

Definition 1.52 specifies that  $R$  is a regular expression if  $R$  is

1.  $a$  for some  $a$  in the alphabet  $\Sigma$
2.  $\epsilon$
3.  $\{\}$
4.  $(R_1 \cup R_2)$  where  $R_1$  and  $R_2$  are regular expressions
5.  $(R_1 \circ R_2)$  where  $R_1$  and  $R_2$  are regular expressions
6.  $R_1^*$  where  $R_1$  is a regular expression

Consider *regular+ expressions* which extend the above definition with two additional cases

1.  $R_1?$  where  $R_1$  is a regular expression
2.  $R_1^k$  where  $R_1$  is a regular expression and  $k$  is an integer

Where  $?$  means 0 or 1 instance of the previous regular expression. Show that regular+ expressions describe the class of regular languages.