## Recitation 3 - Homework 1

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Questions and examples related to homework 1.

Example Conversions: Regular Expression to/from NFAs and NFAs to DFAs.

## Questions?

$\delta_{ extbf{1}}$	0	1	$\epsilon$
1	$\phi$	{2}	$\phi$
2	{3}	{2}	$\phi$
3	$\phi$	{3}	$\phi$

$$\Downarrow \Downarrow \Downarrow$$

$\delta$	0	1	$\epsilon$
1	$\phi$	{2}	$\phi$
2	<sup>φ</sup> {3}	{2}	$\phi$
3	$\phi$	{3}	$\phi \cup \{1\} = \{1\}$

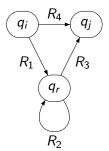
- This construction works for this example.
- ▶ Problem 1.15 ask for an example where this doesn't work.

- ▶ If language A is regular, prove  $A^R$  is regular.
- ▶ Given DFA M which recognizes A, construct DFA or NFA M<sub>1</sub> which recognizes A<sup>R</sup>.
- Remember to prove both ways:
  - ▶ Given  $w \in A$ , show  $M_1$  accepts  $w^R$ , and given  $w \notin A$ , show  $w^R$  not accepted by  $M_1$ .
  - ▶ -or- Given  $w \in A$ , show  $M_1$  accepts  $w^R$ , and given w accepted by  $M_1$  show  $w^R \in A$ .

 $\begin{array}{ll} \text{Regular Expression} & \rightarrow \text{NFA} \\ \text{NFA} & \rightarrow \text{Regular Expression} \\ \text{NFA} & \rightarrow \text{DFA} \end{array}$ 

 $1 \cup (01^*0)$ 

$$1 \cup (01^*0) = (1) \cup (0(((1)^*)0))$$



Remove  $R_1$  and  $R_3$  and replace  $R_4$  with  $R_1R_2^*R_3 \cup R_4$ .

