

Security

2. Cryptography: the main ingredients

Objective

- > Gain understanding of three main ingredients of most security protocols & products
 - > **Symmetric Encryption**
 - > **Public Key Cryptography**
 - > **Cryptographic hash functions**

Introduction

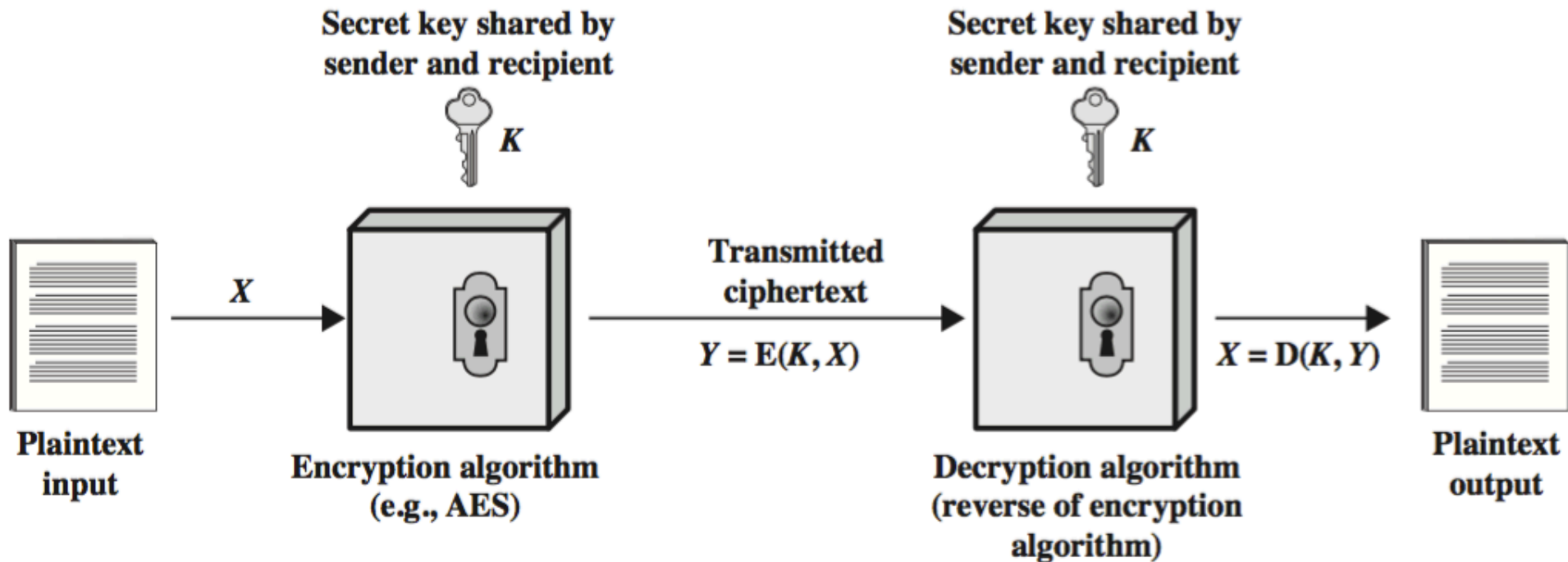
Some jargon

<i>Cryptography:</i>	Science of “secret writing”
<i>Plaintext:</i>	Original message
<i>Ciphertext:</i>	Transformed message
<i>Encryption:</i>	plaintext -> ciphertext process
<i>Decryption:</i>	ciphertext -> plaintext process
<i>Cipher:</i>	“Secret method of writing” (i.e. algorithm)
<i>Key:</i>	Some critical information used by the cipher, known only to sender and/or receiver
<i>Cryptanalysis:</i>	Attempting to discover plaintext or key or both

Symmetric Encryption

- Sender and receiver use same key (shared secret)
- Was the only method used prior to the 1970s & still the main “workhorse”
- Popular algorithms:
 - Advanced Encryption Standard (AES)
 - Triple Data Encryption Standard (3DES)
 - Rivest Cipher 4 (RC4) – *until recently!*
- Fast
- But how to share secret keys?
 - “chicken-and-egg” problem

Symmetric Encryption



Public Key Cryptography

- Major limitations of Symmetric Encryption:
 - Key distribution problem
 - Not suitable for authentication: receiver can forge message & claim it came from sender
- Addressed by Public Key Cryptography
- Public key methods based on sender and receiver using different keys

Public Key Cryptography

- Each party has two keys:
 - a **public key**, known potentially to anybody, used to **encrypt messages**, and **verify signatures**
 - a **private key**, known only to its owner, used to **decrypt messages**, and **create signatures**
- Complements rather than replaces symmetric cryptography
 - Used for exchanging secret keys

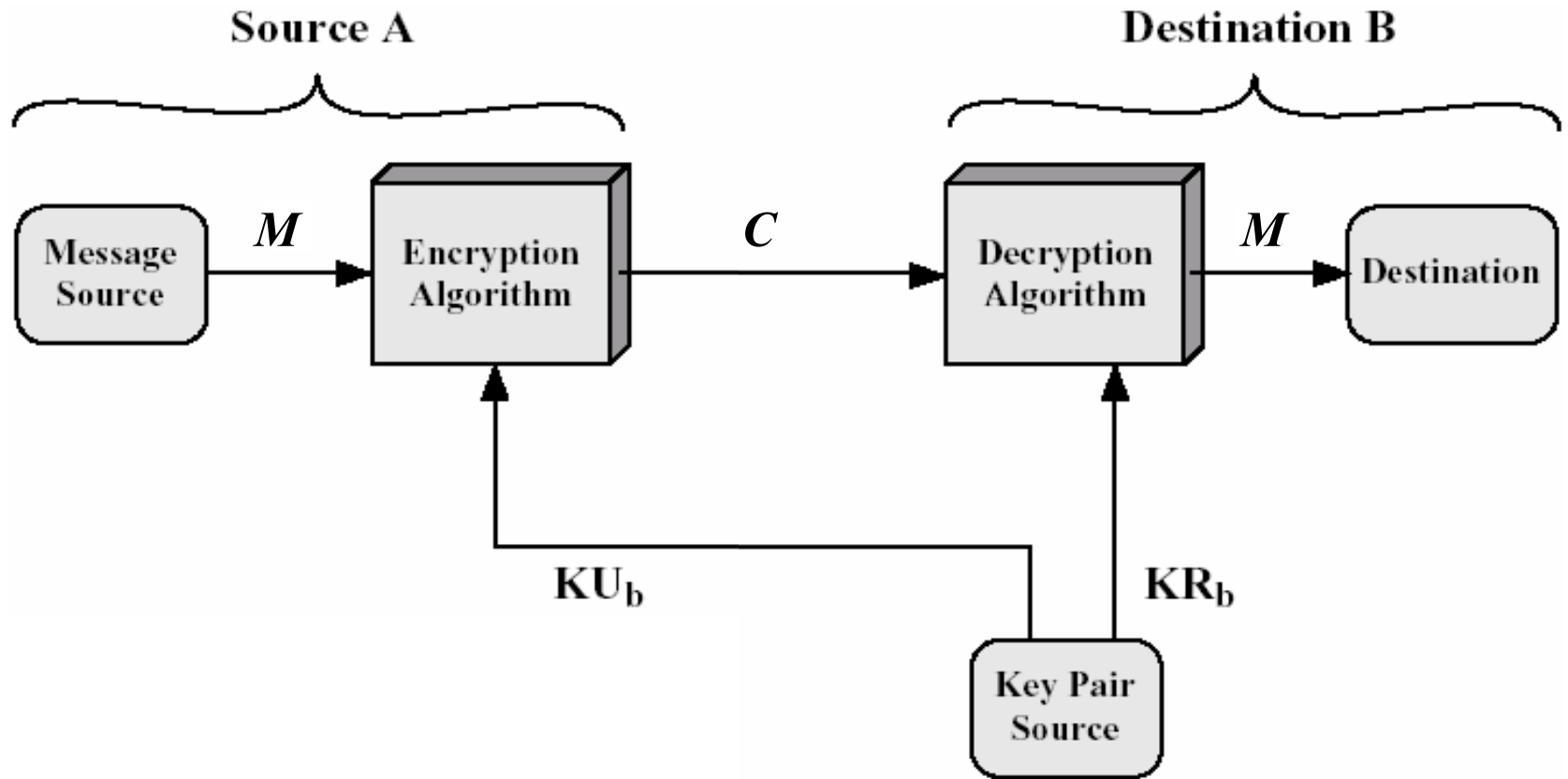
Applications of Public Key Cryptography

- Can classify uses of public key cryptography into 3 categories:
 - 1) **encryption/decryption** (provides secrecy)
 - 2) **digital signatures** (provides authentication)
 - 3) **key exchange** for symmetric encryption
 - which is a special case of (1)
- Some public key algorithms are suitable for all uses; others are specific to one of the above

Application: Secrecy

- Alice (A) sends message to Bob (B) by encrypting with his public key
- Message can only be decrypted with Bob's corresponding private key (known only to him)

Secrecy Model



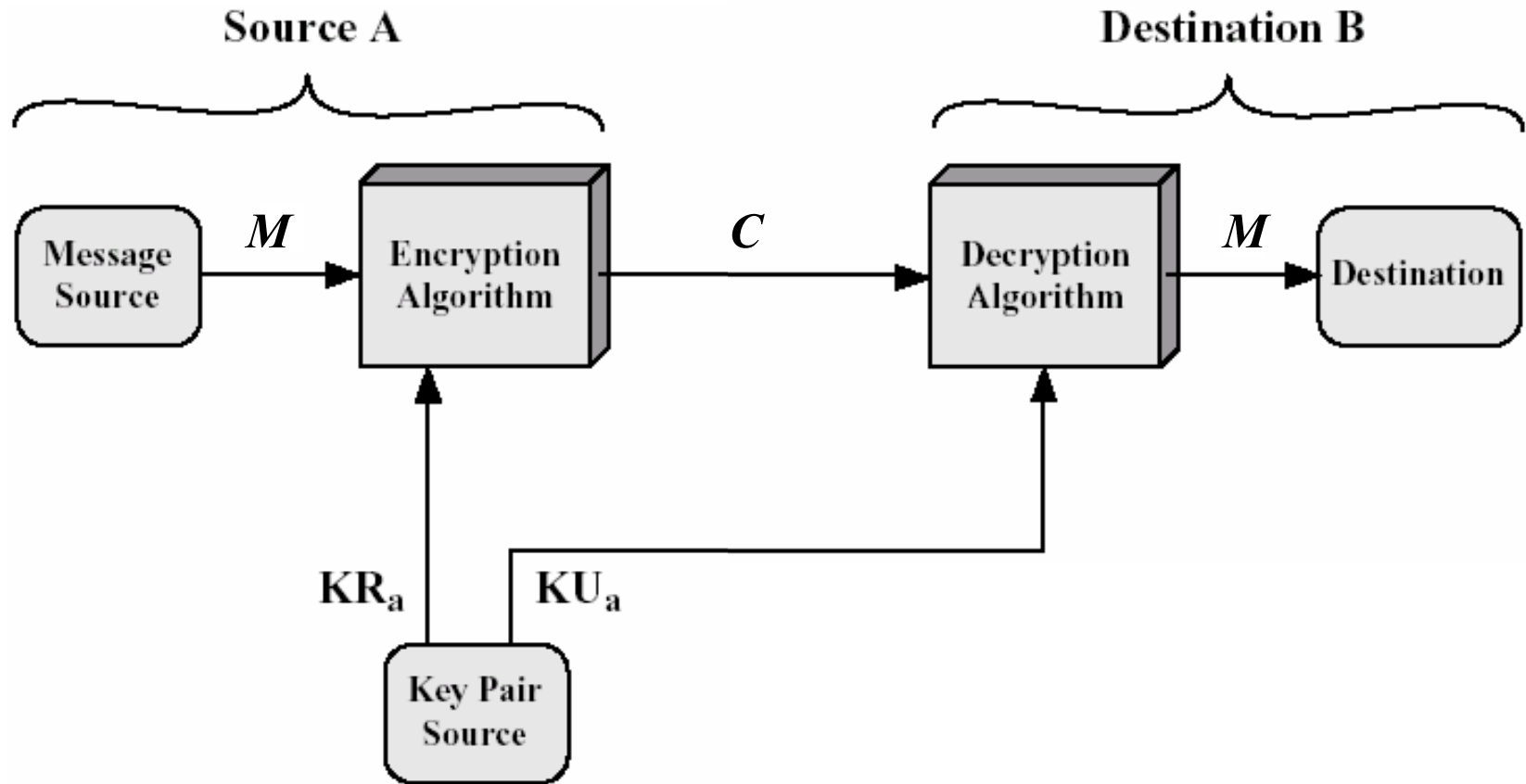
KU_b B's pUblc key

KR_b B's pRivate key

Application: Authentication

- Alice (A) sends message to Bob (B) encrypting it with her own private key (i.e. she signs the message)
- Everyone with Alice's public key can decrypt the message. A message that can be decrypted with Alice's public key ***must have come from Alice.***

Authentication Model



KR_a A's pRivate key

KU_a A's pUblIC key

Limitations of Public Key Cryptography

1. Processing speed

- Calculations required for public-key algorithms (mainly multiplications) much slower than those of conventional algorithms (permutations & XORs)
- Thus public-key methods not suitable for general-purpose encryption/decryption
- Instead often just use public-key method to exchange session (secret) key at beginning of session & use session key thereafter

Limitations of Public Key Cryptography

2. Authenticity of public keys (MITM attack)

- Bob's public key is in the public domain and only Bob has the corresponding private key
 - What happens though if an eavesdropper (Eve) generates another key pair and advertises the public key produced as belonging to Bob?
 - People then may send messages to Bob using the wrong public key, for which Eve has the corresponding private key.
- ⇒ *Need to be able to **trust** that a public key belongs to whom it is reputed to belong.*

Cryptographic strength & cryptanalysis

Kerckhoff's principle

- Security should depend on the secrecy of the key, not the secrecy of the algorithm
- Attempts to keep algorithms secret are usually ineffective (they leak out)
- ... and counterproductive as review by the wider crypto community allows weaknesses to be found early on, before deployment.

Cryptanalysis

- Cryptanalysis is the process of trying to find the plaintext or key
- Two main approaches
 - Brute Force
 - try all possible keys
 - Exploit weaknesses in the algorithm or key
 - e.g. key generated from password entered by user, where user can enter bad password

Cryptanalysis: Brute Force Attack

- Try all possible keys until code is broken
- On average, need to try half of all possible keys
- Infeasible if key length is sufficiently long

Key size (bits)	No. of keys	Time required at 1 encryption per μs	Time required at 10^6 encryptions per μs
32	4.3×10^9	36 minutes	2 milliseconds
56	7.2×10^{16}	1142 years	10 hours
128	3.4×10^{38}	5.4×10^{24} years	5.4×10^{18} years
168	3.7×10^{50}	5.9×10^{36} years	5.9×10^{30} years

Age of universe: $\sim 10^{10}$ years

Note: DES has a 56 bit key; AES key has 128+ bits

Symmetric Block Ciphers

XOR

- Modern techniques use bits rather than text letters
- Most transformations use eXclusive OR
- **Reversibility** and **speed** are the main benefits of using XOR

XOR truth table:

A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

XOR properties:

$$A \oplus A = 0$$

$$A \oplus 0 = A$$

$$(A \oplus B) \oplus B = A$$

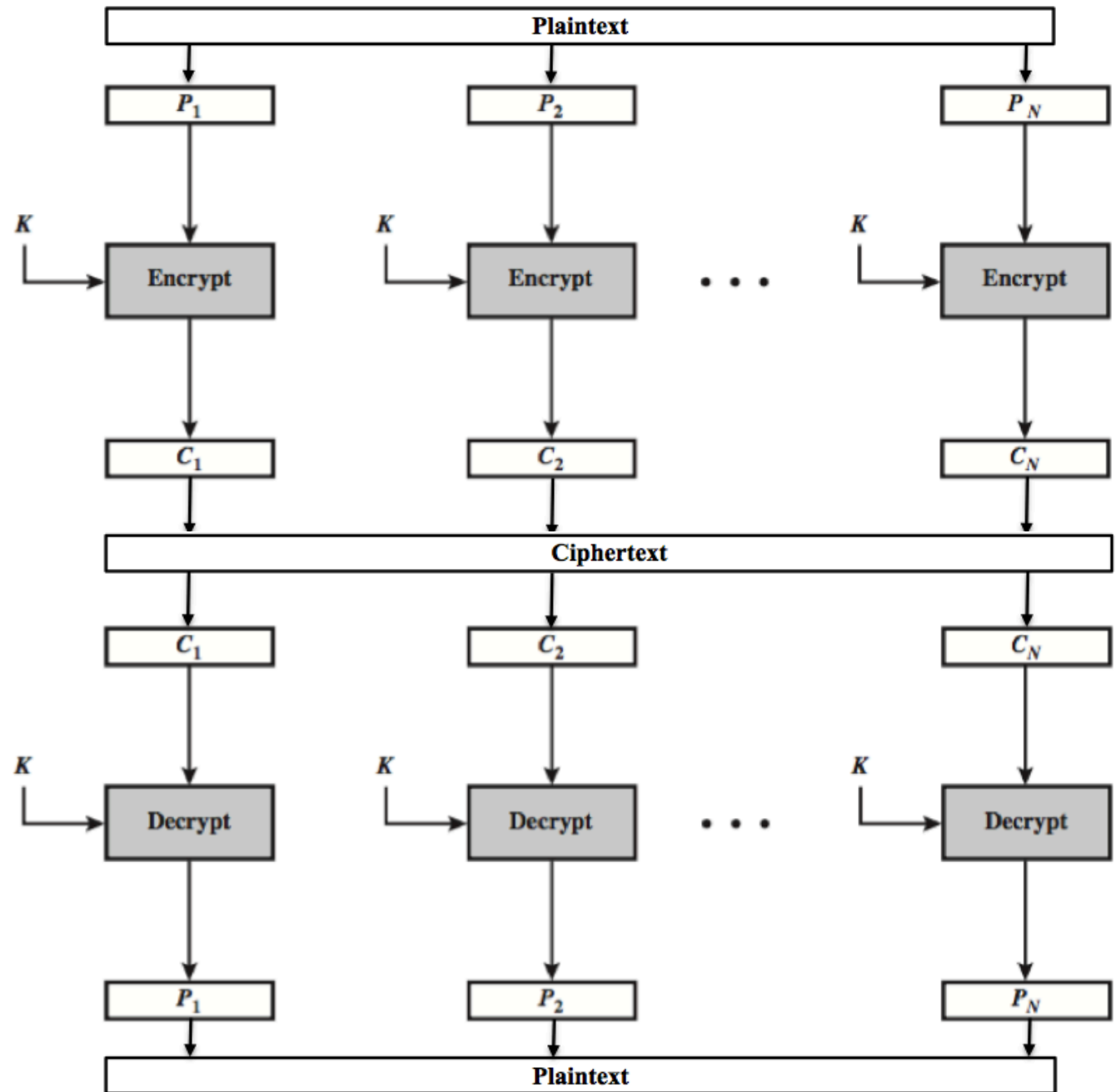
Block Cipher

- A block cipher divides the plaintext into fixed-sized blocks and transforms each block into a corresponding block of ciphertext
- Padding is required where the plaintext size is not an integer multiple of the block size
- Iterated block ciphers are based on a number of rounds where a round function is applied at each round.
- The round function usually takes a round key as one of its inputs.
 - Each round key based on bits extracted from the key

Block Cipher – modes of operation

- **Electronic Codebook (ECB) mode**
 - Each block treated independently.
 - Insecure, as repeated plaintext blocks map to repeated ciphertext blocks
- **Cipher Block Chaining (CBC) mode**
 - Each plaintext block XORed with previous ciphertext block before encryption
- **Counter (CTR) mode**
 - For each plaintext block encrypt a counter and XOR the result with the plaintext block. Increment the counter for the next block

Electronic
Codebook
Mode (ECB)
Encryption



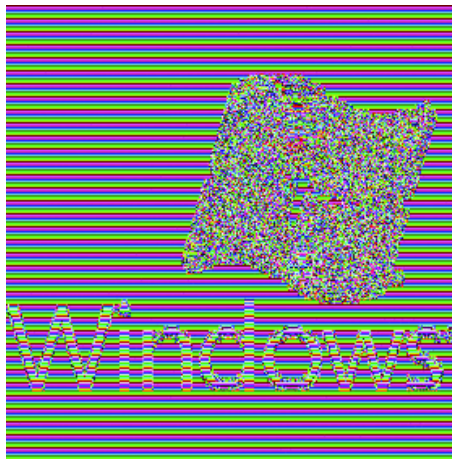
ECB
Decryption

Comparing CBC with ECB

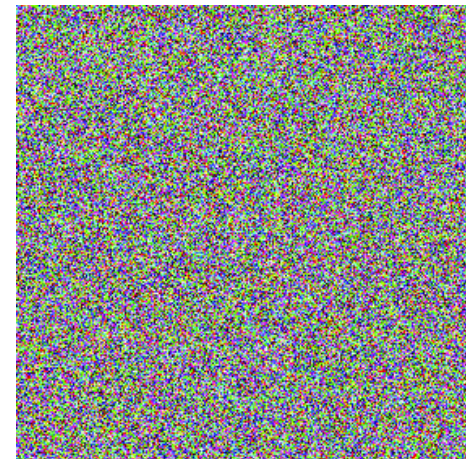
- Codebooks are a problem as patterns in the plaintext may remain in the ciphertext



Plaintext



Ciphertext (ECB)



Ciphertext (CBC)

Source: msdn.microsoft.com

DES

- Data Encryption Standard (1976)
- Block size: 64 bits
- Key size: 56 bits
- No. of rounds: 16
- Based on design by Horst Feistel, IBM
 - Chosen by NBS (now called NIST), US national standards body
 - Influenced by NSA
- Very influential algorithm
- Now obsolete, but lives on in Triple DES (3DES)

AES

- Advanced Encryption Standard (2001)
- Chosen by design competition
 - Organised by NIST (US National Standards Inst.)
 - Winner: Rijndael (Belgium)
- Block size: 128 bits
- Key sizes: 128, 192, 256
- Relatively small memory requirement
- Suitable for variety of hardware and software architectures
- Royalty-free
- Considered secure
- Very widely used

AES

- You can find a nice AES animation here:

http://www.securityfit.cz/download/kib/rijndael_ingles2004.swf

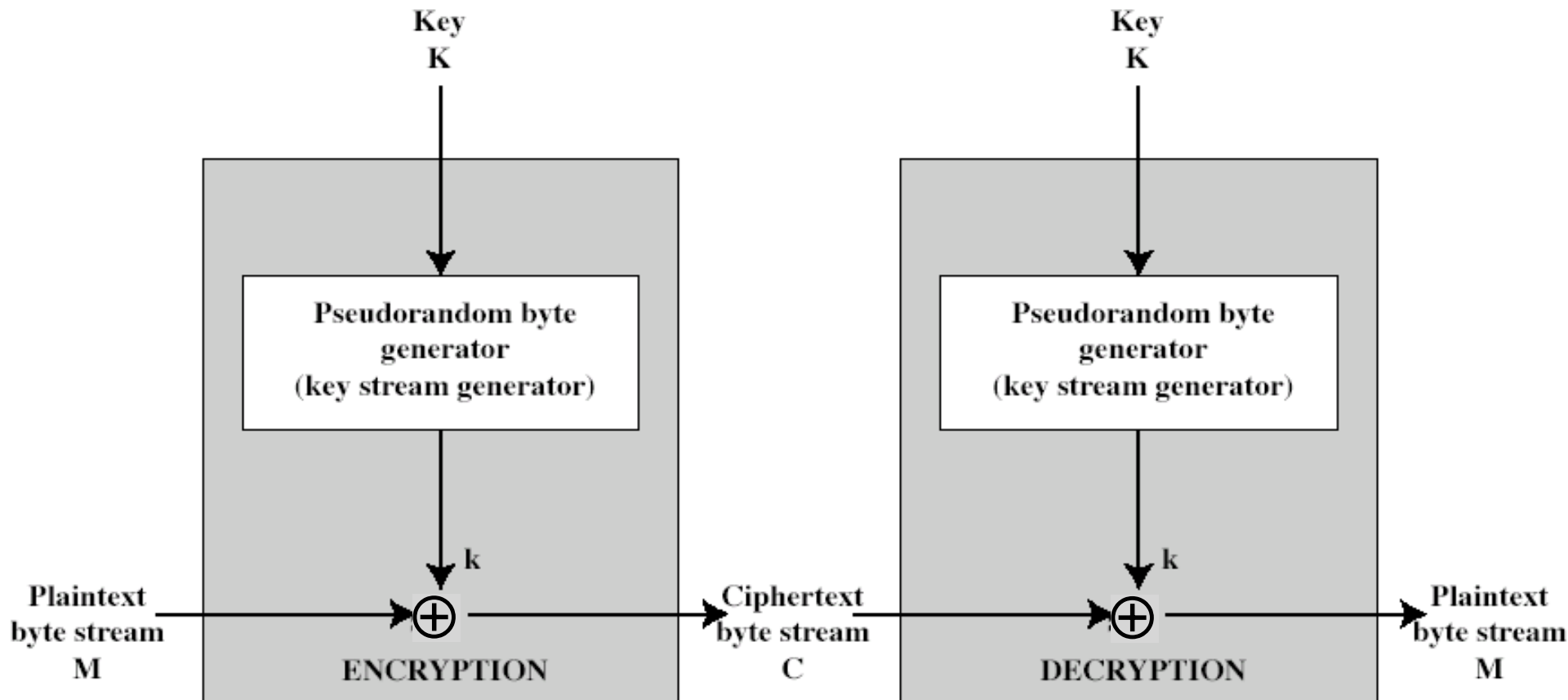
or **<http://tinyurl.com/aesflash>**

Stream Ciphers

Stream Ciphers

- Process message “continuously”
 - Optimised for real-time and two-way comms
 - Usually one byte at a time
 - As distinct from a block cipher
- Typically simple XOR of each plaintext bit with the output of a pseudo-random number generator (PRNG)

Stream Cipher Structure



$$C_i = M_i \oplus k_i$$

$$M_i = C_i \oplus k_i$$

Danger with Stream Cipher

- If plaintext-ciphertext pairs can be gathered, then it is easy to record the keystream:
 - as $M_i \oplus C_i = k_i$
- Thus the cipher is broken if any way to predict key stream for next ciphertext
- Key streams should never be re-used (or re-started with the same seed)

Public-key Algorithms

Trapdoor functions

- Public-key cryptography relies on functions that are computationally easy in one direction and computationally infeasible in the other
- Examples:

“Easy” problem	“Hard” problem	Technique
Multiplying prime numbers, $n = pq$	Factoring n	RSA
Modular exponentiation, $g^x \pmod n$	Calculating discrete log; solving for x in $a = g^x \pmod n$	Diffie-Hellmann
Elliptic curve point multiplication, $R = kP$	Finding elliptic curve multiplicand, k	Elliptic curve cryptography

RSA

- Rivest, Shamir & Adleman, MIT, 1977
- Very well known versatile public-key scheme
- Uses large integers as keys (>1000 bits)
- Security due to extreme difficulty of factoring large “semiprime” integers
 - i.e. factoring product of two prime numbers

RSA

- Based on three related integers: e, d, n
- RSA function (“encryption”):
 - Input: $M < n$
 - Output: $C = M^e \pmod{n}$
- Inverse RSA (“decryption”):
 - Input: C
 - Output: $M = C^d \pmod{n}$

d and e are mathematically related: e is chosen and d is calculated from e and the **factors** of n

Diffie-Hellman

- Public Key Technique for exchanging secret keys
 - First public key technique (1976)
- The secret key is calculated by both parties
- Requires some global public parameters
- Based on difficulty in solving for x :

$$a = g^x \pmod{n}$$

a, g, n known

Elliptic Curve Cryptography

- Majority of public-key crypto (RSA, D-H) use either integer or polynomial arithmetic with very large numbers/polynomials
- Imposes a significant load in storing and processing keys and messages
- An alternative is to use elliptic curves
- Offers same security as RSA with smaller bit sizes and lower processing and memory overhead
- Recent growth in use

Integrity and Authentication

Data Integrity

- Integrity refers to assurance of non-alteration
- Many systems and components have checksums or cyclic redundancy checks that are designed to detect *accidental* errors, etc.
 - For example, a credit card number contains a digit that is used to verify the others
- But such schemes are not sufficient to prevent *deliberate* modifications

Cryptographic Hash Functions

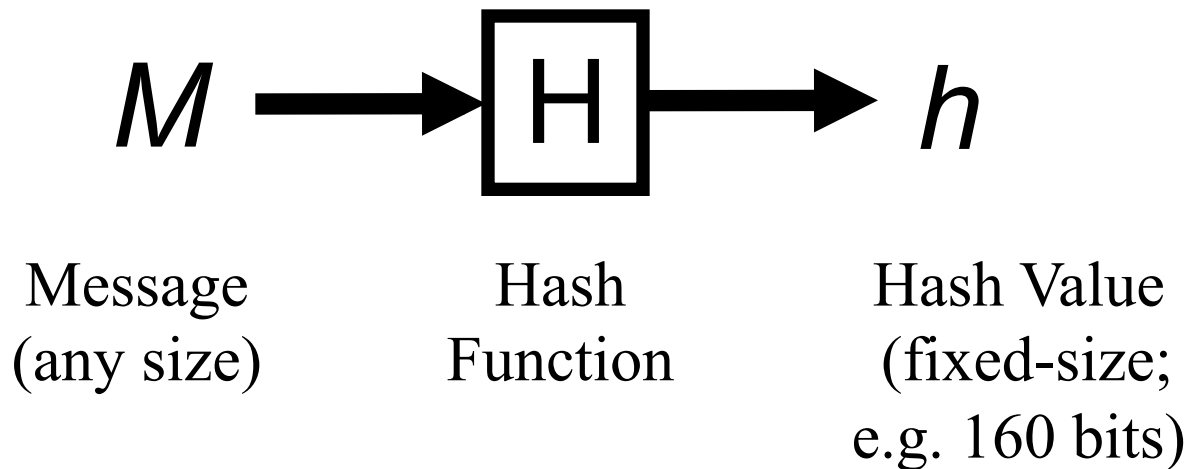
- Used to provide integrity of a message
- Purpose is to produce a fixed-size *hash-value*:

$$h = H(M)$$

where h is the hash value
 H is the hash function
 M is the message

- Any change in M , however small, should produce a different h -value

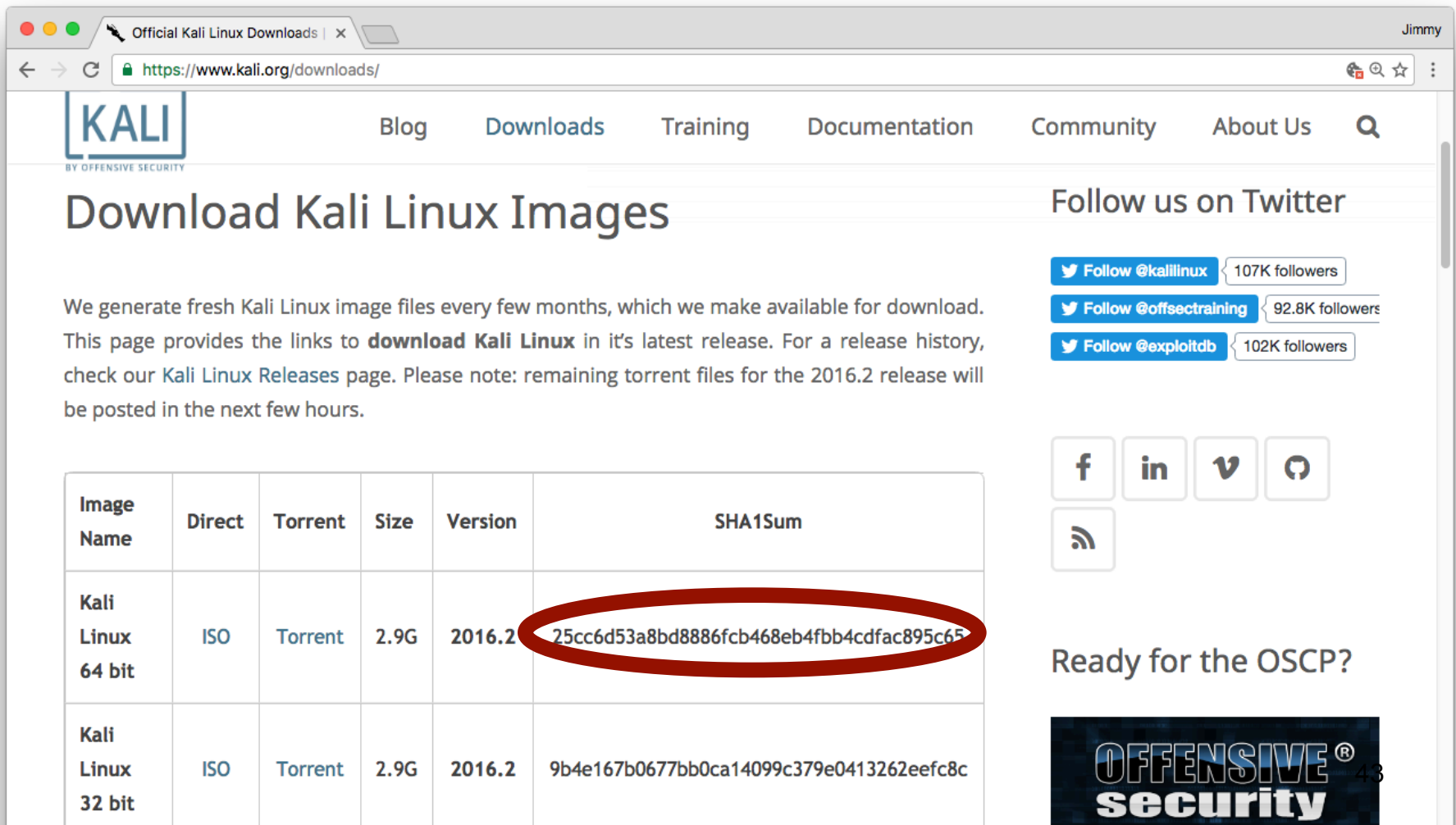
Cryptographic Hash Functions



- Note that a hash function is a many-to-one function. Potentially many messages can have the same hash, but finding these should be very difficult

Applications of Hash Functions

- As cryptographic checksum
 - e.g. to verify software downloads



The screenshot shows the 'Official Kali Linux Downloads' page. The main heading is 'Download Kali Linux Images'. Below it, a paragraph explains that fresh image files are generated every few months and provides links to download the latest release. A table lists two download options: 'Kali Linux 64 bit' and 'Kali Linux 32 bit'. The first row of the table is highlighted with a red oval, specifically focusing on the SHA1Sum column which contains the hash '25cc6d53a8bd8886fcb468eb4fbb4cdfac895c65'.

Image Name	Direct	Torrent	Size	Version	SHA1Sum
Kali Linux 64 bit	ISO	Torrent	2.9G	2016.2	25cc6d53a8bd8886fcb468eb4fbb4cdfac895c65
Kali Linux 32 bit	ISO	Torrent	2.9G	2016.2	9b4e167b0677bb0ca14099c379e0413262eefc8c

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- Follow @exploitdb 102K followers

Ready for the OSCP?

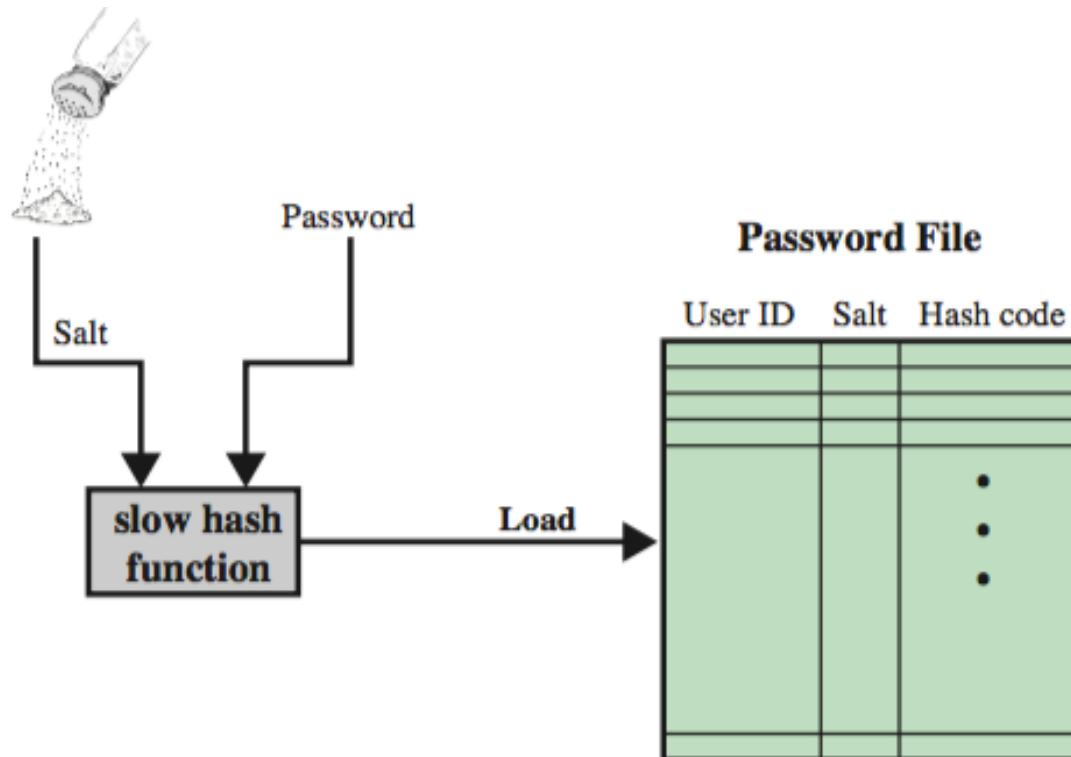
OFFENSIVE security

Applications of Hash Functions

- Authentication
 - It usually makes more sense to sign the hash of a message (with a private key) than to sign the original message
 - This is done with digital certificates and many other authentication schemes

Applications of Hash Functions

- Password storage
 - Store only the hash of password (+ *salt*)
 - e.g. Unix password scheme



Cryptanalysis: Breaking hash functions

- Strength depends on the length, n , in bits of the hash value
- Brute force attacks require time proportional to:
 - one-way property: 2^n
 - weak collisions property: 2^n
 - strong collisions property: $2^{n/2}$
 - This means the ability to find **any** two messages that hash to the same value:

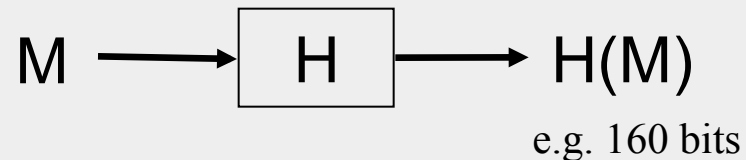
Main Hash Algorithms

- MD5
 - Produces 128-bit hash value (i.e. 64-bit security)
 - Collisions found (2004)
 - No longer recommended for use
- SHA-1
 - Produces 160-bit hash value (80-bit security)
 - Collisions found (2017)
 - No longer recommended for use
- SHA-2
 - Set of 4 hash functions with different size outputs
 - SHA-224, SHA-256, SHA-384, SHA-512
 - Considered safe to use
 - (though new SHA-3 has been established due to concerns over structural similarities with SHA-1)

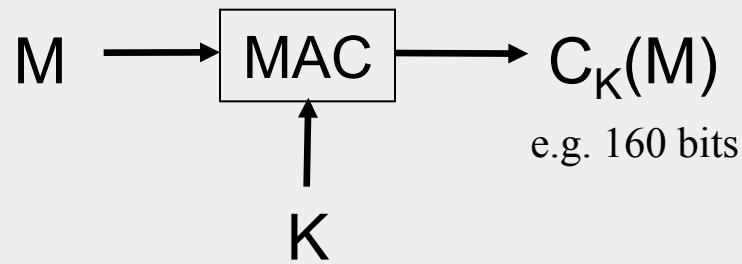
Message Authentication Code (MAC)

- Very similar to Hash Function
- Difference is the use of a key

Hash Function:



MAC:

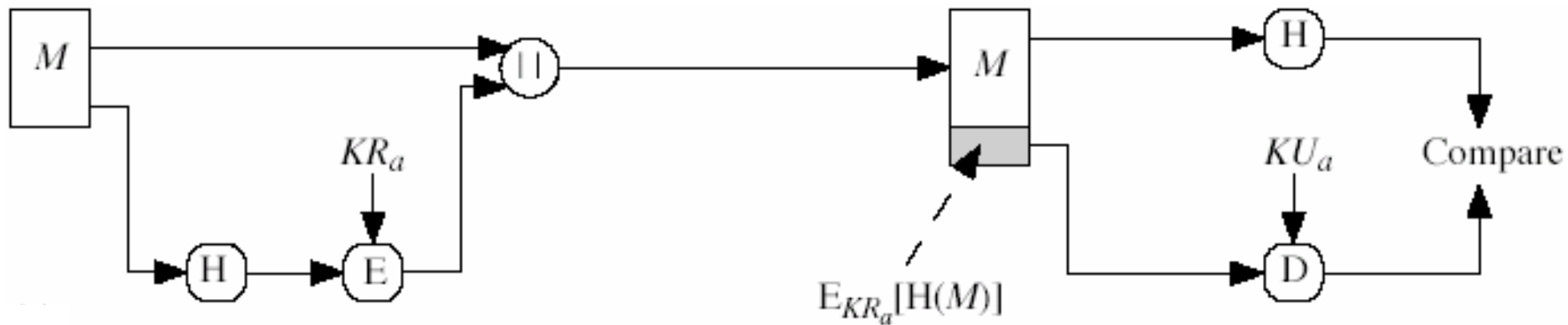


Digital Signatures: signing the hash

- Digital signature created by adding a small authentication block to a message
- Often done by taking the hash of the message and **encrypt the hash** with the **sender's private key**
- The result is a very compact signature (relative to message size)
- And is just as secure as encrypting the entire message with the sender's private key
 - assuming that a secure hash function is used

Typical Use of Hash Function with Digital Signature

- Just sign the hash
 - much more efficient than signing full message



KR_a : Sender's Private Key
 KU_a : Sender's Public Key

Note: The $||$ symbol means *concatenate*;
i.e. join inputs together