau) + (1 - \lambda_i(\tau)) s_i(\tau) S_{mi}(t, \tau), \forall \tau \geq t$$

In compact matrix form:

$$\mathbf{S}(t, T) = \mathbf{M}(t) \left( \prod_{\tau=t}^{T-1} (\mathbf{I} - \boldsymbol{\lambda}(\tau)) \left( (\mathbf{I} - \mathbf{s}(\tau)) \boldsymbol{\Pi}(\tau) + \mathbf{s}(\tau) \right) \right)$$

## Pitfall #1: medium of exchange vs store of value

- Dynamics with ‘saving-augmented’ trade shares,

$$S(t, T) = M(t) \left( \prod_{\tau=t}^{T-1} (I - \lambda(\tau)) \tilde{\Pi}(\tau) \right)$$

- Separate origin, destination, and bilateral terms,

$$\tilde{\pi}_{ni}(\tau) = \alpha_n(\tau) \beta_i(\tau) \delta_{ni}(\tau)$$

$$\alpha_n = \frac{1}{\sum_k T_k (w_k d_{nk})^{-\theta}}, \quad \beta_i = T_i (w_i)^{-\theta}$$

$$\delta_{ni} = (d_{ni})^{-\theta}$$

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$$\delta_{ni} = (d_{ni})^{-\theta} \times \begin{cases} (1 - s_n) & \text{if } n \neq i \\ (1 - s_n) + \frac{s_n \sum_k T_k (w_k d_{nk})^{-\theta}}{T_n (w_n d_{nn})^{-\theta}} & \text{if } n = i. \end{cases}$$

- $\frac{\delta_{nj}}{\delta_{ni}} = \frac{(d_{nj})^{-\theta}}{(d_{ni})^{-\theta}}, \forall n \neq i, j, \forall s_n \geq 0$ : no impact on external trade

- $\frac{\delta_{nn}}{\delta_{ni}} > \frac{(d_{nn})^{-\theta}}{(d_{ni})^{-\theta}}, \forall s_n > 0$ : net saving mimics home bias in trade!

## Pitfall #2: stocks vs flows (steady state math)

- SS: no net saving ( $s = 0$ ), only age ( $a$ ) matters, not time ( $t$ ),

$$S(t, t+a) = S(a) = M \left( (I - \lambda) \Pi \right)^a, \forall t$$

- Sum of different vintages (stocks by origin-destination),

$$\sum_{a=0}^A S(a) = M \left( \sum_{a=0}^A \left( (I - \lambda) \Pi \right)^a \right) \underset{A \rightarrow +\infty}{=} M (I - (I - \lambda) \Pi)^{-1}$$

- Naive gravity on stocks gives Leontief inverse of trade shares!  
⇒ inconsistent estimates of trade elasticities/border effects due to model misspecification

▶ Illustration

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## Data generating process

- In  $n$  at  $t$ , a fraction  $\eta_n(t)$  of the coins in circulation  $S_n(t)$  is lost and subsequently found by archaeologists

**Assumption:**  $\eta$  small enough, does not affect model choices.

⇒ For coin shares within a hoard, the  $\eta$ 's cancel out.  $\eta_n(t)$  not used in our identification!

## Taking the model to the data

- 13 regions around the Mediterranean ▶ details
- 20-year time intervals
- Assume constant  $\lambda$  and estimate as exponential decay parameter in within-hoard age distribution:

$$\hat{\lambda}_{20y} = 0.301$$

(or 1.7% per year)

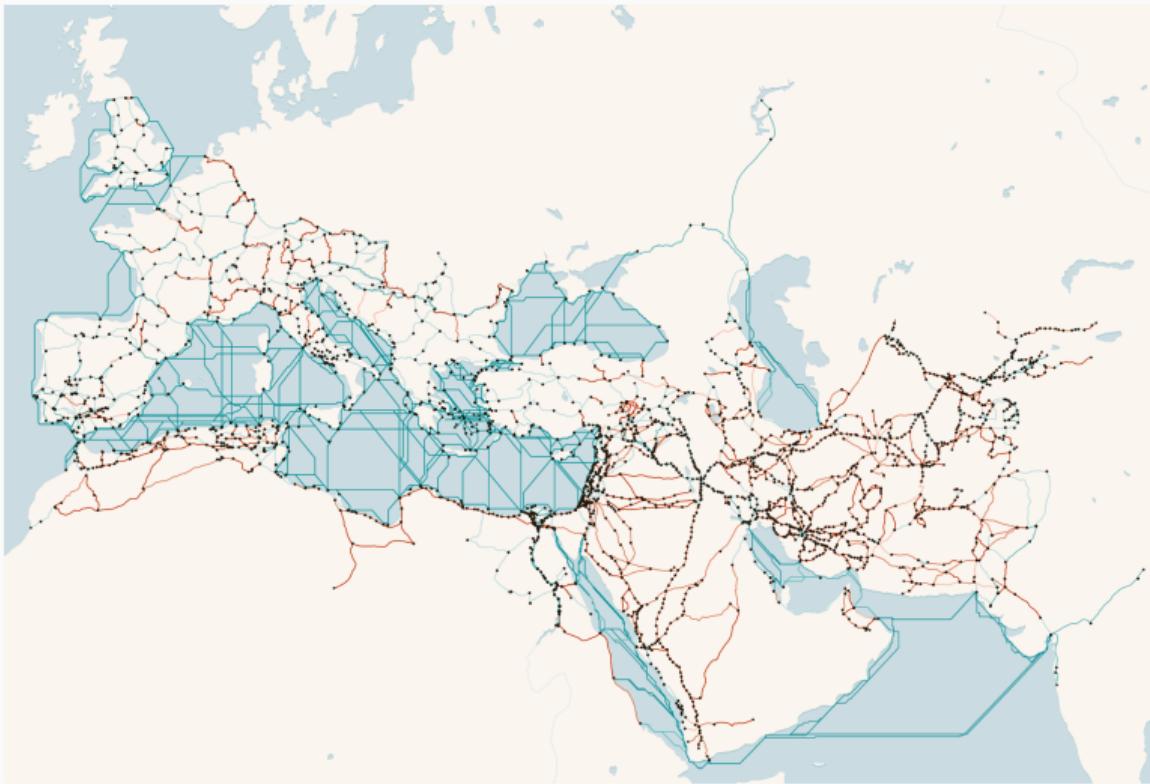
- Parameterize trade frictions,

$$d_{ni}(t)^\theta = \exp(\gamma_0 + \zeta \ln(\text{TravelTime}_{ni}) + \kappa_1 \text{PoliticalBorder}_{ni}(t) + \kappa_2 \text{ReligiousBorder}_{ni}(t))$$

if  $n \neq i$  and  $d_{nn}(t) = 1$ .

- How to split domestic trade vs saving? Calibrate  $\bar{s}_n(t) = 1.5\%$  (Scheidel, 2020).
- For counterfactuals, assume  $\theta = 4$  (Simonovska and Waugh, 2014).

Trade costs *only* depend on travel times (and politics/religion)



Note: Combined geospatial models from Orbis (Scheidel, 2015) and al-Turayyā (Romanov and Seydi, 2022).

al-Maqdisi

## Maximum likelihood estimation

Assume coins in our data are a random sample of coin types in each location  $\times$  time.

- Multinomial distribution of coin types,

$$P(\dots, X_i^{(m,\tau)}(T) = x_i^{(m,\tau)}, \dots) = \frac{N_i(T)!}{\prod_{(m,\tau)} x_i^{(m,\tau)}!} \prod_{(m,\tau)} [p_i^{(m,\tau)}(T)]^{x_i^{(m,\tau)}}$$

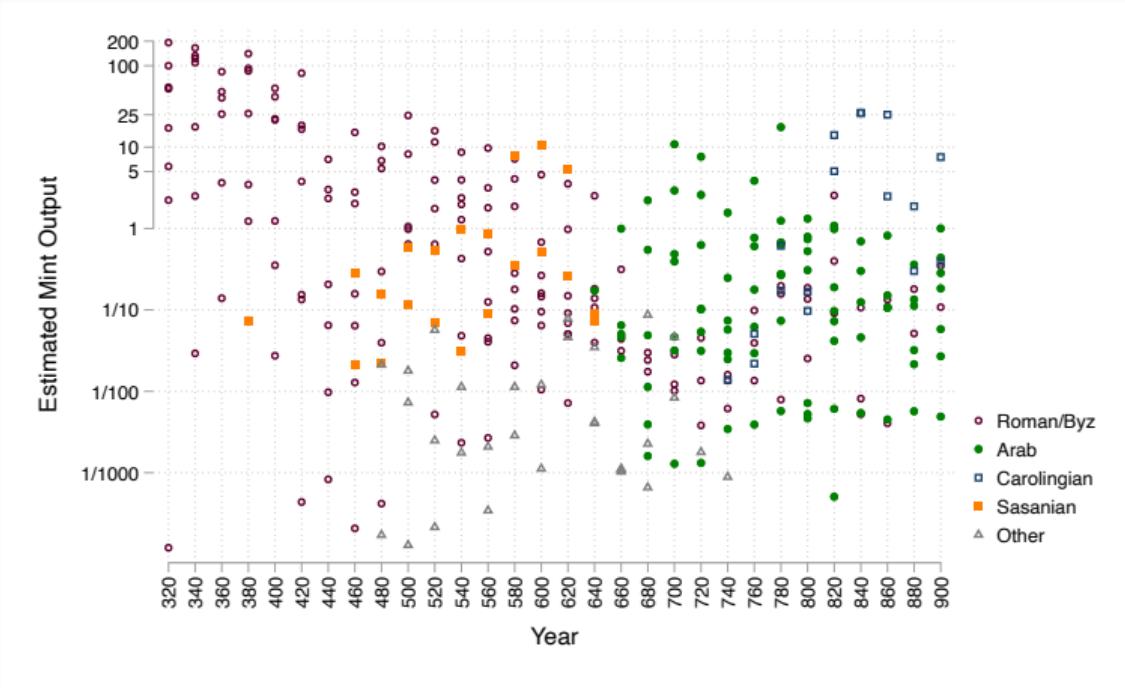
with the probability of drawing a coin of type  $(m, \tau)$ ,

$$p_i^{(m,\tau)}(T) = \frac{S_i^{(m,\tau)}(T)}{\sum_{(m',\tau')} S_i^{(m',\tau')}(T)} = \frac{S_i^{(m,\tau)}(T)}{S_i(T)}.$$

- Likelihood of observing a sample of coins given parameters  $\theta$ ,

$$\ell(X; \theta) = \sum_i \sum_T \sum_{(m,\tau)} x_i^{(m,\tau)} [\log S_i^{(m,\tau)}(T; \theta) - \log S_i(T; \theta)] + \text{constant}$$

## Estimation results: Mint output



Normalization:  $M_{n_0}[t_0] = 100$  (Northern Italy, AD 320-40).

Discussion on Byzantine monetary output: Kazhdan (1954), Pennas (1996)

## Estimation results: Determinants of trade costs

$$\ln((d_{ni}[t])^{-\theta}) = \text{constant}$$

$$- 2.98 \underset{(0.02)}{\ln(TravelTime_{ni})} - 0.3 \underset{(0.02)}{\ln(PoliticalBorder_{ni}[t])} - 4.05 \underset{(0.11)}{\ln(ReligiousBorder_{ni}[t])}$$

- Travel time elasticity similar to estimates on ancient trade.  
Roman trade: Flückiger et al. (2022); Bronze Age trade: Barjamovic et al. (2019).
- Political border tax: 8%  
(with  $\theta = 4$ ,  $d_{between}/d_{within} = e^{0.3/4} \approx 1.08$ )
- Religious border tax: 175%  
(with  $\theta = 4$ ,  $d_{between}/d_{within} = e^{4.05/4} \approx 2.75$ )
- Anderson and van Wincoop (2003) US-Canada border tax: 49%  
(with  $\theta = 4$ ,  $d_{between}/d_{within} = e^{1.59/4} \approx 1.49$ )

## Welfare and counterfactuals

Real consumption depends on a combination of  $L$  and  $T$  (that's not separately identified):

$$X_n/p_n = \gamma^{-1} (\pi_{nn})^{-1/\theta} (L_n T_n^{1/\theta}) \left(1 + \frac{M_n - \lambda w_n L_n}{w_n L_n}\right)$$

or equivalently in per capita terms

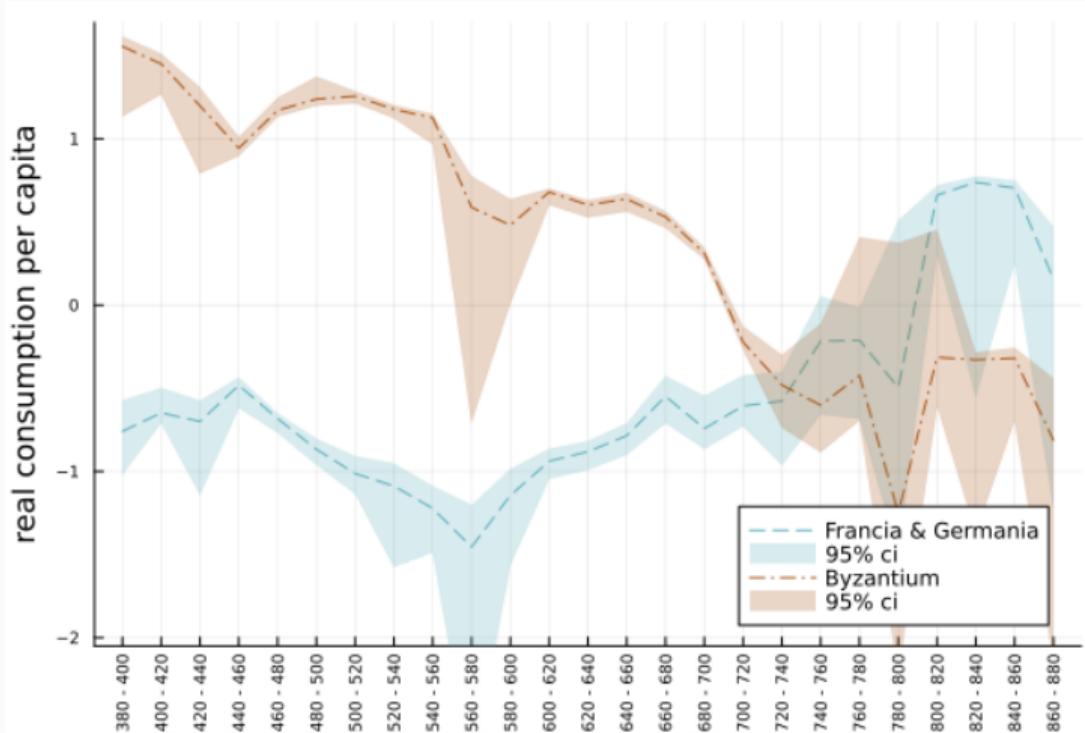
$$\underbrace{\frac{X_n/p_n}{L_n}}_{\text{Real Consumption}} = \underbrace{\gamma^{-1} (\pi_{nn})^{-1/\theta}}_{\text{Openness}} \underbrace{(T_n)^{1/\theta}}_{\text{Technology}} \underbrace{\left(1 + \frac{M_n - \lambda w_n L_n}{w_n L_n}\right)}_{\text{Trade Deficit}}$$

Note:  $T$  and  $L$  are not separately identified. We separate  $L$  and  $T$  through a Malthusian assumption

$$L_n = T_n \quad \forall n$$

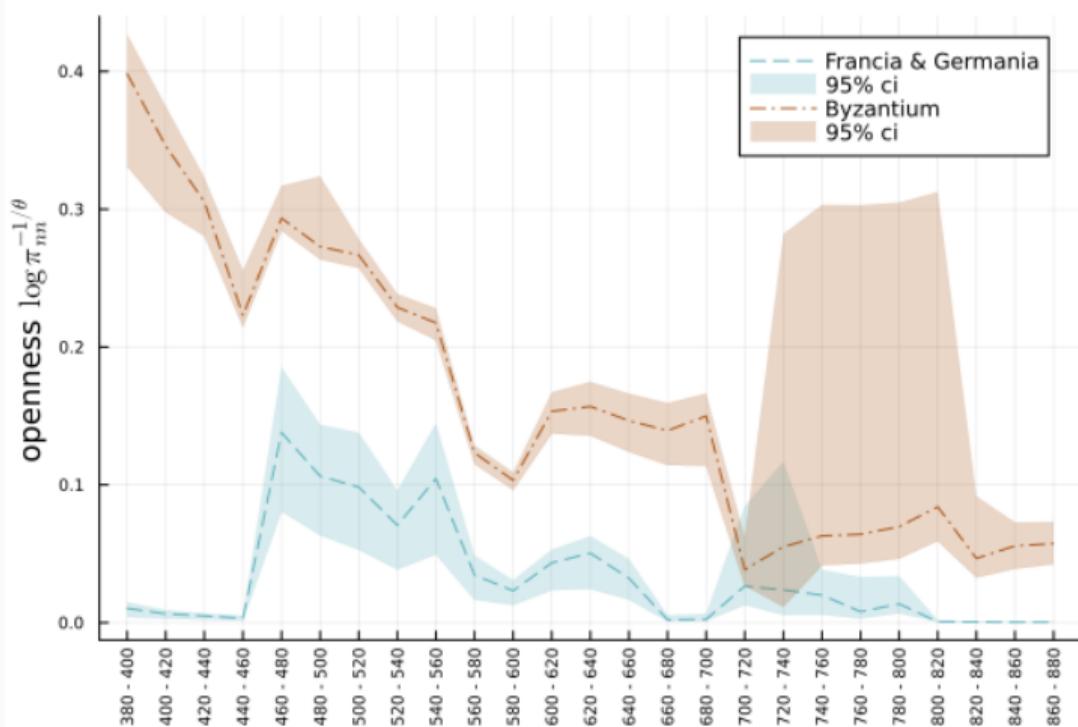
and decompose per-capita real consumption into the three components

# Byzantium vs northern Europe (380-880): *real consumption per capita*



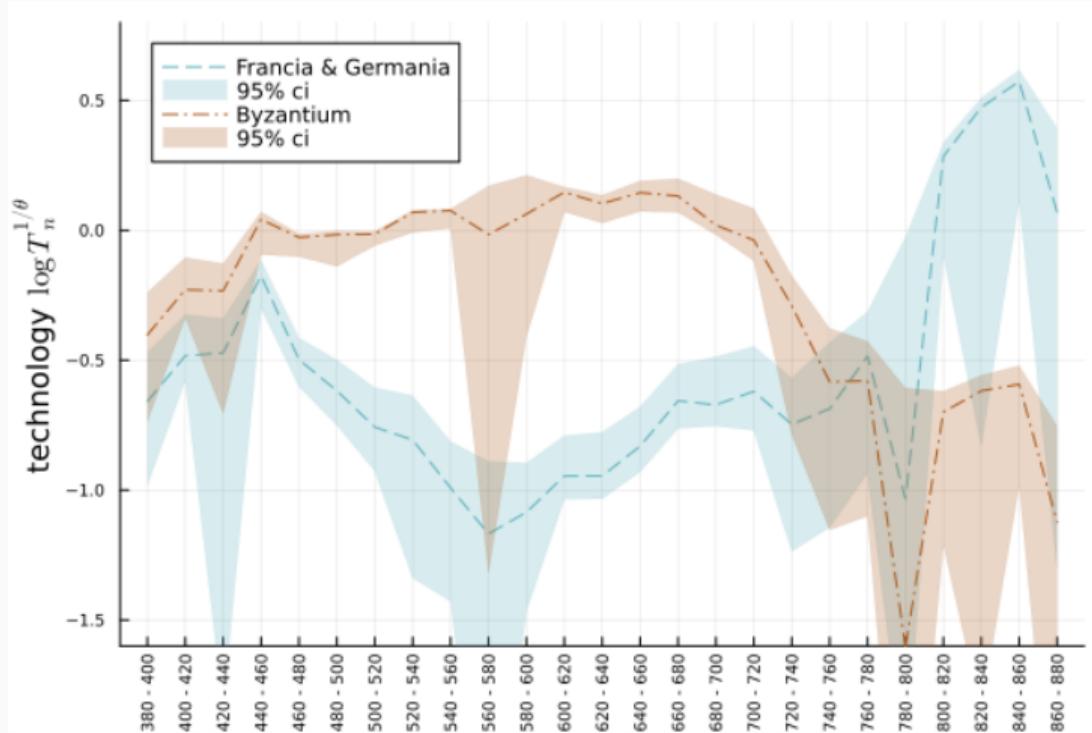
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Byzantium vs northern Europe (380-880): trade openness



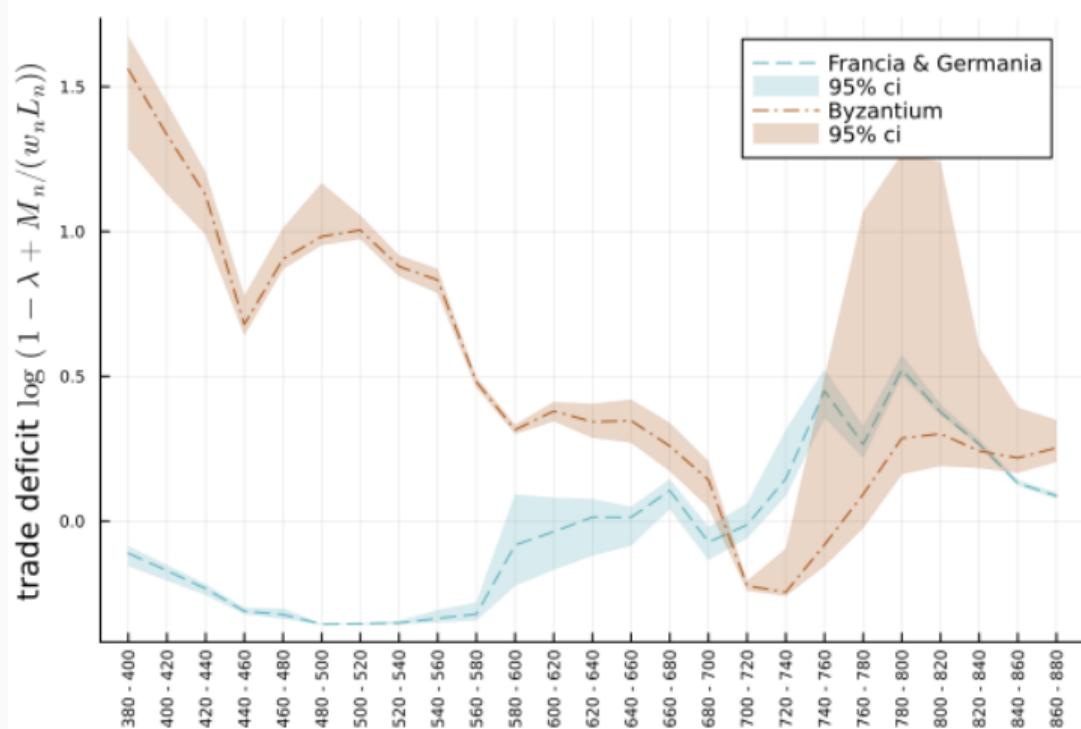
Bootstrapped 95% confidence intervals.

# Byzantium vs northern Europe (380-880): technology



Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Byzantium vs northern Europe (380-880): trade deficits



Bootstrapped 95% confidence intervals.

# Real consumption per capita: technology, geography, and trade (deficits)

Table 3: Real consumption in the ancient world from AD 460-620 to AD 700-900

|                      | Consumption<br>$\Delta \log \left( \frac{X_n / P_n}{L_n} \right)$<br>(1) | Openness<br>$\Delta \log \left( \pi_{nn}^{-1/\theta} \right)$<br>(2) | Technology<br>$\Delta \log \left( T_n^{1/\theta} \right)$<br>(5) | Trade Deficits<br>$\Delta \log \left( 1 + \frac{M_n - \lambda w_n L_n}{w_n L_n} \right)$<br>(7) |  |
|----------------------|--|--|--|---|--|
| al-Andalus           | 0.53<br>( 0.08 )   | -0.04<br>( 0.01 )  | 0.65<br>( 0.10 )   | -0.08<br>( 0.05 )   |  |
| Francia and Germania | 1.99<br>( 0.14 )   | -0.07<br>( 0.02 )  | 1.94<br>( 0.16 )   | 0.12<br>( 0.04 )  |  |
| Byzantine Heartlands | -1.56<br>( 0.22 )  | -0.16<br>( 0.06 )  | -0.74<br>( 0.13 )  | -0.66<br>( 0.25 )   |  |
| Arabian Peninsula    | 1.12<br>( 0.28 )   | -0.02<br>( 0.04 )  | 0.98<br>( 0.37 )   | 0.15<br>( 0.23 )  |  |

## Compare to relative urbanization rates, 700–900 AD

Top: Change in total urban population (urban: > 1k inhabitants), data from Buringh (2021)



Bottom:  $\Delta W_n / L_n$



# Counterfactuals

Table 4: Counterfactual changes in real consumption per capita after AD 700

|                      | Log consumption |          | Counterfactual log consumption change if: |          |            |          |            |          |
|----------------------|-----------------|----------|---|----------|------------|----------|------------|----------|
|                      | All parameters  |          | Religious border                          |          | Technology |          | Minting    |          |
|                      | AD 460-620      |          | AD 700-900                                |          | AD 700-900 |          | AD 700-900 |          |
|                      | (1)             | (2)      | (3)                                       | (4)      | (5)        | (6)      | (7)        | (8)      |
| al-Andalus           | -0.66           | ( 0.03 ) | 0.07                                      | ( 0.01 ) | 0.53       | ( 0.05 ) | 1.15       | ( 0.18 ) |
| Francia and Germania | -1.53           | ( 0.08 ) | -0.09                                     | ( 0.02 ) | 1.78       | ( 0.11 ) | 6.70       | ( 0.54 ) |
| Byzantine Heartlands | 1.17            | ( 0.03 ) | -0.61                                     | ( 0.03 ) | -0.64      | ( 0.06 ) | -1.34      | ( 0.05 ) |
| Arabian Peninsula    | -1.50           | ( 0.22 ) | 0.13                                      | ( 0.04 ) | 1.05       | ( 0.37 ) | 2.03       | ( 0.50 ) |

## Taking stock

- Clear pattern of change in economic geography before vs after conquest
- Trade disruption can account for the relative decline in the eastern Mediterranean
- Change in trade cost *alone* not able to account for urbanization in Muslim Spain, or in Carolingian empire
- In conjunction with changes in technology  $T_i$  and mint output, can account for urbanization patterns.

Back to Pirenne:

- Yes, new political and religious borders change market access, quant'ly relevant
- But unlikely to account for entire shift towards north-east
- Seignorage and technical change seem to be more important drivers

## Conclusion

*“Simply looking at the Mediterranean cannot of course explain everything about a complicated past created by human agents, with varying doses of calculation, caprice and misadventure. But this is a sea that patiently recreates for us scenes from the past, breathing new life into them, locating them under a sky and in a landscape that we can see with our own eyes, a landscape and sky like those of long ago. A moment’s concentration or daydreaming, and that past comes back to life.”*

*Fernand Braudel, Les Mémoires de la Méditerranée*

THANK YOU!

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## BACKUP SLIDES

## References

- al 'Ush, Abu'l-Faraj. 1972. *The silver hoard of Damascus: Sasanian, Arab-Sasanian, Khuwarizmian, and Umayyad kept in the National Museum of Damascus.* Damascus:Direction General of Antiquities and Museums.
- Anderson, James E., and Eric van Wincoop. 2003. "Gravity with Gravitas: A Solution to the Border Puzzle." *American Economic Review*, 93(1): 170–192.
- Barjamovic, Gojko, Thomas Chaney, Kerem Coşar, and Ali Hortaçsu. 2019. "Trade, merchants, and the lost cities of the bronze age." *The Quarterly Journal of Economics*, 134(3): 1455–1503.
- Brandes, Wolfram. 1989. *Die Städte Kleinasiens im 7. und 8. Jahrhundert.* De Gruyter.
- Buringh, Eltjo. 2021. "The population of European cities from 700 to 2000: Social and economic history." *Research Data Journal for the Humanities and Social Sciences*, 6(1): 1–18.
- Dekle, Robert, Jonathan Eaton, and Samuel Kortum. 2007. "Unbalanced Trade." *American Economic Review, Papers and Proceedings*, 97(2): 351–355.
- Eaton, Jonathan, and Samuel Kortum. 2002. "Technology, Geography, and Trade." *Econometrica*, 70(5): 1741–1779.

# Regions



## Fact #3: Coin flows before/after the Arab conquests

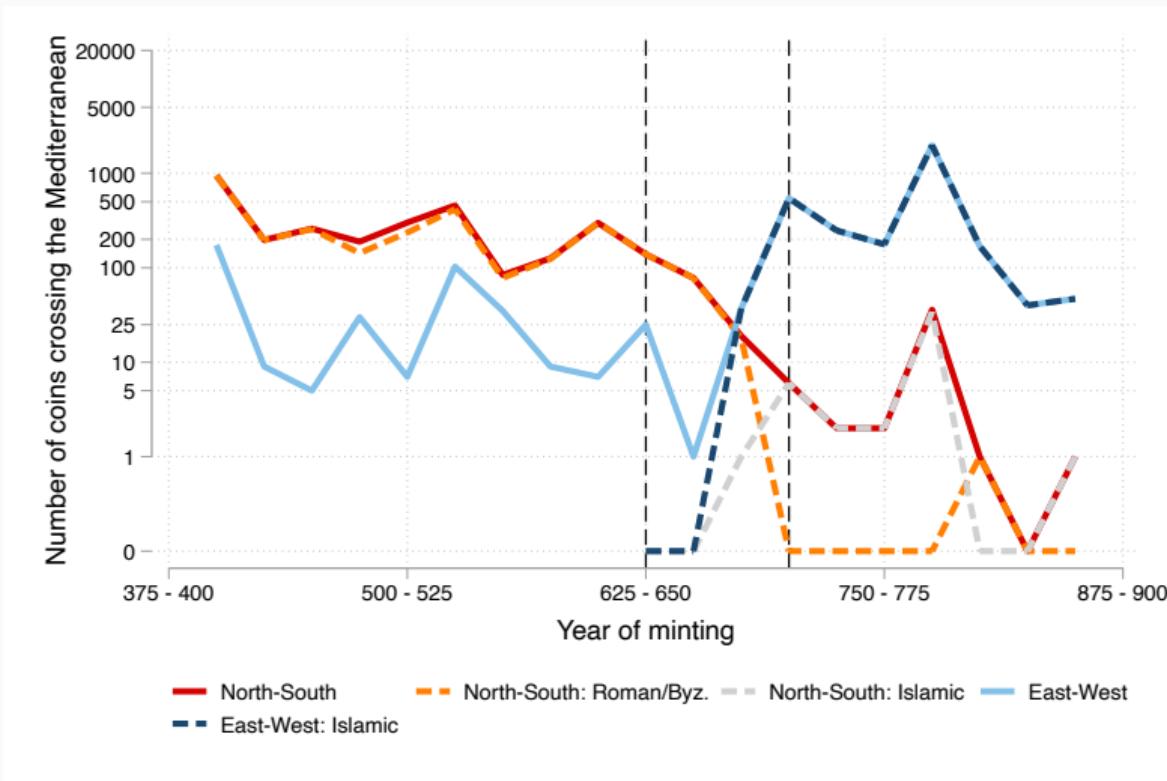


Figure 7: Number of coins flowing across the Mediterranean

## Fact #3: Coin flows before/after the Arab conquests

Table 5: The Mediterranean Before and After the Arab Conquest

|   | Dependent variable: Number of Coins |                     |                     |                     |
|---|-------------------------------------|---------------------|---------------------|---------------------|
|   | (1)                                 | (2)                 | (3)                 | (4)                 |
| Crossing Mediterranean × After Conquests                | -1.893***<br>(0.48)                 | -3.246***<br>(0.53) | -0.662<br>(0.63)    | -1.736<br>(1.27)    |
| Crossing Mediterranean × After Conquests × Islamic Coin |                                     | 7.267***<br>(0.90)  | 4.789***<br>(0.95)  | 7.545***<br>(0.89)  |
| Crossing Mediterranean × After Conquests × Roman Coin   |                                     |                     | -3.287***<br>(0.75) | -2.893***<br>(0.61) |
| Mint Cell × Empire FE                                   | Yes                                 | Yes                 | Yes                 | Yes                 |
| Mint Cell × Hoard Cell FE                               | Yes                                 | Yes                 | Yes                 | Yes                 |
| After Conquests FE                                      | Yes                                 | Yes                 | Yes                 |                     |
| Mint Cell × After Conquests FE                          |                                     |                     |                     | Yes                 |
| Hoard Cell × After Conquests FE                         |                                     |                     |                     | Yes                 |
| Estimator   | PPML                                | PPML                | PPML                | PPML                |
| Observations  | 10480                               | 10480               | 10480               | 6208                |

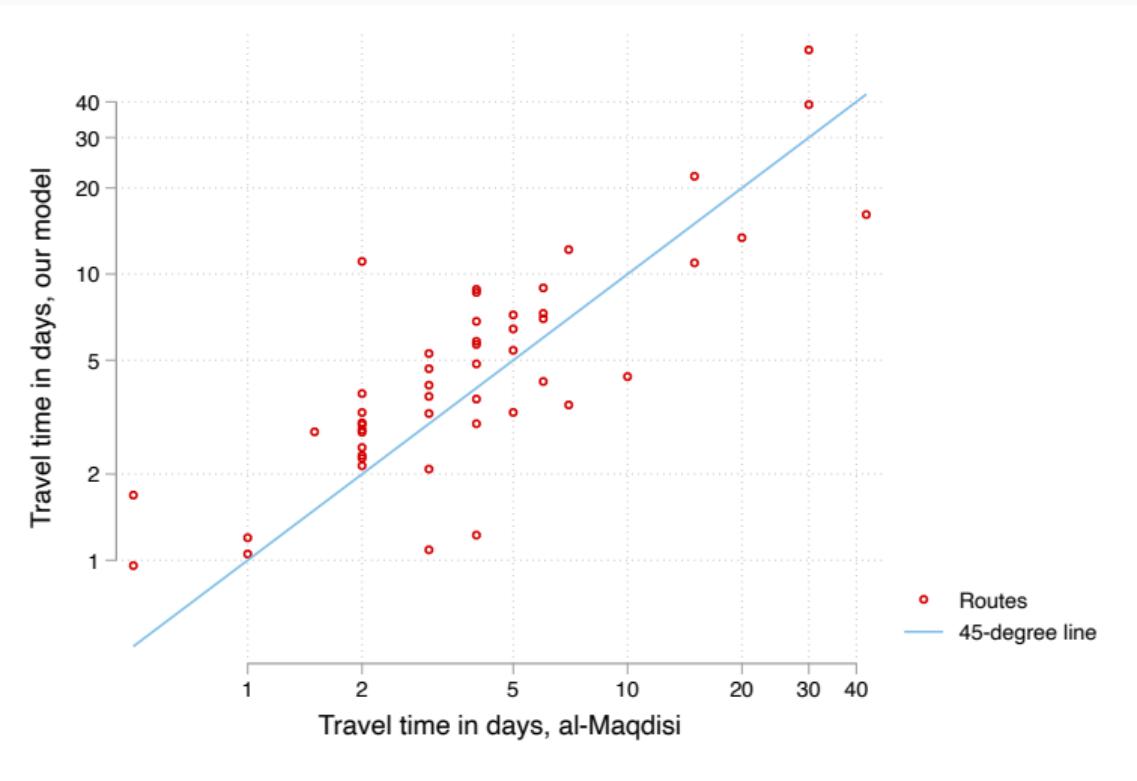
Standard errors in parentheses, clustered at the hoard × era and mint × era level.

+  $p < 0.10$ , \*  $p < 0.05$ , \*\*  $p < 0.01$

Estimating eqn:  $\text{count}_{mdht} = \exp(\gamma_1 \text{mediterranean}_{mh} \times \text{after}_t + \dots + \alpha_{md} + \alpha_{mh} + \varepsilon_{mhdt})$

# Validating Travel Times

Al-Maqdisi (c. 945–991): *The Best Divisions for Knowledge of the Regions*



## Unsolved problems (as of yet)

- *Lucas critique #1*: cost function does not minimize costs

$$\ln(\delta_{ni}(t)) = \min_{p \in paths(i \rightarrow n)} \left( \gamma_0 + \gamma_1 \ln(TravelTime_p(t)) + \sum_{pb: \text{ all political borders along } p} \gamma_2 PoliticalBorder_{pb}(t) + \sum_{rb: \text{ all religious borders along } p} \gamma_3 ReligiousBorder_{rb}(t) \right)$$

- *Lucas critique #2*: net saving (in  $\delta_{nn}$ ) depends on parameters.
- *Fix for #2*: location-specific intercepts ( $\gamma_{0,n}$ ) and  $\delta_{nn}$ 's.

For now: constant  $\gamma_0$ , and  $\delta_{nn} = 1$ ...

## Fact #3: Arab conquests disrupt Mediterranean trade: Gold only

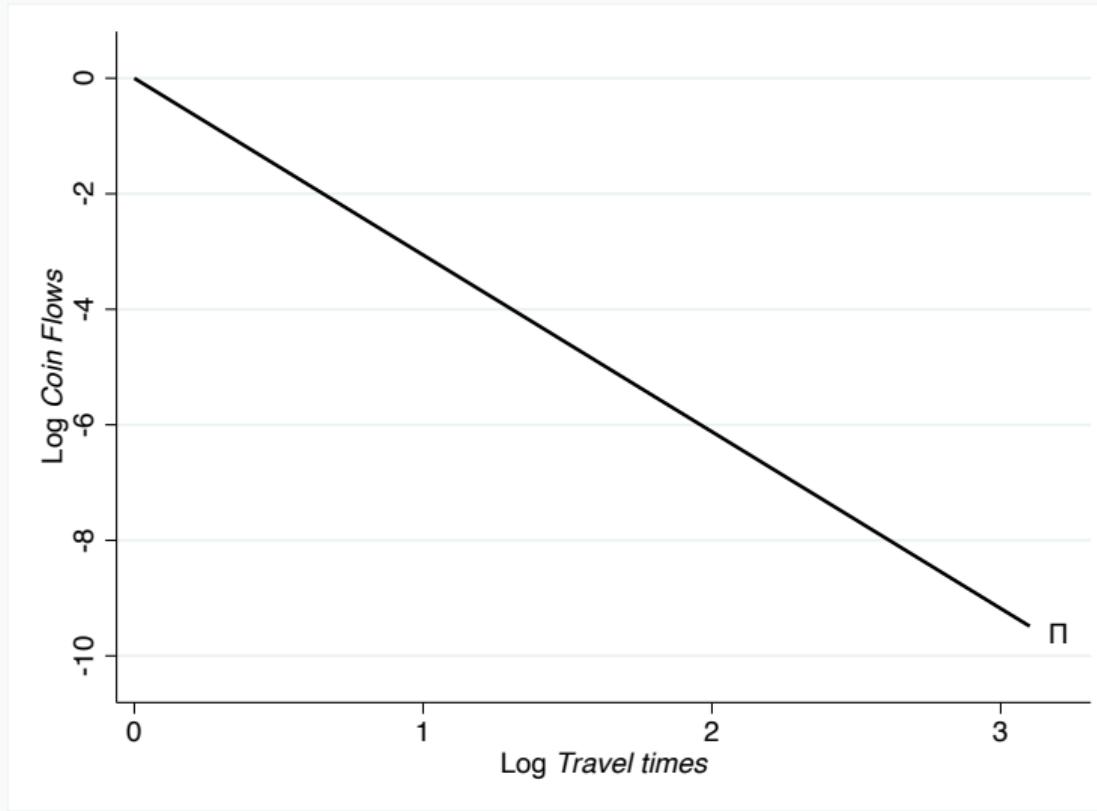
|   | Dependent variable: Number of Coins |                     |                     |                     |                     |
|---|-------------------------------------|---------------------|---------------------|---------------------|---------------------|
|   | (1)                                 | (2)                 | (3)                 | (4)                 | (5)                 |
| Log Distance  | -1.516***<br>(0.13)                 | -1.541***<br>(0.13) | -1.544***<br>(0.13) | -1.189***<br>(0.15) | -1.193***<br>(0.15) |
| Crossing Mediterranean                                  | 0.298<br>(0.40)                     | 0.307<br>(0.39)     | 0.320<br>(0.39)     | 0.0942<br>(0.31)    | 0.122<br>(0.31)     |
| Crossing Mediterranean × After Conquests                | -1.600**<br>(0.70)                  | -2.858***<br>(0.68) | -1.719**<br>(0.69)  | -2.576***<br>(0.98) | -3.379***<br>(1.13) |
| Crossing Mediterranean × After Conquests × Islamic Coin |                                     | 3.020***<br>(0.71)  | 1.864**<br>(0.76)   |                     | 2.985**<br>(1.20)   |
| Crossing Mediterranean × After Conquests × Roman Coin   |                                     |                     | -1.699<br>(1.04)    |                     |                     |
| Mint Cell × Empire FE                                   | Yes                                 | Yes                 | Yes                 | Yes                 | Yes                 |
| Hoard Cell × After Conquests FE                         | Yes                                 | Yes                 | Yes                 | Yes                 | Yes                 |
| Sample  |                                     |                     |                     | Gold only           | Gold only           |
| Observations  | 172442                              | 172442              | 172442              | 32024               | 32024               |

Standard errors in parentheses, clustered at the hoard × era and mint × era level.

+  $p < 0.10$ , \*  $p < 0.05$ , \*\*  $p < 0.01$

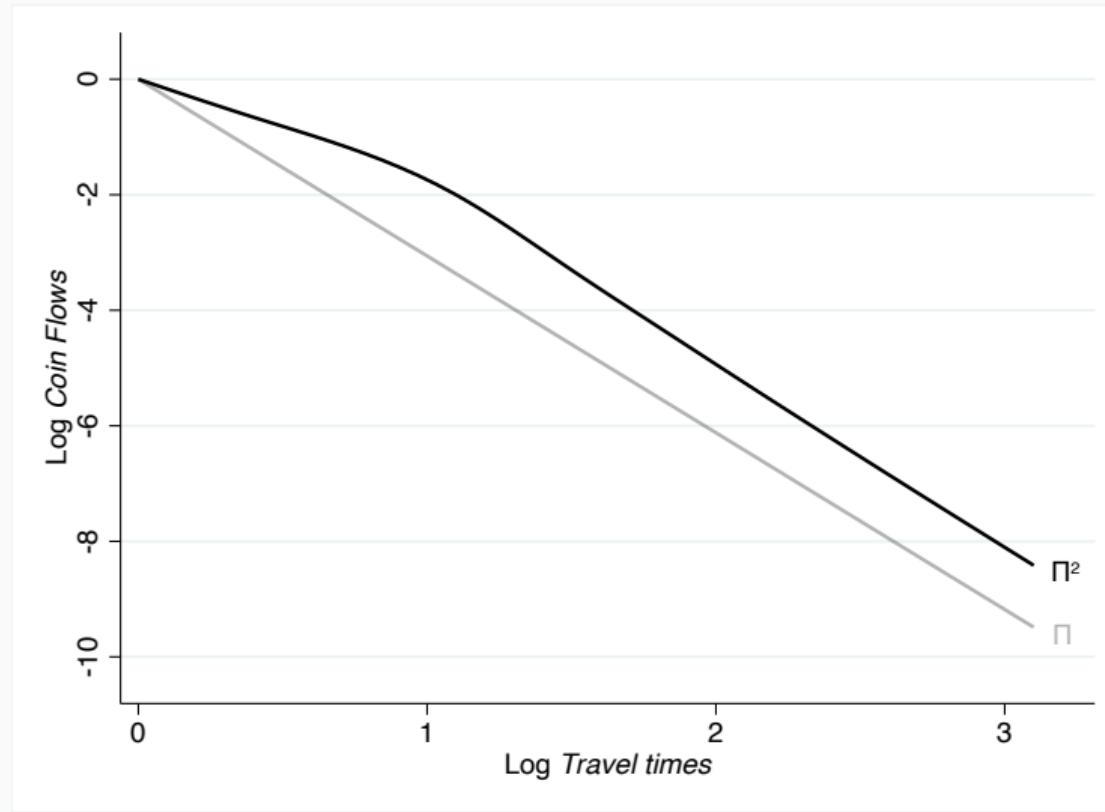
Before: 400–630; after: 713–950

## Pitfall #2: stocks vs flows (numerical example)



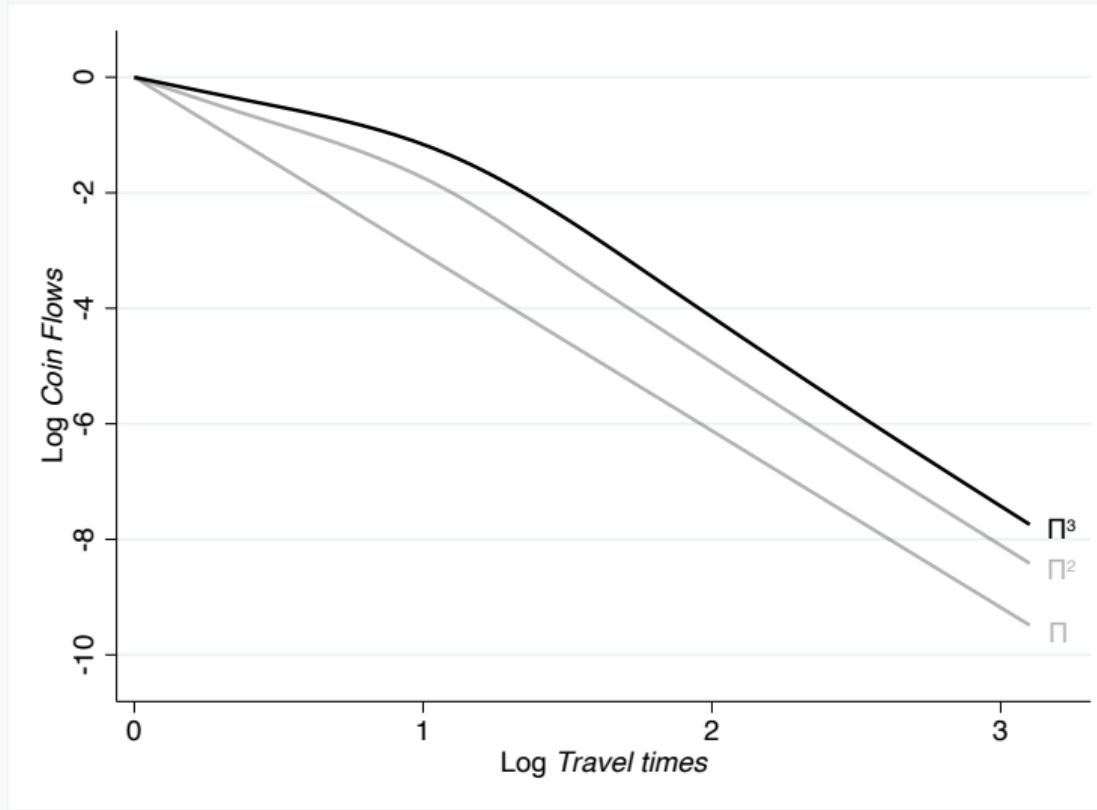
- Flow of coins: age 1 (same as trade flows  $\Pi$ )

## Pitfall #2: stocks vs flows (numerical example)



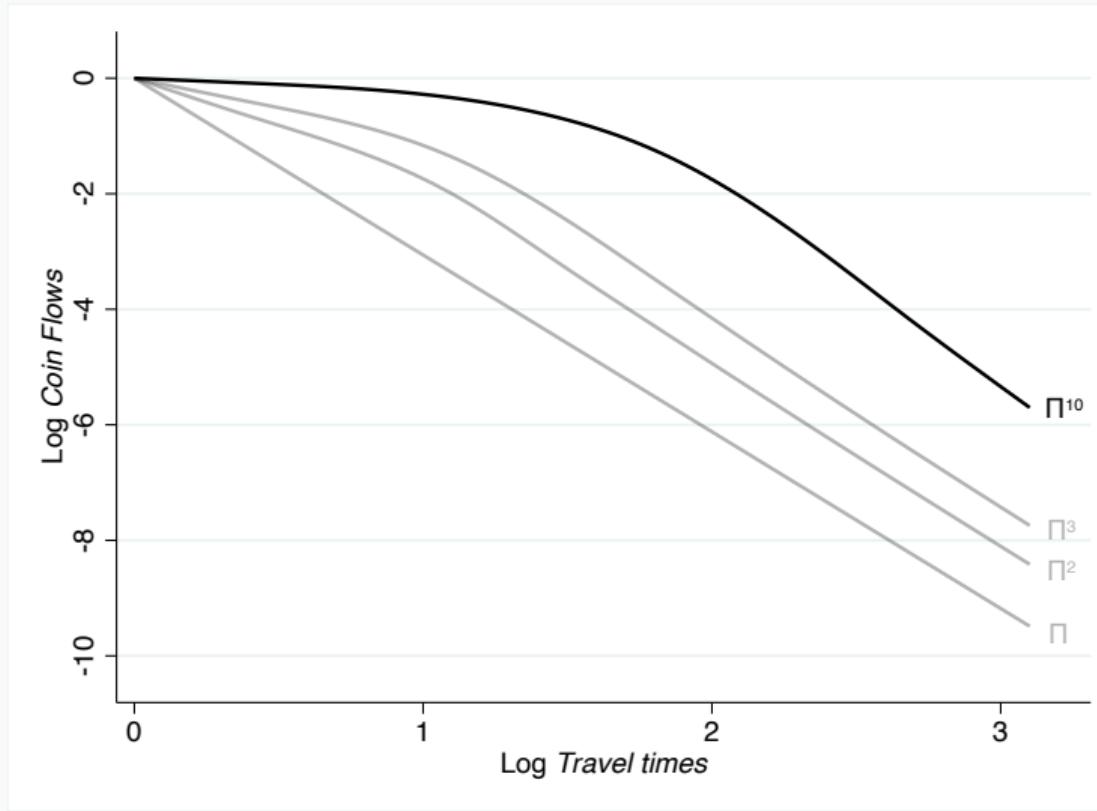
- Flow of coins: age 1, age 2

## Pitfall #2: stocks vs flows (numerical example)



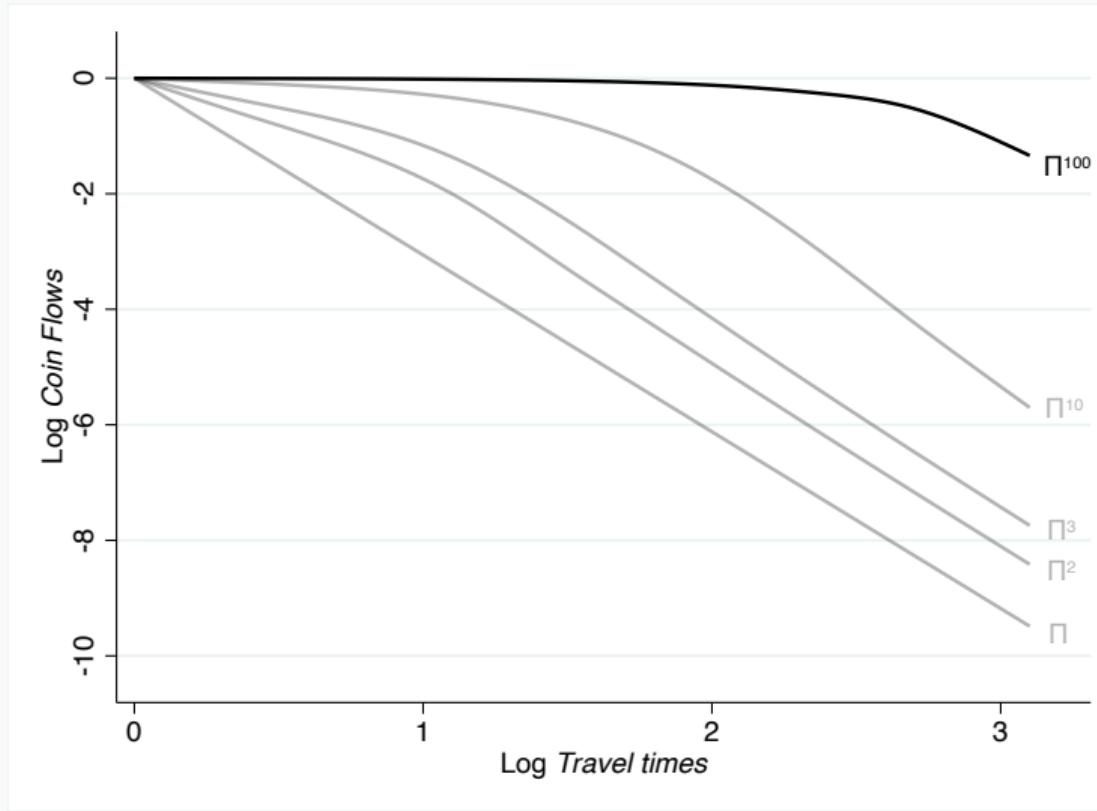
- Flow of coins: age 1, age 2, age 3

## Pitfall #2: stocks vs flows (numerical example)



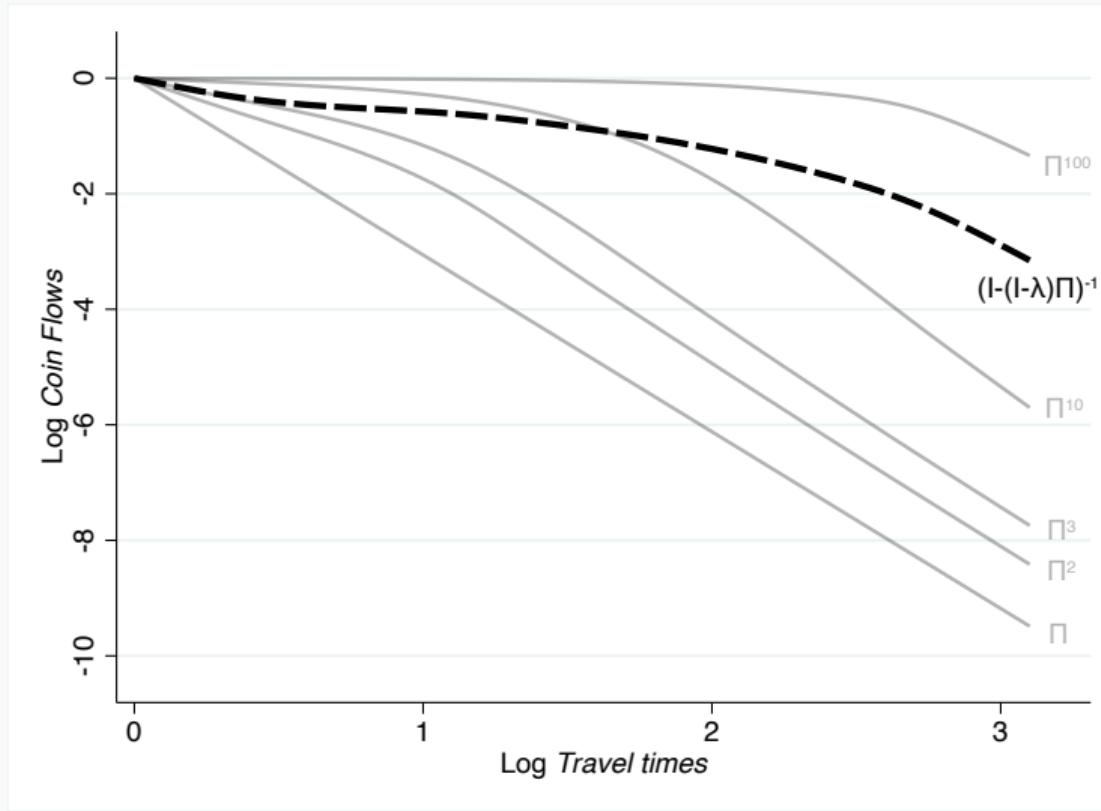
- Flow of coins: age 1, age 2, age 3, age 10

## Pitfall #2: stocks vs flows (numerical example)



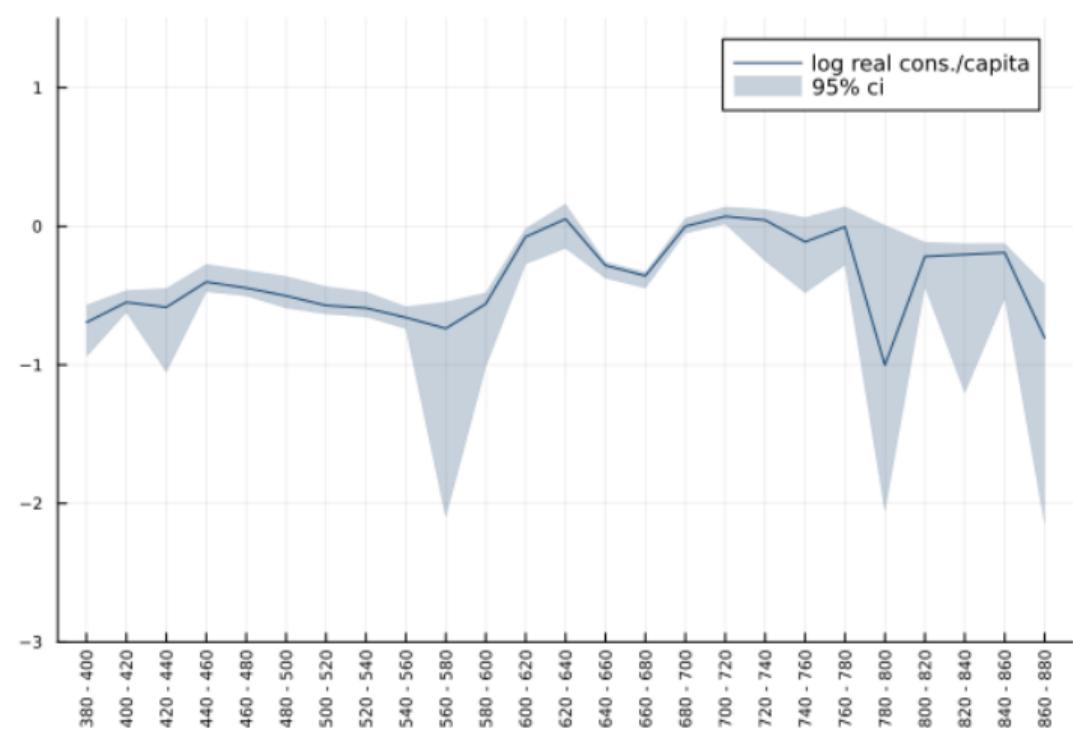
- Flow of coins: age 1, age 2, age 3, age 10, age 100

## Pitfall #2: stocks vs flows (numerical example)



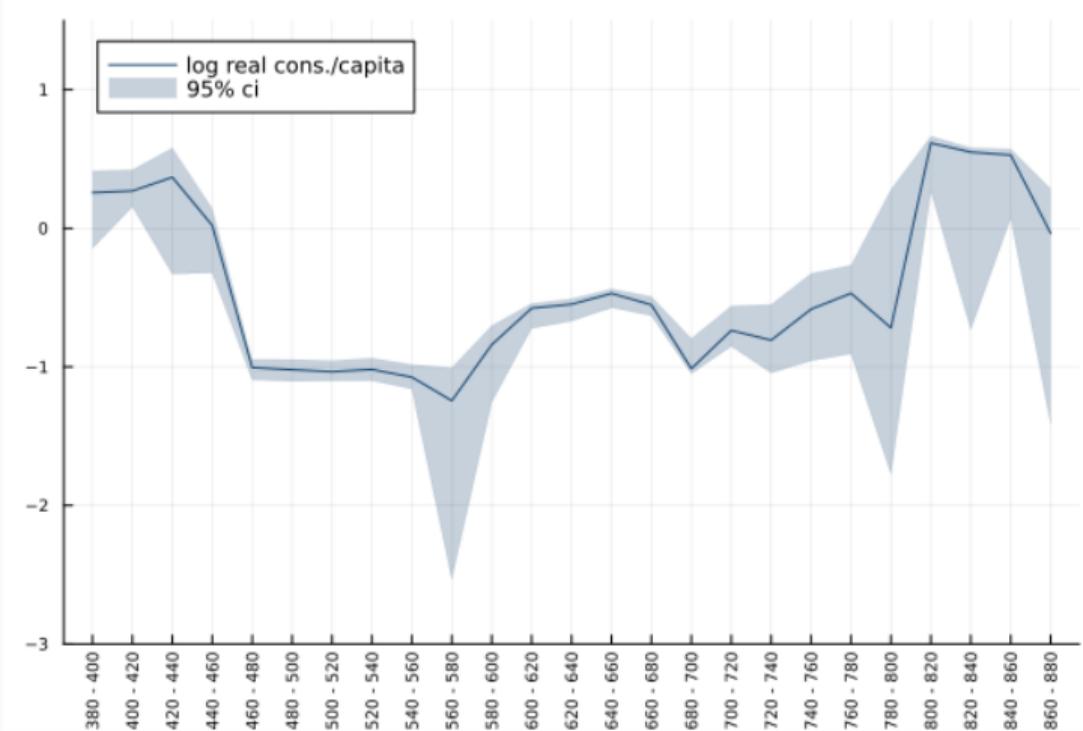
- Flow of coins: age 1, age 2, age 3, age 10, age 100, all ages

# Real consumption per capita (380-880): al-Andalus (Spain)



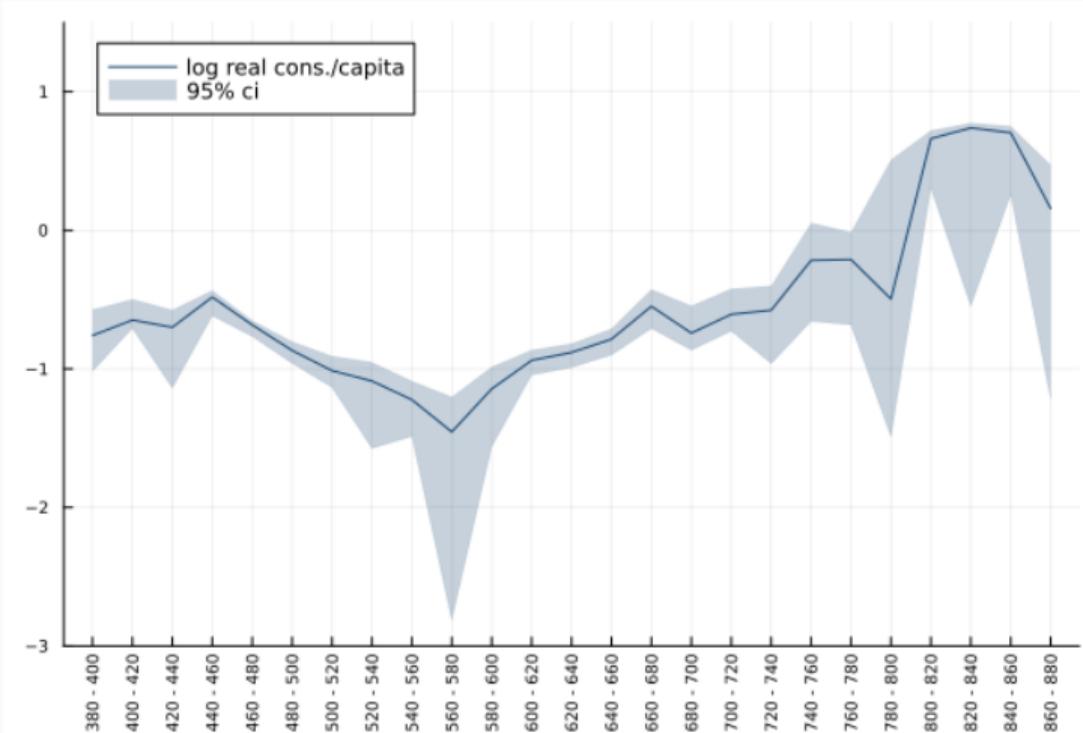
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Aquitaine (South France)



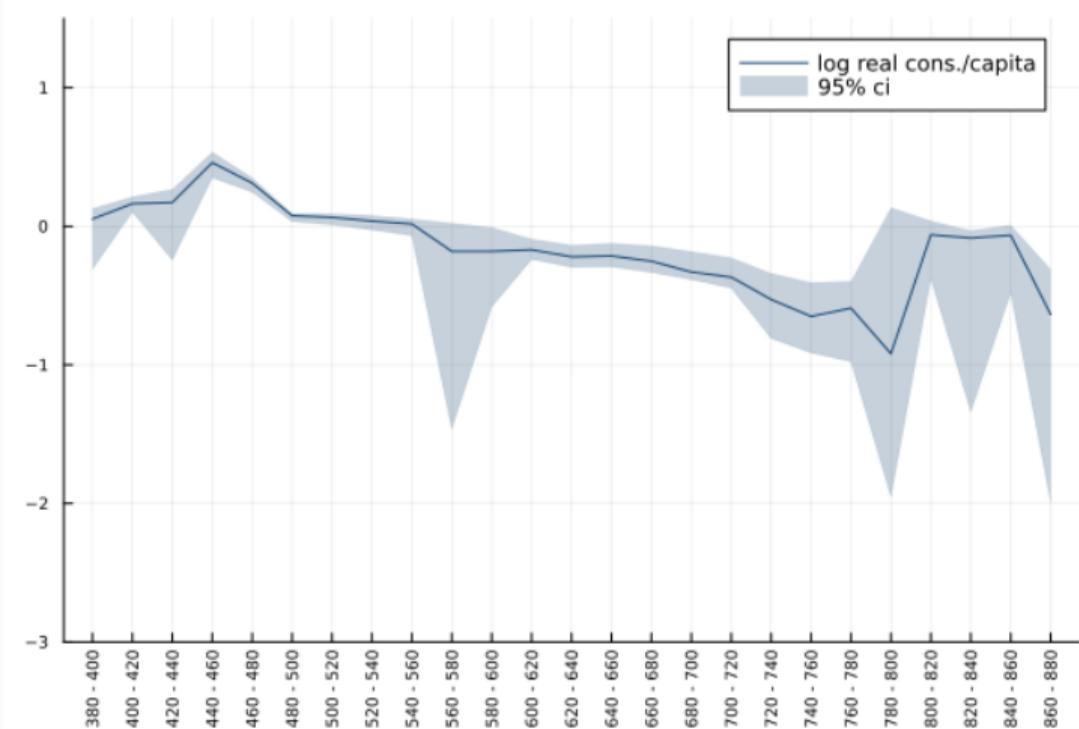
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Francia and Germania



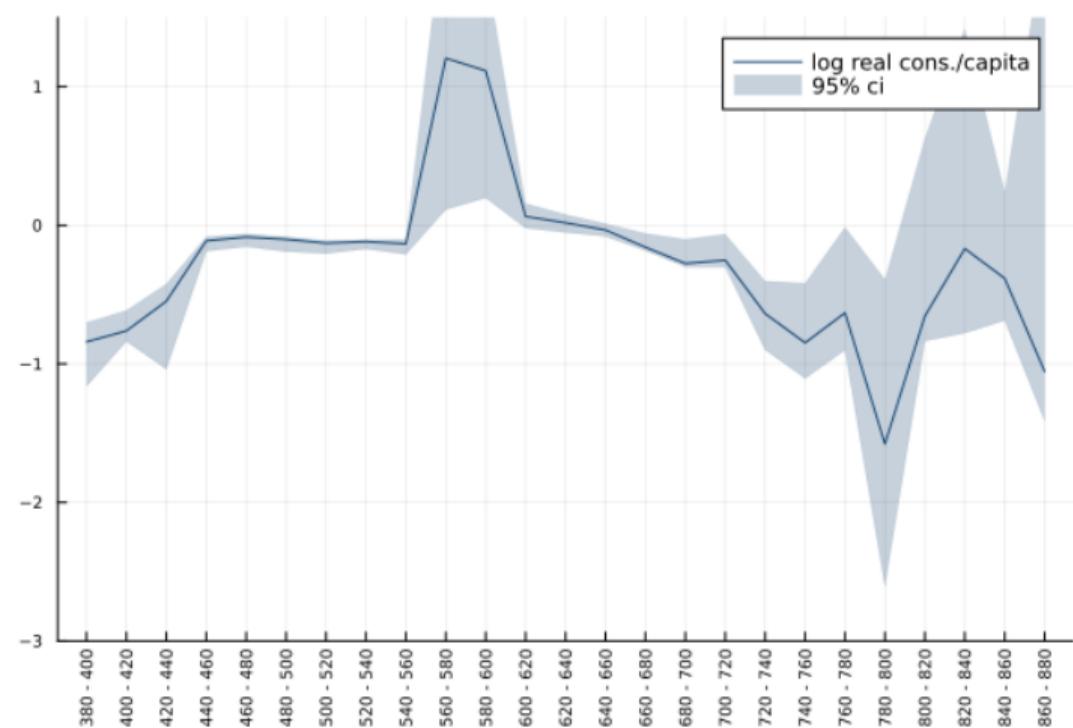
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Northern Italy



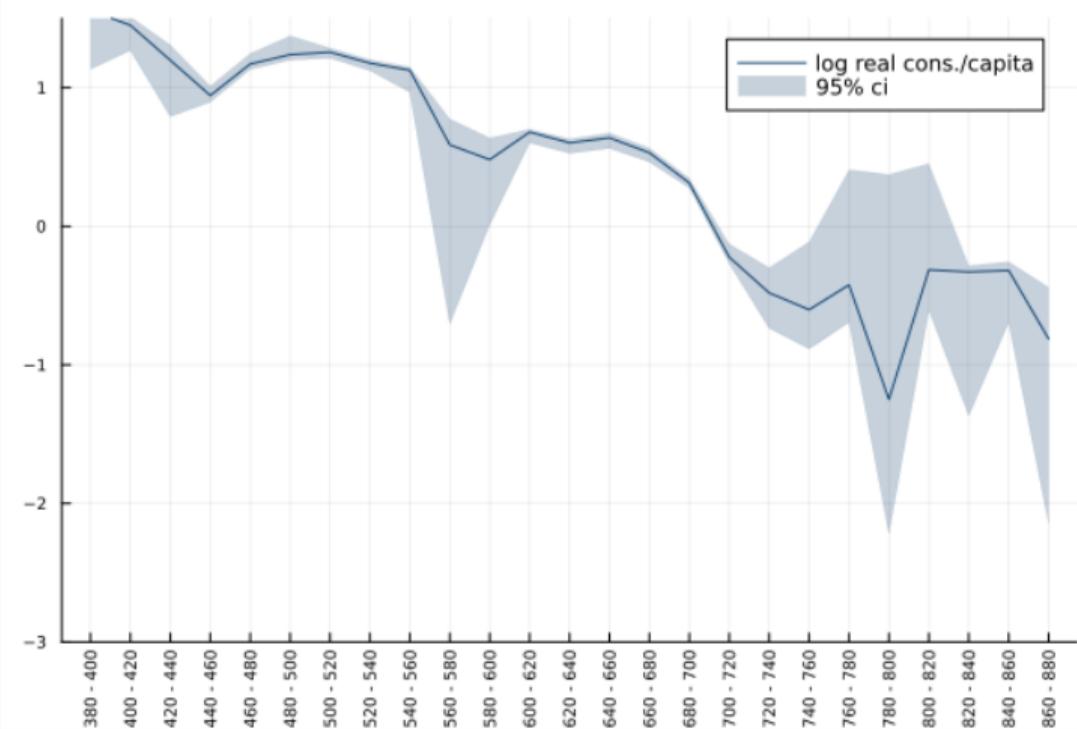
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Southern Italy



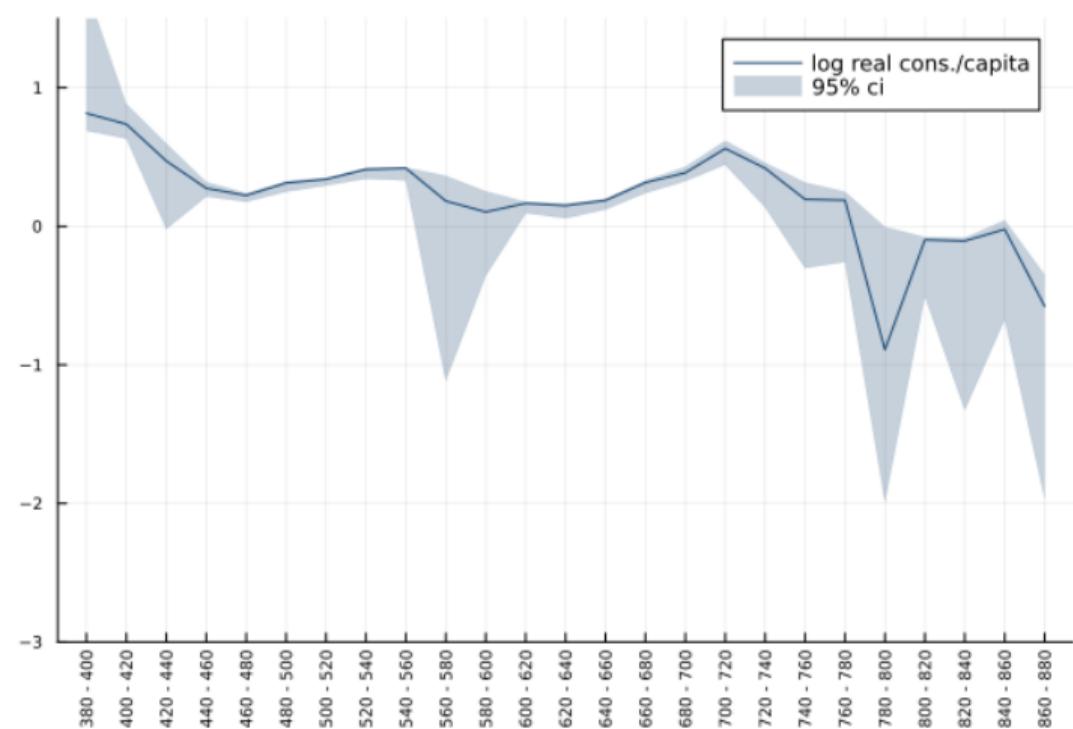
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Byzantine Heartlands



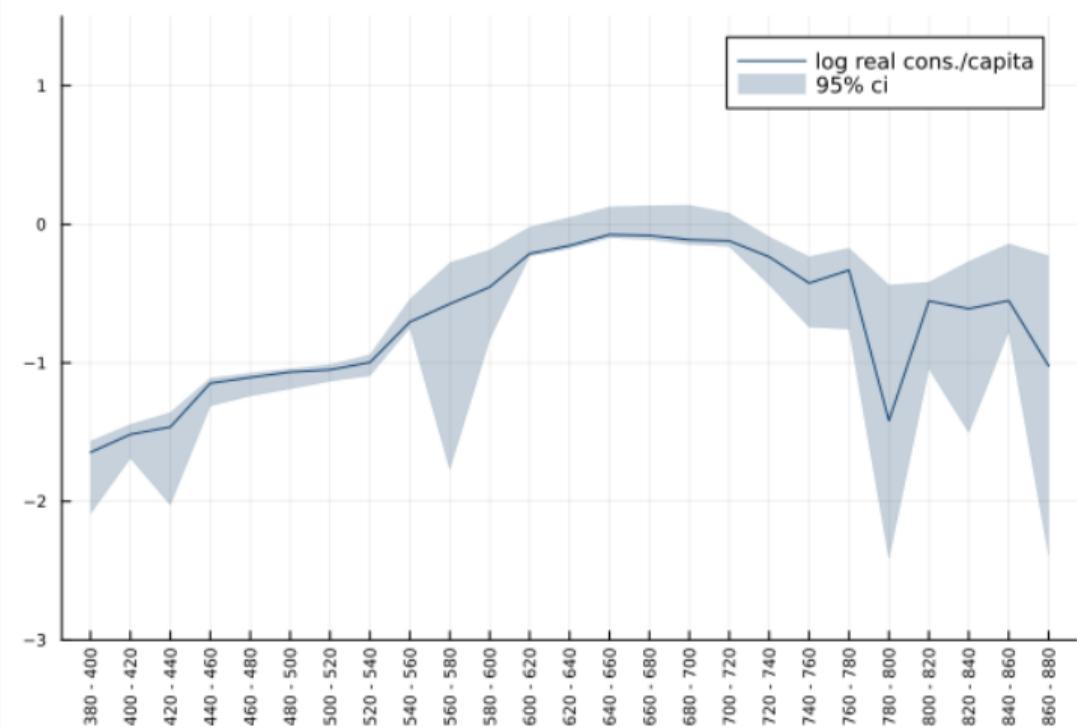
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/P_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): al-Sham (Greater Syria)



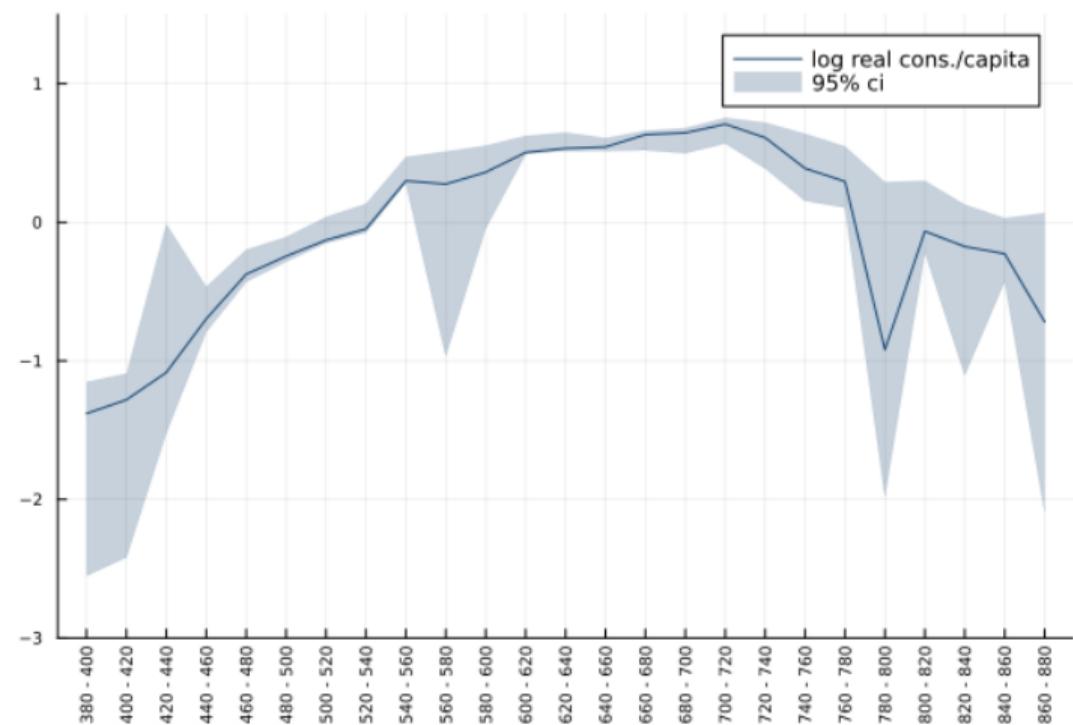
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Northern Syria, Caucasus



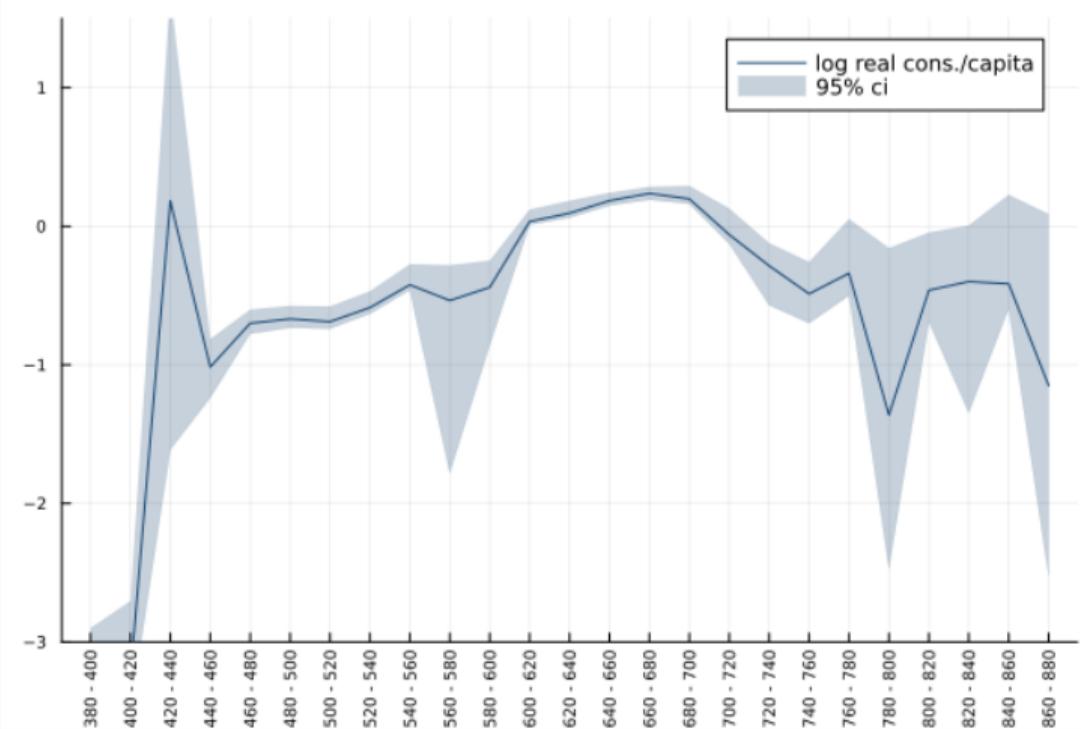
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Iraq, Iran



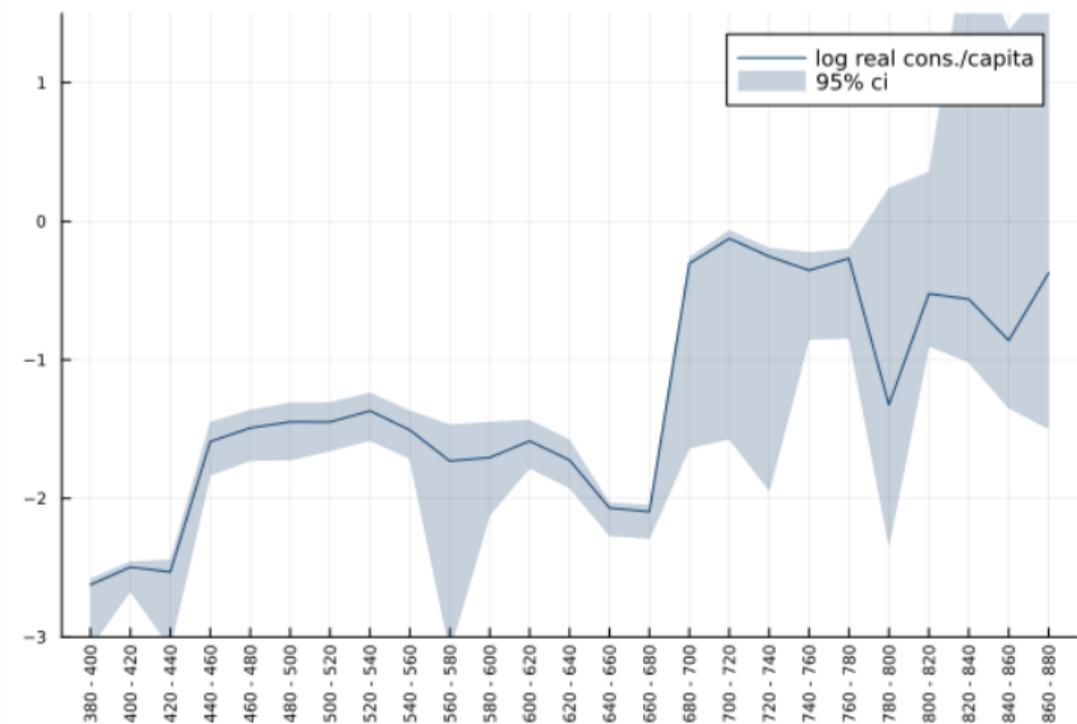
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Eastern Caliphate



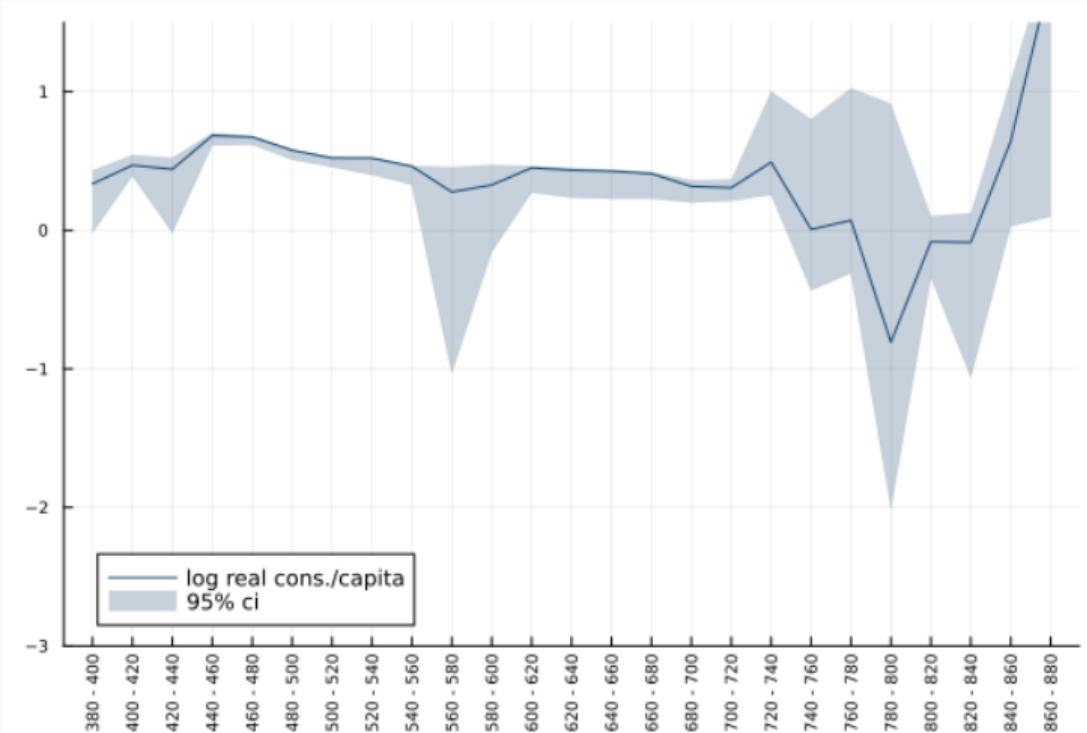
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Arabian Peninsula



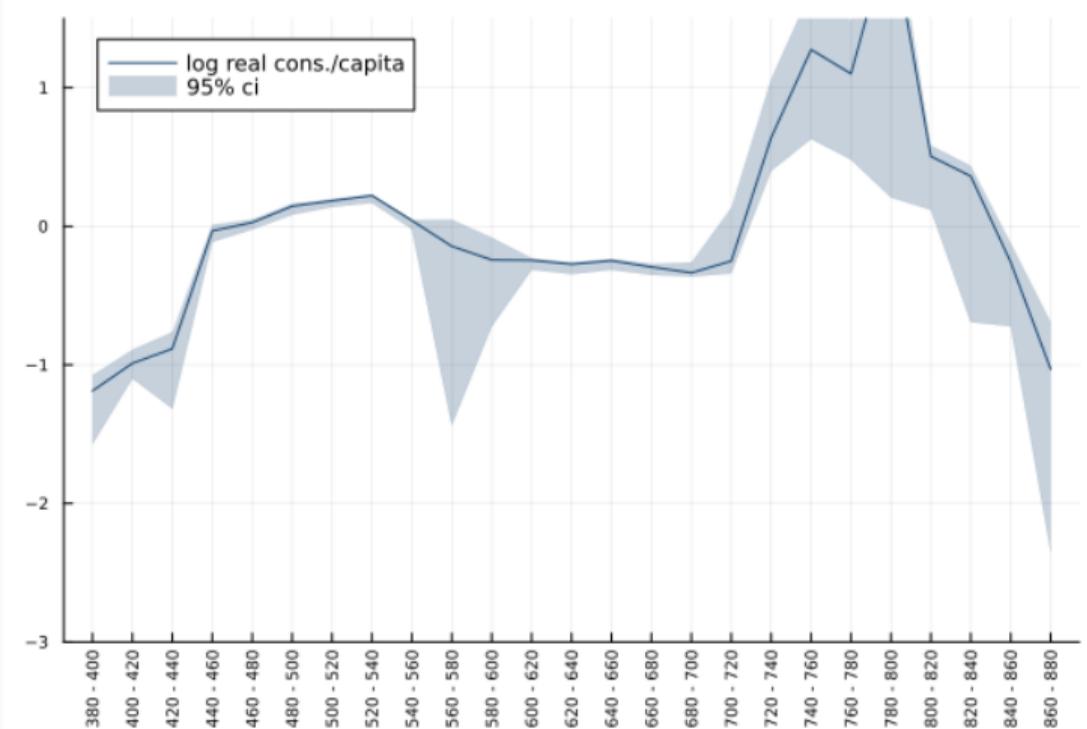
Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Real consumption per capita (380-880): Misr (Egypt)



Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

## Real consumption per capita (380-880): al-Maghrib



Bootstrapped 95% confidence intervals. Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t.$

# Realized vs counterfactual changes in real consumption per capita

Realized changes, from AD 460-620 to AD 700-900

|                             | Real consumption<br>$\Delta \log \left( \frac{X_n/p_n}{L_n} \right)$ | Openness<br>$\Delta \log \left( \pi_{nn}^{-1/\theta} \right)$ | Technology<br>$\Delta \log \left( T_n^{1/\theta} \right)$ | Trade Deficit<br>$\Delta \log \left( 1 + \frac{M_n - \lambda w_n L_n}{w_n L_n} \right)$ |
|-----------------------------|--|---|---|---|
| al-Andalus (Spain)          | 0.62<br>( 0.25 )   | -0.06<br>( 0.04 )   | 0.77<br>( 0.32 )  | -0.09<br>( 0.18 )   |
| Aquitaine (South France)    | 1.28<br>( 0.23 )   | -0.05<br>( 0.01 )   | 1.22<br>( 0.23 )  | 0.11<br>( 0.06 )  |
| <b>Francia and Germania</b> | <b>1.96</b><br><b>( 0.24 )</b>                                       | <b>-0.05</b><br><b>( 0.01 )</b>                               | <b>1.80</b><br><b>( 0.26 )</b>                            | <b>0.20</b><br><b>( 0.04 )</b>  |
| Northern Italy              | -0.31<br>( 0.24 )  | -0.08<br>( 0.03 )   | -0.10<br>( 0.26 )   | -0.13<br>( 0.10 )   |
| Southern Italy              | -0.20<br>( 0.34 )  | 0.19<br>( 0.18 )  | -0.94<br>( 0.37 )   | 0.55<br>( 0.40 )  |
| <b>Byzantine Heartlands</b> | <b>-1.56</b><br><b>( 0.33 )</b>                                      | <b>-0.23</b><br><b>( 0.14 )</b>                               | <b>-0.44</b><br><b>( 0.41 )</b>                           | <b>-0.89</b><br><b>( 0.54 )</b>   |
| al-Sham (Greater Syria)     | -0.32<br>( 0.27 )  | -0.04<br>( 0.02 )   | -0.11<br>( 0.29 )   | -0.17<br>( 0.11 )   |
| Northern Syria, Caucasus    | 0.22<br>( 0.30 )   | -0.01<br>( 0.03 )   | 0.15<br>( 0.37 )  | 0.08<br>( 0.12 )  |
| Iraq, Iran                  | 0.06<br>( 0.27 )   | -0.00<br>( 0.01 )   | 0.06<br>( 0.29 )  | -0.00<br>( 0.04 )   |
| Eastern Caliphate           | 0.37<br>( 0.33 )   | -0.00<br>( 0.00 )   | 0.39<br>( 0.34 )  | -0.02<br>( 0.04 )   |
| <b>Arabian Peninsula</b>    | <b>1.16</b><br><b>( 0.34 )</b>                                       | <b>-0.01</b><br><b>( 0.04 )</b>                               | <b>0.66</b><br><b>( 0.45 )</b>                            | <b>0.51</b><br><b>( 0.26 )</b>  |
| Misr (Egypt)                | -0.36<br>( 0.72 )  | 0.09<br>( 0.23 )  | -0.82<br>( 0.50 )   | 0.37<br>( 0.90 )  |
| al-Maghrib                  | 0.28<br>( 0.33 )   | 0.13<br>( 0.07 )  | -0.49<br>( 0.27 )   | 0.65<br>( 0.30 )  |

Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t$ . Bootstrapped s.e.'s in parentheses (100 bootstraps).

back

# Realized vs counterfactual changes in real consumption per capita

Counterfactual changes relative to AD 700-900

|                             | Initial $\log\left(\frac{X_n/p_n}{L_n}\right)$ |                 | Counterfactual $\Delta \log\left(\frac{X_n/p_n}{L_n}\right)$ if: |                 |              |                 |              |                 |
|-----------------------------|--|-----------------|--|-----------------|--------------|-----------------|--------------|-----------------|
|                             | All parameters                                 |                 | Religious border   |                 | Technology   |                 | Minting      |                 |
|                             | AD 460-620                                     | AD 700-900      | AD 700-900   | AD 700-900      | AD 700-900   | AD 700-900      | AD 700-900   | AD 700-900      |
| al-Andalus (Spain)          | -0.70  | ( 0.10 )        | 0.09   | ( 0.02 )        | 0.55         | ( 0.10 )        | 1.57         | ( 0.31 )        |
| Aquitaine (South France)    | -1.04  | ( 0.08 )        | -0.15  | ( 0.03 )        | 0.99         | ( 0.09 )        | 3.93         | ( 0.30 )        |
| <b>Francia and Germania</b> | <b>-1.55</b>                                   | <b>( 0.09 )</b> | <b>-0.07</b>   | <b>( 0.02 )</b> | <b>1.68</b>  | <b>( 0.11 )</b> | <b>6.17</b>  | <b>( 0.47 )</b> |
| Northern Italy              | 0.07   | ( 0.04 )        | -0.24  | ( 0.05 )        | -0.24        | ( 0.08 )        | -0.21        | ( 0.07 )        |
| Southern Italy              | -0.25  | ( 0.06 )        | -0.11  | ( 0.02 )        | -0.60        | ( 0.13 )        | -0.03        | ( 0.02 )        |
| <b>Byzantine Heartlands</b> | <b>1.22</b>                                    | <b>( 0.11 )</b> | <b>-0.69</b>   | <b>( 0.08 )</b> | <b>-0.57</b> | <b>( 0.13 )</b> | <b>-1.41</b> | <b>( 0.19 )</b> |
| al-Sham (Greater Syria)     | 0.30   | ( 0.04 )        | 0.04   | ( 0.01 )        | -0.18        | ( 0.10 )        | -0.22        | ( 0.08 )        |
| Northern Syria, Caucasus    | -0.34  | ( 0.11 )        | 0.02   | ( 0.02 )        | 0.15         | ( 0.22 )        | 0.19         | ( 0.19 )        |
| Iraq, Iran                  | 0.28   | ( 0.08 )        | 0.01   | ( 0.00 )        | 0.03         | ( 0.08 )        | 0.03         | ( 0.06 )        |
| Eastern Caliphate           | -0.44  | ( 0.08 )        | 0.01   | ( 0.00 )        | 0.38         | ( 0.16 )        | 0.34         | ( 0.26 )        |
| <b>Arabian Peninsula</b>    | <b>-1.80</b>                                   | <b>( 0.18 )</b> | <b>0.26</b>  | <b>( 0.09 )</b> | <b>0.66</b>  | <b>( 0.40 )</b> | <b>2.71</b>  | <b>( 0.84 )</b> |
| Misr (Egypt)                | 0.32   | ( 0.07 )        | 0.02   | ( 0.00 )        | -0.71        | ( 0.24 )        | -0.09        | ( 0.02 )        |
| al-Maghrib                  | 0.12   | ( 0.06 )        | 0.01   | ( 0.00 )        | -0.46        | ( 0.17 )        | -0.05        | ( 0.06 )        |

Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t$ . Bootstrapped s.e's in parentheses (100 bootstraps).

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# Realized vs counterfactual changes in real consumption per capita

Realized changes, from AD 460-620 to AD 700-900

|                      | Real consumption<br>$\Delta \log \left( \frac{X_n/p_n}{L_n} \right)$ | Openness<br>$\Delta \log \left( \pi_{nn}^{-1/\theta} \right)$ | Technology<br>$\Delta \log \left( T_n^{1/\theta} \right)$ | Trade Deficit<br>$\Delta \log \left( 1 + \frac{M_n - \lambda w_n L_n}{w_n L_n} \right)$ |
|----------------------|--|---|---|---|
| Francia and Germania | 1.96<br>( 0.24 )   | -0.05<br>( 0.01 )   | 1.80<br>( 0.26 )  | 0.20<br>( 0.04 )  |
| Byzantine Heartlands | -1.56<br>( 0.33 )  | -0.23<br>( 0.14 )   | -0.44<br>( 0.41 )   | -0.89<br>( 0.54 )   |
| Arabian Peninsula    | 1.16<br>( 0.34 )   | -0.01<br>( 0.04 )   | 0.66<br>( 0.45 )  | 0.51<br>( 0.26 )  |

Counterfactual changes relative to AD 700-900

|                      | Initial $\log \left( \frac{X_n/p_n}{L_n} \right)$ | Counterfactual $\Delta \log \left( \frac{X_n/p_n}{L_n} \right)$ if: |                   |                                |  |                          |                       |
|----------------------|---|---|-------------------|--------------------------------|--|--------------------------|-----------------------|
|                      |   | All parameters<br>AD 460-620  |                   | Religious border<br>AD 700-900 |  | Technology<br>AD 700-900 | Minting<br>AD 700-900 |
|                      |   |   |                   |                                |  |                          |                       |
| Francia and Germania | -1.55<br>( 0.09 )                                 | -0.07<br>( 0.02 )   | 1.68<br>( 0.11 )  | 6.17<br>( 0.47 )               |  |                          |                       |
| Byzantine Heartlands | 1.22<br>( 0.11 )                                  | -0.69<br>( 0.08 )   | -0.57<br>( 0.13 ) | -1.41<br>( 0.19 )              |  |                          |                       |
| Arabian Peninsula    | -1.80<br>( 0.18 )                                 | 0.26<br>( 0.09 )  | 0.66<br>( 0.40 )  | 2.71<br>( 0.84 )               |  |                          |                       |

Normalizations:  $E_t \left[ \frac{X_n[t]/p_n[t]}{L_n[t]} \right] \equiv 1, \forall t$ . Bootstrapped s.e.'s in parentheses (100 bootstraps).