

For a language  $A$ , the  $PALINDROME(A)$  operator applied to  $A$  is

$$\{w \mid w \in A \text{ and } w^R \in A\}$$

Show that the class of regular languages is closed under the  $PALINDROME$  operation.