Recitation 3

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 $\{w \mid w \text{ is not a palindrome}\}$

$$\{wtw \mid w, t \in \{0,1\}^+\}$$

What are some strings people tried to derive contradictions with?

A Quick Note About Homeworks

- ► These problems are hard. On proof problems prepare yourself for spending a lot of time
- ▶ Be sure to understand the problem thoroughly first
 - What are some examples?
 - ▶ What are some related problems that are easier?
 - ► How is this the same and how is this different then the problems you have seen so far?
- ▶ When you see examples in the book, in lecture, in recitation, etc. think about the why not just the mechanics
- Unclear about a question, ask about it on the forum
- ▶ Not sure if your answer is right, e-mail John
- ► Form study groups, share ideas and approaches, NOT answers
- Start early

$$\Sigma = \{a, b, c, d\}$$

$$A = \{a^k b^l c^m d^n \mid k + l = m + n\}$$

What are some strings in this language, what are the intresting cases?

What are some easier languages that are related? Give CFGs for these languages.

Give a CFG for B.

$$\Sigma = \{a, b, c, d\}$$

$$B = \{a^k b^l c^m d^n \mid k = l + m = n\}$$

What are some strings in this language, what are the intresting cases?

Prove B is not context-free.

Pumping Lemma for context-free langauges

- \triangleright s = uvxyz
- ▶ $|vxy| \le p$
- ▶ |vy| > 0
- $ightharpoonup uv^i xy^i z \in L$

$$\Sigma = \{0,1,2\}$$

 $C = \{w \mid w \text{ contains and equal number of 0s, 1s, and 2s}\}$

Prove *C* is not context-free.

Pumping Lemma for context-free langauges

- ightharpoonup s = uvxyz
- ▶ $|vxy| \le p$
- ▶ |vy| > 0
- $ightharpoonup uv^i xy^i z \in L$

$$\Sigma=\{0,1,\#\}$$

$$D = \{ w \# t \mid w \text{ is a substring of t } \}$$

What are some strings in this language, what are the intresting cases?

Prove *D* is not context-free.

Pumping Lemma for context-free langauges

- ightharpoonup s = uvxyz
- ▶ $|vxy| \le p$
- ▶ |vy| > 0
- $\vdash uv^ixy^iz \in L$